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THE COLLECTED MATHEMATICAL WORKS

OF

GEORGE WILLIAM HILL

VOLUME THREE

*Αστρων κάτοιδα νυκτέρων δμήγυριν.—Æschylus.

THE COLLECTED

MATHEMATICAL WORKS

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GEORGE WILLIAM HILL

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A NEW THEORY OF JUPITER AND SATURN

(ASTRONOMICAL PAPERS OF THE AMERICAN EPHEMERIS, Vol. IV.)

INTRODUCTION.	Page.
History of previous attempts at the solution of this problem	11
CHAPTER I. MUTUAL ACTION OF JUPITER AND SATURN. DEVELOPMENT OF THE RECIPROCAL OF THE DISTANCE BETWEEN THE PLANETS AND ITS ODD POWERS IN PERIODIC SERIES WHEN ELLIPTIC VALUES ARE SUBSTITUTED FOR THE CO-ORDINATES.	
Elements of Jupiter and Saturn adopted	. 19
Correction of the semi-axes for the constant terms of the radii vectores	. 20
Relative position of the planes of the orbits	
Degree of accuracy required in the developments	
Value of certain constants employed in the developments	
Values of certain quantities for sixteen points of the circumference with respect to the mean anomaly of Saturn. Separation of the distance into factors	
Values of the Laplace coefficients $b_{\mathfrak{g}}^{(i)}$ for the sixteen points of the circumference	
Formulæ and values belonging to the development of the second factor of the distance	
Values of certain coefficients for the first power of the reciprocal of the distance	
The similar coefficients for the third power	
The similar coefficients for the fifth power	
The similar coefficients for the seventh power	
Application of mechanical quadratures to these coefficients	
Derivation of coefficients beyond the limits by induction	
Expressions of the odd powers of the reciprocal of the distance in terms of the mean anomaly of Saturn and the eccentric of Jupiter	
Values of the Besselian functions corresponding to multiples of the eccentricities of Jupiter and Saturn	•
Expressions of the odd powers of the reciprocal of the distance in terms of the mean anomalies of both planets.	
CHAPTER II. PERTURBATIONS OF JUPITER AND SATURN ARISING FROM THEIR MUTUAL ACTION AND OF THE FIRST ORDER WITH RESPECT TO DISTURBING FORCES.	
Values of four factors required in obtaining the forces	59
Products of the cube of the reciprocal of the distance by these factors	
Developments of the reactions of Jupiter and Saturn on the Sun	
Expressions for the three functions denoting the action of Saturn on Jupiter	
The same relative to the action of Jupiter on Saturn	69
Expressions for the multipliers A, B, and C for Jupiter and A', B', and C' for Saturn	
Values of the constants η and θ	
Developments of the similar functions for Saturn	
Values of the integrating factors for Jupiter	92
Values of the similar factors for Saturn	
Illustration of the method of forming \overline{W} and $\overline{W'}$	
Values assumed for the arbitrary constants	
Expressions for the differentials of δz and ν	
Expressions for the differentials of $\delta z'$ and v'	
Formulæ for the secular portions of the six co-ordinates of Jupiter and Saturn	101
Expressions for the perturbations of the co-ordinates of Jupiter	103
Expressions for the perturbations of the co-ordinates of Saturn	106

CHAPTER III. PERTURBATIONS OF SATURN BY URANUS OF THE FIRST ORDER WITH RESPECT TO THE DISTURBING FORCE.	
Adopted elements of Uranus Values of certain constants employed in the developments. Values of certain quantities for twelve points of the circumference with respect to the mean anomaly of Uranus. Values of the Laplace coefficients b ₄ (4) Values of the A for the first power of the reciprocal of the distance The similar coefficients for the third power The similar coefficients for the fifth power. Application of mechanical quadratures to these coefficients Expressions of the odd powers of the reciprocal of the distance in terms of the mean anomaly of Uranus and the eccentric of Saturn The same in terms of the mean anomalies of both planets Values of Besselian functions corresponding to the eccentricity of Uranus Products of the cube of the reciprocal of the distance by three factors Expressions for the treaction of Uranus on the Sun Expressions for the three functions denoting the action of Uranus on Saturn Expression for the differential of R Values of the integrating factors Expression for the differentials of dz and v Expressions for the perturbations of the co-ordinates of Saturn	109 1109 110 1114 116 117 118 119 122 124 125 127 128 130 134 135 136 138
CHAPTER IV. PERTURBATIONS OF JUPITER BY URANUS OF THE FIRST ORDER WITH RESPECT TO DISTURBING FORCES.	
Values of certain constants employed in the developments Values of certain quantities for twelve points of the circumference in reference to the mean anomaly of Uranus Values of the a Values of the A Expressions for the odd powers of the reciprocal of the distance in terms of the mean anomaly of Uranus and eccentric of Jupiter The same in terms of the mean anomalies of both planets Values of Besselian functions corresponding to the eccentricity of Uranus Products of the cube of the reciprocal of the distance by four factors Expression for the reaction of Uranus on the Sun Expressions for the three functions denoting the action of Uranus on Jupiter Expression for T and the differential of R Values of the integrating factors Expressions for the differentials of \$\delta z\$ and \$\nu\$ Expressions for the perturbations of the co-ordinates of Jupiter	140 141 142 144 147 148 150 151 153 154 156 158
CHAPTER V. PERTURBATIONS OF SATURN BY NEPTUNE. Elements of Neptune and resulting constants Values of certain quantities for twelve points of the circumference with reference to the mean anomaly of Neptune. Values of the a Values of the A for two powers of the reciprocal of the distance Expressions of the odd powers of the distance in terms of the mean anomaly of Neptune and the eccentric of Saturn. The same in terms of the mean anomalies of both planets Products of the cube of the reciprocal of the distance by two factors Expressions for the reaction of Neptune on the Sun Expressions for the three functions which denote the action of Neptune on Saturn Expressions for T and the differential of R Values of the integrating factors Expressions for the differentials of \$\delta z\$ and \$\nu\$ Expressions for the perturbations of the co-ordinates of Saturn	161 162 163 164 164 171 172 173 173
CHAPTER VI. PERTURBATIONS OF JUPITER BY NEPTUNE.	•
Values of constants employed in the developments	18 18 18

CHAPTER VI. PERTURBATIONS OF JUPITER BY NEPTUNE-Continued.	
Values of Besselian functions corresponding to the eccentricity of Neptune Products of the cube of the reciprocal of the distance by two factors Expression of the reaction of Neptune on the Sun Expressions of the three functions denoting the action of Neptune on Jupiter Expressions for T and the differential of R Values of the integrating factors Expressions for the differentials of \$\partial x\$ and \$\nu\$ Expressions for the differentials of \$\partial x\$ and \$\nu\$	182 186 187 189 190 190
CHAPTER VII. PERTURBATIONS OF JUPITER AND SATURN BY THE FOUR INTERIOR PLANETS.	
Action of Mercury on Jupiter Action of Venus on Jupiter Action of the Earth on Jupiter Action of Mars on Jupiter Action of Mercury on Saturn Action of Venus on Saturn Action of Venus on Saturn Action of the Earth on Saturn	192 193 193 195 196 196 196
CHAPTER VIII. PERTURBATIONS OF THE SECOND ORDER WITH RESPECT TO DISTURBING FORCES IN THE LONGITUDES AND RADII VECTORES ARISING FROM THE MUTUAL ACTION OF JUPITER AND SATURN. DERIVATION OF THE FACTORS OF ST AND ST.	
Formulæ for the eight factors Products of the fifth power of the reciprocal of the distance by four factors Expressions for the reactionary terms Expressions for four derivatives of the perturbative function for Jupiter The similar quantities for Saturn The two multipliers M and N, and their values for Jupiter and Saturn Expressions for the factors V, X, B, and G Expression for T Expressions for the factors C, D, E, and H Expressions for the factors V', X', B', and G' Expression for T Expression for T Expressions for the factors C', D', E', and H' Expressions for the factors C', D', E', and H' Expressions for two of the secondary factors of ott	999 999 904 908 908 911 912 921 921 921 921 921 921 921 921
Chapter IX. CALCULATION OF THE TERMS OF δ T AND δ T' WHOSE ARGUMENTS ARE γ AND γ' .	
Constituent parts of the coefficients of the terms here discussed	49 51 52 53
CHAPTER X. CALCULATION OF THE PORTION OF ST NOT FACTORED BY nt.	
	55 55
CHAPTER XI. CALCULATION OF THE PORTION OF ST FACTORED BY nt.	
	62 62
CHAPTER XII. SECOND-ORDER PERTURBATIONS OF THE MEAN ANOMALY AND RADIUS-VECTOR OF JUPITER ARISING FROM THE MUTUAL ACTION OF THIS PLANET AND SATURN.	
Special treatment of long-period terms in integration	69 74 76 81

CHAPTER XII. SECOND-ORDER PERTURBATIONS, ETCContinued.
Expression for the supplementary quantity of the differential of $\delta \nu$
CHAPTER XIII. CALCULATION OF THE PORTION OF &T' NOT FACTORED BY n't.
Limits for neglecting terms
CHAPTER XIV. CALCULATION OF THE PORTION OF ST' FACTORED BY n't.
Degree of precision employed
CHAPTER XV. SECOND-ORDER PERTURBATIONS OF THE MEAN ANOMALY AND RADIUS-VECTOR OF SATURN, ARISING FROM THE MUTUAL ACTION OF THIS PLANET AND JUPITER.
Sum of the eight portions of $\delta T'$
CHAPTER XVI. PERTURBATIONS OF THE THIRD ORDER WITH RESPECT TO DISTURBING FORCES IN THE LONGITUDES AND RADII VECTORES ARISING FROM THE MUTUAL ACTION OF JUPITER AND SATURN. DETERMINATION OF THE FACTORS OF &T AND &T/.
The terms retained of $\delta^2 T$ and $\delta^2 T'$. Formulæ for their factors. 344 Fromulæ for their factors. 345 Products of the fifth and seventh powers of the reciprocal of the distance by certain factors. Expressions for the third derivatives of the perturbative functions with reference to the radii vectores. Expressions for Y and Y'. Developments of three factors of the terms of $\delta^2 T$. The similar factors of $\delta^2 T'$. Portions of the secondary factors of $\delta^3 T$ and $\delta^3 T'$ independent of the multipliers nt and $n't$. Derivation of the terms of $\delta^3 T$ and $\delta^3 T'$ having the arguments γ and γ' . Portions of the secondary factors of $\delta^3 T$ and $\delta^3 T'$ multiplied by nt or $n't$. Portions of the secondary factors of $\delta^3 T$ and $\delta^3 T'$ multiplied by nt or $n't$.
CHAPTER XVII. CALCULATION OF THE SEVERAL PORTIONS OF 62T.
Expressions for the fourteen parts independent of nt
CHAPTER XVIII. THIRD-ORDER PERTURBATIONS OF THE MEAN ANOMALY AND RADIUS-VECTOR OF JUPITER ARISING FROM THE MUTUAL ACTION OF THIS PLANET AND SATURN.
Sum of the fourteen portions of $\delta^2 T$. Special treatment in integration of the long-period terms The expression for $\delta^3 W_0$. Expression for the y derivative of the preceding. Supplementary quantities completing the value of the differential of $n\delta^3 z$ Expression for the differential of $\delta^3 z$. Modification of the great inequality by third-order terms Expression for $n\delta^3 z$. Expression for $\delta^3 v$.
CHAPTER XIX. CALCULATION OF THE SEVERAL PORTIONS OF 6°T'.
Expressions for the fourteen parts independent of $n't$

OF SATURN ARISING FROM THE MUTUAL ACTION OF THIS PLANET AND JUPITER.
Sum of the fourteen portions of $\delta^g T'$
Expression for the γ' derivative of the preceding
Expression for the differential of δ^3z'
Expression for $n'\delta^3z'$
Expression for $\delta^2 \nu'$
CHAPTER XXI. PERTURBATIONS OF SATURN OF THE SECOND ORDER FROM THE ACTION OF URANUS AND FACTORED BY n't.
The terms of δT'
Formulæ for their primary factors
Expression for V'
Expressions for the derivatives of T' with respect to the radii
Expression for C'
Expressions for $\overline{\delta W_0}'$ and its γ' derivative
Expressions for the differentials of $\delta^{3}z'$ and $\delta v'$
Long-period term in $n'\delta^2z'$ not multiplied by $n't$
CHAPTER XXII. PERTURBATIONS OF JUPITER PROPORTIONAL TO THE PRODUCT OF THE MASSES OF SATURN AND URANUS.
The several terms of δT
Derivation of certain of their primary factors 4 Combinations in the products which give sensible results 4 Mode of taking account of third-order terms 4 Expression for δT 4 Expressions for $n\delta z$ and v 4
Combinations in the products which give sensible results
Combinations in the products which give sensible results
Combinations in the products which give sensible results Mode of taking account of third-order terms Expression for δT Expressions for $n\delta z$ and v CHAPTER XXIII. PERTURBATIONS OF SATURN PROPORTIONAL TO THE PRODUCT OF THE MASSES OF JUPITER AND URANUS. The several terms of $\delta T'$ Expressions for certain of their factors Quantities required in considering certain third-order terms Separate terms of, and complete value of $\delta T'$ Expressions for $\delta W_{0'}$ and its γ' derivative Supplementary quantities completing the value of the differential of $\delta^2 z'$ Expressions for $n' \delta^2 z'$ and $\delta v'$
Combinations in the products which give sensible results Mode of taking account of third-order terms Expression for δT Expressions for nδz and ν CHAPTER XXIII. PERTURBATIONS OF SATURN PROPORTIONAL TO THE PRODUCT OF THE MASSES OF JUPITER AND URANUS. The several terms of δT' Expressions for certain of their factors Quantities required in considering certain third-order terms Separate terms of, and complete value of δT' Expressions for δW₀' and its γ' derivative Supplementary quantities completing the value of the differential of δ²z' Additional long-period terms in n'δ²z' of minor importance CHAPTER XXIV. PERTURBATIONS OF THE LATITUDE OF JUPITER OF THE SECOND ORDER

CHAPTER XXV. PERTURBATIONS OF THE LATITUDE OF SATURN OF THE SECOND ORDER WITH RESPECT TO DISTURBING FORCES.
Terms of $\delta U'$ and formulæ for their primary factors
CHAPTER XXVI. FORMULÆ FOR THE MOTION OF THE PLANE OF THE ECLIPTIC AND FOR PRECESSION.
Values of certain planetary elements for 1600, 1850, and 2100
CHAPTER XXVII. REFERENCE OF THE LONGITUDES AND LATITUDES OF JUPITER AND SATURN TO THE MEAN EQUINOX AND ECLIPTIC OF DATE.
Reduction to the primitive plane of the orbit
Application of the formulæ to Jupiter
Reduction of the longitude to the ecliptic and mean equinox of date Expression for the correction to be applied to the fundamental argument. The corresponding corrections of the logarithm of the radius-vector and of the sine of the latitude. Application of the formulæ to Saturn. Parts of the sine of Saturn's latitude resulting severally from the motion of the plane of its orbit and from that of
the ecliptic
CHAPTER XXVIII. PRELIMINARY COMPARISON OF THE PRECEDING THEORY WITH OBSERVATION, AND DERIVATION OF APPROXIMATE CORRECTIONS FOR THE ELEMENTS EMPLOYED IN THE CALCULATION OF THE PERTURBATIONS.
Normals in heliocentric longitude for Saturn
Equations of condition in three different suppositions
CHAPTER XXIX. RECTIFICATION OF THE FORMULÆ FOR THE PERTURBATIONS ON ACCOUNT OF THE CORRECTIONS OF THE ELEMENTS JUST DETERMINED.
Formulæ employed for this purpose

9

CHAPTER XXX. ADDITION OF THE S ORDINATES OF JUPITER AND FORM.	_						-					
Values of planetary masses finally adopte	d								 			,
Corrections to certain terms in the co-ord	inates for changes in t	hes e	va	lues	з.				 			
Corrections to pass from ν and ν' to log (
Corrected elements of the two planets .												
Logarithms of their semi-axes												
Values of the constituents of the argument												
Inequalities of the fundamental argument												
Inequalities of the logarithm of the radiu												
Periodic inequalities of the latitude of Ju												
Formulæ for the principal terms of the co												
Inequalities of the fundamental argument												
Inequalities of the logarithm of the radiu												
Periodic inequalities of the latitude of Sa												
Formulæ for the principal terms of the co												
ADDENDA												



INTRODUCTION.

Jupiter and Saturn must have presented to the earliest observers of the celestial motions less difficulties than the interior planets. The first things noted, undoubtedly, were, that the first made a circuit of the heavens in about twelve and the second in about thirty years. Then the retrograde motion, at the time of opposition, and its extent would be perceived. The slowness and steadiness of the motion would naturally suggest the hypothesis of circular motion, but it was certainly reserved for a later and more philosophic age to explain the later-observed phenomenon by means of an epicycle.

The earliest tables of the motions of Jupiter and Saturn, as well as those of the other large planets which have come down to us, are those contained in the Syntaxis of CLAUDIUS PTOLEMY. The annual parallax is there taken into account by one epicycle and the proper eccentricity of the orbit by a second. This, in the main, is the character of all the tables of the planets until the publication of Kepler's Tabulæ Rudolphinæ in 1627, where, for the first time, the equation of the center is derived from an elliptic formula, and we pass from heliocentric to geocentric positions in the modern way. From Kepler onwards the fact of the deviation of Jupiter and Saturn from a purely elliptic theory was recognized. Many attempts were made to better the theory; but it was found that no observations, embracing a long period of time, could be satisfied by elliptic elements varying proportionally to the time. Halley seems to have been the most successful in his tables; he adopted terms in the mean longitudes varying as the square of the time.

It was not until 1748 that any computation of the perturbations of Jupiter and Saturn, in accordance with the theory of gravitation, was undertaken. This was by Euler. He appears to have limited himself to the terms which have the mean elongation of the planets from each other as their argument. Later the terms factored by the simple power of the eccentricities were added by himself, Lalande, Lagrange, Bailly, and Lambert. But these terms not bringing about a reconciliation between observation and theory, Lagrange and Laplace were led to make their notable researches on the possibility of secular equations in the mean motions of the planets. At length the whole difficulty with Jupiter and Saturn was removed by Laplace's discovery of the great inequalities in 1786.

DELAMBRE almost immediately constructed tables for these planets which far exceeded in accuracy any previously possessed. They are those which appear in the third edition of LALANDE'S Astronomie. This great success seems to have stirred up

Laplace and his colaborers to pushing the approximations still further. On the publication of the third volume of the *Mécanique Céleste*, terms of the fifth order with respect to the eccentricities and mutual inclination, as well as some of two dimensions with respect to disturbing forces, had been added to the coefficients of the great inequalities. That these advances might be utilized Bouvard constructed tables of the planets founded on observed oppositions from 1747 to 1803. The formulæ used are very nearly those given in the *Mécanique Céleste*, Tom. III. These tables were published by the Bureau des Longitudes in 1808. It was discovered, however, that the terms of the fifth order, mentioned above, had been taken with the wrong sign. This led Bouvard to prepare a new edition of his tables, which appeared in 1821, and in which this error was rectified, and the observations employed in the discussion extended to 1814.* Although Bouvard himself speaks in admiration of the small residuals shown by the comparison of his theory with the observations, yet a glance shows their tendency to a systematic character, and this, too, with observations rather rudely reduced.

Plana undertook, shortly after, to compute the portions of the great inequalities which arise from considering the square of the disturbing force.† The results he obtained failed to satisfy an equation of condition which Laplace had employed in his investigation. After some discussion Laplace abandoned his equation and substituted for it another, which Plana's results were as far from satisfying as before. Pontécoulant then, taking up the subject, discovered that Laplace's results had been taken with the wrong sign, and that Plana had made errors of some importance in his investigation. When these oversights had been corrected the different results were brought into tolerable agreement.

However, the failure of Bouvard's tables to better represent observations, and his getting for the mass of Jupiter a value so much smaller than was shortly after obtained from the action of this planet on the asteroids and on its own satellites, can not be explained by this error of sign. It is somewhat singular that no one has yet pointed out the real cause, which, it seems, must be either some error in the coefficients of his formulæ or some error in putting his equations in tables.

Neither Laplace's, Plana's, nor Pontécoulant's determination of these secondorder terms can be regarded as anything else than a very rude and inadequate approximation.

Hansen had, a short time previous, imagined a new method of treating perturbations. In the *Mécanique Céleste* Laplace had determined all long-period inequalities as if they were to be applied to the mean longitude, and had so directed they should, while the short-period ones were derived as if they were to be added to the true longitude. There is, therefore, a want of congruity, and even of rigor, in this way of proceeding. For Laplace has nowhere shown how these two modes of application can be employed in unison. It is plain there would be as many methods of perturbations as there were opinions as to the dividing line separating long from short-period

^{*}Comparisons extending to 1819 are given in the preface to the tables; but it appears those of the last five years were added after the discussion was completed. See, on this point, LAPLACE, Théorie Analytique des Probabilités, Supplement I, p. 21.

[†] Memoirs Roy. Ast. Soc., Vol. II.

INTRODUCTION. 13

inequalities. These imperfections no doubt attracted the attention of Hansen, whose thought must have been: Since it is advantageous to apply the long-period terms to the mean longitude, and indifferent whether the short-period ones are applied to the mean or true, why not apply all to the mean, and, moreover, compute the radius-vector and latitude with this equated quantity? Then the additional quantities necessary to complete the values of the latter co-ordinates would be, for the first, a function of three variations of the elements, and for the second, a function of two only. This, undoubtedly, was the origin of Hansen's new method.

He determined to apply it to Jupiter and Saturn, and his memoir, crowned by the Berlin Academy, must be regarded as the earliest example of an adequate treatment of perturbations of the second order with respect to disturbing forces. In all previous investigations it is impossible to form a conception of the probable magnitude of the terms passed over on account of the habit of the investigator of selecting here and there a term to be computed. But in Hansen the continuity in the computed terms enables one to form a fair judgment as to the importance of those neglected. However, Saturn alone is treated with a fair degree of completeness. The expressions for Jupiter are limited to the terms arising from the first power of the disturbing force. Had this theory of Saturn been completed by the addition of the terms due to the action of Uranus and the whole compared with the observations more carefully reduced, as they then could have been by the aid of Bessel's Tabulæ Regiomontanæ, very excellent tables would have been obtained. But Hansen seems to have been carried away with the ambition of applying his peculiar method of treatment to the lunar theory.

A long period of over forty years now elapsed without anything being contributed to the theories of Jupiter and Saturn, for the expressions of the perturbations given in Pontécoulant's Théorie Analytique du Système du Monde, beyond the correction of the error of sign in the second-order terms of the great inequalities, do not seem to be in anything more perfect than those found in the Mécanique Céleste.

In 1868 Mr. Hugh Breen published a memoir containing equations of condition for the whole series of observations of the two planets made at Greenwich from 1750 to 1865, and, dividing them into four groups, obtained solutions for each. But as the equations contained no terms for the corrections of the acting masses, and no investigation was made of the errors of the formulæ actually employed in the construction of Bouvard's tables, the corrections obtained, when applied to Bouvard's elements, do not give anything like a fair approximation to the actual elements.

Hansen, in 1875, published a memoir on Jupiter. But here, deserting his earlier notions on the lack of convergence in algebraical developments, he confines himself to calculating the easier terms of the co-ordinates. Hence this memoir can not be regarded as advancing much our knowledge of the subject.

In the years 1874 to 1876 appeared Leverrier's investigation, concluding with the tables which are at present employed for all the European ephemerides. The method followed is that of attributing the perturbations to the six elements of the Keplerian ellipse; and, contrary to the mode followed in his earlier planetary theories, these are also the quantities tabulated. Leverrier's labor is very much increased by his undertaking to exhibit, in the first instance, all his developments in a form where all

the elements, save the mean distances, appear as indeterminates. This he does on the plea that, however far in the future the observations may be prolonged, they ought to be represented by one and the same theory. This notion must be approved by all, but it must be pointed out that it is not completely attained by substituting, in a set of formulæ belonging to an old epoch, the values the varying elements have arrived at, at the new epoch. It is true the two sets of formulæ may be in perfect consonance, but they can not be considered as one and the same. At best, this is but a distant imitation of the method of obtaining integrals by mechanical quadratures. If we wish to have theories good for all time we shall find ourselves driven to making the coefficients of our periodic terms perfectly constant, and to admitting about three elementary constituents into the arguments for every planet that acts. Leverrier's hope that his work would serve as a foundation for future investigations is not warranted by past experience. For if at any time it is found not adequate to present wants the suspicion is sure to arise that this is due, in part at least, to not carefully enough performed calculations. Besides, we can not expect that work of this difficult nature will ever be undertaken except by well-trained experts, who will feel that they ought to be permitted to choose methods satisfactory to themselves. Thus every investigator of the planetary theories sets out ab origine.

In consequence of this adoption of indeterminate elements in the formulæ Lever-RIER'S values of the coefficients are less precise than if the latter had been treated as wholes. In the case of Saturn, however, he made an additional development by mechanical quadratures. There is not a very close agreement between the results of this and the algebraically derived formulæ. The difference, for instance, in the case of the coefficient of the great inequality exceeds 40". With the exception of the terms constituting the great inequality and a term denoting a secular acceleration of the mean longitude Leverrier employed, in the construction of his tables, formulæ resulting from this process of mechanical quadratures. The way in which the observations of Saturn were represented by this theory was not satisfactory, the residuals being larger at times than could be accepted as errors of the observers; and the comparisons made with observation since the publication of the tables have shown residuals somewhat larger. With Jupiter Leverrier was more successful, but his discussion led him to assign to Saturn a mass which astronomers at present regard as too small. However, I have not been able to discover any oversight in Leverrier's theories which would account for these discrepancies. A few trifling errors, having plainly no effect on the representation of observation, were all that were found.

The desirableness of a new investigation of the subject has been generally admitted, and fault has been found with the amount of labor required to deduce positions of the planets from Leverrier's tables. But I had not these inducements to take up the subject when I began work, for these tables were then unpublished. The long interval which occurred between the publication of Leverrier's theory of Mars and the appearance of anything from him on Jupiter and Saturn was the occasion of leading me to consider the undertaking. On making known to the Superintendent of the American Ephemeris my desire to take up the problem I was relieved from all other routine work, and supplied with the assistance necessary to duplicate all my

INTRODUCTION.

15

computations which required this safeguard against error. It was desired to abandon the use of the antiquated tables of Bouvard, and it appeared uncertain when Lever-RIER would publish his.

The plan, therefore, was to form theories of Jupiter and Saturn which would be practically serviceable for a space of three hundred years on each side of a central epoch taken near the center of gravity of all the times of observation; theories whose errors in this interval would simply result not from neglected terms in the developments, but from the unavoidable imperfections in the values of the arbitrary constants and masses adopted from the indications of observation.

Such were the considerations which influenced the adoption of the course to be followed. As there was no desire to lose time by forming a special method of treatment for the problem in hand it was decided to employ the method of Hansen, with such slight modifications as the exigencies of the case might suggest. On account of the presence of the great inequalities this method seemed to me to give expressions best suited to tabulation. The latest form of this method appears in Hansen's memoir entitled Auseinandersetzung, etc. The employment of the eccentric anomaly of the planet whose co-ordinates are sought as the independent variable undoubtedly augments the convergence of the series; but the adoption of this mode of proceeding would bring about the use of two independent variables, one for the co-ordinates of Jupiter, another for those of Saturn. As the developments have to be pushed to terms of three dimensions with respect to disturbing forces the heaviest part of the labor consists in forming products of periodic series, one of which belongs to Jupiter, the other to Saturn; and as integration can not be performed unless these products are transformed so as to involve but one variable we should have an endless series of transformations to make. It therefore seems a necessity to have a single independent variable for the whole work. In consequence the final form adopted for all the periodic series is in terms of the mean anomalies, so that the time is always the independent variable. Fortunately very slight and readily perceived changes only are necessary in the formulæ of the Auseinandersetzung to render them applicable to the modified mode of proceeding.

Hansen's method makes two transformations of the series representing the odd powers of the distance between the acting planets in which Besselian functions are employed as multipliers; and he has thus no less than three different forms for these series, the first being that in which the eccentric anomalies of both planets appear, the second that in which one of the eccentric anomalies is replaced by a mean anomaly, and the third in which the expression is so transformed that it may be integrated by treating the first eccentric anomaly as the independent variable. One of these transformations and forms for the series can be avoided. By making the division of the circumference with reference to the mean anomaly instead of the eccentric, and computing all the auxilliary quantities to be employed so that they correspond to the points of this division, we obtain at once, and without any need of a transformation, the series in Hansen's second form. The additional labor required to make the auxilliary quantities correspond to given values of the mean anomaly instead of the eccentric is very trifling. Consequently I have adopted this way of proceeding.

On arriving at the treatment of terms of the second and third orders with respect to disturbing forces, another, and as it seems to me quite advantageous, modification was made in Hansen's method, by which the more important terms of the third order were included in the computation of those of the second order; and again, on making the computation of the third-order terms the more important terms of the fourth order were included. Past experience has shown that in the second-order terms, and presumably in all higher orders, the secular terms of lower orders cause larger modifications than the periodic terms. Thus the great inequalities, in their modification by the consideration of second-order terms, are affected about six times more by the secular than the periodic terms. Again, it is known that the second-order terms contribute very important portions to the secular terms. Hence, if on commencing the calculation of the second-order terms one could attribute to the secular terms, not their firstorder values, but these augmented by an approximate estimate of the corrections which in the obvious course of proceeding would be found for them, it is evident that the third-order terms, to be computed afterwards, would be much reduced in magnitude. And in computing the third-order terms a like method of treatment could be used with like benefit, and thus the fourth-order terms be rendered more easily negligible. This way of proceeding, of course, requires that the computation of every succeeding order of terms should be modified; but this is not difficult.

Thus the method I have followed is this: On arriving at the treatment of second-order terms ascertain first the two terms of δT , which are rigorously proportional to $\sin \gamma$ and $\cos \gamma$, and apply the corresponding secular terms to the secular terms of the first order, and with these terms so corrected proceed to the general determination of δT ; and in third-order terms proceed in like manner. The terms of δT having the argument γ constitute a very fair approximation to the second-order portion of the secular terms, as the supplementary quantities added after the integration of T contribute in comparison quite insignificant corrections.

For the sake of brevity in the tables I have ventured, at the end, to make an alteration in the signification of the fundamental argument. In the Auseinandersetzung Hansen defines this so that, on entering a table, constructed from a purely elliptic theory, we obtain the exact angle described by the radius-vector between any given To flatten this out into a plane he is obliged to compute the expression of a fourth co-ordinate, \(\Gamma \). Hansen's only apparent reason for adopting such a signification for his z is that the differential equation determining it is thereby slightly simplified. But astronomers care nothing for the description of angle by the radius; all they wish to know is whereabouts is the planet. In the Tables du Soleil HANSEN has modified his z in such a way that it gives directly, by the employment of a purely elliptic table, the apparent tropical longitude of the Sun. But by making his z thus include the effect of precession he was led into a difficulty. By stopping with terms multiplied by the square of the time his tables, at remote epochs, failed to give sufficiently approximate longitudes of the Sun. Hence he published a supplement containing the terms involving the next two higher powers of the time. adopt a similar mode of treating Jupiter and Saturn our difficulties would be greater, as the eccentricities of these planets are three or four times greater than that of the

Earth. However all embarassment is escaped if we agree to apply the principal term of precession, viz, that which is proportional to the time, outside of the table in which the argument is z.

Therefore I have equated z in such a way that it takes account of all the inequalities of the reduction to the ecliptic, secular and periodic, and also of all that part of precession which involves the square and higher powers of the time. This modification of z in no respect complicates its expression, which has the same form as before, only with numerical coefficients changed by amounts generally very small. In this way we escape the necessity of giving separate tables for the reduction to the ecliptic and for its periodic and secular perturbations. This method of treatment resembles that of Plana and Delaunay in the lunar theory, for they pay no attention to the orbit longitude of the Moon, but proceed immediately to the ecliptic longitude.

As the formulæ which have been given for the motion of the plane of the ecliptic and for precession appear to me to be lacking in the precision sufficient for these late times, on account of their being limited to terms involving the time and its square, I have devoted a chapter to this subject, in which the expressions are prolonged so as to include the cubes of the time. These expressions are not, however, the definitive ones to be employed in the construction of the tables. The determination of the motions of the equator and ecliptic belongs to the theory of the four inner planets, and when this theory is completed the necessary modifications in the final formulæ of the present work can readily be made.

I have everywhere employed the notation of Hansen without explanation, as it must now be very familiar to all who work in the planetary theories. Also, no demonstrations of the formulæ used are given whenever it is possible to make a reference to places where they may be found, generally the memoirs of Hansen. But in all important cases the formulæ actually used are set down in the interest of the detection of any errors; and it seems to me that it would be possible for one to repeat all the computations of this investigation without hindrance from obscurity in the explanations.

The arrangement of the work will be easily seen from a glance at the table of contents. The terms arising from the first power of the disturbing force are considered by themselves. This occupies Chapters I to VII. The second-order terms in the fundamental arguments and the radii vectores, due to the interaction of Jupiter and Saturn, follow. This investigation is comprised in Chapters VIII to XV. The similar terms of the third order are next treated, and fill up Chapters XVI to XX. The perturbations of the two planets which are of the second order and have the mass of Uranus as factor follow. They are contained in Chapters XXI to XXIII. The second-order terms of the latitudes are then derived in Chapters XXIV and XXV. The motions of the ecliptic and precession are treated in Chapter XXVI. The longitudes and latitudes are referred to the mean equinox and ecliptic in Chapter XXVIII. Corrections for the provisionally adopted elements are, in the next place, found by a comparison of the previously obtained theory with observation. This fills Chapter XXVIII. The formulæ for the perturbations are rectified on account of these corrections in Chapter XXIX. In fine, the summed expressions for the co-ordinates of Jupiter and Saturn are given in Chapter XXXX.

In the long period of seven and a half years in which the computations of this investigation were carried on some modifications of the ideas entertained as to the proper values to be attributed to the planetary masses could scarcely fail to occur, and one will notice some incongruity in this respect; but the final results, given in Chapter XXX, are reduced to perfect uniformity in this respect. The values to which they correspond are those stated at the beginning of Chapter XXVI.

A careful comparison of the expressions obtained for the co-ordinates by Lever-RIER with those obtained in this investigation would undoubtedly have much interest, and might lead to the detection of the causes of disagreement. But the very great labor involved in carrying it out must be my excuse for not undertaking it. In the case of Saturn, too, whether Leverrier's elaboration by the algebraical process or that by mechanical quadratures should be taken for comparison would be an embarrassing question. The latter is very incomplete, yet Leverrier very nearly, as far as he could, used it for his tables. In the circumstances I must limit myself to pointing out, in a rude way, the more striking discrepancies. I have made a reduction of Leverrier's algebraically-determined coefficient of the great inequality of Saturn to Hansen's form of the perturbations and to Bessel's value of the mass of Jupiter, and it comes out 2944".80. The value assigned in Chapter XXX is 2907".85. LEVERRIER'S is therefore the larger by 36".95. Had we taken for reduction the value given by Leverrier's other process the difference would have been smaller. motions assigned to the eccentricity and perihelion of Saturn in Leverrier's tables are considerably greater than those given by my theory. In the case of Jupiter LEVERRIER'S values of the coefficients of the large terms are quite as large as mine, although they profess to correspond to the value $\frac{1}{3529.6}$ of the mass of Saturn, while

mine have been computed with the mass $\frac{1}{3501.6}$. This, perhaps, explains why Lever-RIER'S discussion led him to the too small mass of Saturn.

In performing the very large mass of computations demanded by this investigation, by direction of the Superintendent, I have been assisted by various gentlemen connected with this office; all, however, to small amounts, with the exception of Mr. W. F. McK. RITTER, who, with the greatest efficiency, has made a duplicate of about two-thirds of the computations. Without help such as he has rendered it would have been impossible for me to have brought this undertaking to a conclusion. But all the original computations have been performed by myself.

A NEW THEORY OF JUPITER AND SATURN.

CHAPTER I.

MUTUAL ACTION OF JUPITER AND SATURN.—DEVELOPMENT OF THE RECIPROCAL OF THE DISTANCE BETWEEN THE PLANETS AND ITS ODD POWERS IN PERIODIC SERIES, WHEN ELLIPTIC VALUES ARE SUBSTITUTED FOR THE CO-ORDINATES.

The first step in determining the absolute perturbations of the elliptic motions arising from the mutual action of two planets is to obtain the expansion of the reciprocal of their distance and its odd powers in periodic series. The first and third powers alone are necessary in treating the perturbations due to the first power of the disturbing force; the fifth, in addition, is required when the second and the seventh when the third power of this force is taken into consideration. In this chapter we shall be engaged in developing these four powers of the reciprocal of the distance between Jupiter and Saturn, it being understood that elliptic values are attributed to the coordinates. The method pursued demands that these developments in their final form should appear as functions of the mean anomalies of the two planets, or in other words as functions of the time.

The elements adopted for the two planets are:

Elements of Jupiter and Saturn.

Epoch, 1850, Jan. o.od, Greenwich M. T.

$$\begin{array}{lll} \mathbf{L} = 159^{\circ} \ 56' \ 26''.60 & \mathbf{L}' = 14^{\circ} \ 49' \ 34.''04 \\ \pi = 11^{\circ} \ 56' \ 9''.33 & \pi' = 90^{\circ} \ 6' \ 46''.22 \\ \theta = 98^{\circ} \ 56' \ 19''.79 & \theta' = 112^{\circ} \ 20' \ 49.''05 \\ \mathbf{i} = 1^{\circ} \ 18' \ 42.''10 & \mathbf{i}' = 2^{\circ} \ 29' \ 40''.19 \\ e = 0.04824277 & e' = 0.05605688 \\ n = 109256''.55563 & n' = 43996''.07844 \\ m = \frac{1}{1047.879} & m' = \frac{1}{3501.6} \end{array}$$

It is scarcely necessary to go into details as to the derivation of these elements. They are supposed to be mean elements derived in such a way that the perturbations of the fundamental argument and the latitude have no terms whose period is the same as that of the mean anomaly, and the former no constant term or term proportional to the time. The elements of Saturn have been obtained from a previous investigation, and are supposed to be quite approximate. Those of Jupiter have been got by apply-

ing to Bouvard's values the corrections found by Mr. Breen.* On account of the errors of Bouvard's formulæ for the perturbations these values will probably be found to need quite large corrections. But they are sufficiently accurate to serve our purpose, as it is proposed at the end of this investigation to ascertain rudely their errors and correct the expressions for the perturbations by the differential method where the squares and products of these errors may be neglected.

In computing the mutual perturbations of two planets we need consider only the ratio of the mean distances. This is given by the equation

$$\alpha = \frac{a}{a'} = \left[\frac{\mathbf{I} + m}{\mathbf{I} + m'}\right]^{\frac{1}{3}} \left(\frac{n'}{n}\right)^{\frac{2}{3}}$$

whence, on substitution of the numerical values,

$$\log \alpha = 9.7367410563$$

But a considerable portion of the perturbations of the second order will be included in the computation of the terms of the first order if we apply severally to $\log a$ and $\log a'$ the constant parts of the perturbations of $\log r$ and $\log r'$. For the action of all the planets excepting Jupiter and Saturn these parts can be, with sufficient accuracy, obtained from the following formulæ:

For the action of an outer on an inner planet

$$\delta \log a = -\frac{1}{6} \operatorname{M} m' \alpha^2 \frac{db_{\frac{1}{2}}^{(0)}}{d\alpha}$$

for the action of an inner on an outer planet

$$\delta \log a' = \frac{1}{6} Mm' \left(b_{\frac{1}{2}}^{(0)} + \alpha \frac{db_{\frac{1}{2}}^{(0)}}{d\alpha} \right)$$

where M is the modulus of common logarithms. For the action of Jupiter and Saturn the values are obtained from Hansen.†

		δ log a	$\delta \log a'$
Action of Mercury, mass	5000000	+.00000003	+.00000003
Action of Venus, mass	425000	+.00000035	+.00000034
Action of the Earth, mass	322800	+.00000046	+.00000045
Action of Mars, mass	3095000	+.00000005	+.00000005
Action of Jupiter,	- 70		+.00018522
Action of Saturn,		00000502	
Action of Uranus, mass	21000	00000007	00000058
Action of Neptune, mass	19700	00000002	00000013
Sums,		00000423	+.00018538

^{*} Correction of Bouvard's Elements of Jupiter and Saturn. Appendix I to Greenwich Observations, 1868. † Untersuchung über die gegenseitigen Störungen des Jupiter und Saturn. Berlin, 1831.

To avoid confusion we will designate a and a', after their correction by these quantities, as a and a', but α will be employed as the equivalent of $\frac{a}{a'}$. When we come to the treatment of the perturbations of the second order it will be necessary to remember that this modification has been made.

The quantities which define the relative position of the planes of the orbits can be obtained from the equations

Here J denotes the inclination of the planes of the orbits, and Π and Π' , severally, the angular distances of the perihelia of Jupiter and Saturn from the ascending node of Saturn's orbit on that of Jupiter.

The coefficients of the terms of the developments of the reciprocal of the distance between the planets $\frac{a'}{\triangle}$ and its odd powers $\left(\frac{a'}{\triangle}\right)^3$, $\left(\frac{a'}{\triangle}\right)^5$, etc., as periodic functions of the two anomalies, are then functions of the following six elements:

We must now consider the degree of accuracy with which these coefficients must be computed in order that a proposed degree of accuracy may be obtained in the coefficients of the perturbations. Let it be demanded that the latter shall be got correct to 0".001 in the longitude and latitude. The coefficients of the terms in $\frac{a'}{\triangle}$, whose argument is 5g'-2g, will be multiplied by the factor

15
$$\frac{m}{1+m'} \frac{n'^2}{(5n'-2n-82'')^2} \times 206264''.8$$
, (log = 6.4738)

in order to obtain the coefficients of the perturbation of the mean anomaly of Saturn. It is thus seen that o''.oo1 in the latter is equivalent to 0.0000000034 in the former. Consequently ten-place logarithms will have to be used until we get the coefficients of the terms in $\frac{a'}{\triangle}$, which have the argument 5g'-2g. Recourse has been had to V_{EGA} 's Thesaurus Logarithmorum for the logarithms.

In the case of $\left(\frac{\mathbf{a}'}{\Delta}\right)^3$ a far less degree of accuracy will suffice; nevertheless, for those terms on which depend the secular perturbations a degree of accuracy has been adopted which is equivalent to the employment of eight-place logarithms. For $\left(\frac{\mathbf{a}'}{\Delta}\right)^5$ and $\left(\frac{\mathbf{a}'}{\Delta}\right)^7$, respectively, seven and five-place logarithms suffice.

In developing these quantities after the manner of Hansen,* it is preferable to take Saturn as the disturbed planet, for the reason that in this way the quantity he has denoted by γ_2 is less than one-fifteenth of what it is when Jupiter is so taken.

We have the well-known equations

$$H = \cos (f + \Pi) \cos (f' + \Pi') + \cos J \sin (f + \Pi) \sin (f' + \Pi')$$

$$\wedge^2 = r'^2 - 2rr' H + r^2$$

If the constants k, K, k_1 , K_1 are obtained from the equations

$$k \cos (\Pi' - K) = \cos \Pi$$
 $k_1 \cos (\Pi' - K_1) = \cos \mathbf{J} \cos \mathbf{\Pi}$ $k \sin (\Pi' - K) = \cos \mathbf{J} \sin \Pi$ $k_1 \sin (\Pi' - K_1) = \sin \mathbf{\Pi}$

we have

$$\mathbf{H} = k \cos (f' + \mathbf{K}) \cos f + k_1 \sin (f' + \mathbf{K}_1) \sin f$$

The numerical substitutions give

$$\log k = 9.9999134935$$
 $K = 78 \text{ 10 } 31.71660$
 $\log k_1 = 9.9999821696$ $K_1 = 78 \text{ 9 } 54.40637$

The square of the distance between the planets is reduced to the form

$$\left(\frac{\triangle}{\mathbf{a}'}\right)^2 = \gamma_0 - f \cos\left(\varepsilon - \mathbf{F}\right) + \gamma_2 \cos^2 \varepsilon$$

by computing p, P, v, V, w, W, w_1 , W_1 from the equations (φ and φ' denoting the angles of the eccentricities)

$$p \sin P = 2\alpha \left(\alpha \frac{e}{e'} - k \cos K\right)$$

$$p \cos P = 2\alpha k_1 \cos \varphi \sin K_1$$

$$v \sin \nabla = 2\alpha k \cos \varphi' \sin K$$

$$v \cos \nabla = 2\alpha k_1 \cos \varphi \cos \varphi' \cos K_1$$

$$w \sin W = p - 2\alpha^2 \frac{e}{e'} \sin P$$

$$w \cos W = v \cos (\nabla - P)$$

$$w_1 \sin W_1 = v \sin (\nabla - P)$$

$$w_1 \cos W_1 = 2\alpha^2 \frac{e}{e'} \cos P$$

$$R = 1 + \alpha^2 - 2\alpha^2 e^2$$

$$y_2 = \alpha^2 e^2$$

After which

$$f \sin (\mathbf{F} - \mathbf{P}) = w \sin (\varepsilon' + \mathbf{W}) - e'p$$

$$f \cos (\mathbf{F} - \mathbf{P}) = w_1 \cos (\varepsilon' + \mathbf{W}_1)$$

$$y_0 = \mathbf{R} - 2e' \cos \varepsilon' + e'^2 \cos^2 \varepsilon' + ef \cos \mathbf{F}$$

The numerical substitutions give

^{*}Auseinandersetzung einer zweckmässigen Methode zur Berechnung der absoluten Störungen der kleinen Planeten. Abhandlung I, s. 138.

In the last equation the brackets denote that the common logarithms are given instead of the numbers corresponding.

It will suffice to divide the circumference with respect to the mean anomaly of Saturn (for the reasons stated in the Introduction we adopt the mean anomaly instead of the eccentric, which Hansen uses) into sixteen parts. In this way the errors committed in the coefficients belonging to the great inequality are of the 16-3 = thirteenth order with respect to the eccentricities and inclination of the orbits. The errors relative to double the argument of this inequality are of the 16-6 = tenth order. This is certainly a sufficient degree of exactitude.

We compute by trial from the equation

$$g' = \varepsilon' - e' \sin \varepsilon'$$

where log (e' in seconds of arc) = 4.0630540554, the values of ϵ' corresponding to the seven following values of g':

The values for the remaining points of division of the circumference are either known or readily deducible from these. By substituting them in the preceding equations which give the values of γ_0 , f, and F, we get the following table:

g'	7 0	$\log f$	$\mathbf{F}-g'$		
o			0	,	"
0	1. 1984385810	0. 0146441389	76	36	30. 05448
22.5	1. 1858045730	0.0116067484	7 9	15	27.87825
45	1. 1916240568	0.0131809243	81	42	56. 61757
67.5	1.2147457246	0. 0188912301	83	32	2. 35338
90	1.2509960366	0.0273706837	84	26	6. 62580
112.5	1.2942528243	0. 0369329790	84	20	48. 21352
135	1.3377252007	0. 0460462355	83	21	48. 24421
157.5	1. 3750575191	0. 0535462990	81	41	8. 79693
180	1.4011119502	0. 0586511882	79	34	7. 28496
202.5	1.4124496841	0. 0608956692	77	17	19. 95693
225	1. 4075886817	0.0600677450	75	7	38. 21369
247.5	1. 3871073227	0. 0561863167	73	21	27.02105
270	1. 3536269388	0. 0495348409	72	13	53.72792
292.5	1. 3116584293	0. 0407480405	71	57	17. 20268
315	r. 2672436572	0. 0309155839	72	38	35. 73266
337.5	1. 2272790242	0.0216041043	74	16	5.05534

These quantities can be subjected to the following important test: The sum of the values which correspond to 0°, 45°, 90°... 315° ought to be nearly equal to the sum of the values which correspond to 22°.5, 67°.5, 112°.5... 337°.5. It is known that the difference is of the eighth order with respect to the eccentricities and mutual inclination. Calling these sums S and S' the result here is:

	<i>y</i> ₀	$\log f$	$\mathbf{F}-g'$		-g'
S S'	10. 4083551030	o. 3004113404 o. 3004113872	_		36. 50129 36. 47808

This test is applicable to many of the following computations, and the result of its application will always be given.

Following Hansen's procedure, we separate the square of the distance into two factors, such that

$$\left(\frac{\triangle}{\mathbf{a}'}\right)^2 = \left[\mathbf{C} - q\cos\left(\varepsilon - \mathbf{Q}\right)\right] \left[\mathbf{I} - \frac{\gamma_2}{q}\cos\left(\varepsilon + \mathbf{Q}\right)\right]$$

which gives, for determining C, q, and Q, the equations

$$\begin{aligned} \mathbf{C} &= \gamma_0 + \gamma_2 \sin^2 \mathbf{Q} \\ f \sin \mathbf{F} &= \left(q - \frac{\gamma_2 \mathbf{C}}{q} \right) \sin \mathbf{Q} \\ f \cos \mathbf{F} &= \left(q + \frac{\gamma_2 \mathbf{C}}{q} \right) \cos \mathbf{Q} \end{aligned}$$

By eliminating C and q we get

$$\sin{(Q - F)} = \frac{\gamma_2}{f^2} \frac{\gamma_0 + \gamma_2 \sin^2{Q}}{\sin{(Q + F)}} \sin^2{2Q}$$

from which, by trial, Q may readily be obtained. In like manner q may be got from the equation

$$q = f \cos (\mathbf{Q} - \mathbf{F}) - \frac{\gamma_2 \mathbf{C}}{q} \cos 2\mathbf{Q}$$

By development from these may be obtained series, proceeding according to ascending powers of γ_2 , which give the values of Q—F and $\log \frac{q}{f}$. They have been derived by Hansen.* In our case we have preferred the method by trial. The numerical results obtained are

^{*} Auseinandersetzung, Abhandlung I, S. 146, Gl. (120).

g,	C	$\log q$		Q-	-g'
			0	,	"
0	1.1990933606	o. 0149445 349	76	37	41.97691
22.5	1. 1864677121	0. 01 19163222	79	14	23. 98190
45	1.1920690737	0.0132773656	81	40	23. 28806
67.5	1.2149083561	0. 0187137572	83	29	47. 52405
90	1.2510025615	0. 0270452279	84	25	36. 181 20
112.5	1. 2943110889	0. 0366599027	84	22	14. 80626
135	1. 3379921669	0.0459719049	83	24	18. 63371
157.5	1. 3755681686	0. 0536999596	81	43	23. 61467
180	1. 4017811164	0. 0589513080	79	35	1. 54460
202. 5	1.4131215236	0. 0611975819	77	16	29. 02016
225	1. 4081065680	0. 0602270953	75	5	26. 06779
247.5	1. 3873834732	0.0561213072	73	18	57. 30456
270	1. 3536915381	0.0492712795	72	12	24. 19588
292.5	1. 3116626153	0.0404249841	71	57	41. 28342
315	1. 2673929280	0. 0307276532	72	40	44. 82897
3 37⋅5	1. 2277063745	0. 0216826028	74	18	39. 15769
s	10.4111293132	0. 3004163693	625	41	36.71712
S'		0. 3004163093	625	41	36. 69271
3	10.4111293123	0.3004104177	025	41	30.092/1

It seems desirable to make one more transformation in the form of Δ^2 ; we put

$$\frac{q}{\overline{C}} = \sin \chi \qquad \qquad \mathbf{a} = \tan \frac{\mathbf{I}}{2} \chi$$

$$\frac{\gamma_2}{q} = \sin \chi_1 \qquad \qquad \mathbf{b} = \tan \frac{\mathbf{I}}{2} \chi_1$$

$$\mathbf{N} = \frac{\sec \frac{\mathbf{I}}{2} \chi \sec \frac{\mathbf{I}}{2} \chi_1}{\sqrt{\overline{C}}}$$

In this way

$$\frac{\mathbf{a}'}{\triangle} = \mathbf{N} \left[\mathbf{1} - 2\mathbf{a}\cos\left(\varepsilon - \mathbf{Q}\right) + \mathbf{a}^2 \right]^{-\frac{1}{2}} \left[\mathbf{1} - 2\mathbf{b}\cos\left(\varepsilon + \mathbf{Q}\right) + \mathbf{b}^2 \right]^{-\frac{1}{2}}$$

g'	log N	log a	log b		
0					
0	0. 0223304134	9. 7585753170	6. 5239929		
22. 5	0. 0254063724	9. 7616990221	6. 5270211		
45	0. 0240423963	9. 7603321138	6. 5256601		
67.5	0. 0185553673	9. 7547944485	6. 5202237		
90	0.0101630309	9. 7463412483	6. 5118922		
112.5	0.0005153668	9. 7366605966	6. 5022775		
135	9. 9912124592	9. 7273667855	6. 4929655		
157.5	9. 9835260741	9. 7197220711	6. 4852375		
180	9. 9783269754	9.7145752236	6.4799861		
202. 5	9. 9761202182	9. 7124079836	6. 4777398		
225	9. 9771006514	9. 7133983631	6. 4787103		
247.5	9. 981 1817 483	9. 7174547678	6. 4828161		
270	9. 9879825162	9. 7242062749	6. 4896661		
292. 5	9. 9967796223	9. 7329541897	6. 4985124		
315	0.0064581878	9. 7426139882	6. 5082098		
337⋅5	0. 0155318861	9. 7517163322	6. 5172548		
s	9. 9976166306	7. 8874093144	72. 01 10830		
S'	9. 9976166555	7.8874094116	72.0110829		

The next step is the calculation of the values of Laplace's coefficients $b_s^{(i)}$, corresponding to each of the sixteen values of **a** just given. We proceed as follows:

Deriving θ from the equation

$$\sin \theta = a$$

we get

$$b = \cos \theta \qquad a^0 = \tan^2 \frac{1}{2}\theta \qquad b^0 = \frac{\sqrt{b}}{\cos^2 \frac{1}{2}\theta}$$

$$p = \frac{\left(\frac{1}{2}a^0\right)^2}{b^0} \qquad P = Mp^2 \qquad \log a^{00} = \log p - P \qquad \log b^{00} = -\frac{1}{2}P$$

where M is the modulus of common logarithms. Then

$$K = \sqrt{\frac{b^0 \ b^{00}}{b}} \qquad \qquad H = \frac{a^0}{2} \left[\ r + \frac{a^{00}}{2 \sqrt[4]{b^{00}}} \right]$$

and

$$b_{\frac{1}{3}}^{(0)} = 2K \qquad b_{\frac{1}{3}}^{(1)} = aK (r + H) \qquad b_{\frac{1}{3}}^{(2)} = \frac{2}{3}K \left[a^{2} (r + H) + H \right]$$

$$b_{\frac{1}{3}}^{(0)} = \frac{2K}{b^{4}} \left[r - a^{2}H \right] \qquad b_{\frac{3}{3}}^{(2)} = b_{\frac{3}{3}}^{(0)} - 2K (r + H) \qquad b_{\frac{3}{3}}^{(1)} = \frac{\sin \chi}{4} \left(3b_{\frac{3}{3}}^{(0)} + b_{\frac{3}{3}}^{(2)} \right)^{*}$$

On account of the importance of $b_{\frac{1}{2}}^{(2)}$ and $b_{\frac{1}{2}}^{(4)}$ and as a check their values have also been computed from the following series given by Leverrier† (the coefficients are replaced by their logarithms):

^{*} For the proof of these formulæ consult Legendre, Traité des Fonctions Elliptiques, Tome II, pp. 6 and 548. † Annales de l'Observatoire de Paris, Mémoires, Tome II, Additions, p. 2.

The remainders of these series can be summed as geometrical progressions. In this way have been obtained the following values, corresponding to intervals of 0.005 in $\log \alpha$. From these, by interpolation, it is easy to get the values corresponding to the sixteen values of $\log a$:

log a	$\logb_{rac{1}{2}}^{(2)}$	$\log b_{\frac{1}{2}}^{(4)}$
9. 710	9. 3493888435	8. 636820535
9. 715	9. 360848808	8. 658411500
9. 720	9. 3723541687	8. 680052169
9. 725	9. 3839064789	8. 701744508
9. 730	9. 3955076774	8. 723490591
9. 735	9. 4071597303	8. 745292605
9. 740	9. 4188647109	8. 767152856
9. 745	9. 4306248085	8. 789073783
9. 750	9. 4424423364	8. 811057961
9. 755	9. 4543197411	8. 833108118
9. 760	9. 4662596138	8. 855227147
9. 765	9. 4782647015	8. 877418108

The remaining coefficients $b_{\frac{1}{4}}^{(i)}$ can be got from the formula

$$b_{\frac{1}{2}}^{(i)} = \frac{4(i-1)}{2i-1} \frac{b_{\frac{1}{2}}^{(i-1)}}{\sin \chi} - \frac{2i-3}{2i-1} b_{\frac{1}{2}}^{(i-2)}$$

taking care, however, to use one more decimal in calculating than we wish to retain. But for large values of i it will be more convenient to compute the continued fraction

$$\frac{b_{\frac{1}{2}}^{(i)}}{b_{\frac{1}{2}}^{(i-1)}} = \frac{\frac{2i-1}{2i}\alpha}{1-\frac{\alpha^2}{4i(i+1)}} \frac{\alpha}{1-\frac{(2i+1)^2}{4(i+1)(i+2)}\alpha^2}$$

The remaining coefficients $b_{i}^{(i)}$ are got from the equation

$$b_{\frac{3}{4}}^{(i)} = b_{\frac{3}{4}}^{(i-2)} - \frac{2(i-1)}{\alpha} b_{\frac{1}{4}}^{(i-1)}$$

When i is large one can readily deduce the ratio between the quantities for two successive values of i by induction from the differences of the preceding logarithms.

The values of the $b_s^{(i)}$ are obtained from the formulæ

$$b_{\frac{s}{2}}^{(0)} + b_{\frac{s}{2}}^{(1)} = \frac{b_{\frac{s}{2}}^{(0)} + \frac{1}{3}b_{\frac{s}{2}}^{(1)}}{(1-\alpha)^2} \qquad b_{\frac{s}{2}}^{(0)} - b_{\frac{s}{2}}^{(1)} = \frac{b_{\frac{s}{2}}^{(0)} - \frac{1}{3}b_{\frac{s}{2}}^{(1)}}{(1+\alpha)^2} \qquad b_{\frac{s}{2}}^{(i)} = b_{\frac{s}{2}}^{(i-2)} - \frac{2(i-1)}{3\alpha}b_{\frac{s}{2}}^{(i-1)}$$

The formulæ used for obtaining the $b_{i}^{(i)}$ are

$$b_{\frac{z}{4}}^{(0)} + b_{\frac{z}{4}}^{(1)} = \frac{b_{\frac{z}{4}}^{(0)} + \frac{3}{5}b_{\frac{z}{4}}^{(1)}}{(\mathbf{x} - \alpha)^2} \qquad b_{\frac{z}{4}}^{(0)} - b_{\frac{z}{4}}^{(1)} = \frac{b_{\frac{z}{4}}^{(0)} - \frac{3}{5}b_{\frac{z}{4}}^{(1)}}{(\mathbf{x} + \alpha)^2} \qquad b_{\frac{z}{4}}^{(i)} = b_{\frac{z}{4}}^{(i-2)} - \frac{2(i-\mathbf{x})}{5\alpha}b_{\frac{z}{4}}^{(i-1)}$$

The following table contains all of these quantities it has been deemed necessary to compute. For convenience the points of division of the circumference relative to g' are designated as (0), (1), . . . (15):

	$\log\frac{1}{2}b_{\frac{1}{8}}^{(0)}$	$\log b_{\frac{1}{2}}^{(1)}$	$\logb_{rac{1}{2}}^{(2)}$	$\log b_{\frac{1}{3}}^{(3)}$	$\log b_{rac{1}{2}}^{(4)}$	$\log b_{rac{1}{2}}^{(5)}$	$\log b_{\frac{1}{2}}^{(6)}$	
(0)	0.0422349759	9. 8219019233	9. 4628509859	9. 1460177531	8. 848917435	8. 56330651	8. 2852309	
(1)	0. 0429700812	9. 8261268967	9. 4703315379	9. 1566921194	8. 862759506	8. 58030264	8. 3053729	
(2)	0. 0426465422	9. 8242752976	9. 4670549712	9. 1520177694	8. 856698867	8. 57286172	8. 2965554	
(3)	0. 0413651511	9. 8168178994	9. 4538302440	9. 1331333789	8. 832200292	8. 54277272	8. 2608899	
(4)	0. 0394960133	9. 8055641686	9. 4337891208	9. 1044619178	8. 794964713	8. 49700758	8. 2066157	
(5)	0. 0374762256	9. 7928569388	9.4110412050	9. 0718430303	8. 752546239	8. 44482671	8. 1446944	
(6)	0. 0356497314	9. 7808259144	9. 3893917767	9. 0407286674	8. 712031341	8. 39494475	8. 0854651	
(7)	0. 0342243503	9. 7710449263	9. 3717134206	9. 0152727021	8. 678847918	8. 35405988	8. 0368941	
(8)	0. 0333016727	9. 7645151480	9· 359 ⁸ 735555	8. 9982002666	8. 656575328	8. 32660393	8. 0042646	
(9)	0. 0329217162	9. 7617784029	9. 3549024197	8.9910266600	8. 647212588	8. 31505899	7. 9905416	
(10)	0. 0330947278	9. 7630281054	9. 3571730733	8. 9943037308	8. 651490004	8. 32033359	7. 9968115	
(11)	0. 0338143165	9. 7681630622	9. 3664916805	9. 0077455337	8. 669029733	8. 34195815	8. 0225132	
(12)	0. 0350522873	9. 7767700094	9. 3820693919	9.0301900000	8. 698297424	8. 37802650	8. 0653689	
(13)	0. 0367350622	9. 7880398438	9. 4023858750	9. 0594117420	8. 736365143	8. 42490941	8. 1210489	
(14)	0. 0387035953	9. 8006495388	9. 4250058437	9.0918765767	8. 778605336	8. 47688877	8. 1827461	
(15)	0. 0406726683	9. 8127022707	9. 4465125737	9. 1226718514	8. 818619460	8. 52608541	8. 2411037	
S	0. 3001795459	8. 3375301055	5. 2772087190	2. 5577966818	89. 997580448	87. 52997335	85. 1230582	
S'	0. 3001795714	8. 3375302408	5. 2772089564	2. 5577970178	89. 997580879	87. 52997391	85. 1230587	

	$\log b_{\frac{1}{4}}^{(7)}$	$\log b_{rac{1}{2}}^{(8)}$	$\log b_{\frac{1}{2}}^{(9)}$	$\log b_{\frac{1}{4}}^{(10)}$	$\log b_{rac{1}{2}}^{(11)}$	$\log b_{\frac{1}{2}}^{(12)}$	$\log \frac{1}{2} b_{\frac{3}{4}}^{(0)}$
	105 01	105 01	10g 01g	10g 01	rog v ₁	log $v_{\frac{1}{3}}$	108 2 03
(0)	8. 012484	7 74271	7.4780	7 0747	6 0505	6 6000	0.0000000000000000000000000000000000000
(1)	8. 035767	7. 74371 7. 77013	7. 5076	7.2147	6. 9535 6. 9893	6. 6939	o. 3815770471 o. 3882685965
(2)	8. 025575	7. 75856	7. 4946	7. 2474	6.9736	6. 7329 6. 7158	
(3)	7. 984342	7. 71177	7. 4940 7. 4423	7. 2331 7. 1752	6. 9102	6. 6468	0. 3853231659
(4)	7. 934342	7. 64051	7. 3625	7. 1/32	6. 8135	6. 5416	0. 3736623431
(5)	7. 849925	· .		6. 9862		- ·	0.3566666681
(6)	7. 781360	7.55915	7. 2715		6. 7030	6. 4215	0. 3383167742
(7)	1	7. 48126	7. 1843	6. 8897	6. 5972	6. 3064	0. 3217379468
	7.725113	7.41734	7. 1127	6. 8105	6. 5103	6. 2118	0. 3088090996
(8)	7. 687316	7.37438	7. 0645	6.7572	6. 4518	6. 1482	0. 3004441223
(9)	7. 671418	7. 35631	7.0443	6. 7348	6. 4273	6. 1215	0. 2970003660
(10)	7.678682	7. 36457	7. 0536	6. 7450	6. 4385	6. 1337	0. 2985684015
(11)	7.708455	7. 39841	7. 0915	6. 7870	6. 4845	6. 1837	0. 3050913479
(12)	7. 758090	7. 45482	7. 1546	6.8569	6. 5612	6. 2672	0. 3163179042
(13)	7.822556	7. 52806	7. 2366	6. 9477	6.6608	6. 3755	0. 3315877222
(14)	7. 893957	7. 60916	7 · 3274	7. 0482	6. 7709	6. 4953	0. 3494650909
(15)	7. 961462	7. 68580	7. 4132	7. 1431	6. 8749	6. 6085	0. 3673637317
S	82. 759036	80. 42696	78. 1195	75. 8318	73. 5602	71. 3021	2.7100997468
S′	82. 759039	80. 42697	78. 1197	75. 8319	73. 5603	71. 3022	2.7100999812
	$\log b_{\frac{3}{2}}^{(1)}$	$\log b_{\frac{3}{2}}^{(2)}$	$\logb_{\frac{3}{2}}^{(3)}$	$\logb_{\frac32}^{(4)}$	$\logb_{\frac{3}{2}}^{(5)}$	$\logb_{\frac{3}{2}}^{(6)}$	$\logb_{\frac32}^{(7)}$
(0)	0. 5631118888	0. 3981406377	0. 21280182	0. 0157694	9.8111164	9. 601092	9. 387073
(1)	0. 5721300721	0. 4099407726	0. 22753282	0. 0334998	9. 8318830	9.624918	9.413973
(2)	0. 5681679947	0. 4047621302	0. 22107214	0. 0257271	9. 8227817	9. 614478	9. 402188
(3)	0. 5523652504	0. 3840182539	0. 19512648	9. 9944604	9. 7861294	9. 572400	9. 354660
(4)	0. 5289763121	0. 3530493494	0. 15619400	9. 9473895	9. 7308256	9. 508806	9. 282738
(5)	0. 5032062005	0. 3185462420	0. 11253865	9. 8943923	9.6683838	9. 436858	9. 201243
(6)	0.3032002003						3.20123
	0. 4704072587	1					0. 123813
	0.4794072587	0. 2863139951	0. 07148990	9. 8443547	9.6092648	9. 368601	9. 123813
(7)	0.4604721309	o. 2863139951 o. 2604079767	o. 07148990 o. 03831122	9. 8443547 9. 8037684	9. 6092648 9. 5611982	9. 368601 9. 313011	9. 060671
(7) (8)	o. 4604721309 o. 4480304051	o. 2863139951 o. 2604079767 o. 2432566373	o. 07148990 o. 03831122 o. 01625366	9. 8443547 9. 8037684 9. 7767170	9. 6092648 9. 5611982 9. 5291062	9. 368601 9. 313011 9. 275850	9. 060 671 9. 018424
(7) (8) (9)	o. 4604721309 o. 4480304051 o. 4428622608	o. 2863139951 o. 2604079767 o. 2432566373 o. 2361015454	o. 07148990 o. 03831122 o. 01625366 o. 00703035	9. 8443547 9. 8037684 9. 7767170 9. 7653894	9. 6092648 9. 5611982 9. 5291062 9. 5156546	9. 368601 9. 313011 9. 275850 9. 260264	9. 060671 9. 018424 9. 000693
(7) (8) (9) (10)	0. 4604721309 0. 4480304051 0. 4428622608 0. 4452188662	o. 2863139951 o. 2604079767 o. 2432566373 o. 2361015454 o. 2393664182	o. 07148990 o. 03831122 o. 01625366 o. 00703035 o. 01124053	9. 8443547 9. 8037684 9. 7767170 9. 7653894 9. 7705612	9. 6092648 9. 5611982 9. 5291062 9. 5156546 9. 5217972	9. 368601 9. 313011 9. 275850 9. 260264 9. 267382	9. 060671 9. 018424 9. 000693 9. 008791
(7) (8) (9) (10) (11)	o. 4604721309 o. 4480304051 o. 4428622608 o. 4452188662 o. 4549614963	o. 2863139951 o. 2604079767 o. 2432566373 o. 2361015454 o. 2393664182 o. 2528244432	o. 07148990 o. 03831122 o. 01625366 o. 00703035 o. 01124053 o. 02856678	9. 8443547 9. 8037684 9. 7767170 9. 7653894 9. 7705612 9. 7918252	9. 6092648 9. 5611982 9. 5291062 9. 5156546 9. 5217972 9. 5470335	9. 368601 9. 313011 9. 275850 9. 260264 9. 267382 9. 296615	9. 060671 9. 018424 9. 000693 9. 008791 9. 042030
(7) (8) (9) (10) (11) (12)	o. 4604721309 o. 4480304051 o. 4428622608 o. 4452188662 o. 4549614963 o. 4715112882	o. 2863139951 o. 2604079767 o. 2432566373 o. 2361015454 o. 2393664182 o. 2528244432 o. 2755397030	o. 07148990 o. 03831122 o. 01625366 o. 00703035 o. 01124053 o. 02856678 o. 05771104	9. 8443547 9. 8037684 9. 7767170 9. 7653894 9. 7705612 9. 7918252 9. 8275149	9. 6092648 9. 5611982 9. 5291062 9. 5156546 9. 5217972 9. 5470335 9. 5893332	9. 368601 9. 313011 9. 275850 9. 260264 9. 267382 9. 296615 9. 345560	9. 060671 9. 018424 9. 000693 9. 008791 9. 042030 9. 097650
(7) (8) (9) (10) (11) (12) (13)	o. 4604721309 o. 4480304051 o. 4428622608 o. 4452188662 o. 4549614963 o. 4715112882 o. 4936087427	o. 2863139951 o. 2604079767 o. 2432566373 o. 2361015454 o. 2393664182 o. 2528244432 o. 2755397030 o. 3055911562	o. 07148990 o. 03831122 o. 01625366 o. 00703035 o. 01124053 o. 02856678 o. 05771104 o. 09607087	9. 8443547 9. 8037684 9. 7767170 9. 7653894 9. 7705612 9. 7918252 9. 8275149 9. 8743422	9. 6092648 9. 5611982 9. 5291062 9. 5156546 9. 5217972 9. 5470335 9. 5893332 9. 6447152	9. 368601 9. 313011 9. 275850 9. 260264 9. 267382 9. 296615 9. 345560 9. 409545	9. 060671 9. 018424 9. 000693 9. 008791 9. 042030 9. 097650 9. 170277
(7) (8) (9) (10) (11) (12) (13) (14)	o. 4604721309 o. 4480304051 o. 4428622608 o. 4452188662 o. 4549614963 o. 4715112882 o. 4936087427 o. 5189305295	o. 2863139951 o. 2604079767 o. 2432566373 o. 2361015454 o. 2393664182 o. 2528244432 o. 2755397030 o. 3055911562 o. 3396476025	o. 07148990 o. 03831122 o. 01625366 o. 00703035 o. 01124053 o. 02856678 o. 05771104 o. 09607087 o. 13927240	9. 8443547 9. 8037684 9. 7767170 9. 7653894 9. 7705612 9. 7918252 9. 8275149 9. 8743422 9. 9268738	9. 6092648 9. 5611982 9. 5291062 9. 5156546 9. 5217972 9. 5470335 9. 5893332 9. 6447152 9. 7066745	9. 368601 9. 313011 9. 275850 9. 260264 9. 267382 9. 296615 9. 345560 9. 409545 9. 480997	9. 060671 9. 018424 9. 000693 9. 008791 9. 042030 9. 097650 9. 170277 9. 251252
(7) (8) (9) (10) (11) (12) (13)	o. 4604721309 o. 4480304051 o. 4428622608 o. 4452188662 o. 4549614963 o. 4715112882 o. 4936087427	o. 2863139951 o. 2604079767 o. 2432566373 o. 2361015454 o. 2393664182 o. 2528244432 o. 2755397030 o. 3055911562	o. 07148990 o. 03831122 o. 01625366 o. 00703035 o. 01124053 o. 02856678 o. 05771104 o. 09607087	9. 8443547 9. 8037684 9. 7767170 9. 7653894 9. 7705612 9. 7918252 9. 8275149 9. 8743422	9. 6092648 9. 5611982 9. 5291062 9. 5156546 9. 5217972 9. 5470335 9. 5893332 9. 6447152	9. 368601 9. 313011 9. 275850 9. 260264 9. 267382 9. 296615 9. 345560 9. 409545	9. 060671 9. 018424 9. 000693 9. 008791 9. 042030 9. 097650 9. 170277
(7) (8) (9) (10) (11) (12) (13) (14)	o. 4604721309 o. 4480304051 o. 4428622608 o. 4452188662 o. 4549614963 o. 4715112882 o. 4936087427 o. 5189305295	o. 2863139951 o. 2604079767 o. 2432566373 o. 2361015454 o. 2393664182 o. 2528244432 o. 2755397030 o. 3055911562 o. 3396476025	o. 07148990 o. 03831122 o. 01625366 o. 00703035 o. 01124053 o. 02856678 o. 05771104 o. 09607087 o. 13927240	9. 8443547 9. 8037684 9. 7767170 9. 7653894 9. 7705612 9. 7918252 9. 8275149 9. 8743422 9. 9268738	9. 6092648 9. 5611982 9. 5291062 9. 5156546 9. 5217972 9. 5470335 9. 5893332 9. 6447152 9. 7066745	9. 368601 9. 313011 9. 275850 9. 260264 9. 267382 9. 296615 9. 345560 9. 409545 9. 480997	9. 060671 9. 018424 9. 000693 9. 008791 9. 042030 9. 097650 9. 170277 9. 251252

	$\logb_{rac{3}{4}}^{(8)}$	$\logb_{rac{3}{2}}^{(9)}$	$\log b_{rac{3}{2}}^{(10)}$	$\log b_{\frac{3}{2}}^{(11)}$	$\log b_{\frac{3}{4}}^{(12)}$	$\log rac{1}{2} b_{rac{\pi}{2}}^{(0)}$	$\log b_{\frac{5}{4}}^{(1)}$
(0)	9. 16997	8. 95040	8. 7288	8. 5056	8. 2810	0. 9374315	1. 2004172
(1)	9. 19995	8. 98348	8. 7650	8. 5449	8. 3234	0. 9525706	1.2165967
(2)	9. 18682	8. 96898	8. 7491	8. 5276	8. 3047	0. 9459100	1. 2094831
(3)	9. 13382	8. 91051	8.6852	8.4582	8. 2298	0. 9194893	1. 1811967
(4)	9. 05354	8.82186	8. 5882	8. 3528	8. 1160	0. 8808271	1.1395928
(5)	8. 96247	8. 72119	8. 4779	8. 2329	7.9865	0. 8388731	1.0941309
(6)	8. 87584	8.62534	8. 3728	8. 1185	7.8629	0.8007651	1.0525155
(7)	8. 80513	8. 54706	8. 2869	8. 0251	7. 7619	0.7709072	1.0196702
(8)	8. 75779	8.49461	8. 2294	7.9624	7.6940	0. 7515206	0. 9982205
(9)	8. 73791	8. 47257	8. 2052	7 . 9360	7. 6655	0. 7435236	0. 9893423
(10)	8. 7 4699	8.48263	8. 2162	7. 9481	7. 6785	0. 7471661	0. 9933884
(11)	8. 78425	8. 52391	8. 2615	7.9974	7.7319	0. 7622975	1. 0101569
(12)	8. 84655	8. 59293	8. 3373	8. 0799	7.8211	0. 7882634	1. 0387900
(13)	8. 92784	8. 68290	8. 4359	8. 1873	7. 9372	0. 8234295	1.0773050
(14)	9. 01837	8. 78299	8. 5456	8. 3065	8. 0660	0. 8643897	1. 1218225
(15)	9. 10450	8. 87814	8. 6498	8. 4197	8. 1883	0. 9051830	1. 1658323
S	1.65587	89. 71974	87. 7674	85. 8014	83. 8242	6. 7162735	8. 7542300
S'	1. 65587	89. 71975	87. 7674	85.8015	83. 824 5	6. 7162738	8. 7542310
	$\logb_{rac{5}{2}}^{(2)}$	$\logb_{\frac{5}{2}}^{(3)}$	$\logb_{rac{5}{2}}^{(4)}$	$\logb_{rac{5}{2}}^{\scriptscriptstyle{(5)}}$	$\log b_{rac{5}{2}}^{(6)}$	$\log b_{\frac{5}{2}}^{(7)}$	$\log b_{\frac{5}{4}}^{(8)}$
(0)	1. 1161428	1.0021564	0.8677099	0. 7183764	0. 5577605	0. 38831	0. 21173
(1)	1. 1342473	1.0226184	0. 8907638	0. 7441686	0. 5863792	0.41981	0. 24618
(2)	1. 1262929	1.0136345	0.8806463	0. 7328547	0. 5738282	0. 40598	0. 23108
(3)	1.0945691	0. 9777147	9. 8401145	0.6874605	0. 5234092	0. 35043	0. 17031
(4)	1.0476238	0. 9242889	0. 7795902	0.6194680	0. 4477105	0. 26688	0.07875
(5)	0. 9959088	0.8650458	0.7121354	0. 5433964	0. 3627626	0. 17288	9.97558
(6)	0.9481583	0. 8099664	o. 649094 5	0. 4720231	0. 2828182	0. 08420	9. 87807
(7)	0. 9101740	0. 7658824	0. 5984099	0. 4144423	0. 2181537	0. 01233	9. 79890
(8)	0. 8852179	0. 7367855	0. 5648423	0. 3762126	0. 1751457	9.96446	9.74613
(9)	0. 8748524	0.7246685	0. 5508369	0. 3602400	0. 1571561	9. 94441	9. 72401
(10)	0.8795790	0. 7301962	0. 5572280	o. 3675309	o. 1653688	9. 95357	9. 73410
(11)	0. 8991204	0.7530082	0.5835689	0. 3975494	0. 1991628	9. 99120	9. 77561
(12)	0. 9323184	0. 7916123	0. 6280176	0.4480994	0. 2559730	0. 05439	9. 84523
(13)	0. 9766515	0.8428772	o. 6868009	0. 5147454	0. 3306976	0. 13735	9. 93651
(14)	1.0274626	0. 901 2426	0. 7533918	0. 5899603	0.4147915	0. 23048	0. 03884
1 />	1.0772728	0. 9580689	0.8178919	0. 6625245	0. 4956722	0. 31983	0. 13681
(15)	i	1					
S S'	7. 9627957 7. 9627963	6. 9098828 6. 909884 1	5.6805206	4. 3245254	2. 8733964	1. 34827	9. 76393

	$\logb_{rac{\pi}{2}}^{(9)}$	$\logb_{\frac{5}{2}}^{(10)}$	$\logb_{rac{5}{3}}^{(11)}$	$\logb_{rac{5}{2}}^{\scriptscriptstyle (12)}$	$\log \frac{\mathrm{I}}{2} b_{\frac{7}{2}}^{(0)}$	$\log b_{\frac{7}{2}}^{(1)}$	$\logb_{\frac{7}{2}}^{(2)}$
(0)	0. 0293	9. 8420	9. 6506	9. 4556	1. 57609	1.85858	1.80816
(1)	0.0667	9, 8824	9.6940	9. 5021	1. 59982	1.88283	1.83370
(2)	0. 0503	9. 8647	9.6750	9. 4817	1. 58938	1.87216	1.82247
(3)	9. 9843	9.7934	9. 5983	9. 3996	1.54794	r. 82978	1.77778
(4)	9. 8847	9.6856	9. 4824	9. 2755	1.48718	1.76753	1.71191
(5)	9.7723	9. 5639	9. 3512	9. 1349	1.42105	1.69961	1.63971
(6)	9. 6658	9. 4484	9. 2268	9.0014	1. 36082	1.63758	1.57342
(7)	9.5793	9. 3545	9. 1254	8.8926	1. 31349	1.58869	1. 52093
(8)	9. 5215	9. 2918	9. 0576	8. 8198	1. 28270	1. 55683	1. 48659
(9)	9.4973	9. 2654	9. 0292	8. 7892	1.26999	1. 54365	1.47236
(10)	9. 5084	9. 2775	9.0422	8. 8032	1.27578	1. 54965	1. 47884
(11)	9.5538	9. 3268	9. 0955	8. 8604	1. 29982	1.57455	1.50570
(12)	9.6300	9. 4095	9. 1847	8. 9563	1. 34102	1.61714	1.55150
(13)	9.7297	9.5177	9. 3014	9. 0815	1. 39666	1.67452	1.61293
(14)	9.8412	9. 6385	9. 4317	9. 2212	1.46129	1.74097	1.68372
(15)	9. 9478	9.7540	9. 5559	9. 3543	1. 52547	1.80678	1.75348
s	8. 1312	6. 4580	4.7510	3.0146	11. 37426	13. 60044	13. 11661
S'	8. 1312	6. 4581	4.7509	3. 0146	11. 37424	13. 60041	13. 11659
	-		. , ,		"		
	$\log b_{ ilde{7}}^{(3)}$	$\log b_{rac{7}{2}}^{(4)}$	$\logb_{rac{7}{2}}^{(5)}$	$\logb_{\frac{7}{2}}^{(6)}$	$\log b_{\frac{7}{2}}^{(7)}$	$\log b_{ ilde{j}}^{(8)}$	$\log b_{\frac{7}{2}}^{(9)}$
(0)	$\log b_{\frac{7}{2}}^{(3)}$	$\log b_{\frac{7}{2}}^{(4)}$	$\log b_{\frac{7}{2}}^{(5)}$	$\logb_{ ilde{Z}}^{(6)}$	$\log b_{rac{7}{2}}^{(7)}$	$\log b_{\frac{7}{2}}^{(8)}$	$\logb_{_{2}}^{(9)}$
(0)	log $b_{\frac{7}{2}}^{(3)}$	log b ₂ ⁽⁴⁾	log $b_{\frac{7}{2}}^{(5)}$	log $b_{\frac{7}{2}}^{(6)}$	log $b_{\frac{7}{2}}^{(7)}$	log $b_{\frac{7}{2}}^{(8)}$	log $b_{\frac{7}{2}}^{(9)}$
(1)	log $b_{\frac{7}{2}}^{(3)}$ 1. 73225 1. 75959	log b ₄ ⁽⁴⁾ 1.*63615 1. 66565	log $b_{\frac{7}{2}}^{(5)}$ 1. 52389 1. 55573	log b ₂ ⁽⁶⁾ 1. 39853 1. 43295	log $b_{\frac{7}{2}}^{(7)}$ 1. 2624 1. 2993	log $b_{\frac{7}{2}}^{(8)}$	log $b_{\frac{7}{2}}^{(9)}$ o. 9644 1. 0067
(I) (2)	log $b_{\frac{7}{2}}^{(3)}$ 1. 73225 1. 75959 1. 74758	log b ₂ ⁽⁴⁾ 163615 1. 66565 1. 65267	log b ₂ ⁽⁵⁾ 1. 52389 1. 55573 1. 54175	log b ₂ ⁽⁶⁾ 1. 39853 1. 43295 1. 41781	log $b_{\frac{7}{2}}^{(7)}$ 1. 2624 1. 2993 1. 2832	log $b_{\frac{7}{2}}^{(8)}$ I. 1171 I. 1572 I. 1395	log $b_{\frac{7}{2}}^{(9)}$ o. 9644 1. 0067 o. 9885
(I) (2) (3)	log $b_{\frac{7}{2}}^{(3)}$ 1. 73225 1. 75959 1. 74758 1. 69964	log b ₂ ⁽⁴⁾ 163615 1. 66565 1. 65267 1. 60097	1. 52389 1. 55573 1. 54175 1. 48566	log b ₂ ⁽⁶⁾ 1. 39853 1. 43295 1. 41781 1. 35740	1. 2624 1. 2993 1. 2832 1. 2178	log $b_{\frac{7}{2}}^{(8)}$ I. 1171 I. 1572 I. 1395 I. 0694	o. 9644 1. 0067 o. 9885 o. 9120
(1) (2) (3) (4)	log $b_{\frac{7}{2}}^{(3)}$ 1. 73225 1. 75959 1. 74758 1. 69964 1. 62881	log b ₂ ⁽⁴⁾ 1.*63615 1. 66565 1. 65267 1. 60097 1. 52421	1. 52389 1. 55573 1. 54175 1. 48566 1. 40258	log b ₂ ⁽⁶⁾ 1. 39853 1. 43295 1. 41781 1. 35740 1. 26723	log b _{\(\frac{7}{2}\) 1. 2624 1. 2993 1. 2832 1. 2178 1. 1207}	log $b_{\frac{7}{2}}^{(8)}$ I. 1171 I. 1572 I. 1395 I. 0694 O. 9646	o. 9644 1. 0067 0. 9885 0. 9120 0. 8011
(1) (2) (3) (4) (5)	log $b_{\frac{7}{4}}^{(3)}$ 1. 73225 1. 75959 1. 74758 1. 69964 1. 62881 1. 55073	1.*63615 1. 66565 1. 65267 1. 60097 1. 52421 1. 43925	1. 52389 1. 55573 1. 54175 1. 48566 1. 40258 1. 31004	log b ₂ ⁽⁶⁾ 1. 39853 1. 43295 1. 41781 1. 35740 1. 26723 1. 16667	log b _{\(\frac{7}{2}\) 1. 2624 1. 2993 1. 2832 1. 2178 1. 1207 1. 0116}	log $b_{\frac{7}{2}}^{(8)}$ I. 1171 I. 1572 I. 1395 I. 0694 O. 9646 O. 8472	0. 9644 1. 0067 0. 9885 0. 9120 0. 8011 0. 6742
(1) (2) (3) (4) (5) (6)	1. 73225 1. 75959 1. 74758 1. 69964 1. 62881 1. 55073 1. 47868	log b ₂ ⁽⁴⁾ 1.*63615 1. 66565 1. 65267 1. 60097 1. 52421 1. 43925 1. 36047	1. 52389 1. 55573 1. 54175 1. 48566 1. 40258 1. 31004 1. 22392	1. 39853 1. 43295 1. 41781 1. 35740 1. 26723 1. 16667 1. 07276	1. 2624 1. 2993 1. 2832 1. 2178 1. 1207 1. 0116 0. 9098	I. 1171 I. 1572 I. 1395 I. 0694 O. 9646 O. 8472 O. 7370	0. 9644 1. 0067 0. 9885 0. 9120 0. 8011 0. 6742 0. 5559
(1) (2) (3) (4) (5) (6) (7)	1. 73225 1. 75959 1. 74758 1. 69964 1. 62881 1. 55073 1. 47868 1. 42134	log b ₂ ⁽⁴⁾ 163615 1. 66565 1. 65267 1. 60097 1. 52421 1. 43925 1. 36047 1. 29751	1. 52389 1. 55573 1. 54175 1. 48566 1. 40258 1. 31004 1. 22392 1. 15483	1. 39853 1. 43295 1. 41781 1. 35740 1. 26723 1. 16667 1. 07276 0. 99721	1. 2624 1. 2993 1. 2832 1. 2178 1. 1207 1. 0116 0. 9098 0. 8274	I. 1171 I. 1572 I. 1395 I. 0694 O. 9646 O. 8472 O. 7370 O. 6478	0. 9644 1. 0067 0. 9885 0. 9120 0. 8011 0. 6742 0. 5559 0. 4595
(1) (2) (3) (4) (5) (6) (7) (8)	1. 73225 1. 75959 1. 74758 1. 69964 1. 62881 1. 55073 1. 47868 1. 42134 1. 38369	log b ₂ ⁽⁴⁾ 1.*63615 1. 66565 1. 65267 1. 60097 1. 52421 1. 43925 1. 36047 1. 29751 1. 25603	1. 52389 1. 55573 1. 54175 1. 48566 1. 40258 1. 31004 1. 22392 1. 15483 1. 10920	log b ₂ ⁽⁶⁾ 1. 39853 1. 43295 1. 41781 1. 35740 1. 26723 1. 16667 1. 07276 0. 99721 0. 94720	1. 2624 1. 2993 1. 2832 1. 2178 1. 1207 1. 0116 0. 9098 0. 8274 0. 7730	1. 1171 1. 1572 1. 1395 1. 0694 0. 9646 0. 8472 0. 7370 0. 6478 0. 5885	0. 9644 1. 0067 0. 9885 0. 9120 0. 8011 0. 6742 0. 5559 0. 4595 0. 3959
(1) (2) (3) (4) (5) (6) (7) (8) (9)	1. 73225 1. 75959 1. 74758 1. 69964 1. 62881 1. 55073 1. 47868 1. 42134 1. 38369 1. 36806	log b ₂ ⁽⁴⁾ 163615 1. 66565 1. 65267 1. 60097 1. 52421 1. 43925 1. 36047 1. 29751 1. 25603 1. 23878	1. 52389 1. 55573 1. 54175 1. 48566 1. 40258 1. 31004 1. 22392 1. 15483 1. 10920 1. 09021	log b ₂ ⁽⁶⁾ 1. 39853 1. 43295 1. 41781 1. 35740 1. 26723 1. 16667 1. 07276 0. 99721 0. 94720 0. 92635	1. 2624 1. 2993 1. 2832 1. 2178 1. 1207 1. 0116 0. 9098 0. 8274 0. 7730 0. 7502	1. 1171 1. 1572 1. 1395 1. 0694 0. 9646 0. 8472 0. 7370 0. 6478 0. 5885 0. 5639	0. 9644 1. 0067 0. 9885 0. 9120 0. 8011 0. 6742 0. 5559 0. 4595 0. 3959 0. 3715
(1) (2) (3) (4) (5) (6) (7) (8) (9) (10)	1. 73225 1. 75959 1. 74758 1. 69964 1. 62881 1. 55073 1. 47868 1. 42134 1. 38369 1. 36806 1. 37518	log b ₂ ⁽⁴⁾ 1.*63615 1. 66565 1. 65267 1. 60097 1. 52421 1. 43925 1. 36047 1. 29751 1. 25603 1. 23878 1. 24664	1. 52389 1. 55573 1. 54175 1. 48566 1. 40258 1. 31004 1. 22392 1. 15483 1. 10920 1. 09021 1. 09886	log b ₂ ⁽⁶⁾ 1. 39853 1. 43295 1. 41781 1. 35740 1. 26723 1. 16667 1. 07276 0. 99721 0. 94720 0. 92635 0. 93585	1. 2624 1. 2993 1. 2832 1. 2178 1. 1207 1. 0116 0. 9098 0. 8274 0. 7730	1. 1171 1. 1572 1. 1395 1. 0694 0. 9646 0. 8472 0. 7370 0. 6478 0. 5885	0. 9644 1. 0067 0. 9885 0. 9120 0. 8011 0. 6742 0. 5559 0. 4595 0. 3959 0. 3715 0. 3808
(1) (2) (3) (4) (5) (6) (7) (8) (9) (10) (11)	log b ₂ ⁽³⁾ 1. 73225 1. 75959 1. 74758 1. 69964 1. 62881 1. 55073 1. 47868 1. 42134 1. 38369 1. 36806 1. 37518 1. 40466	log b ₂ ⁽⁴⁾ 1.*63615 1. 66565 1. 65267 1. 60097 1. 52421 1. 43925 1. 36047 1. 29751 1. 25603 1. 23878 1. 24664 1. 27914	1. 52389 1. 55573 1. 54175 1. 48566 1. 40258 1. 31004 1. 22392 1. 15483 1. 10920 1. 09021 1. 09886 1. 13464	log b ₂ ⁽⁶⁾ 1. 39853 1. 43295 1. 41781 1. 35740 1. 26723 1. 16667 1. 07276 0. 99721 0. 94720 0. 92635 0. 93585 0. 97507	1. 2624 1. 2993 1. 2832 1. 2178 1. 1207 1. 0116 0. 9098 0. 8274 0. 7730 0. 7502 0. 7606 0. 8031	1. 1171 1. 1572 1. 1395 1. 0694 0. 9646 0. 8472 0. 7370 0. 6478 0. 5885 0. 5639 0. 5746 0. 6216	0. 9644 1. 0067 0. 9885 0. 9120 0. 8011 0. 6742 0. 5559 0. 4595 0. 3959 0. 3715 0. 3808 0. 4306
(1) (2) (3) (4) (5) (6) (7) (8) (9) (10) (11) (12)	1. 73225 1. 73225 1. 75959 1. 74758 1. 69964 1. 62881 1. 55073 1. 47868 1. 42134 1. 38369 1. 36806 1. 37518 1. 40466 1. 45477	log b ₂ ⁽⁴⁾ 1.*63615 1. 66565 1. 65267 1. 60097 1. 52421 1. 43925 1. 36047 1. 29751 1. 25603 1. 23878 1. 24664 1. 27914 1. 33424	1. 52389 1. 55573 1. 54175 1. 48566 1. 40258 1. 31004 1. 22392 1. 15483 1. 10920 1. 09021 1. 09886	$\log b_{\frac{7}{2}}^{(6)}$ 1. 39853 1. 43295 1. 41781 1. 35740 1. 26723 1. 16667 1. 07276 0. 99721 0. 94720 0. 92635 0. 93585 0. 97507 1. 04135	1. 2624 1. 2993 1. 2832 1. 2178 1. 1207 1. 0116 0. 9098 0. 8274 0. 7730 0. 7502 0. 7606	1. 1171 1. 1572 1. 1395 1. 0694 0. 9646 0. 8472 0. 7370 0. 6478 0. 5885 0. 5639 0. 5746	0. 9644 1. 0067 0. 9885 0. 9120 0. 8011 0. 6742 0. 5559 0. 4595 0. 3959 0. 3715 0. 3808 0. 4306 0. 5180
(1) (2) (3) (4) (5) (6) (7) (8) (9) (10) (11) (12) (13)	log b ₂ ⁽³⁾ 1. 73225 1. 75959 1. 74758 1. 69964 1. 62881 1. 55073 1. 47868 1. 42134 1. 38369 1. 36806 1. 37518 1. 40466 1. 45477 1. 52168	log b ₂ ⁽⁴⁾ 1.*63615 1. 66565 1. 65267 1. 60097 1. 52421 1. 43925 1. 36047 1. 29751 1. 25603 1. 23878 1. 24664 1. 27914 1. 33424 1. 40753	1. 52389 1. 55573 1. 54175 1. 48566 1. 40258 1. 31004 1. 22392 1. 15483 1. 10920 1. 09021 1. 09886 1. 13464 1. 19518	log b ₂ ⁽⁶⁾ 1. 39853 1. 43295 1. 41781 1. 35740 1. 26723 1. 16667 1. 07276 0. 99721 0. 94720 0. 92635 0. 93585 0. 97507	1. 2624 1. 2993 1. 2832 1. 2178 1. 1207 1. 0116 0. 9098 0. 8274 0. 7730 0. 7502 0. 7606 0. 8031 0. 8756	1. 1171 1. 1572 1. 1395 1. 0694 0. 9646 0. 8472 0. 7370 0. 6478 0. 5885 0. 5639 0. 5746 0. 6216 0. 6999	0. 9644 1. 0067 0. 9885 0. 9120 0. 8011 0. 6742 0. 5559 0. 4595 0. 3959 0. 3715 0. 3808 0. 4306
(1) (2) (3) (4) (5) (6) (7) (8) (9) (10) (11) (12)	1. 73225 1. 73225 1. 75959 1. 74758 1. 69964 1. 62881 1. 55073 1. 47868 1. 42134 1. 38369 1. 36806 1. 37518 1. 40466 1. 45477	log b ₂ ⁽⁴⁾ 1.*63615 1. 66565 1. 65267 1. 60097 1. 52421 1. 43925 1. 36047 1. 29751 1. 25603 1. 23878 1. 24664 1. 27914 1. 33424	1. 52389 1. 55573 1. 54175 1. 48566 1. 40258 1. 31004 1. 22392 1. 15483 1. 10920 1. 09021 1. 09886 1. 13464 1. 19518 1. 27541	log b ₂ ⁽⁶⁾ 1. 39853 1. 43295 1. 41781 1. 35740 1. 26723 1. 16667 1. 07276 0. 99721 0. 94720 0. 92635 0. 93585 0. 97507 1. 04135 1. 12896	1. 2624 1. 2993 1. 2832 1. 2178 1. 1207 1. 0116 0. 9098 0. 8274 0. 7730 0. 7502 0. 7606 0. 8031 0. 8756 0. 9707	1. 1171 1. 1572 1. 1395 1. 0694 0. 9646 0. 8472 0. 7370 0. 6478 0. 5885 0. 5639 0. 5746 0. 6216 0. 6999 0. 8032	0. 9644 1. 0067 0. 9885 0. 9120 0. 8011 0. 6742 0. 5559 0. 4595 0. 3959 0. 3715 0. 3808 0. 4306 0. 5180 0. 6268
(1) (2) (3) (4) (5) (6) (7) (8) (9) (10) (11) (12) (13) (14)	log b ₂ ⁽³⁾ 1. 73225 1. 75959 1. 74758 1. 69964 1. 62881 1. 55073 1. 47868 1. 42134 1. 38369 1. 36806 1. 37518 1. 40466 1. 45477 1. 52168 1. 59838	log b ₂ ⁽⁴⁾ 1.*63615 1. 66565 1. 65267 1. 60097 1. 52421 1. 43925 1. 36047 1. 29751 1. 25603 1. 23878 1. 24664 1. 27914 1. 33424 1. 40753 1. 49114	1. 52389 1. 55573 1. 54175 1. 48566 1. 40258 1. 31004 1. 22392 1. 15483 1. 10920 1. 09021 1. 09886 1. 13464 1. 19518 1. 27541 1. 36661	log b ₂ ⁽⁶⁾ 1. 39853 1. 43295 1. 41781 1. 35740 1. 26723 1. 16667 1. 07276 0. 99721 0. 94720 0. 92635 0. 93585 0. 97507 1. 04135 1. 12896 1. 22819	1. 2624 1. 2993 1. 2832 1. 2178 1. 1207 1. 0116 0. 9098 0. 8274 0. 7730 0. 7502 0. 7606 0. 8031 0. 8756 0. 9707 1. 0784	1. 1171 1. 1572 1. 1395 1. 0694 0. 9646 0. 8472 0. 7370 0. 6478 0. 5885 0. 5639 0. 5746 0. 6216 0. 6999 0. 8032 0. 9192	0. 9644 1. 0067 0. 9885 0. 9120 0. 8011 0. 6742 0. 5559 0. 4595 0. 3959 0. 3715 0. 3808 0. 4306 0. 5180 0. 6268

Putting

 $\left[\mathbf{1}-2\mathbf{b}\cos\left(\epsilon+\mathbf{Q}\right)+\mathbf{b}^{2}\right]^{-\frac{n}{2}}=\frac{\mathbf{I}}{2}B_{\frac{n}{2}}^{(0)}+B_{\frac{n}{2}}^{(1)}\cos\left(\epsilon+\mathbf{Q}\right)+B_{\frac{n}{2}}^{(2)}\cos\,2\,\left(\epsilon+\mathbf{Q}\right)+\ \cdot \ \cdot \ \cdot$ it will suffice to compute the $B_{\frac{n}{2}}^{(i)}$ by the following formulæ:

$$\begin{split} \log\left(\frac{1}{2}B_{\frac{1}{8}}^{(0)}\right) &= \frac{1}{4}Mb^{2} & \log\left(\frac{1}{2}B_{\frac{3}{2}}^{(0)}\right) = \frac{9}{4}Mb^{2} & \log\left(\frac{1}{2}B_{\frac{3}{2}}^{(0)}\right) = 0 & \log\left(\frac{1}{2}B_{\frac{1}{8}}^{(0)}\right) = 0 \\ B_{\frac{1}{8}}^{(1)} &= b & B_{\frac{3}{8}}^{(1)} = 3b & B_{\frac{3}{2}}^{(1)} = 5b & B_{\frac{1}{8}}^{(1)} = 7b \\ B_{\frac{1}{8}}^{(2)} &= \frac{3}{8}b^{2} & B_{\frac{2}{3}}^{(2)} = \frac{15}{4}b^{3} \end{split}$$

Then, if we put θ for $Q - \varepsilon$, and

$$c_{\frac{n}{2}}^{(i)} = \frac{1}{2} \mathbf{N}^{n} \mathbf{B}_{\frac{n}{2}}^{(i)} \cos \, 2i \mathbf{Q} \qquad \qquad \mathbf{s}_{\frac{n}{2}}^{(i)} = \frac{1}{2} \mathbf{N}^{n} \mathbf{B}_{\frac{n}{2}}^{(i)} \sin \, 2i \mathbf{Q}$$

and, for convenience, omit everywhere the subscript $\frac{n}{2}$ from the quantities b and c, according as 1 or 3 or 5 or 7 is substituted for n, we have the development of $\frac{\mathbf{a}'}{\Delta}$ or $\left(\frac{\mathbf{a}'}{\Delta}\right)^3$ or $\left(\frac{\mathbf{a}'}{\Delta}\right)^5$ or $\left(\frac{\mathbf{a}'}{\Delta}\right)^7$ given by the following series, the law of which is easily recognized:

$$\begin{split} &\frac{1}{2}b^{(0)}c^{(0)} + b^{(1)}c^{(1)} + b^{(2)}c^{(2)} \\ &+ \left[b^{(1)}c^{(0)} + \left(b^{(0)} + b^{(2)}\right)c^{(1)} + \left(b^{(1)} + b^{(3)}\right)c^{(2)}\right]\cos\theta \\ &+ \left[\qquad \left(b^{(0)} - b^{(2)}\right)s^{(1)} + \left(b^{(1)} - b^{(3)}\right)s^{(2)}\right]\sin\theta \\ &+ \left[b^{(2)}c^{(0)} + \left(b^{(1)} + b^{(3)}\right)c^{(1)} + \left(b^{(0)} + b^{(4)}\right)c^{(2)}\right]\cos2\theta \\ &+ \left[\qquad \left(b^{(1)} - b^{(3)}\right)s^{(1)} + \left(b^{(0)} - b^{(4)}\right)s^{(2)}\right]\sin2\theta \\ &+ \left[b^{(3)}c^{(0)} + \left(b^{(2)} + b^{(4)}\right)c^{(1)} + \left(b^{(1)} + b^{(5)}\right)c^{(2)}\right]\cos3\theta \\ &+ \left[\qquad \left(b^{(2)} - b^{(4)}\right)s^{(1)} + \left(b^{(1)} - b^{(5)}\right)s^{(2)}\right]\sin3\theta \end{split}$$

If we put

$$k_{i} \cos K_{i} = b^{(i)}c^{(0)} + (b^{(i-1)} + b^{(i+1)})c^{(1)} + (b^{(i-2)} + b^{(i+2)})c^{(2)}$$

$$k_{i} \sin K_{i} = (b^{(i-1)} - b^{(i+1)})s^{(1)} + (b^{(i-2)} - b^{(i+2)})s^{(2)}$$

 k_i will not differ much from $b^{(i)}$, and K_i will be a small positive or negative angle. The terms having $c^{(1)}$ and $c^{(2)}$ as factors are much smaller than $b^{(i)}c^{(0)}$, and the union of the terms can be made with addition and subtraction logarithms: when these do not give sufficiently accurate results, as in the cases where $\log k_i$ must have more than seven decimals, the following approximate formulæ can be used with advantage: x being very small, we have nearly

$$\log (1+x) = \frac{Mx}{\sqrt{1+x}} \qquad \log (1-x) = -\frac{Mx}{\sqrt{1-x}}$$

Our series now takes the form

$$\sum k_i \cos(i\theta - K_i)$$

or, restoring for θ its value $Q - \varepsilon$,

$$\sum_{i} \{k_i \cos [i(\mathbf{Q} - g') - \mathbf{K}_i] \cos i(g' - \varepsilon) + k_i \sin [i(\mathbf{Q} - g') - \mathbf{K}_i] \sin i(g' - \varepsilon) \}$$

Let us put

$$\mathbf{A}_{i}^{(s)} = \frac{\mathbf{I}}{8}k_{i}\cos\left[i(\mathbf{Q} - g') - \mathbf{K}_{i}\right] \qquad \qquad \mathbf{A}_{i}^{(s)} = -\frac{\mathbf{I}}{8}k_{i}\sin\left[i(\mathbf{Q} - g') - \mathbf{K}_{i}\right]$$

This division by 8 is made in order to save the constant division by these integers which occurs in the quadratures to follow. For this purpose $\log 8$ has been subtracted from $\log N^n$.

The form of our series is now

$$\sum_{i} \left[\mathbf{A}_{i}^{(c)} \cos i(g' - \varepsilon) + \mathbf{A}_{i}^{(s)} \sin i(g' - \varepsilon) \right]$$

The values of

$$\delta \log k_i = \log k_i - \log \left(b^{(i)}c^{(0)}\right)$$

and K_i follow. In the case of the former the numbers given are units of the last decimal place employed; the small figure at the top of the column indicates the order.

25 AST—3

The values for the development of $\frac{\mathbf{a}'}{\triangle}$ are:

	$\delta \log k_0$	$\delta \log k_1$	$\delta \log k_2$	δ lo	g k ₃	δlo	g k4	δ log k	$\delta \log k_6$	$\delta \log k_7$	$\delta \log k_8$
	10	10	10		,	9	,	8	7	6	5
(0)	-390183	-2436623	1793306	—16	7087	I	1998	—1592	4 -1576	-156	—16
(1)	406799	2504487	1845594	17	2035	16	6830	1640	1623	161	16
(2)	126309	— 781866	— 57733 ⁸	<u> </u>	3765	— <u>5</u>	2127	— 512	4 - 506	- 50	— 5
(3)	+227251	+1443713	+1060737	+ 9	8785	+ 9	5 75 3	+ 941	1 + 931	+ 92	+ 9
(4)	404078	2666780	1955126	1	1809	17	6117	1730	2 1711	170	17
(5)	326817	2254312	1645886	15	2880	14	8005	1453	5 1437	143	14
(6)	+ 85703	+ 617318	+ 447659		1573		0231	+ 395	0 + 391	+ 39	+ 4
(7)	-172497	-1285014	— 93 27 93	8	6452	_ 8	3607	820	1	80	- 8
(8)	330048	2518043	1821824	l	8818	16	3226	1601	7 1583	157	16
(9)	329268	2536963	1834082	i .	9912		4263	1611		157	16
(10)	—1745 98		— 969398	— 8	9782	- 8	6795	- 851	6 — 841	83	8
(11)	+ 72156	,	+ 392696	+ 3	643 1		5235	+ 345	8 + 342	+ 34	+ 3
(12)	300855	2196182	+1595893	14	8012	14	3183	1405	4 1389	138	14
(13)	381342	2674751	1950814		1099	17	5282	1721	1701	169	17
(14)	+229910		+1128914	+10		+10	1659	+ 998	6 + 988	+ 98	+10
(15)	— 99 5 93	— 641048	— 4 7 1966	— 4.	3894	- 4	2530	— 417	9 - 413	— 41	— 4
	K,	K ₂	K ₃		K.	4]	ζ _δ	K ₆	K ₇	K ₈
	//	"	"		//	,		,,	//	//	//
(0)	+ 44.7526	+27.93535	+24. 32	14	+22.	6863	+21	745	+21.15	+20.7	+20
(1)	— 39. 4886	-24.62136	-21.42	35	-19.	9755	—19	. 142	—18. 6 1	—1 8. 2	—18
(2)	95. 0603	59. 37668	51.65	95	48.	1724	46	. 166	44. 88	44. 0	44
(3)	84.6114	53. 04022	46. 17	33	43.	0825	41	. 305	40. 12	39⋅ 3	39
(4)	— 1 9. 4464	-12. 23565	—10.66	51	 9.	9605	<u> </u>	. 556	9. 28	9. I	9
(5)	+ 56.3853	+35.57332	+31.06		+29.	0403	+27	. 882	+27.09	+26.5	+26
(6)	99. 6608	62. 96929	55. 08.		51.	5518	49	. 528	48. 19	47.2	47
(7)	90. 5860	57-27495	50. 18	12	47.	0014	45	. 180	44. 02	43.2	43
(8)	+ 36.7892	+23. 27107	+20.40	96	+19.		+18	. 392	+17.93	+17.6	+17
(9)	— 34. 6673	-21.94106	—19. 24	-	 18.	0423	-17	. 352	— 16. 92	16.6	—16
(10)	89. 7918	56. 86664	49.87	00	46.	7373	44	945	43. 80	43.0	43
(11)	1 01.0218	64. 00032	56.07	09	52.	5251	50	497	49. 18	48. 2	48
(12)	5 9. 6880	-37. 79195	—33. 06.		<u>30.</u>	9519	29	. 743	—28. 92	28. 3	—28
(13)	+ 15.7935	+ 9.97826	+ 8.71	72	+ 8.	1530	+ 7	. 830	+ 7.61	+ 7.5	+7
(14)	83. 0739	52. 28706	45.61	63	42.	6220	40	. 903	39.75	39.0	39
(15)	+ 97.3145	+60.96963	+53.130	00	+ 49.	5953	+47	. 563	+46. 24	+45.3	+45

The values for the development of $\left(\frac{a'}{\triangle}\right)^3$ are:

	$\delta \log k_0$	$\delta \log k_1$	$\delta \log k_2$	$\delta \log k_3$	$\delta \log k_4$	δ1	og ‰	δ log	k_6	$\delta \log k_7$	$\delta \log k_8$
	8	8	8	8	7		7	6		6	5
(0)	-29535	—38906	-41121	-4214 6	-4275	_	4314	-43	35	437	-44
(1)	30710	40185	42429	43472	4408		4450	44	18	450	45
(2)	9551	—12534	—13247	—1 3577	—1377	-	1389	-14	ţo	-141	-14
(3)	+17248	+22904	+24234	+24851	+2520	+	2545	+25	56	+257	+26
(4)	30886	41784	44347	45527	4621	.	4666	47	70	472	47
(5)	25169	34807	37061	38085	3868		3908	39	94	396	40
(6)	+ 6642	+ 9388	+10016	+10304	+1047	+	1058	+10	7	+108	+11
(7)	-13455	-19372	-20737	—21 361	-2172	-	2196	-22	15	-222	22
(8)	25831	37661	40367	41603	4233		4278	43	31	433	43
(9)	25807	37829	40575	41828	4254	.	4301	43	33	435	44
(10)	13677	-19999	-21451	-22113	2249	-	2275	22	9	—23o	-23
(11)	+ 5631	+ 8151	+ 8722	+ 8984	+ 914	+	923	+ 9	93	十 93	+ 9
(12)	23382	33296	35586	36634	3724		3764	37	79	381	38
(13)	29450	41079	43786	45027	4575		4621	46	55	467	47
(14)	+17623	+24043	+25541	+26226	+2664	+:	2690	+27	7 I	+272	+27
(15)	- 75 86	-10143	-10751	-11031	1120	-	1130	11	4	-115	-12
	K ₁	\mathbb{K}_2	K ₃	K4	K	5]	ζ ₆		K ₇	K ₈
	"	//	//			//		//		,,	//
(0)	+29.449	+37.646	+ 41.712				+	47. I	+	- 48.0	+ 48
(1)	25. 781	—32. 995	36. 580	— 38. <u>·</u>		1	_	41.3		- 42. I	— 43
(2)	62. 288	79.715	88. 358	93.	58 97	. IO	ł .	99.7		101.6	103
(3)	56.210	71.845	79.563		22 87	· 34		89. 7		91.4	93
(4)	-13.178	<u>16.802</u>	— 18. 579	19.0	55 — 20	. 36	_	20.9		- 21.3	— 2I
(5)	+39.025	+49.603	+ 54.760				+	61.5	+	- 62.7	+ 63
(6)	70. 295	89.066	98. 166	103.	59 107	. 20	1	10.0		112.0	113
(7)	64. 837	81.928	90. 186	1		. 35	1	00.9		102.7	104
(8)	+26.582	+33.530	+ 36.880	+ 38.8	1			41.2	+	- 42.0	+ 42
(9)	25. 147	-31.701	_ 34.858	1	I '		_	39.0	_	- 39.8	- 40
(10)	65.022	82, 022	90. 208	95.0		. 28	1	00, 8		102.7	104
(11)	72. 622	91.755	100. 984	106. 4	16 , 110	. 12	I	12.9		114.9	116
(12)	42. 367	-53.654	— 59. 114		ŀ	. 52		66.2	_	- 67.4	— 68
(13)	+11.016	+13.988	+ 15.433		1	-	+	17.3		- 17.6	+ 18
(14)	56.760	72. 260	79.850	1 '	12 87	. 48		89. 7	·	91.4	92
(15)	+65. 114	+83.088	+ 91.954	1				03.5	+	-105.4	+107

The values for the development of $\left(\frac{a'}{\triangle}\right)^s$ are:

	$\delta \log k_0$	$\delta \log k_1$	$\delta \log k_2$	$\delta \log k_3$	$\delta \log k_4$	$\delta \log k_5$	$\delta \log k_6$
	7	7	7	7	7	7	7
(0)	 5939	6209	6444	—6593	-6717	-6812	6887
(1)	6158	6425	6648	6811	6936	7032	7108
(2)	-1919	-2003	-2074	2126	-2164	2194	-2219
(3)	+3479	+3644	+3776	+3880	+3953	+4010	+4057
(4)	6280	6615	6882	7 076	7221	7331	7421
(5)	5164	5477	5718	5 895	6023	6123	6200
(6)	+1374	+1467	+1538	+1588	+1626	+1654	+1677
(7)	-2805	-3014	-3171	-3282	-3363	-3424	-3463
(8)	5409	5837	6154	63 7 9	6540	6662	6758
(9)	5415	5855	6177	6407	6573	6695	6792
(10)	2868	—3 098	-3268	—3388	3474	-3540	-3591
(11)	+1176	+1264	+1332	+1379	+1413	+1439	+1460
(12)	4852	5194	5453	5637	5772	5875	5954
(13)	6064	6449	6744	6957	7116	7235	7 326
(14)	+3599	+3796	+3955	+4073	+4157	+4223	+4275
(15)	-1536	—1613	—1674	-1720	1754	—1780	-1800
	K ₁	K ₂	K ₃	B	<u> </u>	К5	\mathbf{K}_{6}
	//	"	,	,,	//	//	//
(0)	+20°.74	+34.52	+ 43	. 90 +	50.70	+ 55.79	+ 59.76
(1)	—18. o7	—30. II	_ 38	. 36 —	44- 33	- 48.83	— 52.35
(2)	43. 78	72.85	92	e. 8o	107. 27	117. 97	126, 44
(3)	39. 98	66. 38	84	. 10	96. 98	106.63	114. 13
(4)	— 9. 51	-15.65	- 19	81	22.80	- 25.03	- 26.75
(5)	+28.58	+46.79	+ 59	o. 03 +-	67. 72	+ 74.20	+ 79.18
(6)	52. 14	85.00	106	5. 88	122. 34	133.78	142.60
(7)	48. 58	78. 92	98	3. 97	113.05	123.51	131.49
(8)	+20.04	+32.49	+ 40	. 66 +	46.41	+ 50.64	+ 53.90
(9)	19.02	30. 79	— 38	B. 5 3 —	43.94	— 47 . 93	— 50.99
(10)	49. 13	79. 56	99	. 56	113.61	123. 94	131.82
(11)	54. 64	88. 58	1	L.	126. 80	138.42	147.30
(12)	— 31.61	-51.38	— 64	- 53	73.82	— 80. 70	85.96
(13)	+ 8.12	+13.25	+ 16	5.70 +	19.15	+ 20.96	+ 22.36
(14)	41.18	67 . 66	85	5. 56	98. 30	117.82	115. 21
(15)	+46.45	+76.88	+ 97	· 57 +	112.40	+123.54	+132.12

The values for the development of $\left(\frac{a'}{\triangle}\right)^7$ are:

	1			1	1	1	
	$\delta \log k_{\rm o}$	$\delta \log k_1$	$\delta \log k_2$	$\delta \log k_3$	$\delta \log k_4$	$\delta \log k_{\scriptscriptstyle 5}$	$\delta \log k_6$
	5	5	Б	5	5	5	Б
(0)	—89	77	80	83	84	85	—86
(1)	-93	<u>—</u> 80	84	87	—88	89	90
(2)	-29	-25	-26	-26	26	-26	27
(3)	+52	+46	+47	+47	+48	+48	+49
(4)	+94	+82	+86	+87	+90	+91	+92
(5)	+78	+69	+71	+72	+74	+75	+76
(6)	+20	+18	+19	+20	+20	+21	+21
(7)	—42	-37	4 0	— 41	4I	-42	-42
(8)	—81	—73	77	<u>_80</u>	·8r	83	-84
(9)	—81	— 74	—77	<u>_80</u>	81	83	84
(10)	—43	38	41	-42	43	-44	45
(11)	+18	+16	+16	+16	+17	+17	+17
(12)	+73	+65	+68	+70	+72	十73	+74
(13)	+91	+80	+84	+-86	+89	+.90	+92
(14)	+54	+47	+50	+51	+52	+.53	+53
(15)	22	-20	-21	-21	21	2I	—21
<u>'</u>		1.	1	l .	1	1	1
		1			1		
	K1	K ₂	K ₃	K	4	Kδ	K ₆
	K ₁	K ₂	"		4	К5	K ₆
(0)	+16	// + 41	+ 44	1 +	58	+ 67	// + 72
(1)	"	// + 41 - 35	+ 44 - 38	+ + -	// 58 50	+ 67 - 58	// + 7 ² — 6 ²
(1) (2)	// +16 -16 -39	// + 41 - 35 - 87	+ 44 - 38 - 99	+ + 313	// 58 50	+ 67 - 58 -140	// + 72 - 62 -151
(1) (2) (3)	// +16 -16 -39 -38	+ 41 - 35 - 87 - 77	+ 44 - 33 - 93 - 82	+ + 3 1 3 1	58 50 122	" + 67 - 58 -140 128	+ 72 - 62 -151 -138
(1) (2) (3) (4)	// +16 -16 -39 -38 -7	+ 41 - 35 - 87 - 77 - 18	+ 44 33 93 82 20	+ + + 3 1 - 1 - 1 - 1 - 1 - 1 - 1 - 1 - 1	77 58 50 122 111 26	+ 67 - 58 -140 -128	// + 72 - 62 - 151 - 138 - 32
(1) (2) (3) (4) (5)	" +16 -16 -39 -38 -7 +25	+ 41 - 35 - 87 - 77 - 18 + 55	+ 44 33 93 86 26 + 59	+ + + 3 1 + -	58 50 122 111 26 78	+ 67 - 58 -140 -128 - 30 + 90	// + 72 - 62 151 138 32 + 97
(1) (2) (3) (4) (5) (6)	+16 -16 -39 -38 -7 +25 +41	+ 41 - 35 - 87 - 77 - 18 + 55 + 102	+ 44 33 93 82 20 +- 59 +- 109	+ + + + + + + + + + + + + + + + + + +	58 50 122 111 26 78	+ 67 - 58 -140 -128 - 30 + 90 +160	// + 72 - 62 151 138 32 + 97 +-171
(1) (2) (3) (4) (5) (6) (7)	// +16 -16 -39 -38 -7 +25 +41 +40	+ 41 - 35 - 87 - 77 - 18 + 55 + 102 + 92	+ 44 - 33 - 93 - 86 - 20 + 59 + 109	+ + + + + + + + + + + + + + + + + + +	58 50 122 111 26 78 139	// + 67 - 58 -140 128 30 + 90 +160 +150	// + 72 - 62 151 138 32 + 97 +-171 +-161
(1) (2) (3) (4) (5) (6) (7) (8)	" +16 -16 -39 -38 -7 +25 +41 +40 +16	+ 41 - 35 - 87 - 77 - 18 + 55 + 102 + 92 + 39	+ 44 - 33 - 93 - 84 - 20 + 59 + 109 + 4	+ + + + + + + + + + + + + + + + + + +	77 58 50 122 111 26 78 139 130 53	// + 67 - 58 -140 128 30 + 90 +160 +150 + 61	// + 72 - 62 151 138 32 + 97 +-171 +-161 +- 65
(1) (2) (3) (4) (5) (6) (7) (8) (9)	" +16 -16 -39 -38 -7 +25 +41 +40 +16 -15	+ 41 - 35 - 87 - 77 - 18 + 55 + 102 + 92 + 39 - 36	+ 44 - 33 - 93 - 82 - 109 + 109 + 44 - 33	+ + + + + + + + + + + + + + + + + + +	77 58 50 122 111 26 78 139 130 53 51	" + 67 - 58 - 140 - 128 - 30 + 90 + 160 + 150 + 61 - 59	// + 72 - 62 - 151 - 138 - 32 + 97 + 171 + 161 + 65 - 64
(1) (2) (3) (4) (5) (6) (7) (8) (9) (10)	" +16 -16 -39 -38 -7 +25 +41 +40 +16 -15 -39	+ 41 - 35 - 87 - 77 - 18 + 55 + 102 + 39 - 36 - 95	+ 44 - 33 - 93 - 82 - 20 + 59 + 10 + 44 - 39 - 100	+ + + + + + + + + + + + + + + + + + +	77 58 50 122 111 26 78 139 130 53 51 130	"" + 67 - 58 -140128 30 + 90 +160 +150 + 61 59148	+ 72 - 62 - 151 - 138 - 32 + 97 + 171 + 161 + 65 - 64 - 158
(1) (2) (3) (4) (5) (6) (7) (8) (9) (10) (11)	" +16 -16 -39 -38 -7 +25 +41 +40 +16 -15 -39 -44	+ 41 - 35 - 87 - 77 - 18 + 55 + 102 + 39 - 36 - 95 - 104	+ 44 - 33 - 93 - 82 - 20 + 59 + 10 + 44 - 39 - 100 - 11	+ + + + + + + + + + + + + + + + + + +	77 58 50 122 111 26 78 139 130 53 51 130	"" + 67 - 58 - 140 - 128 - 30 + 90 + 160 + 150 + 61 - 59 - 148 - 167	+ 72 - 62 - 151 - 138 - 32 + 97 + 171 + 161 + 65 - 64 - 158 - 180
(1) (2) (3) (4) (5) (6) (7) (8) (9) (10) (11) (12)	// +16 -16 -39 -38 -7 +25 +41 +40 +16 -15 -39 -44 -25	+ 41 - 35 - 87 - 77 - 18 + 55 + 102 + 92 + 39 - 36 - 95 - 104 - 61	+ 44 - 33 - 93 - 82 - 20 + 59 + 10 + 44 - 39 - 100 - 11 - 69	+ + + + + + + + + + + + + + + + + + +	77 558 550 122 1111 226 78 139 130 1553 551 130 1445 84	"" + 67 - 58 -140128 30 + 90 +160 +150 + 61 59148	+ 72 - 62 - 151 - 138 - 32 + 97 + 171 + 161 + 65 - 64 - 158 - 180 - 103
(1) (2) (3) (4) (5) (6) (7) (8) (9) (10) (11) (12) (13)	" +16 -16 -39 -38 -7 +25 +41 +40 +16 -15 -39 -44 -25 +6	+ 41 - 35 - 87 - 77 - 18 + 55 + 102 + 92 + 39 - 36 - 95 - 104 - 61 + 15	+ 44 - 33 - 93 - 82 - 20 + 59 + 10 + 44 - 39 - 100 - 11 - 69 + 19	+ + + + + + + + + + + + + + + + + + +	77 58 50 122 111 26 78 139 130 53 51 130 145 84 23	// + 67 - 58 -140 128 30 + 90 +160 +150 + 61 59 148 167 97 + 26	// + 72 - 62
(1) (2) (3) (4) (5) (6) (7) (8) (9) (10) (11) (12)	// +16 -16 -39 -38 -7 +25 +41 +40 +16 -15 -39 -44 -25	+ 41 - 35 - 87 - 77 - 18 + 55 + 102 + 92 + 39 - 36 - 95 - 104 - 61	+ 44 - 33 - 93 - 82 - 20 + 59 + 10 + 44 - 39 - 100 - 11 - 69	+ + + + + + + + + + + + + + + + + + +	77 58 50 122 111 26 78 139 130 153 51 130 145 84 23 112	"" + 67 - 58 -140128 30 + 90 +160 +150 + 61 59148	+ 72 - 62 - 151 - 138 - 32 + 97 + 171 + 161 + 65 - 64 - 158 - 180 - 103

Then in the expansion of $\frac{\mathbf{a}'}{\triangle}$ we have:

	$\mathbf{A_0}$	$\mathbf{A_{1}^{(c)}}$	$\mathbf{A}_1^{(s)}$	$\mathbf{A_2^{(c)}}$	$\mathbf{A}_2^{(s)}$	A ₃ ^(e)
	10	10	10	11	11	10
(0)	1450228368	+ 202026552	— 849063514	— 34099 5 8446	- 1718843096	— 118646864
(1)	1463004962	165534743	871976671	3640004664	1434802629	101473601
(2)	1457425396	127235650	872119792	3710027586	1108633113	79125332
(3)	1435004518	96594253	850441063	3615257970	834129533	59175347
(4)	1401552842	79393961	814422998	3410294766	671741875	46834975
(5)	1364376712	76442920	773386511	3163570196	630325000	42931597
(6)	1329783024	85298720	734687422	2923596837	686107798	45577632
(7)	1302096579	102538880	702712207	2714169129	807553772	52363664
(8)	1283824520	125058969	679625103	2544173764	968420038	61418720
(9)	1276200852	150383334	666455050	2417898623	1150402242	71594188
(10)	1279640398	176449375	663868971	2341401552	1341099104	82325461
(11)	1293937512	201197979	672502830	2325293606	1530361315	93402992
(12)	1318180590	222136767	692842956	2384491313	1705621583	104636227
(13)	1350401285	236036572	724598535	2533891037	1846379573	115315760
(14)	1387058565	239080805	765531034	2777564222	1920143086	123519532
(15)	1422671462	+ 227952301	810089284	<u> </u>	<u> </u>	125827915
S	1.0907693703	+1256680799	-6072161790	-23501508486	-10120609693	662084743
S/	1. 0907693882	+1256680982	-6072162151	23501511907	-10120612155	662085064
		1	1	1		1
	A ₃ ^(*)	A ₄ ^(c)	A ₄ ⁽⁸⁾	$\mathbf{A}_{5}^{(c)}$	$\mathbf{A}_{5}^{(a)}$	A ₆ (c)
ļ	10	11	11	10	10	9
(0)	10 +140789048	+ 552656433	+ 746681339	+ 44256400	18909459	9 430248
(1)	10 +140789048 160676350	11 + 552656433 705980548	+ 746681339 659132055	+ 44256400 40670344	10 — 18909459 29771961	9 430248 1149843
(I) (2)	10 +140789048 160676350 169946161	+ 552656433 705980548 793843408	+ 746681339 659132055 521340176	10 + 44256400 40670344 32814529	10 — 18909459 29771961 36931974	9 430248 1149843 1682626
(1) (2) (3)	10 +140789048 160676350 169946161 167128543	+ 552656433 705980548 793843408 796919804	+ 746681339 659132055 521340176 388716382	+ 44256400 40670344 32814529 24469122	18909459 29771961 36931974 38400170	- 430248 1149843 1682626 1848808
(1) (2) (3) (4)	10 +140789048 160676350 169946161 167128543 155942105	11 + 552656433 705980548 793843408 796919804 738727075	11 + 746681339 659132055 521340176 388716382 302828944	+ 44256400 40670344 32814529 24469122 18789498	10 18909459 29771961 36931974 38400170 35541528	9 430248 1149843 1682626 1848808 1719023
(1) (2) (3) (4) (5)	10 +140789048 160676350 169946161 167128543 155942105 141337426	+ 552656433 705980548 793843408 796919804 738727075 654118754	11 + 746681339 659132055 521340176 388716382 302828944 271278616	10 + 44256400 40670344 32814529 24469122 18789498 16451022	10 — 18909459 29771961 36931974 38400170 35541528 30740457	9 430248 1149843 1682626 1848808 1719023 1451923
(1) (2) (3) (4) (5) (6)	10 +140789048 160676350 169946161 167128543 155942105 141337426 126598317	+ 552656433 705980548 793843408 796919804 738727075 654118754 565439767	11 + 746681339 659132055 521340176 388716382 302828944 271278616 280608214	10 + 44256400 40670344 32814529 24469122 18789498 16451022 16560520	10 — 18909459 29771961 36931974 38400170 35541528 30740457 25512780	9 430248 1149843 1682626 1848808 1719023 1451923 1149523
(1) (2) (3) (4) (5) (6) (7)	10 +140789048 160676350 169946161 167128543 155942105 141337426 126598317 113095826	+ 552656433 705980548 793843408 796919804 738727075 654118754 565439767 481059746	+ 746681339 659132055 521340176 388716382 302828944 271278616 280608214 313840044	10 + 44256400 40670344 32814529 24469122 18789498 16451022 16560520 17979990	10 — 18909459 29771961 36931974 38400170 35541528 30740457 25512780 20396865	- 430248 1149843 1682626 1848808 1719023 1451923 1149523 847724
(1) (2) (3) (4) (5) (6) (7) (8)	10 +140789048 160676350 169946161 167128543 155942105 141337426 126598317 113095826 101197466	+ 552656433 705980548 793843408 796919804 738727075 654118754 565439767 481059746 402679958	+ 746681339 659132055 521340176 388716382 302828944 271278616 280608214 313840044 358400034	10 + 44256400 40670344 32814529 24469122 18789498 16451022 16560520 17979990 19894049	10 — 18909459 29771961 36931974 38400170 35541528 30740457 25512780 20396865 15494742	9 430248 1149843 1682626 1848808 1719023 1451923 1149523 847724 554261
(1) (2) (3) (4) (5) (6) (7) (8) (9)	10 +140789048 160676350 169946161 167128543 155942105 141337426 126598317 113095826 101197466 91076536	+ 552656433 705980548 793843408 796919804 738727075 654118754 565439767 481059746 402679958 331071140	+ 746681339 659132055 521340176 388716382 302828944 271278616 280608214 313840044 358400034 407325962	10 + 44256400 40670344 32814529 24469122 18789498 16451022 16560520 17979990 19894049 21886552	10 18909459 29771961 36931974 38400170 35541528 30740457 25512780 20396865 15494742 10854325	9 430248 1149843 1682626 1848808 1719023 1451923 1149523 847724 554261 273151
(1) (2) (3) (4) (5) (6) (7) (8) (9) (10)	10 +140789048 160676350 169946161 167128543 155942105 141337426 126598317 113095826 101197466 91076536 83150239	+ 552656433 705980548 793843408 796919804 738727075 654118754 565439767 481059746 402679958 331071140 268703826	+ 746681339 659132055 521340176 388716382 302828944 271278616 280608214 313840044 358400034 407325962 458447644	10 + 44256400 40670344 32814529 24469122 18789498 16451022 16560520 17979990 19894049 21886552 23891442	10 — 18909459 29771961 36931974 38400170 35541528 30740457 25512780 20396865 15494742 10854325 6610129	9 430248 1149843 1682626 1848808 1719023 1451923 1149523 847724 554261 273151 11412
(1) (2) (3) (4) (5) (6) (7) (8) (9) (10) (11)	10 +140789048 160676350 169946161 167128543 155942105 141337426 126598317 113095826 101197466 91076536 83150239 78272599	+ 552656433 705980548 793843408 796919804 738727075 654118754 565439767 481059746 402679958 331071140 268703826 220785424	11 + 746681339 659132055 521340176 388716382 302828944 271278616 280608214 313840044 358400034 407325962 458447644 513193884	10 + 44256400 40670344 32814529 24469122 18789498 16451022 16560520 17979990 19894049 21886552 23891442 26133786	10 18909459 29771961 36931974 38400170 35541528 30740457 25512780 20396865 15494742 10854325 6610129 3020832	9 430248 1149843 1682626 1848808 1719023 1451923 1149523 847724 554261 273151 11412 + 220900
(1) (2) (3) (4) (5) (6) (7) (8) (9) (10) (11) (12)	10 +140789048 160676350 169946161 167128543 155942105 141337426 126598317 113095826 101197466 91076536 83150239 78272599 77792910	+ 552656433 705980548 793843408 796919804 738727075 654118754 565439767 481059746 402679958 331071140 268703826 220785424 196036282	11 + 746681339 659132055 521340176 388716382 302828944 271278616 280608214 313840044 358400034 407325962 458447644 513193884 574685970	10 + 44256400 40670344 32814529 24469122 18789498 16451022 16560520 17979990 19894049 21886552 23891442 26133786 29039408	10 18909459 29771961 36931974 38400170 35541528 30740457 25512780 20396865 15494742 10854325 6610129 3020832 528111	9 - 430248 1149843 1682626 1848808 1719023 1451923 1149523 847724 554261 273151 - 11412 + 220900 407502
(1) (2) (3) (4) (5) (6) (7) (8) (9) (10) (11) (12) (13)	10 +140789048 160676350 169946161 167128543 155942105 141337426 126598317 113095826 101197466 91076536 83150239 78272599 77792910 83419434	+ 552656433 705980548 793843408 796919804 738727075 654118754 565439767 481059746 402679958 331071140 268703826 220785424 196036282 207275019	11 + 746681339 659132055 521340176 388716382 302828944 271278616 280608214 313840044 358400034 407325962 458447644 513193884 574685970 643902015	10 + 44256400 40670344 32814529 24469122 18789498 16451022 16560520 17979990 19894049 21886552 23891442 26133786 29039408 33019360	10 18909459 29771961 36931974 38400170 35541528 30740457 25512780 20396865 15494742 10854325 6610129 3020832 528111 + 112284	9 - 430248 1149843 1682626 1848808 1719023 1451923 1149523 847724 554261 273151 - 11412 + 220900 407502 513211
(1) (2) (3) (4) (5) (6) (7) (8) (9) (10) (11) (12) (13) (14)	10 +140789048 160676350 169946161 167128543 155942105 141337426 126598317 113095826 101197466 91076536 83150239 78272599 77792910 83419434 96589768	+ 552656433 705980548 793843408 796919804 738727075 654118754 565439767 481059746 402679958 331071140 268703826 220785424 196036282 207275019 269480117	+ 746681339 659132055 521340176 388716382 302828944 271278616 280608214 313840044 358400034 407325962 458447644 513193884 574685970 643902015 712983914	10 + 44256400 40670344 32814529 24469122 18789498 16451022 16560520 17979990 19894049 21886552 23891442 26133786 29039408 33019360 37983836	10 18909459 29771961 36931974 38400170 35541528 30740457 25512780 20396865 15494742 10854325 6610129 3020832 528111 +- 112284 2246167	9 430248 1149843 1682626 1848808 1719023 1451923 1149523 847724 554261 273151 11412 +- 220900 407502 513211 465530
(1) (2) (3) (4) (5) (6) (7) (8) (9) (10) (11) (12) (13)	10 +140789048 160676350 169946161 167128543 155942105 141337426 126598317 113095826 101197466 91076536 83150239 78272599 77792910 83419434	+ 552656433 705980548 793843408 796919804 738727075 654118754 565439767 481059746 402679958 331071140 268703826 220785424 196036282 207275019	11 + 746681339 659132055 521340176 388716382 302828944 271278616 280608214 313840044 358400034 407325962 458447644 513193884 574685970 643902015	10 + 44256400 40670344 32814529 24469122 18789498 16451022 16560520 17979990 19894049 21886552 23891442 26133786 29039408 33019360	10 18909459 29771961 36931974 38400170 35541528 30740457 25512780 20396865 15494742 10854325 6610129 3020832 528111 + 112284	9 - 430248 1149843 1682626 1848808 1719023 1451923 1149523 847724 554261 273151 - 11412 + 220900 407502 513211
(1) (2) (3) (4) (5) (6) (7) (8) (9) (10) (11) (12) (13) (14)	10 +140789048 160676350 169946161 167128543 155942105 141337426 126598317 113095826 101197466 91076536 83150239 78272599 77792910 83419434 96589768	+ 552656433 705980548 793843408 796919804 738727075 654118754 565439767 481059746 402679958 331071140 268703826 220785424 196036282 207275019 269480117	+ 746681339 659132055 521340176 388716382 302828944 271278616 280608214 313840044 358400034 407325962 458447644 513193884 574685970 643902015 712983914	10 + 44256400 40670344 32814529 24469122 18789498 16451022 16560520 17979990 19894049 21886552 23891442 26133786 29039408 33019360 37983836	10 18909459 29771961 36931974 38400170 35541528 30740457 25512780 20396865 15494742 10854325 6610129 3020832 528111 +- 112284 2246167	9 430248 1149843 1682626 1848808 1719023 1451923 1149523 847724 554261 273151 11412 +- 220900 407502 513211 465530

	A ₆ (e)	A ₇ ^(c)	$\mathbf{A}_{7}^{(s)}$		A	(¢) 8		A ₈ ^(*)	$\mathbf{A}_{9}^{(e)}$
(0)	25002II	—135116	8t	518		8 21291	+	8 69732	7 + 3413
(1)	2416648	139155		1 68	1	5342	•	77852	4235
(2)	2001634	119178	_ I		5	30086		69535	3985
(3)	1497651	89792	1	198	l	11353		52961	3080
(4)	1135085	67264			Į.	39845		39269	2264
(5)	971348	56259	1		1	32055		32100	1808
(6)	950371	53425		274		22448		29543	1611
(7)	998643	54156		907		12681		28787	1503
(8)	1064833	55310		996	+	3267		27958	1377
(9)	1124512	55492		399	· ·	5493		26296	1192
(10)	1176841	54807			Į.	13417		23944	961
(11)	1241277	54617	1	559		20607		21746	7 35
(12)	1353841	57396		514		27439		21178	590
(13)	1557889	66507		804		34008		24428	649
(14)	1876019	84979		581		38690		34138	1101
(15)	2250948	111506	.			36511	+	51140	+ 2101
S	—12058835	627475		240		5191		315297	+15302
S'	—120 5 8916	-627484	1			5188		315310	+15302
	12030910	02/404) + °		3100		313310	1 *33~3
	$\mathbf{A}_9^{(s)}$	$\mathbf{A}_{10}^{(c)}$	$\mathbf{A}_{10}^{(s)}$	1	A ₁₁ ^(c)	A ₁₁ ^(s)		A ₁₂ ^(c)	$\mathbf{A}_{12}^{(s)}$
	7	7	7		7	7		7	7
(0)	+1999	+1491	1559	-	642	- 99	2	— 613	+ 217
(1)	+ 507	+ 708	2233		1138	61	4	452	556
(2)	—1073	265	2244		1243	1	4	- 118	677
(3)	1887	825	1770		1006	+ 33	6	+ 120	566
(4)	1889	88o	1292		731	40	0	175	410
(5)	1482	673	1009		557	29	7	126	305
(6)	954	387	868		462	+ 14	4	+ 47	244
(7)	417	98	772		390	—	7	— 32	193
(8)	+ 90	+ 166	659		306	14	.0	96	137
(9)	544	389	511		204	24	.2	139	72
(10)	935	565	339	-	90	31	3	161	+ 3
(11)	1282	714	167	+	22	36	5	171	- 63
(12)	1632	874	— 32		120	42	6	188	124
(13)	2039	1100	+ 12		180	53		237	175
(14)	2462	1408	— 167	+	137	73	- 1	351	186
(15)	+2615	+1656	707	-	125	— 96	3	— 523	— 76
S	+3202	+2972	7160	;	3217	—209	7	-1305	+1378
S′	+3201	+2971	—7157	;	3218	209	7	—1308	+1378

In the expansion of $\left(\frac{a'}{\triangle}\right)^3$ we have:

	\mathbf{A}_0	A ₁ ^(o)	$\mathbf{A}_1^{(s)}$	$\mathbf{A}_2^{(c)}$		A	(s) 2		$\mathbf{A}_3^{(\sigma)}$		A ₃
	8	8	8	8			•		8		8 .
(0)	35089976	+12331006	5184099		2992		405728		5328172	+	
(1)	36399108	10368258	5459639	9 3558	6989	14	ი25867		3418173		21250198
(2)	35831498	7888818	5401277	76 3590	1058	10	724124	I	0356352		22253821
(3)	33605553	5730867	5039416	57 3354	1581	7735653		7433543			21005313
(4)	30505218	4403645	4515836	54 2969	1228	5	847739		5531546		18420444
(5)	27354241	3930701	3980181	19 25 63	9731	5	110397		4730376		15566695
(6)	24680381	4087409	3524912	I .	6607	5	200308		4701661		13050975
(7)	22707163	4644416	3185661	14 1946	4988	5	794001		5118886		11050226
(8)	21482105	5458113	2967002	20 1759	3578	6	697861		5791861		9541327
(9)	20990030	6463806	2863954	1646	8922	7	834727	(6650155		8461126
(10)	21215032	7640861	2873389	6 1606	1400	9	196986		7699370		7779549
(11)	22161697	8974548	2998232	I .	5743		800639		8985035		7532876
(12)	23845661	10412474	3246705	1766	2465	12	631871	10	0552267		7847264
(13)	26250114	11809186	3625536	1998	8913	14.	565988		2370479		8948193
(14)	29236542	12872141	4123477	2351	4502	16	259050	I	1199125		11099630
(15)	32418555	+13172728	— 468408 4	.6 — 2800	70 90	170	096490		5453849	+	14364166
S	2. 21886413	+65094467	-3. 1836699	8 -1.9511	3830	82	963667	— 74	1160354	+	1.08178652
S'	2. 21886461	+65094510	-3. 1836708				963 762		<u> 1160496</u>	+	1.08178793
	$\mathbf{A}_{4}^{(c)}$	A4(s)	A ₅ ^(o)	$\mathbf{A}_{5}^{(s)}$	A	(c) 6	A ₆)	A ₇ ^(c)		A ₇ ^(s)
	8	8				7	7		7		7
(0)	+ 8987554	+12145522	+ 8673540	— 3704 75 2	_	98548	— 57	3100	— 354.	546	22400
(1)	11751919	10970062	8153752	5970082	2	69656	56	6582	373	435	+ 97911
(2)	13086548	8590198	6514222	7335251	3	90879	46	4736	316	759	195941
(3)	12617811	6151518	4667605	7328629	4	12819	33	4245	229	471	225476
(4)	11003715	4510084	3375280	6385368	3	61504	23	8674	162	012	200018
(5)	9093835	3772919	2761546	5158312	2	85325	19	0954	126	732	154166
(6)	7364525	3657075	2606588	4013196	2	11855	17	5258	112	934	108319
(7)	5942540	3878846	2685155	3044511	1	48300	17	4800	108	717	68008
(8)	4802403	4275141	2868451	2233644		93667	18	0000	107	227	32935
(9)	3891580	4787033	3109732	1542615		45528	18	7345	106	040	+ 1729
(10)	3181133	5424561	3417701	946538	_	1968	ı	7398	105	446	— 269 5 1
(11)	2688125	6243783	3843124	445356	+	38016	21	4001	107	992	54448
(12)	2500012	7325205	4471921	— 82081		73496	24	4336	118	769	81732
(13)	2807451	8722558	5400372	+ 18601		98335	29	8456	146		107167
(14)	3905202	10338624	6644708	— 39 1 428		95436	38	4195	199		121075
(15)	+ 6037771	+11739930	+ 7951480	<u> </u>	+	35769	l	1360	- 278		-100637
S	+54831092	+56266410	+38572411	25092258	c	89489	-245	7697	—1477	050	+285055
S/	+54831032	+56266649	+38572766	-25092462	1	89508	-245		-1477	- 1	+285038

	A ₈ ^(c)	A ₈ ^(s)	$\mathbf{A}_{9}^{(c)}$	A ₉ (s)	A ₁₀ ^(c)	A ₁₀ ^(s)	A ₁₁ ^(c)	$\mathbf{A}_{11}^{(s)}$	$\mathbf{A}_{12}^{(c)}$	$\mathbf{A_{12}^{(s)}}$
	6	6	6	6	6	6	6	6	6;	6
(0)	- 6296	+20609	+11218	+6569	+5392	 5 640	— 2537	3918	2623	+ 930
(1)	+ 1617	23513	14225	+1703	+2619	8256	4593	2478	1981	2437
(2)	9014	20816	13263	-3575	— 97 I	8222	4969	— 1 37	— 512	2931
(3)	11912	15247	9866	6045	2909	6243	3874	+1295	+ 501	2361
(4)	10815	10658	6838	5707	2928	4298	2654	1452	688	1613
(5)	8136	8151	5112	4187	2095	3140	1894	1010	465	1125
(6)	5346	7041	4274	2529	1131	2535	1475	+ 463	+ 162	843
(7)	2868	6516	3787	-1049	— 27I	2141	1181	— 22	— 105	636
(8)	+ 714	6114	3351	+ 220	+ 446	1768	897	410	305	435
(9)	— 1183	5669	2860	1304	1028	1352	584	696	436	225
(10)	2910	5197	2325	2257	1505	902	- 261	910	509	+ 10
(11)	4593	4851	1827	3181	1957	457	+ 67	1090	556	204
(12)	6401	4942	1534	4241	2502	90	375	1332	636	421
(13)	8418	6046	1788	5619	3339	+ 36	596	1787	852	629
(14)	10233	9024	3238	7244	4561	543	+ 485	2604	1346	712
(15)	—10287	+14400	+ 6580	+8193	+5714	— 24 37	- 471	3627	-2124	— 309
s	+ 49	+84401	+46041	+8720	+9376	23998	—11933	7396	5081	+5629
S'	+ 52	+84393	+46045	+8719	+9382	—23990	11934	7395	—5088	+5642

In the expansion of $\left(\frac{\mathbf{a}'}{\triangle}\right)^5$ we have:

	Ao	$\mathbf{A}_{1}^{(c)}$	$\mathbf{A}_1^{(s)}$	$\mathbf{A}_{2}^{(c)}$	$\mathbb{A}_2^{(s)}$	$\mathbf{A}_3^{(c)}$	$\mathbf{A}_3^{(s)}$
	7	6	6	6	6	6	6
(0)	1. 3976550	+ 592456	-2. 491221	—1. 883176	— 949320	—1.045379	+1.240231
(1)	1.4993293	513843	2. 705203	2. 11 9180	835265	940458	1.489421
(2)	1.4549244	386015	2. 641289	2. 111756	630886	717393	1. 541628
(3)	1. 2868392	265827	2. 335899	1. 876627	432856	490916	1. 387302
(4)	1.0694995	188399	1. 931629	1. 540895	303491	340026	1, 132334
(5)	8687136	153604	1.556182	1. 223261	243792	268332	882959
(6)	7142908	146793	1. 266890	976410	229253	247320	686426
(7)	6097718	155897	1.069910	805313	239699	253352	546854
(8)	5489399	175228	952703	697844	265665	275293	453490
(9)	5254040	203732	902561	641865	305357	310798	395449
(10)	5361580	242957	913370	631077	361373	3 62639	366449
(11)	5824171	295627	987320	666748	438698	436873	366302
(12)	6692240	363961	1. 134661	75 ⁸ 545	542510	541254	402529
(13)	8032381	446366	1. 370453	923946	673277	680769	492428
(14)	9861677	531488	1. 703027	1. 180903	816494	845868	661188
(15)	1. 2011551	+ 592412	— 2. 107287	—I. 523724	— 930071	— 993712	+ 923593
S	7. 3768593	+2.627297	— 1 3. 0 34790	<u>9.78</u> 0606	4. 0 98992	-4. 375172	+6.484275
S'	7. 3768682	+2.627308	—13. o34815	9. 780664	4. 099015	-4. 375210	+6.484308

	$\mathbf{A_4^{(c)}}$	A.4	s)	A ₅ ^(c)	$\mathbf{A}_{5}^{(s)}$	A ₆ ^(c)	A(8)	A	(c)	A ₇ ^(e)
	6		6	6	6	6	6		4	4
(0)	+ 70791	4 + 9	56717 +	_	— 331422	- 98757		528 —	3938	— ² 49
(1)	95048	2 8	87199	748488	548082	277250	582	456	4252	+1115
(2)	1.04657	3 6	86886	591413	666088	397615	4720	620	3568	2208
(3)	96361	9 4	69716	405153	636264	401857	325	102	2476	2434
(4)	78400	5 3	21333	273852	518114	329325	2174	416	1638	2022
(5)	59941	5 2	48724	207718	387933	241255	1612	471	1191	1448
(6)	45117	8 2	24097	182558	280994	166988	1381	186	990	9 49
(7)	34318	0 2	24045	177502	201208	110443	1302	216	901	564
(8)	26666	2 2	37420	182468	142072	67180	1291	120	856	2 63
(9)	21261	8 2	61523	194670	96580	32157	1322	289	834	+ 14
(10)	17514	4 2	98598	215540	5 9 72 3	- 1421	1404	411	835	213
(11)	15265		54476	249809	28917	+ 27831	1568	817	881	444
(12)	14951	1	38010	305799	— 5 637	56588	1881	189	1018	700
(13)	17970		58365	394707	+ 1368	80858	245	389	1335	979
(14)	26986	7	14591	523400	30781	84488	3399	942	1958	1190
(15)	+ 44923	8 + 8	73662 +	673097	— 137189	+ 34028	- 466	563 —	2935	—106o
s	+3.85085	8 +3.8	77652 +	3. 051057	-2. 034831	-920210	2. 2004	112	4801	+3090
S'	+3.85091		I .	3.051044	-2. 034805	—920245	2. 2004		4805	+3092
							1			
	A ₈ ^(c)	$\mathbf{A}_8^{(s)}$	A ₉ ^(c)	A ₉ (s)	A(c)	A ₁₀ ^(s)	$\mathbf{A}_{11}^{(c)}$	$\mathbf{A}_{11}^{(s)}$	${f A}_{12}^{(c)}$	A ₁₂ ^(s)
	4	4	4	4	4	4	x	4	4	4
(0)	— 7 68	+2513	+1490			- 811	— 392	- 606	-434	1
(1)	+ 202	2940	1936	1	I	1216	727	392	335	1
(2)	1115	2574	1786	<u> </u>	32 — 142	1198	7 79	— 21	— 86	1 '
(3)	1412	1807	1274	. 78	31 407	872	582	+ 195	+ 81	
(4)	1202	1184	829	69	384	564	375	205	104	1 -
(5)	841	843	577	47	256	384	249	133	66	1
(6)	516	680	451	26	66 129	290	182	+ 57	+ 21	1
(7)	262	595	378	- 10	05 - 29	232	138	— з	- 13	80
(8)	+ 63	538	323	+ 2	+ 47	185	101	46	37	53
(9)	_ 103	492	271	12	106	139	65	78	52	1
(10)	254	454	222	21	5 156	93	- 29	102	61	1
(11)	413	436	180	1	208	49	+ 8	125	69	- 25
(12)	604	467	158	1	280	10	45	161	82	1
(13)	847	608	196	61	7 397	+ 3	76	229	117	1 -
(14)	1106	975	381	85	582	- 69	+ 67	358	198	
(15)	1190	+1666	+ 829	+103	4 + 780	- 332	69	— 533	-334	
s	+ 164	+9385	+5640	+ 96	60 + 1185	-3220	1746	—1032	—773	i
S'	+ 164	+9387	+5641	1		-3221	1746	—1032	—773 —773	1
1				1				,-	113	' 598

In the expansion of $\left(\frac{a'}{\triangle}\right)^7$ we have:

1	\mathbf{A}_0	$\mathbf{A}_{1}^{(c)}$	$\mathbf{A}_{1}^{(s)}$	$\mathbf{A}_{2}^{(c)}$	$\mathbf{A_{2}^{(s)}}$	A ₃ ^(c)	A ₃	· .	A ₄ ^(c)	$A_4^{(s)}$
(0)	6. 7363	+ 2.9876	—12. 5 626	—10. 2662	5. 1752	— 6. 220 <u>9</u>	+ 7.3	3804 + 4	4. 6006	+ 6.2189
(1)	7 · 4755	2. 6776	14. 0955	11. 9195	4. 6978	5.7671	9.1	336	5. 3606	5.9367
(2)	7. 1499	1.9830	13. 5684	11.7182	3. 5007	4. 3425	9.3	319	5.9158	4. 5389
(3)	5. 9601	1. 2895	11. 3305	9.8582	2. 2733	2.8192	7.9	670	6. 0529	2.9500
(4)	4. 5307	8385	8. 5968	7. 4569	1.4687	1.8052	6. 0	0115	4. 5650	1.8710
(5)	3. 3293	6208	6. 2910	5. 4011	1.0766	1.3047	4. 2	932	3. 2061	1.3305
(6)	2.4913	5423	4. 6801	3. 9569	9290	1.1077	3.0	745	2. 2294	1. 1073
(7)	1.9708	5354	3.6757	3. 0456	9067	1.0621	2. 2	925	1. 5907	1. 0386
(8)	1.6869	5737	3. 1195	2. 5213	9599	1.1046	1.8	3196	1. 1849	1.0549
(9)	1.5810	6539	z. 8964	2. 2753	1.0823	1. 2245	1.5	581	9283	1. 1417
(10)	1.6291	7 869	2.9582	2. 2566	1. 2922	1. 4407	1.4	1558	7708	1.3140
(11)	1.8415	9945	3. 3208	2.4714	1.6259	1.7963	1.5	062	6946	1.6126
(12)	2. 2622	1. 3047	4. 0674	2. 9871	2. 1364	2. 3586	1.7	541	7195	2. 1078
(13)	2.9644	1.7402	5. 3430	3.9414	2. 8722	3. 2026	2. 3	3166	9310	2. 8929
(14)	4.0174	2. 2785	7. 3010	5.5143	3. 8127	4. 3397	3-3	3922	1. 5203	4.0256
(15)	5. 3812	+ 2.7831	9.9015	— 7. 7 644	— 4. 7 40 1	 5 · 5435	+ 5.1	524 + 2	2. 7439	+ 5.3358
s	30. 5038	+11.2952	56.8540	-46.6775	19. 2748	—22.7199	+34.2	200 +2	2. 5063	+22. 2384
S'	30. 5038	+11.2950	56. 8544	—46. 6 7 69	—19. 2749	—22. 7200			2. 5081	+22. 2388
							1			
	$\mathbf{A}_{5}^{(c)}$	$\mathbf{A}_{5}^{(s)}$	A ₆ (c)	$\mathbf{A}_6^{(s)}$	A ₇ ^(c)	A ₇ ^(s)	A ₈ ^(c)	$\mathbf{A}_8^{(s)}$	A ₉ ^(c)	$\mathbf{A}_{9}^{(s)}$
(0)	+ 5.4939	 2. 3463	7583	- 4.4113	— 3. 27 1	206	— 684 °	+2.244	+1.42	4 +834
(1)	5. 4500	3. 9912		4. 5973	3. 627		+ 185	2. 697	1.89	1 !
(2)	4. 2543	4. 7914	_	3. 6857	3.007	1.858	1.008	2. 33I	1.73	
(3)	2.7729	4. 3556	1	2.4176	1.986	1.950	1. 217	1.559	1.17	1 1
(4)	1.7424	3. 2964		1.5042	1. 224	1.510	96 6	953	71	
(5)	1.2171	2. 2725	1.5399	1.0310	822	1.000	626	627	46	
(6)	9903	1.5243		8182	636	611	358	471	33	
(7)	9050		1	7257	546	342	172	390	26	
(8)	892u	6950	3596	6911	500		+ 40	339	21	_ I I
(9)	9362	4646		6964	478	+ 8	64	305	18	
(10)	1.0446	2895	— 75	7447	482	124	159	283	14	_
(11)	1. 2505	1452		8584	524	264	266	280	12	
(12)	1.6167	298	3267	1.0866	637	439	409	315	111	5 319
(13)	2. 2419	+ 78	5008	1.5198	895	656	613	440	15	
(14)	3. 2248	_ 1897	5665	2. 2794	1.420	862	863	731	32	
	+ 4. 4857	- 9142	+ 2464	— 3· 3774	2. 298		-1.00I	+1.404	+ 74	
		!	—6. 6004		1	1			1	i i
	+19.2596	-13. 1624		15. 2212	—11. 177		+ 257	+7.667 +7.702	+5.01	
S'	+19. 2593	13. 1611	6. 6009	<u>-15. 2236</u>	<u>—11. 176</u>	+2.502	+ 256	十7.702	+5. oc	75 +700

The next step is to apply the process of mechanical quadratures to the preceding values. Let us denote any one of the coefficients $A_i^{(o)}$, $A_i^{(s)}$ by Y; and the sixteen special values of Y by Y_0 , Y_1 , Y_2 Y_{15} . If Y is developed in a periodic series as a function of g', we have

$$Y = c_0 + c_1 \cos g' + c_2 \cos 2g' + c_3 \cos 3g' + \dots + s_1 \sin g' + s_2 \sin 2g' + s_3 \sin 3g' + \dots$$

and the following formulæ determine c_0, c_1, s_1 , etc., from the special values of Y.* Let

$$\begin{array}{lll} (\circ.8) = Y_0 + Y_8 & \left(\frac{\circ}{8}\right) = Y_0 - Y_8 \\ (1.9) = Y_1 + Y_9 & \left(\frac{1}{9}\right) = Y_1 - Y_9 \\ (2.10) = Y_2 + Y_{10} & \left(\frac{2}{10}\right) = Y_2 - Y_{10} \\ \vdots & \vdots & \vdots & \vdots \\ (7.15) = Y_7 + Y_{15} & \left(\frac{7}{15}\right) = Y_7 - Y_{15} \\ \hline (0.4) = (0.8) + (4.12) & \left(0.2\right) = (0.4) + (2.6) \\ (1.5) = (1.9) + (5.13) & \left(0.2\right) = (0.4) + (2.6) \\ (2.6) = (2.10) + (6.14) & \left(0.37\right) = (3.11) + (7.15) \end{array}$$

Then,

$$8 (c_{0} + c_{8}) = (0.2)$$

$$8 (c_{0} - c_{8}) = (1.3)$$

$$4 (c_{2} + c_{6}) = (0.8) - (4.12)$$

$$4 (c_{2} - c_{6}) = \{ [(1.9) - (5.13)] - [(3.11) - (7.15)] \} \cos 45^{\circ}$$

$$8c_{4} = (0.4) - (2.6)$$

$$4 (s_{2} + s_{6}) = \{ [(1.9) - (5.13)] + [(3.11) - (7.15)] \} \cos 45^{\circ}$$

$$4 (s_{2} - s_{6}) = (2.10) - (6.14)$$

$$8s_{4} = (1.5) - (3.7)$$

$$4 (c_{1} + c_{7}) = \left(\frac{0}{8}\right) + \left\{\left(\frac{2}{10}\right) - \left(\frac{6}{14}\right)\right\} \cos 45^{\circ}$$

$$4 (c_{1} - c_{7}) = \left\{\left(\frac{1}{9}\right) - \left(\frac{7}{15}\right)\right\} \cos 22^{\circ} \cdot 5 + \left\{\left(\frac{3}{11}\right) - \left(\frac{5}{13}\right)\right\} \cos 67^{\circ} \cdot 5$$

$$4 (c_{3} + c_{5}) = \left(\frac{0}{8}\right) - \left\{\left(\frac{2}{10}\right) - \left(\frac{6}{14}\right)\right\} \cos 45^{\circ}$$

$$4 (s_{1} + s_{7}) = \left\{\left(\frac{1}{9}\right) - \left(\frac{7}{15}\right)\right\} \sin 22^{\circ} \cdot 5 - \left\{\left(\frac{3}{11}\right) - \left(\frac{5}{13}\right)\right\} \sin 67^{\circ} \cdot 5$$

$$4 (s_{1} + s_{7}) = \left\{\left(\frac{1}{9}\right) + \left(\frac{7}{15}\right)\right\} \sin 22^{\circ} \cdot 5 + \left\{\left(\frac{3}{11}\right) + \left(\frac{5}{13}\right)\right\} \sin 67^{\circ} \cdot 5$$

$$4 (s_{1} + s_{7}) = \left\{\left(\frac{2}{10}\right) + \left(\frac{6}{14}\right)\right\} \cos 45^{\circ} + \left(\frac{4}{12}\right)$$

$$4 (s_{3} + s_{5}) = \left\{\left(\frac{1}{9}\right) + \left(\frac{7}{15}\right)\right\} \cos 22^{\circ} \cdot 5 - \left\{\left(\frac{3}{11}\right) + \left(\frac{5}{13}\right)\right\} \cos 67^{\circ} \cdot 5$$

$$4 (s_{3} + s_{5}) = \left\{\left(\frac{1}{9}\right) + \left(\frac{7}{15}\right)\right\} \cos 22^{\circ} \cdot 5 - \left\{\left(\frac{3}{11}\right) + \left(\frac{5}{13}\right)\right\} \cos 67^{\circ} \cdot 5$$

^{*}Auseinandersetzung, Abh. I, ss. 160, 161.

As the values of the Y have already been divided by 8 we have no need to make this division in obtaining the values of c_i and s_i .

If we suppose that

$$\begin{split} \mathbf{A}_{i}^{(s)} &= \mathbf{C}_{i,\,0}^{s} + \mathbf{C}_{i,\,1}^{s} \cos g' + \mathbf{C}_{i,\,2}^{s} \cos 2g' + \dots \\ &\quad + \mathbf{C}_{i,\,1}^{s} \sin g' + \mathbf{C}_{i,\,2}^{s} \sin 2g' + \dots \\ \mathbf{A}_{i}^{(s)} &= \mathbf{S}_{i,\,0}^{s} + \mathbf{S}_{i,\,1}^{s} \cos g' + \mathbf{S}_{i,\,2}^{s} \cos 2g' + \dots \\ &\quad + \mathbf{S}_{i,\,1}^{s} \sin g' + \mathbf{S}_{i,\,2}^{s} \sin 2g' + \dots \end{split}$$

the terms in the developed function, which belong to each value of ν , are*

$$\frac{\mathrm{I}}{2} \bigg(\operatorname{C}^{\circ}_{i,\,\nu} \pm \operatorname{S}^{\circ}_{i,\,\nu} \bigg) \cos \bigg[(i \mp \nu) g' - i \varepsilon \bigg] \mp \frac{\mathrm{I}}{2} \bigg(\operatorname{C}^{\circ}_{i,\,\nu} \mp \operatorname{S}^{\circ}_{i,\,\nu} \bigg) \sin \bigg[(i \mp \nu) g' - i \varepsilon \bigg]$$

except for $\nu = 0$, when we have

$$C_{i,0}^c \cos (ig' - i\varepsilon) + S_{i,0}^{(c)} \sin (ig' - i\varepsilon)$$

It may be observed that in all the following expansions the constant terms are not doubled as is generally done.

It is supposed that it will be sufficiently accurate to stop with the terms whose argument involves the twelfth multiple of the motion of either planet; but as the coefficients below this limit will be modified through corrections arising from terms involving higher multiplies, it has been deemed advisable to prolong the series considerably beyond this limit. Thus, some coefficients are needed which are not given by the division of the circumference into sixteen parts. However, it is possible to derive these with sufficient accuracy for our purpose by induction from the rest. For, when the terms involving the argument $(i + \nu)g' - i\varepsilon$ are put in the form

$$k\,\cos\,\left[(i+\nu)g'-i\varepsilon\,+\beta\right]$$

it is found that when i is tolerably large and ν not too large with reference to i, log k and β , for the same value of ν , will difference, and thus may be considered as continuous functions of i. These differences may be conjecturally prolonged, and values of k and β , for larger values of i, be obtained.

^{*}Auseinandersetzung, Abh, I, s. 165, gl. (136).

I give here three specimens of this method of induction, taken from the development of $\frac{\mathbf{a}'}{\triangle}$. All the quantities below the line have been inferred from the corresponding quantities above it:

Arg.	$\log k$	β
g' ε $8-9$ $9-10$ $10-11$ $11-12$ $12-13$ $13-14$ $14-15$	6. 5752 6. 3340 2464 6. 0876 2504 5. 8372 5. 5838 2534 20 2554 5. 0717 2567	160 16 239 21 79 8 318 29 79 4 37 33 116 39 79 6 195 45 79 6 274 51 79 6
9-9 $10-10$ $11-11$ $12-12$ $13-13$ $14-14$ $15-15$	7. 1941 6. 8893 6. 5844 3060 6. 2784 5. 9727 5. 6670 5. 3613	$ \begin{array}{cccccccccccccccccccccccccccccccccccc$
10 9 11 10 12 11 13 12 14 13 15 14 16 15	7. 1213 6. 8697 6. 6148 2549 17 6. 3582 6. 1006 2576 5. 8425 5. 5840 2576 2581 2581 2581 2581 2581	$ \begin{array}{cccccccccccccccccccccccccccccccccccc$

All the coefficients in the following expressions, which belong to arguments having a multiple of ε higher than the twelfth, have been derived in this way.

These series are the developments of the first four odd powers of the reciprocal of the distance between the planets in terms of the mean anomaly of Saturn and the eccentric anomaly of Jupiter, having the general form, which may be denoted thus:

$$\sum_{i',i} [C_{i',i} \cos(i'g' + i\varepsilon) + S_{i',i} \sin(i'g' + i\varepsilon)]$$

Arg.	4	<u>3'</u>	(<u>a</u>	<u>(</u>)³	$\left(\frac{\mathbf{a}'}{\triangle}\right)^5$	
	cos.	sin.	cos.	sin.	cos.	sin.
i' i o o o o I o - 2 o - 3 o - 4 o - 5	1. 090769379 —0. 009611762 —0. 000029218 +0. 000014879 —0. 000000353 —0. 000000011	-0.005222181 +0.000403992 -0.000003042 -0.000000516 +0.00000024	2. 21886437 — 0. 13073646 — 0. 01248822 + 0. 00122596 — 0. 00002614 — 0. 00000220	-0. 32233309 +0. 01678057 +0. 00012614 -0. 00006522 +0. 00000309	7. 376863 —0. 919969 —0. 228893 +0. 026086 —0. 000377 —0. 000110	-2. 722383 +0. 216600 +0. 008834 -0. 002112 +0. 000069

Arg.	<u>a'</u> △		$\left(\frac{\mathbf{a}'}{\triangle}\right)$	3	(<u>a</u>	<u>4</u>) ⁵
8.	cos.	sin.	cos.	sin.	cos.	sin.
i' i 1 + 4	0. 000000055	+0.000000028	—o. ooooo641	- - 0. 00000630	-0.000173	+ 0.000218
1+3	+0.000001213	+0.000000886	+0.00013146	+0.00005714	+0.003737	+ 0.000801
I + 2	+0.000010986	-0. 000037004	-0. 000 25 189	—o. 00244367	-0.012724	- 0.045109
1+1	-0.001021715	+0.000073316	-0. 03290290	+0.02458293	—o. 369508	+ 0. 328868
1 0	+0.066523370	+0.033717067	+0. 54330098	+0. 27546502	+3. 381297	+ 1.715381
1-1	+0. 125668089	-0. 607216197	+0.65094488	-3. 18367041	+2.627302	—13. 0348o2
I — 2	+0.003405534	+0.006381882	—o. 16421930	+0.06482696	—I. 913345	+ 0.395249
1-3	+0.000131740	+0.000061991	+0.00847042	+0.00620331	+0. 121067	+ 0. 146816
1-4	-0.000000988	-0.000006126	+o. oooo6848	0. 00060403	+0.005713	— 0. 014632
1-5	-0.000000225	+0.000000147	-0.00003190	+0,00001265	-0.001207	+ 0.000159
1-6	+0.000000012	+0.000000005	+0.0000014	+0.0000013	+0.000046	+ 0.000059
2+4	—0. 000000002	0, 000000000	-0.00000215	+0.00000020	-0.000043	+ 0.000011
2+3	+0.00000066	+0.000000130	+0.00000996	+0.00001301	+0.000381	+ 0.000345
2+2	+0.000002326	—0. 0000 02868	+0.00011554	—0. 00026211	+0.001659	— o. oo6430
2+1	—0.000088053	0. 000038336	—0. 00479184	+0.00053154	-0. 074745	+ 0.016074
2 0	+0.002864107	+0.004044874	+0. 04443816	+0, 06259484	+0.416081	+ 0.581322
2 — I	+0.039793422	o. o62478629	+0. 39593654	—o. 56323564	+2.500797	— 3. 415191
2 — 2	—0. 235015102	—0. 1012 06109	-1. 95113893	—о. 82963714	—9. 78o635	4. 099003
2-3	+0.005066355	0. 003542935	+0. 04056762	+0.07642442	+0.134383	+ 1.226405
2-4	+0.000069656	0.00000812	+0.00313416	-0.00412321	+0.089266	— o. o65707
2 5	—0. 000003104	+o. 000000692	0. 00029492	—0, 00003828	o. oo8oo6	0.003483
2-6	+0,000000061	+0.000000099	+0.0000056	+0.0000158	+0,000072	+ 0.000634
2 — 7			+0.0000007	-0.000011		
3+3	+0,000000001	+0.000000008	+0.00000030	+0.00000182	+0.000021	+ 0.000064
3+2	+0.000000312	-0.000000155	+0.00002632	-0.00001996	+0.000645	o. ooo645
3 + 1	—0. 000005984	—0. 000006925	0.00051581	0. 00022369	—0. 010596	- 0,003290
3 0	+0.000040251	+0.000369645	+0.00111299	+0.00916223	+0.015511	+ 0.115941
3 — 1	+0.006132504	—0. 004211786	+0.09235900	—o. o5316203	+0.800117	— O. 427144
3 — 2	—o. 038011415	-o. o35554695	—o. 434694 <u>5</u> 8	—o. 436977o8	—2. 840628	— 2. 974234
3 — 3	—o. 066208490	+0.095200620	-0.74160425	+1.08178722	4. 375191	+ 6.484291
3 — 4	—0. 002210673	-o. oo384 7 996	+0.03442962	0. 03119988	+0.740468	— o. o38081
3 — 5	+0.000053949	0. 000051903	-0.00180789	0, 00160898	—o. o34747	0.052383
3 — 6	+0.000000564	+0.000002257	-0.0000211	+0.0001442	0, 002090	+ 0.004311
3 — 7	+0.0000003	—0.0000002	+0.0000091	-0. 0000039	+0.0002	0,0000
4+3	+0.00000008	-0.00000001	+0.00000022	+0.00000016	+0.000002	+ 0.000009
4+2	+0.000000024	-0.00000004	+0.00000359	—о. ооооообо	+0.000108	0,000026
4 + 1	—0. 000000225	—o. oooooo835	—0. 0000 3936	—0. 00005157	—o. oo1o61	- 0.001118
4 0	—o, 000012106	+0.000027374	0. 00040493	+0.00100525	0. 006223	+ 0.016502
4-1	+0.000689461	0. 000117837	+0.01440813	—o. ooo96355	+0. 161572	— o. oo4719
4 2	—0. 003158672	0. 006601681	-0. 04321484	—о. 10925388	—о. 335176	— o. 95453o
4-3	0. 027082107	+0.019492364	— 0. 40318669	+0. 27357050	—3. 022802	+ 1.973497
4 4	+0.037875691	+0.039559784	+0. 54831062	+0.56266530	+3.850885	+ 3.877681
4-5	0. 002708439	+0.001068270	-0. 02530938	—о. 01666339	0. 017672	— o. 434243
4 — 6	—0. 000027431	—o. oooo66585	-0. 0007872	+0.0006010	o. 029824	+ 0.017755
4-7	+0.00000199	—0,00000026	+0.0000743	+0.0000150	+0.0023	+ 0.0011
4-8			0.000010	0. 000003	0,0000	o. ooor

Ang	<u>a</u> ' ∆	,	(<mark>a</mark> ⁄∆)3	(<u>a</u> ∆	() ⁵
Arg	cos.	sin.	cos.	sin.	cos.	sin.
i' i 5 + 2 5 + 1	+0.000000001 +0.000000006	—0. 000000011 —0. 000000070	+0.00000046 -0.00000120	-0. 00000008 -0. 00000730	+0. 000013 0. 000051	-0.000012 -0.000201
5 0	0. 000002061	+0.000001483	—o. oooo9749	+0.00007917	0.001905	+0.001651
5 — I 5 — 2 5 — 3	+0.0000611541 -0.0000440511 -0.005850270	+0.000183402 -0.0008744402 +0.001589795	+0.00167590 +0.00088227 —0.10919015	+0.00071761 -0.01843048	+0.023387 +0.019972 0.999876	+0. 011072 -0. 198533
5 — 4 5 — 5	+0.008451522 +0.022322999	+0.01389795 +0.018617851 -0.014177514	+0. 14044483 +0. 38572588	+0. 02304507 +0. 32787286 —0. 25092360	+1. 118180 +3. 051100	+0. 172078 +2. 719583 -2. 034818
5 — 6 5 — 7	+0.000374093 -0.00005898	+0.001776944 +0.00000758	-0.0098351 +0.0000239	+0. 0197303 +0. 0003108	-0. 255592 +0. 0087	+0. 020664 +0. 0163
5 — 8 6 + 1	+0.00000010 +0.000000023	-0. 00000178	0,000000	-0. 000043 +0. 0000015	+0.0007 +0.000004	-0. 0011 -0. 000028
6 o 6— I	-0.000000216 +0.000004134	+0.00000033 +0.000004042	-0.00001412 +0.00013941	+0.0000270	-0. 000337 +0. 002336	+0.000076 +0.003077
6— 2 6— 3	+0.000034393 0.000882242	o. 000089303 o. 000098703	+0. 00121750 -0. 01984301	0. 00228942 0. 00393200	+0.018026 -0.215399	-0. 029410 -0. 054884
6 — 4 6 — 5	+0.000343775 +0.011872674	+0.004551938 -0.002749242	+0.00267385 +0.24231846	+0. 09583348 —0. 05190099	0. 005696 + 2. 218561	+0. 935477 -0. 448374
6-6	0. 004674085 0. 00109630	0. 012058875 0. 00003131	—0. 0989498 +0. 0143572	-0. 2457720 +0. 0071733	0. 920227 	-2. 200452 +0. 1557
6— 8 6— 9	o. 00000448 o. 0000017	+0. 00004450 -0. 0000004	+0.000027 -0.000023	+0.000189 -0.000009	+0. ∞85 -0. ∞66	0. 0037 0. 0004
7 o 7— 1	-0. 00000020 +0. 000000163	+0.000000005 +0.000000500	o. 00000164 	0. 00000032 -+0. 00002562		-0. 000009 +0. 000543
7 - 2 7 - 3	+0.000007141 -0.000100096	—0. 000006850 —0. 000055409	+0.00027509 -0.00260484	-0. 00019927 -0. 00183584	+0. 004637 -0. 032469	—0. 002897 —0. 026305
7 — 4 7 — 5 7 — 6	-0. 000226657 +0. 003210470	+0.000759906 +0.000382706	-0. 00701279 +0. 07571960	+0.01854593 +0.01209625	-0. 090968 +0. 792862	+0. 208031 +0. 151209
7 — 6 7 — 7 7 — 8	-0.000205770 -0.00627479 +0.00010073	—0. 007123398 +0. 00111343 —0. 00063987	—0. 0026960 —0. 1477090 —0. 005769	0. 1657167 +0. 0285046	0. 012445 1. 4803	—1. 666873 +0. 3091
7 — 9 7 — 10	+0.0000304 -0.0000005	+0.0000097 +0.0000007	+0.000232 -0.000003	0. 009714 0. 000114 	+0.1000 0.0015 0.0003	0. 0236 0. 0039 +-0. 0003
8— 1 8— 2	+0.00000034 +0.00000944	+0. 00000062 -0. 00000307	-0. 00000069 +0. 00004193	+0. 00000209	-0.000022	+0.000072
8 — 3 8 — 4	-0.000008249 -0.000073320	-0. 000010756 -0. 000092680	-0. 00022931 -0. 00241109	-0. 00000687 -0. 00039576 +0. 00252016	+0. 000801 0. 003068 0. 034289	-0. 000064 -0. 006384
8— 5 8— 6	+0.000578366 +0.000679098	+0. 000298475 -0. 002086163	+0.01535549 +0.0198473	+0.00232010 +0.00915939 -0.0546519	+0. 180088 +0. 241701	+0. 031420 +0. 119135 0. 614590
8 — 7 8 — 8	0. 00404931 0. 00005190	—0. 00069304 +0. 00315303	—0. 1059393 +0. 000050	0. 0191499 +0. 084397	—1. 1646 +0. 0164	-0. 2181 +0. 9386
8 — 10	-0. 0003539 +0. 0000105	0. 0001270 0. 0000189	-0.006098 +0.000169	0. 004642 0. 000200	-0.0187 -0.0014	-0. 0676 +0. 0002
8 — 11	+0.0000007	+0.0000005	+0.000007	+0.000009	+0.0002	+0.0001

Arg.	<u>a′</u> ∆	·	$\left(\frac{\mathbf{a}'}{\Delta}\right)$)³	$\left(\frac{\mathbf{a}'}{\Delta}\right)$)5
8'	008.	sin.	cos.	sin.	cos.	sin.
i' i 9— 2	+0.00000105	+0.000000011	+0.00000506	+0.00000147	+0.000102	+0.000028
9-3	0.000000347	-0.000001478	0. 00000497	-0.00006134	+0.000003	-0.001114
9-4	-0.000013864	+0.000007724	—o. ooo50777	+0.00021178	0. 008041	+0.002627
9 5	+0.000073128	+0.000082574	+0.00209163	+0.00279303	+0.026442	+0.040181
9 6	+0.000311153	o. ooo394850	+0.0099776	-0. 0113624	+0. 133724	—о. 139955
9 – 7	-0.00125724	0. 00070623	-o. o362737	-0. 0217643	—0. 4374	—0. 2763
9 8	0. 00084109	+0.00218541	—o. o2495o	+0.063599	—o. 3017	+0 7604
9 5	+0.0015302	+0.0003202	+0.046043	+0.008720	+0. 5640	+o. o96o
9 — 10	-0.0001100	+0.0001856	-o. 003582	+0.003558	-0. 0472	+0.0123
9-11	0.0000106	0. 0000092	-0.000125	-o. 000181	0,0000	0.0000
9 — 12	+0.0000006	0. 0000006	+0.000011	0.000002	+0.0001	0.0001
10-3	+0.000000031	—o. oooooo166	+0.00000281	-0. 00000752	+0.000073	-0.000149
10 — 4	-0.0000019688	+0.0000002034	-0.00008126	-0.00000258	-0.001414	-0. 000171
10 — 5	+0.000005589	+0.000015625	+0.00014437	+0.00058416	+0.001554	+0.009252
10 6	+0.000081939	0.000049204	+0.0028987	0.0014681	+0.042790	0. 018728
10 — 7	-0.00024173	-o. ooo28135	-0. 0074859	-0.0095793	о. 0968	—o. 1339
10 — 8	-0. 00060228	+0.00070156	<u> </u>	+0.022108	— 0. 2676	+0. 2851
10 9	+0.0011171	+0.0007077	+o. 035851	+0.022907	+o. 4639	+o. 2976
10 — 10	+0.0002972	-0. 0007158	+0.009379	—0. 023994	+o. 1184	0. 3220
10 — 11	+0,0000916	+0.0000811	+o. 001899	+0.002612	+0.0068	+ 0. 0329
10 — 12	0.0000072	+0.0000052	—o. ooo158	+0.000073	0, 0004	0, 0000
10-13	-o. oooooo5	0. 0000006	+ 0. 000002	0. 000009		
11 — 4	—0 , 000000226	-0.00000072	0.00000981	-0.00000619	0. 000176	-0.000117
11 5	0, 000000111	+0.000002286	0. 00001586	+0.00009324	0. 000444	+0.001645
rr — 6	+0.000015719	<i>—о.</i> 000002670	+0.0006086	-0.0000475	+0.009827	0. 000089
11 7	-0, 00002700	-0.00007344	0.0008149	-0.0027374	-0.0101	-0. 0418
11 - 8	—0. 00022986	+0.00012997	— 0. 008343	+0.004277	-0. I224	+0.0575
11 - 9	+0.0003583	+0.0004580	+o. 012228	+0.016330	+о. 1680	+0. 2325
11 10	+0.0005112	—0. 0005361	+0.018019	o. 018847	+0.2512	— 0. 2628
11 11	-0.0003217	-0.0002097	0.011933	—0. 007 396	—0. 1746	-0. I032
11 — 12	+0.0000545	0.0000419	+0.001804	0.000910	+0.0227	-0. 0027
11 — 13	+0.0000021	+0.0000051	+0.000034	+0.000127		
11 — 14	—o. oooooo6	+0.0000003	0. 000006	0.000003		
12 5	—0. 000000129	+0.000000269	0.00000787	+0.00001157	0.000143	+0.000232
12 — 6	+0.000002358	+0.000000512	+0.0000984	+0.0000327	+0.001721	+0.000738
12 7	+0.00000022	-0.00001435	+0.0000533	—0. 0005819	+0.0015	0.0094
12 8	0. 00006043	+0.00000978	o. 002375	+0.000248	o. o378	+0.0020
12 — 9	+0.0000572	+0.0001738	+0.001950	+0.006724	+0.0267	+0. 1039
12 — 10	+0.0003212	-0.0001616	+0.012315	—o. oo5919	+o. 1859	—o. o86o
12 — 11	-0. 0002373	—о. 0003367	—o. oogo85	0. 012877	—o. 1362	-0. 1921
12 — 12	0. 0001 306	+0.0001378	—0. 005 084	+0.005635	o. o773	+0.0897
12 — 13	0. 0000172	0. 0000343	o. ooc333	—0. 001179	0.0000	-0.0154
12 — 14	+0.0000034	0,0000004	+0.000095	— 0. 000008		
12 15	+0.0000001	+0.0000005	0. 000004	+0.000004		
				<u> </u>		

Arg.		<u>a′</u> ∆	(1/2	<u>a'</u>)³	(<u>a</u>	<u>(</u>) ⁵
	cos.	sin.	cos.	sin.	cos.	sin.
i' i 13 — 6	+0.000000279	+0.000000194	+0, 0000122	+0.0000107	+0.000213	+0.000241
13 7	+0.00000089	-0. 00000218	+0.0000515	-0,0000945	+0.0011	0. 0016
13 — 8	-0.00001200	-0.00000243	-0. 000499	0.000140	o. oo85	-0. 0029
13- 9	0.0000014	+0.0000463	-0.000159	+0.001925	0. 0040	+0.0318
13 — 10	+0.0001225	-0.0000152	+0.005049	0.000456	+0. 0820	0.0051
13 — 11	-0.0000582	-0. 0002114	-0. 002249	o. oo8688	0. 0341	—о. 1389
13 — 12	<u> </u>	+0.0000928	—o. oo8593	+0.003852	0. 1368	+0.0619
13 — 13	+0.0000557	+0.0000756	+0.002503	+0.003219	+0.0433	+0.0530
13 — 14	-0.0000205	+0.0000058	—0.000731	+0.000039	-0.0101	0. 0015
13 — 15	+0.0000003	—0. 0000017	+0.000006	-0.000067		
14 — 7	+0.00000024	0.00000026	+0,0000141	-0.0000112	+0.0003	0, 0002
14 8	0. 00000184	-o. ooooo118	0.000075	0. 000057	-0.0015	-0.0014
14 9	0, 0000039	+0.0000092	0.000198	+0.000408	-0.0039	+0.0073
14 — 10	+0.0000322	+0.0000076	+0.001441	+0.000403	+0.0251	+0.0080
14 11	+0.0000061	-0.0000815	+0.000375	-0.003575	+0.0078	0, 0609
I4 — I2	0.0001319	+0.0000094	-0.005794	+0.000338	o. o 9 79	+0.0046
14 — 13	+0.0000279	+0.0001229	+0.001267	+0.005432	+0.0218	+0.0919
14 — 14	+0.0000416	-0. 0000207	+0.001927	-0.001021	+0.0343	-0.0191
14 — 15	+0.0000010	+0.0000118	-0.000049	+0.000427	0.0021	+0.0064
14 — 16	-0.000011	-0, 0000005	0. 000044	-0.000012		•
15 — 8	0.00000021	0, 00000028	0, 000006	0. 000008	0.0002	0.0003
15 9	0.0000014	+0.0000015	-o, oooo68	+0.000064	-0.0014	+0.0012
15 10	+0.0000065	+0.0000045	+0.000299	+0.000234	+0.0055	+0.0045
15 — 11	+0.0000099	-0.0000219	+0.000507	0. 001018	+0.0100	0. 0184
15 12	-0.0000513	-0.0000143	0. 002384	-0.000732	0.0426	-0.0142
15 13	-0.0000099	+0.0000784	0. 00 0506	+0.003669	-0.0097	+0.0654
15 — 14	+0.0000695	0.0000019	+0.003279	-0.000122	+0.0586	-0.0024
15 — 15	—o. ooooo66	0.0000220	0.000360	-0. 001 105	-0.0073	-0.0211
15 — 16	+0.0000065	+0.0000007	+0.000236	+0.000077	+0.0038	+0.0021
15 — 17	-0.0000005	+0.0000006	-0.000013	+0.000027		·
16 — 9	-0.0000003	+0.0000002	0.000014	+0.000007	0. 0003	+0.0001
16 — 10	+0.0000010	+0.0000016	+0.000048	+0.000076	+0.0008	+0.0014
16 — 11	+0.0000042	0, 0000044	+0.000227	-0. 000209	+0.0045	-0.0039
16 — 12	-0.0000138	-0.0000097	0.000672	0. 000517	-0.0125	-0.0102
16 — 13	-0.0000155	+0.0000305	-0.000779	+0.001493	+0.0158	+0.0281
16 — 14	+0.0000444	+0.0000149	+0.002210	+0.000762	+0.0414	+0.0147
16 — 15	+0.0000064	0.0000378	+0. 000289	-0. 001897	+0.0054	—o. o357
16 — 16	-0.0000113	+0.0000014	0. 000611	0. 000089	+0.0125	+0.0020
16 — 17	+o. oooooo o	-0.0000034	+0.000071	0. 000124	+0.0019	-0.0022
16 — 18	-0.0000002	+0.0000004	+0.000015	+0.000011		

				$\left(\frac{\mathbf{a}'}{\triangle}\right)^7$				
Arg.	008	sin.	Arg.	cos.	sin.	Arg.	cos.	sin.
i' i			i' i			i' i		
0 0	30. 504		3 — 1	+ 5.965	— 3. 074	6— 6	— 6. 600	15. 225
0-1	— 5. 696	—17. 950	3 — 2	16. 682	-17.875	6 — 7	— o. 726	+ 1.821
0 2	— 2. 40 <u>5</u>	+ 1.974	3-3	—22. 72 0	+34. 220	6 8	+ 0.215	0.018
0-3	+ o. 335	+ 0. 164	3-4	+ 7.243	+ o. 818			
0-4	0.001	— o. o38	3-5	— o. 332	o. 82o	7 2	+ 0.057	— o. o33
0-5	— o. oo5	+ 0.002	3-6	— 0 . 056	+ 0.069	7 — 3	0. 321	— o. 283
			3 — 7	+ 0.008	+ 0.002	7 — 4	о. 878	+ 1.827
1+4	0.004	+ 0.006				7 — 5	+ 6. 396	+ 1.367
1 + 3	+ 0.062	+ 0.005	4 →- 1	— o. 014	- 0.020	7 — 6	0. 023	—I 2. 726
1+2	— o. 201	o. 538	4 0	— o. 072	+ 0. 196	7 - 7	—11. 173	+ 2.503
I + I	— 3. 129	+ 2.978	4 — I	+ 1.480	0. 024	7 — 8	+ 1.135	+ 0.483
1 0	+20. 066	+10.186	4 — 2	— 2. 295	— 7. o35	7 — 9	+ o. ∞3	0.112
11	+11.295	56. 854	4-3	—1 9. 060	+12.142			
I — 2	—14. 393	+ 2.242	4-4	+22.507	+22. 239	8 2	+ 0.010	o. oo1
1 — 3	+ 1.158	+ 1.786	4 — 5	+ 1.061	— 4. 708	8 - 3	— o. o38	— o. o78
1-4	+ 0. 121	o. 206	4-6	o. 521	+ 0. 163	8 — 4	— o. 365	+ 0.305
1 5	— 0. 029	0.002	4-7	+ 0.037	+ 0.039	8 5	+ 1.617	+ 1.150
ı — 6	+ 0.001	+ 0.004				8 - 6	+ 2.166	5. 200
1	ŀ		5 0	0.026	+ 0.023	8 — 7	— 9. 498	— 1.819
2 + 3	+ 0.003	— 0,006	5 — 1	+ o. 256	+ 0. 126	8 8	+ 0. 264	+ 7.678
2+2	+ 0.016	0.096	5 — 2	+ 0. 227	— I. 746	8- 9	+ 0. 295	— o. 656
2 + I	— o. 812	+ 0. 207	5-3	- 7. 484	+ 1.101	8 — 10	+ 0.058	o. oo8
2 0	+ 3.266	+ 4.542	5 — 4	+ 7.280	+18, 200			
2 — 1	+14. 662	19. 650	5 — 5	+19.255	—13. 169	9 — 3	+ 0.001	— o. o16
2 2	-46.677	—19. 275	5 6	2. 953	— o. 945	9 4	0.096	+ 0.025
2 — 3	+ 0. 141	+10.570	5 — 7	+ 0.007	+ 0. 331	9 — 5	+ o. 261	+ 0.429
2 4	+ 1.240	— o. 638	5 8	+ 0.037	0. 002	9 6	+ 1.317	— I. 292
2 5	— O. I2I	o. o86				9 - 7	— 3. 845	— 2. 557
2 — 6	0.002	+ 0.014	6 — I	+ 0.028	+ o. o36	9 - 8	— 2.657	+ 6.605
			6 — 2	+ 0. 199	— 0. 302	9 9	+ 5.006	+ 0.763
3+2	+ 0.010	— 0. OI 2	6 3	— 1 .879	— o. 547	9 — 10	— o. 379	- o. 18o
3 + 1	— O. I42	o. o36	64	— o. 217	+ 7.233	9-11	– о. оот	+ 0.029
3 0	+ o. 159	+ 1.135	6 5	+15.843	— 3. 07 6			

In order to be serviceable in the method of treating the problem we intend to follow it is necessary to transform the preceding series into others, the arguments of whose terms are of the general form i'g'+ig. This is done by means of the Besselian functions $J_{l}^{(k)}$ (we use Hansen's notation for these quantities). The following formulæ serve for their computation:*

Derive p_{k} from

$$\frac{\mathbf{I}}{\bar{p}_{k}} = r_{k} - p_{k+1}$$

^{*}Auseinandersetzung, Abh. I, s. 173,

where

$$r_{\scriptscriptstyle k} = rac{k}{l}$$

in which equations we must begin with so large an integer for k that, for the first application, we can put $p_{k+1} \equiv 0$. This integer, in the present case, may be assumed as about 8 or 9. The value of $J_l^{(k)}$ is then

$$\mathbf{J}_{\cdot}^{(k)} = \mathbf{J}_{\cdot}^{(0)} p_{\cdot} p_{\cdot} p_{\cdot} p_{\cdot} \dots p_{\cdot}$$

where

$$J_{t}^{(0)} = I - \frac{l^{2}}{I^{2}} + \frac{l^{4}}{I^{2} \cdot 2^{2}} - \frac{l^{6}}{I^{2} \cdot 2^{2} \cdot 3^{2}} + \dots$$

For the present purpose it suffices to suppose in these formulæ l equal in succession to $\frac{e}{2}$, e, $\frac{3}{2}e$, 2e, etc.; but as we shall hereafter need these functions corresponding to the eccentricity e' of Saturn, the following tables contain the latter quantities also:

i	$\log\left(J_{\frac{l_0}{2}}^{(0)}-1 ight)$	$\log rac{\mathbf{I}}{i} \mathbf{J}_{rac{ie}{2}}^{(1)}$	$\log rac{1}{i} J_{rac{ie}{2}}^{(2)}$	$\log rac{1}{i} J_{rac{ie}{2}}^{(3)}$	$\log \frac{1}{i} J_{\frac{ie}{2}}^{(4)}$	$\log \frac{1}{i} J_{\frac{io}{2}}^{(5)}$
I	6. 76464 <i>n</i>	8. 3822758	6. 4636901	4. 3689921	2. 1493469	
2	7. 3666118 <i>n</i>	8. 3818968	6. 7644675	4. 9708626	3.0522853	
3	7. 7184785n	8. 3812646	6. 9401375	5. 3227293	3. 5803065	1. 7409358
4	7. 9679134n	8. 3803790	7.0644861	5. 5721642	3. 9547687	2. 2403957
5	8. 1611649n	8. 3792397	7. 1606373	5. 7654153	4. 2450436	2. 6276565
6	8. 3188323n	8. 3778459	7. 2388909	5. 9230826	4. 4820315	2. 9439185
7	8. 4518964n	8. 3761967	7. 3047404	6. 0561538	4. 6822141	3. 2111575
8	8. 5 669394 <i>n</i>	8. 3742908	7. 3614652	6. 1711884	4. 8554309	3. 4424930
9	8. 6681692n	8. 3721278	7.4111809	6. 2724174	5. 0080283	3. 6463866
10	8. 7584745n	8. 3697058	7.4553308	6. 3627288	5. 1443388	3. 8286154
11	8. 8398n	8. 36701	7. 4949	6. 4441	5. 267	3. 994
12	8. 9138n	8. 36404	7.5307	6. 5181	5. 380	4. 145
13	8. 9814n	8. 36078	7. 5632	6. 5858	5. 484	4. 284
13	8. 9814n	8. 36078	7. 5632	6. 5858	5.484	4. 284

i'	$\log \left(J_{\frac{i'o'}{2}}^{(0)}-1\right)$	$\log J_{\frac{t'e'}{2}}^{(1)}$	$\log J_{rac{d' heta'}{2}}^{(2)}$	$\log J_{rac{oldsymbol{i}'oldsymbol{e}'}{2}}^{(3)}$	$\log J_{\underline{\epsilon'e'}}^{(4)}$	$\log J_{\frac{4'a'}{2}}^{(5)}$	$\log J_{\frac{\ell' e'}{2}}^{(6)}$
1	6.8951130n	8. 4474282	6. 5940540	4. 5645600	2. 4101160	0. 1587563	
2	7.4969158n	8. 7479463	7. 1957728	5. 4673942	3. 6140313	1.6637357	
3	7.8486718n	8. 9231839	7. 5473865	5. 9952414	4. 3180552	2. 5439078	1
4	8. 0979528n	9. 0469266	7. 7964672	6. 3694592	4. 8173311	3. 1682020	
5	8. 2910046n	9. 1422972	7. 9892624	6. 6594221	5. 2043580	3. 6522414	2.0209
6	8. 4484286n	9. 2195944	8. 1463714	6. 8960265	5. 5203318	4. 0475219	2. 4944
7	8. 5812122n	9. 2843110	8. 2787822	7. 0957559	5. 7872306	4. 3815156	2. 8961

The transformation we seek to accomplish is arrived at by the aid of the equations

$$\cos (\beta - k\varepsilon) = \sum_{i = -\infty}^{i = +\infty} \frac{k}{i} J_{\frac{i\delta}{2}}^{(i-h)} \cos (\beta - ig)$$

$$\sin (\beta - k\varepsilon) = \sum_{i = -\infty}^{i = +\infty} \frac{k}{i} J_{\frac{i\delta}{2}}^{(i-h)} \sin (\beta - ig)$$

where β denotes any arbitrary angle. In employing these equations it must be remembered that

$$\mathbf{J}_{t}^{(-k)} = (-1)^{k} \mathbf{J}_{t}^{(k)} \qquad \qquad \mathbf{J}_{-t}^{(k)} = (-1)^{k} \mathbf{J}_{t}^{(k)} \qquad \qquad \mathbf{J}_{-t}^{(-k)} = \mathbf{J}_{t}^{(k)}$$

and when $i \equiv 0$ and $k \equiv 1$ or -1 we must suppose that the multiplier

$$\frac{k}{i}\,\mathbf{J}_{\frac{is}{2}}^{(i-k)} = -\,\tfrac{\mathbf{I}}{2}e$$

but when k has, in the same case, values different from i or -i this multiplier vanishes.

The developments found for the four odd powers of the reciprocal of the distance of the planets, when the terms are made to take the form

$$C^{(c)} \cos (i'g'+ig) + C^{(c)} \sin (i'g'+ig)$$

are as follows:

Arg.	<u> </u>	<u>'</u>	(<u>a</u>	() ³	$\left(\frac{\mathbf{a}'}{\triangle}\right)^{5}$		
Mg.	cos.	sin.	cos.	sin.	cos.	sin.	
i' i o o o o o o o o o o o o o o o o o o	1. 090999230. 009601950. 00026172 +-0. 00000505 +-0. 00000000 +-0. 000000000 +-0. 000000800. 00014980. 00105822 +-0. 063516727 +-0. 12543117 +-0. 00641586 +-0. 00040449 +-0. 00002113 +-0. 000000088 +-0. 00000004	-0.00524015 +0.00027740 +0.00001192 +0.00000001 0.00000000 +0.00000000 -0.00002952 +0.00029165 +0.048362194 -0.60717079 -0.00826731 -0.00015969 -0.00000046 -0.00000001	2. 222017910. 130018960. 01569650 +-0. 00050731 +-0. 00000131 +-0. 00000131 +-0. 00000350. 001059600. 03306005 +-0. 52839296 +-0. 658503330. 14876566 +-0. 00108483 +-0. 000325050. 000006090. 00000075	-0. 32304848 +0. 00896318 +0. 00065823 -0. 00002901 -0. 00000126 +0. 00003872 -0. 00182006 +0. 02561226 +0. 35166657 -3. 18494695 -0. 01247904 +0. 00657454 -0. 00012160 -0. 00001649 +0. 00000029	7. 39905 —0. 908103 —0. 25240 +0. 01419 +0. 00094 —0. 00007 +0. 00281 —0. 02186 —0. 36944 +3. 326835 +2. 718265 —1. 854333 +0. 03012 +0. 01018 —0. 00036 +0. 00004	- 2. 732029 + 0. 14988 + 0. 01703 - 0. 00106 - 0. 00010 - 0. 03715 + 0. 33465 + 2. 021865 - 13. 046252 + 0. 069633 + 0. 15512 - 0. 00351 - 0. 00060 - 0. 00004	
2+4 2+3 2+2 2+1	+0.0000001 +0.0000008 -0.0000012 -0.00009858	0. 00000000 0. 00000002 0. 00000319 0. 00001954	-0. 00000133 +0. 00001138 -0. 00000416 -0. 00490064	+0.0000056 +0.0000099 -0.00024417 +0.00071159	+0.00040 -0.00017 -0.07545	+ 0.00004 - 0.00605 + 0.01738	

Arg.	<u>a</u> 2		(<u>a</u>)3	$\left(\frac{\mathbf{a}'}{\triangle}\right)^5$		
	cos.	sin.	cos.	sin.	cos.	sin.	
i' i	16-6			1	1	1 - 66	
2 0	+0,00190636	+0.00555286	+0.03500321	+0.07616804	+0. 357561	+0.663313	
2 — I	+0.05110921	—o. o5756433	+0. 48984397	-0.52282903	+2.971190	—3. 214450	
2 — 2	—o. 23387573	-0. 10221994	—1. 93998606	—0. 84681116	-9.707139	4. 260549	
2 — 3	-0.00624030	0. 00844844	-0. 05348459	+0.03601136	—o. 343378	+1.026094	
2 — 4	0.00010949	-0.00049321	+0.00155033	-0.00052144	+0. 07647	+0.01401	
2 5	-0.00000172	—0,00002670	—0. 00004175	—0. 00020075	+0.00010	0. 00496	
2 — 6	+0,00000001	-0.00000134	-0.00000972	0.0000341	—0. 00032	+0.00006	
2 — 7	0. 0000000	0, 00000006	—0.00000012	-0.0000027			
3 + 3	+0.00000001	0.00000000	+0.00000108	+0. 00000068			
3 + 2	+0.00000012	—0, 00000027	+0.00001305	0.00002483	+0.00038	-0.00072	
3+ 1	0.00000760	0.0000551	—0.00054159	—0. 00020514	0. 01084	0.00313	
3 0	0. 00010753	+0.00047141	0. 00110240	+0.01044997	0. 00353	+0. 12632	
3 — 1	+0.00790442	0. 00241147	+0. 11262276	-0. 03111197	+0. 932828	0. 277793	
3 — 2	—u. 03299484	—0. 04246351	—o. 37777494	—o. 51550556	—2. 496 7 81	3. 446378	
3 — 3	0. 06747291	+0.09335838	—o. 76188256	+1.05805306	-4. 5597°	+6. 31032	
3 — 4	-0.00705343	+0.00296843	—o. o2oo9453	+0.04618699	+0.41605	+0. 42870	
3 - 5 3 - 6	0. 00045060	-0.00001077	-0.00175177	+0.00005193	+0.01765	0. 02808	
1 ° 1	-0.00002521	0. 00000696	-0.00018823	+0.00000271	0.00219	0, 00066	
3 - 7 $3 - 8$	0.00000133	-0.0000061	-0.00000757	+0.00000181	-0.0003	+0.0002	
3 - 8	0. 00000007	0, 00000005					
4 + 2	+0.00000001	0.0000002	+0.00000251	—o. ooooo183			
4+ 1	-0.00000042	-o. oooooo78	0. 00004348	—0. 00005072	0.0011	-0.0011	
4 0	0.00002873	+0.00003023	-o. ooo75153	+0.00102973	-0. 01009	+0.01664	
4- 1	+0.00081742	+0.00021726	+0.01612695	+0.00453965	+o. 174970	+0.043006	
4- 2	0.001089010	0. 007906123	—o. 01234856	o. 12748736	o. 1 03 061	—1. 086030	
4 — 3	0. 03074857	+0.01527037	—0. 456020 7 4	+0. 21266233	—3. 39363 5	+1.542189	
4 — 4	+0. 03589089	+0.04045233	+0.51711042	+0. 57889510	+3.59852	+4. 03385	
4 — 5	+0.00084473	+0.00493552	+0.02593559	+0.03856237	+0. 3427	—o. o5o5	
4-6	—0. 00009466	+0.00034150	-0.00010393	+0.00256650	0.0058	-0.0072	
4 — 7	-0.00001245	+0.00001929	-0. 00004875	+0.00019287	0.0005	+0.0010	
4 — 8	0,00000100	+0.00000097	0.000010	+0.000012	+0.0001	+0.0001	
4-9	0.0000006	+0.0000005					
5 + 2			+0.00000041	-0.0000027			
5 + 1			-0. 00000171	-0.0000741			
5 0	-0.00000354	+0. 00000104	—o. ooo13788	+0.00006204	-0. 0025	+0.0014	
5 ·- I	+0.00005805	+0.00006172	+0.00153582	+0.00162309	+0.02154	+0.02075	
5 — 2	+0.0003989933	0. 0009429136	+0.00912144	-0. 01926179	+0, 09521	-0. 20382	
5 — 3	-0. 006537862	0. 000314216	0. 12040911	-0. 01060942	1. o8796	—0. 10894	
5 4	+0.00527436	+0.02027174	+0, 08490433	+0.35670452	+o. 66777	+2.95066	
5 — 5	+0.02272923	-0.01243714	+0. 39452729	-0. 21861518	+3. 1465	1.7469	
5 — 6	+0.00309749	+0.00017604	+0.0373479	-0.0084018	+o. 1198	—0. 2063	
5 — 7	+0.00022496	+0.00012675	+0.0025727	+0.0007449	+0.0033	0.0004	
5 — 8	+0.00001228	+0.00001409	+0.000158	+0.000106	+0.0009	+0.0005	
5 — 9	+0.00000052	+0.00000101	+0.000009	+0.000007			

Arg.	<u>w</u> △		$\left(\frac{\mathbf{a}'}{\triangle}\right)$	3	(<mark>a</mark> ′)5
	CO#6	sin.	cos.	sin.	cos.	sin.
i' i 6 o	0. 00000032	o. ooooooo7	-0.0000175	0, 0000014		
6 1	+0.00000170	+0.00000822	+0,0000633	+0.0002772	+0.0012	+0.0045
6- 2	+0.0000984225	-0.0000711576	+0.00264710	-0.00177064	+0.03351	-0. 02311
6 3	0. 00085675	—o. ooo55099	—о. о188698	—0. 0134388	—o. 20307	—o. 14769
6-4	0.00118097	+0.00474846	—o. o285594	+o. 0991728	o. 2938	+ 0. 9612
6— 5	+0.01241237	—o. 00054155	+o. 2533389	0. 0066021	+2. 3174	—o. o348
6 6	-0. 00334080	0. 01209833	—o. 0703527	0. 2473777	0. 6403	2. 2278
6- 7	+0.00051911	—o. 00178506	+0. 0022716	—o. 0286114	o. o867	0. 1660
6 8	+0.00012209	0, 00013046	+0.0012304	—o. 0020526	+0.0013	0. 0083
6 9	+0.00001267	0. 00000623	+0.0001426	-o. 0001228	+0.0005	0.0008
6 — 10	+0.00000076	0.00000013	+0.0000182	o, ooooo4o		
6 11	+0.00000005	+0.00000002				
7 0			-o. ooooo17	—0. 0000009		
7- 1	—0.00000027	+0.00000078	0. 0000104	+0.0000334	0.0001	+0.0006
7 2	+0.00001367	—0.00000107	+0.000443I	-0.000023I	+o. oo67	-0.0005
7 – 3	-0.00006343	0.00012601	-0.0015734	0. 0035468	0.0198	-0. 0454
7 — 4	0. 00061694	+0,00065304	-o. o162048	+0.0156279	—о. 1874	+0. 1744
7-5	+0.00310773	+0.00148474	+0.0728272	+0.0377925	+0.7594	+0.4114
7 — 6	+0.00122992	-0.00711895	+0. 0335344	0. 1655894	+0. 3306	-1.6647
7 - 7	o. oo611335	+o. ooo 19169	—0. 144245 3	+0.0060336	-1.4512	+ 0. 0688
7 — 8	0. 00094401	—0. 00053174	o. 0189536	-o. 00693 2 0	—0. 1484	+0.0048
7-9	0. 00006403	0. 00009925	—o. oo13549	-0.0013939	o. oo93	0, 0048
7 — 10	0. 00000770	-0.00001066	—о. 0000604	—o. ooo1589	0. 0007	+0.0010
7 — 11	-0. 00000051	—0. 00000099	—o. oooooo5	- 0.0000141		
7 — 12	—0. 00000002	—0. 00000008				
8— I			-0. 0000029	+0.0000021		
8- 2	+0.0000013	+0.0000007	+0.0000521	+0.0000272	+0.0009	+0.0005
8-3	+0.00000131	-o. oooo180 7	+0,0000700	_o. ooo <u>5</u> 898	+0.0010	-o. oo88
8- 4	0.0001368	+0.0000409	-0, 0040826	+0.0009939	—o. o538	+0.0120
8 5		+0.0005943	+0.0109759	+0.0168853	+0. 1277	+0. 2061
8 — 6	+0.0014097	0. 0018469	+0. 0389561	-0. 0480294	+o. 4528	—o. 5379
8- 7	-o. oo3828 5	—o. oo15701	—o. 1000754	-0. 0424509	1.0987	—o. 4782
8 — 8	—o. ooo6357	+0.0029199	o, o1592 o	+0.078347	0. 1 698	+0.8739
8- 9	0. 0004220	+0.0004628	-o. 007732	+0.011120	<u> </u>	+0. 1078
8 — 10	—0. 0000725	+0.0000260	<u> </u>	+0.000721	0.0067	+0.0070
8 — 11	-0. 0000075	—0, 0000006	—0. 000139	+0.000012	—o. ooo8	+0.0003
8 — 12	0. 0000004	—0.0000004	—o. 000011	-0.000004		

Arg.	<u>s</u>	<u>'</u>	(a/Z	<u>('</u>)³	$\left(\frac{\mathbf{a}'}{\triangle}\right)^5$		
Arg.	cos.	sin.	cos.	sin.	008.	sin.	
i' i 9 2			+0.0000042	+0.0000063			
9-3	+0.0000013	-o, ooooo18	+0.0000518	-0.0000678	+0.0009	-0.0012	
9 4	-0.00002004	0. 00000492	—o. ooo6759	-0. 0002028	-0.0101	0. 0032	
9- 5	+0.0000137	+0.0001308	+0.0002240	+0.0041555	+0.0017	+o. o568	
9- 6	+0.0005105	-0. 0002285	+0.0156959	-0.0062787	+0. 2025	-0. 0757	
9 — 7	0. 0009886	-0.0011518	-0.0282181	—o. o346847	-o. 3379	-0.4310	
9 — 8	0. 0013426	+0.0019186	0. 039794	+0.055715	o. 4826	+0.6645	
9-9	+0.0013036	+0.0006601	+0.039393	+0.019050	+0.4842	+0. 2267	
9-10	+0.0002004	+0.0002937	+0.005737	+0.006654	+o. o668	+c.0488	
9 — 11	-0.0000052	+ 0. 0000486	+0.000282	+0.001044	+0.0041	+0.0073	
9 — 12	-0.0000015	+0.0000047	-0.000012	+0.000111	+0.0001	+0.0007	
	Ī				l '		
10-3	+0.000000234	-0.00000111	+0.0000108	-0.0000046			
10 — 4	0.0000019808	-0, 0000019503	o. oooo755	-0.0000807	-0.0013	0.0014	
10-5	—o. ooooo86o	+0.00001932	-0.0003480	+0.0006794	o. oo55	+0.0104	
10- 6	+0.0001121	+0,0000099	+0.003803	+0.000523	+0. 0543	+0.0090	
10 - 7	0. 0000885	-0.0003999	0. 002426	-0. 0I 3274	o. o288	0. 1812	
10 8	-0. 0008504	+0.0004610	-0. 027830	+0. 014248	—o. 3692	+0.1812	
10 — 9	+0.0008799	+0.0009726	+0. 028136	+0.031559	+0. 3625	+0.4118	
10 — 10	+0.0004779	0. 0005308	+0.015439	0. 017969	+0. 2014	0. 2430	
10 — 11	+o. ooo1866	-0.0000712	+0. 004959	0. 002484	+0.0463	0. 0354	
10 12	+0,0000302	+0.0000035	+0.000757	0. 000008	+o. oo66	0.0015	
10 — 13	+o. 0000026	+0.0000032	+0. 000080	+0. 000029			
11-4	0. 000000096	-0.00000344	0, 000004	-0.000016			
11 5	—0.0000026	+0.0000019	-0. 000108	+0.000069	-o. oo18	+0.0012	
11 6	+0.0000164	+0.0000115	+o. ooo6o6	+0.000468	+0.0095	+0.0077	
11 7	+0.0000256	-0.0000875	+0. 001082	0. 003163	 -0. 0176	—0. 0470	
11 — 8	0. 0002897	+0.0000035	0. 010335	0. 000236	— 0. 1492	o. oo68	
11 — 9	+o. 0001682	+0.0005804	+0.005485	+0.020559	+0.0727	+0. 2907	
11 — 10	+0.0006370	-0. 0003533	+0. 022510	0. 012355	+0. 3152	0. 1710	
11-11	0. 0001860	-0. 0002949	—0. 007 090	—0. 010545	-o. 1059	0. 1499	
11 — 12	-0. 0000139	0, 0001101	-0.000743	0. 003345	o. o146	o. o369	
11 - 13	+0.0000062	0.0000175	+0.000122	0.000502			
11 - 14	+0.0000013	-0.0000015	+0.000037	-0.000052		l	
12 — 5	-0. 00000047	+0.0000005	-0. 000020	+0.000001			
12 — 6	+0.0000016	+0.0000029	+0.000052	+0.000128	+0.0008	+0.0021	
12 - 7	+0.0000126	-0.0000123	+0.000539	-0.000480	+0.0003	0. 002 1 0. 007 5	
12 - 8	0, 0000626	-0.0000332	0. 002394	-0.001405	-0. 0375	0.00/3 0.0234	
12 — 9	0. 0000390	+0.0001956	-0.001737	+0.007464	-0.03/3 -0.029I	+0.1140	
12 — 10	+0.0003701	-0. 0000240	+0.014134	- 0.000643	+0. 2124	—0. 0066	
12 — 11	-0.0001088	-o. ooo386o	-0.004134	0.014787	-0. 2124 -0. 0613	-0. 2210	
12 — 12	0. 0001638	+0.0000463	-0. 006451	+0.002072	—0. 0013 —0. 0991	+0. 0308	
12 13	0. 0000609	0. 0000071	-0.002051	o. oooo5o	J. 0991	, 5, 5,00	
12 — 14	-0.0000094	—o. ooooo59	—0. 002051 —0. 000295	0.000159			
12 15	-0. 0000006	—o. oooooog	0.000293 0.000031	0.000139 0.000034			
			-0.00031	0.00034			

Arg.	<u>a</u>	7.	$\left(\frac{\mathbf{a}'}{\triangle}\right)$)³	(a')5 △)5		
Ang.	cos.	sin.	COB.	sin.	cos.	sin.	
š' š	-						
13- 6	0.0000000	+0.0000006	0.00001	+0.00003		l l	
13- 7	+0.0000031	0,0000008	+0.00014	0. 00003			
13 — 8	—0. 000008 3	—0. 0000126	—0. 00032	0. 00056			
13- 9	o. oooo336	+0.0000410	—o. oo147	+0.00165			
13 — 10	+0.0001226	+0.0000529	+0.00500	+0.00233			
13-11	+0.0000349	—0. 0002218	+0.00159	-0.00910			
13 — 12	0. 0002197	+0.0000086	-0.00907	+0.00034			
13 — 13	-0.0000022	+0.0000835	+0.00006	+o. oo36o			
13 — 14	—0.0000119	+0.0000315	—0. 000 33	+0.00115		l i	
13 — 15	-0.0000045	+0.0000050	0.00013	+0.00015			
14-7	+0.0000004	+0.0000001	+0.00002	+0.00001			
14 8	-0, 0000002	0. 0000029	0, 00000	-0.00013			
14 — 9	-0.0000114	+0.0000044	0, 00052	+0.00018			
14-10	+0.0000234	+0.0000300	+0.00102	+0.00137			
14 — 11	+0. 0000509	-0.0000713	+0.00233	-0.00309			
14 — 12	-0. 0001248	-0.0000499	0. 00545	-0. 00227			
14-13	-0. 0000241	+0.0001177	0. 00105	+0.00521			
14 14	+0.0000387	+0.0000139	+0.00185	+0.00055			
14 — 15	+0.0000152	+0.0000107	+0.00062	+0.00036			
14 — 16	+0.0000021	+0.000032	+0.00008	+0.00011			
15 — 8	+o. 0000002	0. 0000005	+0.00001	-0.0000I			
15 — 9	0. 0000024	-0.0000004	0.00012	0.00002			
15 — 10	+0. 0000014	+0.0000094	+0. 00006	+0.00045			
15 — 11	+0.0000251	-0.0000122	+0.00119	—o. ooo55			
15 — 12	-o. oooo441	0. 0000421	-0.00175	-0.00202			
15 — 13	—o. oooo474	+0.0000655	0. 00217	+0.00306			
15 — 14	+o. oooo650	+0, 0000283	+0.00280	+0.00132			
15 15	+0.0000141	-0.0000159	+0.00061	0.00083			
15 — 16	+o. 0000081	o. ooooo66	+0.00030	—0, 00029			
15 — 17	+0.0000020	—0. 0000006	+0.00008	-0.00002			
16 — 9	-0, 0000004	-0.000003	-0.00001	0.00002			
16 — 10	-0.000008	+0,0000022	—0. 00003	+0.00011			
16 — 11	+0.0000072	+0.0000001	+0.00037	+0.00002			
16 — 12	0. 0000048	-0.0000182	—0. 00022	-0.00093			
16 — 13	0. 0000314	+0.0000178	—o. oo158	+0.00085			
16—14	+0.0000314	+0.0000347	+o. 00156	+0.00173			
16 — 15	+0.0000230	0. 0000274	+0.00114	-0,00132			
16 — 16	0. 0000052	-0.0000092	o. 00032	-o. ooo61			
16 — 17	—o. 0000025	-o. ooooo51	-o. ooo13	-0.00025			
16 — 18	0. 0000002	0.0000013	0,00001	0.00007			

		-		$\left(\frac{\mathbf{a}'}{\triangle}\right)^7$				
Arg.	cos.	sin.	Arg.	cos.	sin.	Arg.	cos.	sin.
Arg. i' i 0 0 0-1 0-2 0-3 0-4 0-5 1+4 1+3 1+2 1+1 1 0 1-1	30. 641 - 5. 575 - 2. 560 + 0. 212 + 0. 017 - 0. 004 0. 000 + 0. 049 - 0. 280 - 3. 120 + 19. 869 + 11. 984	sin. -18.040 + 1.525 + 0.247 - 0.021 - 0.001 + 0.005 - 0.465 + 3.019 +11.485 -56.928	Arg. i' i 3-1 3-2 3-3 3-4 3-5 3-6 3-7 4+1 4 0 4-1 4-2 4-3	+ 6.746 -14.840 -24.097 + 5.541 + 0.274 - 0.054 0.000 - 0.014 - 0.107 + 1.573 - 0.826 -21.229	6in. - 2. 180 -20. 378 +33. 095 + 3. 332 - 0. 593 - 0. 015 + 0. 004 - 0. 020 + 0. 197 + 0. 326 - 7. 847 + 9. 580	i' i 6 - 6 6 - 7 6 - 8 7 - 2 7 - 3 7 - 4 7 - 5 7 - 6 7 - 7 8 7 - 9 8 - 2	- 4. 450 - 1. 528 + 0. 008 + 0. 078 - 0. 204 - 1. 658 + 6. 108 + 2. 618 - 11. 012 - 0. 754 + 0. 016	-15. 528 - 0. 427 + 0. 082 - 0. 009 - 0. 452 + 1. 537 + 3. 375 - 12. 697 + 0. 537 + 0. 729 + 0. 017
I - 2 I - 3 I - 4 I - 5 I - 6 2 + 3 2 + 2 2 + I 2	-14. 172 + 0. 457 + 0. 174 - 0. 015 - 0. 002 + 0. 003 - 0. 004 - 0. 817 + 2. 932 + 16. 904 - 46. 222 - 2. 212 + 1. 145 - 0. 004 - 0. 006 + 0. 007 - 0. 144 + 0. 018	+ 0. 738 + 1. 856 - 0. 072 - 0. 014 + 0. 003 - 0. 011 - 0. 091 + 0. 218 + 5. 011 - 18. 700 - 20. 468 + 9. 632 + 0. 093 - 0. 104 + 0. 003 - 0. 013 - 0. 034 + 1. 210	4-4 4-5 4-6 4-7 5-1 5-2 5-3 5-4 5-5 5-6 5-7 5-8 6-1 6-2 6-3 6-4 6-5	+20. 788 + 3. 194 - 0. 238 - 0. 017 - 0. 032 + 0. 239 + 0. 789 - 8. 050 + 4. 342 +20. 065 - 0. 547 - 0. 223 + 0. 010 + 0. 016 + 0. 334 - 1. 768 - 2. 298 + 16. 525	+23.456 -2.481 -0.250 +0.023 +0.020 +0.211 -1.775 -0.798 +19.680 -11.090 -2.426 +0.062 +0.031 +0.050 -0.243 -1.265 +7.387 -0.135	8 — 2 8 — 3 8 — 4 8 — 5 8 — 6 8 — 7 8 — 8 8 — 9 8 — 10 9 — 3 9 — 4 9 — 5 9 — 6 9 — 7 9 — 8 9 — 9 9 — 10 9 — 11	+ 0.012 + 0.004 - 0.541 + 1.152 + 3.901 - 8.949 - 1.352 + 0.162 + 0.111 + 0.011 - 0.117 + 0.021 + 1.919 - 2.949 - 4.245 + 4.205 + 0.610 + 0.128	+ 0.006 - 0.102 + 0.121 + 1.887 - 4.542 - 3.971 + 7.163 + 0.783 + 0.026 - 0.016 - 0.035 + 0.582 - 0.696 - 3.907 + 5.757 + 1.925 + 0.128 + 0.065

CHAPTER II.

PERTURBATIONS OF JUPITER AND SATURN ARISING FROM THEIR MUTUAL ACTION AND OF THE FIRST ORDER WITH RESPECT TO DISTURBING FORCES.

The next step in arriving at the proper expressions for the forces which the planets exert on each other is to multiply the function $\left(\frac{\mathbf{a}'}{\triangle}\right)^3$ in its final form, given in the preceding chapter, severally by each of the four factors

$$a^2 \left(\frac{r}{a}\right)^2$$
 $\left(\frac{r'}{a'}\right)^2$ $\frac{r'}{a'}\sin(f' + \Pi')$ $-\frac{r}{a}\sin(f + \Pi)$

We have*

$$\left(\frac{r}{a}\right)^2 = 1 + \frac{3}{2}e^2 - \frac{4}{1}J_{\frac{a}{2}}^{(1)}\cos g - \frac{4}{4}J_{\frac{a}{2}}^{(2)}\cos 2g - \frac{4}{9}J_{\frac{3}{2}e}^{(8)}\cos 3g - \dots$$

with a similar equation for $\left(\frac{r'}{a'}\right)^{1}$.

In addition †

with a similar expression for $\frac{r}{a} \sin (f + \Pi)$.

The numerical expressions for these four factors are (the logarithms of the coefficients are given)

$$\alpha^{3} \left(\frac{r}{a}\right)^{2} = [9.4746164] \qquad \left(\frac{r'}{a'}\right)^{3} = [0.0020422] \\ -2[8.1564087] \cos g \qquad -2[8.7484582] \cos g' \\ -2[6.2375704] \cos 2g \qquad -2[6.8947428] \cos 2g' \\ -2[4.6197410] \cos 3g \qquad -2[5.3420289] \cos 3g' \\ -2[3.1268416] \cos 4g \qquad -2[3.9142411] \cos 4g' \\ -2[2.5553314] \cos 5g'$$

^{*}Auseinandersetzung, Abh. I, s. 175.
† Auseinandersetzung, Abh. I, s. 176.

$$\frac{r'}{a'}\sin(f' + \Pi') = + [8.6965298]$$

$$+ 2[9.6046934]\sin g' - 2[9.4702676]\cos g'$$

$$+ 2[8.0520079]\sin 2g' - 2[7.9174682]\cos 2g'$$

$$+ 2[6.6753852]\sin 3g' - 2[6.5407886]\cos 3g'$$

$$+ 2[5.3725363]\sin 4g' - 2[5.2379055]\cos 4g'$$

$$+ 2[4.1105366]\sin 5g' - 2[3.9758829]\cos 5g'$$

$$-\frac{r}{a}\sin(f + \Pi) = - [8.8188230]$$

$$+ 2[9.3147278]\sin g + 2[9.6578903]\cos g$$

$$+ 2[7.6969195]\sin 2g + 2[8.0399977]\cos 2g$$

$$+ 2[6.2551813]\sin 3g + 2[6.5982173]\cos 3g$$

$$+ 2[4.8872207]\sin 4g + 2[5.2302313]\cos 4g$$

$$+ 2[3.5601085]\sin 5g + 2[3.9931023]\cos 5g$$

The required products are:

Arg.	$\alpha^2 \left(\frac{r}{a}\right)^2$	$\left(\frac{\mathbf{a}'}{\triangle}\right)^3$	$\left(\frac{r'}{a'}\right)^2$	$\left(\frac{\mathbf{a}'}{\triangle}\right)^3$	$\left(\frac{\mathbf{a}'}{\triangle}\right)^3 \frac{r'}{\mathbf{a}'}$ so	in $(f'+\Pi')$	$-\left(\frac{\mathbf{a}'}{\triangle}\right)^3\frac{r}{\mathbf{a}}$	$\sin (f+\Pi)$
Arg.	cos.	sin.	cos.	sin.	sin.	cos.	sin.	cos.
i' i								
0 0	+0.6646384		+2. 20285566			+0. 096539		-0. 139090
0 1	—o. 102240 7 8	0. 09654157	—о. 16606148	o. 14425645	+0.652427	-1.472529	0. 890963	+2.021227
0 — 2	0. 00359271	+0.00729372	-0. 00584431	+0.01027942	+0.092267	+0.044090	-0. 1 42260	—o. 07596o
0-3	+0.00037990	+0.00012406	+0.00050293	+0.00024342	-0. 002049	+0.003890	+0.003572	o. oo658o
0-4	+0.00000398	-0. 00001827	+0.00000947	-0.00002311	-0. 000137	-0.000129	+0.000233	+0.000204
0-5	-0.00000072	-0. 00000007	0, 00000066	0.00000021				
1+4	0. 00000066	+0. 00000240	—0. 00000051	+0.00000398				
1+3	+0.00004553	+0.00001192	+0.00006269	+0.00000476	+0.000439	+0.000255	—o. ooo732	-0.000421
I + 2	+0.00006254	-0. 00095698	-0.00002512	-0.00134143	o. oo6697	+0.009449	+0.010197	-0. 015371
1+1	0.01753370	+0.00317476	—o. 02618290	+0.00508023	0. 163541	0. 133286	+0. 235056	+0. 192100
1 0	+o. 14866616	+0. 15018589	+0. 27948671	+0. 34932553	+1.778166	-1. 266003	1. 318411	+0.910778
1-1	+0. 19097831	0. 95485704	+0. 64138181	—3. 15251634	—0. 159202	-o. 154638	+0. 224895	+0. 204201
I — 2	0. 05391969	+0.04178008	0. 03958295	+0.03481677	+1.029740	+0. 222978	—1. 5 79388	-o. 341385
1 3	+0.00233553	+0.00269350	+0.00466646	+0.00371574	+0.011210	+0.048408	-0. 013547	—о. 078501
1 4	+0.00010439	0.00011490	+0.00024243	-0. 00014058	-0.001063	+0.000140	+0.001990	-0. 000163
1 5	0. 00000614	0. 00000384	0. 00000325	-0. 00000596	+0.000065	-0.000057	-o. oooo87	+0.000093
ı — 6	-0.00000017	+0.0000035	0. 00000009	+0, 00000044				
2+4	0, 00000054	+0.00000019	0, 00000144	+0.00000022				
2 + 3	+0.00000410	+0.0000342	+0.00000596	+0.00000385			0. 000097	+0.000001
2+2	+0.00006102	0. 00009392	+0.00007165	—o. ooo13682	-0.000139	+0.001320	+0.000186	-0. 002105
2 + 1	-0.00204003	0. 00078227	0. 002 95369	-0.00103270	-0. 025483	-0.005037	+0.037735	+0.007827
2 0	+0.00382420	+0. 03034997	+0.00212295	+0.05624290	+0. 1604 07	—о. 328034	o. 159335	+0. 309261
2 I	+0. 17342674	—0. 14490556	+0. 44903301	0. 34483157	+1.144372	+1.070503	—o. 723589	—o. 709105
2 — 2	—o. 58491034	0. 24561672	-1.91960384	0. 82112372	+0. 206918	-0. 144719	-0. 277128	+0. 211746
2 — 3	+0. 01 175029	+0.02297816	o. 01074537	-0.02364232	0. 002108	+0.651351	+0.004800	-1.050101
2-4	+0.00156295	-0.00052038	+0.00225773	0. 00356737	—o. 016195	+0. 026941	+0. 027428	-0. 042361
2 — 5	-0. 00001728	0. 00005498	+0.00002732	-0.00022913	-0.000033	+0.000521	+0.000113	0. 000727
2 — 6	-0. 00000209	+0.00000191	+0.00000010	-0.0000522	+0. 000044	+0.000065	o. 00007 I	-0.000100
2 — 7	+0.00000011	0.00000000	+0.00000029	0.0000052				

Arg.	$\alpha^2 \left(\frac{r}{a}\right)^2$	$\left(\frac{\mathbf{a}'}{\Delta}\right)^3$	$\left(\frac{r'}{a'}\right)^2$	$\left(\frac{\mathbf{a}'}{\triangle}\right)^3$	$\left(\frac{\mathbf{a}'}{\triangle}\right)^3 \frac{\mathbf{r}'}{\mathbf{a}'} \sin$	$n(f'+\Pi')$	$-\left(\frac{\mathbf{a}'}{\triangle}\right)^3 \frac{r}{\mathbf{a}}$	sin (f+II)
	808.	sin.	cos.	sin.	sin.	cos.	sin.	cos.
i' i								
3 + 3	+0.00000020	+0.00000056	+0, 00000037	+0.00000066				
3 + 2	+0,00001141	0. 00000609	+0.00001456	-o. ooooo958	+0.000065	+0.000141	—o. 000097	-0, 000220
3 + I	0. 00016372	-0. 00020324	—0. 00023885	-0. 00027297	0. 002959	+0.000917	+0.004484	0. 001309
3 0	-o. oo186708	+0.00365057	o. oo353956	+0.00589773	-0.002715	-0. 050285	+0.∞1175	+0.055370
3 — I	+0.03915569	-0. 00222274	+0. 08428652	+0.00028893	+0. 375924	+0.099078	—0. 2 97611	0. 084841
3 - 2	—о. 10336968	0. 16849363	—0. 27004 696	0. 46331603	-o. 515184		+o. 321116	-0. 49 5 661
3 — 3	o. 22156586	+0. 32232369	o. 73682965	+1.04910933	+0. 142585	+0. 184461	-o. 210273	-0. 245654
3 - 4	+0.00501813	-0.00130270	0. 04931858	+0.01371360	o . 379900	+0. 082387	+0. 631353	-0. 134324
3 — 5	—0. 0000 9853	-0. 00082735	0. 00352623	-0.00192573	—0. 02454 0	+0.002047	+0.040371	-0. 002909
3 — 6	-0.00002422	-0.00001228	-0.00021055	-0.00012873	-0. 000948	+0.000551	+0.001542	-o. ooo886
3 - 7	+0.000000 92	+0.00000016	—o. ooooo682	-0.0000892			+0.0 00096	0.000109
4+ 2	+0,00000143	0. 00000000	+0.00000182	0.00000021			İ	
4+ 1	-0. 00000491	-0.00003014	-0. 00000857	-0.00004059	- 0. 000249	+0.000267	+0.000393	0. 000390
4 0	-0.00045076	+0.00026387	-0.00072831	+0.00037805	-0.003442	1	+0.003869	+0.006707
4- 1	+0.00507472	+0.00312773	+0.00940728	+0.00669380	+0.064903	1	o. o59831	+0.013548
4-2	+0.00253344	-0.04124030	+0.00977433	-0.09745652		i	+o. 018700	
4-3	—o, 14326266	+0.05695325	-o. 40867444	+0. 15495361	-0. 557465		+0. 301129	
4 - 4	+0. 16040847	+0. 16908990	+0.51593778	+0.55897005		+0. 132894		-0. 194550
4 - 5	+0.00040331	+0.00313047	+0.00384834	+0.05099580	-0. 095862	1	+0. 159746	+0. 348452
4 6	-0.00048955	+0.00010905	-0.00213220		-0.009616	1	+0. 016037	+0.028111
4- 7	-0.00001948	+0.00001147	-0.00019125	+0.00017428	-0.000969	Į.	+0.001616	+0.001256
4 — 8	—o. 00000244	+0.00000011	_0. 000020	+0.000008	-0. 000080	I	+0.000144	+0.000061
5 + I	+0.00000118	-0.0000330	+0.00000128	0. 00000449		ļ		
5 o	-0.00006421	- 0. 00000133	0. 00009593	-0.00000545	-0.000696	—0. 000 369	+ o. 000 866	+0.000518
5— 1	+0.00034972	+0.00075972	+0.00053616	+0.00139932	+0.007133	-o. oo6858	—0. 007 490	+o. oo6686
5 — 2	+0.00440850	-0. 00567722	+o. o1004694	—о. от 168643	+0. 030550	+0.063918	0. 023671	-o. 052800
5 — 3	—o. o3733148	0. 00796436	0. 09376594	—o. 02265121	-0. 252 613	+0.037606	+0. 169414	-0. 021443
5 4	+0. 02138719	+0. 10968672	+0.05795719	+0. 32034193	+0. 036543	0. 333149	-0.021647	+0. 162487
5 - 5	+0. 11594525	—0. 07019864	+0. 38068179	-o. 22146658	o. 112988	_o. o81190	+o. 163516	+0. 103628
5 — 6	+0.00543316	+0.00055559	+0.0414448	+0.0054077	+0. 101134	0 . 080101	—0. 175 942	+0. 135550
5 — 7	+0.00016122	+0.00037740	+0.0025756	+0.0023371	+0.009132	—о. 010846	o. o 15 734	+0.018470
5 — 8	+0.00000202	+0.00002314	+0.000106	+0.000223	+0.000356	-0.001060	0. 000625	+0.001806
5 — 9	0. 00000024	+0.00000050	+0.000002	+0.000015	+0.000007	-0.0000 89	—0. 00000 9	+0.000144
6 o	0.0000065	0. 0000040	-0.0000092	0. 0000058	0.000095	+0.000001	+0.000127	+0.000001
6— і	—0. 0000154	+0.0001100	-0.0000375	+0.0001833	+0.000375	-0. 001292	0. 000480	+0.001392
6— 2	+0.001063053	o. ooo356 5 38	+0.00214318	-o. ooo58631	+0.009983	+0.00701 9	0. 008794	0. 006602
6 — 3	0. 0053004	-0.0054027	0. 0117489	0. 0128985	0. 051937	+0. 039058	+0. 039831	—0. 028 5 49
6 — 4	-o. o11868o	+0.0299111	—o. 0329458	+0.0783205	—o. oб3277	o. 169741	+0. 037431	+0. 107611
6 — 5	+0.0769855	+0.0001624	+0. 2283160	+0.0034555	+0. 182241	—0. 02277 6	0. 07 5 963	+0.009741
6— 6	— 0. 0246439	—o. o732984	o. 0746870	o. 238 75 83	+0.040547	—о. 088585	—o. 05 0329	+0. 125647
6- 7	+0.0016248	-o. 0049578	+0.0103000	-0. 0290922	+0. 057162	+0.044418	—0. 098086	0. 079475
6-8	+0.0003435	0.0001575	+0.0023028	-0.0017425	+0.009136	+0.003838	—0. 01578 3	o. oo6766
6— 9	+0.0000245	—0. 0000012	+0.0002239	-0.0000548	+0.000922	+0.000024	<u> </u>	0.000050
6 — 10	+0.0000032	+0.0000011	+0.0000226	+0.0000042	+0.000075	-0. 000025	-o. 000128	+0.000035
	1							J

Ana	$\alpha^2 \left(\frac{r}{a}\right)^2$	$\left(\frac{\mathbf{a}'}{\triangle}\right)^3$	$\left(\frac{r'}{a'}\right)^2$	$\left(\frac{\mathbf{a}'}{\triangle}\right)^3$	$\left(rac{{\sf a}'}{ riangle} ight)^2rac{r'}{{\sf a}'}$ si	n (f'+Π')	$-\left(\frac{\mathbf{a}'}{\Delta}\right)^3\frac{\mathbf{r}'}{\mathbf{a}}$	sin (f+Π)
Arg.	cos.	sin.	cos.	sin.	sin.	cos.	sin.	cos.
i' i 7 0	- 0.0000005	0, 0000008	0. 0000006	-0.0000008				
7 1	0. 0000091	+0.0000108	0.0000153	+0.0000166	-0. 000042	-0.000172	+0.000036	+0.000201
7 — 2	+0.0001574	+0.0000405	+0.0002875	+0.0000928	+0.001858	+0.000173	-o. oo1804	-0. 000243
7 - 3	0. 0002 5 61	0. 0012874	0. 0004222	—0. 0027746	-0.005250	+0.011804	+0.004611	-0. 009643
7 — 4	-o, oo58602	+0.0041990	0. 0145296	+0.0097964	0. 0 40 5 93	—о. 035851	+o. 028230	+0. 026086
7 — 5	+0.0214993	+0.0134218	+0. 0580492	+0. 0375619	+0. 102594	-o. o65760	—o. 061125	+0. 038835
7 6	+0.0110324	-0. 0500209	+0. 0354100	0. 1498052	+0.035375	+0.090744		-0. 028417
7 - 7	0 . 043 2 461	+0.0042664	—o. 1394246	+0.0100710	+0.0631 06	+0.015946	—о. 089666	0. 015636
7 — 8	0. 0035723	-0. 0021057	—o. 0181881	-0.0112840	—о. о <u>15</u> 975	+0. 036724	+0. 030078	—o. o63868
7 - 9	0.0001067	-0.0003143	-o. ooo9675	0.0020323	—o. ooo775	+0.006593	+0.001481	-o. o11523
7 — to	+0.0000053	0. 0000260	+0.0000061	-0. 0002046	+o. ooo 188	+o. ooo681	-0. 000301	0. 001198
7 — 11	+0.0000011	-0.0000017	+0.0000070	-0.0000156	+0.000037	+0.000054	-0.000067	0. 000093
8 1	0,0000016	+0.0000003	0.0000023	0.0000000	-0,00002	-0.00002		
8 2	+0.0000152	+0.0000163	+0,0000250	+0.0000301	+0.00024	-0.00011	0.00026	+0.00010
8 — 3	+0.0000766	-0.0001932	+0.0001734	-0.0003796	+0.00021	+0.00221	-0.00012	-0.00198
8 - 4	-0.0013823	+0.0000713	-0. 0031357	+0.0000484	-0.01198	-0. 00269	+0.00923	+0,00232
8 - 5	+0.0027912	+0.0057178	+0.0067270	+0.0146239	+0,02084	_o. o3661	-0.01457	+0.02435
8 — 6	+0.0129004	-o. o139732	+0. 0364325	-0. 0384313	+0.05677	+0.05485	—o. o3o57	0. 03146
8 - 7	0. 0301808	-0.0131014	-0.0908832	-0.0410126	-0. 03994	+0.02974	+0.00548	-0.00895
8 — 8	0.0032098	+0.0238263	-0.012682	+0.075973	-0.00189	-0.04217	-0.00107	_o. o5887
8 — 9	-0, 0020423	+0.0021910	-0. 009922	+0.010158	0. 02164	-0. 00326	+0.03826	+0.00739
8 — 10	-0.0002706	+0.0000423	0.001633	+0.000375	0.00425	+0.00066	+0.00752	-0.00104
8 — 11	-0.0000213	-0.000089	0. 000160	0.000043	0.00044	+0.00026	+0.00079	-0.00045
8 — 12	0. 0000010	-0.0000015	-0.000011	-0.000010	''		+0.00005	-0.00007
				10.000018		0.00000		
9 — 2	+0.0000007	+0.0000029	+0.0000009	+0.0000048	+0.00002	-0.00003		
9 - 3	+0.0000249	-0.000181	+0.0000492	-0.0000316	+0.00020	+0.00028	0.00018	0, 00028
9 - 4	-0.0002080	-0.0001179	-0.0004329	-0.0002698	-0, 00226	+0.00067	+0.00190	-0.00050
9 — 5	-0.0001434	+0.0013382	—o. 0004333	+0.0031614	+0,00022	0.01076	-0.00035	+0.00791
9 — 6	+0.0050898	-0.0014450	+0.0133486	-0.0035112	+0.02965	+0.00942	-0.01891	— 0. 00646
9-7	-0.0080781	0. 0110583	-0. 0224950	—0. 0317272	0.02622	+0.04170	+0.01377	0. 02153
9 — 8	0. 0120336	+0.0168420	—0. 037508 →0. 038422	+0.050795	-0.01982	-0. 01454	+0.00313	0.00321
9-9	+0.0122431	+0.0047938	+0.038433	+0.010733	0. 02633	+0.00438	+0.03628	-0,00844
9 — 10	+0.0011494 -0.0000046	+0.0016872 +0.0002109	+0.004953	+0.007662	-0.00147	-0.01174	+0.00143	+0.02121
9-11		1	+0.000019	+0.001196	-0.00110	-0. 00248	+0.00186	+0.00446
9 — 12	0.0000087	+0.0000169	—0. 000052	+0.000115	0. 00026	-0.00025	+0.00045	+0,00046
10 3	+0,0000044	-0.0000003	+0.0000079	-0.000002	+0.00005	+0.00002		
10 — 4	0,0000184	0.0000337	0.0000342	-0.0000700	-0. 00028	+0.00029	+0.00026	-0.00025
10- 5	—o. ooo1567	+0.0001985	—0. 0003664	+0.0004318	-0.00107	-0.00202	+o. ooo8o	+0.00162
10 6	+0.0011787	+0.0003340	+0.002876	+0.000893	+0.00873	0.00162	0.00616	+0.0009 9
10 7	—0. 0003842	-0.0041766	0. 000836	-0. 011183	-0.00212	+0.02192	+0.00155	0. 01344
10 8	—o. oo86730	+0.0039907	—o. o25138	+0.011146	 0. 02833	—o. oo983	+0.01355	+0.00458
10 9	+0.0085693	+0.0094695	+0.025762	+0.029474	+0,00330	-0.01121	+0.00502	0. 00086
10 — 10	+0.0041353	-0. 0057791	+0.013920	-0.017735	-0.00614	-0. 01534	+0.00992	+0. 02083
10 — 11	+0.0012421	-0. 0004888	+0.005366	-0.001951	+o. 00582	-0.00254	0.01083	+0.00379
10 12	+0.0001508	+0.0000358	+0.000809	+0.000168	+0.00129	0.00105	-0. 00242	+0.00179
		1	!					, i

	$\alpha^2 \left(\frac{r}{a}\right)^2$	$\left(\frac{\mathbf{a}'}{\triangle}\right)^3$	$\binom{r'}{\mathbf{a}'}^2$	$\left(\frac{\mathbf{a}'}{\triangle}\right)^3$	$\left(\frac{\mathbf{a}'}{\triangle}\right)^3 \frac{\mathbf{r}'}{\mathbf{a}'} \sin\left(f' + \Pi'\right)$		$-\left(\frac{1}{\Delta}\right)^3 \frac{r}{a} \sin\left(f+II\right)$	
Arg.	cos.	sin.	608.	sin.	sin.	cos.	sin.	DON:
i' i								
11 4	+0,0000002	—o. ooooo59	+0.000001	0.000012	0,0000	+0.0001	0.0000	-0.0001
11 5	0.0000410	+0.0000146	-0.000089	+0.000028	0.0004	-0, 0002	+0.0003	+0.0002
11 — 6	+-o. ooo1686	+0.0001838	+0.000380	+0.000440	+0.0016	0.0013	0.0012	+0.0010
11 7	+0.0004611	0. 0009502	+0.001217	–·o. 002379	+0.0026	+0.0064	-0.0017	0. 0044
11 — 8	-0. 0031808	-0.0003171	—о. 008660	-0.001002	-0. 0150	+0.0018	+0.0088	0. 00 09
11 9	+0.0014625	+0.0063151	+0.004001	+o. 018454	+0.0018	0. 0178	0.0005	+0.0077
11 — 10	+0.0067393	-0, 0038281	+0. 020951	-o. o11377	+0.0054	—0. 0008	+0.0028	+0,0041
11-11	—0. 0024282	-0.0029259	0.007171	0. 009626	+0.0082	-o. oo55	-o. oi io	+o. oo87
11 — 12	0. 0001255	—o. ooo8371	-0, 000410	-0.003438	+0.0023	+0.0024	u. 0034	0.0052
12 5	0. 000007	-o. 000002	-0.000014	0, 000004	-0.0001	0, 0000]	
12 6	+0.000008	+0.000045	+0.000015	+0.000101	+0.0002	-0,0004	0.0001	+0,0003
12 - 7	+0.000194	-0.000126	+0.000476	0. 000294	+0.0014	+0.0012	0,0010	0.0008
12 — 8	0. 000699	-0.000519	-0.001785	-o. oo138o	— 0. 0046	+0.0031	+0.0029	-0.0019
12- 9	—о. 000686	+0.002258	-0.001993	+0,006230	-0.0034	-0. 0106	+0.0018	+0.0053
12 — 10	+0.004300	_o. oooo88	+o. 012646	0.000076	+0.0130	-0.0009	0. 0038	+0.0009
12 — 11	0. 001344	-0.004433	0.003837	-0.013705	-0.0004	+0.0061	-0.0027	+0.0032
12 — 12	0.001838	+0.000830	—o. 006034	+0,001897	+0.0008	+0,0012	0. 0060	0.0043

In order to get the developments of the disturbing forces it is necessary to have the expressions for the action of each disturbing planet on the Sun. In the case of Jupiter disturbed by Saturn this is proportional to the function $a' \frac{r}{r'^2}H$, and, in the case of Saturn disturbed by Jupiter, to the function $a' \frac{r'}{r^2}H$ (the signification of H has been given, page 22). To obtain the periodic developments of these quantities in terms of the mean anomalies of the two planets we employ some of the auxiliary constants of page 22, as well as the Besselian functions. We compute*

$$\begin{split} h &= \alpha k \, \cos \, \mathbb{K} & l = \frac{\mathrm{I}}{2} p \, \cos \, \mathbb{P} \\ h_1 &= \frac{\mathrm{I}}{2} v \, \cos \, \mathbb{V} & l_1 = \frac{\mathrm{I}}{2} v \, \sin \, \mathbb{V} \\ \mathbf{P}_i &= \frac{\mathrm{I}}{i} \left[\, \mathbf{J}_{\frac{ie}{2}}^{(i-1)} - \mathbf{J}_{\frac{ie}{2}}^{(i+1)} \right] & \mathbf{Q}_i = \frac{\mathrm{I}}{i} \left[\, \mathbf{J}_{\frac{ie}{2}}^{(i-1)} + \mathbf{J}_{\frac{ie}{2}}^{(i+1)} \right] \\ \mathbf{P}_i' &= \frac{\mathrm{I}}{i} \left[\, \mathbf{J}_{\frac{ie'}{2}}^{(i-1)} - \mathbf{J}_{\frac{ie'}{2}}^{(i+1)} \right] & \mathbf{Q}_i' = \frac{\mathrm{I}}{i} \left[\, \mathbf{J}_{\frac{ie'}{2}}^{(i-1)} + \mathbf{J}_{\frac{ie'}{2}}^{(i+1)} \right] \end{split}$$

notice being taken that

$$P_0 = -3e$$
 $Q_0 = 0$ $P_0' = -3e'$ $Q_0' = 0$

Then

$$\begin{aligned} \mathbf{a}' \frac{r}{r'^{2}} \mathbf{H} &= \frac{\mathbf{i}}{2} i'^{2} \left[h \mathbf{P}_{i} \mathbf{P}_{i'} \pm h_{1} \mathbf{Q}_{i} \mathbf{Q}_{i'}' \right] \cos \left(\pm i' g' - i g \right) - \frac{\mathbf{i}}{2} i'^{2} \left[l \mathbf{Q}_{i} \mathbf{P}_{i'} \pm l_{1} \mathbf{P}_{i} \mathbf{Q}_{i'}' \right] \sin \left(\pm i' g' - i g \right) \\ \mathbf{a}' \frac{r'}{r^{2}} \mathbf{H} &= \frac{\mathbf{i}}{2} \frac{i^{2}}{\alpha^{3}} \left[h \mathbf{P}_{i} \mathbf{P}_{i'} \pm h_{1} \mathbf{Q}_{i} \mathbf{Q}_{i'}' \right] \cos \left(\pm i' g' - i g \right) - \frac{\mathbf{i}}{2} \frac{i^{2}}{\alpha^{3}} \left[l \mathbf{Q}_{i} \mathbf{P}_{i'} \pm l_{1} \mathbf{P}_{i} \mathbf{Q}_{i'}' \right] \sin \left(\pm i' g' - i g \right) \end{aligned}$$

in which one attributes all positive integral values to i and i', and takes the double sign in both significations.

^{*}Auseinandersetzung, Abh. I, s. 177, and Gegenseitige Störungen des Jupiter und Saturn, s. 46.

The numerical values being substituted, we have

 $\log h = 9.0480387$ $\log l = 9.7266962$ $\log h_1 = 9.0472930$ $\log l_1 = 9.7264665$ $\log P_0 = 9.1605535n$ $\log P_0' = 9.2257502n$ $\log P_1 = 9.9996208$ $\log P_1' = 9.9994880$ $\log Q_1 = 9.9998736$ $\log Q_1' = 9.9998294$ $\log P_2' = 8.4466886$ $\log Q_2 = 8.3820653$ $\log Q_2' = 8.4471439$ $\log P_2 = 8.3817282$ $\log P_3 = 6.9399478$ $\log Q_3 = 6.9403271$ $\log P_3' = 7.0700000$ $\log Q_3' = 7.0705212$ $\log Q_4 = 5.5723665$ $\log P_4 = 5.5719618$ $\log P_4' = 5.7671259$ $\log Q_4' = 5.7676723$ $\log Q_{5}' = 4.5056725$ $\log P_5 = 4.2448328$ $\log Q_5 = 4.2452543$ $\log P_5' = 4.5051033$ $\log P_6 = 2.9437$ $\log Q_6 = 2.9441$ $\log P_6' = 3.2690$ $\log Q_6' = 3.2696$

Arg.	$-\mathbf{a}'\frac{1}{r}$	$r_{ m 2}{ m H}$	—a'	$rac{r^{'}}{r^{2}} ext{H}$
	. cos.	sin.	cos.	sin.
i' i I O 2 O 3 O	+0. 0080 7 328 +0. 00090430 +0. 00008547	0. 03853181 0. 00431712 0. 00040808		
4 0 5 0 6 0	+0. 00000756 +0. 00000065 +0. 00000005	-0.00003612 -0.00000309 -0.0000026		
-3-I -2-I -I-I 0-I	+0. 00000003 -0. 00000054 -0. 00001944	-0.0000019 +0.00000187 +0.00008644	+0.0000002 -0.00000083 -0.00011995 +0.05790623	—0. 00000013 +0. 00000288 +0. 00053340 —0. 27646210
1 — I 2 — I 3 — I 4 — I	0. 11144785 0. 01248502 0. 00118010 0. 00010445	+0. 53209260 +0. 05960803 +0. 00563425 +0. 00049871	0. 68772890 0. 01926083 0. 00080914	+3. 28346820 +0. 09195819 +0. 00386313
5 — I 6 — I 7 — I	-0. 00000893 0. 00000075 0. 00000006	+0.00004262 +0.00000356 +0.0000030	0. 00004029 0. 00000220 0. 00000013 0. 00000001	+0.00019234 +0.00001052 +0.00000061 +0.00000004
-3-2 -2-2 -1-2 0-2	+0. 00000002 0. 00000021	+0.0000018 +0.0000333	+0.0000001 +0.0000010 -0.0000513 +0.00558332	+0.0000002 +0.0000114 +0.0008217 -0.02666167
1 - 2 $2 - 2$ $3 - 2$ $4 - 2$		+0.01282735 +0.00143699 +0.00013583 +0.000012023	—0. 06631731 —0. 00185731 —0. 00007803 —0. 000003885	+0. 31662297 +0. 00886747 +0. 00037253 +0. 000018548
5-2 $ 6-2 $ $ -2-3$	—0. 0000002152 —0. 0000000180	+0.0000010276 +0.0000000859	-0. 0000002125 -0. 00000001 +0. 00000001	+0.0000010145 +0.00000006 +0.00000010
0-3 1-3 2-3		+0.0000014 +0.00046385 +0.00005196	—0. 00000016 +0. 00045426 — 0. 00539573 —0. 00015112	+0. 00000794 -0. 00216936 +0. 02576117 +0. 00072147
3-3 4-3 5-3	0. 00000103 0. 00000009 0. 000000008	+0.00000491 +0.00000043 +0.000000037	0. 00000635 0. 00000032 0. 00000002	+0.00003031 +0.00000151 +0.00000008

Arg.	 8	$\mathbf{r}'rac{r}{r'^2}\mathbf{H}$	$-\mathrm{a}'rac{r'}{r^2}\mathrm{H}$		
	cos.	sin.	cos.	sin.	
-2-4 -1-4 0-4 1-4 2-4 3-4 4-4 -1-5 0-5 1-5 2-5 3-5 0-6 1-6 2-6	-0. 00000416 -0. 00000047 -0. 00000004 -0. 00000020 -0. 00000002	+0.00001988 +0.00000223 +0.00000021 +0.00000094 +0.00000010	0. 00000000 0. 00000000 +0. 00003461 -0. 00041111 -0. 0000151 -0. 0000002 0. 00000000 +0. 00000255 -0. 00000035 -0. 00000003 +0. 00000018 -0. 00000018 -0. 00000018	+0.0000001 +0.0000003 -0.00016530 +0.00196280 +0.0000231 +0.00000009 +0.00000004 -0.0001216 +0.00014440 +0.00000013 -0.00000088 +0.00001040 +0.00000029	

On account of the action of the disturbing planets on the Sun it is necessary to include in the disturbing forces perpendicular to the planes of the orbits, respectively in the motions of Jupiter and Saturn, terms which are proportional to

$$-\left(\frac{\mathbf{a}'}{r'}\right)^2 \sin\left(f^{\mathbf{v}} + \Pi'\right)$$
 and $\frac{\mathbf{I}}{\alpha^3} \left(\frac{\mathbf{a}}{r}\right)^2 \sin\left(f + \Pi\right)$

We have*

with a similar formula for $\left(\frac{a'}{r'}\right)^2 \sin\left(f' + \Pi'\right)$. The numerical values being substituted, we get:

Arg.	$-\left(\frac{\mathbf{a}'}{r'}\right)^2\sin \theta$	$(f' + \Pi')$	Arg.	$\frac{1}{\alpha^3} \left(\frac{\mathbf{a}}{r}\right)^2 \sin\left(f + \Pi\right)$		
	sin.	cos.		sin.	cos.	
i' i 1 0 2 0 3 0 4 0 5 0	-0. 804866 -0. 090177 -0. 008524 -0. 000755 -0. 000064	+0. 590606 +0. 066154 +0. 006253 +0. 000554 +0. 000047	$ \begin{array}{ccccccccccccccccccccccccccccccccccc$	+2. 547437 +0. 245672 +0. 019989 +0. 001523 +0. 000112	—5. 613916 —0. 541294 —0. 044039 —0. 003355 —0. 000247	
6 0	—o. ooooo5	+0.000004	0-6	+0.000008	-0.000018	

^{*}Auseinandersetzung, Abh. I, s. 178.

Certain factors dependent upon the masses are here necessary. We put

$$\mu = \frac{m'}{1 + m} \alpha \frac{a}{a} \qquad \qquad \mu' = \frac{m}{1 + m'} \frac{a'}{a'}$$

These factors being expressed in seconds of arc by multiplying by the radius in seconds, we have for Jupiter

 $\log \mu = 1.5063000$

 $\log (\mu \alpha \sin J) = 9.5836560$

and for Saturn

 $\log \mu' = 2.2938045$

 $\log (\mu'\alpha \sin J) = 0.3711605$

For Jupiter, then, we compute the three functions

$$\begin{split} a\Omega &= \mu \left[\frac{\mathbf{a}'}{\triangle} - \mathbf{a}' \frac{\mathbf{r}}{\mathbf{r}'^2} \mathbf{H} \right] \\ ar \frac{d\Omega}{dr} &= \mu \left[-\frac{\mathbf{I}}{2} \left(\frac{\mathbf{a}'}{\triangle} \right)^3 \left(\alpha' \frac{\mathbf{r}^2}{\mathbf{a}^2} - \frac{\mathbf{r}'^2}{\mathbf{a}'^2} \right) - \frac{\mathbf{I}}{2} \frac{\mathbf{a}'}{\triangle} - \mathbf{a}' \frac{\mathbf{r}}{\mathbf{r}'^2} \mathbf{H} \right] \\ a^2 \frac{d\Omega}{dZ} &= \mu \alpha \sin \mathbf{J} \left[\left(\frac{\mathbf{a}'}{\triangle} \right)^3 \frac{\mathbf{r}'}{\mathbf{a}'} \sin \left(f' + H' \right) - \left(\frac{\mathbf{a}'}{\mathbf{r}'} \right)^2 \sin \left(f' + H' \right) \right] \end{split}$$

and for Saturn the three functions

$$\begin{aligned} \alpha'\Omega' &= \mu' \left[\frac{\mathbf{a}'}{\triangle} - \mathbf{a}' \frac{r'}{r^2} \mathbf{H} \right] \\ \alpha'r' \frac{d\Omega'}{dr'} &= \mu' \left[\frac{\mathbf{I}}{2} \left(\frac{\mathbf{a}'}{\triangle} \right)^3 \left(\alpha^2 \frac{r^2}{\mathbf{a}^2} - \frac{r'^2}{\mathbf{a}'^2} \right) - \frac{\mathbf{I}}{2} \frac{\mathbf{a}'}{\triangle} - \mathbf{a}' \frac{r'}{r^2} \mathbf{H} \right] \\ \alpha'^2 \frac{d\Omega'}{dZ'} &= \mu' \alpha \sin \mathbf{J} \left[- \left(\frac{\mathbf{a}'}{\triangle} \right)^3 \frac{r}{\mathbf{a}} \sin \left(f + \Pi \right) + \frac{\mathbf{I}}{\alpha^3} \left(\frac{\mathbf{a}}{r} \right)^2 \sin \left(f + \Pi \right) \right] \end{aligned}$$

The quantities $a\Omega$ and $a'\Omega'$ are, moreover, differentiated severally with respect to g and g'. For Jupiter the three functions are:

Arg.	a^{d}	$rac{d\Omega}{dg}$	$urrac{d\Omega}{dr}$ $a^2rac{d\Omega}{dZ}$			lΩ IZ
	sin.	cos.	cos.	sin.	sin.	cos.
i' i o o o o - 1 o - 2 o - 3		+0. 1681294 -0. 017801 -0. 001147	+7. 174462 -0. 8698000 -0. 031923 +0. 001893	-0. 6813978 +0. 043448 +0. 001551	+0. 2501428 +0. 035375 -0. 00079	+0. 037014 -0. 5645727 +0. 016904 +0. 00149
0- 4 1+ 4	+0.000037	-0.00001	+0.000083 +0.000002	—0. 000078 —0. 000025	-0.00005	0. 00005
1+3 1+2 1+1 1 0 1-1 1-2 1-3 1-4	-0. 000077 +0. 000975 +0. 034578 +0. 448653 +0. 239298 +0. 029583 +0. 002181	-0.000071 -0.002108 +0.005301 +2.408872 -0.292616 -0.029277 -0.001338	+0.000262 -0.001173 -0.122401 +1.338747 +1.637557 +0.040867 +0.027787 +0.001742	-0. 000110 -0. 000580 +0. 023759 +1. 182548 -8. 443179 +0. 432481 +0. 033842 +0. 000378	+0.00017 -0.00257 -0.06270 +0.37316 -0.06104 +0.39480 +0.00430 -0.00041	+0.00010 +0.00362 -0.05110 -0.25895 -0.05929 +0.08549 +0.01856 +0.00005
1-5	+0.000109	-0.000077	+0.000026	+0.000004	+0,00002	0, 00002

Arg.	$a\frac{d}{d}$	$rac{d\Omega}{dg}$	ar	$rac{d\Omega_{c}}{dr}$	$a^2 \frac{d}{d}$	$rac{\Omega}{dZ}$
į	sin.	cos.	cos.	sin.	sin.	cos.
i' i	"	"	11	11	11	"
2+4			- 0.000014	0,000000		
2+3			+ 0.000029	+ 0.000007		1
2 + 2	+ 0.000006	-0.000216	+ 0.000173	— 0. 000643	0.00005	+0.00051
2 + 1	+ 0.003180	o. ooo687	— 0.013093	— o. oo3764	—o. 00977	-0.00193
2 0		0.064480	— 0. 028860	+ 0. 187790	+0.02692	-0. 10041
2 — I	+ 1. 239251	o. o65572	+ 3. 200897	— 0. 371312 — 7. 546567	+0.43875	+0.41043
2-2	—15. 027048 — 0. 601705	+6. 467210 +0. 808199	—17. 669445 — 0. 261124	— 7. 540307 — 0. 610705	+0.07933 -0.00081	0.05549
2 — 3			- 0. 201124 + 0. 012887		-0.00621	+0. 24973
2 - 4	0.014112	+0.063011 +0.004268		0. 040897 0. 002262	-0.00021 -0.00001	+0.01033
2 — 5 2 — 6	- 0.000279 - 0.000002	+0.004268 +0.000258	+ 0.000742 + 0.000035	— 0, 002362 — 0, 000093	+0.00001 +0.00002	+0.00020 +0.00002
1	T 0.00002	-0.00250	,			·
3 + 2			+ 0.000048	— 0. 000052	+0.00002	+0.00005
3+1	+ o. 000243	0.000171	— 0. 001082	— 0.001024	0.00113	+0.00035
3 0			— o. o22363	+ 0.015394	-0.00431	—o. o1688
3 — I	+ 0. 215749	-0. 103402	+ 0. 559338	+ o. 259753	+0. 14413	+0.03798
3 - 2	2. 119094	+2.716155	— 2. 1 45503	— 4. 044090	-0. 19752	+0. 32525
3 — 3	— 6. 4946 7 3	—8. 986642	— 7. 18 <u>3</u> 684	+10.161867	+0.05467	+0.07072
3 — 4	- o. 905238	—o. 380993	— o. 758540	+ 0. 193284	0. 14566	+0.03159
3 — 5	— o. 072287	+0.001728	— o. 047760	— 0. 017444	0. 00941	+0.00078
3 — 6	o. oo4853	+0.001340	0. 002585	0.001756	0. 00036	+0.00021
3 - 7	— 0.000299	+0.000137	— 0, 000103	— 0.000136		
4+ 1	+ 0.000013	0. 000025	0. 000052	— 0.000155	-0.00010	+0.00010
4 0			0. 003749	+ 0.000188	-0.00161	0. 00187
4- 1	+ 0.022875	—0. 022972	+ 0. 053040	+ o. 069724	+0.02488	—о. 0063 6
4 — 2	— o. 0700420	+o. 5065620	+ 0. 133551	— 0. 77462 <u>5</u>	-0.00731	+o. 12789
4-3	— 2. 959698	—1. 469884	— 3. 764 5 70	+ 1.327203	0. 21374	0. 07367
4-4	+ 4.606216	<u>—5. 191627</u>	+ 5.127778	+ 5.605672	—o. o5o96	+0.05095
4 5	+ o. 135515	—o. 79177 7	+ 0.041715	+ o. 688698	o. o3675	o. 07855
4 6	o. o18223	0. 065741	— o. o24833	+ 0.044863	<u> </u>	-o. oo639
4 - 7	— o. 002796	—o. 004332	— o. oo2556	+ 0,002303	-0, 00037	-0.00029
4-8	— o. 000257	0. 000249	— 0.000311	+ 0.000111	—0. 00003	-o. oooo r
5 0			— 0.000431	— ი. 000182	-0.00029	-0.00012
5 — I	+ 0.001576	0, 003348	+ 0.001773	+ 0.010638	+0.002735	0. 002629
5 — 2	+ 0. 02558947	+0.06044055	+ 0. 0840463	— o. 081 2 427	+0.01171	+0.02451
5 — 3	— o. 6292999	+0.0302412	— o. 800463	— o. 230570	—o. 096852	+0.014418
5 — 4	+ 0.676908	2. 601663	+ 0. 502058	+ 3.054213	+0.01401	—о. 12773
5 — 5	+ 3.646320	+1.995219	+ 3.822384	— 2. 227183 [.]	-0.04332	0. 03113
5 — 6	+ o. 596295	—о. 033889	+ 0. 528020	+ 0.075013	+0.03877	-0.03071
5 7	+ 0.050524	<u> </u>	+ 0.035123	+ 0.029403	+0.00350	0.00416
5 — 8	+ 0.003152	—o. 00361 7	+ 0.001476	+ 0.002984	+0.00014	-0.00041
5 — 9	+ 0.000150	-0,000292	0.000000	+ 0.000225	0.00000	-0.00003
6 o			o. oooo38	— o. oooo35	0. 00004	0.00000
6— г	+ 0.000030	—0. 000378	— o. 000404	+ 0.001158	+0.00014	0, 00050
6- 2	+ 0.00631401	+0.00456065	+ 0.0157483	— o. 0025418	+0.00383	+0.00269
				- 1		

Arg.	a	$rac{d\Omega}{dg}$	a	$\frac{d\Omega}{dr}$	$a^{s} rac{d\Omega}{dZ}$		
	sin.	cos.	cos.	sin.	sin.	cos.	
i' i	"	"	"	"	"	"	
6-3	o. o82465	+0.053035	o. o897o6	-0.111411	0. 01991	+0.01497	
6 4	—о. 151565	—o. 609415	—o. 319198	+0.700425	-0. 02426	—o. o6508	
6 5	+1.991245	+0. 086878	+2. 228580	+0.061513	+0.06987	-o. oo873	
6 6	—0. 643134	+2. 329039	0. 749217	-2. 460292	+o. o1555	—o. o3396	
6- 7	+ 0. 116590	+0.400914	+o. 130843	—о. 358535	+0.02192	+0.01703	
6 8	+0.031338	+0.033486	+0.02947	-0.02333	+0.00350	+0.00147	
6-9	+0.003659	+0.001799	+0.00299	0.00076	+0.00035	+0.00001	
6 10	+0.000244	+0.000042	+0. 00030	+0.00005	+0.00003	-0.0001	
7 — I	0,000011	—0. 000025	0. 000096	+0.000090	— 0. 00002	o. oooo7	
7 — 2	+o. ooo877	+0,000069	+0.001867	+o. ooo857	+0.00071	+0.00007	
7 — 3	—o. oo6105	+0.012129	0. 001646	-0. 021836	-0.00201	+0.00452	
7 — 4	o. 079178	o. o83811	—0. 129178	+0.079320	—0. 01556	-o. o1375	
7 — 5	+0. 498555	u. 238188	+o. 5 36494	+0. 363447	+ 0. 03934	-0. 02521	
7 — 6	+0. 236771	+1.370463	+0. 371344	—1. 486 <u>57</u> 7	+o. o1357	十0.03479	
7 - 7	-1. 373021	0. 043052	—1. 444864	+0. 090045	+0.02419	+o. 00611	
7 — 8	<u> </u>	+o. 136486	—0. 2 1932	—0. 13871	—o. 00612	+0.01408	
7- 9	 0. 01848	+0. 02865	0. 01278	0. 02596	<u> </u>	+0.00253	
7-10	-0. 00247	+0.00343	+0.00014	0. 00269	+0.00007	+0, 00026	
7 11	0.00018	+0.00035	+0.00010	-0.00021	+0.00001	+0.00002	
8 2	+0.00008	-0. 00004	+0.00013	+0.00021	+0.00009	—o. 00004	
8- 3	+0.000126	+0.001740	+0.001530	—o. oo2698	+0.00008	+0.00085	
8 4	o. 01756	-0. 00525	0. 02593	0. 00102	0. 00459	-0.00103	
8 — 5	+0. 06808	0. 09534	+o. o5633	+0. 13332	+0.00799	-0.01404	
8 6	+0. 27138	+0. 35555	十0.35490	o. 36274	+o. o2176	+0.02103	
8 — 7	—о. 85986	+o. 35263	— 0. 91239	 0. 42257	—o. o1531	+0.01140	
8 8	—о. 16317	— 0. 74948	—o. 14176	+0. 7 8972	o. ooo73	o. 01617	
8- 9	—o. 12186	—0. 13364	—0. 11965	+0. 12039	0. 00830	—o. 00125	
or —8	-0. 02319	0. 00837	0. 02070	+0.00492	0, 00163	+0.00025	
811	0, 00265	+0.00021	-0.00210	—0. 00050	-0.00017	+0.00010	
8 — 12	0.00023	+0.00019	-0.00014	—0, 00009			
9-3	+0.00013	+0.00017	+0.00037	0.00019	+0, 00008	+0.00011	
9-4	0. 00257	+o. ooo63	0. 00329	0. 00236	o. ooo87	+0.00026	
9 5	+0.00220	0. 02099	o. oo487	+0.02715	+o. oooo8	-0.00413	
9 6	+0.09828	+0.04399	+o. 12430	o. o2948	+o. o1137	+0.00361	
9 — 7	—0. 22203	+0. 25869	—o. 21542	-0.31311	—o. o1005	+0.01599	
9 — 8	— 0. 34462	—0. 49246	о. 38713	+0.51385	—o. oo76o	o. oo557	
9-9	+o. 37643	0. 19061	+0. 39923	+0. 18094	0. 01010	+0.00168	
9 — 10	+0.06430	0. 09423	+0.05780	+0.09114	0, 00056	o. oo45o	
9 — 11	+0.00191	-0.01708	+0.00029	+0.01502	-0. 00042	—o. ooo95	
9 12	-o. ooo58	0. 00181	0. 00069	+0,00149	-0.00010	0.00010	
10-3	+0.000023	+0.000011	+0.000052	+0.000003	∔0. 0000 18	+0.000007	
10 4	°—0. 0002542	+0.0002503	-0.000221	0, 000552	0.00011	+0.00011	
10 5	-o. oo138o	0. 003099	0.003224	+0.003433	0, 000409	0. 000776	
10 6	+0.02158	0.00191	+0.02541	+0.00879	+0.00335	0. 00062	
10- 7	—o. o198 7	+0.08981	0. 00584	—0. 10598	o. ooo81	+0.00841	

Arg.	$arac{d}{d}$	$rac{\Omega}{dg}$	$arrac{d\Omega}{dr}$ $a^2rac{d}{d}$			$rac{\partial \Omega}{\partial Z}$
	sin.	cos.	cos.	sin.	sin.	cos.
i' i 10 — 8 10 — 9 10 — 10	"0. 21828 +-0. 25409 +-0. 15333	-0. 11833 -0. 28085 +0. 17031	 0. 2505 +0. 2617 +0. 1493	+0. 1074 +0. 3053 —0. 1833	" —0. 01086 +0. 00126 —0. 00235	,,, -0. 00377 -0. 00430 -0. 00588
10 — 11 10 — 12 11 — 4	+0.06586 +0.01155 +0.000012	+0. 02513 -0. 00127 -0. 000044	+0. 0632 +0. 0100 0. 000000	-0. 0223 +0. 0021 +0. 00081	+0.00223 +0.00050 -0.00001	—0. 00097 —0. 00040 —0. 00002
11 — 5 11 — 6 11 — 7	0.000417 	0. 000304 0. 00221 +-0. 01965		+0.000160 +0.00391 -0.02153	0. 00014 +-0. 00062 +-0. 00101	0. 00009 0. 00050 0. 00247
11 — 10 11 — 11	—0. 07436 +0. 04857 +0. 20438 —0. 06568	-0. 00090 -0. 16760 +0. 11335 +0. 10415	0. 0832 +-0. 0380 +-0. 2178 0. 0731	-0.0110 +0.1854 -0.1154 -0.1029	0.00574 +-0.00069 +-0.00208 +-0.00315	+0.00068 -0.00681 -0.00029 -0.00213
11 — 12 12 — 5 12 — 6	-0.00512 -0.000075 +0.000308	+0. 04181 -0. 000008 -0. 000558	-0.0045 -0.000106 +0.00006	-0. 0397 -0. 000030 +0. 00083	+0.00087 -0.00003 +0.00006	+0.00091 0.00000 -0.00015
12 — 7 12 — 8 12 — 9	+0. 00283 -0. 01607 -0. 01126	+0.00276 +0.00852 -0.05648	+0.00443 -0.0167 -0.0217	-0. 00250 -0. 0138 +0. 0621	+0.00055 -0.00178 -0.00131	+0.00045 +0.00118 -0.00406
12 — 10 12 — 11 12 — 12	+0. 11875 -0. 03815 -0. 06514	+0. 00770 +0. 13574 —0. 01386	+0. 1324 -0. 0369 -0. 0719	+0.0027 ' -0.1510 +0.0184	+0. 00498 -0. 00015 +0. 00030	-0.00035 +0.00235 +0.00047

The similar quantities for Saturn are:

Arg.	$a' \frac{d}{d}$	$rac{\Omega'}{dg'}$	a'r'	$a'r'rac{d\Omega'}{dr'}$		$a'^2 rac{d\Omega \Omega'}{dZ'}$	
	sin.	cos.	cos.	sin.	sin.	cos.	
i' i	"	"	258. 5835	11	"	,, 0. 32693	
1 0	— 12 . 493747	+ 9.512847	19. 11307	— 24 . 34181	—3. 098926	+2. 140785	
2 0	— 0. 7 49962	+ 2.184496	— 0. 02017	- 3. 09269	o. 37452	+0.72692	
3 0	+ 0.063454	+ 0.278183	+ 0.17506	— o. 26737	+0.00276	+0. 13015	
4 0	+ 0.02260	+ 0.02378	+ 0.03012	— 0. 0I420	+0.00909	+0.01576	
5 0	+ 0.00348	+ 0.00102	+ 0.00347	+ 0.00030	+0.00204	+0.00122	
6 o	+ 0.00038	- o. oooo8	+ 0.00030	+ 0.00018	+0.00030	0.00000	
-4 I	— 0.00033	— o, ooo61	+ 0.00040	- 0.00110	0. 00092	0. 00092	
-3 - 1	— o. 00447	— o. oo317	+ 0.00814	0.00742	0, 01054	o. oo3o8	
-2 - I	— 0.03910	— o. oo882	+ 0.09939	- o. o2598	о. 08870	+0.01840	
—т — т	— o. 23174	0.05542	+ 0.93113	+ 0.31707	o. 55250	+0.45153	
о— 1			+ 18.61128	— 49. 171 98	+3.89354	8. 44462	
1 — 1	+110.60400	+526.42790	—191. 90960	+921.71340	+o. 52862	+0.47997	

Arg.	a' '	$rac{d\Omega'}{dg'}$	a'r'	$rac{d\Omega'}{dr'}$	$a'^2 \frac{d}{d}$	$rac{d\Omega'}{dZ'}$
	sin.	cos.	cos.	sin.	sin.	cos.
i' i	11	11	11	"	11	11
2 — I	—12. 52916	+13.53055	35. 92108	+43.41236	—1. 7008o	-1.66675
3 — 1	— 4. 18693	+ 0.85662	- 5.37518	+ 0.75002	0. 69954	0. 19941
4 — 1	— o. 61143	+ 0. 32227	— o. 51443	- o. 33426	—0. 14063	+0. 03184
5 — I	0. 05492	+ 0.07103	— 0.02448	— 0. 06690	—0. 01762	+0.01572
6 — 1	— o. oo185	+ 0.01042	+ 0.00199	— o. oo789	-0,00113	+0.00327
7 - 1	+ 0.00039	+ 0.00113	+ o. ooo63	— o. ooo65	+0.00008	+0.00047
-3-2			— 0.00032	— o. ooo37	+0.00023	0.00052
- 2 - 2	— 0.00001	- 0.00170	— 0.00101	— o. oo431	0. 00044	0. 00495
<u> </u>	— o. oo396	- 0, 02197	+ 0.00908	— o. o2455	0. 02397	0. 03613
0 — 2			+ 1.34542	— 5. 56528	+0. 24307	—1. 45086
1 — 2	+11.78262	+6o. 65358	15. 08564	+63. 77769	—3. 71235	-0. 80243
2 — 2	+92.73743	—36. 72487	+153. 90350	+68. 39870	—o. 65139	+0.49771
3 2	+19.51631	-24. 83790	+ 19. 62241	+33. 24536	+0.75478	-1. 16505
4 — 2	+ o. 859890	— 6. 205946	— o. 605801	+ 6. 310084	+0.043954	0. 562835
5 — 2	— 0. <u>3922011</u>	— o. 9263581	— o. 59382	+ 0.68394	0. 05564	-0. 12411
6 2	— o. 1161438	— o. o839107	- 0. 115913	+ 0.029608	—o. o2o67	0.01552
7 - 2	— o. 01882	- 0.00147	0.01414	— o. oo5o3	-0. 00424	—o. ooo57
8 — 2	— o. oo2o5	+ 0.00110	0.00108	— 0. 00142	—о. 00060	+0.00024
— 2 — 3			— o. ooo19	+ 0.00006	+0.00023	0.00000
— 1 — 3	T 0.00013	— o. oo168	0.00180	+ 0.00080	+0.00172	-0, 00099
0 — 3			+ o. o7676	— 0.43962	+0.05525	-0.11898
1 — 3	+ o. 98178	+ 5.03581	— I. 33037	+ 4.98239	—0. 03184	0. 18451
2 — 3	+ 2.51439	— 3. 03979	+ 2.79646	+ 5.55794	+0.01128	2. 46826
3 — 3	+39.81953	+55. 10867	+ 57.31092	—80. 6 552 3	-0. 49425	—o. 57741
4-3	+24. 19323	+12.01592	+ 29. 12732	—11. 13988	+0. 70780	→ o. 26828
5 — 3	+ 6.43001	— o. 30895	+ 6. 19333	+ 1.47537	+0. 39821	-0. 05040
6 — 3	+ 1.01114	— o. 6 5 028	+ 0.71845	+ 0.79138	+0.09362	0. 06710
7 - 3	+ 0.08734	— о. 17350	+ 0.02256	+ 0. 15867	+0.01084	—0. 0226 7
8 — 3	0,00206	0. 02844	0.00964	+ 0.02010	0. 00029	0. 00465
9 - 3	- 0,00230	— 0. 00319	- 0.00252	+ 0.00149	0.00042	<u></u> 0. 00065
10 — 3	+ 0.00046	— 0,00022	— o. ooo37	0.00000		
- I - 4	!		— 0.00002	+ 0.00026		
o — 4			+ 0.00624	— 0. 03204	+0.00413	0. 00741
1 — 4	+ 0.07671	+ 0. 38422	— 0.096 <u>5</u> 2	+ 0. 38954	+0.00468	0, 00038
2 — 4	+ 0.04760	— 0. 17240	— o. o5983	+ 0. 35900	+0.06447	o. 099 57
3 — 4	+ 4.16251	+ 1.75303	+ 6.03763	— 1. 7 6834	+1.48400	—o. 31573
44	28. 23897	+31.82790	— 38. 49617	— 42. 32321	+0.40969	-0.45 72 9
5 — 4	— 5. 18733	+19.93726	— 4. 11539	—22. 71167	-o. o5o88	+0. 38193
6-4	+ 1.39378	+ 5.60414	+ 2.18915	— 5. 22807	+0.08798	+0. 25294
7 — 4	+ 0.84946	+ 0.89916	+ 0.91330	— v. 61473	+o. o663 5	+o. o6132
8 4	+ 0.21528	+ 0.06436	+ 0.18587	— o. oo177	+0.02170	+0.00546
9 — 4	+ 0.03548	— o. oo871	+ 0.024077	+ 0.015421	+0.00446	-0.00118
10 — 4	+ 0.0038962	— o. oo38362	+ 0.00175	+ 0.00376	+0.00061	—o. ooo58
11 - 4	+ 0.000208	— o. ooo745	+ 0.000019	- 0. 000429		

i' i o - 5 1 - 5 2 - 5	sin. + 0.00578 + 0.00101 + 0.26592	+ 0.0283I	008. + 0.00050	sin.	sin.	cos.
0— 5 1— 5	+ 0.00578 + 0.00101					
1 - 5	+ 0.00101	+ 0.02831	- 0. 000K0	"	11	"
	+ 0.00101	+ 0.02831		— o. oo238	+0.00026	—0.00058
1 - 3		0	— 0, 00632	+ 0.02866	0. 00020	+0.00022
3 — 5	+ 0.20592	- 0.00891	- 0.00438	+ 0.02055	+0.00027	-0.00171
4 5	0.66461	— 0. 00628	+ 0. 38143	+ 0.10911	+0.09487	0.00684
5-5	-22. 3542I	+ 3.88327 -12.23193	— 0.42190 —28.27227	5. 19296 16. 10040	+0.37548	+0.81904
6-5	—14. 64908	— 12. 23193 — 0. 63903	—26, 27227 —16, 10411	— 0. 27062	+0. 38434 -0. 17855	+0. 24358
7 5	- 4. 27903	+ 2.04434	— 3. 90033	2. 52020	-0. 17855 -0. 14367	+0.02454
8 — 5	— o. 66790	+ 0.93520	0. 42883	— 0. 93435	0. 14307 0. 03424	+0.09128 +0.05723
9 - 5	0. 02425	+ 0. 23150	+ 0.02716	0. 19218	-0. 03424 -0. 00082	+0.03/23 +0.01860
10 5	+ 0.01692	+ 0.03800	+ 0.02146	0. 02484	+0.00188	+0.00381
11 — 5	+ 0.00563	+ 0.00411	+ 0,00492	0.00138	+0.00069	+0.00048
12- 5	+ 0.00111	+ 0.00012	+ 0.00059	+ 0.00020	1	, 555.45
ı — 6	+ 0.00042	+ 0.00204	— 0, 00044	+ 0, 00204		
2-6	0.00000	— v. 00053	— o. oooz3	+ 0.00089	-0.00017	-0.00024
3 — 6	+ 0.01488	— 0. 00411	+ 0.02080	+ 0.01214	+0.00363	0. 00208
4 6	+ 0.07448	+ 0. 26869	+ 0. 17086	0. 34221	+0.03769	+ 0. 06608
5 — 6	3. 04638	+ 0.17313	— 3.84637	— 0. 49450	-0.41355	+o. 31861
6— 6	+ 3.94281	—14. 27845	+ 5.25030	+17.46285	—0. 11830	+0. 29533
7 6	I. 69348	<u> </u>	- 2.51849	+10.51393	—о . 03262	—o. o6679
8— 6	2. 21830	— 2. 90630	— 2. 45303	+ 2.58710	o. 07187	0.07395
9 6	- 0.90365	— 0.404 39	— o. 86244	+ 0.22567	— 0. 04446	-0.01518
10— 6	- 0.22050	+ 0.01947	— o. 17783	— o. o5586	-0.01448	+0.00234
11 — 6	- o. o3548	+ 0. 02488	0. 02223	0.02616	0.00291	+0.00225
12 — 6	— o. oo378	+ 0.00684	0.00079	— o. oo570	0.00033	+0.00073
3 — 7	+ 0.0008	0.0004	+ 0,0009	+ 0.0010	+0.0002	-0.0003
4-7	+ 0.0098	+ 0.0152	+ 0.0181	— 0.0179	+0.0038	+0.0030
5 — 7	- O. 22I2	+ 0. 1247	— 0. 25 96	0. 2052	0. 0370	+0.0434
6 7	— o. 6127	2 1067	— 0 . 9042	+ 2.5492	0. 2305	—о. 1 868
	+ 8.4175	+ 0.2639	+10.0604	— o. 5897	-0. 2108	o. o367
	+ 6.0245	2.4707	+ 6.3466	+ 2.8995	+0.0129	-0.0210
1 1	+ 1.7498	- 2.0390	+ 1.5151	+ 2.1461	+0.0324	o. o5o6
,	+ 0.1741	— o. 7867	+ 0.0531	+ o. 7285	+0.0036	o, o316
1	— o. o554	— о. 1893	— o. o769	+ 0. 1491	 0, 0040	-0.0103
1 1	— o. o297	0. 0290	- o. o297	+ 0.0177	-0.0023	-0,0020
i	+ 0.0008	+ 0.0008	+ 0.0021	— o. ooog	+0.0003	+o. ooo1
1	- 0.0121	+ 0.0139	- 0.0114	- 0.0210	0.0015	+0.0042
	— 0. I44I	— o. 1540	— O. 2047	+ 0. 1687	-0.0371	-0.0159
	+ 1.2998	— 0. 732I	+ 1.5303	+ 0.9550	+0.0707	0. 1501
	+ 1.0003	+ 4. 5946	+ 0.9941	- 5.4158	0,0025	0. 1384
	+ 2.3768	+ 3. 3965	+ 2.6374	— 3. 5 276	+0.0074	0,0076
	+ 1.6726	+ 0.9068	+ 1.7026	— 0. 7490	+0.0319	+0.0108
	+ 0. 6269 + 0. 1478	+ 0.0076 - 0.0784	+ 0.5673 + 0.1147	+ 0.0671 + 0.0909	+0.0207 +0.0067	0.0021 0.0044
		. 0,0,04	F 01+14/	- 0, 0909	1.01.0007	0,0044

	$a'\frac{d}{c}$	$\frac{\Omega'}{lg'}$	a'r	$rac{d\Omega'}{dr'}$	a'2	$a'^2 \frac{d\Omega'}{dZ'}$	
Arg.	sin.	cos.	cos.	sin.	sin.	cos.	
i' i 5 - 9 6 - 9 7 - 9 8 - 9 9 - 9 10 - 9	"0. 00050. 0150 +-0. 0881 +-0. 66402. 30771. 7310	+0.0010 0.0073 0.1366 +0.7283 +1.1684 +1.9130	","0. 00020. 0208 +-0. 0909 +-0. 81652. 70391. 7775	"0.0014 +-0.0059 +-0.17870.82911.23912.0630	0.0000 -0.0037 +0.0035 +0.0899 +0.0853 +0.0118	+0.0003 -0.0001 -0.0271 +0.0174 -0.0198 -0.0020	
11 — 9 12 — 9	0. 3639 -+0. 0921	+1.2557 +0.4618	0. 2661 -+0. 1405	—1.2511 —0.4190	-0.0012 +0.0042	+0.0180 +0.0125	
6 — 10 7 — 10 8 — 10 9 — 10 10 — 10 11 — 10	-0.0009 +0.0106 +0.1138 -0.3547 -0.9402 -1.3782 -0.8736	-0.0002 -0.0147 +0.0411 +0.5199 -1.0440 -0.7645 -0.0566	-0.0020 +0.0007 +0.1411 -0.3938 -1.0093 -1.4608 -0.8847	-0.0003 +0.0186 -0.0353 -0.6165 +1.2280 +0.7770 -0.0118	-0.0003 -0.0007 +0.0177 +0.0034 +0.0233 +0.0065 -0.0089	+0. 0001 -0. 0028 -0. 0024 +0. 0498 +0. 0490 +0. 0096 +0. 0021	
7 — 11 8 — 11 9 — 11 10 — 11 11 — 11	+0.0007 +0.0118 -0.0096 -0.3670 +0.4026 +0.2552	-0. 0014 -0. 0009 +0. 0857 -0. 1401 -0. 6386 -0. 9078	-0.0005 +0.0143 -0.0028 -0.4238 +0.4847 +0.2474	+0.0015 +0.0032 -0.1016 +0.1507 +0.6888 +1.0020	-0.0002 +0.0019 +0.0044 -0.0255 -0.0259 -0.0064	-0.0002 -0.0011 +0.0105 +0.0089 +0.0204 +0.0076	
8 — 12 9 — 12 10 — 12 11 — 12 12 — 12	+0.0009 +0.0027 -0.0590 +0.0288 +0.3994	0, 0008 +0, 0083 +0, 0065 0, 2349 +0, 0850	+0.0010 +0.0045 -0.0675 +0.0299 +0.4738	+0.0006 0.0101 0.0132 +0.2649 0.1202	+0.0001 +0.0011 -0.0057 -0.0079 -0.0142	-0.0002 +0.0011 +0.0042 -0.0121 -0.0102	

Following Hansen's method of integration we now introduce a set of symbols, τ , γ , ρ , and φ , which are, respectively, the equivalents of t, g, r, and f, except that they are regarded as constant whenever we integrate. When the integration is accomplished the original symbols are restored. The next step in deriving the perturbations is to obtain the development for Jupiter of the functions *

$$T = \frac{1}{n} \frac{dW}{dt} = Aa \frac{d\Omega}{dq} + Bar \frac{d\Omega}{dr} \qquad \qquad \frac{1}{n} \frac{dR}{dt} = Ca^2 \frac{d\Omega}{dZ}$$

and for Saturn the similar functions

$$\mathbf{T}' = \frac{\mathbf{I}}{n'} \frac{d\mathbf{W}'}{dt} = \mathbf{A}' a' \frac{d\Omega'}{dg'} + \mathbf{B}' a' r' \frac{d\Omega'}{dr'} \qquad \qquad \frac{\mathbf{I}}{n'} \frac{d\mathbf{R}'}{dt} = \mathbf{C}' a'' \frac{d\Omega'}{dZ'}$$

^{*}Gegenseitige Störungen des Jupiter und Saturn, s. 9, and Störungen der grossen Planeten, insbesondere des Jupiter, ss. 37, 50.

The expressions for A. B. and C are

$$\begin{split} \mathbf{A} &= -3 + \frac{1}{1 - e^2} \left\{ \left(2\frac{\rho}{\mathbf{a}} \cos \varphi + 3e \right) \frac{\mathbf{a}^2 (\mathbf{1} - e^2) - r^2}{\mathbf{a}^2 e} + 2\frac{\rho \sin \varphi}{\mathbf{a} \sqrt{1 - e^2}} \int \left(2\frac{r}{\mathbf{a}} \cos f + 3e \right) dg \right\} \\ \mathbf{B} &= \frac{1}{1 - e^2} \left\{ \left(2\frac{\rho}{\mathbf{a}} \cos \varphi + 3e \right) \frac{r \sin f}{\mathbf{a} \sqrt{1 - e^2}} - 2\frac{\rho \sin \varphi}{\mathbf{a} \sqrt{1 - e^2}} \left(\frac{r}{\mathbf{a}} \cos f + 2e \right) \right\} \\ \mathbf{C} &= \frac{1}{\sqrt{1 - e^2}} \frac{r}{\mathbf{a}} \frac{\rho}{\mathbf{a}} \sin (\varphi - f) \end{split}$$

The expressions for A', B', and C' are obtained by accenting all the symbols contained in these equations.

In developing T and $\frac{\mathbf{r}}{n} \frac{d\mathbf{R}}{dt}$ in a series of periodic terms whose arguments are composed of integral multiples of γ , g', and g we need compute directly only the terms which involve $\pm \gamma$, and in the case of the first function those which are independent of γ . The rest are readily supplied after integration in the functions W and R. This simplification is available, not only for the first order approximation, but for all succeeding orders. In deriving the proper developments of the multipliers A, B, and C we can employ the quantities P_i and Q_i of page 63. Thus it suffices to put

$$\frac{2\rho \sin \varphi}{a \sqrt{1 - e^2}} = 2Q_1 \sin \gamma + \dots \qquad 2\frac{\rho \sin \varphi}{a \sqrt{1 - e^2}} = 2Q_1 \sin \gamma + \dots \\
\frac{a^2(1 - e^2) - r^2}{a^2 e} = -\frac{5}{2}e + \frac{2}{1}Q_1 \cos g + \frac{2}{2}Q_2 \cos 2g + \frac{2}{3}Q_3 \cos 3g + \dots \\
\int \left(2\frac{r}{a} \cos f + 3e\right) dg = \frac{2}{1}P_1 \sin g + \frac{2}{2}P_2 \sin 2g + \frac{2}{3}P_3 \sin 3g + \dots \\
\frac{r \sin f}{a \sqrt{1 - e^2}} = Q_1 \sin g + Q_2 \sin 2g + Q_3 \sin 3g + \dots \\
\frac{r}{2} \cos f + 2e = \frac{1}{2}e + P_1 \cos g + P_2 \cos 2g + P_3 \cos 3g + \dots$$

The portion of C which involves the single multiple of γ is

$$C = \Sigma_i \cdot \frac{1}{2} (P_i Q_i \pm P_1 Q_i) \sin (\gamma \mp ig)$$

the double sign being taken both ways.

With the understood restriction the three multipliers for Jupiter are

The corresponding quantities for Saturn are

The terms of W or R, which involve other multiples of γ than ± 1 , are obtained in the following way:*

Let

Wor
$$R = \sum \alpha^{(i)} \frac{\sin}{\cos} \left(i\gamma + \beta t \right)$$

then

$$\alpha^{(\pm i)} = \eta^{(i)} \alpha^{(\pm 1)} + \theta^{(i)} \alpha^{(\mp 1)}$$

where

$$\eta^{(i)} = \frac{\mathbf{1}}{2} \frac{\mathbf{P}_i}{\mathbf{P}_1} + \frac{\mathbf{I}}{2i} \frac{\mathbf{J}_{ie}^{(i)}}{\mathbf{J}_{\frac{e}{2}}^{(1)}} \qquad \qquad \theta^{(i)} = \frac{\mathbf{1}}{2} \frac{\mathbf{P}_i}{\mathbf{P}_1} - \frac{\mathbf{I}}{2i} \frac{\mathbf{J}_{ie}^{(i)}}{\mathbf{J}_{\frac{e}{2}}^{(1)}}$$

In the case of R we have, in addition,

$$\alpha^{(0)} = \eta^{(0)}(\alpha^{(1)} + \alpha^{(-1)})$$

where

$$\eta^{(0)} = \frac{1}{2} \frac{P_0}{P_1}$$

For Jupiter

$$\log \eta^{(0)} = 8.8599027n$$

$$\log \eta^{(2)} = 8.3821495$$

$$\log \eta^{(3)} = 6.9403902$$

$$\log \eta^{(4)} = 5.5724169$$

$$\log \eta^{(5)} = 4.2453$$

$$\log \eta^{(6)} = 2.9442$$

For Saturn

$$\log \eta^{(0)} = 8.9252322n$$

$$\log \eta^{(2)} = 8.4472576$$

$$\log \eta^{(3)} = 7.0706064$$

$$\log \eta^{(4)} = 5.7677404$$

$$\log \eta^{(6)} = 3.2696$$

$$\log \eta^{(6)} = 3.2696$$

The developments of T and $\frac{1}{n} \frac{d\mathbf{R}}{dt}$ follow; they have the form

$$\mathbf{A}_{\cos}^{\sin}\Big($$
 $ny + i'g' + ig\Big)$

^{*}Gegenseitige Störungen des Jupiter und Saturn, ss. 25-29, and Störungen der grossen Planeten, insbesondere des Jupiter, ss. 37-39.

	1. 1420391	008. '' - 0. 0163215 + 1. 0173637 - 0. 5043882 - 0. 341651 - 0. 08305 + 0. 053403 - 0. 00437 - 0. 00275 + 0. 00344	-0. 0207 -0. 0017	sin. +0. 0506 +0. 2844315 -0. 2819 -0. 0288
	1. 27897 — 1. 1420391 — 2. 9242313 — 2. 08864 — 2. 04934 — 2. 050385 — 2. 00074 — 2. 000146 — 2. 00052 —	- 0.0163215 + 1.0173637 - 0.5043882 - 0.341651 - 0.08305 + 0.053403 - 0.00437 - 0.00275	+0. 0120 +0. 1253514 -0. 1235 +0. 0087 -0. 0207	+0. 0506 +0. 2844315 -0. 2819 -0. 0288
-I 0 0 -I + 0 0 0 -I 1 0 0 0 -I 1 0 0 0 -I 1 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0	1. 1420391	+ 1.0173637 - 0.5043882 - 0.341651 - 0.08305 + 0.053403 - 0.00437 - 0.00275	+0. 1253514 -0. 1235 +0. 0087 -0. 0207	+0. 2844315 0. 2819 0. 0288
0 0-1	0. 9242313 0. 08864 0. 04934 0. 050385 0. 00074 0. 00412 0. 00146 0. 00052	— 0. 5043882 — 0. 341651 — 0. 08305 + 0. 053403 — 0. 00437 — 0. 00275	-0. 1235 +0. 0087 -0. 0207	0. 2819 0. 0288
I 0-2 -I 0-I 0 0-2 -I 0-I 0 0-2 -I 0-3 -I 0-2 -I 0-3 -I 0-4 -I 0-3 -I 0-4 -I 0-3 -I 0-4 -I 0-5 -I 1+3 -I 1+2 -I 1+3 -I 1+2 -I 1+1 -I 1+1 -I 1-I -I I 0 -I I+I -I I-I -I I 0 -I 0 -	0. 08864 0. 04934 0. 050385 0. 00074 0. 00412 0. 00146 0. 00052	0. 341651 0. 08305 +- 0. 053403 0. 00437 0. 00275	+o. 0087 o. 0207	o. o288
-I O-I	0. 04934 0. 050385 0. 00074 0. 00412 0. 00146 0. 00052	— 0. 08305 + 0. 053403 — 0. 00437 — 0. 00275	+o. 0087 o. 0207	o. o288
0 0-2	0. 050385 0. 00074 0. 00412 0. 00146 0. 00052	+ 0.053403 - 0.00437 - 0.00275	o. o2o7	
I 0-3 - 0 -I 0-2 + 0 0 0-3 -0 I 0-4 - 0 -I 0-3 + 0 0 0-4 -0 I 0-5 -0 I 1+3 + 0 I 1+3 + 0 I 1+2 - 0 I 1+1 + 0 I 1-1 - 0 I 1-1 - 0 I 1-1 - 0 I 1-1 - 0 I 1-2 - 0 I 1-3 + 0 I 1-3 - 0 I	0. 00074 0. 00412 0. 00146 0. 00052	— 0. 00437 — 0. 00275	-	1
-1 0-2 + 0 0 0-3 1 0-4 -0 1 0-3 + 0 0 0-4 -0 1 0-5 -0 1 1+3 + 0 1 1+3 + 0 1 1+3 -0 1 1+1 -0 1 1+1 -1 1 1 1-1 -1 1 1 1-1 -1 1 1 1-2 -1 1 1 1-2 -1 1 1 1-3 + 1 1 1-2 -1 1 1 1-3 + 1 1 1-2 + 1 1 1-3 + 1 1-3 -1 1 1-2 + 1 1-3 -1 1 1-3 + 1 1-3 -1 1 1-3 + 1 1-3 -1 1 1-3	0. 00412 - 0. 00146 - 0. 00052 -	0. 00275	-	1
0 0-3 -0 0 -	0.00146 -		-0.0017	+0.0015
I 0-4 -0 -I 0-3 +0 0 0-4 -0 I 0-5 -0 I 1+3 +0 I 1+2 -0 -I 1+3 -0 I 1+2 -0 I 1+1 +0 I 1-1 -0 I 1-1 -0 I 1-1 -0 I 1-2 -0 I 1-3 +0 I 1-3 +0 I 1-3 +0 I 1-1 -1 I 1-2 +0 I 1-3 -0 I	0.00052 -	+ 0.00344		0.0001
-I 0-3 + 0 0 0-4 I 0-5 - 0 I I+3 + 0 I I+3 + 0 I I+2 - 0 I I+1 + 0	_			
0 0-4	0.00017 -	o. ooo62	-0.000I	+0.0007
I 0-5	1	+ 0.00022		
I I+3 + 0 I+3 + 0 I+3 + 0 I+3 + 0 I+4 - 0 I+1 + 0 I+1	0.00011	0.00000		
0	0.00006 -	— o. oooo8		
I I+2 -0 -I I+3 -0 0 I+2 -0 I I+I +0 I I+1 +0 I I+2 -0 0 I+I -0 I I+1 +1 I I O +0 -I I+I +1 I I-I -1 I I-I I-I -1 I I-I I-I -1 I I-I I-I -1 I I-I I-I I-I I I-I I-I I-I I I-I I-I I	0.00001 -	0.00011		
-I I+3 - 0 0 I+2 - 0 I I+I + 0 I I+I + 0 I I+I - 0 I I+I	0.00023 -	+ 0.00021		
0 I+2	0. 00050 -	— 0.00144	-0,0002	-0.000I
I I+I + 0 I I+2 - 0 I I+1 - 0 I I O + 0 I I-1 - 0 I I-1 - 0 I I-2 - 1 I I-3 + 1 I I-2 + 1 I I-3 + 1 I I-3 - 1 I I-2 + 1 I I-3 - 1	0.00010 -	+ 0.00045	-0.0019	0.0011
-I I+2 - 0 0 I+I - 0 I I 0 + 0 -I I+I + 1 I I-I - 0 -I I-I - 1 I I-2 - 0 -I I-1 + 0 0 I-2 - 0 I I-3 + 0 0 I-3 - 0	0.00292 -	+ 0.00632		
0 I+I	0.00190 -	— о. отооб	-0.0010	+o. oo36
I I O + O + O + O + O + O + O + O + O +	0. 01946 -	— o. o3253	-o. o267	+o. o28 7
-I I+I + I I-II I 0 + 0 I-I - I I-2I I-1 + 0 I-2 - I I-3 + -I I-2 + 0 I-3 -	0. 10373	— o. o1590		
I I-I	0. 15948 -	+ 0.06278	+0.0448	0.0161
-I I O + 0 I-I - I I-2 - -I I-I + 0 I-2 - I I-3 + -I I-2 + 0 I-3 -	1. 38370	— 0. 92376	+o. 1882	+0. 128 2
0 I-I - I I-2 - -I I-I + 0 I-2 - I I-3 + -I I-2 + 0 I-3 -	1	+ 0.68960	—0. 1878	o. 1278
I I-2 - -I I-I + 0 I-2 I I-3 + -I I-2 + 0 I-3 -		+13.23026	-o. o392	+0.0192
$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$		— 7. 22662		
0 I-2 I I-3 + -I I-2 + 0 I-3 -		— 3· 55532	+0.0403	o. o358
$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$	0. 50684	I. 1073I	+o. 1994	-0.0450
- I I - 2 + 0 I - 3 -	1	+ 0.87785		1
0 1-3 -	0.40413	— 0. 29319	—0. 1 966	+0.0412
		— o. o6763	-o. o123	o. oo62
1 1-4 1 +		+ 0.08783	0.0060	100===
	- '	- 0.02711	0. 0068	+0.0103
	-	— 0.00034	-0.0003	+0.0007
1	· ·	+ 0.00401		
i I		- 0,00225		
	0.00005	0,00000		
		+ 0.00023		
1 1		— 0.00019		
	0, 00020	+ 0.00012		
	0, 00020	+ 0.00013		
1 1	0. 00020 0. 00003 0. 00005	+ 0.00065		
1 1	0, 00020 0, 00003 0, 00005 0, 00002			1
1	0, 00020 0, 00003 0, 00005 0, 00002 0, 00022	o. oo1o8		
0 2+1 -	0. 00020 0. 00003 0. 00005 0. 00002 0. 00022 - 0. 000487		-0.0044	+0.0020

	T Arg.		r	$\frac{1}{n}$	$rac{d\mathbf{R}}{dt}$
		sin.	cos.	cos.	sin.
н	i' i	11	11	"	"
1	2 0	+ 0.02018	— o. ooo63	+0.0059	+0.0026
_ I	2 + I	+ 0.05341	— o. 17006	+0.0191	+0.0451
1	2 — 1	— o. 19776	+ o. 18685	+0,0026	-o. o649
— 1	2 0	+ 4.89560	+ 0.57514	+0. 2191	-0. 208 1
0	2 — 1	— 3. 717 753	+ 0. 196716		
1	2 2	+ 1.51956	— 1. 46206	o. 2165	+0. 2058
— 1	2 — 1	-47. 87233	+20. 55610	+0.0237	+0.0395
0	2 — 2	+45. 08114	-19. 40163		
I	2 — 3	—12. 36743	+ 5.27139	-0, 0449	-0.0318
- 1	2 2	— o. 07834	+ 1.63350	-0.0034	-0. 1268
0	2-3	+ 1.80511	- 2, 42460		
1	2 — 4	— o. 88o28	+ 0. 97188	0.0010	+0. 1239
— 1	2 — 3	+ 0.05101	+ 0.08440	-0. 0031	+0.0038
٥	2 — 4	+ 0.04234	— о. 18903		
1	2 5	— o. 04279	+ 0.08655	+0.0031	+0.0082
- 1	2 — 4	+ 0.00219	+ 0.00428	+0.0002	+0.0003
0	2 — 5	+ 0.00084	— o. o128o		
I	2 — 6	— o. oo169	+ 0.00646		
— I	2 — 5	+ 0.00008	+ 0.00015		
٥	2 — 6	— o. oooo1	— o. ooo77		
1	2 — 7	o. oooo8	+ 0, 00043		
1	3+1	o. oooo5	0. 00005	!	
- 1	3+2	— o. ooo63	+ 0,00021		
0	3 + I	– o. ooo73	+ 0.00051		
1	3 0	+ 0.00211	0.00098	+0.0004	+0.0008
— І	3 + I	— 0. 00723	— 0. 01958	—o. ooo6	+0.0075
I	3 — I	— o. o1716	+ 0.03416	+0.0074	—0. 0095
— т	3 0	+ 0.87841	— v. 31841	+ 0.0698	0. 0235
٥	3 — I	- o. 64 7 247	+ 0.310206		
I	3 2	+ 0.18035	— o. 3 72 44	0. 0790	+0.0070
— I	3 — 1	— 6. 73 5 00	+ 9.03111	0. 1032	<u> </u>
٥	3 — 2	+ 6. 357282	- 8. 148465		
1	3-3	— I. I453I	+ 2.72466	+0.0989	+0. 1603
— I	3-2	—20. o3269	—28. 41215	+0. 0326	0. 0239
٥	3 — 3	+19.48402	+26. 95993		1
I	3-4	- 5 . 68448	- 7. 80172	-o. o3o3	+0.0381
— I	3-3	— 1.96410	- 0. 11612	-0.0748	-0. of 32
0	3 — 4	+ 2.71571	+ 1.14298	, ,	
I	35	- 1.02603	0. 54359	+0.0718	+0.0168
— I	3-4	— 0. 10172	+ 0.06235	+0.0006	+0.0007
0	3-5	+ 0.21686	— o. oo518		
I	3-6	— 0.09729	— 0.01520	+0.0065	+0.0008
1 - 1	3-5	0.00474	+ 0.00465		
0	3 — 6	+ 0.01456	0.00402		
1	3-7	— o. oo741	+ o. ooo68		
L					

Arg.	1		1 <u>d</u>	
8	sin.	cos.	cos.	sin.
\varkappa i' i	11	"	11	<i>n</i>
_I 3-6	0. 00017	+ 0.00029		
0 3-7	+ 0.00090	— 0.0004I		
1 3-8	— o. ooo55	+ 0.00011		
1 4+2	— o. oooo5	+ 0.00008		
1	_	+ 0.00007		
1 4 0	- 0.00004 + 0.00017	- 0.0002I		
-1 4+1	- 0.00203	- 0.00021 - 0.00153		
1 4-1	- 0.00203 - 0.00029	+ 0.00465	+0.0017	-0.0007
-I 4 0	+ 0.09561	— 0. 08720	+0.0123	+0.0016
0 41	— o. o68625	+ 0.068916	10.0123	
1 4-2	- 0.00198	— o. o5611	o. 0127	o. oo78
-1 4-1	- o. 16313	+ 1.71546	-0.0072	o, o632
0 4-2	+ 0. 210126	- 1.519686	1 0.00/2	0,0032
I 4-3	+ o. 17380	+ 0. 44953	0, 0043	+o. o665
-1 4-2	- 9.4485I	- 4. 57606	0. 1070	+0.0408
0 4-3	+ 8.87909	+ 4. 40965		,
1 4-4	2. 84258	- o. 85831	+0. 1050	0. 0371
-1 4-3	+14.62768	— 15 . 89793	o. o182	_o. o273
0 4-4	—13. 81865	+15.57488		,,,
1 4-5	+ 4.09131	- 4. 67472	+0. 0268	+0.0275
_1 4-4	0. 12034	— 1. 786oI	_o. o166	+0.0411
0 4-5	o. 40655	+ 2. 37533	ľ	, ,
1 4-6	+ 0. 22138	— o. 87661	+0.0190	-0. 0384
-1 4-5	— o. o7683	- 0.09770	0.0005	+0.0004
0 4-6	+ 0.05467	+ 0. 19722		
1 4-7	 0. 01066	— o. o8671	+0.0022	0.0041
-1 4-6	- o. oo656	U. 00412		-
0 4-7	+ 0.00839	+ 0.01300		
1 4-8	- 0, 00291	0.00659		
- I 4-7	— 0.00054	- 0.00015	i	
0 4-8	+ 0.00077	+ 0.00075	ł	
1 4-9	o. 00020	- 0.00042	ļ	
-1 5 + 1	— 0. 00031	— 0.00004	ĺ .	
1 5-1	+ 0,00020	+ 0,00048	+0.0002	0.0000
_ I 5 0	+ 0.00653	— o. o1387	+0.0015	+0.0010
0 5-1	— o. 004728	+ 0.010044		,
I 5-2	— o. oo372	- o. oo531	0, 00095	-0.00220
_ I 5 — I	+ 0. 10176	+ 0. 20473	+0,0045	-0.0125
0 5-2	— o. o7676841	- 0. 18132165	' ' '	J
1 5-3	+ 0.06246	+ 0.03064	0. 0093	+0.0117
_1 5-z	_ 2.02853	+ 0. 15265	0.04865	-0.00476
0 5-3	+ 1.887900	- 0. 090724	· ŭ	.,-
1 5-4	— o. 55397	+ 0.21727	+0.0488	+0.0121
-I 5-3	+ 2.09722	— 8. 16344	+0.0100	+0.0647
0 5-4	_ 2.03072	+ 7.80499	,	• ••
		' ' ' '		

Arg.	7	r		$rac{d\mathbf{R}}{dt}$
	sin.	cos.	cos.	sin.
и i' i	"	"	"	"
I 5 5	+ o. 32258	-2.45130	0.0074	0, 0625
—I 5— 4	+11.14562	+6. 46261	<u> </u>	+0.0113
0 5 - 5	—10. 93896	5. 98566		
1 5 — 6	+ 3. 33401	+1.78195	+0.0228	o. o159
—I 5— 5	+ 1.37812	0. 33152	+0.0210	+ 0. 0143
o 5 — 6	— 1. 78888	+0. 10167		
I 5 — 7	+ 0.65267	+0.00695	—o. 0188	o. o156
-ı <u>5</u> - 6	+ 0.07719	o. o8431	+0.0003	+0.0010
0 5 - 7	— o. 15157	+0.08540		ļ
1 5-8	+ 0.06594	0. 02677	-0.0022	0. 0025
-I 5- 7	+ 0.00254	0.00743		
0 5 8	— 0. 00946	+0. 01085		
1 5 9	+ 0.00500	-0. 00425		
-1 5 - 8	- 0.00004	-0.00021		
0 5 - 9	— o. ooo45	+0.00088		
1 5-10	+ 0.00033	0. 00059		
1 6- I	0.00000	+0.00008		
— 1 6 о	+ 0.00005	-0. 00165		
o 6 1	0.00009	+0.00113		
ı 6— 2	o. ooo68	-0.00021	0, 0000	-0.0003
—ı 6— ı	+ 0.02401	+0.01471	+0.0017	o. oo15
0 6— 2	— o. o189420	—o. o136819		
1 6-3	+ 0.00900	0. 00249	0, 0026	+0.0008
—ı 6— 2	— o. 26360	+0. 18577	—0. 0103	0.0066
o 6— 3	+ 0. 247395	0. 159105		
1 6-4	0. 04954	+0.08524	+0,0090	+0.0099
-1 6-3	- o. 51443	-1.92108	<u> </u>	+0.0331
0 6-4	+ 0.45469	+1.82824		
1 6- 5	o. 27814	-0. 52941	+0.0148	—o. o320
-ı 6- 4	+ 6. 19549	+0.28513	+ 0. 0360	+0.0024
0 6— 5	— 5· 97373	—o. 26063		
ı 6— 6	+ 1.85582	-0. 10314	-0.0340	0.0040
—ı 6— 5	<u> </u>	+7. 13306	+0.0056	+0.0165
0 6— 6	+ t. 92940	-6. 98712		
1 6 7	— o. 56043	+2. 14709	—o. 0078	o. o177
-ı 6- 6	+ 0.42549	+0.94126	+0.0103	0. 0097
0 6-7	— o. 34977	—I. 20274		
ı 6— 8	+ 0.09974	+0.43618	0.0110	+0.0080
-1 6- 7	+ 0.08149	+0.05070	+0.0009	0,0001
o 6— 8	0.09401	-0. 10046		,
1 6— 9	+ 0.03261	+0.04370	-0, 0020	+0.0009
-r 6-8	+ 0.00724	+0.00088		
0 6—9	0.01098	0.00540		
1 6—10	+ 0.00432	+0.00295		
-ı 6— 9	+ 0.00042	0.00017		
			•	1

Arg.	1	7	$\frac{1}{n}$	
	sin.	cos.	cos.	sin.
u i' i	11	11	//	"
o 6 — 10	-0.00073	0.00013		
1 6 — 11	+0.00020	+0.00014		
_I 7 0	0. 00005	o. ooo13		
0 7— 1	+0.00003	+0,00007		
1 7— 2	-0.00008	+0.00004		
-I 7- I	+0.00330	0.00003		
0 7-2	0. 00263	o. 0002I		
I 7-3	+0.00067	0. 00099	-0.0005	-0.0002
- r 7 - 2	-0.01820	+0.04180	-0.0012	0. 0021
0 7 - 3	+o. 018315	o. o36387		
ı 7—4	+0.00204	+0.01448 -	+0.0004	+0.0028
-ı 7-3	o. 26181	—o. 26059	0. 0072	+0.0074
0 7 — 4	+o. 23753	+0. 25143		
1 7- 5	<u> </u>	—0. 05109	+0.0092	0. 0059
<u>-</u> 1 7— 4	+1.55438	—o. 7637 5	+0.0204	+0.0117
0 7 - 5	—1. 49 <u>5</u> 66	+0.71456		
ı 7—6	+0. 42479	o. 31465	—o. o189	0.0141
- I 7 - 5	+0.73029	+4. 24941	+0.0057	—o. o184
0 7 — 6	—o. 71031	<u>—4. 11139</u>		
r 7— 7	+0. 30222	+1.26623	0. 0064	+0.0169
<u> </u>	-4. 22658	o. 29928	+0.0115	0. 0020
0 7 7	<u>+</u> 4. 11906	+0. 12916		
r 7—8	<u>—1. 2715</u> 6	—0. 01850	0.0125	+0.0030
- I 7 - 7	—0. 57462	+0.41645	0, 0040	o. oo68
0 7 - 8	+0. 72692	—o. 40946		
1 7— 9	o. 26152	+0.13102	+0.0028	+0.0070
_ r 7 - 8	—o. o2589	+0.07035	+0.0001	—o. ooo8
0 7 - 9	+o. 05544	o. o8595		
1 7—10	—o. 0240I	+0.03087	+0.0002	+0.0015
- I 7 — 9	o. 00289	+0.00674		
0 7—10	+o. 00741	-0. 01029		
1 7—11	-0.00514	+0.00415		
- I 7 — IO	+0.00005	+0.00057		
0 7—11	+0.00054	-0.00105		
1 7 — 12	0,00051	+0.00052		
_ I 8 — I	+0.00031	0,00020		
0 8- 2	-0. 00024	+0.00012		
ı 8 — 3	0. 00002	-0.00015		
- I 8 2	+0. 00082	+0,00592	0.0000	0.0004
0 8-3	o. ooo378	-0.005220		
1 8-4	+0.00147	+0.00139	0, 0002	+0.0004
_ I 8 - 3	0. 05766	—o. 01461	0, 0022	+0.0007
0 8-4	+o. o5268	+0.01575	[
ı 8— 5	-o, o1882	+0.00319	+o. 0026	0,0000
_ I 8— 4	+0. 20803	o. 30585	+0.0045	+0.0067
,				

Arg.	Т		$rac{1}{n}rac{d\mathbf{R}}{dt}$	
	sin.	cos.	cos.	sin.
н i' i	"	"		"
0 8- 5	-0. 20424	+0. 28602		
I 8— 6	⊹ o. o3879	<u></u> 0. 10928	0, 0031	—o. oo78
— I 8— 5	+o. 84886	+1.10096	+0.0104	-0.0111
o 8 6	—0. 81414	—1. o6665		
1 8— 7	+o. 31429	+0. 29688	 0. 0116	+0.0099
—ı 8— 6	2. 66695	+1.05766	0.0084	—o. oo47
0 8-7	+2.57958	-1.05789	ł	
ı 8— 8	—о. 78720	+0. 39256	+0.0073	+o. oo66
<u> </u>	—о. 39269	—2. 32986	+0.0001	+0.0085
o 8—8	+o. 48951	+2.24844	1	
I 8 9	—0, 16606	0. 69278	+0.0003	o. oo8o
r 8 — 8	—о. 34858	0. 31699	0, 0041	0.0000
0 8-9	+o. 36558	+0.40092		
1 8—10	0. 12114	— 0. 14513	+0.0040	0.0008
—ı 8— 9	0. 05544	0. 00845	0, 0005	-0.0001
o 8—10	+o. o695 7	+0.02511		
1 8 11	o. o2535	0. 01199	+0.0009	+0.0001
1 8 10	-o. oo510	+5.00181		
o 8—11	-\ 0.00795	— 0. 00063		
1 8 12	0. 00320	-0.00012		
- 1 8 - 11	-o. ooo33	+0.00046		
0 8—12	+ 0.00069	-o. ooo57		
1 8 13	0. 00031	+0.00029		
- 1 9 - 2	+0.00048	+0.00059		
0 9-3	0, 00039	0,00051		
1 9 — 4	+0.00027	+0,00002		
-1 9-3	—o. oo836	+0.00250		
0 9-4	+0.00771	0. 00189		-
1 9 - 5	-0.0020I	+0.00209	+0.0005	+0.0002
-1 9-4	+0.00479	<u>0. 06705</u>	0.0000	+0.0021
0 9- 5	o. oo66o	+o. o6297		
1 9 — 6	o. oo557	0. 02090	+0.0003	-0.0021
_r 9_5	+0. 30975	+0.13250	+0.0056	-0.0021
0 9-6	— 0. 29484	—0. 13197		
19-7	+0.10452	+0.01988	—o. oo61	+0.0012
- r 9 - 6	—o. 68623	+0.80230	0.0054	-0.0079
0 9-7	+0.66609	<u>-0.77607</u>		
1 9— 8	—о . 17 856	+0. 27679	+o. 0046	+0.0082
_I 9— 7	—1. 03723	—1. 53330	-o. oo35	+0.0034
0 9 - 8	+1.03386	+1.47738		
1 9— 9	—о. 35780	—0. 44556	+0.0035	-0.0027
-r 9-8	+1. 18867	—0. 52024	-0.0047	-0.0009
0 9-9	—1. 12 929	+0.57183		
1 9-10	+0. 34595	—0. 18655	+0.0051	+0.0009
1 9 9	+0. 15083	-0. 26204	+0.0001	+0.0023

Arg.	т		$\frac{1}{n}\frac{d}{d}$	
	sin.	cos.	cos.	ein.
н i' i о 9— 10	,, —0. 19290	,, +0. 28269	"	"
1 9-11	+0.07024	-0.09511	+0.0004	0. 0022
- I 9 - IO	-0. 00227	-0. 04014	-0.0002	+0.0003
0 9-11	0.00573	+0.05124		,
1 9-12	+o. oo365	-o. o189o		
-1 9-11	-o. oo2o8	-0.00341		
0 9-12	+0.00174	+0.00543		
1 9-13	-0. 00045	-0.00215		
0 10 — 3	-0.00007	0, 00003		
1 10 - 4	+0.00003	-0.00004		
- I IO - 3	0, 00081	+0.00090	-0.0001	0, 0001
0 10 — 4	+0.0007626	—0. 0007509		
1 10 - 5	0, 00004	+0.00040	+0.0001	+0.0001
- I IO - 4	0. 00484	-0.00979	0, 00016	+0.00040
0 10 5	+0.00414	+0.00930	1.0.000	
1 10 — 6	—o. oo276	0.00233	+0.0003	-0.0004
- I IO - 5	+0.06777	-0.00776	+0.0017	+0.0002
0 10 — 6	0. 06474	+0.00573		
1 10-7	+0.02036	-0.00842	-0.0017	0.0006
_ i io _ 6	—o. o5858	+0. 28008	—o. ooo6	-0.0042
0 10 - 7	- -0. 05961	-0. 26943		1 0 0010
1 10 — 8	—0, 00162	+0.09079	0.0000	+0.0043
— I IO— 7	0, 67294	—o. 36663	0.0054	+0.0023
o 10 — 8	+0.65484	+0. 35499	10.00*4	2 2276
1 10 — 9 — 1 10 — 8	-0. 22364	0. 08854 0. 84775	+0.0054	-0.0016
1	+0. 79847	1	+0.0010	+0.0021
0 10 - 9	—0. 76227	+0.84255	—0. 0006	0.0010
1 10 10	+0. 22542 +0. 42528	—o. 28203 ⊥o. 55215	_0.0000 _0.0012	-0.0019 -0.0027
- I IO - 9	+0. 43528	+0.55215	-0.0012	+0.0027
0 10 — 10	—o. 45999	0. 51093 0. 15461	+0.0013	0. 0030
	+0. 14795 +0. 18069	+0.15401	+0.0013	
- I 10 - I0	-0. 19758	-0.03042 -0.07539	+0.0012	+0.0003
0 IO — II I IO — I2	+0.06700	-0.07539 +0.02798	-0.0011	0, 0005
	+0.00700	-0.02798 -0.00710	+0,0001	+0.0002
	0. 02070 0. 03465		+ 0,0001	 0.0002
1	-0.03405 +0.01311	+0.00381 -0.00047		
1 10-13				
0 11 — 4	—o. oooo36	+0.000132		
1 11 — 5	+0.00007	+0.00004		
- I II - 4	0. 00137	-0. 00089		i
0 11 — 5	+0.00125	+0.00091		
1 11 - 6	0.00058	o. oooo8		
-1 11-5	+0.00978	0. 00732	+0.0003	+0.0003
0 11 — 6	0. 00948	+o. o o663		

Arg.	Т		$rac{1}{n}rac{d ext{R}}{dt}$	
	sin.	cos.	cos.	sin.
и i' i	"	"	11	"
1 11 — 7	+0.00223	0. 00340	—о. 0003	-0, 0002
- 1 11 - 6	+0.01919	+0.06105	+0,0004	+0.0012
o 11 — 7	— 0. 01725	—o. o5895		:
1 11 — 8	+0.01078	+0.01769	-0. 0007	0.0012
_I II — 7	0. 23021	-0.00103	0. 0029	o. ooo3
o 11 — 8	+ o . 22308	+0.00270		
I II 9	—0. 07247	+0.01189	+0.0029	+0.0005
_1 11 <u>8</u>	+0. 15237	0. 51520	+0.0005	+0.0034
0 11 - 9	—o. 14571	+0. 50280		
1 11 - 10	+0.02946	0. 16672	-0.0001	0.0034
-I II — 9	+0.61899	+0. 36725	+0.0010	-0.0001
0 11 10	0. 61314	0. 34005		ĺ
1 11-11	+0. 20117	+o. o9678	—0.000 9	-0.0001
_1 II _ IO	0. 22432	+0. 30259	+0.0015	+0.0011
0 11-11	+0. 19704	0. 31245		
I II I2	—o. o5793	+0.09947	0, 0016	-0.0011
-1 11-11	o. oo855	+0. 11339	+0.0003	0.0005
0 11 — 12	+0.01536	—o. 12543		
1 11 — 13	-0.00569	+0.04396		
o 12 — 5	+0.000225	+0.000024		
1 12 — 6	-0.00004	+0.00009		
— I I2 — 5	+0.00085	-0.00182		
0 12 — 6	-0,00092	+0.00167		
1 12 — 7	+0.00011	0. 00067		
<u>-1</u> 12 - 6	+0.00925	+0.00855	+0.0003	0.0002
0 12 - 7	0, 00849	0.00828		
ı 12— 8	+0.00358	+0.00167	0. 0004	+0,0002
—I I2— 7	o. o4976	+0.02772	-0.0009	_o. ooo6
0 12 — 8	+0.04821	—o. o2556		
I 12 9	0. 01355	+0.01160	+0.0009	+0.0007
_1 I2 — 8	o. o3667	—o. 17558	-0.0005	+0.0020
0 12- 9	+0.03378	+0. 16944	ĺ	,
I 12 — 10	-o. o184o	-0.05193	+0.0009	0.0020
—I I2— 9	+o. 36928	+0.02495	+0.0025	+0.0001
0 12 — 10	—o. 35625	-0.02310	' ' '	,
1 12-11	+0.11091	-0.00180	o. 0025	-0.0003
I I2 — IO	—o. 12776	+0.42118	-0,0003	-0.0012
0 12-11	+0.11445	-0.40722	5553	
1 12 - 12	—0. 03014	+0. 12294	0, 0000	+0.0012
-I 12 - II	—0. 19867	-0. 05897	0.000	70.0012
0 12-12				
	+0. 19542	+0.04158		
1 12 — 13	—o. o5857	0. 00965		

The developments of T' and $\frac{1}{n'}\frac{d\mathbf{R}'}{dt}$, which follow, have the form

$$\mathbf{A} \frac{\sin}{\cos} \left(\varkappa \gamma' + i'g' + ig \right)$$

Arg.	7	Γ'	$rac{1}{n'}rac{d\mathbf{R}'}{dt}$	
g,	sin.	cos.	cos.	sin.
μ i' i —I I D —I 2 D O I O I O O —I 3 D O 2 O I I O —I 4 O D 3 D I 2 O —I 5 D	" -516.95043 - 58.58491 + 37.48124 + 8.631067 - 3.02325 + 2.24989 + 0.80623 + 0.21579 - 0.19036 + 0.05554 + 0.07799 - 0.06780	" - 1. 069530 + 43. 19474 - 28. 53854 - 5. 350080 + 8. 39040 - 6. 55349 - 0. 74136 + 1. 00619 - 0. 83455 - 0. 10394 + 0. 08407 - 0. 07134	+0. 1737 -1. 5295 +1. 552265 -0. 2303 +0. 0568 -0. 0060 -0. 0172 +0. 0041	+0. 3861 -1. 0304 +1. 106428 -0. 3870 +0. 2747 -0. 0758 +0. 0347 -0. 0101
1 3 0 -1 6 0 5 0 1 4 0 0 6 0 1 5 0 -1 -3 - 1	- 0.00780 + 0.00109 + 0.01205 - 0.01044 - 0.00051 - 0.00114 - 0.00013 + 0.00060	- 0.07134 - 0.01303 + 0.00368 - 0.00306 - 0.00137 + 0.00024 - 0.00012 + 0.00053	-0.0044 +0.0011 -0.0096	+0.0024 -0.0009 -0.0001 +0.0006
0-4- I -I-2- I 0-3- I I-4- I -I-I- I	+ 0.00099 + 0.00745 + 0.01341 - 0.02257 + 0.08115	+ 0.00183 + 0.00309 + 0.00951 - 0.01363 + 0.01269	0, 0016 0, 0067 0, 0212	+0.0023 -0.0010 +0.0098
0-2- I I-3- I -I 0- I 0-I- I I-2- I	+ 0.11730 - 0.21738 + 0.99324 + 0.69522 - 1.60135	+ 0.02646 - 0.02439 + 0.95414 + 0.16626 + 0.33043	+0. 0493 -0. 4406 +0. 2174	+0.0104 -0.5806 +0.1068
-I I I I I I - I I I - I I I -I I I I O I I I I O I I -I 3 - I	- 2. 26425 - 10. 11588 + 30. 6172 - 331. 8120 +413. 9052 - 62. 89740	— 50. 58646 — 8. 54976 + 129. 6082 —1579. 2837 +1977. 8997 — 27. 54848	+1.9137 -1.9733 +0.3895 -0.0761 -0.8100	+4. 2296 -4. 2290 -0. 1918 +0. 5711 +0. 8220
0 2— I I I— I —I 4— I 0 3— I I 2— I	+ 37.58748 + 0.77630 - 15.19654 + 12.56079 - 0.23716	 40. 59165 22. 61485 0. 57900 2. 56986 1. 78715 	+0. 8812 0. 3667 +0. 2797	—0. 8551 +0. 1240 —0. 0291

Arg.	מ	r,	$\frac{1}{n'}$	đR' đt
	sin	cos.	cos.	sin.
н i' i —1 5— 1	" — 2.06132	" + 0.89623	,, 0. 0803	,, -0. 0114
o 4— i	+ 1.83429	— 0. 96681		
1 3—1	+ 0.02828	+ 0.21024	+0.0410	+o. 0245
— 1 6— 1	o. 17839	+ 0.22186	-0.0112	-0.0080
o 5— 1	+ o. 16476	- o. 21309		
I 4— I	+ 0.01448	+ 0.02047	+0.0029	+0.0065
—ı 7— ı	— o. oo563	+ 0.03301	-0.0003	—0. 0002
о 6— 1	+ 0.00555	— 0. 03126		
1 5— 1	+ 0.00264	+ 0.00113	-0.0001	+0.0009
—ı 8— ı	+ 0.00124	+ 0.00347		
0 7— I	- 0.00117	- 0.00339	ĺ	
1 6— 1	+ 0.00033	- 0.00018	,	
-1-2-2	- 0.00003	+ 0.00035	a aaa	(
—I — I— 2	- 0.00019 + 0.00003	+ 0.00514	+0.0008	+0.0010
0-2-2 1-3-2	— 0.0002I	+ 0.00510 - 0.00985	+0.0005	0 0030
1 O 2	+ 0.03874	+ 0.13724	-0.0222	0. 0039 0. 0429
0-1-2	+ 0.01188	+ 0.06591	0.0222	-0.0429
I 2 2	- 0. 03406	- 0.09873	+0.0108	— о. 0386
—I I— 2	— o. 7308o	- 4· 73524	+0. 2770	+0.6911
I — I— 2	— o. 7o265	— 2. 02830	-0.0700	0.7337
—I 2— 2	— o. 16574	+ 61.01074	—1. 8224	+0.4418
0 I 2	— 35. 34786	181.96074		1
I 0 2	+ 36.95055	+186. 12850	+1.8721	— о. 3333
—ī 3— 2	+337.63347	—139. 59991	0. 4087	0. 2854
0 2— 2	—278. 21 22 9	+110.17461		
I I- 2	+ 30. 38905	— 11. 54497	+0. 1586	+0.2656
—ı 4— 2	+ 65.51974	— 85. 33376	+0. 3637	+0.5514
0 3— 2	— 58. 548 93	+ 74.51370	_	
I 2 2	+ 2.13473	9. 37408	-0. 4048	—o. 6105
—I 5— 2	+ 2.50567	20. 38129	+0.03434	+0. 29178
0 4— 2 I 3— 2	— 2. 57967 — 0. 95705	+ 18.61784 - 1.69618	+0.0106	_0 2225
-I 6- 2	— 1. 31008	— 1. 09018 — 2. 94476	-0.0258	—0. 2337 —0. 0699
0 5-2	+ 1.1766033	+ 2. 7790743	-0.0230	 0,0099
I 4— 2	— 0. 293699	— 0. 123765	+0.0298	o. o385
—I 7— 2	— 0. 3720I	— 0. 25777	-0. 0109	+0.0097
0 6— 2	+ 0.3484314	+ 0. 2517321		, , , ,
I 5— 2	— 0.04472	+ 0.01049	+0.00804	-0.00254
—ı 8— 2	— o. o59o7	0. 00340	-0. 0024	+0.0006
0 7— 2	+ 0.05646	+ 0.00441		ļ
1 6— 2	— o. oo4oo	+ 0.00456	+0.0012	+0.0004
—I 9 — 2	— o. oo639	+ 0.00354		ļ
0 8 2	+ 0.00615	0. 00330		1
I 7— 2	+ 0.00002	+ 0.00086		1
		,		

Arg.	\mathbf{T}'		$rac{1}{n'}rac{d\mathbf{R}'}{dt}$	
	sin.	cos.	cos.	sin.
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	— o. oooo7	,, + 0.00026	11	"
i o 3	+ 0.00059	+ 0.00814	0, 0014	0, 0045
0-1-3	— o. ooo39	+ 0.00504		
1-2-3	+ 0.00197	- 0.00509	<u> </u>	-0.0024
_1 I— 3	- 0.09853	— 0. 40 7 00	+0. 0289	+0.0516
I — I — 3	0.01560	— o. 158o3	-0.0271	0.0634
_1 2— 3	+ 0.36186	+ 5.38023	-o. o156	0.0099
o 1— 3	— 2. 94534	— 15. 10743		
r o 3	+ 3.25176	+ 15.08398	+0.0183	—0. 1219
-r 3— 3	+ 3.84726	17. 12524	+ 0. 0260	+1.2106
0 2-3	— 7·54317	+ 9.11937		1
1 I— 3	+ 1.62923	— 1.8o976	0. 0004	—I. 2323
—I 4— 3	+134.73558	+189. 55633	— 0. 2762	+0.3342
0 3-3	—119. 45859	165. 32601		
1 2— 3	+ 21.79101	+ 30. 21788	+0. 2371	0. 1808
— I 5— 3	+ 79.63698	+ 39. 02827	+0. 3297	—0. 1265
0 4-3	— 72. 57969	— 36. o4776		
1 3— 3	+ 12.09393	+ 2.94027	—о. 3798	+0. 1575
— 1 6— 3	+ 20. 55631	1. 24009	+0. 2045	+0.0190
o 5— 3	— 1 9. 29003	+ 0.92685		
I 4-3	+ 2.46966	— I. I3752	—0. 1704	—o. o374
-I 7-3	+ 3.14534	- 2.09648	+0.0522	+0.0330
o 6— 3	- 3.03342	+ 1.95084		
1 5— 3	+ 0.23109	— 0. 42504	-0.0302	-0.0317
—I 8— 3	+ 0.26103	- 0. 54421	+0.0069	+0.0120
o 7— 3 1 6— 3	— 0. 26202 — 0. 00941	+ 0.52050 - 0.07521	-0.0015	_o. oo86
ŭ	- 0.00941 - 0.00817	- 0.07521 - 0.08750	-0.0015 -0.0002	+0.0026
о 8— 3	+ 0.00618	+ 0.08532	70.0002	7-0.0020
I 7— 3	- 0.00731	- 0.00807	+0.000 6	-0.0013
_1 103	- 0.00727	— o. 00964	1	
0 9-3	+ 0.00690	+ 0.00957		
1 8-3	- 0.00153	— o. ooo33		
_1 II- 3	— 0. 00014	- 0.00018		
0 10—3	— 0. 00138	+ 0.00066		
I 9 3	+ 0.00039	+ 0.00049		
_I 0— 4	+ 0.00018	+ 0.00090		
_I I _ 4	— 0.00724	- 0.03283	+0.0019	+0.0037
1-1-4	— o. oo139	0.01029	-0, 0022	-o. oo38
.—I 2— 4	+ o. 04884	+ o. 39446	-0.0003	-0.0039
o I—4	— o. 23o13	— 1. 152 66	_	
1 0-4	+ 0. 25078	+ 1.16180	— о. 0039	-o. oo15
—ı 3— 4	- o. 37993	— o. 90147	<u> </u>	+0.0364
0 2 4	— o. 1428o	+ 0.51720		
1 1-4	+ 0.11784	- o. o5486	-0.0529	-0.0544
—I 4— 4	+ 17.26822	+ 1.98797	+0.7245	+o. 1398

Arg.		T'		$\frac{d\mathbf{R}}{dt}$
	sin.	608.	cos.	sin.
ж i' i	"	"	n	"
0 3—4	—12. 48753	- 5. 25909		
I 2— 4	+ 2.57442	+ 1.46913	—o. 7438	—o. 1596
-I 5-4 0 4-4	94. 22508	+104.08309	+o. 22 7 3	+0. 2489
' '	+84. 71691 18. 79588	— 95.48370	0.7475	0.0006
I 3— 4 —I 6— 4	—16. 5o867	+ 20. 99078 + 64. 12834	—0. 1415 —0. 0225	0. 2096
0 5-4	+15.56199	— 59. 81178		—о. 1735
1 4-4	- 1. 24466	+ 11.54170	+0.0414	+0. 2134
_I 7— 4	+ 4. 56295	+ 17.62466	+0.0406	-0. 1287
0 6-4	— 4. 18134	— 16.81242	1 5. 5400	
1 5-4	+ 1.44161	+ 2.55979	<u> </u>	+0. 1111
—ı 8— 4	+ 2.67978	+ 2.75756	+0. 0334	-0.0341
0 7—4	2. 54838	- 2.69748	l 32.	
ı 6—4	+ 0.53021	+ 0.25365	0. 0297	+0.0201
-I 9-4	+ 0.66570	+ o. 18655	+0. 0116	0, 0037
0 8-4	— o. 64584	— o. 19308		
I 7— 4	+ 0. 10036	o. o1604	-o. oo81	+0,0001
—I IO— 4	+ 0. 10783	— o. o2865	+0.00257	+0.00047
0 9—4	— 0. 10644	+ 0.02613		
18-4	+ 0.01155	— o. o1104	-0.0013	0.0008
—I II— 4	+ 0.01170	— o. or 199	+0.0004	+0.0003
0 10—4	— o. o116886	+ 0.0115086		
1 9— 4	+ 0.00039	— 0.0022 7	0.0001	—о. оооз
0 11—4	— 0. 00062	+ 0.00223		
I 10— 4	0, 00060	+ 0.00065		
_1 I— 5	— 0. 00049	- 0.00241		
I — I — 5	— 0.00017	— o. ooo78		
—I 2— 5	+ 0.00500	+ 0.02873		
o 1— 5	- 0.01734	— o. o8493		
I 0— 5	+ 0.01789	+ 0.08566		
-r 3-5	— 0. 02898	— o. o4o6o	0.0041	+0.0006
0 2— 5 1 1— 5	0.00303 0.00353	+ 0.02673		
I I 5 -I 4- 5	+ 0.00352 + 0.99604	— 0.00005 — 0.53330	-0.0014	0.000 5
0 3-5	0. 79776	— 0. 52220 + 0. 01884	+0.0316	+o. o378
1 2-5	+ 0. 16006	+ 0.01004	0. 0528	±0.0080
—I 5— 5	+ 0.60860	+ 14. 24175	+0. 1725	+0. 0080 0. 3986
0 4-5	+ 1.99383	— 11. 64981		-0. 3900
1 3-5	— o. 78322	+ 2.68920	— 0. 1886	+0.4126
—ı 6— 5	71. 52119	— 40. 27642	+0. 2047	-0. 1320
0 5 5	+67. 06263	+ 36.69579	''	
I 4 5	— 16. 31481	 9. 09478	—о. 1735	+o. o876
<u>-1</u> 7— 5	 46. 403 72	2. 01085	o. 0776	-0.0115
0 6— 5	+43.94724	+ 1.91709	İ	Ť
I 5— 5	 9. 29195	+ 0.60525	+0. 1073	+0.0025
—1 8— 5	— 1 3. 30987	+ 6.47574	- 0. 0726	0. 0436

Arg.	Т	N	$\frac{1}{n'}$	$rac{d\mathbf{R}'}{dt}$
J	sin.	cos.	cos.	sin.
ж i ' i	11	,,	"	"
0 7-5	+12.83709	- 6. 13302		
ı 6— 5	- 2. 16221	+ 1.65307	+0.0647	+0.0454
—ı 9— 5	- 2. 02539	+ 2.90856	-0, 0192	0. 0291
o 8— 5	+ 2.00370	— 2.8o56o		
I 7— 5	— o. 19946	+ o. 58058	+0.0111	+0.0251
—I 10— 5	— o. o6333	+ 0.70862	0. 0011	-0.0100
0 9— 5	+ 0.07275	— o. 69450		
I 8— 5	+ 0.02979	+ 0.11411	0.0010	+0.0070
—I II— 5	+ 0.05337	+ 0. 11438	+0.0009	0. 0022
0 10— 5	— o. o5o76	0. II400		
I 9— 5	+ 0.01501	+ 0.01342	-0.0009	+0.0011
-1 12-5	+ 0.01710	+ 0.01185	+0.0003	-0.0003
0 11-5	— 0. 01689	- 0.01233	0.0000	0.0000
1 10 5	+ 0.00338 + 0.00282	+ 0. 00084 + 0. 00050	0. 0002	0.0000
—I 13— 5	,	— 0.00036		
0 I2— 5 I II— 5	— 0. 00333 + 0. 00037	+ 0.00005		
o 1— 6	— 0. 00126	— 0. 00612		
-I 3-6	— 0.00120 — 0.00174	— 0. 00171		
0 2-6	0,00000	+ 0.00171		
1 I— 6	+ 0.00004	- 0.00007		
-1 4-6	+ 0.04495	- o. o4847	+0.0002	+0.0038
0 3—6	— 0. 04464	+ 0.01233	10,0002	10.0030
I 2—6	+ 0.00823	+ 0.00215	0, 0021	+0.0001
-ı 5-6	+ 0.64099	+ 0.87014	+0, 0363	_o. o196
0 4-6	— 0. 22344	- o. 8o6o7		
ı 3—6	- 0.00516	+ 0. 19707	—o. o127	+0.0378
— 1 6— 6	—10. <u>353</u> 97	+ 2. 37338	0. 2010	— 0. 1476
o 5 6	+ 9. 13914	— o. 51939	ľ	
r 4—6	— 2. 30015	— o. 10173	+0. 2098	+o. 1604
_1 7— 6	+13.13057	-44. 99210	о. об35	—о. 1547
0 6-6	11.82843	+42.83535	1	1
ı 5—6	+ 3. 19966	—11. 12902	+0.0422	+0. 1331
—ı 8— 6	— 5. 42124	—30. 71983	—o. 0152	+0.0259
o 7— 6	+ 5.08044	+29. 40624		
1 6—6	— 1. <u>5</u> 6414	— 6.6 17 80	+0.0123	0. 0467
_1 9—6	— 6. 9069 7	— 8. 96409	o. o346	+0.0370
o 8 6	+ 6.65490	+ 8.71890		[
1 7— 6	— 1.67922	— 1. 5 6369	+0.0351	o. o343
—ı 10— 6	— 2. 7 8286	— 1. 21282	— 0. 0226	+0.0087
0 9—6	+ 2.71095	+ 1.21317	ŀ	}
и 86	— o. 56704	— 0. 10429	+0.0194	~ 0. 0045
-1 II 6	— o. 66978	+ 0.06823	o. 0077	-0.0009
о 10— 6	+ 0.66150	— o. o5841	l	
1 9— 6	o. 11282	+ 0.04610	+o. oo53	+0.0018
— I 12— 6	— о. 10593	+ 0.07651	0.0017	0.0011

Arg.	Т	,		dR' di
	sin.	cos.	808	sin.
и i' i о п— 6	" + 0. 10644	., 0. 07464	"	"
1 10—6	- 0.01295	+o. 01935	1.0.0000	+0.0010
1 13 6	— 0. 01044	+0. 02091	+0,0009	70.00.0
0 12— 6	+ 0.01134	-0. 02052		
1 11-6	— 0.00117	+0.00377	Ī	
I 14 6	— 0. 00020	+0.00040	İ	
1 12—6	+ 0.00055	-0.00112	İ	
	,			
-I 4-7	+ 0.00160	—0. 00329		
0 3-7	— 0. 0024	+0.0012	}	
I 2— 7	+ 0.00058	+0.00011	10.0006	
-I 5- 7	+ 0.06154	+0.03657	+0.0036	+0.0003
0 4— 7 1 3— 7	- 0.0294 + 0.00263	—0. 0456 —0. 01163	o. oo13	10,000
	_ 0. 64180	+0.68033		+0.0020
O 5-7	+ 0.6636	+0.00033 0.3741	—o. oo87	0, 0295
1 ' '	_ 0. 18233		10.0220	10.0700
I 4— 7 —I 7— 7	3. 04559	+0.05361	+0. 0220 -0. 1067	+0.0190
0 6-7		—6. 7844 7	-0.1007	+0.0912
I 5— 7	- 0. 33211	+6. 3201 -1. 69777	+0. 1164	0. 0956
_1 8— 7	+26. 22716	十1. 25454	—o. 1089	+0.0200
0 7-7	25. 2525	-0. 7917	-0.1009	70.0200
I 6 7	+ 6.88722	+0.31847	+0. 0953	o, o1o8
I 9- 7	+18.73810	-7. 60789	+0.0020	+0.0090
0 8-7	18. o735	+7.4121	1 , 0. 0020	70.0090
1 7-7	+ 4. 25317	-2.09548	-o. o158	-o. oog7
—I IO— 7	+ 5. 36501	-6. 29392	+0.0161	+0.0243
0 9—7	— 5. 2494	+ 6. 1170	'	' ' '
ı 8— 7	+ 0. 96673	—1. 50824	0. 0158	0. 0248
-ı ıı- 7	+ 0.51209	2. 40578	+0.0025	+0.0161
0 10-7	— 0. 5223	+2.360 1		,
I 9— 7	+ 0.00785	о. 50066	-0.0003	0. 0138
—I I2— 7	— 0. 17451	0. 57187	-0.0020	+0.0054
0 11-7	+ 0. 1662	+0. 5679	l	
1 10— 7	- 0.05982	0. 09927	+0.0022	0. 0038
I 13 7	— 0. 09269	-o. o87o6	-0.0012	+0.0011
o 12— 7	+ 0.0891	+0.0870	1	
1 11-7	— o. o1989	—о. 0096 7	+0.0009	o. ooo6
—ı 14— 7	0. 00179	-0.00171		
I I2 7	+ 0.00501	-+0. 00458		1
—ı 5— 8	+ 0.00510	+0.00104		
0 4 8	0.0024	-0.0024		
ı 3—8	— o. ooo51	+0.00056		
—ı 6— 8	— o. o2106	+0.06573	+0.0009	0, 002 ²
0 5—8	+ 0. 0363	0.0417	, , , ,	.,
1 4 8	- 0.01205	+0.00730	+0.0012	+0.0018
_r 7— 8	— o. 63382	-0. 40047	0.0215	+0.0015
				[-0.00 1]

Arg.	Т	ı	$\frac{1}{n'}\frac{d\mathbf{R'}}{dt}$	
	sin.	cos.	eos.	sin.
n i' i	"	"	"	"
o 6 8	+0.4323	+ 0.4620	10.0774	0.0103
1 5—8	—o. o8852	— o. 13862	+0.0174	-0.0103 +0.0693
—ı 8— 8	+4. 01398	- 2.92508	+0.0349	70.0093
0 7—8	3. 8994	+ 2. 1963	0. 0369	o. o761
1 6—8	+1.09582	— o. 50831	o, ooo6	+0.0709
—ı 9— 8	+2.81889	+14. 20255	_0,0000	10.0709
o 8— 8	—3. 0009	—13. 7838	+0.0042	0. 0629
1 7—8	+0.77454	+ 3.90507	+0.0024	+0.0063
_1 10— 8	+7. 27448	+10. 50958		1 -1 -1 -1
0 9 8	—7. I304	—10. 1895	0. 0042	+0,0022
1 8-8	+1.95009	+ 2.47755	+0.0151	0. 0053
-1 II-8	+5. 12638	+ 2.76778	· •	20
0 10-8	5. 0178	2. 7204	o. o159	+0.0057
1 9— 8 —1 12— 8	+1. 23890	+ 0.49213	+0.0104	+0.0007
-I I2- 8 0 II- 8	+1. 90645 -1. 8807	+ 0.01015	,	
1 10—8	· ·	0.0238	-o. oog1	0.0017
-I I3-8	+0.40603	— 0. 06564 — 0. 24774	+0.0037	+0.0022
0 12— 8	+0.44791	+ 0. 2352		
1 11—8	—0. 4434 +0. 07719	- 0. 06511	0. 0025	-0, 0021
_1 11— 8	+0.00868	— 0. 00475		
1 12— 8	-0.02396	+ 0.01355		
_1 6_9	+0.00029	+ 0.00423		
0 5-9	+0.0015	0.0030		
1 4-9	-0.00072	+ v. 00061	l	
_i 7— 9	o. o6o68	— o. oo639	-0, 0020	—0. 0010
0 6 9	+0.0450	+ 0.0219		
I 5— 9	-0,00942	— o. oo833	+0.0018	0. 0005
—ı 8— 9	+0. 19633	- o. 53191	-0, 0022	+0.0142
0 7— 9	— 0. 2643	+ 0.4098		
ı 6— 9	+0.08526	— 0. 09689	-0.0033	o. o133
-ı 9-9	+2.4010	+ 2.1511	+0.0413	-0.0091
0 8-9	—1.9920	— 2. 1849		
1 7—9	+0.5093	+ 0.6496	— о. 0 460	+0.0095
— 1 10— 9	 7. 0961	+ 3.4142	+0. 0434	+0.0096
0 9—9	+6.9231	- 3. 5052		
ı 89	2. 0293	+ 0.9691	—o. o390	0. 0106
_1 II— 9	5 . 3431	+ 5.8259	+0.0072	+0.0021
0 10-9	+5. 1930	5.7390		
I 9— 9	1.2898	+ 1.5666	— 0. 002 3	+0.0001
I I2 9	—1. 108 ₀	+ 3.8293	0.0005	o. oo85
o 11— 9	+1.0917	— 3. 7671		
1 10-9	—o. 170 <u>5</u>	+ 0. 9368	+0,0010	+0.0093
-1 13 9	+0. 3036	+ 1.4189	+0.0021	0, 0065
0 12 9	0. 2763	— 1.3854		
1 11-9	+0. 1023	+ 0. 2936	0.0021	+0.0054

Arg.	,	T'		dR' di
	sin.	608.	cos.	sin.
n i' i	,,	"	//	"
—î 14— 9	+0.0057	+0.0274		}
1 12-9	—o. o168	-o. o766		
—1 7—10	0. 0053	+0.0016		
0 6-10	+0.0027	+0.0006		
1 5—10	+0.0004	-o. ooo5		
_т 8—то	+0.0098	0. 0529	-0.0011	+0.0013
o 7—10	o. o318	+0.0441		
1 6—10	+0. 0202	-0.0109	+0.0002	-0.0014
-1 9 - 10	+0. 4082	+0. 0610	+0.0087	+0.0033
о 8—10	—0. 3414	—о. 1233		
1 7—10	+o. o868	+0.0475	-o. oo88	-0.0004
1 1010	0. 9941	+1.7732	+0.0009	0, 0228
0 910	+1.0641	—r. 5597		
1 8—10	—o. 333 5	+0. 4226	-0.0013	+0.0257
—I II—IO	—2. 7624	—3. 2038	+0.0113	-0. o24 7
0 10-10	+2.8206	+3. 1320	[
1 9—10	—о. 8о8 7	0.9511	0. 0116	+0. 0224
—I I2—I0	-4. 1813	-2. 3639	+0.0040	-0. 0054
0 1110	+4. 1346	+2. 2935		
1 10-10	—1. 1369	—o. 5739	-0, 0022	+0.0027
—I I3—I0	 2. 71 7 6	—o. 1471	-o. oo43	0. 0011
0 12-10	+2.6208	+o. 1698		
01	 0. 6290	+0.0038	+0.0047	+o. ooo6
—I I4—I0	0.0522	0. 0029		
I 12—10	+0. 1476	+0.0077		
—ı 8—ıı	0.0004	0. 0043		
0 7—11	0.0021	+0,0042		
1 6—11	+0.0018	-0.0012	i	
1 911	+0. 0391	-0.0142	+0.0007	+0.0009
o 811	0. 0354	+0.0027		
¥ 711	+0.0092	+0.0011	-0.0010	0, 0004
-I IO-II	+0.0184	+o. 2888	+0.0033	0, 0048
0 9—11	+o. o288	—o. 2571		
1 811	0. 0171	+0.0706	0.0017	+0.0053
I IIII	—1. 2030	—о. 3558	o. o115	0. 0036
0 10—11	+1. 1010	+0. 4203		
1 9—11	0. 3117	0. 1426	+0.0133	+0.0043
I I2II	+1.2409	—r. 8777	—0. 0130	0, 0100
11—11 O	—1. 2078	+1.9158		
1 10—11	+0.3848	o. 562 6	+0.0119	+0.0099
—I I3—II	+0.7830	—2. 85 95	-0.0036	0. 0041
D 12—11	—о. 7656	+2.7234		
1 11—11	+0. 1932	-0. 7059	+0.0021	+0.0029
—I I4—II	+0.0150	-0.0549		
I I2—II	0. 0428	+0. 1557		

Arg.	T		$rac{1}{n'}rac{d{ m R}'}{dt}$		
	sin.	cos.	cos.	sin.	
и i' i -1 9-12 о 8-12 1 7-12	+0. 0026 -0. 0027 +0. 0010	-0.0031 +0.0024 -0.0011	u		
—I 10—I2	+0. 0162 - 0. 0081	+0. 0263 -0. 0249	+0.0007	0.0003	
1 8—12 —1 11—12	+0.0009 0.1888	+0. 0066 +0. 0523	0. 0004 0. 0025	+0.0006 -0.0026	
0 10—12 1 9—12 —1 12—12	+0. 1770 0. 0514 +0. 0411	—0. 0195 —0. 0009 —0. 7440	+0. 0029 -0. 0034	+0.0019 +0.0056	
0 II—I2 I I0—I2	—o. 0864 —o. 0358	+0.7047 0.2076	- +0. 0039	—0. 0064	
-I I3-I2 0 I2-I2 I II-I2	+1. 2761 -1. 1982 +0. 3206	+0. 2766 -0. 2550 +0. 0902	-0. 0072 +0. 0068	+0.0053 -0.0046	
—I I4—I2 I I2—I2	+0. 0245 0. 0694	+0. 0053 -0. 0153			

The preceding expressions have to be integrated, consequently we give the logarithms of the factors proper to each argument:

Logarithms of the integrating factors for Jupiter.

Arg.	$\log \frac{n}{i'n'+in}$	Arg.	$\log \frac{n}{i'n'+in}$	Arg.	$\log \frac{n}{i'n'+in}$	Arg.	$\log \frac{n}{i'n'+in}$
	i'n'+in	Aig.	i'n' + in	Aig.	i'n' + in	6,	i'n'+in
i' i		i' i		i' i		i' i	
1 —0	0. 0000000 <i>n</i>	3-5	9.4211383 <i>n</i>	6 6	9. 4456460 <i>n</i>	9 9	9. 26955n
0 2	9. 6989700n	3 — 6	9. 31949 <i>n</i>	6— 7	9. 3387663 <i>n</i>	9 — 10	9. 19546n
0 — 3	9. 5228787 <i>n</i>	3 - 7	9. 23718n	6 8	9. 2530636n	9 — 11	9. 13219n
0-4	9. 397942	3 8	9. 1680n	6 9	9. 18152n	9 — 12	9. 07697 <i>n</i>
0 5	9. 3010 <i>n</i>	3 - 9	9. 1084n	6 — 10	9. 12011 <i>n</i>	9-13	9. 02799n
o — 6	9. 2218n	4+2	9. 4424	6 — 11	9. 0663 <i>n</i>	10 — 3	9. 9885
1+5	9. 2674	4+ 1	9. 58324	7 0	9. 5499	10 — 4	1.57090
1+4	9. 3563	4 0	9.7929735	7— I	9. 74021	10 — 5	0. 01 182 <i>n</i>
1+3	9. 46818	4- 1	0. 2141409	7 — 2	0. 08682	10 6	9. 70484 <i>n</i>
1+2	9. 61930	4- 2	0. 4097644 <i>n</i>	7 — 3	0. 7418456n	10 7	9. 52678n
1+1	9. 8530395	4-3	9. 8572177 <i>n</i>	7 - 4	9. 9276772n	10 — 8	9. 40087 <i>n</i>
1 0	0. 3950335	4 4	9. 6217373n	7 — 5	9. 6613048 <i>n</i>	10-9	9. 30337n
1 — 1	o. 2237972n	4 — 5	9. 4698956n	7 6	9.4974092n	10 — 10	9. 22380n
I — 2	9. 7966097 <i>n</i>	4 - 6	9. 3576090n	7 7	9. 3786993 <i>n</i>	10 — 11	9. 15 657 n
1 — 3	9. 5854756n	4 - 7	9. 26847n	7 — 8	9. 28557n	10 12	9. 0983 7 n
1-4	9. 4440216 <i>n</i>	4 8	9. 19455n	7 9	9. 20893n	10 — 13	9. 0471 <i>n</i>
1 5	9. 33750n	4- 9	9. 1314n	7 10	9. 14380 <i>n</i>	10 14	9.001 <i>2n</i>
1 6	9. 2520n	4 — 10	9. 0763 <i>n</i>	7 11	9. 08718 #	17 _ 4	0.26600
1 — 7	9. 1806n	5 + 2	9. 3965	7 12	9. 0371 n	11 — 4	0. 36699 0. 24378 <i>n</i>
2+4	9. 3183	5+1	9. 5209	8 — I	9. 6534	11 — 6	9. 80397 n
2+3	9.4196	5 0	9. 69606	8 — 2	9. 91311	11 - 7	9. 58999 <i>n</i>
2+2	9. 55201	5 1	9. 9942063	8 — 3	0. 6546508	11 8	9. 30999n 9. 44728n
z + 1	9. 7434333	5 - 2	1. 8719342	8 — 4	0. 1087344n	11 — 9	9. 447 2015 9. 34004n
2 0	0. 0940035	5 - 3	o. 0058720n	8 — 5	9. 7499431 <i>n</i>	11 — 10	9. 25411n
2 — I	0.7107944 <i>n</i>	5 — 4	9.7018961n	8 6	9. 5561876n	11-11	9. 18240n
2 2	9. 9227672n	5-5	9. 5248272n	8 7	9. 4226792 <i>n</i>	11 — 12	9. 12088n
2-3	9. 6586391 <i>n</i>	5 — 6	9. 3994005 <i>n</i>	8-8	9. 3207072n	11 — 13	9. 0670n
2-4	9. 4955797#	5 — 7	9. 3021981 <i>n</i>	8 9	9. 2381840n	11 — 14	9. 0191 <i>n</i>
2-5	9. 37731n	5 - 8	9. 22282n	8 — 10	9. 16887n		
2 6	9. 28445n	5-9	9. 15574n	8 — 11	9. 10910 <i>n</i>	12 — 5	0.77529n
2 — 7	9. 2080n	5 — 10	9. 0976n	8 — 12	9. 05658n	12 — 6	9. 93264n
2 — 8	9. 1430n	5 — 11	9. 0464 <i>n</i>	8 — 13	9.0097 <i>n</i>	12 7	9. 66399 <i>n</i>
3+3	9- 3759				_	12 - 8	9. 49925n
3+2	9. 4938	6 + I	9. 4665	9 — 2	9. 7894	12 9	9. 38010n
3+1	9. 65599	6— 1	9. 6169 9. 84890	9-3	0. 20469	12 — 10	9. 28670n
3 0	9. 9179122	6- 2	o. 3807859	9-4	0.42501 <i>n</i>	12 — 11	9. 20987 <i>n</i>
3 1	0. 6818160	1		9 — 5 9 — 6	9. 86144n	12 — 12	9. 14462 <i>n</i>
3-2	o. 1013065n	6-3	0. 2336731 <i>n</i> 9. 8002765 <i>n</i>	·	9. 62419n	12 — 13	9. 0879 <i>n</i>
3-3	9. 7466760 <i>n</i> 9. 5540936 <i>n</i>	6— 4 6— 5	9. 5877269n	9 - 7	9. 47162n	12 — 14	9. 0377 <i>n</i>
3-4	9. 55409307	· - 3	y. 50//2091	9- 0	9. 35894 <i>n</i>	12 — 15	8. 9928 <i>n</i>

Logarithms of the integrating factors for Saturn.

1		41	1	1		II .	
Arg.	$\log \frac{n'}{i'n'+in}$	Arg.	$\log \frac{n'}{i'n'+in}$	Arg.	$\log \frac{n'}{i'n'+in}$	Arg.	$\log \frac{n'}{i'n'+in}$
i' i		i' i		i' i		i' i	
10	0,0000000	6—3	9.8386396n	56	9. 0043670n	7— 9	8.81389n
2 0	9. 6989700	7—3	0. 3468120n	66	9. 0506124n	8 9	8.84315n
3 0	9. 5228787	83	0. 2596173	7—6	9. 1023757n	9 — 9	8. 87452n
4 0	9. 3979400	9—3	9. 8096612	8—6	9. 1611541 <i>n</i>	10 9	8. 90834n
5 0	9. 30103	10—3	9. 59346	96	9. 2291518n	11 9	8. 94501n
6 0	9. 2218	11—3	9- 44977	10—6	9. 3098085n	12- 9	8. 98506n
7 0	9. 1549			11-6	9.40894n	13- 9	9. 02919 <i>n</i>
		- 1-4	8. 96125n	12-6	9. 53761n	14 9	9.0783n
-4-1	9. 18820n	04	9. 00291 <i>n</i>	13-6	9. 72126n		
-3-I	9. 26095 <i>n</i>	I—4	9. 0489881 <i>n</i>	14—6	0. 0458n	4—10	8.681 <i>2n</i>
—2 —1	9. 34840n	2-4	9. 1005462n		0 . 0 . 6	5-10	8. 7026n
-I-I	9. 4580060 <i>n</i>	34	9. 1590601 <i>n</i>	1-7	8. 7856n	6—10	8. 7251n
0—1	9. 6049665 <i>n</i>	4-4	9. 2267037n	2-7	8. 8130n	7—10	8. 74877n
1—1	9. 8287637 <i>n</i>	5-4	9. 3068626n	3-7	8. 84214n	8—10	8.77383n
2—1	0. 3157609 <i>n</i>	6—4	9. 4052430n	4-7	8. 87344n	9—10	8. 80043n
3—1	0. 2867824	7—4	9. 5326437n	5-7	8. 907 16n	10—10	8.82876n
4—1	9. 8191074	84	9.7137009n	6—7	8. 9437329n	11-10	8.85908n
5—1	9. 5991729	94	0. 0299790n	7-7	8. 9836657 n	12-10	8.89166n
6—1	9. 4538678	10-4	1. 1758707	8—7	9. 0276457n	13-10	8. 92690n
7—I	9. 3451812	114	9. 9719575	9-7	9. 0765864n	14-10	8. 96 52n
1—8	9. 25832	12—4	9. 68472	10—7	9. 1317510n		
				11-7	9. 19496n	5—11	8. 6514n
<u>-3-2</u>	9.09872n	— 1—5	8.87236n	12-7	9. 26895n	6—11	8. 6713n
-2-2	9. 15698n	0—5	8. 90600n	13-7	9. 3582n	711	8. 6921 <i>n</i>
—I—2	9. 2 242695 <i>n</i>	ī −5	8. 9424624 <i>n</i>	14-7	9.4707n	8—11	8. 71407n
0-2	9. 3039365 <i>n</i>	2—5	8. 9822730n		0	11—6	8. 73716 <i>n</i>
I—2	9. 4015761 <i>n</i>	35	9. 0261048 <i>n</i>	2-8	8. 74796n	10-11	8. 76154 <i>n</i>
2—2	9. 5 277337 n	45	9. 0748621 <i>n</i>	3-8	8. 77297n	11-11	8. 78737n
3-2	9. 7062730n	55	9. 1297937 <i>n</i>	48	8. 79952n	12-11	8. 81484 <i>n</i>
4—2	0.0147309 <i>n</i>	6—5	9. 1926934 <i>n</i>	5-8	8. 82779n	13-11	8. 84416 <i>n</i>
5—2	1.4769007	7-5	9. 266 271 3n	6-8	8.85803n	1411	8. 8756n
6-2	9. 9857524	85	9. 3549096 <i>n</i>	7—8	8. 8905362n		
7—2	9. 6917878	9—5	9. 4 664028 <i>n</i>	8—8	8. 9256737n	6—12	8. 6234 <i>n</i>
8—2	9. 51808	10—5	9. 6167909 <i>n</i>	9-8	8. 9639064n	7-12	8. 6421 <i>n</i>
9—2	9. 39433	11-5	9. 84875n	10—8	9. 0058326n	8-12	8. 6615 <i>n</i>
	0.004####	12-5	0. 38026 <i>n</i>	11-8	9.0522430n	9—12	8. 68194 <i>n</i>
-2-3	9. 02457n	135	0. 23405	128	9. 10421 <i>n</i>	10—12	8. 7 0334 <i>n</i>
-1-3	9. 07314n	14-5	9. 80042	13—8	9. 16326n	11-12	8. 72584n
0—3	9. 1278452n	0 6	9 9060	14—8	9. 2316n	12—12	8. 74958n
1-3	9. 1904421 <i>n</i>	0-6	8. 82682n		9	13-12	8. 77469n
2—3	9. 2636055n	16	8. 85699n	3-9	8.7133n	14-12	8. 801 <i>3n</i>
3-3	9. 3516425n	2—6	8. 88941n	4-9	8.7364n		Ì
4-3	9. 4621841n	36	8. 9244550n	5-9	8. 7607n		
5—3	9. 6108385n	46	8. 9625755n	69	8. 78648n		l

The functions W and R are obtained by means of the formulæ

$$W = \int Tndt \qquad R = \int \left(\frac{1}{n} \frac{dR}{dt}\right) ndt$$

The portions involving other multiples of γ than the single result from employing the system of multipliers η and θ , as has been explained. In most cases the terms arising from the θ multipliers can be neglected. As an illustration of this process, and on account of its interest, the terms which make up the great inequalities of the two planets may be given. They are as follows:

Arg.	cos. sin.	Arg.		
		' <u> </u>	cos.	sin.
-I 5-I - + + + + + + + + + + + + + + + + + +	0.00008	0202 —I 6- 0156 0 5- 3106 I 4- 0264 2 3- 0072 3 2- 0002 4 I- 5 0-	* '' -2	

W and R must be completed by the addition of functions of r, having the forms

$$W = k_0 + k_1 \left(\frac{\rho}{a}\cos\varphi + \frac{3}{2}e\right) + k_2 \frac{\rho}{a}\sin\varphi \qquad \qquad R = k_3 \frac{\rho}{a}\cos\varphi + k_4 \frac{\rho}{a}\sin\varphi$$

the k being constants. It is, however, more commodious to alter the signification of the k so that we may write in the case of Jupiter

$$W = k_0 + k_1 \cos \gamma + k_2 \sin \gamma + k_2 \sin \gamma + [8.3821074] k_1 \cos 2\gamma + [8.3821017] k_2 \sin 2\gamma + [6.9403270] k_1 \cos 3\gamma + [6.9404535] k_2 \sin 3\gamma + [5.5723410] k_1 \cos 4\gamma + [5.5724929] k_2 \sin 4\gamma + [4.2452120] k_1 \cos 5\gamma + [4.2453807] k_2 \sin 5\gamma$$

$$\mathbf{R} = -[8.8599027] k_3 + k_3 \cos \gamma + k_4 \sin \gamma + [8.3821074] k_3 \cos 2\gamma + [8.3821917] k_4 \sin 2\gamma + [8.3821074] k_3 \cos 2\gamma + [8.3821917] k_4 \sin 2\gamma + [8.3821074] k_5 \cos 2\gamma + [8.3821917] k_6 \sin 2\gamma + [8.3821074] k_6 \sin 2\gamma + [8.3821074] k_7 \sin 2\gamma + [8.3821074] k_8 \sin 2\gamma + [8.$$

and in the case of Saturn

$$W' = k_0 + k_1 \cos \gamma' + k_2 \sin \gamma'$$

$$+ [8.4472006] k_1 \cos 2\gamma' + [8.4473145] k_2 \sin 2\gamma'$$

$$+ [7.0705210] k_1 \cos 3\gamma' + [7.0706918] k_2 \sin 3\gamma'$$

$$+ [5.7676379] k_1 \cos 4\gamma' + [5.7678429] k_2 \sin 4\gamma'$$

$$+ [4.5056153] k_1 \cos 5\gamma' + [4.5058431] k_2 \sin 5\gamma$$

$$\mathbf{R}' = -[8.9252322] k_3$$

$$+ k_3 \cos \gamma' + k_4 \sin \gamma'$$

$$+ \dots \dots \dots \dots$$

The perturbations of the fundamental argument, the residual perturbations of the natural logarithm of the radius vector, and the perturbations perpendicular to the plane of the orbit, so far as they depend on the first power of the disturbing force, are given by the formulæ

$$\frac{d\delta z}{dt} = \overline{W} \qquad \qquad \frac{\mathbf{i}}{n} \frac{d\nu}{dt} = -\frac{\mathbf{i}}{2} \left(\frac{d\overline{W}}{d\nu} \right) \qquad \qquad \frac{u}{\cos i} = \overline{R}$$

where the dash above the quantities denotes that τ has been changed into t or, which is the same thing, γ into g.

The arbitrary constants k have been so assumed that the expressions for the perturbations may be simplified as much as possible. We take k_0 , so that δz may contain no term proportional to t, k_1 , and k_2 , so that the terms having the argument g may disappear. In like manner k_3 and k_4 are determined so that $\frac{u}{\cos i}$ may be free from terms having the argument g. In the case of Jupiter this has led us to put

$$k_0 = + 14''.2801$$
 $k_1 = - 1''.6777$ $k_2 = + 1''.6921$ $k_3 = + 0''.0636$ $k_4 = + 0''.1414$

and in the case of Saturn

$$k_0 = -517''.7721$$
 $k_1 = -14''.9831$ $k_2 = +1''.5080$ $k_3 = -0''.5642$ $k_4 = +0''.7901$

The expressions for $\frac{d\delta z}{dt}$ and $\frac{1}{n}\frac{d\nu}{dt}$ follow:

Arg.	do d	$\frac{\delta z}{t}$	$\frac{1}{n}$	đ v đt
	608;	sin.	sin.	cos.
i' i	11	"	"	// 0. 0122808
0— 1	— I. I420	— 1.0174	+ 1.1610	— o. 9308
	+ 1.0173636nt	- I. 1420391nt	— 0. 5086818 <i>nt</i>	— 0. 5710195 <i>nt</i>
0— 2	o. o771	+ 0.0170	+ o. o835	0.0000
1	+ 0.0245236 <i>nt</i>	— 0. 0275342nt	— 0.0245236 <i>nt</i>	- 0. 0275342nt
o— 3	— o. oo17	+ 0.0010	+ 0.0033	+ 0.0004
	+ o. 0008868nt	— 0.0009957nt	— 0.0013302nt	- 0. 001493 5 nt
1+3	0.00032	o. ooo61	— o. ooo6	+ 0.0004
1+ 2	- o. o118	0.0017	— o. o133	+ 0.0013
1+1	- o. 3720	+ 0.1052	— o. 2603	0. 0597
1 0	— 3. 3928	1.7597	— o. 7161	+ o. 1939
1-1	— 9. 1757	+47. 1662	+ 2.9759	+15. 2960
I— 2	+ o. 3997	+ 2. 2087	— 0. 1906	+ 1.6614
1 — 3	+ 0.0274	+ 0.0893	o. o258	+ 0. 1050
1— 4	+ 0.0014	+ 0.0033	— o. oo19	+ 0.0057
2+ 2	— o. oo14	- 0.0012	— o. oo19	+ 0.0016
2+ I	— o. o417	— 0. 0223	— o. o366	+ o. o218
2 0	— 1. O199	- I. o268	0.4698	+ 0.4065
2— I	- 24. 04532	+ o. 86691	+ 3.53984	— 0. 19888
2— 2	-214.0201	—91 . 76 88	+120. 3064	—51. 5832
2— 3	- 5.4539	- 3. 1129	+ 5.8327	— 3. 0764
2 4	o. 1899	— o. 1250	+ 0.3069	— о. 1800
2- 5	— o. oo81	- 0.0054	+ 0.0174	— o. o106
3+ 1	+ 0.0010	+ 0.0039	+ 0.0013	0.0042
3 0	+ 0.0906	+ 0. 1654	+ 0.0440	o. og6o
3— 1	+ 2.5944	+ 1.6632	+ 0.4591	— o. 3340
3— 2	+ 39.6924	+52. 2365	16, 5368	+22. 3896
3 3	— 15. 6852 — 0. 9761	+24.6755	+ 10.8438	+17.5836
3— 4 3— 5	- 0. 9/01 - 0. 0467	+ 0. 7016 + 0. 0168	+ 0.9797	+ 0.8822
3— 5 3— 6	— 0. 0022	+ 0.0005	+ 0.0651	+ 0.0390
4 0	+ 0.0013	+ 0.0102	+ 0.0041 0.0001	+ 0.0020
4— I	+ 0.0498	+ 0. 1955		0.0072
4 2	+ 0.9030	+ 6. 3979	+ 0.0288 - 0.0967	— 0. 0919 — 1. 5544
4 3	19. 0362	+ 9.0422	+ 11.5647	+ 1.5544
4— 4	+ 5.3687	+ 6. 5947	- 4. 0749	+ 5.7324
4 5	+ 0. 1126	+ 0.5330	- 0. 1716	+ 5.3143
4— 6	— o. oo51	+ 0.0284	- 0.0005	+ 0.5649 + 0.0402
4— 7	0.0005	+ 0.0013	+ 0.0003	+ 0.0025
5 0	+ 0.0067	— 0. 0090	+ 0.0066	
5— I	+ 0. 2796	— 0. 3932	+ 0.1413	+ 0.0093
	- 17-	353~	1 011413	+ 0. 1951

Arg.	$\frac{d\delta}{dt}$	<u>z</u>	$\frac{1}{n}$	
ŭ	cos.	sin.	sin.	cos.
i' i	"	"	11	"
5— 2	+ 5.67254	13. 33271	+ 0.07542	+0.11796
5— 3	+152.6838	+11.3735	75 .6574	+5.7237
5 4	+ 4.8731	+ 5.4299	— 4. 629 7	+4.0120
5— 5	+ 2.9701	— 1. 486 <u>5</u>	— 2. 6327	1. 1887
5— 6	+ 0.2863	+ 0.0133	— o. 3146	0.0105
5 7	+ 0.0164	+ 0.0087	0.0236	+0.0074
5 8	+ 0.0007	+ 0.0008	— o. oo14	+0.0008
6 1	+ 0.0021	0.0003	+ 0.0012	0.0000
6— 2	+ 0.0430	— o. o193	+ 0.0153	+0.0041
6— 3	+ 1.0234	+ 0.6703	— o. 33389	+0. 24544
6— 4	— о. 6738	+ 2.3519	+ 0.3837	+1.5534
6— 5	+ 2.0940	+ 0.0180	— 1.679 5	0. 0131
6 6	— o. 3486	— I. 2827	+ 0.2755	—I. 1442
6 7	+ 0.0431	0. 1452	— o. o346	0. 1587
6— 8	+ 0.0083	0.0084	- o. oo85	-0.0121
6 9	+ 0.0007	0.0004	— o. ooo8	-o. ooo7
7— 2	+ 0.0051	+ 0.0049	+ 0.0027	-0.0024
7— 3	+ 0.1240	+ 0. 2402	- 0.0112	+0.0309
7-4	— 1.2870	+ 1.2519	+ o. 7017	+o. 7065
7— 5	+ 0.7304	+ 0.4453	— o. 555o	+o. 3159
7— 6	+ o. 2083	0. 9416	— 0. 1670	— 0. 8053
7— 7	— o. 5807	+ 0.0198	+ 0.5308	-0.0003
7— 8	- 0.0711	— 0. 0412	+ 0.0792	-0. 0394
7 9	— 0.0038	— o. oo63	+ 0.0060	0.0070
7—10	— 0.0003	— o. ooo6	+ 0.0002	-o. ooo6
8 2	+ 0.0002	— 0. 0007	+ 0.0001	+0.0002
8— 3	+ 0.0026	— 0. 0206	+ 0.0009	+0.0033
8— 4	+ 0.3177	— 0. 0869	o. 1351	-o. o33o
8— 5	+ 0.1746	+ 0. 2678	— o. 1311	+0. 1772
8— 6	+ o. 2701	— 0. 3063	— o. 2077	o. 2588
8— 7	- 0.4311	— o. 1945	+ o. 3854	—о. 1666
8 8	— o. o533	+ 0. 2568	十 0.0597	+0. 2379
8— 9	— о. озо8	+ 0.0329	+ 0.0312	+o. o368
8—10	— o. oo45	+ 0.0014	+ 0.0051	+0.0024
8—11	0.0004	- 0.0002	+ 0.0004	o. 000I
9 3	+ 0.0010	— 0. 0005	+ 0.0005	+0.0002
9— 4	+ 0.0323	+ 0.0077	— 0. 0075	+0.0025
9 5	+ 0.0066	+ 0. 1417	— 0. 0071	+0.0850
9 6	+ 0.1313	— 0. 0439	0.0983	-0.0394
9-7	— o. 1285	— 0. 1712	+ 0.1170	0. 1412
9— 8	— o. 1431	+ 0. 1919	+ 0. 1283	+o. 1767
9 9	+ 0.1083	+ 0.0527	— 0. 1007	+0.0550
9—10	+ 0.0135	+ 0.0206	— o. o154	+0.0214
9—11	+ 0.0001	+ 0.0030	— o. ooo6	+0.0034
912	0.0001	+ 0.0003	+ 0.0001	+0.0003
L	A CUTD. 7		L	

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Arg.	$rac{d\delta z}{dt}$		$rac{1}{n} rac{d u}{dt}$	
	cos.	sin.	cos.	sin.
i' i	"	"	"	"
10 4	—o. 02767	<u> </u>	0. 00044	+0,00061
10— 5	+o. 1833	— 0. 3728	<u> </u>	—0. 1829
10 6	+0.0479	-0.0014	o. o357	o. oo57
10-7	-0. 0092	— о. 0739	+0.0116	о. обо2
1o— 8	—o. 1064	+0.0495	+0.0923	+0.0482
10 9	+o. o8o3	+0.0935	0. 0756	+0.0863
1010	+o. o365	0. 0427	— о. 0374	— 0. 0390
1011	+ 0.0126	0, 0046	-o. o133	0.0054
10—12	+0.0017	+0.0004	0.0019	+0.0003
11 5	+0.0050	0. 0036	_o. oo18	-0.0010
11- 6	+0.0121	+0.0098	0. 0080	+0.0059
11-7	+0.0085	0. 0208	—o. oo54	—o. 0165
11-8	<u></u> 0. 0426	0. 0032	+o. o367	-0.0001
11-9	- 0. 0146	+ 0. 0638	—о. 0158	+0.0576
11-10	+ 0. 0568	— о. озо9	o. o536	-0. 029 I
11-11	-0. 0147	0. 0218	+0.0130	0. 0225
11-12	-0.0010	—0. 0071	+0.0013	0.0074
12- 6	+0.0044	+0.0097	-0.0025	+0.0052
12- 7	+0.0052	-0.0037	-0.0035	—о. 0031
12- 8	0.0110	-0.0075	+ 0, 0096	0. 0054
12-9	-0.0072	-0. 0244	+0, 0049	+0.0224
12-10	+0.0373	0. 0003	0. 0351	0.0014
12-11	-o. oo82	0. 0328	+o. oo81	-0. 0322
12-12	0. 0127	+0.0030	+0.0131	+0.0022

The corresponding quantities for Saturn are :

Arg.		$rac{d\delta z'}{dt}$		$rac{1}{n'}rac{d u'}{dt}$	
		cos.	sin.	sin.	cos.
i' 0	<i>i</i>	"	11	11	,,, + o. 075066
I	0	-8. 6311	—5. 3501	— 7. 6361	+10. 1319
	ı	-5. 350080n't	+8. 631067n't	2.675040n't	- 4. 315533n't
2	0	—0. 7346	—I. 1722	-0. 4093	+ 1.7346
		-0. 149816n't	+0.241756n't	—0. 149816 <i>n't</i>	- 0. 241756n't
3	0	- 0. 0303	-0.0972	+0. 0233	+ 0. 1703
		0. 006294 <i>n't</i>	+0.010158n't	-0. 009441 <i>n't</i>	- 0.015237n't
4	0	0.0002	0.0077	+0.0078	+ 0.0132
	1	-0.000312n't	+0.000504n't	-0. 000624 <i>n't</i>	0. 001020n't
5	٥	- -0.0002	0.0005	+0.0010	+ 0.0006
-4-	. 1	+0.0003	0. 0003	0. 0000	+ 0.0002
-3-	1	+0.0019	+0.0004	-0. 0042	0,0000

Arg.	<u>d</u> d d	<u>Sz'</u> t	$\frac{1}{n'}\frac{\epsilon}{\epsilon}$	$rac{dv'}{dt}$
	608.	sin.	sin.	C OS.
i' i	,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,	"	"	"
-2- I	+ 0.0227	+ 0.0114	— o. o478	+ 0.0163
1-1-1	+ 0. 2802	+ 0.1311	— 0.4629	+ 0. 3204
0— I	- 2. 5227	+ 28. 9829	— 2. 6889	+ 8. 2224
1—1	+ 9.6656	— I. 3654	+48. 1544	+262. 5939
2.— Ⅰ	+204.9729	- 6.8944	 56. 2251	+ 3.2555
3 1	14. 5483	— Io. 4073	— 4. 969 7	+ 3.5005
4— I	— 0. 4471	— o. o399	- o. 4316	+ 0.1989
5— I 6— I	— o. o263	0.0040	— o. o316	+ 0.0280
	- 0.0018	- 0.0005	— o. oo15	+ 0.0027
7— 1	— 0.000I	- 0.0002	+ 0.0001	+ 0.0003
_2 2	+ 0,0006	— o. ooo6	- 0.0014	- 0.0015
—I— 2	+ 0.0099	— o. o108	— 0.0217	- 0.0146
0— 2 I— 2	— 0. 0979	+ 1.0448	— 0. 2758	— 0.0188
2— 2	+ 3. 3526 +87. 5789	— 10. 1030	1. 1744 90 #669	+ 10.5178 + 36.4790
3 2	+36.8496	+ 37.4603	—83. 5668	
4— 2	+ 30. 8490 7 8. 2220	+ 36.4676	-31. 2005	+ 25.4230 306.1645
5— 2		-629. 5161 + 80. 63232	+37.3212	— 1. 52185
6 2	—34. 32403 + 1. 1778		0, 80297	- 0. 2259
7— 2	+ 0.0331	+ 0.4359 + 0.0168	+ 0.5690 + 0.0295	— 0. 2239 — 0. 0142
8— 2	+ 0.0013	1 :	+ 0.0293	— 0.0006
i 3	+ 0.0002	+ 0.0008 - 0.0007	0.0000	— o. oo18
0— 3	— o. o118	+ 0.0554	0.0015	— 0, 0052
1-3	+ 0.1182	— 0.6269	+ 0.0881	+ 0.5273
2-3	+ 0.8781	+ 0.8416	1. 4465	+ 0.2740
3-3	+17.1428	— 23. 77 61	—18. 4562	25. 1481
4-3	+14.7028	- 6. 2679	—15. 1906	 7·4477
5-3	+ 7.2953	+ 0.9109	— 6. 8424	+ 0.4197
6- 3	+ 5.0024	+ 3.4675	— 3. 4094	+ 2.2076
7-3	— 1. o596	— 2. o9o5	+ 0. 2382	— o. 5277
8 3	— 0. 022I	+ 0.1181	0.0109	— o. o391
9— 3	+ 0.0007	+ 0.0024	o. ooo5	- 0,0022
0 4	— o. ooo7	+ 0,0032	+ 0.0001	0.0001
1- 4	+ 0.0064	— o. o358	+ o. oo81	+ 0.0341
2- 4	o. oooi	+ 0.0324	 0.0127	+ 0.0167
3- 4	+ 0.8945	- o. 3721	— o. 7506	o. 6953
4— 4	— 7. 6391	— 8. 501 7	+ 8. 3181	— 9· 4975
5— 4	— 1. 2828	— 6. 38oI	+ 1.8724	— 7. 265 I
6— 4	+ 0.8151	- 2. 3512	— o. 6822	— 2. 7251
7— 4	+ 0.6780	 0. 5943	— o. 6353	— o. 6689
8— 4	+ 0.3723	— 0. 1089	— o. 2900	— o. 1119
9— 4	— 1.7237	— 0. 4 <u>5</u> 20	+ 0.8129	— 0. 2179
10-4	+ 0. 16489	+ 0.16391	+ 0.00591	- 0.00701
11-4	+ 0.0084	+ 0.0077	+ 0.0045	— o. oo5o
1 5	— 0. 001	— o. oo3	0. 000	+ 0.002

Arg.	$\frac{d\delta}{d}$		$\frac{1}{n'}\frac{d}{d}$	
	cos.	sin.	sin.	cos.
i' i	"	"	"	"
2- 5	0, 001	+0.001	0,000	-0.001
3- 5	+o. o36	- +0. 00 6	-o. o33	0. 010
4- 5	—o. o86	o. 646	+ 0. 245	-0.641
5— 5	 4. 288	+2.410	+4.848	+2.613
6— 5	-3. 1103	0. 0213	+3.6879	+0. 1539
7-5	—1. o347	—o. 616 7	+1.3164	<u></u> 0. 6281
8 5	0. 1878	о. 3388	+ 0. 2670	-0. 3732
9 5	+0.0014	—o. 1213	+o. o135	—о. 1326
10- 5	+0. 0224	—о. 0390	—o. o175	0. 0384
11-5	+0.0305	-0. O20I	0. 0196	-0.0142
12— 5	0. 0113	+ 0. 0026	+0.0025	+0.0004
3 6	-0.002	+0.001	— 0. 003	-0,000
4— 6	+0.014	-o. o31	-0.002	-0.032
5— 6	-0. 405	-0.041	- +0. 431	+ 0. 030
6— 6	+ 0. 627	+2. 133	—o. 652	+2.413
7— 6	0. 3429	+1.5477	+0. 3477	+1.8657
8— 6	0.4394	+0.4827	+0.4909	+o. 6449
9— 6	0. 2016	+o. o63o	+0. 2413	+o. 1087
10— 6	— 0. 0594	—о. 0135	+0.0746	-o. oo62
11 6	—0. 0126	—0. 0117	+o. o165	o. o114
12 6	-0. 0020	-0. 0050	+0.0025	 0. 0049
4- 7	+0.001	0, 002	0.000	-0.002
5— 7	-0.021	-o. o16	+0.025	0.010
6 7	—о. 078	+o. 232	+0.051	+o. 256
7— 7	+1.031	—о. 056	—1. 161	o. o31
8— 7	+o. 756	+0. 342	0.915	+0. 377
9— 7	+o. 218	+0. 301	—0. 302	+o. 351
10— 7	+0.012	+0. 125	o. o36	+0. 156
11-7	-0.015	+0.033	+0.013	+0.046
12 7	0. 007	+0.006	+0.009	+0.009
5 8	-0.001	0.001	0, 000	0.001
6 8	0. 015	+0.012	+0.012	+0.015
7 8	+0. 122	+0.074	0. 138	+ 0.066
8 8	+0. 090	— о. 478	0. 120	o. 532
9- 8	+0. 263	—о. 353	—о. 300	-0.429
10 8	+0. 1 96	0. 087	-0. 234	0. 128
11— 8	+ 0. 076	+0.009	0. 100	-0.002
12— 8	+0.019	+0.013	o. 027	+0.015
6— 9	0.002	0.000	+0,001	+0.001
7-9	+0.00 6	+0.011	0.009	+0.010
8 9	+0.057	 0. 060	<u> </u>	—0. 069
9— 9	— 0. 209	— 0. 096	+0. 231	-0. 117
10- 9	0. 155	—0. 177	+ 0. 186	0. 206
11-9	0. 027	-0. 121	+0.042	— 0. 148
12 9	+0.014	— 0. 046	0.012	—o. o61

		$\frac{\delta z'}{4t}$	$rac{1}{n'} rac{d u'}{dt}$		
	cos.	sin.	sin.	cos.	
i' i 7—10 8—10 9—10 10—10 11—10	+0.001 +0.009 -0.026 -0.071 -0.111 -0.073	+0.002 -0.003 -0.041 +0.085 +0.059	0.000 -0.009 +0.029 +0.083 +0.130 +0.091	 0. 000 0. 004 0. 042 +-0. 092 +-0. 071 +-0. 005	
9—11 10—11 11—11 12—11 10—12 11—12	0. 000 0. 025 +0. 031 +0. 018 0. 003 +0. 001 +0. 026	-0.006 +0.009 +0.044 +0.066 -0.001 +0.015 -0.007	+0.001 +0.027 -0.031 -0.020 +0.004 -0.002 -0.030	-0.005 +0.010 +0.051 +0.078 0.000 +0.016 -0.006	

The integration of the preceding expressions gives those for δz and ν , except that we do not thus obtain the constant term of the latter quantity. This, however, is known to be

$$-\frac{1}{6}\left[k_0+\frac{3}{2}\frac{e}{P_1}k_1\right]$$

where P₁ has the signification attributed to it at page 63.**

This formula gives us in the case of Jupiter as the constant term of $\nu - 2''$.3598, and in the case of Saturn as the constant term of $\nu' + 86''$.5056.

With regard to the terms of the perturbations factored by t it may be noted that if we denote the terms in $n\delta z$, having the argument g, by

$$k_1nt \sin g + k_2nt \cos g$$

and those in $\frac{u}{\cos i}$ by

$$k_3nt\sin g + k_4nt\cos g$$

the complete expressions for these parts of the perturbations will be

$$n\delta z = k_{1}nt \left[\sin g + \frac{1}{2} \frac{P_{2}}{P_{1}} \sin 2g + \frac{1}{3} \frac{P_{3}}{P_{1}} \sin 3g + \dots \right]$$

$$+ k_{2}nt \left[\cos g + \frac{1}{2} \frac{Q_{2}}{Q_{1}} \cos 2g + \frac{1}{3} \frac{Q_{3}}{Q_{1}} \cos 3g + \dots \right]$$

$$\nu = -\frac{1}{2}k_{1}nt \left[\frac{1}{2} \frac{e}{P_{1}} + \cos g + \frac{P_{2}}{P_{1}} \cos 2g + \frac{P_{3}}{P_{1}} \cos 3g + \dots \right]$$

$$+ \frac{1}{2}k_{2}nt \left[\sin g + \frac{Q_{2}}{Q_{1}} \sin 2g + \frac{Q_{3}}{Q_{1}} \sin 3g + \dots \right]$$

$$\frac{u}{\cos i} = k_{3}nt \left[\sin g + \frac{Q_{2}}{Q_{1}} \sin 2g + \frac{Q_{3}}{Q_{1}} \sin 3g + \dots \right]$$

$$+ k_{4}nt \left[-\frac{3}{2} \frac{e}{P_{1}} + \cos g + \frac{P_{2}}{P_{1}} \cos 2g + \frac{P_{3}}{P_{1}} \cos 3g + \dots \right]$$

The P and Q have been defined (page 63).

In the case of Jupiter these equations give

$$n\delta z = k_1 nt \sin (-g) + k_2 nt \cos (-g) + [8.0810774] k_1 nt \sin (-2g) + [8.0811617] k_2 nt \cos (-2g) + [6.4632057] k_1 nt \sin (-3g) + [6.4633322] k_2 nt \cos (-3g) + [4.9702810] k_1 nt \sin (-4g) + [4.9704329] k_2 nt \cos (-4g) + [3.5462420] k_1 nt \sin (-5g) + [3.5464107] k_2 nt \cos (-5g)$$

$$v = [8.0817514] k_1 nt + \frac{1}{2} k_1 nt \cos (-g) - \frac{1}{2} k_2 nt \sin (-g) + [6.6392970] k_1 nt \cos (-2g) - [8.0811617] k_2 nt \sin (-2g) + [6.6392970] k_1 nt \cos (-3g) - [6.6394235] k_2 nt \sin (-3g) + [5.2713110] k_1 nt \cos (-4g) - [5.2714629] k_2 nt \sin (-4g) + [3.9441820] k_1 nt \cos (-5g) - [3.9443507] k_2 nt \sin (-5g)$$

$$\frac{u}{\cos i} = -[8.8599027] k_4 nt + k_3 nt \sin (-g) + k_4 nt \cos (-g) + [8.3821917] k_3 nt \sin (-2g) + [8.3821074] k_4 nt \cos (-2g) + [6.9404535] k_3 nt \sin (-3g) + [6.9403270] k_4 nt \cos (-3g) + [5.5724929] k_3 nt \sin (-4g) + [5.5723410] k_4 nt \cos (-4g) + [4.2453807] k_3 nt \sin (-5g) + [4.2452120] k_4 nt \cos (-5g)$$

And in the case of Saturn

$$n'\delta z' = k'_1n't \sin g' + k'_2n't \cos g' + [8.1461706] k'_1n't \sin 2g' + [8.1462845] k'_2n't \cos 2g' + [6.5933997] k'_1n't \sin 3g' + [6.5935705] k'_2n't \cos 3g' + [5.1655779] k'_1n't \sin 4g' + [5.1657829] k'_2n't \cos 4g' + [3.8066453] k'_1n't \sin 5g' + [3.8068731] k'_2n't \cos 5g'$$

$$v' = -[8.1470809] k'_1n't - \frac{1}{2}k'_2n't \sin g' - \frac{1}{2}k'_2n't \cos 2g' + [8.1462845] k'_2n't \sin 2g' - [6.7694910] k'_1n't \cos 2g' + [8.1462845] k'_2n't \sin 2g' - [5.4666079] k'_1n't \cos 4g' + [5.4668129] k'_2n't \sin 3g' - [4.2045853] k'_1n't \cos 5g' + [4.2048131] k'_2n't \sin 5g'$$

$$\frac{w'}{\cos i} = -[8.9252322] k'_4n't - [8.4473145] k'_3n't \sin 2g' + [8.4472006] k'_4n't \cos 2g' + [7.0706918] k'_3n't \sin 3g' + [7.0705210] k'_4n't \cos 3g' + [5.7678429] k'_3n't \sin 4g' + [5.7676379] k'_4n't \cos 4g' + [4.5058431] k'_3n't \sin 5g' + [4.5056153] k'_4n't \cos 5g'$$

The expressions for the perturbations of Jupiter and Saturn, arising from their mutual action, and of the first order with respect to disturbing forces, are as follows:

$egin{arg} ext{Arg}=\ i'g'+ig \ \end{array}$	$n\delta$	z	ν		u cos	i i
19 7 19	sin.	cos.	cos.	sin.	sin.	cos.
i' i	"	"	// 2. 3598 0. 0122808nt	″	"	// +0.0369 —0.0090789 <i>nt</i>
o — 1	0. 0000	0.0000	+ 0.5900	+ 0. 4221	0.0000	0,0000
1	1.0173636nt	- 1. 1420391 <i>nt</i>	— 0.5086818nt	+ 0.5710195 <i>nt</i>	+0. 2844315nt	+0.1253514 <i>nt</i>
0 2	+ 0.0316	+ 0.0146	+ 0. 0348	o. oo61	-o. oo79	o. 0147
	— 0.0122618nt	- 0.0137671nt	0.0122618nt	+ 0.0137671nt	+0.0068576nt	+0.0030216 <i>nt</i>
o — 3	+ 0.0005	+ 0.0004	+ 0.0009	o. ooo3	0.0000	-0.0004
	— 0.0002956 <i>nt</i>	— 0.0003319nt	— 0.0004434 <i>nt</i>	+ 0.0004979nt	+0.0002480nt	+0.0001118nt
0 — 4	— 0.0000095nt	— 0.0000107 <i>nt</i>	— 0.0000190 <i>nt</i>	+ 0.0000213nt	+0.0000106 <i>nt</i>	+0.0000047nt
0 5	— 0.000004 <i>nt</i>	- 0, 0000004nt	— 0.0000009nt	+ 0.0000010nt	+0.0000005 <i>nt</i>	+0.0000002nt
1 + 3	0.0001	+ 0.0002	+ 0.0002	+ 0.0001		
1 + 2	0.0049	+ 0.0007	+ 0.0055	+ 0.0005	+0.0025	0. 0006
1 + 1	o. 2652	0.0750	+ o. 1856	— o. o426	+o. o983	+0. c297
1 0	— 8. 42 <u>5</u> 4	+ 4.3699	+ 1.7783	+ 0.4815	+o. 4468	o. 3o56
1 — 1	+ 15.3616	+78.9638	+ 4.9822	25, 6080	-o, 1161	—o. o5o9
I — 2	0. 2503	+ 1.3828	— 0.1193	— 1.0401	0. 2 590	o. o586
I — 3	— o. o106	+ 0.0344	— 0.0099	0.0404	0, 0040	-o. oo39
1 — 4	— 0.0004	+ 0.0009	0.0005	— o. oo16	o. 000 I	+0.0001
2 + 2	— o. ooo5	+ 0.0004	+ 0.0007	+ 0.0006		
2 + I	- 0.0231	+ 0.0124	+ 0.0203	+ 0.0121	+0,0049	—0. 0099
2 0	— 1. 26 64	+ 1.2749	+ 0.5833	+ 0.5047	—o. o186	—o. 3728
2 — I	+123.5450	+ 4.4541	+ 18.1877	+ 1.0218	+0.4637	+0. 4391
2 — 2	+179. 1521	—76. 81 7 9	+100.7061	+43. 1791	—о. 1080	+0. 1908
2 — 3	+ 2.4851	— I.4I84	+ 2.6577	+ 1.4018	-0.0014	0. 0615
2 — 4	+ 0.0595	— o. o391	+ 0.0961	+ 0.0563	+0.0007	- 0.0015
2 5	+ 0.0019	0.0013	+ 0.0041	+ 0.0025	+0.0002	-0.000I
3 + 1	+ 0.0005	0, 0018	— o. ooo6	- 0.0019	+0.0013	+0.0005
3 0	+ 0.0750	— 0. 1369	0.0364	- 0.0795	+0.0335	+0.0412
3 — 1	+ 12.4697	— 7. 9940	— 2. 2066	— I. 6053	+0.1895	-0.0292
3 2	— 50. I203	+65.9600	20. 8813	—28. 2718	-o. 5536	+0.8698
3-3	+ 8.7532	+13.7703	+ 6.0514	— 9. 8126	—0.0420	-0.0038
3 — 4	+ 0.3496	+ 0. 2513	+ 0.3509	— o. 3160	+0.0206	-0.0040
3 - 5	+ 0.0123	+ 0.0045	+ 0.0172	- 0.0103	+0.0008	0,0000
3 — 6	+ 0.0005	+ 0.0001	+ 0.0009	- 0,0004	l .	
4 0	+ 0.0008	0.0063	+ 0.0001	0.0045	+0.0031	+0.0007
4 — 1	+ 0.0815	— o. 3201	0.0472	— o. 1504	+0.0410	0. 0274
4 — 2	— 2. 3198	+16.4362	— o. 2484	— 3. 9932	—o. o319	+0. 1450
4 3	+ 13.7024	+ 6.5087	+ 8. 3244	— 4. I262	+0. 2293	+0.0900
4 — 4	— 2. 2470	+ 2,7601	— I. 7055	— 2. 2242	+0.0144	—o. 0092
4 — 5	- 0.0332	+ 0.1572	o. o <u>5</u> 06	o. 1667	+0.0037	+0.0075
4 — 6	+ 0.0012	+ 0.0065	— 0.000I	0. 0092	+0.0002	+0.0003
4 — 7	+ 0.0001	+ 0.0002	+ 0.0001	- o. ooo5		

Arg=	nó	Sz		ν		u s i
i'g'+ig	sin.	cos.	cos.	sin.	sin.	cos.
i' i	"	"	"	11	11	"
5 0	+ 0.0033	+ 0.0045	— 0.0033	+o. 0046	0.0016	+0, 0039
5 1	+ 0. 2759	+ o. 388o	— o. 1394	+0. 1924	0.0701	+o. 162 7
5 — 2	+422. 3883	+992.7791	— 5.6159	+8.7834	+0. 2807	o. o133
5 - 3	—154. 7622	+ 11.5283	76. 6873	<u>—5. 8016</u>	<u>—3. 6469</u>	+0. 3547
5 — 4	— 2. 453 1	+ 2.7333	— 2. <u>33</u> 05	<u>—2. 0196</u>	0.0940	+0.0523
5 — 5	— o. 994 5	— o. 49 7 7	o. 8815	+o. 3980	+0,0022	+0.0047
5 — 6	— o. o7 18	+ 0.0033	o. o789	+0.0026	—o, oo25	+0. 0022
5 — 7	— o. oo33	+ 0.0017	0. 0047	0.0015	-0.0002	+0.0002
5 — 8	o, ooo1	+ 0.0001	— o. ooo2	0, 0001		·
6 — I	+ 0.0015	+ 0.0002	— o. ooo8	0.0000	0.0000	+0.0007
6 — 2	+ 0. 1034	+ 0.0464	— o. o368	+0.0099	+0.0073	+0.0013
6 — 3	— 1.75 28	+ 1.1480	— o. 5718	-0. 42 05	-0.0322	+0.0175
6 — 4	+ 0.4254	+ 1.4849	+ 0. 2423	— 0. 9807	+0.0141	+0.0441
6 — 5	— o. 8104 ⁻	+ 0.0070	— o. 6500	+0.0051	0. 0122	+0.0021
6 — 6	+ 0.0972	— o. 3579	+ 0.0769	+o. 3193	-0.0015	+0.0028
6 — 7	— o. oog4	- 0.0317	o. oo75	+o. o346	0.0011	0.0009
6 — 8	— o. oo15	— o. oo15	0.0015	+0.0022	0,0000	0,0000
6 — 9	_ 0.0001	— o. ooo1	— o. oooi	+0.0001		
7 — 2	+ 0.0062	— o. oo6o	— v. 0033	0. 0029	+0.0029	-0.0012
7 - 3	- o. 6842	+ 1.3256	— o. o618	—0. 1705	—o. oo5o	+0,0020
7 4	+ 1.0896	+ 1.0599	+ 0. 5940	-0. 5981	+0.0368	+0.0372
7 — 5	— o. 3348	+ 0. 2042	— o. 2545	—0. 1448	— о. 0099	+0.0074
7 — 6	— o. o655	— o. 296o	0. 0525	+o. 2531	0, 0015	— 0. 0039
7 — 7	+ 0.1389	+ 0.0047	+ 0. 1269	+0.0001	-0.0016	-0, 0004
7 8	+ 0.0137	— o. oo8o	+ 0.0153	+0,0076	+0.0002	 0. 0005
7 — 9	+ 0.0006	- 0,0010	+ 0.0010	+0.0011		
7 —10	0.0000	— o. ooo1	0.0000	+0.0001		
8 2	+ 0.0002	+ 0.0006	0.0001	+o. 0002		
8 — 3	+ 0.0117	+ 0.0930	0.0041	+ 0. 0149	+0.0010	+0.0010
8 — 4	— o. 4o8o	— o. 1116	— o. 1735	+0.0424	-0.0110	-0.0039
8 — 5	— o. o981	+ 0.1506	— o. o ₇₃₇	<u> </u>	0. 0043	+0.0063
8 — 6	- 0.0972	— O. I 102	— o. o748	+0.0932	0. 0031	— 0. 0031
8 7	+ 0.1141	— o. o515	+ 0. 1020	+0.0441	+0.0012	0. 0009
8 8	+ 0.0112	+ 0.0537	+ 0.0125	o. o498	0.0000	+0.0007
8 — 9	+ 0.0053	+ 0.0057	+ 0.0054	—o. oo64	+0.0003	+0.0001
8 —10	+ 0.0007	+ 0.0002	+ 0.0008	-0, 0004		
8 —11	+ 0.0001	0.0000	+ 0.0001	0,0000		
9 — 3	+ 0.0016	+ 0.0008	— o. ooo8	+0.0003		
9 — 4	— o. o859	+ 0.0205	- 0.0200	—o. 0067	-0.0004	0.0003
9 — 5	 0.0048	+ 0. 1030	0.0052	o. o618	+0.0002	+0.0048
9 — 6	o. o553	— o. o185	- 0.0414	+o. o166	0. 0025	-0.0008
9 — 7	+ 0.0381	— o. o5o7	+ 0.0347	+0.0418	+0.0009	0.0015
9 — 8	+ 0.0327	+ 0.0438	+ 0.0293	0. 0404	+0.0004	+0.0003
9 — 9	— o. o201	+ 0.0098	— o. o187	-0. 0102	+0.0002	-0.0001

$\begin{array}{c} \text{Arg} = \\ i'g' + ig \end{array}$	ni	$n\delta z$		$n\delta z$ $ u$,	$\frac{u}{\cos i}$	
vg - vg	sin.	cos.	cos.	sin.	sin.	cos.		
i' i 9—10 9—11 10— 4 10— 5 10— 6 10— 7 10— 8 10—10 10—11	-0.0021 0.0000 -1.0301 -0.1884 -0.0243 +0.0031 +0.0268 -0.0161 -0.0061 -0.0018	+0.0032 +0.0004 +1.0224 -0.3832 -0.0007 -0.0249 +0.0125 +0.0188 -0.0071	-0.0024 -0.0001 +0.0164 -0.0931 -0.0181 +0.0039 +0.0232 -0.0152 -0.0063 -0.0019	-0.0034 -0.0005 +0.0227 +0.1880 +0.0029 +0.0202 -0.0121 -0.0174 +0.0065 +0.0008	+0.0003 -0.0061 -0.0012 +0.0002 +0.0007	+0.0012 -0.0151 -0.0003 -0.0011 +0.0003		
10—12 11— 5 11— 6 11— 7 11— 8 11— 9 11—10 11—11 11—12 12— 5 12— 6 12— 7 12— 8 12— 9 12—10 12—11 12—12	-0.0002 -0.0088 -0.0077 -0.0033 +0.0119 -0.0032 -0.0102 +0.0022 +0.0001 -0.0068 -0.0038 -0.0024 +0.0035 +0.0017 -0.0072 +0.0013 +0.0018	+0.0001 -0.0063 +0.0062 -0.0081 -0.0009 +0.0140 -0.0055 -0.0033 -0.0009 -0.0017 +0.0083 -0.0017 -0.0024 +0.0059 -0.0001 -0.0053 +0.0004	-0.0002 -0.0032 -0.0051 -0.0021 +0.0103 -0.0035 -0.0096 +0.0020 +0.0002 -0.0016 +0.0030 +0.0012 -0.0068 +0.0013 +0.0018	-0.0000 +0.0018 -0.0038 +0.0064 0.0000 -0.0126 +0.0052 +0.0034 +0.0010 -0.0045 +0.0014 +0.0017 -0.0054 +0.0003 +0.0052 -0.0003	-0.0004 -0.0002 +0.0005 -0.0001	+0,0003 +0.0005 -0.0001 +0.0004		

Arg=i'g+	ig	n'	δ <i>z'</i>		ν'		<u>u'</u> 8 ••'
		sin.	cos.	cos.	sin.	sin.	cos.
i' i		"	"	,,, + 86. 5056	"	"	" —0. 3240
l				+ 0.075066 <i>n't</i>			—0. 1306 77#/ t
I O	·	0,0000	0. 0000	+ 3.3206	+ 7.4569	0.0000	0.0000
1		— 5. 350080 <i>n</i> ′t	- 8.631067n't	+ 2.675040n't		+1.106428n't	+1.552265n't
2 0	·	— o. 3069	+ 0.5487	+ o. 1442	+ 0.8298	+0.0670	-0. 2034
		— 0.074908 <i>n</i> /t	— 0. 120878 <i>n't</i>	+ 0.074908n/t	- 0.120878n't	+0.030991 <i>n't</i>	+0.043468n't
3 0	١	- 0.0090	+ 0.0317	— 0. 0095	+ 0.0557	-0,0010	—0. 0176
	ı	- 0.002098n't	— 0.003386n't	+ 0.003147 <i>n</i> / <i>t</i>	- 0.005078n't	+0.001302n't	+0.001826 <i>n't</i>
4 0		0.0000	+ 0.0019	— 0.002I	+ 0.0033	— 0. 0008	o . 0009
1		- 0.000078n't	- 0.000126n't	+ 0.000157 <i>n't</i>	- 0.000253n't	+0.000065 <i>n't</i>	+0.000091 <i>n't</i>
5 0		0.0000	+ 0.0001	- 0.0002	+ 0,0001	1	
!		— 0.000003 <i>n</i> / <i>t</i>	— 0 . 000006 <i>n</i> / <i>t</i>	+ 0.000009 <i>n</i> / <i>t</i>		+0.000004 <i>n</i> ′ <i>t</i>	+0.000005 <i>n't</i>
— 3— I	- 1	- 0.0003	+ 0.0001	— o. ooo8	0,0000	+0.0005	+0.0001
- 2- I		- 0.0051	+ 0.0025	0.0107	— o. oo36	+ o . 0046	-0.0005
- I- I	- 1	— o. o8o4	+ 0.0376	— 0. I329.	- 0.0920	+0.0433	o. o286
0— 1	- 1	+ 1.0159	+ 11.6710	1.0828	— 3. 311o	—0. 7669	+1.6253
1— 1	- 1	— 6.5162	- 0. 9205	+ 32.4638	—177. o3o6	o. 6452	o. 4370
2 I	- 1	— 424 . 0893	— 14. 2645	—116. 3299	— 6. 7355	—2. o5o5	—2. 1264
3- 1	- 1	— 28. 1575	+ 20.1428	+ 9.6186	+ 6.7750	0. 7127	—0. 0198
4- 1		— o. 2948	-+ o. o263	+ 0. 2846	+ 0.1311	+0.0507	—o. o38o
5— 1		- 0.0105	+ 0.0016	+ 0.0126	+ 0.0111	+0.0029	—o. oo38
6— 1		— o. ooo5	+ 0.0001	+ 0.0004	+ 0.0008	+0.0005	0. 0007
- 2- 2		- 0.0001	— o. ooo1	0. 0002	+ 0.0002	-0. 000 I	+0,0002
— I— 2		- o. oo17	— 0.0018	— o. oo36	+ 0.0024	+0.0006	+0.0013
0— 2		+ 0.0197	+ 0.2104	— o. o555	+ 0.0038	0, 0091	+0.0615
I- 2	- 1	- o. 8452	— 2. 5 470	— o. 2961	— 2.6516	+0. 2524	+0.0542
2— 2	١	— 29. 5211	+ 12.6271	— 28. 1687	— 12. 2964	+0.0847	—0. 0696
3— 2	١	— 18. 7373	+ 18.5430	15. 8648	— 12.9271	— 0. 2295	+o. 1436
4- 2		+ 80.9207	651. 2349	+ 38.6088	+316.7274	+1.0617	—8. 9202
5 2		1029. 1981	-2417. 7411	+ 24. 0769	- 45.6323	0. 1630	+o. 6190
6— 2		+ 1.1398	— o. 4218	— o. 5506	— o. 2186	+o. 2368	+0.0758
7— 2		+ 0.0163	— o. oo83	0.0145	- o. oo7o	+0.0077	+0.0019
8— 2	- [+ 0.0004	— 0.0003	— о. оооб	— 0. 0002		
_ I- 3	١	0.0000	— o. ooo1	0.0000	+ 0.0002	0,0000	0.0001
o— 3		+ 0.0016	+ 0.0074	— 0,0002	+ 0.0007	0.0010	+0.0021
1-3		- o. o183	- 0.0972	+ 0.0137	- 0.0817	+0.0008	+0.0021
2— 3	1	— o. 1611	+ 0.1544	- o. 2654	- 0.0503	-0, 0004	+0.0859
3-3	- 1	— 3. 8 ₅₂₃	- 5.3430	- 4. 1475	+ 5.6513	+0.0259	+0.0311
4-3		— 4. 2617	— 1. 8168	4. 4031	+ 2.1588	-0.0652	—0. 0240
5— 3		— 2. 9777	+ o. 3718	— 2. 7928	— o. 1713	-0. 0822	+0.0108
6 3		— 3.4500	+ 2.3914	— 2. <u>35</u> 14	- 1. 5225	-0. 0900	+0.0589
7-3		+ 2.3548	— 4. 6458	+ 0.5294	+ 1.1726	+0.0238	—0. 0340
8-3		— 0. 0402	- 0.2147	+ 0.0198	- 0.0711	-0.0238 -0.0023	_0. 0340 _0. 0030
9— 3		+ 0.0005	- o. oo15	+ 0.0003	- 0.0014	5.5523	-0.0030
بُ سُ	1		Ž				

	m Arg= $i'g+ig$	n' δ	z'	ν	,,	_1/2 COS	,' 3 i '
1		sin.	cos.	cos.	sın.	sin.	cos.
2-4 0,0000						il.	11
2-4	I— 4	0. 0007	0. 0040	+0.0009	0.0038	o. ooo i	-0,0001
4-4 +1.2875 -1.4328 +1.4019 +1.6007 -0.0120 +0.65 5-4 +0.2600 -1.2933 +0.3795 +1.4727 +0.021 -0.06 6-4 -0.2072 -0.5978 -0.1734 +0.6928 -0.061 -0.05 7-4 -0.2311 -0.2026 -0.2166 +0.2280 -0.0088 -0.0068 9-4 +1.8469 -0.4843 +0.8710 +0.2335 +0.0403 -0.06 9-4 +1.8469 -0.4843 +0.8710 +0.2335 +0.0403 -0.06 10-4 +2.4721 -2.4574 -0.0886 -0.1031 +0.0027 -0.027 1-5 +0.0001 -0.0003 0.0000 -0.0047 +0.0021 -0.0027 1-5 +0.0001 -0.0003 0.0000 -0.0001 +0.0001 -0.0002 2-5 +0.0001 +0.0001 0.0000 -0.0001 +0.0001 +0.0001 -0.0003 +0.0001 -0.00001 +0.0537 +0.0537 -0.053 +0.0011	2— 4	0, 0000	+0.0041	-0.0016	-0,0021	0.0012	+0.0016
4-4 +1.2875 -1.4328 +1.4019 +1.6007 -0.0120 +0.650 5-4 +0.2600 -1.2933 +0.3795 +1.4727 +0.021 -0.06 6-4 -0.2072 -0.5978 -0.1734 +0.6928 -0.061 -0.05 7-4 -0.2311 -0.2026 -0.2166 +0.2280 -0.0088 -0.0088 8-4 -0.1926 -0.0563 -0.1500 +0.0579 -0.069 -0.069 9-4 +1.8469 -0.4843 +0.8710 +0.2335 +0.0403 -0.06 10-4 +2.4721 -2.4574 -0.0886 -0.1051 +0.0403 -0.027 1-5 +0.0001 -0.0003 0.0000 -0.0047 +0.0021 -0.0047 1-5 +0.0001 -0.0003 0.0000 -0.0001 -0.0001 -0.0002 2-5 +0.0001 +0.0001 0.0000 -0.0001 +0.0001 -0.0001 -0.0001 -0.0001 -0.0001 -0.0001 -0.0001 -0.0001 -0.000	3— 4	—o. 1290	-o. o537	—о, 1083	+0.1003	o. o315	+0.0067
6-4	4 4	+1.2875	—I. 4328	+1.4019	l I	0, 0120	+0.0134
7-4	5— 4	+0, 2600	-1. 2933	+o. 3795	+1.4727	+0.0021	-0.0164
8- 4 -0.1926 -0.0563 -0.1500 +0.0579 -0.0669 -0.0493 9- 4 +1.8469 -0.4843 +0.8710 +0.2335 +0.0403 -0.06 10- 4 +2.4721 -2.4574 -0.0886 -0.1051 -0.0027 0.0 11- 4 +0.0084 -0.0092 -0.0042 -0.0047 -0.0027 0.0 1- 5 +0.0001 -0.0003 0.0000 -0.0002 -0.0001 0.0000 -0.0001 -0.0011 +0.011 +0.011 +0.011 +0.0041 +0.0045 +0.0045 +0.0045 +0.0045	6 4	0. 2072	o. 5978	0. 1734	+o. 6928	—0. 0061	—0.017 6
9-4	7— 4	-0. 2311	0. 2026	—0. 2166	+0. 2280	—o. 0088	—o. oo83
104	8 4	0. 1926	o. o563	0. 1500	+0.0579	o, oo69	0.0025
10- 4	9 4	+1.8469	-o. 4843	+o. 8710		+0.0403	0. 0070
1— 5 +0.0001 -0.0003 0.0000 -0.0002 2— 5 +0.0001 +0.0001 0.0000 -0.0001 3— 5 +0.0012 -0.0767 +0.0291 +0.0762 -0.055 4— 5 +0.0102 -0.0767 +0.0291 +0.0762 -0.055 5— 5 +0.5781 +0.3249 +0.6537 -0.3523 -0.071 -0.0 6— 5 +0.4847 -0.0033 +0.5747 -0.0240 +0.0045 -0.0 6— 5 +0.4847 -0.0767 +0.0605 +0.0245 -0.051 -0.0 8— 5 +0.0425 -0.0767 +0.0605 +0.0845 +0.0051 -0.0 9— 5 -0.0024 -0.0355 +0.040 +0.0388 +0.0001 -0.0 10— 5 -0.0093 -0.0161 -0.0072 +0.0159 -0.003 -0.0 11— 5 -0.0215 -0.0142 -0.0138 +0.0100 -0.000 -0.000 3— 6 +0.0271 +0.0062 +0.000 -0	10— 4	+2.4721	2. 4574	—о. 0886	1		0,0000
2-5	11 4	+0.0084	—0. 0092	0. 0042	0. 0047		
3-5	1 5	+0.0001	-0.0003	0,0000	-0.0002		
4—5 +0.0102 -0.0767 +0.0291 +0.0762 -0.055 -0.071 5—5 +0.5781 +0.3249 +0.6537 -0.3523 -0.0071 -0.0 6—5 +0.4847 -0.0033 +0.5747 -0.0240 +0.0045 -0.0 7—5 +0.1910 -0.1139 +0.2430 +0.1159 +0.0051 -0.0 8—5 +0.0425 -0.0767 +0.0605 +0.0845 +0.0019 -0.0 9—5 -0.0004 -0.0355 +0.0040 +0.0388 +0.0001 -0.0 10—5 -0.0093 -0.0161 -0.0072 +0.0159 -0.0003 -0.003 11—5 -0.0215 +0.0062 +0.0062 +0.0100 -0.0007 -0.0007 12—5 +0.0271 +0.0062 +0.0003 +0.0000 -0.0000 3—6 +0.00271 +0.0001 -0.0003 +0.0029 -0.0000 4—6 -0.0013 +0.0001 +0.0435 -0.0029 -0.0004 5—6 +	2 5	+0.0001	+0.0001	0,0000	-0.0001	İ	
5—5 +0.5781 +0.3249 +0.6337 -0.3523 -0.0071 -0.05 6—5 +0.4847 -0.0033 +0.5747 -0.0240 +0.0045 -0.0 7—5 +0.1910 -0.1139 +0.2430 +0.1159 +0.0051 -0.0 8—5 +0.0425 -0.0767 +0.0605 +0.0845 +0.0019 -0.0 9—5 -0.0004 -0.0355 +0.0040 +0.0388 +0.0001 -0.0 10—5 -0.093 -0.0161 -0.0072 +0.0159 -0.0003 -0.00 11—5 -0.0215 -0.0142 -0.0138 +0.0100 -0.0007 -0.00 12—5 +0.0271 +0.0062 +0.060 -0.0010 -0.000 -0.000 3—6 +0.0021 +0.0001 -0.0003 0.000 -0.000 -0.000 4—6 -0.0013 -0.0028 -0.0002 +0.0029 -0.004 -0.004 5—6 +0.0409 -0.044 +0.0435 -0.030 +0.004 -0.00	3 5	-o. oo38	+0.0006	0. 0035	+0,0011	0. 0011	+0,0001
6 - 5	4 5	+0.0102	—0. 0767	+0.0291	+0.0762	0. 0055	0,0118
7-5 +0.1910 -0.1139 +0.2430 +0.1159 +0.0051 -0.05 8-5 +0.0425 -0.0767 +0.0605 +0.0845 +0.0019 -0.0 9-5 -0.0004 -0.0355 +0.0040 +0.0388 +0.0001 -0.0 10-5 -0.0093 -0.0161 -0.0072 +0.0159 -0.0003 -0.00 11-5 -0.0215 -0.0142 -0.0138 +0.0100 -0.0007 -0.0007 12-5 +0.0271 +0.0062 +0.0060 -0.0010 -0.0007 -0.0007 3-6 +0.0021 +0.0001 -0.0003 0.0000 -0.0000 -0.0001 3-6 +0.0029 -0.0013 -0.0002 +0.0029 -0.0004 -0.0000 4-6 -0.0013 -0.0028 -0.0029 +0.0029 -0.0043 -0.0001 5-6 +0.0499 -0.0041 +0.0435 -0.02711 +0.0015 -0.0015 -0.0015 7-6 +0.0434 +0.1959 +0.0440 -0.2362 </td <td>5 5</td> <td>+o. 5781</td> <td>+0. 3249</td> <td>+0.6537</td> <td>—0. 3523</td> <td>0. 0071</td> <td>o. oo46</td>	5 5	+o. 5781	+0. 3249	+0.6537	— 0. 3 52 3	0. 0071	o. oo46
8-5	6-5	+ 0. 484 7	0, 0033	+0.5747		+0.0045	-0.0005
9-5	7— 5	+o. 1910	—о. 1139	+0. 2430	+0.1159	+0.0051	-0.0032
10-5 -0.0093 -0.0161 -0.0072 +0.0159 -0.0003 -0.00 11-5 -0.0215 +0.0062 +0.0060 -0.0010 -0.0007 -0.00 3-6 +0.0021 +0.0001 -0.0003 0.0000 -0.0004 4-6 -0.0013 -0.0028 -0.0002 +0.0029 -0.0004 5-6 +0.0409 -0.0041 +0.0435 -0.0030 +0.0043 6-6 -0.0704 +0.2397 -0.0732 -0.2711 +0.0015 -0.0 7-6 +0.0434 +0.1959 +0.0440 -0.2362 +0.0006 +0.0 8-6 +0.0637 +0.0699 +0.0711 -0.0935 +0.0017 +0.0 9-6 +0.0342 +0.0107 +0.0409 -0.0184 +0.0017 +0.0 10-6 +0.0121 -0.0028 +0.0152 +0.0013 +0.0006 -0.0 11-6 +0.0032 -0.003 +0.0042 +0.0017 +0.0002 -0.0 4-7 -0.0001	8 5	+0.0425	—o. 0767	<u>+</u> 0. 0605	+0. 0845	+0.0019	-0.0031
11-5 -0.0215 -0.0142 -0.0138 +0.0100 -0.0007 -0.00 12-5 +0.0271 +0.0062 +0.0060 -0.0010 -0.0007 -0.00 3-6 +0.0002 +0.0001 -0.0003 0.0000 -0.0004 -0.00 4-6 -0.0013 -0.0028 -0.0002 +0.0029 -0.0004 -0.00 5-6 +0.0409 -0.0041 +0.0435 -0.0030 +0.0043 -0.00 6-6 -0.0704 +0.2397 -0.0732 -0.2711 +0.0015 -0.0 7-6 +0.0434 +0.1959 +0.0440 -0.2362 +0.0006 +0.0 8-6 +0.0637 +0.0699 +0.0711 -0.0935 +0.0017 +0.00 9-6 +0.0342 +0.0107 +0.0409 -0.0184 +0.0014 +0.0 10-6 +0.0121 -0.0028 +0.0152 +0.0013 +0.0006 +0.0 11-6 +0.0032 -0.0017 +0.0009 +0.0017 +0.0009 <t< td=""><td>9 5</td><td>-0, 0004</td><td>o. o355</td><td>+0.0040</td><td>+o. o388</td><td>+o. ooo1</td><td>- 0.0017</td></t<>	9 5	-0, 0004	o. o355	+0.0040	+o. o388	+o. ooo1	- 0.0017
12- 5	10— 5	-0,0093	<u>—0. 0161</u>	-0. 0072	+0.0159	-0.0003	0.0009
3-6	11 5	-0. 0215	0. 0142	0. 0138	+0.0100	-0.0007	0, 0007
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	12 5	+0.0271	+0.0062	+0,0060	0,0010		
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	3- 6	+ 0.0002	+0,0001	0. 0003	0.0000		
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	4 6	-0.0013	-0.0028	0, 0002	+0.0029	0, 0004	o. ooo6
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	5— 6	+0.0409	-0.0041	+0.0435	—0. 0030	+0.0043	-o. oo33
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	6— 6	0. 0704	+0. 2397	o. 0732	0. 2711	+0.0015	-o. oo38
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	7 6	+0.0434	+0. 1959	+o. o44o	—0. 2362	+0,0006	+0.0012
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	8— 6	+0.0637	+0.0699	+0.0711	o. o935	+0.0017	+0.0016
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	9— 6	+0.0342	+0.0107	+0. 0409	-o. o184	+0.0014	+0.0004
$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$		+0.0121	—o. 0028	+0.0152	+0.0013	1	0.0001
$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$	11- 6	1	-0.0030	+0.0042		+0.0002	-0.0002
$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$	12 6	+o. ooo7	-0.0017	+0.0009	+0.0017		
6— 7	i i				1		
7-7 -0.0993 -0.0054 -0.1118 +0.0030 +0.0019 +0.0	5 7	5	_			1	0. 0003
	6— 7	+0.0069		1	-	+0.0019	+0.0015
0 - 1 0006 10006 0000 0000 0000	7— 7		1	—о. 1118	+0,0030	+0.0019	+0.0003
	8— 7	—o. o8o6	+o. o368	—o. o975	-0. 0402	0,0001	+0.0003
	9— 7	—o. o26o	+0.0359	—o, o36o	-0.0419	0.0005	+0.0008
	10 7	0.0016	+0.0169	o. oo49		0, 0002	+0.0006
	11 7	+0.0023	+0.0052	+0.0020	0.0072	1	+0.0005
12-7 +0.0013 +0.0011 +0.0017 -0.0017 +0.0002 +0.00	12-7	+0.0013	+0.0011	+0.0017	-0.0017	+0.0002	+0.0001

Arg = i'g + ig	n'e	52'	1	v'	60	u' 8 i'
	sin.	cos.	cos.	sin.	sin.	cos.
i' i 6— 8 7— 8	// +0.0011 —0.0095	+0.0009 +0.0057	// +0.0009 0.0107		// +0.0002 —0.0003	+0.0001
8— 8 9— 8 10— 8 11— 8		0. 0403 0. 0325 0. 0088 +-0. 0010 +-0. 0017	-0.0101 -0.0276 -0.0237 -0.0113	+0. 0448 +0. 0395 +0. 0130 +0. 0002 -0. 0019	+o. 0001	+0.0009
7— 9 8— 9 9— 9 10— 9	-0. 0004 -0. 0040 +0. 0157 +0. 0125 +0. 0024	+0.0007 -0.0042 -0.0072 -0.0143 -0.0107	-0.0034 -0.0006 -0.0039 +0.0173 +0.0151 +0.0037	-0.0007 +0.0048 +0.0088 +0.0167 +0.0130	—0. 0004 —0. 0007	-0.0001 +0.0001
8—I0 9—I0 I0—I0 II—I0 I2—I0	-0. 0014 -0. 0005 +0. 0016 +0. 0048 +0. 0080 +0. 0057	-0. 0044 -0. 0002 -0. 0026 +0. 0057 +0. 0043 0. 0000	-0.0012 -0.0005 +0.0018 +0.0056 +0.0094 +0.0071	+0.0059 +0.0002 +0.0027 -0.0062 -0.0051 -0.0004		
9—II I0—II II—II I2—II I0—I2 II—I2 I1—I2	0,0000 +0,0014 -0,0019 -0,0012 +0,0002 -0,0001	-0.0003 +0.0005 +0.0027 +0.0043 -0.0001 +0.0008 -0.0004	+0.0001 +0.0016 -0.0019 -0.0013 +0.0002 -0.0001	+0.0003 0.0006 0.0031 0.0051 0.0000 0.0009 +0.0003		

CHAPTER III.

PERTURBATIONS OF SATURN BY URANUS OF THE FIRST ORDER WITH RESPECT TO THE DISTURBING FORCE.

The method to be followed in this chapter is almost precisely identical with that of the preceding chapters. This will relieve us from the necessity of restating formulæ. The single point of difference is that here it will suffice to divide the circumference, with reference to the mean anomaly of Uranus, into twelve parts, instead of the sixteen which were employed for Saturn in Chapter I. As here the elements of Saturn take the place of those of Jupiter, and the elements of Uranus the place of those of Saturn, for convenience we will denote the former without accents and the latter with a single accent, reserving to ourselves the liberty of denoting, at the end, the mean anomaly of Uranus as g''.

The elements of Uranus adopted are as follows:*

Epoch, 1850, Jan. o.o, Greenwich M. T.

$$L' = 28^{\circ} 25' 17.''05$$

$$\pi' = 168^{\circ} 15' 6.''7$$

$$\theta' = 73^{\circ} 14' 8.''0$$

$$i' = 0^{\circ} 46' 20.''54$$

$$e' = 0.0469236$$

$$\pi' = 15425.''752$$

$$m' = \frac{1}{21000}$$

$$\log a' = 1.2831044$$

These elements include the effect of the 4000 year inequality produced by Neptune. It seems better to do this than to take mean elements, for the reason that, in the latter way, it would be necessary to consider terms proportional to the product of the masses of Uranus and Neptune and involving the anomalies of all three planets. Log a' includes the constant term of the perturbations of the logarithm of the radius vector, which is ± 0.0001972 . For a like reason, adding to $\log a$ of Saturn ± 0.0001854 , we have $\log a = 0.9796819$, which gives $\log \alpha = 9.6965775$.

The coefficients of the terms of the developments of the reciprocal of the distance between Saturn and Uranus $\frac{a'}{\triangle}$ and its odd powers, as periodic functions of the two mean anomalies, are then functions of the following six elements:

	0	/	"
$\log \alpha = 9.6965775$	J = 1	57	24.44
e = 0.05605688	$\Pi = 143$	20	42.93
<i>e'</i> = 0.0469236	$\Pi'=221$	29	41.56

^{*}An Investigation of the Orbit of Uranus, with General Tables of its Motion. By Prof. S. Newcomb, p. 181.

 Π and Π' are measured from the ascending node of the orbit of Uranus on that of Saturn. In developing these quantities it is preferable to proceed as if Uranus were the disturbed planet, as in this way γ_2 is smaller.

The values of the auxilliary constants, entirely similar to those of Chapter I, are

 $y_0 = 1.2457067 - [8.9724213] \cos \varepsilon' + [7.3427826] \cos^2 \varepsilon' + [8.7486289] f \cos \mathbf{F}$

We compute the values of ε' corresponding to the five following values of g':

The values for the seven remaining points of division of the circumference are either known or readily deducible from these. By substituting them in the equations which give the values of γ_0 , f, and F we get the following table:

g'	γο	log f		\mathbf{F}	g'
О			0	,	"
0	1. 1665387	9. 9787586	76	28	56.89
30	1. 1496185	9. 9746368	79	25	47.29
60	1. 1607263	9. 9776345	81	5 9	12.98
90	1. 1961616	9. 9862614	83	21	40. 55
120	1. 2452725	9. 9972220	83	15	36. 05
150	1.2945026	0.0073536	81	51	46. 09
180	1. 3313106	0.0145142	79	37	5.58
210	1. 3468479	0.0175338	77	4	25. 21
240	1. 3374098	0. 0159203	74	47	12.93
270	1. 3050141	0.0097458	73	16	49.81
300	1. 2572822	9. 9998678	72	58	59. 03
330	1.2063954	9. 9883863	74	6	34.67
5	7. 4985401	9. 9839171	469	7	3.50
S'	7. 4985401	9. 9839171	469	7	3⋅54

In the next step we obtain

g'	C	$\log q$		Q-9	<i>'</i>
			0	,	11
(0)	1. 1672734	9. 9791451	76	30	30.41
(1)	1. 1503098	9-9749759	79	23	37.58
(2)	1. 1610217	9. 9775301	81	55	52.67
(3)	1. 1961720	9. 9858422	83	20	53-54
(4)	1. 2453941	9. 9969293	83	18	3.05
(5)	1. 2949840	0. 0074544	81	55	0.82
(6)	1. 3320624	0. 0149069	79	38	16. 18
(7)	1. 3475581	0.0178806	77	2	33. 62
(8)	1. 3378019	0. 0159238	74	43	53.70
(9)	1. 3050786	0.0093943	73	14	59. 36
(10)	1. 2573216	9. 9994858	73	0	27.55
(11)	1. 2067726	9. 9883736	74	9	58.57
s	7. 5008751	9. 9839210	469	7	3. 56
S'	7. 5008751	9. 9839210	469	7	3.49

And in fine

g'	log N	log a	log b
(0)	0. 0179713	9. 7140577	6. 61024
(1)	0. 0219611	9. 7178680	6. 61441
(2)	0.0194011	9.7153021	6. 61185
(3)	0.0112542	9. 7073206	6. 60354
(4)	0.0003161	9. 6965315	6. 59245
(5)	9. 9897914	9. 6860072	6. 58193
(6)	9. 9822142	9. 6783051	6. 57448
(7)	9. 9791056	9. 6750617	6. 57150
(8)	9. 9810313	9. 6769564	6. 57346
(9)	9. 9876671	9. 6836984	6. 57999
(10)	9.9977306	9. 6939169	6. 58990
(11)	0, 0088850	9. 7051136	6. 60101
S	9. 9986646	8. 1750697	89. 55238
S'	9. 9986644	8. 1750695	89. 55239

The values of the $b_s^{(i)}$ are taken from Runkle's Tables.* We get

	$\log b_{\frac{1}{2}}^{(0)}$	$\logb_{\frac{1}{2}}^{(1)}$	log	$b_{rac{1}{2}}^{(2)}$	$\log b_{\frac{1}{2}}^{(i)}$	1)	$\log b_{\frac{1}{2}}^{(4)}$		$\logb_{\frac{1}{3}}^{(5)}$	$\log b_{\frac{1}{2}}^{(6)}$
(0)	0. 3342404	9. 7638610	9. 35	;868 <u>5</u> 6	8. 9964	.864	8. 654338		8. 323844	8. 00097
(1)	0. 3349185	9. 7686880		574426	9. 0091	166	8. 670818	- 1	8. 344162	8. 02511
(2)	0. 3344602	9. 7654350	1	515427	9.0006		8. 659717	.	8. 330477	8. 00885
(3)	0. 3330791	9.7553834	9.34	132656	8. 9742	217	8. 625270	,	8. 287993	7. 95834
(4)	0. 3313146	9. 7419491	1	87311	8. 9387	355	8. 578894		8. 230757	7. 89028
(5)	0. 32 96984	9. 7290018	9. 29	949759	8. 9043	078	8. 533850	.	8. 175127	7. 82409
(6)	0. 3285771	9. 7196184	9. 27	776942	8. 8792	213	8. 500998		8. 134529	7. 77576
(7)	0. 3281197	9. 7156892	9. 27	704416	8. 8686	836	8. 487192		8. 117462	7.75541
(8)	0. 3283857	9. 7179830	9. 27	746766	8. 8748	376	8. 495256		8. 127431	7. 76730
(9)	0. 3293570	9.7261811	9. 28	397866	8. 8967	784	8. 523993		8. 162 948	7. 80959
(10)	o. 3309036	9. 7387185	9. 31	128136	8. 9301	657	8. 567687		8. 216919	7. 87380
(11)	0. 3327087	9. 7526214	9. 33	382313	8. 9669	462	8. 615766		8. 276267	7. 94440
s	1.9878816	8. 4475650	5, 90	041438	3. 6200	547	1. 456890		89. 363957	87. 31696
S'	1. 9878814	8. 4475649	_	041436	3. 6200		1. 456889	- 1	89. 363959	87. 31694
	$\log b_{\frac{1}{2}}^{(7)}$	log	b ₁ (8)	log	b ₁ (9)	10	og $b_{\frac{1}{2}}^{(10)}$	lo	og $b_{\frac{3}{2}}^{(0)}$	$\log b_{\frac{3}{4}}^{(1)}$
(0)	7. 68353	7.3	7005	7.0	5989	6	. 7527	0.	6006482	0. 4467923
(1)	7. 71150	7.40	184	7.0	9551	6	. 7922	0.	6067952	0. 4559624
(2)	7. 69265	7.3	3043	7.0	7152	6	. 7656	0.	6026394	0.4497729
(3)	7. 63414	7-3	389	6. 9	9698	6	. 6830	о.	5901237	0. 4308901
(4)	7. 55523	7. 2:	416	6.8	9642	6	. 5717	0.	5741411	o. 406 20 60
(5)	7. 47848	7. 1	684	6. 7	9854	6	. 4633	0.	5595140	0. 3829910
(6)	7. 42242	1	306		2703	6	. 3841	٥.	5493706	0. 3665031
(7)	7. 39880	7.02	620	6.6	9693	6	. 3507	0.	5452339	0. 3596800
(8)	7. 41259	7.00	189	6. 7	1452	6	3703	0.	5476408	0. 3636573
(9)	7. 46166	7. 11	771	6.7	7709		. 4396	0.	5564251	0. 3780055
(10)	7. 53614		245		37208		. 5448		5704212	0. 4003617
(11)	7. 61798	7. 29	552	6. 9	7638	6	6602	0.	5867688	0. 4257641
S	85. 30256	83. 3	204	81.3	4146	79	. 3892	3.	4448613	1. 6332933
S'	85. 30256	83. 3	200	0.	4143		. 3892		4448607	1. 6332931

^{*}New Tables of the Coefficients of the Perturbative Function.

	$\log b_{\frac{3}{2}}^{(2)}$	$\log b_{\frac{3}{2}}^{(3)}$	$\log b_{\frac{3}{2}}^{(4)}$	lo	g $b_{\frac{3}{4}}^{(5)}$	log	$b_{\frac{3}{2}}^{(6)}$	$\log b_{\frac{3}{2}}^{(7)}$	$\log b_{\frac{3}{2}}^{(8)}$
(0)	0. 2415444	0.0140476	9. 7740086	9. 5	258905	9. 27	2126	9. 01418	8. 75302
(1)	o. 2542033	0. 0303401	9. 7939980	9.5	496131	9. 29	9601	9. 04543	8. 78804
(2)	0. 2456651	0. 0193555	9. 7805243	9. 5	336254	9. 28	1087	9. 02437	8. 76445
(3)	0. 2194566	9. 9855253	9. 7389410	9.4	842189	9. 22	3814	8. 95921	8. 69138
(4)	0. 1848239	9. 9405628	9. 6834802	9.4	181700	9. 14	7123	8. 87184	8. 59331
(5)	o. 1518569	9. 8974915	9. 6301498	9.3	544982	9.07	3061	8. 78736	8. 49839
(6)	0. 1282042	9. 8664278	9. 5915693	9.3	083396	9.01	9292	8.72597	8. 42934
(7)	0. 1183573	9.8534560	9. 5754269	9. 2	890071	8.99	6753	8. 70021	8. 40036
(8)	0. 1241015	9. 8610258	9. 5848450	9.3	002930	9.00	9899	8. 71522	8.41726
(9)	0. 1447261	9. 8881404	9. 6185459	9.3	406239	9.05	6907	8. 76892	8. 47765
(10)	0. 1765611	9. 9297923	9. 6701626	9.4	.022843	9. 12	8657	8.85079	8. 56967
(11)	0. 2122997	9. 9762577	9. 7275277	9.4	706408	9. 20	8060	8. 94128	8. 67127
s	1. 1009002	9. 6312118	8. 0845910	6. 4	886028	4. 85	8184	3. 20237	1. 52705
S'	1. 1008999	9. 6312110	8. 0845901	6.4	886020	4. 85	8196	3. 20241	1. 52709
	$\log b_{\frac{3}{2}}^{(9)}$	$\logb_{rac{3}{2}}^{(10)}$	$\log b_{\frac{5}{2}}^{(0)}$		log l	(1) 9 <u>5</u>	10	og $b_{\frac{5}{2}}^{(2)}$	$\logb_{rac{5}{2}}^{(3)}$
(0)	8. 48933	8. 2234	1, 0506	3	0.99	609	0	. 88273	0. 73389
(1)	8. 52813	8. 2660	1.0648	9	1.01	189	o	. 90113	o. 75536
(2)	8. 50199	8. 2373	1.0552	6	1.00	122	0	. 88872	0.74086
(3)	8. 42099	8. 1484	1.0261	6	o. 96	885	0	. 85085	0. 69654
(4)	8. 31221	8. 0285	0. 9888	0	o. 92	69 1	0	. 80132	0. 63817
(5)	8. 20683	7. 9126	0.9544	3	o. 88	790	0	· 75479	0. 58291
(6)	8. 13012	7.8283	0. 9304	9	o. 86	045	0	. 72176	0. 54344
(7)	8. 09792	7. 7929	0. 9206	9	o. 8 ₄	.914	0	. 70804	0. 52700
(8)	8. 11671	7.8137	0. 9264	.0	o. 85	573	0	. 71606	o. 53660
(9)	8. 18380	7. 8875	0. 9471	7	o. 87	959	1	. 74483	0.57102
(10)	8. 28596	7. 9997	0, 9800	8	0.91	705	0	. 78962	0. 62430
(11)	8. 39867	8. 1235	1.0183	3	o. 96	010	0	. 84055	o. 68444
s	89. 83632	88. 1309	5. 9316	6	5 - 55	745	4	. 80021	3.81726
S'	89. 83634	88. 1309	5. 9316	7	5.55	747	4	. 80019	3. 81727

25 AST-8

	$\logb_{rac{5}{2}}^{4)}$	$\logb_{rac{5}{4}}^{(5)}$	$\logb_{rac{5}{2}}^{(6)}$	$\logb_{\frac{5}{2}}^{(7)}$	$\logb_{\frac{5}{2}}^{(8)}$	$\logb_{\frac{5}{2}}^{(9)}$
(0)	0. 56148	0. 37240	0. 17082	9. 95968	9. 7411	9. 5165
(1)	o. 58627	0.40065	0. 20263	9. 99512	9. 7801	9. 5591
(2)	o. 56956	0. 38170	0. 18119	9. 97108	9.7538	9. 5304
(3)	0. 51826	0. 32305	0. 11522	9. 89771	9.6725	9. 4411
(4)	0. 45037	o. 24528	0. 02727	9. 79946	9. 5639	9. 3220
(5)	o. 38580	0. 17103	9. 94318	9. 70534	9-4595	9. 2072
(6)	0. 33948	0. 11762	9. 88259	9. 63746	9. 3843	9. 1245
(7)	0. 32005	0. 09520	9.85684	9. 60864	9. 3523	9. 0894
(8)	0. 33144	0. 10832	9.87204	9. 62560	9. 3711	9. 1100
(9)	0. 37190	0. 15500	9. 92513	9. 68507	9. 4369	9. 1821
(10)	0. 43423	0. 22672	0. 00637	9.77600	9.5376	9. 2927
(11)	0. 50420	0. 30697	0. 09701	9.87738	9. 6501	9. 4168
s	2. 68656	1.45204	0. 14028	8. 76928	7. 3518	5. 8961
S'	2, 68648	1.45190	0. 14001	8. 76926	7. 3514	5. 8957

The quantities $\delta \log k_i$ and K_i were computed as in Chapter I, but we pass over them to the coefficients A.* In the development of $\frac{a'}{\triangle}$ the latter are:

	A ₀ (c)	A ₁ ^(c)	$A_1^{(s)}$	$\mathbf{A}_{2}^{(c)}$	$\mathbf{A_2^{(s)}}$	A ₃ ^(o)	$\mathbf{A_3^{(*)}}$
	7	8	8	8		8	
(0)	1874943	+1177066	4899385	— 17 66623	— 899917	— 5 59069	+ 654946
(1)	1895225	944398	5055152	1903671	738274	471567	760405
(2)	1882312	709523	5028771	1924952	556101	357552	796140
(3)	1841607	563723	4840437	1835652	433858	275136	7 5 7 9 7 3
(4)	1788462	539609	4574377	1690549	403260	249140	680311
(5)	1738996	616009	4316660	1541518	447582	268384	595211
(6)	1704404	754842	4122426	1417124	5 36430	312651	518401
(7)	1690485	923128	4019319	1331006	646312	368098	456851
(8)	1699164	1094561	4020736	1293582	762323	428572	417018
(9)	1729327	1241964	4132273	1317235	871408	491164	408667
(10)	1776200	1329741	4346774	1413165	953038	548722	444557
(11)	1829843	+1316124	— 4628633	— 1576929	973637	— 581363	+532293
S	1.0725485	+5605342	26992469	- 9505995	-4111069	-2455706	+3511373
S'	1.0725483	+5605346	—2 69924 7 4	<u> —9506011 </u>	-4111071	-2455712	+3511400

^{*} These coefficients have all been divided by 12 in order to save the division by 6 and afterwards by 2, which otherwise would have to be performed in the following process of mechanical quadratures.

	A_4^(0)	A ₄ ⁽⁸⁾	A5(0)	$\mathbf{A}_{5}^{(s)}$	A(c)	A(6)	$\mathbf{A}_{7}^{(c)}$
	8	8	8	8	8	8	8
(0)	+ 230353	+ 316767	+169020	 70126	— 13674	— 8 5 928	- 41765
(1)	303146	276930	154603	116421	41240	83172	43395
(2)	336667	212463	120708	142210	59060	66506	35797
(3)	322830	161679	91066	138875	59632	49871	26755
(4)	282354	142699	7 8353	118332	49485	41832	21876
(5)	235041	148889	79004	92715	35955	40665	20448
(6)	189918	167766	85665	67368	22265	42194	20173
(7)	150672	191591	94119	44339	— 9604	44169	19884
(8)	120769	218345	103940	25296	+ 1296	46664	19740
(9)	105863	249265	117227	12860	9517	51397	20858
(10)	114928	284148	136144	11982	12856	60675	24940
(11)	+ 157470	+ 313849	+157834	30142	+ 6551	— 74548	— 32981
s	+1274989	+1342188	+693830	-435314	-130332	343800	—16429 1
s′	+1275022	+1342203	+693853	-435352	-130363	—343822	-164321
	$\mathbf{A}_{7}^{(s)}$	A (C)	A (8)	A (c)	1	.(0)	A (8)
	A ₇	A ₆ (c)	$\mathbf{A}_8^{(s)}$	$\mathbf{A}_{9}^{(c)}$	A ₉ (*)	A ₁₀	A ₁₀
	A ₇	8	A ₈ ''	8	A ₉ ''	A ₁₀ '	A 10'
(0)			+19364				
(o)	8	8		8	8	п	8
1	8 3250	- 6270	+19364	+ 8503	* +5197	+3468	* 3479
(1)	8 3250 +12253	8 6270 + 1988	+19364 22013	* + 8503 10868	8 +5197 +1036	#3468 +1501	* 3479 5218
(I) (2)	8 3250 +12253 23726	8 6270 + 1988 8998	+19364 22013 18893	* + 8503 10868 9805 7348 5709	** +5197 +1036 -3072	+3468 +1501 - 824	8 3479 5218 5012
(1) (2) (3)	8 3250 +12253 23726 25338	*	+19364 22013 18893	* + 8503 10868 9805 7348	8 +5197 +1036 -3072 4266	+3468 +1501 - 824	8 — 3479 5218 5012 3782
(1) (2) (3) (4)	8 3250 +12253 23726 25338 20466	8	+19364 22013 18893 14116 11252 10082 9388	* + 8503 10868 9805 7348 5709	8 +5197 +1036 -3072 4266 3256	+3468 +1501 - 824 1643	8 3479 5218 5012 3782 2863
(1) (2) (3) (4) (5)	8 - 3250 +12253 23726 25338 20466 13482 + 6344 - 240	8 	+19364 22013 18893 14116 11252 10082	* + 8503 10868 9805 7348 5709 4888	8 +5197 +1036 -3072 4266 3256 -1516	+3468 +1501 - 824 1643 1216 - 376	8 3479 5218 5012 3782 2863 2335
(1) (2) (3) (4) (5) (6)	8 3250 +12253 23726 25338 20466 13482 + 6344 240 5982	8	+19364 22013 18893 14116 11252 10082 9388	* + 8503 10868 9805 7348 5709 4888 4258	* +5197 +1036 -3072 4266 3256 -1516 + 243	+3468 +1501 - 824 1643 1216 - 376 + 456	8 3479 5218 5012 3782 2863 2335 1881
(1) (2) (3) (4) (5) (6) (7)	8 - 3250 +12253 23726 25338 20466 13482 + 6344 - 240	8	+19364 22013 18893 14116 11252 10082 9388 8580	** + 8503 10868 9805 7348 5709 4888 4258 3532	** +5197 +1036 -3072 4266 3256 -1516 + 243 1769	+3468 +1501 - 824 1643 1216 - 376 + 456	8
(1) (2) (3) (4) (5) (6) (7) (8)	8 3250 +12253 23726 25338 20466 13482 + 6344 240 5982	8	19364 22013 18893 14116 11252 10082 9388 8580 7790 7645 9191	** + 8503 10868 9805 7348 5709 4888 4258 3532 2798	** +5197 +1036 -3072 +266 3256 -1516 + 243 1769 3043	+3468 +1501 - 824 1643 1216 - 376 + 456 1134 1662	8
(1) (2) (3) (4) (5) (6) (7) (8) (9)	8 - 3250 +12253 23726 25338 20466 13482 + 6344 - 240 5982 10738	*	19364 22013 18893 14116 11252 10082 9388 8580 7790 7645	** + 8503 10868 9805 7348 5709 4888 4258 3532 2798 2370	** +5197 +1036 -3072 +266 3256 -1516 + 243 1769 3043 4231	+3468 +1501 - 824 1643 1216 - 376 + 456 1134 1662 2176	8
(1) (2) (3) (4) (5) (6) (7) (8) (9) (10)	8 - 3250 + 12253 23726 25338 20466 13482 + 6344 - 240 5982 10738 13799	*	19364 22013 18893 14116 11252 10082 9388 8580 7790 7645 9191	* + 8503 10868 9805 7348 5709 4888 4258 3532 2798 2370 2811	8 +5197 +1036 -3072 4266 3256 -1516 + 243 1769 3043 4231 5501	+3468 +1501 - 824 1643 1216 - 376 + 456 1134 1662 2176 2863	8

In the development of $\left(\frac{a'}{\triangle}\right)^3$ the coefficients are:

	$\mathbf{A_0^{(c)}}$	$\mathbf{A}_{1}^{(c)}$	A ₁ (*)	$\mathbf{A_{g}^{(c)}}$	$\mathbb{A}_2^{(s)}$	A ₈ ⁽⁰⁾	A(a)
	y	7	7	7	7	7	7
(0)	3758796	+ 615689	<u> </u>	—1464338	— 746092	— 632006	+ 740184
(1)	3919241	508729	2721311	1621970	628809	547365	883001
(2)	3817256	375589	2658486	1612294	465458	408028	909249
(3)	3507985	281454	2415836	1454794	343773	297590	820013
(4)	3134340	249239	2115153	1244371	297026	250852	684493
(5)	2815968	264622	1856488	1057581	307310	252204	558847
(6)	2609347	308240	1683942	924813	350156	279553	463397
(7)	2 529922	369410	1607757	851309	413247	322526	400448
(8)	2579589	443847	1629379	838178	493 ⁶ 95	380301	370301
(9)	2757523	526661	1751727	891710	589751	455135	378832
(10)	3053091	603826	1974374	1022472	689690	543002	439795
(11)	3421787	+ 645563	- 2271919	1229155	— 759248	— 618961	+ 56636 1
S	1.8952419	+2596430	-1. 2625015	 7106466	-3042117	-2493742	+3607419
S'	1.8952426	+2596439	—1. 2625038	—7106519	<u>-3042138</u>	—2493781	+3607502
	A(c)	A ₄ ^(*)	A ₅ ^(c)	$\mathbb{A}_{5}^{(s)}$	$\mathbf{A}_{6}^{(c)}$	$\mathbf{A}_{6}^{(s)}$	A ₇ ⁽⁰⁾
	7	7	7	¥	7	7	7
(0)	+ 329286	+ 452971	+ 292157	-121152	— 27677	-174135	- 97057
(1)		1 13-71-					
(")	445195	406510	274288	206655	85834	172991	103502
(2)	445195 486402		274288 210659	206655 248380	85834 120958	172991 136095	103502 84010
		406510	1		120958 115846		
(2)	486402	406510 306719	210659	248380	120958	136095 96865 75757	84010
(2) (3)	486402 442114	406510 306719 221371	210659 150799	248380 230015	120958 115846	136095 96865	84010 59613
(2) (3) (4)	486402 442114 359918	406510 306719 221371 182025	210659 150799 120937	248380 230015 182524	120958 115846 89559	136095 96865 75757	84010 59613 45462
(2) (3) (4) (5)	486402 442114 359918 279792	406510 306719 221371 182025 177387	210659 150799 120937 113954	248380 230015 182524 133616	120958 115846 89559 60814	136095 96865 75757 68842	84010 59613 45462 39732
(2) (3) (4) (5) (6)	486402 442114 359918 279792 215365	406510 306719 221371 182025 177387 190299	210659 150799 120937 113954 117692	248380 230015 182524 133616 92525	120958 115846 89559 60814 35900	136095 96865 75757 68842 68059	84010 59613 45462 39732 37359
(2) (3) (4) (5) (6) (7)	486402 442114 359918 279792 215365 167613	406510 306719 221371 182025 177387 190299 213033	210659 150799 120937 113954 117692 126788	248380 230015 182524 133616 92525 59767	120958 115846 89559 60814 35900 — 15213	136095 96865 75757 68842 68059 69877	84010 59613 45462 39732 37359 36125
(2) (3) (4) (5) (6) (7) (8)	486402 442114 359918 279792 215365 167613 136120	406510 306719 221371 182025 177387 190299 213033 245866	210659 150799 120937 113954 117692 126788	248380 230015 182524 133616 92525 59767 34575	120958 115846 89559 60814 35900 — 15213 + 2041	136095 96865 75757 68842 68059 69877 74756	84010 59613 45462 39732 37359 36125 36316
(2) (3) (4) (5) (6) (7) (8) (9)	486402 442114 359918 279792 215365 167613 136120	406510 306719 221371 182025 177387 190299 213033 245866 292961	210659 150799 120937 113954 117692 126788 141794 166853	248380 230015 182524 133616 92525 59767 34575 18344	120958 115846 89559 60814 35900 — 15213 + 2041 15881	136095 96865 75757 68842 68059 69877 74756 85888	84010 59613 45462 39732 37359 36125 36316 40018
(2) (3) (4) (5) (6) (7) (8) (9) (10)	486402 442114 359918 279792 215365 167613 136120 124495 144048	406510 306719 221371 182025 177387 190299 213033 245866 292961 356320	210659 150799 120937 113954 117692 126788 141794 166853 206619	248380 230015 182524 133616 92525 59767 34575 18344 18145	120958 115846 89559 60814 35900 — 15213 + 2041 15881 22917	136095 96865 75757 68842 68059 69877 74756 85888 108059	84010 59613 45462 39732 37359 36125 36316 40018 50971

	$\mathbf{A}_{7}^{(s)}$	A ₈ (0)	$\mathbf{A}_8^{(s)}$	A (c)	A ₉ (*)	A ₁₀	A ₁₀
(-)	7	7	7	7	7	7	7
(0)	- 7572	16446	+ 50757	+24804	+15167	+11130	—11156
(1)	+29256	+ 5367	59220	32538	+ 3092	+ 4936	17179
(2)	55736	23851	50019	28891	— 9068	— 2674	16240
(3)	56466	26545	35488	20563	11941	5062	11641
(4)	42501	19435	2 6386	14905	8493	3483	8217
(5)	26172	10448	22114	11940	3697	— 1006	6268
(6)	+11742	+ 2440	19629	9915	+ 568	+ 1168	4816
(7)	— 425	— 4269	17602	8072	4040	2848	3448
(8)	10987	10152	16185	6477	7036	4228	2189
(9)	20589	15980	16562	5721	10205	5772	1281
(10)	28215	21922	21200	7216	14133	8085	1433
(11)	-27589	—248 5 1	+ 33322	+13493	+17616	+10947	— 4338
S	+63205	2794	+184176	+92208	+19343	+18454	<u> 44051 </u>
S'	+63291	2740	+184308	+92327	+19315	+18435	-44155

In the development of $\left(\frac{a'}{\triangle}\right)^5$ the coefficients are:

	$\mathbf{A}_0^{(c)}$	A ₁ ^(c)	$\mathbf{A}_1^{(s)}$	$\mathbf{A_2^{(c)}}$	$\mathbf{A_2^{(s)}}$	$\mathbf{A_3^{(c)}}$	A ₃ ^(a)	$\mathbf{A_4^{(c)}}$	A ₄ ^(s)
		б	5	5	6	b	5	5	5
(0)	1. 14989	+23672	— 98590	69581	— 3545 ²	— 3599 5	+ 42155	+ 21912	+ 30146
(1)	1. 24434	20243	108237	79550	30841	32133	51840	30516	27861
(2)	1. 18376	14635	103505	77514	22377	23498	52370	32729	20634
(3)	1.00912	10239	87870	65616	15505	16122	44427	28033	14036
(4)	81594	8276	70291	51559	12307	12529	34185	21083	10665
(5)	66690	8066	56640	40435	11749	11661	25836	15204	9642
(6)	57781	8848	48352	33401	12646	12236	20281	11097	9806
(7)	54516	10353	45044	30042	14583	13806	17142	8451	10740
(8)	56541	12635	46360	30016	17680	16510	16077	6961	12570
(9)	64100	15806	52558	33568	22200	20730	17256	6670	15695
(10)	77652	19645	64250	41538	28019	26611	21552	8285	20495
(11)	96292	+ 23006	— 81006	— 54405	- 33605	— 32935	+ 30132	+ 13206	+ 26352
s	5 . 06933	+ 87711	-4. 31348	-3. 03609	-1. 28481	—1.27379	+1.86620	+1.02067	+1.04316
S'	5. 06944	+ 87713	4. 31355	—3. o3616	—I. 28483	—1. 27 387	+1.86633	+1.02080	+1.04326

	A ₅ ^(c)	A ₅ ^(s)	A ₆ ^(c)	A(s)	A ₇ ^(c)	A ₇ ^(*)	A ₈ ^(c)	A ₈ ⁽⁴⁾	$\mathbf{A}_{9}^{(c)}$	A ₉ ^(a)
	5	5	Б	5	5	5	5	5	5	6
(0)	+22274	- 9235	— 2378	-14972	— 9294	— 726	1738	+ 5361	+2867	+1753
(1)	21522	16219	7594	15302	10193	+2883	+ 583	6430	3864	+ 367
(2)	16235	19148	10513	11824	8126	5393	2545	5337	3373	—1059
(3)	10965	16726	9508	7950	5453	5165	2679	3581	2270	1318
(4)	8140	12281	6808	5762	3857	3604	1820	2471	1527	870
(5)	7126	8353	4301	4871	3139	2066	911	1929	1140	— 353
(6)	6985	5491	2412	4575	2806	+ 882	+ 202	1629	901	+ 52
(7)	7366	3473	- 1001	4596	2656	— 31	— 347	1430	718	360
(8)	8351	2038	+ 135	4987	2708	818	837	1333	584	635
(9)	10287	1132	1108	5994	3119	1604	1376	1426	539	961
(10)	13657	1198	1713	8074	4248	2352	2016	1950	726	1421
(11)	+18387	- 3500	+ 1018	11497	6503	-2483	2466	+ 3306	+1465	+1913
S	+75642	49391	—2026 3	50194	31039	+5983	— 24	+18081	+9978	+1932
S'	+75653	-49403	20278	—50210	—31063	+5996	— 16	+18102	+9996	+1930

The formulæ for mechanical quadratures, when the circumference is divided into twelve parts, are the following:*

Let

$$(0.6) = Y_0 + Y_6$$

$$\begin{pmatrix} \frac{0}{6} \end{pmatrix} = Y_0 - Y_6$$

$$(1.7) = Y_1 + Y_7$$

$$\begin{pmatrix} \frac{1}{7} \end{pmatrix} = Y_1 - Y_7$$

$$(2.8) = Y_2 + Y_8$$

$$\begin{pmatrix} \frac{2}{8} \end{pmatrix} = Y_2 - Y_8$$

$$(5.11) = Y_5 + Y_{11}$$

$$\begin{pmatrix} \frac{5}{11} \end{pmatrix} = Y_5 - Y_{11}$$

Then will

$$6 (c_0 + c_6) = (0.6) + (2.8) + (4.10)$$

$$6 (c_0 - c_6) = (1.7) + (3.9) + (5.11)$$

$$3 (c_2 + c_4) = (0.6) - \{(2.8) + (4.10)\} \sin 30^{\circ}$$

$$3 (c_2 - c_4) = \{(1.7) + (5.11)\} \sin 30^{\circ} - (3.9)$$

$$3 (s_2 + s_4) = \{(1.7) - (5.11)\} \cos 30^{\circ}$$

$$3 (s_2 - s_4) = \{(2.8) - (4.10)\} \cos 30^{\circ}$$

$$3 (c_1 + c_5) = (\frac{0}{6}) + \{(\frac{2}{8}) - (\frac{4}{10})\} \sin 30^{\circ}$$

$$3 (c_1 - c_5) = \{(\frac{1}{7}) - (\frac{5}{11})\} \cos 30^{\circ}$$

$$6c_3 = (\frac{0}{6}) - (\frac{2}{8}) + (\frac{4}{10})$$

$$3 (s_1 + s_5) = \{(\frac{1}{7}) + (\frac{5}{11})\} \sin 30^{\circ} + (\frac{3}{9})$$

$$3 (s_1 - s_5) = \{(\frac{2}{8}) + (\frac{4}{10})\} \cos 30^{\circ}$$

$$6s_3 = (\frac{1}{7}) - (\frac{3}{9}) + (\frac{5}{11})$$

The developments of the reciprocal of the distance between Saturn and Uranus, in terms of the eccentric anomaly of the former and the mean anomaly of the latter, having the form

$$\mathcal{Z}$$
 . C $\cos_{\sin}(i'g' + i\,\varepsilon)$

follow:

Ага	<u>.</u>	<u>z'</u>	(½	$\left(\frac{7}{7}\right)_3$	$\left(\frac{\mathbf{a}'}{\triangle}\right)$)5
	cos.	sin.	cos.	sin,	cos.	sin.
Arg. i' i o o o o - 1 o - 2 o - 3 o - 4 o - 5 I + 4 I + 3 I + 2 I - 3 I - 4 I - 5 c + 3 c + 2 c + I c o o o - 5 c + 3 c + 2 c + I c o o o o o o o o o o o o o o o o o o	008. 1. 0725484 -0. 00890679 +0. 00018228 -0. 00000690 +0. 0000001 -0. 00000055 +0. 00001030 -0. 00033698 +0. 0511968 +0. 11210688 +0. 00256211 -0. 00003945 -0. 00000072 +0. 000000000 -0. 000000022 +0. 00001434					
2 0 2 1 2 2 2 3 2 4 2 5 2 6 3 + 2 3 + 1 3 0 3 - 1 3 - 2 3 - 3 3 - 4 3 - 5 3 - 6 3 - 7 4 + 1 4 0	+0. 0012618 +0. 03389697 -0. 19012006 +0. 00343686 -0. 0000179 +0. 0000003 -0. 00000003 +0. 0000347 +0. 00412364 -0. 02362413 -0. 04911418 -0. 00125449 +0. 00004566 -0. 00000040 -0. 00000062	+0. 0029172 -0. 04369799 -0. 08222140 -0. 00225108 +0. 00005201 -0. 00000009 -0. 00000011 +0. 00000019 +0. 001613 -0. 02644531 +0. 07022773 -0. 00230408 +0. 00002260 -0. 00000056 +0. 00000005	+0. 0153956 +0. 2927492 -1. 4212985 +0. 0332629 -0. 0003964 +0. 0000107 -0. 0000001 +0. 0000021 -0. 0000380 -0. 0006969 +0. 0519270 -0. 2360369 -0. 4987523 +0. 0166941 -0. 0005478 +0. 0000283 -0. 000014 +0. 0001946	+0. 0304443 -0. 3380255 -0. 6084255 +0. 0390821 -0. 0014002 +0. 0000560 -0. 0000024 -0. 0000875 +0. 0033038 -0. 0176977 -0. 2881422 +0. 7214921 -0. 0220076 +0. 0004550 -0. 0000142 +0. 0000010 -0. 0000061 +0. 0001727	+0.11043 +1.52456 -6.07225 +0.16153 +0.01492 -0.00117 +0.00004 +0.00011 -0.00133 -0.00685 +0.36525 -1.28925 -2.54766 +0.31695 -0.01447 +0.00037 -0.00004 0.00000 -0.00265	+0. 27401 -1. 67824 -2. 56964 +0. 55248 -0. 02746 +0. 00066 -0. 00010 -0. 00002 -0. 0144 +0. 03504 -0. 10750 -1. 65646 +3. 73253 -0. 08208 -0. 00645 +0. 00001 -0. 00016 +0. 00257

Arg.	<u>8</u>	<u>7</u>	$\left(\frac{\mathbf{s}'}{\triangle}\right)$	(2)3	(<u>a</u> ∆	<u>(</u>) ⁵
	cos.	sin.	cos.	sin.	cos.	sin.
i' i' 4 — 1	+0.00032826	+0.00002869	+0.0055134	+0.0012174	+0. 04970	- +0. 01383
4-2	-0.00110824	0.00396710	0.0109087	o. o564675	0.05873	—o. 40866
4- 3	-0. 01786394	+0.01058360	-0. 2382085	+0.1305823	—I. 53333	+0. 79638
4 4	+0.02550011	+0.02684391	+0. 3342387	+0.3468465	+2.04147	+2.08642
4-5	-0.00145411	+0.00054586	—o. o151338	—o. oo78763	-o. 04808	—o. 17767
4- 6	+0.00001511	0. 00003423	+0.0003827	+0.0001791	—o, oo226	+0.00762
4 7	-0.0000008	+0.00000044	-0.0000108	-0.0000129	+0.00015	0. 00024
4- 8	0.00000002	0.0000000	+0.0000003	+0.0000005	0. 00005	+0.00003
5 0	-0.0000004	-0.0000004	—o. oooo182	-0, 0000003	-0.00032	+0.00006
5 — 1	+0.00001760	+0.00001261	+0.0003644	+0.0003619	+0.00405	+0.00448
5 - 2	+0.00007944	_o. ooo38768	+0.0022294	-0.0067512	+0.02394	-o. o5887
5 — 3	-0.00312321	+0.00028971	-0. 0509773	+0.0013033	—o. 39350	-0.00779
5 - 4	+0.00384527	+0.01097506	+0.0558747	+0.1741100	+o. 37661	+1.25378
5 — 5	+0.01387683	0.00870666	+0.2179809	-0. 1394720	+1.51295	-0. 98794
5 6	+0.00017098	+0.00086282	-0.0045475	+0.0101665	-0. 10047	+0.03192
5 - 7	-0.00002302	-0.00001163	+0.0000332	-0. 0002946	+o. 00404	+0.00039
5 - 8	+0.00000039	0.00000006	-0.0000048	+0.0000070	—o. ooo18	0.00003
5 — 9	-0.0000001	o. 00000001	+0.0000004	0.0000002	+0.00002	+0.00005
6- 1	+0.00000033	+0.00000123	+0.0000074		+o. 00010	+0.00060
6 — 2	+0.00002126	-0.00002574	+0.0005661	0.0005055	+0.00657	0, 00500
6-3	-0. 00035022	0. 00013341	0. 0066434	-0. 0033090	—o. o5920	-0. o3447
6 4	-0.00021055	+0.00215581	0. 0061802	+0. 0400880	o. o6562	+0.33418
6 5	+0.00627977	0. 00087136	+0. 1158520	—o. 0135815	+o. 92810	-0. 09417
6— 6	—o. oo260695	-0. 00687621	—o. 0498377	-0. 1273840	-0. 40541	1.00404
6 — 7	+0.00048380	-0.00000971	+0.0064929	+0.0031357	+0. 02204	+o. o5876
6 8	0. 00000904	+0.00001420	-0. 0002185	+0.0000129	0.00033	-0. 00215
6- 9	0. 00000009	0. 00000033	+0.0000049	+0.0000006	-0. 00002	+0.00014
6 — 10	+0.00000002	0. 00000001	0. 0000007	-0.000011		
7 - 2	+0.00000237	0.00000087	+0.0000711	0. 0000130	+0.00101	0.00008
7 — 3	0.00002587	-0.00002841	0. 0005245	-0.0007503	⊸ 0. 00506	-0.00859
7 — 4	-0.00016002	+0.00026512	-0.0039942	+0.0055240	—0. 04225	+0.05146
7 - 5	+0.00134634	+0.00040426	+0.0282162	+0.0099378	+0. 25479	+0. 10029
7 — 6	+0.00020896	—o. oo338676	+0.0056211	0. 0713663	+0.05783	o. 63154
7 - 7	0.00328612	+0.00055036	—o. 0702487	+0.0126496	0.62102	+0.11979
7 — 8	+0.00004209 +0.00000813	—0.00025749	+0.0023135	0.0039054	+0.03598	0. 01463
7 — 9 7 — 10	-0.00000013 -0.00000028	+0.00000679 +0.00000004	+0.0000190 -0.0000005	+0.0001576 0.0000042	-0.00118	+0.00055
8 3	0. 00000088	-o. ooooo336	0. 0000097	0.0000991	+0.00001	-0.00108
8-4	-0.00003137	+0.00002019	-o. ooo8558	+0.0004268		0.00128
8 5	+0.00017436	+0.00015621	+0.0039729	+0.0004208	0. 00992 0. 03893	+0.00408
8 6	+0.00040985	-o. 00077163	+0.0105231	o. 0180233	+0.03093 +0.11040	+0.04500
8- 7	-0.00173114	-0.00046247	—o. 0410675	-0. 0115685	o. 39870	—0. 17588 —0. 11670
8 8	-o. oooo4388	+0.00151783	-0. 0005534	+0. 0368484	-0. 00040	+0. 36183
8 — 9	-0. 00013034	-0.00004727	-0.0022034	-0. 0016872	-0.00894	—0. 02283
8 10	+0.00000478	-0. 00000431	+0.0001091	-0.0000119	2.00094	-0.02203
	,	-10	,/-			

	<u>a</u>	,	$\left(\frac{\mathbf{a}'}{\triangle}\right)$	3	(<u>a'</u> ∆)5
Arg.	cos.	sin.	cos.	sin.	cos.	sin.
i' i 9 - 4 9 - 5 9 - 6 9 - 7 9 - 8 9 - 9 9 - 10 10 - 5 10 - 6 10 - 7 10 - 8 10 - 10 11 - 6 11 - 7 11 - 8 11 - 9 11 - 10	-0. 00000393 +0. 00001242 +0. 00013252 -0. 00040704 -0. 00041581 +0. 00067791 -0. 0000025 +0. 00002535 -0. 00004934 -0. 00023910 +0. 00038360 +0. 000012816 +0. 0000338 -0. 0000036 -0. 00007111 +0. 00008339 +0. 000120	sin. +0.00000040 +0.00002990 -0.00010042 -0.00033329 +0.00015303 +0.0000539 -0.0000539 -0.00010118 +0.00019580 +0.00029707 -0.00029228 +0.0000084 -0.00019537 -0.00015737 -0.00016364 -0.00000269	-0. 0001175 +0. 0002644 +0. 0037209 -0. 0104824 -0. 0112711 +0. 0184535 -0. 0011778 -0. 0000220 +0. 0007751 -0. 0012882 -0. 0071473 +0. 0111602 +0. 0036889 +0. 0001107 +0. 000358 -0. 0023016 +0. 0025234 +0. 0060688 +0. 000525	sin. -0.000036 +0.0008598 -0.0024728 -0.0092088 +0.0221456 +0.0038658 +0.0011569 +0.0001211 -0.0000971 -0.0030513 +0.0055011 +0.0087864 -0.0088206 +0.0000397 -0.0006364 +0.0004890 +0.0051955 -0.0000911	-0. 00153 +0. 00235 +0. 04285 -0. 11012 -0. 12170 +0. 19974 -0. 00046 +0. 00966 -0. 01373 -0. 08475 +0. 12826 +0. 00151 +0. 00088 -0. 02954 +0. 03012 +0. 00086	sin. -0. 00016 +0. 01027 -0. 02544 -0. 10241 +0. 23453 +0. 03862 +0. 00153 -0. 00060 -0. 03702 +0. 06185 +0. 10217 +0. 00068 -0. 00827 +0. 00501 +0. 06429 -0. 00132
12 — 7 12 — 8 12 — 9 12 — 10 13 — 8 13 — 9 13 — 10 14 — 9 14 — 10	+0.0000120 -0.00001388 +0.0000281 +0.0000187 -0.0000351 +0.00002866 -0.0000126 +0.0000554 +0.0000071	-0.0000209 -0.0000244 +0.00002877 -0.0000135 +0.00000913 +0.00000394 +0.00000121 +0.00000353 +0.00000110	+0.000525 -0.0004793 +0.000279 +0.0033653 -0.000677 -0.0001528 +0.0010597 -0.000548 +0.0002143 +0.000282	-0.000911 -0.0001181 +0.0016148 -0.0009135 -0.0000568 +0.0003342 +0.0001896 +0.0000542 +0.0001533 +0.0000477	-0. 00096 -0. 00096 -0. 00090	-0.00132 -0.00193 +0.02194 -0.00091 +0.00479 +0.00063

These expressions are now changed to the form

$$\Sigma$$
. C $\frac{\cos}{\sin} \left(i'g' + ig \right)$

The data and formulæ for this operation have already been given (pp. 52, 53). The resulting expressions are

Ann	<u>8</u>	<u>v,</u>	$\left(\frac{\mathbf{a}'}{\triangle}\right)$)3	(<u>a</u>	<u>(</u>) ⁵
Arg.	cos.	sin.	cos.	sin.	cos.	sin.
i' i						
0 0	1.0727980		1. 8983958		5. 0880	Ì
0 — I	0. 00890652	-0. 00299095	—o. 1122762	o. 1919365	—0. 6604	—1. 3589
O- 2	—о, ооооб683	0. 00004887	—o. o o50426	+0.0022754	0, 0742	+0.0587
o— 3	-0. 00000716	—o. ooooo466	-0.0001100	+0.0000188	+0.0015	+0.0026
0- 4	—0. 00000034	0. 00000009	—0.0000 064	+0, 0000046		ĺ
1+ 3	0. 00000045	+0.00000023	0. 0000117	—0. 000002I		
I + 2	0. 00000075	+0.00000799	-0,0001798	0. 0002353	0.0028	0. 0084
1 + 1	0. 00038134	0. 00017655	0. 0173889	+0.0073338	-0. 1717	+0.0919
1 0	+o. 0480640	+0.0489876	+0. 3314766	+0. 2990375	+1.6788	+1.3786
1 — 1	+o. 11187535	0. 53970754	+o. 5239494	—2. 5262128	+1.8039	<u>8. 6390</u>
I — 2	+o. oo569463	0. 01008010	—o. 0757592	-0.0139522	o. 861 <i>2</i>	+0.0910
I — 3	+0.00023582	-0. 00044138	0, 0011221	+0.0003367	+0.0031	+0.0393
I — 4	+0.00001054	—0. 00001967	-0.0000779	+0.0000215	+0.0008	+0, 0006
I — 5	+o, 00000062	—0, 00000105	0.0000017	+0.0000023		
ı — 6	+0.0000003	0, 00000006	+o, oooooo6	+0,0000003		
2+ 2	0. 00000024	+0.00000085	0, 0000041	—o. ooooo8o	+0,0001	o. ooo6
2 + I	+0.00000242	0. 00002305	—o. oo13949	—o, ooo3628	0,0212	-0, 0028
2 0	+0.0003113	+0,0041432	+0.0072264	+0.0459326	+0.0743	+0. 3211
2 — I	+0.04452774	—o. o39o59o4	+0. 3722012	—0. 3036208	+1.8638	—I. 5323
2 — 2	о. 18886318	o. o8299694	—1.4114371	0. 6192600	6. 0240	-2. 6550
z 3	o. 00716277	-o. oo688517	0. 0459755	+0. 0045796	о. 1787	+0.4062
2 4	0. 00034727	—0. 00039658	0, 0020440	0.0000486	+0.0095	+0.0108
2 — 5	0.00001759	—0. 00002263	-0.0000974	+0.0000165	+0.0004	+0.0003
2 — 6	—0. 00000090	-0.0000144	0, 0000048	+0,0000002		
2 — 7	—0, 00000005	-0.00000010	0. 0000001	+0.0000002		
3 + 2	+0.00000002	+0.00000008	+0.0000003	+0.0000004		
3 + 1	+0,00000193	-0,00000026	-0.0000568	-o. oooo786	-0.0014	0.0014
3 0	0.0001504	+0.0002135	0.0021512	+0.0038023	0. 0170	+o. o38o
3 — 1	+0.00538633	0. 00029518	+0.0645244	—o. ooo6875	+0.4341	-0.0102
3 — 2	<u> </u>	-0. 03231744	-0. 1919124	0. 3483735	—1.0601	—1. 9680
3 — 3	0. 04994189	+0.06851021	-0. 5102 2 35	+0.7027453	2. 6368	+3. 6228
3 — 4	—0. 00542270	+0.00350685	—0. 0258488	+0.0375883	+0.0980	+0. 2265
3 — 5	—0. 00038622	+0.00017269	0.0016509	+0.0021759	+0.0058	+0.0060
3 — 6	—o. 0000253 7	+0, 00000841	—0. 0000909	+0.0001241	+0.0004	+0.0003
3 — 7	0.00000171	+0.00000041	0, 0000055	+0.0000079		
3— 8	0. 00000013	+0.00000002	0. 0000003	+0.0000005		
4- 0	0, 0000154	+0.0000042	—0. 0 00350	+0.000139	0. 0040	+0.0022
4 — I	+0.0003687	+0.0002631	+0.005834	+0.004529	+0.0512	+0.0376
4 2	+0.0004843	-0. 0047580	+0.010327	-0. 066129	+0.0780	0. 4674
4-3	-o. o2o6566	+0.0072916	—0. 274560	+0.087712	—1. 7 541	+0. 5345
4 — 4	+0 . 0238870	+0.0273031	+0. 312224	+0. 354333	+1.8943	+2. 1504
4 - 5	+0.0012979	+0.0035822	+0.020807	+0.031507	+0. 1708	+0.0607

Arg.	<u>a</u>	Ź	$\left(\frac{\mathbf{a}'}{\triangle}\right)$	(-)3	$\left(\frac{\mathbf{a}'}{\triangle}\right)^5$	
	cos.	sin,	cos.	sin.	cos.	sin.
i' i 4 — 6	+0.0000449	. +0.0002970	+0.001310	+0.002378	+0.0097	+0.0028
4- 7	+0.0000004	+0.0000217	+0.000079	+0.000160	+0.0006	+0.0002
4 8	-0.000001	+0.0000015	+0.000005	+0.000010	1 00000	
5 — o	0.0000009	-0, 0000008	0. 000028	-0.000010	-0.0004	0.0000
5— I	+0.0000093	+0.0000344	+0.000180	+0.000739	+0.0022	+0.0078
5 2	+0.0003529	-0. 0003754	+0.006671	0.006273	+o. o58o	o. o539
5 — 3	0. 0034448	-0. 0010114	0. 055452	— 0. 019356	0. 4226	—u. 1569
5 — 4	+0.0016055	+0.0120812	+0.020523	+0. 191535	+0. 1275	+1.3752
5 — 5	+o. 01398 5 4	-o. oo746o3	+0. 220383	- 0. 119107	+1.5396	—o. 834 7
5 — 6	+0.0021227	-0. 0002596	+0.026196	u. 007706	+o. 1138	-0. 0939
5 — 7	+0.0001969	+0.0000207	+0.002281	—0. 000378	+o. oo8o	0. 0068
5 — 8	+0.0000155	+0.0000042	+0.000173	-0.000014	+0.0005	-0.0003
5 — 9	0.0000010	+0.0000003	+0.000012	+0.000001		
6 1	-0.0000013	+0.0000024	-0.000033	+0.000064	0, 0004	+0.0009
6— 2	+0.0000494	0.0000075	+0.001093	-0.000097	+0.0113	-0,0011
6- 3	-0. 0002856	0. 0003784	0. 005183	-0. 007847	0. 0455	0. 0722
6-4	o. oo11363	+0.0021744	0. 023261	+0.040002	-0. 2027	+0.3308
6- 5	+0.0065724	+0.0005291	+0. 121250	+0.012370	+0.9702	+0. 1125
6 6	-0.0017619	-o. oo67813	-0. 033752	—o. 125917	0. 2707	0. 9971
6— 7	+0.0001224	0. 0011570	-0. 000360	0.018156	0, 0330	0. 1096
6-8	+0.0000429	-o. ooo1167	+0.000244	0. 001764	-0.0025	0.0095
6- 9	+0.0000056	0,0000096	+0.000039	-0.000145	-0.0002	о. 0008
6 10	+0.0000005	-0.000007	+0.000002	0,000012		
7 — 2	+0.0000040	+0.0000023	+0.000100	+ 0.000066	+0.0013	+o. ooo8
7 — 3	+0.0000002	0. 0000547	+0.000095	0.001291	+0.0012	—o. 013 5
7 — 4	0. 0003444	+0.0001711	0. 007835	+0,003333	— о. 0768	+0.0303
7 5	+0.0012225	+0.0009977	+0.025322	+0.022413	+0. 2271	+0. 2107
7- 6	+0.0010241	—0. 00 33446	+0. 022957	—o. o7o45б	+0.2118	o. 6229
7 7	-0.0031172	+0.0000333	o. o66772	+0.001398	0. 5922	+ 0.0156
7 - 8	0.0005851	0, 0002034	-0.011109	-0, 002641	- -0. 0829	0. 0027
7-9	—0, 0000623	-0.000421	0, 001169	-o. 000517	o. 008 <i>2</i>	—o. ooog
7 10	—o. ooooo53	-0.000054	0.000100	—o. oooo65	—o. ooo8	o. ooo1
7 — 11	—o, oooooo5	0, 0000006	0. 000008	—o. ooooo6		
8-3	+0, 0000035	0. 0000046	+0.000109	0, 000118	+0.0013	0.0015
8-4	<u> </u>	-o. ooooog1	-0. 001283	-0.000321	-0. 0141	-0.0041
8 — 5	+ 0.0000758	+0.0002764	+ 0. 001487	+o. oo6887	+0.0132	+0.0720
8 6	+0.0007564	-0, 0006102	+o. o18706	0. 014018	+o. 1897	—о. 1354
8 — 7	—o, oo15886	-0.0009052	—0. 037644	-0.022189	—o. 3649	0. 2209
8 — 8	—0. 0003329	+0.0013513	-o. oo7637	+0. 032892	—o. 0725	+0. 3239
8— 9	0.0001741	+0.0002739	0. 003192	+0.006112	0. 0179	+0.0541
8 — 10	-0. 0000328	+0.0000297	—0. 000551	+0.000676	—0. 0032	+0.0053
8—11	—0.0000040	+0.0000023	—0. 000061	+0. 000061	0.0004	+0.0005
9 4	0. 0000042	-0.0000046	-0. 000114	-0.000143	0.0014	-0.0018
9 5	o. 0000155	+0.0000409	—o. ooo5o8	+0.001114	—o. oo64	+0.0127

Arg.		a' ∆	($\left(\frac{\mathbf{a}'}{\triangle}\right)^3$	$\left(\frac{\mathbf{a}'}{\triangle}\right)^5$	
mg,	cos.	sin.	cos.	sin.	cos.	sin.
i' i 9 - 6 9 - 7 9 - 8 9 - 9 9 - 10 9 - 11 10 - 5 10 - 10 10 - 11 11 - 6 11 - 7 11 - 8 11 - 9 11 - 10 11 - 11	+0.0002006 -0.0002012 -0.0006385 +0.0005456 +0.0001164 +0.0000130 -0.0000289 +0.0000289 +0.0000265 +0.0002717 +0.0002039 +0.0000200 +0.0000175 -0.0000823 +0.0000115 +0.0001924 +0.0000541	-0.000135 -0.0005177 +0.0006958 +0.0003003 +0.0001199 +0.0000253 +0.0000182 -0.0001334 +0.0000845 +0.0003978 -0.0001921 -0.0000680 +0.000047 -0.0000187 -0.0000297 +0.0001925 -0.0001122 -0.0000377	+0.005449 -0.006532 -0.017222 +0.014921 +0.003018 +0.000318 -0.000164 +0.000853 +0.000727 -0.009655 +0.007878 +0.005889 +0.001382 +0.00055 +0.000610 -0.002612 +0.000219 +0.001705	-0.000095 -0.014033 +0.018323 +0.007893 +0.002659 +0.000526 +0.000606 -0.003928 +0.01751 -0.005852 -0.002065 +0.000165 -0.00165 -0.00167 +0.006264 -0.003546 -0.001225	+0.0607 -0.0671 -0.1851 +0.1582 +0.0444 +0.0068	+0.0009 -0.1532 +0.1933 +0.0846 +0.0163 +0.0022

By the method previously given (p. 52), we compute the Besselian functions corresponding to various multiples of half the eccentricity of Uranus, and find

The expressions for the three multipliers of $\left(\frac{\mathbf{a'}}{\triangle}\right)^{s}$ are

The expressions for the three multipliers of
$$\left(\frac{r}{\Delta}\right)$$
 are
$$a^{2}\left(\frac{r}{a}\right)^{2} = [9.3951972] - 2[8.1416132] \cos g - 2[6.28790] \cos 2g - 2[4.7352] \cos 3g - 2[3.31] \cos 4g$$

$$\left(\frac{r'}{a'}\right)^{2} = 1 + [7.51887] - 2[8.6712719] \cos g' - 2[6.74040] \cos 2g' - 2[5.1105] \cos 3g' - 2[3.61] \cos 4g'$$

$$\frac{r'}{a'} \sin (f' + II') = + [8.6687033]$$

$$- 2[9.5728624] \sin g' - 2[9.5198320] \cos g'$$

$$- 2[7.94302] \sin 2g' - 2[7.88991] \cos 2g'$$

$$- 2[6.4893] \sin 3g' - 2[6.4361] \cos 3g'$$

$$- 2[5.1092] \sin 4g' - 2[5.0561] \cos 4g'$$

The multiplication being performed, we obtain

Arg=i'g+ig	$lpha^2rac{r^2}{\mathbf{a}^2}$	$\left(\frac{\mathbf{a}'}{\triangle}\right)^3$	$\frac{r'^2}{a'^2}\bigg($	$\left(\frac{\mathbf{a}'}{\triangle}\right)^3$	$\left(\frac{\mathbf{a}'}{\triangle}\right)^3 \frac{\mathbf{r}'}{\mathbf{a}'} \sin$	(f'+П')
	cos.	sin.	cos.	sin.	sin.	cos.
i' i	0 4702677		. 99			2 222.9
0 0	0.4731677		1.8891119		1	o. 1 33487
0— I	-0. 0804060	0. 0477507	-0.1366148	-0. 0735532	+1.037767	+0.768901
0— 2	-0.0004317	+0.0032233	0.0007182	+0.0032715	-0.031155	+0.046753
0-3	+0.0000439	+0.0000103	-0. 0000254	—o. ooooo86	-0.001320	+0,000486
0 4	+0.0000007	+0.0000014	0.0000013	+o. 0000031	-0.000072	+0.000020
1+ 3	+0.0000011	+0.0000003	0, 0000051	0, 0000006	+0.000090	+0.000043
1+ 2	+0.0001293	0.0002043	+0.0001163	-0.0001448	+0.003449	+0.002106
1+1	-0.0090114	0. 0018278	0.0124069	0. 0030223	—o. o46000	+0. 126816
10	+0.0753436	+0. 1091910	+0. 1539410	+0. 2980334	-1.419151	—I. 266090
1— 1	+0. 1266233	o. 6315286	+0.5134607	—2. 5113038	+0. 228194	—0. 020260
I— 2	-0. 0261287	+0.0314724	0. 0094558	+0.0151373	0. 321366	+0.702339
1 3	+0.0006687	+0.0007652	+0.0013203	0. 0002655	o. o28698	+0.011342
1-4	+o. ooooo8o	+0.0000169	+0,0000282	0.0000016	o. oo1269	+0.000370
1— 5	÷0.0000012	+0.0000008	+0.0000038	+0.0000003	—o. 000071	+0.000015
2+ 2	+0.0000152	-0.0000042	+0.0000087	+0.0000038	+0.000237	+0,000040
2+ I	-0.0005110	o. 000664 1	-o. ooo5263	-0.0008426	+0.002698	+0.011672
2 0	0. 0030683	+0.0157428	-0,0102913	+0.0318817	—o, 256196	-0.027903
2 I	+0.1119294	0, 0674846	+0. 3458836	—o. 1859817	+0.652930	—I. I22850
2— 2	—o. 3551586	—0. 1 497059	1.4035449	—o. 6042733	+0.048245	+0. 148410
2 — 3	+0.0080904	+0.0097770	<u> </u>	0. 0284357	—o. 426008	0.094198
2— 4	+0.0004023	+o. 000046 1	—0, 0010063	0. 0020105	-0.022147	-0.011159
2— 5	+0.0000207	+0.0000074	-0, 0000344	-0.0001014	0. 001295	-0.000732
2 — 6	+0.0000011	0.0000001	0.0000012	—o. ooooo69	-0.000070	-0, 000050
3+ I	+0.0000043	0.0000703	+0.0000192	0. 0000694	+0.000681	+0.000638
3 0	—o. 0013876	+0.0010190	0. 0027123	+0.0014893	—0, 024306	+0.013756
3— 1	+o. 0188174	+o. 0044666	+0.0467168	+0.0147328	-0.022958	—0. 263625
3— 2	-0.0414954	— o, o9628o3	—0. 1267809	о. 3173609	+0.743227	+0. 248427
3— 3	0. 1237478	+0. 1788859	-0. 4968410	+0.7007472	0. 083595	+0.051828
3- 4	+0.0007075	-0, 0003612	—0. 0404963	+0.0209869	+0.000692	o. 238255
3- 5	+0.0000494	0, 0001165	0. 0027506	+0.0007696	+0.000382	-0.019411
3— 6	+0.0000082	0.0000105	—o, ooo166 5	+0.0000188	+0.000026	-0.001411
3 7	+0.0000004	—0. 0000004	—0.0000105	+0.0000003	0.000035	-0.000094
4 0	0. 000169	0.000015	0. 000259	—o. oooo68	0.00111	+0.00242
4 I	+0.001362	+0.002020	+0.002605	+0.004741	-0. 02422	-0. 02818
4 2	+0.006227	—о. 017775	+0. 01982 7	 0. 049370	+o. 20580	0.06062
4 3	-o. 072682	+0.017790	—0. 24 8903	+0.055945	<u> </u>	+0.44501
4— 4	+0.081079	+o. o86388	+0. 313519	十0. 344733	0. 04247	0.04139
4— 5	+0. 000878	+o. 002868	+o. 010548	+0.037089	+o. 12416	-0.02714
4 6	0. 000024	+0.000084	+0.000108	+0.002812	+0.01316	-0.00427
4 7	0, 000005	0, 000002	—0, 000029	+0.000189	+0.00111	-0.00043
4— 8	0.000000	+0.000001	-0. 000003	+0,000012		
5 0	0.000011	-0. 000012	0.000011	0.000019	+0.00006	+0.00023
5— I	- 0.00032	+0.000275	—0. 000131	+0.000531	—o. 00425	-0.00098

Arg = i'g' + ig	$lpha^2 rac{r^2}{a^2}$	$\left(\frac{\mathbf{a}'}{\triangle}\right)^3$	$\frac{r'^2}{a'^2}$	<u>'a'</u>)3 ∆	$\left(\frac{\mathbf{a}'}{\triangle}\right)^3 \frac{\mathbf{r}'}{\mathbf{a}'}$ sin	$\Gamma(f'+\Pi')$
ing = vy riy	cos.	sin.	cos.	sin.	sin.	cos.
i' i 5— 2	+0.002417	-0.001337	+0.006281	o. 002987	+0.02316	-0. 02952
5-3	-0.014195	—o. 007353	-0. 042230	—o. o23552	+0.07245	+0.13588
5 4	+0.002807	+0.049502	+0.007053	+0. 173647	-0. 24722	+0.02343
5 5	+0.054113	-0.032132	+0. 214434	—0. 121571	+0.01754	—0. 02996
5-6	+0.003417	—o. 000297	+0.027792	-0.001897	+0.02818	+0. 06037
5-7	+0.000159	+0.000035	+0.002339	+0.000464	+0.00518	+0.00758
5— 8	- -	+0.000004	+0.000169	+0.000070	+0.00058	+0.00069
5-9	+0.000001	0. 000000	+0.000011	+0.000008	1 3	0.00009
			,	·		i I
6— I	-0.000022	+0.000019	0, 000046	+0.000026		4.4-
6— 2	+0.000347	+0,000076	+0.000777	+0.000234	+0.00021	-0.00527
6-3	0, 001006	-0.002505	-0.002445	—0, 006961	+0.02895	+0.01458
6 4	0. 007380	+0.009900	0. 024104	+0.030798	0. 07873	+0.06582
6 5	+0.030913	+0.004270	+0.110113	+0.016926	0. 04083	-0. 12855
6 6	—0. 010056	-0.031208	-0. 036180	—0. 122658	+0.01903	+0.00561
6 7	+0.000352	-0.002743	+0.002685	0. 018252	-0.02716	+0.02115
6-8	+0.000072	-0.000160	+0.000762	0.001663	-0.00375	+0.00438
6-9	+0.000006	0.000008	+0.000095	-0.000124	0. 00036	+0.00055
6—10	0, 000000	0.000000	+0.000007	0.000009		
7— 2	+0.000026	+0.000033	+0.000045	+0.000075	0.00038	-0.00053
7-3	+0.000127	-o. 000372	+0.000367	0.000912	+0.00526	0.00083
7— 4	0, 002302	+0.000550	—o. 006725	+0.001373	o. oo662	+0.02437
7— 5	+0.006095	+0.006498	+0.019527	+0.021650	0.05115	-0.04013
7— 6	+0.006281	0. 017832	+0.023722	-0.064120	+0.06252	—o. o3610
7— 7	—o. 016757	+0.001356	<u> </u>	+0.003304	-0. 00047	+0.01113
7 8	-0. 001823	0. 000654	—0. 010789	0, 004120	-0.01367	0. 01106
7 9	-0.000122	0. 000090	—0. 001033	0. 000803	-0.00312	0.00153
7—10	-0.000007	0.000008	0.000076	0. 000097	0, 00042	-0.00011
7—11	-0, 000001	-0.000001	-0.000005	-0.000009		
8 3	+0.000045	-0.000026	+0.000109	0.000053	+0.00052	-0.00053
8— 4	-0, 000346	-0.000170	0. 000901	0. 000495	+0.00165	+0.00445
8— 5	+0.000135	+0.001913	+0.000258	+0.005802	-o. o1833	-0.00111
8 6	+0.005149	0. 003280	+0.017454	—о. 010686	+0.01743	-0. 03572
8 7	0. 009504	0.005776	—o. o3433o	0. 021658	+0, 02586	+0.02813
8 8	0.001335	+0.008396	-0.006328	+0. 032264	—o. oo6o5	+0.00121
8— 9	0. 000672	+0.001058	0. 003852	+0.005780	+0.00385	0. 00800
810	-0.000091	+0.000076	—o. ooo693	+0.000559	+0,00044	-0.00201
8—11	0. 000006	+0.000005	0. 000077	+0.000037	-0.00002	0. 00030
9— 4	0. 000022	-0.000051	-0.000050	0.000131		
9— 5	0.000198	+0.000283	0. 000588	+0.000779		
9— 6	+0.001454	+0.000151	+0.004537	+0.000576		
9— 7	0. 001462	0.003741	-0. 004785	-0. 012855		
9 8	0.004397	+0.004636	0. 016461	+0.016739		1
9 9	+0.003905	+0.001672	+0.014751	+0.007078		
910	+0.000542	+0.000541	+0.002775	+0.002913		1
9—11	+0.000034	+0.000092	+0.000256	+0.000623		

Arg=i'g'+ig	$lpha^2 rac{lpha^2}{\mathtt{a}^2} \Big(rac{\mathtt{a}'}{ riangle}\Big)^3$		$\frac{r'^2}{a'^2}$	<u>(a'</u>)3	$-\left(\frac{\mathbf{a}'}{\Delta}\right)^3\frac{g'}{\mathbf{a}'}\sin\left(f'+\Pi'\right)$	
	cos.	sin.	cos.	sin.	sin.	cos.
i' i 10-5 10-6 10-7 10-8 10-9 10-10 10-11 11-6 11-7 11-8 11-9 11-10 11-11	-0.000053 +0.000206 +0.000301 -0.002518 +0.002010 +0.001334 +0.000260 +0.000066 +0.000187 -0.000662 +0.000055 +0.001501 +0.000339	+0.000015 +0.000204 -0.001017 +0.000440 +0.002970 -0.001588 -0.000434 +0.000049 -0.000132 -0.000343 +0.001620 -0.000951 -0.000256	-0.000142 +0.000587 +0.001026 -0.008752 +0.007196 +0.005478 +0.001292 +0.00012 +0.000582 -0.000158 -0.000158 +0.005886 +0.001646	+0.000034 +0.000613 -0.003244 +0.011123 -0.005830 -0.002040 +0.000138 -0.000390 -0.001185 +0.005730 -0.003284 -0.001132		

In deriving the portion of the perturbative function, which arises from the action of Uranus on the Sun, we have

 $\log h = 9.0095743$ $\log h_1 = 9.0071829$ $\log l = 9.6864004$ $\log l_1 = 9.6866271$ And the expression of this portion is

Arg=i'g'+ig	—a′ -	<u>r</u> _{r'2} H	Arg=i'g'+ig	$-a'rac{r}{r'^2}\mathrm{H}$		
	cos.	sin.		cos.	sin.	
i' i i i i i i i i i i i i i i i i i i	0.00000220.000005570.00021225 +-0.008588870.101811810.002851380.000119780.000005960.00000500.00000500.00001903 +-0.000805520.009549500.00026745	-0.0000003 +0.0000017 +0.0006955 -0.04085337 +0.48521410 +0.01358911 +0.0002843 +0.0000155 +0.0000013 +0.0000170 -0.00383222 +0.04551090 +0.00127460	i' i 2-3 2-4 3+1 3 0 3-1 3-2 3-3 4 0 4-1 4-2 5 0 5-1 5-2	-0. 00001124 -0. 0000056 -0. 00000147 +0. 00006376 -0. 00075575 -0. 00002116 -0. 00000090 +0. 0000047 -0. 0000016 +0. 0000003 -0. 0000001	+0.00005354 +0.00000267 +0.00000105 -0.00030330 +0.00010087 +0.00010087 +0.00000424 -0.0000225 +0.0000075 -0.000016 +0.0000191 +0.0000005	

For the component of this action perpendicular to the plane of Saturn's orbit, we have

$$-\left(\frac{a'}{r'}\right)^2 \sin (f' + \Pi') = +0.747984 \sin g' + 0.662006 \cos g'$$

$$+0.070164 \sin 2g' + 0.062088 \cos 2g'$$

$$+0.005553 \sin 3g' + 0.004913 \cos 3g'$$

$$+0.00041 \sin 4g' + 0.00036 \cos 4g'$$

$$+0.00003 \sin 5g' + 0.0003 \cos 5g'$$

For the factors proportional to the mass of Uranus (in seconds of arc), we have

$$\log \mu = 0.6884739$$

$$\log (\mu \alpha \sin J) = 8.9183882$$

The expressions for the forces are

Arg=i'g'+ig	$arac{d.\Omega}{dg}$		$arrac{d\Omega}{dr}$		$a^2rac{d\Omega}{d extbf{Z}}$	
	sin.	coa.	cos.	sin.	sin.	cos.
i' i	11	"	11	"	11	//
0 0			+0.837381			-0. 011062
0 — I	0. 04346924	+0.01459765	0. 1154317	—o. o556672	+0.0859979	+0.0637175
0 — 2	—o. 0006524	+0.0004770	0.0005359	+0.0002367	0. 002582	+0.003874
0-3	-0.0001048	+0.0000682	—0.0001513	0. 0000347	0.000109	+0.000040
04	—o. ooooo66	+0.0000017	—0 . 0000039	+0.0000044	—0, 000006	+0.000002
1+3	+0.000010	+0.000003	-0. 000015	-0.000002		
I + 2	+o. 000062	+0.000080	-0.000057	+0.000127	+0.000286	+0.000175
1 + 1	+0. 002891	-0.000522	—0. 008391	0. 002145	-0.003812	+0.010509
1 0			+o. 116430	+0. 141898	0. 055619	—o. o5oo6o
1 — 1	+0.049116	+0. 265961	+o. 174087	0. 902032	+0.018910	0. 001679
1 — 2	+0.027754	0. 034252	+o. 012873	+0.051059	-0. 026631	+0. 058201
1 -3	+0.001699	0.001896	+0.000435	+0.001349	-o. oo2378	+0.000940
1-4	+0.000089	-0.000171	—о. 000006	+0.000142	0. 000105	+0.000031
1 — 5	+0.000007	0.000012	+0.000003	+o. oooóo8	о. оооооб	+0.000001
2+2	+0.000007	+0.000010	-0.000018	+0.000018	+0.000019	+0.000003
2 + I	+0.000081	—0. 000060	0. 000136	0.000327	+0.000214	+0.00096 7
2 0	,		—0. 014454	+0.010570	-0.015416	+0.002833
2 — I	+0. 170715	—o. o31489	+0.415651	+0.028267	+0.054106	—o. o93048
2 — 2	—1. 846 1 45	+0.797709	—2. 098802	-0. 900524	+0.003997	+0.012298
2 — 3	—o. 105041	+0. 100028	—o. 055976	—o. 07 6187	0. 035303	-o. oo78o5
2 4	0. 006790	+0.007690	-0.002593	-0.004031	-0.001835	-0. 000925
2 5	0. 000430	+0.000549	0.000091	0.000210	-0.000107	o. oooo61
2-6	-0.000026	+0.000042	0.000003	-0.000013	0.000006	-0.000004
3 + 1	0.000002	+o. 000004	+0.000024	+0.000008	+0.000056	+0.000053
3 0			-0.002554	o. ooo853	0.001554	+0.001547
3 — 1	+0.0226000	0, 0161382	+0.051250	+0.043351	-0.001902	<u> </u>
3 2	0. 188746	+o. 314473	0. 161091	-0. 460147	+0.061590	+0. 020587
3 — 3	—o. 731254	-1.003177	—0. 788591	+1. 106335	-0. 006928	+0.004294
3 — 4	—о. 105865	o. o68466	-0. 087316	+0.043537	+0.000057	0. 019744
3-5	-0. 009425	0. 004214	0. 005890	+0.001741	+0.000032	-0. 001609

	$arac{d\Omega}{dg}$		$ar\frac{d}{dr}$	$rac{d\Omega}{dr}$	$a^2rac{d\Omega}{dZ}$	
Arg=i'g'+ig	sin.	cos.	cos.	sin.	sin.	cos.
i' i	//	"	,, 0,000364	//	,,	//
3— 6	-0.000743	-0. 000246	-0.000364	+0.000051	0, 000000	0, 000117 0, 000008
3— 7	o. oooo58	0, 000014	0. 000024	0. 000000	0.00000	0.00000
4 0			—0.000156	—0,000244	o. oooo58	+0.000230
4— 1	+0.001526	0. 002587	+0.001860	+0.007302	—0. 002007	-0.002335
4- 2	+0.004711	+0.046370	+0.031996	o. o65453	+0.017054	-0.005023
4-3	—0. 302450	0. 106765	-0. 379621	+0.075313	-0, 004281	+o. o3687 7
4 4	+0. 466332	0. 533023	+0. 508930	+0.563813	—o. 003 52 0	-0.003430
4-5	+0. 031672	-0. 087416	+0.020431	+0.074765	+0.010290	0. 002249
4— 6	+0.001315	o. oo869 8	+0.000210	+0.005930	+0.001091	-0.000354
4-7	+0.000013	-0.000741	0.000059	+0.000410	+0.000091	0. 000035
4— 8	—o. 000004	0.000059	0. 000005	+0.000025		
5 0			0. 000000	—0. 000025		
5 1	+0.000026	0. 000261	-0.000283	+0.000634	—o. ooo35	0, 00008
5— 2	+0.003443	+o. 0036 59	+0. 008564	-0.003109	+0.00192	0. 00245
5— 3	0. 050438	+0.014809	—0. обооо7	o. o37o59	+0.00600	+0.01126
5— 4	+0.03134	0. 23585	+ 0. 00644	+0. 27347	0. 02049	+0.00194
5 5	+0. 34128	+0. 18205	+0. 35710	—o. 20005	+0.00145	0, 00248
5— 6	+0.06216	+0.00760	+0.05430	—o. 0032 7	+0.00233	+0.00500
5 7	+0.00673	0.00071	+0.00484	+0.00100	+0.00043	+0.00063
5— 8	+o. 00061	0.00016	+0.00036	+0.00015	+0.00005	+0.00006
5— 9	+0.00004	—0. 0000I	+0.00001	+0.00002		
6— 2	+0.000482	+0.000073	+0,00093	+0.00037	+0.00002	-0.00044
6— 3	-0.004182	+0.005540	-0.00282	0. 00995	+0.00240	+0.00121
6— 4	-0. 022183	—o. 042449	o. o3804	+0.04570	-0.00652	+0.00545
6- 5	+0. 16039	-0.01291	+0. 17724	+0.02959	—o. oo338	0. 01065
6— 6	-0.05159	+0. 19858	—o. o5945	0. 20661	+0.00158	
6— 7	+0.00418	+0.03953	+0.00539	—0. 03502 —0. 00338	-0.00225	+0.00175 +0.00036
6— 8	+0.00168	+0.00456	+0.00158	0.00338	-0, 0003I -0, 00003	+0.00035
6— 9	+0.00025	+0.00042	+0, 00020	0.00020	-0.00003	
7— 2	+0.000039	-0.000022	+0,00003	+0.00010	0. 00003	0.00004
7 3	+0.000003	+0.000801	+0.00059	-0.00119	+0,00044	0. 00007
7— 4	—0, 006723	0, 003340	—o. 00995	+0.00159	⊸ 0. 00055	+0.00202
7— 5	+0.02983	0. 02435	+0.02979	+0.03454	0, 00424	-0.00333
7— 6	+0. 02999	+0.09794	+0.04006	—0. 10480	+0.00518	-0.00299
7— 7	— o . 106 5 0	-0, 00114	0. 11062	+0.00467	0. 00004	+0.00092
7— 8	—o. o2285	+0.00799	0. 02045	0.00796	-0.00113	-0.00092
7 — 9	-0.00274	+0.00185	—0. 00207	0.00163	—0. 00026	-0.00013
7—10	—0. 00026	+0.00026	0, 00016	—0, 00020		
8 3	+0.000051	+0.000067	+0.00015	0. 00005	+0, 00004	0.00004
8 4	—o. 000995	+0.000178	0.00123	0. 00077	+0.00014	+0.00037
8— 5	+0.00185	0. 00674	+0.00012	+o. 00881	0.00152	0.00009
8 6	+0.02214	+0.01786	+0.02819	—o. 016 5 9	+0.00144	0. 00296
8 7	0. 05427	+0,03092	<u> </u>	o. o3655	+0.00214	+0.00233
8 8	-0.01300	-o. 05276	—о. от 137	+0. 05494	-0.00050	+0.00010
8 9	0. 00764	-o. o1203	-0.00734	+0.01086	+0.00032	<u>_0, 00066</u>

Arg=i'g'+ig	$arac{d\Omega}{dg}$		ar	$rac{d\Omega}{dr}$	$a^2rac{d\Omega}{dZ}$	
	sin.	cos.	cos.	sin.	sin.	cos.
i' i	"	11	//	11	"	"
8—10	0, 00160	-0. 00145	-0. 00139	+0.00110	+0. 00004	0.00017
8—11	-0. 0002I	0. 00012	0. 00016	+0.00007		
9— 4	— 0. 00008	+0.00009	—0. 00006	-0.00018		
9— 5	0. 00038	0. 00100	-0.00091	+0.00111		
9— 6	+0.00587	+0.00040	+0.00703	+0.00107	ļ	
9— 7	—0. 00892	+0.01769	-0.00747	—0. 020 98		
9— 8	-0. 02493	-0. 02717	<u>—</u> 0. 02788	+0.02784		
9— 9	+0.02397	-0. 01319	+0.02513	+0.01246		
9—10	+0.00568	—υ. 00585	+0.00516	+0.00549		
9—11	+0.00070	—о. 00136	+0.00051	+0.00123		
10 5	0,00012	0.00008	0, 00020	+0.00004		
10 6	+0.00085	-0.00053	+o. ooo86	+0.00095		
10-7	<u>+</u> 0. 00064	+0.00456	+0.00172	0.00511		
10— 8	0. 01275	0. 00330	—o. 01442	+0.00210		
10— 9	+0.01194	—0. 01748	+0.01199	+0.01893		
1010	+0, 00995	+0.00938	+0.00962	0. 00988		
10—11	+0.00265	+0.00365	 -0. 00240	0.00375		
11— 6	+0.00006	-0.00014	+0.00001	+0,00020		
11-7	+o. ooo6o	+0.00064	+0.00092	-0.00059		
11 8	0. 00321	+0.00116	o. oo345	-0. 00198		
11— 9	+0.00051	0. 00859	-0, 00042	+0.00096		
1110	+0.00939	+0.00548	+0.01023	0.00542		
1111	+0.00290	+0.00202	+ 0. 00306	-0. 00204		

The expressions for the multipliers to be used in obtaining T and $\frac{1}{n} \frac{d\mathbf{R}}{dt}$ from the preceding quantities have been given (p. 74). There is then obtained

Ann-was Life/ Lin	ŗ		*/-/ !	Т		
$Arg = \varkappa y + i'g' + ig$	sin.	cos.	$Arg = n\gamma + i'g' + ig$		sin.	cos.
1 0 1 1 0 1 1 0 1 1 0 1 1 0 1 1 0 1 1 0 1 1 0 1 1 0 1 1 0 1 1 0 1 1 0 1 1 0 1 1 1 0 1 1 1 0 1 1 1 1 0 1	-1. 66360 -0. 1556525 +0. 1304077 -0. 01818 +0. 00101 +0. 00196 -0. 00070 -0. 00028 +0. 00031 -0. 00005 0. 000000 +0. 00002 0. 000000	-0. 00164 +0. 0850031 -0. 0437929 -0. 02650 +0. 00023 -0. 00143 +0. 00004 +0. 00009 -0. 00020 +0. 00007 -0. 00001 -0. 00000	π -I ο I -I I I -I ο ο ο ο ο ο ο ο ο ο ο	i' i I+ 4 I+ 3 I+ 2 I+ 3 I+ 2 I+ I I	+0.00001 -0.00003 +0.00002 +0.00005 -0.00019 +0.00001 +0.00090 -0.00867 +0.01092 +0.12225 -0.12808 +0.27716 -0.14735	" 0. 00000 -0. 00001 0. 00000 -0. 00003 -0. 00024 +0. 00030 -0. 00162 +0. 00157 +0. 00079 -0. 10932 +0. 07935 +1. 42983 -0. 79788

$Arg = \varkappa \gamma + i'g' + ig$	T			Т	
	sin.	cos.	$Arg = \varkappa \gamma + i'g' + ig$	sin.	cos.
и i' i I I— 2	,, —o. 08349	,, —0. 36046	ж i' i —I 3— I	o. 58397	" +1.03259
—ı ı— ı	+0.06653	o. 13184	0 3—2	+0. 56624	0. 94342
0 1-2	-0.08326	+0. 10276	I 3 3	0. 09272	+0.34179
ı ı— 3	+o. o3881	— 0. 03483	_r 3— 2	-2. 23812	-3. 15197
_r r_2	+0.00030	0.00178	0 3-3	+2. 19376	+3.00953
o I— 3	-0.00510	+0.00569	1 3-4	-o. 65846	—0. 89466
I I— 4	+0.00319	-o. oo28o	—I 3— 3	0. 21942	—o. 07115
_1 I— 3	0.00006	0. 00025	0 3—4	+0. 31759	+o. 20540
o I— 4	-0. 00027	+0.00051	I 3-5	-0. I2I47	-o. o9031
I I-5	+0.00023	-0.00022	—I 3— 4	-0. 01239	<u>0.00180</u>
_I I— 4	0.00000	-0.00001	o 3— 5	+0.02827	+0. 01 ₂₆₄
o I 5	0,00002	+0.00004	ı 3— 6	-o. o1303	о. 00688
1 1— 6	+0.00001	-0.00001	_1 3— 5	0. 00070	0, 00000
	0.00000	0.00003	o 3— 6	+0.00223	+ 0.00074
0 2+ 2	-0.00002	0.00003	I 3— 7	-0.00116	o. ooo48
I 2+ I	+0.00002	+0.00004	-ı 3-6	-o. oooo5	0.00000
-I 2+ 2	+0.00006	0.00007	0 3-7	+0.00017	+0.00004
0 2+ 1	-0.00024	+0.00018	ı 3—8	-0.00011	-0, 00004
I 2 0	+0.00071	-0.00015		0.00006	+0.00009
-I 2+ I	0.00196	—o. o1o55	—I 4+ I	0.00010	+0.00033
I 2— I	0. 02117	+0.01579	I 4— I		_o. oog56
—I 2 O	+0.64706	—o. o4388	—I 4 0	+0.00530	+0.00776
0 2— I	-0. 51214	+0. 12447	0 4 1	0. 00458 0. 00036	-0.00623
I 2— 2	+0. 24430	—o. 17179	I 4— 2		+0. 15242
—I 2— I	-5. 81704	+2.50846	—I 4— I	+0. 02317 0. 01413	-
0 2— 2	+5.53843	-2. 39313	0 4-2		—0. 13911
1 2— 3	-1.58653	+0.67972	I 4 3	+0.03051	+0.04457
—I 2— 2	0. 06648	+0. 19031	— I 4— 2	o. 95843	—o. 32489
o 2— 3	+0.31512	-0. 30008	0 4— 3	+0.90735	+0. 32029 -0. 048 2 6
I 2— 4	—o. 14661	+0. 12000	I 4—4	0. 30618	
—I 2— 3	0. 00303	+0.00756	—I 4— 3	+1.47714	—I. 624I3
0 2-4	+0.02037	0. 02307	0 4 4	—I. 39900	+1.59907
I 2— 5	-0.01131	+0.01151	I 4— 5	+0.42152	o. 48958
—I 2— 4	-0.00007	+0.00034	—I 4— 4	+0.03277	0. 19139
0 2-5	+0.00129	-0. 00165	0 4-5	-0.09502	+0. 26225
I 2 6	0.00083	+0.00095	I 4—6	+0.04180	-0. 09795
—I 2— 5	+0.00001	+0, 00002	—I 4— 5	-0.00105	—0. 01322 —0. 02609
o 2— 6	+0.00008	0.00013	0 4 6	-0.00394	+0. 02009 -0, 01148
I 2 7	—o. oooo7	+0.00009	I 4— 7	+0.00252	-0, 01148 -0, 00085
—I 3+ 2	+0.00001	0.00000	—I 4— 6	~ 0,00020	+0.00222
o 3+ 1	+0,00001	-0.00001	0 4-7	-0, 00004	-0.00222 -0.00111
1 3 о	+0.00005	0.00000	ı 4— 8	+0.00010	-0. 00005
—I 3+ I	0. 00090	-0.00012	—I 4— 7	_0.0000I	+0.00018
I 3— I	0. 00205	+0.00264	0 4-8	+0.00001	· ·
—ı 3 o	+0.085207	0. 056091	I 4— 9	o. 0000I	0.00011
o 3— I	o. o67 8 000	+0. 0484146	_r 5 °	0.00000	—0. 00095
ı 3— 2	+0.025043	<u> </u>	0 5-1	-o. oooo8	+o. ooo78
	1		II .	I	l .

$Arg = n\gamma + i'g' + ig$	Т				Т	
	sin.	cos.	$ \text{Arg} = \varkappa \gamma + i'g' + ig $	sin.	cos.	
и i' i I 5— 2	"		ж i' i —1 6—8	+0,00050	,, +0.00056	
1 -	-0.00039		il .	1 -	—0. 00126	
-1 5- 1 0 5- 2	+0. 01244 -0. 01033	+0. 01 143 0. 01 098	o 6— 9 1 6—10	-0.00075 +0.00028	+0.00061	
I 5-3	+0.00710	+0.00111				
—I 5— 2	0. 15962	+0.05245	—I 7— I	+0.00011	-0.00009	
0 5 3	+0.15131	0. 04443	0 7— 2	0.00012	+0.00007	
I 5— 4	0. 04565	+0.03336	1 7— 3	+0.00003	—0, 00008	
—I 5— 3	+0.09432	—o. 73665	—I 7— 2	+0.00017	+0.00261	
0 5-4	-0.09402	+0.70755	0 7— 3	-0.00001	— 0. 00240	
1 5-5	-0.00137	-0, 23034	1 7-4	+0.00064	+0.00092	
—ı 5— 4	+1.04036	+0.59076	−ı 7 − 3	-o. o2168	0.00981	
0 5— 5	—1. o2384	-0. 5461 5	0 7—4	+0.02017	+0.01002	
ı 5— 6	+0.31645	+0. 16417	1 7 5	0. 00855	0.00072	
—ı 5— 5	+0. 14136	0.00148	—I 7— 4	+0.09201	o. o7725	
0 5 6	—o. 18648	-0. 02280	0 7 5	—0. 08949	+0.07305	
ı 5— 7	+ 0. 06861	+0.01171	1 7— 6	+0. 02467	—o. o3o93	
-ı 5 6	+0.01116	-0.00340	—ı 7— 5	+0.09072	+0. 30347	
0 5—7	0.02019	+0.00213	0 7 6	-o. o8997	o. 29382	
1 5—8	+0.00861	0. 00037	1 7-7	+0.03800	+0.09182	
—ı 5— 7	+0.00077	-0.0004I	—ı 7— 6	0. 32841	—0, 01732	
0 5 8	-0.00183	+0.00048	0 7— 7	+0. 31950	-0.00342	
I 5— 9	+0.00087	0.00016	1 7 8	0. 09905	+0.00089	
1 5 <u></u> 8	+0.00003	0.00003	—ı 7— 7	-0.05455	+0.02401	
0 5-9	-0.00012	+0.00003	0 7-8	+o. o6855	—o. 02397	
1 5—10	+0.00009	0.00001	1 7-9	0. 02477	+0.00769	
—ı 6— ı			-ı 7-8	0.00492	+ 0. 00446	
o 6 2	+0.001647 -0.001446	+0.000127	0 7 9	+0.00822	0. 00555	
	1	—0. 000219	1 7—10	0. 00339	+0.00201	
1 6— 3 —1 6— 2	+0.000703 -0.012600	0.000544	—I 7— 9	0. 00036	+0.00053	
o 6— 3	+0.012546	+0. 018545 -0. 016620	0 7—10	+0.00078	0.00078	
1 6— 4	0.00139	+0. 00838	1 7—11	-0.00037	+0.00032	
_1 6— 3	—0. 07267		_I 8 2	+0.00019	+0.00018	
0 6—4	+o. o6655	-0. 13209	1	1	1	
ı 6— 5	—o. o3388	+0. 12735	0 8— 3 1 8— 4	-0.00015	-0.00020	
—ı 6— 4	+0.49771	—0. 03674	_	+0,00012	+0.00004	
o 6— 5	-0.48117	o. o3938		-0.00313	+0.00071	
ı 6— 6		+0.03873	0 8-4	+0.00298	0.00053	
	+0. 15312 0. 18016	-0.02983	1 8 5	-0.00102	+0.00079	
	l .	+0.60780	—I 8— 4	+0.00523	-0.02131	
	+0. 15477	—0. 59574 →0. 18481	0 8 5	-0.00555	+0.02022	
1 6— 7 —1 6— 6	0. 04500 -+0. 01944	+0. 18481	I 8— 6	-0.00032	0.00768	
	-0.01944 -0.01254	+0.09241	—т 8— 5 о 8— 6	+0.06920	+0.05488	
	+0.00284	—0. 11859 —0. 04315	I	—o. o6642	—o. o5358	
		+0.04315	1 8 7	+0.02539	+0.01386	
	+0.00452	+0.00797	—ı 8— 6	-0. 16854	+0.09347	
	0. 00504 +0. 00173	-0. 01368	0 8 7	+0. 16281	—0. 09276	
1 6 9	70.001/3	+0.00572	ı 8— 8	- 0. 04995	+0. 03431	

Arg=ny+i'g'+ig	Т			Т	
	sin.	008.	$Arg = \kappa y + i'g' + ig$	sin.	cos
π i' i -1 8-7 0 8-8 1 8-9 -1 8-8 0 8-9 1 8-10 -1 8-9 0 8-10 1 8-11 -1 8-10 0 8-11 1 8-12 -1 9-3 0 9-4 1 9-5 -1 9-4 0 9-5 1 9-6 -1 9-5 0 9-6 1 9-7 -1 9-6			Arg=ny+i'g'+ig n i' i 1 10— 6 —1 10— 5 0 10— 6 1 10— 7 —1 10— 8 —1 10— 7 0 10— 8 1 10— 9 —1 10— 8 0 10— 9 1 10—10 —1 10— 9 0 10—10 1 10—11 —1 10—10 0 10—11 1 10—12 —1 11— 5 0 11— 6 1 11— 7	sin. // -0. 00017 +0. 00262 -0. 00255 +0. 00071 +0. 00216 -0. 00192 +0. 00174 -0. 03933 +0. 03825 -0. 01315 +0. 03785 -0. 03582 +0. 01027 +0. 02836 -0. 02985 +0. 00657 -0. 00795 +0. 00291 +0. 00016 -0. 00018 +0. 00002	008. // -0,00002 -0.00174 +0.00159 -0.00090 +0.01411 -0.01368 +0.00455 -0.01022 +0.00990 -0.00153 -0.05302 +0.05244 -0.01767 +0.03081 -0.02814 +0.00830 +0.01003 -0.01003 -0.01095 +0.00354 -0.00045 +0.00042 -0.00018
0 9—7 1 9—8 —1 9—7 0 9—8 1 9—9 —1 9—8 0 9—9 1 9—10 —1 9—9 0 9—10 1 9—11 —1 9—10 0 9—11 1 9—12 —1 10—4 0 10—5	+0. 02676 -0. 00615 -0. 07543 +0. 07479 -0. 02614 +0. 07621 -0. 07191 +0. 02196 +0. 01392 -0. 01704 +0. 00608 +0. 00126 -0. 00210 +0. 00090 -0. 00041 +0. 00036	-0. 05307 +0. 01905 -0. 08493 +0. 08151 -0. 02442 -0. 03618 +0. 03957 -0. 01296 -0. 01579 +0. 01755 -0. 00601 -0. 00329 +0. 00408 -0. 00149 -0. 00024 +0. 00024	-I II-6 0 II-7 I II-8 -I II-7 0 II-8 I II-9 -I II-8 0 II-9 I II-I0 -I II-0 I II-I1 -I II-I0 0 II-I1 I II-I2	+0.001920.00180 +0.000830.00993 +0.009630.001480.001530.00016 +0.029150.02817 +0.00808 +0.007850.00870 +0.00273	+0.00194 -0.00192 +0.00048 +0.00373 -0.00348 +0.00182 -0.02657 +0.02577 -0.00857 +0.01746 -0.01644 +0.00523 +0.00548 -0.00606 +0.00200

Arg = ny + i'g' + ig	$rac{1}{n}rac{d\mathrm{R}}{dt}$		Arc-vy Wa' Lia	$rac{1}{n}rac{d\mathbf{R}}{dt}$	
	cos.	sin.	Arg = ny + i'g' + ig	cos.	sin.
κ i' i I 0— I —I 0 0 I 0— 2	,,, +0. 00481 +0. 0428953 —0. 04299	-0. 01283 -0. 0327927 +0. 03138	ж i' i — t 3— 3	+0.00032 +0.00003 +0.00002	,,, +0. 01006 -0. 00972 -0. 00003
-I 0- I I 0- 3 -I 0- 2 I 0- 4	-0. 00490 +0. 00009 +0. 00006 +0. 00004	+0. 00075 +0. 00281 +0. 00014 +0. 00011	I 3-6 -I 3-5 I 3-7 -I 4+ I	-0,00002 0,00000 0,00000 -0,00005	-0. 00108 -0. 00001 -0. 00009 -0. 00008
-I I+ 3 I I+ I -I I+ 2 I I O	+0. 00006 -0. 00030 -0. 00268 -0. 00044	0. 00021 0. 00035 0. 00454 +-0. 00735	I 4— I —I 4 0 I 4— 2 —I 4— I	-0.00006 -0.00076 +0.00172 +0.00854	+0.00021 +0.00123 -0.00096 +0.00189
-I I+ I I I- I -I I O I I- 2	0. 02737 +-0. 02861 +-0. 01141 0. 00978	+0. 02542 -0. 02477 -0. 00207 -0. 00398	I 4-3 -I 4-2 I 4-4 -I 4-3	0. 00866 0. 00290 +-0. 00175 0. 00144	-0. 00409 -0. 01857 +0. 01848 +0. 00329
-I I I I I I - 3 -I I - 2 I I - 4	-0.01411 +0.01296 -0.00007 +0.00155	-0. 02913 +0. 02896 +0. 00198 +0. 00128	I 4— 5 —I 4— 4 I 4— 6 —I 4— 5	+0.00224 +0.00531 0.00504 +0.00011	-0.00109 +0.00098 -0.00114 +0.00008
-I I-3 I I-5 -I 2+2 I 2 0	+0.00005 +0.00010 -0.00008 -0.00076	+0.00004 +0.00004 -0.00047 +0.00036	I 4-7 -I 4-6 I 4-8 -I 5 0		-0. 00021 +0. 00001 -0. 00002 +0. 00006
-I 2+ I I 2- I -I 2 0 I 2- 2	-0. 00695 +0. 00997 +0. 02770 -0. 02662	-0. 00008 +0. 00533 +0. 04640 -0. 04693	I 5— 2 —I 5— I I 5— 3 —I 5— 2	+0.00024 +0.00104 0.00071 +0.00265	+0.00006 +0.00106 -0.00169 -0.00575
1 2— 1 1 2— 3 —1 2— 2 1 2— 4	-0. 00076 -0. 00423 -0. 01782 +0. 01745	-0. 00994 +0. 00517 +0. 00443 -0. 00374	1 5— 4 —1 5— 3 1 5— 5 —1 5— 4	-0. 00389 -0. 01046 +0. 01021 +0. 00162	+0.00551 -0.00047 +0.00123 +0.00125
-I 2-3 I 2-5 -I 2-4 I 2-6	+0.00056 +0.00141 +0.00003 +0.00010	+0.00013 -0.00056 -0.00001 -0.00004	1 5— 6 —1 5— 5 1 5— 7 —1 5— 6	-0.00034 +0.00112 -0.00116 +0.00011	-0. 00141 -0. 00261 +0. 00244 -0. 00010
-I 3+ 2 I 3 0 -I 3+ I I 3- I	+0.00001 -0.00010 -0.00077 +0.000696	-0.00004 -0.00004 -0.00047 +0.001690	1 5— 8 —1 5— 7 1 5— 9 —1 6— 1	-0.00024 0.00000 -0.00003	+0.00038 0.00000 +0.00004
-I 3 0 I 3-2 -I 3-I	0. 00002 +-0. 00356 +-0. 030730	+0. 01069 -0. 01176 -0. 011244	I 6— 3 —I 6— 2 I 6— 4	+0.00004 +0.00009 +0.001107 -0.00147	+0.00020 -0.00027 -0.000691 +0.00036
I 3— 3 —I 3— 2 I 3— 4	-0. 03101 -0. 00605 +0. 00260	+0.00979 -0.00099 +0.00325	-r 6-3 r 6-5 -r 6-4	0. 00341 +0. 00309 0. 00140	-0. 00252 +0. 00319 +0. 00554

$Arg=n\gamma+i'g'+ig$	$\frac{1}{n}$		Arg=μγ+i'g'+ig	$rac{1}{n}rac{d\mathrm{R}}{dt}$			
	cos. sin.			cos.	sin.		
" i' i 1 6— 6 —1 6— 5 I 6— 7 —I 6— 6 I 6— 8 —1 6— 7 I 6— 9 —I 7— 2 I 7— 4 —I 7— 3 I 7— 5	+0.00185 +0.00090 -0.00084 -0.00119 +0.00109 -0.00006 +0.00019 +0.00021 -0.00024 -0.00035 +0.00008		π i' i -1 7-4 1 7-6 -1 7-5 1 7-7 -1 7-6 1 7-8 -1 7-7 1 7-9 -1 7-8 1 7-10	" -0. 00203 +0. 00235 +0. 00277 -0. 00253 -0. 00026 -0. 00010 -0. 00057 +0. 00056 -0. 00008 +0. 00015	+0.00179 -0.00150 +0.00134 -0.00158 -0.00058 +0.00046 +0.00050 -0.00044 +0.00002 -0.00007		

The logarithms of the integrating factors are contained in the following table:

$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$

In making the integrations, for a like purpose, as in Chapter II, we put $k_0 = +1$ ".6639 $k_1 = -0$ ".2304 $k_2 = -0$ ".1420 $k_3 = -0$ ".0216 $k_4 = -0$ ".0163

The values of $\frac{d\delta z}{dt}$ and $\frac{d\nu}{dt}$ obtained are

Arg.		$rac{\delta z}{\partial t}$		$rac{d oldsymbol{ u}}{dt}$
	cos.	sin.	sin.	608
i' i o o	"	"	.1	
1 —0	- o. 1557	— o. o85o	+o. 1573	o. o776
	+ 0.0850031nt	— 0. 1556525 <i>nt</i>	0. 042501 <i>nt</i>	— 0. 077826nt
0— 2	0. 0067	0.0035	+0.0089	- 0.0041
	+ 0.002382nt	— 0. 004362nt	0. 002382nt	- 0.004362nt
o— 3	— 0.0004	0.0002	+o. o oo6	- 0.0003
o— 3	+ 0.000100nt	— 0. 000183nt	-0.000150nt	- 0.000275nt
1+ 2	- 0.0010	+ 0.0001	-0.0012	0.0001
1+1	o. o3o7	- o. ooo3	0. 0209	+ 0.0016
I O	— o. 28914	— 0. 19699	0. 05475	+ 0.01448
1— 1	— I. 070I	+ 5.5233	+0.3728	+ 1.9271
1— 2	+ 0.0444	+ 0. 2679	0. 0216	+ 0. 2090
i— 3	+ 0.0012	+ 0.0103	-0.0012	+ 0.0130
1— 4	0.0000	+ 0.0004	-0. 000 I	+ 0.0009
2+ 1	— o. oo27	— o. oo14	0. 0022	+ 0.0014
2 0	— o. o652	— o. o557	0. 0319	+ 0.0201
2 1	- 2. 46819	— o. 25498	+o. 53598	— o. o8925
2 2	-15.9230	- 6.8519	+9.4146	- 4.0510
2— 3	— o. 5050	— o. 2877	+0. 5502	— 0 . 2 902
2— 4	— 0. O22O	— 0. 0130	+0.0352	0.0192
2— 5	0.0011	o. ooo7	+0.0023	— o. oo14
3+ 1	+ 0.0011	+ 0.0014	+0.0011	- 0.0014
3 0	+ 0.0406	+ 0.0522	+0.0202	o. o266
3 1	+ 1. 25145	+ 0.92442	+0.05199	— o. o4655
3— 2	+11.8038	+20.7417	—5. 6592	+10.0352
3 3	— I. I433	+ 2.6413	+0. 7523	+ 2.0675
3 4	— o. o887	+ 0.1062	+0.0870	+ 0. 1351
3— 5 3 6	- 0.0049 - 0.0002	+ 0.0049 + 0.0002	+0. 0069 +0. 0006	+ 0.0088 + 0.0005
		· į		7 0.003
4 °	+ 0.0003	+ 0.0011	+0.0001	0.0007
	+ 0.0074 0.0654	+ 0.0221	+0.0019	0.0078
4— 2 4— 3	— 1. 1522	+ 0. 5841 + 0. 3762	+0.0353	+ 0. 2024
4— 3 4— 4	+ 0. 4585	+ 0. 3702 + 0. 5534	+0.7480 -0.2584	+ 0. 2693
4— 4 4— 5	+ 0.0193	+ 0.3534	0. 3584 0. 0340	+ 0.4556
4 6	+ 0.0007	+ 0.0313	0. 0249 0. 0015	+ 0.0545 + 0.0054
5— 1	- 0.0013	+ 0.0034	-0. 0015 -0. 0006	- 0.0054 - 0.0013
5— 2	- o. o5323	+ 0.05842	+0.01054	+ 0.00834
5 — 3	— o. 5458	- 0. 1892	+0. 3136	+ 0.00834 - 0.1003
5— 4	+ 0.0174	+ o. 3398	-0. 0178	- 0. 1003 + 0. 2551
5— 5	+ 0. 2239	- 0. 1172	-0.0178 -0.1948	
5— 6	+ 0.0258	0.0030	-0. 0284	— 0.0960 — 0.0051
5-7	+ 0.0020	+ 0.0002	0.0027	- 0,000I
,	1		/	U, UUU1

Arg.	$\frac{d\delta}{d}$		$\frac{1}{n}\frac{d\nu}{dt}$				
	cos.	sin.	sin.	cos.			
i' i 6— 2	+ 0.01321	o. oo150	+0.00110	o. ooo14			
6— 3	+ 0. 1346	+ 0. 1932	-o. o614	+ 0.0913			
6— 4	— o. o532	+ 0.0981	+0.0324	+ 0.0722			
6— 5	+ o. 1332	+ 0.0183	o. 1 0 97	+ 0.0120			
6— 6	0, 0244	— o. o94o	+0.0194	— o. o849			
6— 7	+ 0.0015	- 0.0127	-0.0011	- 0.0141			
6— 8	+ 0.0003	0. 0010	0,0004	— o. oo15			
7— 3	- 0,0001	+ 0.0095	+0.0003	+ 0.0032			
7- 4	0.0299	+ 0.0122	+0.0184	+ 0.0089			
7-5	+ 0.0304	+ 0.0299	0.0250	+ 0.0217			
7 6	+ 0.0198	— 0. 0561	—0. 0158	— 0. 048I			
7— 7 7— 8	— 0. 0393 — 0. 0060	+ 0.0007 0.0021	+0. 0363 +0. 0067	— 0.0008 — 0.0019			
i i			' '				
8 3	— o. ooog4	+ 0.00122	+0,00016	+ 0.00014			
8 4	0. 0140	0.0034	+0.0078	- 0.0017			
8— 5	+ 0.0016	+ 0.0108	-0.0019	+ 0.0077			
8— 6	+ 0.0167	- 0.0112	-0.0131	0.0101			
8— 7 8— 8	— 0. 0232	— 0.0142	+0.0206	- 0.0122			
8 9	0.0036	+ 0.0158 + 0.0027	+0.0042 +0.0017	+ 0.0149			
	0.0017	,	.	+ 0.0030			
9 4	+ 0.0019	+ 0.0021	—o. ooo8	+ 0.0010			
9- 5	— 0.0007	+ 0.0024	+0.0010	+ 0.0016			
9— 6	+ 0.0053	+ 0.0002	0, 0042	- 0.0004			
9— 7	0, 0036	- 0.0094	+0.0039	0.0076			
9— 8	— 0, 0090 + 0, 0061	+ 0.0090 + 0.0032	+0.0079 0.0058	+ 0.0084 + 0.0034			
9 9	+ 0.0001	+ 0.0032	-0.0012	+ 0.0012			
9—10	. .						
10 5	0,0007	+ 0.0003	+0.0004	+ 0.0002			
10 6	+ 0.0010	+ 0.0009	0.0008	+ 0.0005			
10-7	+ 0.0008	- 0.0028	0.0002	0.0023			
10— 8	— 0. 0052	+ 0.0008	+0.0044	+ 0.0012			
10-9	+ 0.0032	+ 0.0051	-0.0031	+ 0.0046			
10—10	+ 0.0021	0.0021	-0.0021	- 0.0019 - 0.0008			
10—11	+ 0.0003	— o, ooo6	0, 0004				
11— 6	0.0000	+ 0.0003	0,0001	+ 0.0002			
11-7	+ 0.0005	— 0. 0002	0.0003	0. 0005			
11— 8	— 0.0015	0.0008	+0.0013	— 0. 0004			
11 9	+ 0.0001	+ 0.0028	—0. 0002	+ 0.0025			
11-10	+ 0.0022	- 0.0012	0. 0022	- 0.0011			
11-11	+ 0.0006	— o. ooo4	0. 0006	0.0004			

Integrating again we obtain $n\delta z$ and ν . The constant term of the latter quantity is obtained in the way mentioned at the end of Chapter II. As the quantities now given appertain to Saturn, we will restore to the symbols their accent, and the mean anomaly of Uranus will be denoted as g''.

Arg=i''g''+i'g'	$n'\epsilon$	$\Im z'$	1	y'		u's i'
	sin.	cos.	cos.	sin.	sin.	cos.
i'' i'	"	11		11	11	
0 I	0,0000 — 0.085000 <i>n't</i>	0. 0000 — 0. 155652n't	+0.0795	+ 0.0351 + 0.077826n't	0. 0000 —0. 032793 <i>n't</i>	0. 0000 +0. 042895n't
0— 2	+ 0.0022 $- 0.001191n't$	— 0 0011 — 0. 002181 <i>n't</i>	+0.0033 -0.001191n't	+ 0.0014 + 0.002181n't	+0.0025 -0.000918n't	-0.0002 +0.001201n't
o— 3	+ 0.0001 0.000033n't	— 0.0001 — 0.000061 <i>n</i> ′ <i>t</i>	+0.0001 -0.000050n't	+ 0.0001 + 0.000092n't		+0.000050n't
I+ 2 I+ I	— 0. 0004 — 0. 0227	0. 0000 + 0. 0002	+0.0005 +0.0155	+ 0.0000 + 0.0012	—o. 0019	-o. o186
1 0 1— 1	0. 8247 + 1. 6479	+ 0.5618 + 8.5055	+0. 1562 +0. 5741	+ 0.0413 - 2.9676	-0. 0668 +0. 0396	—o. 0556 —o. 0103
I— 2 I— 3	— 0. 0269 — 0. 0005	+ 0. 1624 + 0. 0039	0.0131 0.0005	— 0. 1267 — 0. 0049	+0.0390 +0.0172 +0.0006	
1— 4	0.0000	+ 0.0001	0.0000	0.0002		
2+ I 2 0	— 0.0016 — 0.0930	+ 0.0008 + 0.0794	+0.0013 +0.0455	+ 0.0008 + 0.0287	0.0017 0.0403	+0.0002 +0.0224
2— I 2— 2	+ 8. 2613 +12. 2601	— o. 8535 — 5. 2757	+1.7940 +7.2489	+ 0. 2987 + 3. 1191	+0.0626 +0.0024	0. 1009 0. 0302
2— 3 2— 4	+ 0.2197 + 0.0067	- 0. 1251 - 0. 0039	+0. 2394 +0. 0107	+ 0. 1262 + 0. 0058	+0, 0084	+0.0011
2— 5 3+ 1	+ 0.0003 + 0.0005	— 0. 0002 — 0. 0007	+0.0005 -0.0005	+ 0.0003 - 0.0007	+0.0004	0, 0009
3 ° 3— I	+ 0. 0386 +24. 1362	— 0. 0496 —17. 8289	0. 0192 1. 0026	- 0.0253 - 0.8978	+0.0129 0.0544	-0. 0318 -0. 0380
3— 2 3— 3	—12. 4493 + 0. 5869	+21.8760 + 1.3558	—5. 9688 +0. 3862	—10. 5840 — 1. 0612	+0.6084 +0.0208	+0. 2227 +0. 0053
3-4 3-5	+ 0.0301 + 0.0012	+ 0.0360 + 0.0012	+0.0295 +0.0017	- 0. 0458 - 0. 0022	+0.0008	+0.0029
4 0 4— I	+ 0.0002 + 0.0184	0. 0008 0. 0549	0. 0001 0. 0047	0. 0005 0. 0194	-0.0050	0.0033
4- 2 4- 3	+ 0. 1094 + 0. 7212	+ 0. 9775 + 0. 2354	+0. 0591 +0. 4682	- 0. 3387 - 0. 1686	+0.0264	0. 0022 0. 0043
4— 3 4— 4 4— 5	— 0. 1765 — 0. 0054	+ 0.2130 + 0.0143	-0. 1380 -0. 0069	— 0. 1754 — 0. 0151	+0.0043 +0.0006 -0.0008	-0. 0241 +0. 0003 +0. 0002
4 6	— 0. 0002	+ 0.0007	-0.0003	- 0.0012	-0, 0006	
5 1 5 2	- 0.0017 + 0.2155 + 0.4277	0. 0032 + 0. 2366 0. 1517	+0.0008 +0.0427 +0.2514	0.0017 0.0338 + 0.0804	-0.0012 +0.0030	+0.0003 -0.0008
5— 3	+ 0.4377	- J. 131/	+0. 2514	T 0.0004	0.0099	—o. o2o7

Arg =-i''g''+i'g'	$n'\delta$	z'	ν	,	e cos	<u>,'</u>
	sin.	cos.	cos.	sin.	sin.	cos.
i'' i' 5— 4 5— 5	 — 0. 0077 — 0. 0689	+ 0. 1512 — 0. 0361	.,, 0. 0079 0. 0600	.,, — 0. 1135 — 0. 0296	+0.0049	-0.0010
5— 6 5— 7	- 0.0061 - 0.0004	- 0.0007 0.0000	-0. 0067 0. 0005	+ 0.0012 0.0000		
6— 2 6— 3	+ 0. 1274 - 0. 1501	+ 0.0145 + 0.2155	o. 0106 o. 0685	— 0. 0014 — 0. 1019	-0.0010 +0.0112	-0.0011 `+0.0072
6— 4 6— 5 6— 6	+ 0.0281 - 0.0460 + 0.0063	+ 0.0517 + 0.0063 - 0.0241	+0. 0171 0. 0379 +0. 0050	— 0.0381 — 0.0041 + 0.0218	+0.0029 +0.0004	—0. 0018 +0. 0014
6— 7 6— 8	- 0.0003 - 0.0001	— 0. 0026 — 0. 0002	0.0002 0.0001	+ 0,0029 + 0,0003		
7— 3 7— 4 7— 5	+ 0.0002 + 0.0193 — 0.0119	+ 0.0174 + 0.0079 + 0.0117	+0. 0006 +0. 0119 0. 0098	0. 0059 0. 0058 0. 0085	+0.0006 +0.0005 +0.0007	0.0000 0.0015 0.0007
7— 6 7— 7	— 0.0056 + 0.0086	- 0.0158 + 0.0002	-0. 0045 +0. 0080	+ 0.0136 + 0.0002	0.0005	+0.0002
7— 8 8— 3	+ 0.0011 + 0.0048	- 0.0004 + 0.0063	+0.0012	+ 0.0003 0.0007		
8— 4 8— 5 8— 6	+ 0.0117 - 0.0007 - 0.0052	— 0. 0028 + 0. 0049 — 0. 0035	+0. 0065 -0. 0009 -0. 0041	+ 0.0014 0.0035 + 0.0032		
8— 7 8— 8	+ 0.0054 + 0.0007	- 0.0034 + 0.0030	+0.0049 +0.0008	+ 0.0029 0.0029		
8— 9 9— 4	+ 0.0003 0.0022	+ 0.0004	+0.0003 -0.0009	— 0,0005 — 0,0012 — 0,0009		
9— 5 9— 6 9— 7	+ 0.0004 0.0019 + 0.0009	+ 0.0013 + 0.0001 - 0.0024	+0.0005 -0.0015 +0.0010	+ 0.0001 + 0.0020		
9— 8 9— 9	+ 0.0019 - 0.0010	+ 0.0019	+0.0016 0.0010	- 0.0017 - 0.0006		
9—10	- 0.0002 + 0.0005 - 0.0004	+ 0.0002 + 0.0002 + 0.0004	-0.0002 +0.0003 -0.0003	- 0,0002 0,0001 0,0002		
10— 6 10— 7 10— 8	- 0.0004 - 0.0002 + 0.0012	- 0.0004 - 0.0008 + 0.0002	-0.0001 +0.0010	+ 0.0005 - 0.0003		
10—10	— 0, 0006 — 0, 0003	+ 0.0009 - 0.0003	—0. 0006 —0. 0003	- 0.0008 + 0.0003		
11— 7 11— 8	0. 0002 +- 0. 0004	- 0.0001 - 0.0002	-0.0001 +0.0003	+ 0.0001		
11—10	0. 0000 — 0. 0004	+ 0.0005 0.0002	0, 0000 0, 0004	- 0.0005 + 0.0002		

-1 - -

CHAPTER IV.

PERTURBATIONS OF JUPITER BY URANUS OF THE FIRST ORDER WITH RESPECT TO DISTURBING FORCES.

For a like reason as in the preceding chapter we here denote the quantities pertaining to Jupiter without accents and those pertaining to Uranus with a single accent.

The elements of the two planets being the same as those which have already been given (pages 19, 109), we have the corrected $\log a = 0.7162333$ and corrected $\log a' = 1.2831044$. Whence $\log \alpha = 9.4331289$. The coefficients of the terms of the developments of the reciprocal of the distance between Jupiter and Uranus $\frac{a'}{\triangle}$ and its odd powers are functions of the six following elements:

$$\log \alpha = 9.4331289 \qquad J = 0.42 \quad 3.44$$

$$e = 0.04824277 \qquad \Pi = 64 \quad 26 \quad 56.50$$

$$e' = 0.0469236 \qquad \Pi' = 220 \quad 46 \quad 7.70$$

 Π and Π' are measured from the ascending node of the orbit of Uranus on that of Jupiter. In developing these functions it is better to take the eccentric anomaly of Jupiter, as, in this way, the quantity γ_2 is smaller.

The values of the auxiliary constants, entirely similar to those of Chapter I, are

			0	/	"
$\log k$	=9.9999735	\mathbf{K}	=156	19	17.20
$\log k_1$	=9.9999939	\mathbf{K}_1	=156	19	5.20
$\log p$	=9.8345468	\mathbf{P}	= 71	26	4.40
$\log v$	=9.7332373	\mathbf{v}	=156	17	50.42
$\log w$	=9.7340868	W	= 84	52	22.26
$\log w_1$	=9.7332136	W	1= 84	53	51.63
$\log \frac{1}{2} \gamma$	2=5.9320922				

On account of the smallness of α and the consequent smallness of $\frac{1}{2}\gamma_2$, we shall not employ the transformation involving the quantities we have denoted as N, a and b, and the resulting $\delta \log k$ and K, but proceed by the method of Hansen,* where he puts $D = \gamma_0 + \frac{1}{2}\gamma_2$, and we have

$$\left(\frac{\triangle}{\mathbf{a}'}\right)^2 = \mathbf{D} - f\cos\left(\varepsilon - \mathbf{F}\right) + \frac{1}{2}\gamma_2 \cos 2\varepsilon$$

Here we have

$$D = 1.07323843 - [8.9724213] \cos \varepsilon' + [7.3427826] \cos^2 \varepsilon' + [8.6834322] f \cos F$$

As in the preceding chapter, we divide the circumference into twelve parts, with reference to g' the mean anomaly of Uranus. The values of ε' , for these points, have already been given (page 110), and we obtain:

g'	D	$\log f$		g'	
			0	,	11
(0)	0. 9591055	9. 7077032	156	I	21.54
(1)	0. 9702936	9. 7104830	159	15	53. 22
(2)	1.0112715	9. 7199745	161	35	17. 38
(3)	1.0697477	9.7328869	162	23	4. 63
(4)	1. 1293612	9. 7454930	161	34	9. 60
(5)	1. 1746782	9. 7548019	159	27	53.89
(6)	1. 1947071	9. 7589259	156	37	34. 52
(7)	1. 1847586	9. 7570545	153	42	35.70
(8)	1. 1471045	9.7494304	151	23	25.00
(9)	1.0907100	9. 7374805	150	16	27.65
(10)	1.0298657	9. 7239800	150	45	52. 98
(11)	0. 9812273	9. 7128003	152	51	45 · 93
S	6. 4714155	8. 4055070	937	57	41.02
S'	6. 4714154	8. 4055071	937	57	41.02

We propose now to develop the quantity $[D-f\cos{(\varepsilon-F)}]^{-\frac{n}{2}}$, n being a positive odd integer; afterwards passing thence to the developments of $\frac{\mathbf{a}'}{\triangle}$, $\left(\frac{\mathbf{a}'}{\triangle}\right)^3$, etc., by multiplying by the very small factor $\frac{1}{2}\gamma_2\cos{2\varepsilon}$, and applying the resulting corrections. With Hansen * we put

$$[D - f \cos(\varepsilon - F)]^{-\frac{n}{2}} = a_0^{(n)} + 2a_1^{(n)} \cos(\varepsilon - F) + 2a_2^{(n)} \cos 2(\varepsilon - F) + \dots$$

By the method given by Hansen the values of $\log \frac{1}{6} \alpha_i^{(n)}$ have been computed. The division by six is employed for the purpose of saving the constant division by this integer, which occurs in the following process of mechanical quadratures.

^{*}Auseinandersetzung, Abh. I, s. 150.

	$\log \frac{\mathbf{I}}{6} \alpha_0^{(1)}$	$\log \frac{\mathbf{I}}{6} \alpha_1^{(1)}$	$\log \frac{\mathbf{I}}{6} \alpha_{\mathbf{g}}^{(1)}$	$\log \frac{\mathbf{i}}{6} \alpha_3^{(1)}$	$\log \frac{1}{6} \alpha_4^{(1)}$	$\log \frac{1}{6} \alpha_5^{(1)}$	$\log \frac{\mathbf{i}}{6} \alpha_6^{(1)}$
(0)	9. 2575716	8. 4206334	7. 7566836	7. 1377105	6. 5396124	5. 9535909	5. 375448
(1)	9. 2547321	8. 4150722	7. 7484396	7. 1267938	6. 5260269	5. 9373386	5. 356530
(2)	9. 2445835	8. 3947609	7. 7181073	7. 0864763	6. 4757387	5. 8770870	5. 286320
(3)	9. 2308874	8. 3674017	7. 6772652	7. 0321968	6. 4080401	5.7959785	5. 191807
(4)	9. 2177872	8. 3414298	7.6385808	6. 9808401	6. 3440276	5. 7193187	5. 102504
(5)	9. 2083541	8. 3229231	7. 6111071	6. 9444265	6. 2986849	5. 6650522	5. 039317
(6)	9. 2043262	8. 3151566	7. 5996449	6. 9292792	6. 2798568	5. 6425456	5. 013133
(7)	9. 2063362	8. 3192100	7. 6057184	6. 9373670	6. 2899565	5.6546559	5. 027252
(8)	9. 2140731	8. 3344040	7.6282828	6. 9672800	6. 3272093	5. 6992441	5. 079175
(9)	9. 2261996	8. 3581908	7. 6635882	7. 0140681	6. 3854657	5. 7689615	5. 160349
(10)	9. 2401094	8. 3856285	7. 7043793	7. 0681685	6. 4528575	5. 8496357	5. 254300
(11)	9. 2519417	8. 4092158	7. 7395607	7. 1149033	6. 5111293	5. 9194361	5. 335624
s	5. 3784510	90. 1920132	86. 0456787	82. 1697546	78. 4193023	74. 7414220	71. 110880
S'	5. 3784511	90. 1920136	86. 0456792	82. 1697555	78. 4193034	74. 7414228	71. 110879
	$\log \frac{1}{6} \alpha_7^{(1)}$	$\log \frac{1}{6} \alpha_8^{(1)}$	$\log \frac{\mathbf{i}}{6} \alpha_{\mathfrak{g}}^{(1)}$	$\log \frac{1}{6} \alpha_0^{(3)}$	$\log \frac{1}{6} \alpha_1^{(3)}$	$\log rac{1}{6} lpha_2^{(3)}$	$\log \frac{1}{6} \alpha_3^{(3)}$
(0)	4. 80286	4. 23436	3. 66905	9. 3851417	9.0071131	8. 5587907	8. 0827981
(1)	4. 78126	4. 21011	3. 64214	9. 3759125	8. 9953866	8. 5444601	8. 0658349
(2)	4. 70110	4. 11999	3. 54207	9. 3428932	8. 9530189	8. 4923559	8. 0038910
(3)	4. 59318	3. 99870	3. 40735	9. 2985349	8. 8960351	8. 4222507	7. 9205331
(4)	4. 49123	3. 88410	3. 28014	9. 2563416	8. 8418905	8. 3557136	7. 8414871
(5)	4. 41914	3. 80309	3. 19020	9. 2261067	8. 8031994	8. 3082698	7. 7852125
(6)	4. 38928	3. 76956	3. 15299	9. 2132493	8. 7868506	8. 2883108	7. 7616120
(7)	4. 40542	3. 78770	3. 17315	9. 2197005	8. 7952106	8. 2986443	7. 7739360
	4. 46466	3. 85426	3. 24704	9. 2444834	8. 8269489	8. 3375791	7. 8201 308
(8)		3. 95834	3. 36256	9. 2834348	8. 8767414	8. 3986056	7. 8924949
(8) (9)	4. 55729	3. 33-34			1	1	I .
	4. 55729 4. 66451	4. 07885	3. 49636	9. 3283321	8. 9341604	8. 4690276	7. 9760473
(9)	1		3. 49636 3. 61224	9. 3283321 9. 3667 52 0	8. 9341604 8. 9834097	8. 4690276 8. 5295479	7. 9760473 8. 0479558
(9) (10)	4. 66451	4. 07885	1	{			

	$\log \frac{1}{6} \alpha_4^{(3)}$	$\log rac{\mathfrak{I}}{6} lpha_{\scriptscriptstyle{5}}^{\scriptscriptstyle{(3)}}$	$\log \frac{\mathbf{I}}{6} \alpha_6^{(3)}$	$\log \frac{\mathbf{I}}{6} \alpha_7^{(3)}$	$\log rac{\mathbf{i}}{6} lpha_8^{(3)}$	$\log \frac{\mathbf{I}}{6} \alpha_{9}^{(3)}$	$\log\frac{\mathrm{I}}{6}\alpha_0^{(5)}$
(0)	7. 5919423	7. 0917965	6. 585290	6. 07415	5. 55949	5. 04207	9. 57881
(1)	7. 5723348	7. 0695387	6. 560379	6. 04659	5. 52928	5. 00920	9. 56246
(2)	7. 5005087	6. 9878088	6. 468733	5. 94501	5. 41777	4. 88776	9. 50386
(3)	7. 4038440	6. 8778100	6. 345385	5. 80831	5. 26770	4.72432	9. 42535
(4)	7. 3122414	6. 7736264	6. 228604	5. 67892	5. 12570	4. 56970	9. 35096
(5)	7. 2471039	6. 6996098	6. 145700	5. 58713	5. 02501	4. 46010	9. 29782
(6)	7. 2198491	6. 6686942	6. 111119	5. 54888	4. 98309	4. 41452	9. 27528
(7)	7. 2341706	6. 6850168	6. 129446	5. 56922	5.00544	4. 43888	9. 28664
(8)	7. 2876514	6. 7457967	6. 197532	5.64460	5. 08814	4. 52889	9. 33018
(9)	7. 3713956	6. 8409426	6. 304092	5. 76258	5. 21754	4. 66972	9. 39873
(10)	7. 4681307	6. 9508870	6. 427261	5. 89899	5. 36719	4. 83262	9.47800
(11)	7.5514757	7. 0456931	6. 533543	6. 01675	5. 49644	4. 97336	9. 54609
S	84. 3803236	81. 2186096	78. 018539	74. 79055	71.54138	68. 27556	6. 51709
S'	84. 3803246	81. 2186110	78. 018545	74. 79058	71.54141	68. 27558	6. 51709
	$\log \frac{\mathbf{I}}{6} \alpha_1^{(5)}$	$\log \frac{1}{6} \alpha_2^{(5)}$	$\log \frac{1}{6} \alpha_3^{(5)}$	$\log rac{1}{6} lpha_4^{(5)}$	$\log \frac{1}{6} \alpha_5^{(5)}$	$\log rac{1}{6} lpha_6^{(5)}$	$\log rac{\mathbf{I}}{6} lpha_7^{(5)}$
(0)	9.37475	9. 05490	8. 67889	8. 26947	7. 83799	7. 38991	6. 9308
(1)	9. 35641	9. 03419	8. 65564	8. 24383	7. 80960	7. 36030	6. 9000
(2)	9. 29036	8. 95915	8. 57122	8. 14963	7. 70605	7. 24583	6. 7746
(3)	9. 20166	8. 85829	8. 45759	8. 02292	7. 56586	7. 09149	6, 6061
(4)	9. 11752	8. 76265	8. 34996	7. 90314	7.43419	6. 94840	6. 4516
(5)	9. 05741	8. 69438	8. 27315	7.81777	7. 33990	6. 84633	6. 3417
(6)	9. 03198	8. 66557	8. 24084	7. 78184	7. 30048	6. 80297	6. 2945
(7)	9. 04491	8. 68036	8. 25754	7 . 80047	7. 32110	6. 82525	6. 3184
(8)	9. 09419	8. 73636	8. 32046	7. 87062	7. 39760	6, 90982	6.4110
	9. 17164	8. 82423	8. 41933	7. 98041	7.51916	7. 04098	6. 5518
(9)	1	8. 92570	8. 53336	8. 10735	7. 65870	7. 19389	6. 7181
(9)	9. 26104	1				1 20262	6, 8608
	9. 26104 9. 33781	9. 01286	8. 63148	8. 21656	7.77944	7. 32565	0, 8008
(10)	1 -	1	8. 63148 o. 69473	8. 21656 88. 08205	85. 33501	7. 32505 82. 49082	79. 5806

The values of the coefficients A, precisely as in Chapter III, but relative to $[D-f\cos(\varepsilon-F)]^{-\frac{1}{2}}$, instead of to $\frac{\mathbf{a}'}{\triangle}$, are:

	$\mathbf{A}_0^{(c)}$	A ₁ ^(c)	$A_1^{(s)}$		A(c)	$\mathbf{A}_2^{(s)}$	A	(c) 3	$\mathbf{A}_3^{(s)}$		A ₄ ^(c)
	7	8	8		8	8	8		8		8
(0)	1809554	— 2406800	-107043	- 1	82451	+ 424080		12587	-13054		– 3567
(1)	1797762	2432143	92073	·	19850	371066		52439	11845		+ 4126
(2)	1756238	2354727	78385.	. 1	18273	313178		69584	10025		8420
(3)	1701717	2220979	70519	·	88508	274375	1	55043	8583	-	8558
(4)	1651152	2082389	69395	7 3	48112	261003	1 '	54482	7865	-	6189
(5)	1615675	1969751	73783	- -	07911	268324	1	11843	7740	·	2720
(6)	1600760	1896572	81968	8 2	72566	289721	1 2	28893	7990	٠ ا	- 1161
(7)	1608186	1869782	92370	I 2	45115	320 369) 1	6711	8494	ļ2	5099
(8)	1637092	1896051	103417	8 2	30048	357232	:	6745	9249	7	8 789
(9)	1683448	1981141	113119	9 2	34252	396909)	1484	10328	32	11741
(10)	1738239	2120579	118686	6 2	64745	431527	'	4683	11690)2	12854
(11)	1786248	2283311	—117030	3 + 3	+ 320554 + 4456		• —	9456 —12882;		7 -	-10321
s	1. 0193035	-12757118	-558897	9 +19	16195	+2076741	—20	06974	974 598755		–11762
S'	1.0193036	-12757107	-558896	7 +19	16190	+2076722	-20	06976	— 59874	4 -	-11757
	A ₄ ⁽⁸⁾	A ₅ ^(o)	A ₅ ^(s)	$\mathbf{A}_{6}^{(c)}$	$\mathbf{A}_{6}^{(s)}$	A ₇ ^(c)	A ₇ ^(*)	A ₈ ^(c)	A ₈ (s)	A ₉ ^(c)	A ₉ ^(e)
		8	В	8	8	п	8	В	8	8	
(0)	+ 34459	+ 4478	779I	-1917	+1400	+ 621	—1 34	— 1 68	—35	+ 38	+27
(1)	33321	2047	8411	1284	1875	496	345	157	+40	44	+ 5
(2)	28695	+ 271	7530	676	1811	315	391	111	71	34	— 9
(3)	24115	- 210	6248	421	1497	215	328	77	63	24	9
(4)	21196	+ 197	5236	445	1185	195	241	65	41	18	— 7
(5)	19705	1015	4512	600	916	212	155	61	+17	15	+ 1
(6)	19013	1984	3917	792	659	235	69	58	- 7	12	7
(7)	18818	2989	3384	985	403	254	+ 18	53	31	8	12
(8)	19339	3998	3008	1187	174	273	101	47	54	4	17
(9)	21266	5016	3058	1446	42	318	170	48	77		23
(10)	25291	5876	3937	1790	144	420	193	71	97	4	31
(11)	+ 30758	+ 5944	— 5 803	2069	+ 640	+ 563	+ 99	-122	<u>-92</u>	+ 18	+37
s	+147993	+16804	-31419	<u>6807</u>	+5373	+2059	- 541	—520	_8 ₁	+110	+66
						1 ' - '		-518	1	1 '	

In the case of $[D-f\cos(\varepsilon-F)]^{-\frac{3}{2}}$ we have

	$\mathbf{A}_0^{(c)}$	$\mathbf{A}_{1}^{(c)}$	$\mathbf{A}_1^{(s)}$	$\mathbf{A_2^{(c)}}$	$\mathbf{A_2^{(s)}}$)	A	(0)		A ₃ ^(s)	$\mathbf{A}_{4}^{(c)}$	A ₄ ^(*)
(0)	7 2427402	- 9 ⁷ 28795	- ₄ 13086	7 + 24248	7 4 + 268	8878	— ;	7 37529	_	7	7 — 4023	+ 38871
(1)	2376362	925345	350309	26249		991		54262		102943	+ 4591	37071
(2)	2202385	851527	283461	24871	9 186	226		57534		82890	8914	30379
(3)	1988543	750201	238200	21596	1	521		50297		66374	8475	23883
(4)	1804437	659208	219681	18149	136	075	;	39528		57068	5752	19700
(5)	1683088	595234	222964	15331	6 133	605	:	29000		53647	+ 2416	17499
(6)	1633989	561906	242853	13308	8 141	464	:	19640		54316	— 1011	16559
(7)	1658443	559489	27 6396	12086	157	971	:	11470		58303	4484	16550
(8)	1755834	589379	321470	11779	182	914		4807		65914	8024	17656
(9)	1920591	653832	373327	12726	3 215	630		1121		78064	11366	20588
(10)	2129767	749871	419695	15398	250	990		3788		94558	13314	26196
(11)	2326762	— 856562	- 439028	+ 19764	16 + 274	795	_ :	16677	_	110423	—11326	+ 33753
s	1. 1953814	-4340686	1900246	+107755	7 +1166	5547	I	62826	_	469783	11706	+149361
S′	1. 1953789	—4340663	— 1900224	+107754				62827		469754	—11694	l.
	A ₅ (c)	A ₅ (s)	A ₆ ^(c)	A ₆ ^(e)	A ₇ ^(c)	A	(a) 7	A ₈ ^{(c})	A ₈ ^(s)	A(c)	A(*)
(0)	+ 6156		-3108	+2269	+1160		7 250	— ⁷	55	- ⁷ 74	+ 78	+ 64
(1)	2775	11404	2054	2998	914	•	536	3	28	+ 82	10	1 + 12
(2)	+ 349	9717	1029	2757	553	•	686	2:	20	141	7.	5 <u> </u>
(3)	- 253	7542	599	2132	353		537	I.	44	117	4	9 19
(4)	+ 223	5934	595	1585	301	. 3	37 I	I	13	72	3	4 - 9
(5)	1099	4885	766	1170	312	2	229	I	02	+ 29) 2	9 + 2
(6)	2108	4160	993	826	340		100	1	95	— 12	2	2 13
(7)	3205	3629	1247	510	370	+	26	1	87	51	ı	5 23
(8)	4451	3348	1559	229	414	i	153		81	92	2	7 33
(9)	5920	3609	2013	58	511	1	272	1	88	140		2 47
(10)	7419	4971	3666	214	720	1	330	I	37	188		S 68
(11)	十 7949	— 776 1	—3264	+1009	+1024	+	180	— 2	50	189	9 + 4	1 + 85
S	+20706	—3884 1	—9950	+788o	+3488	-	924	-10	oı	-152	2 +23	+150
S′	+20695	<u>38830</u>	-9943	+7877	+3484	-	924	— 9	99	-153	3 +23	7 +150
	E Lam	10	<u> </u>			1		<u> </u>		<u> </u>		

25 AST-10

In the case of $[D-f\cos(\varepsilon-F)]^{-\frac{5}{2}}$ we have

	A ₀ (c)	A ₁ ^(c)	A ₁ (s)	A ₂ ^(c)		A ₂ (s)	A ₃ ^(c)	A ₃ ^(a)
(o)	5 37915	-5 -21655		31 + 7	600	+ 8428	-1481	- 4538
(1)	36514	21249	1	i .	106	7165	2110	4003
(2)	31905	18516	616	54 7	286	5455	2125	3061
(3)	26629	15163	1	5 5	894	4163	1732	2286
(4)	22437	12435	414	14 4	.632	3473	1275	1840
(5)	19853	10688	400	3 3	730	3250	892	1650
(6)	18849	9881	427	70 3	172	3372	592	1638
(7)	19348	9942	491	12 2	911	3805	349	1775
(8)	21388	10905	594	µ8 2	951	4581	152	2086
(9)	25046	12893	736	52 3	391	5745	38	2626
(10)	30061	15917	890	9 4	407	7183	137	3412
(11)	35163	— 1937 I	— 99 2	29 + 6	014	+ 8360	— 639	- 4233
s	1.62555	89309	3906	66 +30	048	+32492	—5762	—16575
S'	1.62553	89306	į.		I .	+32488	5760	—16573
]	1			1			<u> </u>
	A ₄ ^(c)	A ₄ ^(s)	A ₅ ^(c)	$\mathbf{A}_{5}^{(s)}$	$\mathbf{A}_{6}^{(c)}$	$\mathbf{A}_{6}^{(s)}$	A ₇ ^(c)	A ₇ ^(s)
(2)	5	5	5	5	5	6	ıı + 83	5—18
(0)	-191	+1850	+343	—597	-19		1	1
(1)	+215	1740	153 + 18	627	130	1	-	45
(2) (3)	397 353	1354 994	+ 10 - 12	508 368			•	46
(4)	224	768	+ 10	272	3	I	33 18	34
(5)	+ 90	651	48	213	3	1	18	13
(6)	- 37	604	90	178	4	1	μ 19 19	- 6
(7)	165	610	139	157	6	1	25 21	+ 1
(8)	307	676	200	150	8		24	9
		1	282	172	11	1	3 31	17
(9)	462	037	202					
(10) (9)	462 580	837		-	15	6 1	-	
(10)	580 -524	1142	379	254 — 420	15 20	1	3 47	22
(11)	580 —524	1142 +1561	379 + 431	254 — 420	20	2 + 6	13 47 52 + 71	22 +13
(10)	580	1142	379	254	· -	2 + 6 6 +45	$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$	22

From these coefficients are derived the developments of the form $[D-f\cos(\varepsilon-F)]^{-\frac{n}{2}}$, where n successively is 1, 3, and 5; which, as they are so nearly those of $\frac{a'}{\triangle}$, etc., we do not give, but pass immediately to the expressions of the latter functions. We have

Arg=i'g'+iarepsilon	a Z	<u>''</u>	(a	$\left(\frac{\mathbf{a}'}{\triangle}\right)^3$)5
	cos.	sin.	cos.	sin.	cos.	sin.
i' i	1.0193035		1. 195379		1. 6255	
10	-0, 00229705	—0. 00015659	—o. o673943	0. 0205274	o. 2675	-0.0854
0— 2	+0.0000457	+0.0000144	+0.001493	+0.000834	+0.0114	+0.0070
0-3	0, 0000005	-0. 0000004	0, 000028	-0, 000026	0, 0004	0.0003
1+ 2	+0.0000040	0. 0000010	+0.000155	-0.000062	+0.0015	-o. ooo6
1+1	-0. 0004047	-0.0000231	0. 006846	+0.001093	o. o356	+o. oo68
1 0	+0.0623805	+0.0055532	+0. 235847	+0.021001	+0.5626	+0.0502
ı— 1	-o. 2551421	-o. 1117795	—о. 868133	— о. 380047	—1. 7861	— 0. 7813
I— 2	-0. 0004761	-o. ooo7546	+0.012844	+0.009831	+0.0805	+0.0678
1-3	0. 0000068	-0.0000085	-0.000259	0.000301	-0. 0027	-0.0034
2+ I	o. oooo362	_o. ooooo63	0. 000678	+0.000022	0. 0043	+0.0003
2 0	+0.0037678	+0.0006847	+0. 022799	+0.004199	+0.0763	+0.0142
2— I	0. 0280461	-0.0147239	0. 149878	—0. 079949	0. 4252	0. 2285
2— 2	+0. 0383234	+0.0415345	+0. 215505	+0. 233305	+0.6009	+0.6498
2— 3	+0.0001270	+0.0004814	0. 001697	0.002229	-0. 0158	0.0294
2— 4	+0,0000001	+0.0000044	+0.000031	+0.000088	+0.0005	+0.0013
3+ 1	—0. 0000030	-0, 0000008	0. 000065	-0. 000005	-0.0005	0, 0000
3 0	+0.0002550	+0.0000720	+0.002142	+0.000615	+0.0092	+0.0027
3— 1	0. 0026134	-0.0016411	-0. 019031	o. o12257	-o. o688	-0.0449
3— 2	+0.0069628	+0.0086560	+0.051549	+0. 064745	+o. 1787	+0. 2259
3 3	0.0041391	-o. o119747	-0. 032561	-0.093951	o. 1152	-o. 3315
3— 4	+0.0000239	0.0001866	+0.000259	+0.000119	+0.0012	+0.0092
3 5	+0.0000009	0.0000017	+0.000003	-0.000024	0.0000	0, 0004
4 0	o. oooo182	+0.0000072	+0.000197	+0.000078	+0.0010	+0.0004
4— 1	0. 0002277	-0.0001706	-0, 002108	-0. 001630	—o, 0093	-0.0073
4— 2	+0.0008709	+0.0012602	+o. oo8oo1	+0.011812	+0.0332	+0.0498
4-3	0.0009323	0.0034235	o. oo8829	0. 032913	0, 0365	0. 1373
4 4	0.0002354	+0.0029595	-0, 002342	+0. 029867	0. 0099	+0. 1279
4- 5	0. 0000316	+0.0000542	o. ooo155	+0.000121	+0.0004	-0.0022
4— 6	о, ооооооб	+0.0000005	0. 000004	+0.000006		
5— 1	o. 0000191	-0,0000170	-0, 000215	0. 000199	0.0011	0, 0011
5— 2	+0.0000915	+0.0001570	+0.001003	+0.001774	+0.0049	+0.0088
5 3	-0.0001233	-0, 0006229	-o. oo1353	-0.007117	-0, 0064	-0. 0345
5-4	-o. ooo1576	+0.0010713	-0. 001894	+0.012619	0. 0094	+0.0616
5— 5	+0.0003361	-0.0006282	+0.004140	-0.007765	+0.0208	-0. 0392
5— 6	+0.0000158	0. 0000117	+0.000103	-0.000051	-0.0001	+0.0004
5— 7	+0.0000003	0. 0000000	+o. ooooo3	-0.000001		
6— г	0. 0000015	-0.0000016	—0. 0000 20	0. 000023		
6- 2	+0.0000086	+0.0000179	+0.000110	+0.000237	+o. ooo6	+0.0014
~ _	,			1 2. 20023/	1	0.0014

$Arg=i'g'+i\varepsilon$	<u>a'</u> ∆		(<u>a</u>	$\left(\frac{\underline{a}'}{\triangle}\right)^3$)5
1	cos:	sin.	cos.	sin.	cos.	sin.
6' 6 3 6 4 6 5 6 6 6 7 7 7 2 7 3 7 4 7 5 7 6 7 7 8 8 3 8 4 8 5 8 6 8 7 8 8 8 9 4 9 5 9 6	-0.0000112 -0.0000510 +0.0001702 -0.0001361 -0.0000058 -0.0000005 -0.000005 -0.0000117 +0.0000412 +0.0000017 0.0000000 -0.0000022 +0.0000109 -0.0000264 -0.0000104 -0.0000004 -0.0000004	-0. 0000919 +0. 0002332 -0. 0002726 +0. 0001074 +0. 0000013 -0. 0000019 -0. 0000119 +0. 0000396 -0. 0000683 +0. 0000529 -0. 0000108 +0. 0000003 -0. 000015 +0. 0000015 +0. 0000015 +0. 000016 +0. 0000016 +0. 0000016 +0. 0000021 +0. 0000029	-0. 000136 -0. 000710 +0. 002389 -0. 001989 -0. 000050 +0. 000011 -0. 00006 -0. 001252 +0. 000697 +0. 000019 +0. 000019 -0. 00039 +0. 000441 +0. 000486 -0. 000200 -0. 000007 +0. 000039 -0. 000007	-0. 001218 +0. 003155 -0. 003807 +0. 001575 +0. 000006 +0. 000029 -0. 000181 +0. 000607 -0. 001069 +0. 000855 -0. 000184 +0. 000005 -0. 000024 +0. 000099 -0. 000225 +0. 0000257 -0. 000092 -0. 000030 +0. 000014 -0. 000056	-0.0007 -0.0040 +0.0134 -0.0115 0.0000 -0.0012 +0.0049 -0.0079 +0.0046	-0. 0067 +0. 0174 -0. 0213 +0. 0091 -0. 0011 +0. 0037 -0. 0066 +0. 0053 -0. 0012
9— 7 9— 8 9— 9	+0.0000093 -0.0000075 +0.0000022	-0. 0000012 -0. 0000017 +0. 0000013	+0.000186 0.000154 +0.000047	-0. 000022 -0. 000035 +0. 000030		

These expressions are now transformed so as to involve arguments of the general form i'g + ig. The numerical data and formulæ for this transformation have already been given (pages 52, 53).

A	$\frac{\mathbf{a}'}{\Delta}$		$\left(\frac{\mathbf{a}'}{\triangle}\right)^3$		$(\frac{\mathbf{a}'}{\triangle})^5$	
Arg=i'g+ig	608.	sin.	COS.	sin.	cos.	sin.
i' i o o o o l o l o l o l o l o l o l o l	1. 0193589 0. 00029724 0. 0000097 0. 0000034 0. 0003305 +-0. 0685447 0. 2549706 0. 0066217 0. 0002520	-0.00015724 +0.0000106 +0.0000002 -0.0000005 +0.0000094 +0.0082500 -0.1116781 -0.0034453 -0.0001422	1. 1970050. 06740750. 0001310. 0000150. 0000020. 006596 +-0. 2569520. 8682450. 0080830. 000396	-0. 0205617 +0. 000339 -0. 000004 -0. 000032 +0. 001206 +0. 030142 -0. 380300 +0. 000674 -0. 000157	1. 6320 —0. 2678 +0. 0050 —0. 0001 +0. 0006 —0. 0353 +0. 6065 —1. 7890 +0. 0375 —0. 0004	-0. 0857 +0. 0049 -0. 0001 -0. 0004 +0. 0070 +0. 0688 -0. 7841 +0. 0490 -0. 0008

Arg=i'g+ig	<u>a'</u> ∆		$\left(\frac{\mathbf{a}'}{\triangle}\right)^3$		$\left(\frac{\mathbf{a}'}{\triangle}\right)^{\frac{1}{2}}$	
	cos.	sin.	cos.	sin.	cos.	sin.
i' i I— 4	-0.000111	o. ooooo66	-0.000021	—o. oooo13		
I— 5	0. 0000005	0. 0000003				
2+ I	0.0000282	0, 0000022	0. 000635	+0.000044	-0.0042	+o. 00 04
2 0	+0.0044452	+0.0010401	+0. 026430	+0.006126	+0.0867	+o. 0197
2 I	0. 0298780	o. 0167181	-o. 160186	o. og 1157	—o. 4540	—0. 2597
2— 2	+0.0375494	+0.0410484	+0.211516	+0. 230997	+0.5904	+0.6449
2— 3	+0.0019459	+0.0024642	+0.008547	+0.008931	+0.0128	+0.0018
2 4	+0.0000971	+0.0001350	+0.000403	+0.000464	+0.0008	+0.0007
2— 5	+0.0000050	+0.0000073	+0.000021	+0.000025		
3+ 1	0,0000022	0. 0000003	_o. oooo6o	o. 000001	o. ooo5	0.0000
3 0	+0.0003181	+0.0001116	+0. 002603	+0.000911	+0.0109	+0.0038
3 1	0.0029513	—0. 0020 680	-0. 021534	o. o15454	-o. o ₇₇₅	o. 0561
3— 2	+0.0071828	+0.0094615	+0.053324	+0.071090	+0. 1849	+0. 2483
3— 3	—o. oo37870	o. 0114790	0. 029953	—o. 09036 7	—о. 1062	—0. 3198
3— 4	-0. 0002584	—0. 0010272	0. 001969	о. 00б495	0.0067	0.0143
3— 5	-0.0000140	—o. oooo7o6	0. 000107	-o. 000413	-o. 0004	—0. 0009
3— 6	—o. oooooo7	0. 0000044	0. 000006	—o, oooo26		
4 0	+0.0000237	+0.0000113	+0.000248	+0.000117	+0.0012	+0.0006
4— 1	0. 0002704	0. 0002343	-0.002501	0. 002228	0. 0109	—o. oo98
4— 2	+0.0009303	+0.0015075	+0, 008564	+0.014194	+o. o355	+0.0597
4- 3	o. ooo8631	—o. 0036297	0. 008176	0. 035048	—o. o337	—o. 1465
4 4	0. 0002945	+0.0026818	0. 002918	+0.027233	-0, 0123	-i 0. 1172
4- 5	0. 0000574	+0.0003220	-0.000414	+0.002838	_o. ooo8	+0.0095
4— 6	—o. ooooo62	+0.0000266	-0, 000040	+0.000219	—0, 000I	+0.0006
4— 7	o. oooooo5	+0.0000019	—0. 000003	+0.000015		
5— I	—o. oooo236	0. 0000251	-0. 000264	0, 000291	—o. oo13	-0.0015
5— 2	+0.0000993	+0.0002037	+0.001090	+0.002308	+0.0054	+o. o114
5-3	—0.0001016	—o. ooo7178	—0. 001098	0. 008243	0.0052	-0.0400
5— 4	—0. 0002050	+0.0010922	—0, 0 02467	+0.012925	-0.0123	+0. 0632
5— 5	+0,0003133	0.0005174	+0.003878	o. oo6467	+0.0196	—o. o329
5— 6	+0.0000545	—o. oooo793	+0.000582	0.000892	+0.0023	-0.0039
5— 7	+0.0000059	0.0000075	+0.000059	-0.000079	+0,0002	0.0004
5— 8	+0.0000005	—0. 0000007	+0.000004	0, 000007		
6— 1	0.0000019	—o. ooooo26	—o. 000025	0. 000035	Ι.	
6— 2	+ 0. 0000093	- 	+0.000118	+0.000330	+o. 000 7	+0.0019
6— 3	—0. 0000051	-0.0001141	0. 000051	-0.001522	-0, 0002	—0. 0084
6— 4	—o. 0000727	+0.0002578	0. 001014	+0.003507	—o. oo58	+0.0194
6— 5	+0.0001823	-0. 000262I	+0.002571	-o. oo3681	+0.0145	0.0206
6— 6	-0. 0001124	+0.0000741	—0. 001660	+0.001109	—o. oo97	+0.0065
6 7	0. 0000235	+0.0000140	0. 000309	+0.000194	0. 0015	+0.0011
6— 8	0. 0000028	+0.0000015	—o. oooo33	+0, 000020		1
7— I	—o. oooooo165	0, 000000262				
7— 2		+0.0000029	+0,000011	+0.000044	l .	
7— 3	+0.0000008	0. 0000158	+0.000016	-0.000242	+0.0001	-0.0015
7— 4	0.0000180	+0.0000469	—0. 000286	+0.000722	0.0019	+0.0044

Arg-i/g-li-	$\frac{\mathbf{a}'}{\Delta}$		$\left(\frac{\mathbf{a}'}{\triangle}\right)^3$		$\left(rac{\mathbf{a}'}{ riangle} ight)^{oldsymbol{5}}$	
Arg=i'g+ig	cos.	sin.	cos.	sin.	cos.	sin.
i' i 7-5 7-6 7-7 7-8 7-9 8-3 8-4 8-5 8-6 8-7 8-8 8-9 9-4 9-5 9-6 9-7 9-8 9-9	+0.0000591 -0.0000767 +0.0000292 +0.000009 +0.0000002 -0.0000037 +0.0000143 -0.0000272 +0.0000243 -0.0000059 -0.0000006 +0.0000029 -0.0000072 +0.0000096 -0.0000063 +0.0000009	-0. 0000713 +0. 0000458 -0. 0000037 -0. 0000009 -0. 0000001 -0. 0000022 +0. 0000134 -0. 0000134 -0. 0000021 -0. 0000021 -0. 0000024 +0. 0000027 -0. 0000021 +0. 0000021 +0. 0000021 +0. 0000021	+0.000940 -0.001250 +0.000502 +0.000117 +0.000016 +0.000065 -0.000253 -0.000493 +0.000449 -0.000118 -0.000029 -0.000013 +0.000056 -0.000141 +0.000195 -0.000129 +0.000019	-0. 001122 +0. 000744 -0. 000069 -0. 000014 -0. 000035 +0. 000125 -0. 000241 -0. 000048 -0. 000040 -0. 000045 +0. 000054 -0. 000054 -0. 000063 +0. 000063	+0.0058 -0.0079 +0.0034 +0.0007	0. 0069 +-0. 0046 0. 0001
8— 8 8— 9 9— 4 9— 5 9— 6 9— 7 9— 8	-0. 0000059 -0. 0000015 -0. 0000006 +0. 0000029 -0. 0000072 +0. 0000096 -0. 0000063	-0.000021 -0.000004 +0.000011 -0.000024 +0.000027 -0.000005 -0.0000021	-0. 000118 -0. 000029 -0. 000013 +0. 000056 -0. 000141 +0. 000195 -0. 000129	-0. 000040 -0. 000019 -0. 000045 +0. 000054 -0. 000005 -0. 000043		

We compute the following Besselian functions, corresponding to the multiples of half the eccentricity of Uranus, by means of the process given, (page 52):

	$l=\frac{1}{2}e'$	l = e'	$l=\frac{3}{2}e'$	l=2e'	$l=\frac{5}{2}e'$
$\log {f J}_{\imath}^{{\scriptscriptstyle (0)}}$	9.9997610	9.9990432	9.9978458	9.9961666	9.99400
$\log { m J}_{\imath}^{{\scriptscriptstyle (1)}}$	8.3702419	8.6709131	8.8464064	8.97051	9.06634
$\log J_i^{(i)}$	6. 43961 3 0	7.0414338	7.3932179	7.64254	7.83564
$\log J_i^{\scriptscriptstyle{(3)}}$	4.3328729	5.2357835	5.7637586	6.1 3 816	6.42835
$\log J_i^{(4)}$	2.1011862	3.3051637	4.0092888	4.50871	4.89592
$\log { m J}_{\imath}^{\scriptscriptstyle (5)}$			2.1578731	2.78229	3.26648

Then, for the three multipliers of $\left(\frac{a}{\triangle}\right)^3$, we have:

$$\alpha^2 \frac{r^2}{a^2} = [8.8677713] - 2[7.5495636] \cos g - 2[5.63073] \cos 2g - 2[4.0129] \cos 3g$$

$$\frac{r'^2}{a^2} = [0.0014320] - 2[8.6712719] \cos g' - 2[6.74040] \cos 2g' - 2[5.1105] \cos 3g'$$

$$\frac{\mathbf{r}'}{\mathbf{a}'}\sin(f' + \Pi') = + \begin{bmatrix} 8.6624013 \end{bmatrix} \\
-2[9.5776690] \sin g' \\
-2[7.94783] \sin 2g' \\
-2[6.4941] \sin 3g' \\
-2[5.1139] \sin 4g' + \begin{bmatrix} 8.6624013 \end{bmatrix} \\
-2[9.5135301] \cos g' \\
-2[7.88361] \cos 2g' \\
-2[6.4298] \cos 3g' \\
-2[5.0500] \cos 4g'$$

The products are:

Arg=i'g'+ig	$\alpha^2 \frac{r^2}{a^2}$	$\left(\frac{\mathbf{a}'}{\triangle}\right)^3$	$\frac{r'^2}{\mathbf{a}'^2} \left(\frac{r}{r} \right)$	<u>a'</u>)³
	cos.	sin.	cos.	sin.
i' i				
0 0	+0.088520		1. 188889	
O I	—о. 134538	—o. o15185	—0 , 265023	o. o26828
0— 2	+0.000127	+0.000098	+0.000131	+0.000178
o— 3	0, 000000	0.000000	—o. ooooo1	0. 000001
I+ 2	+0.000013	0. 000007	+0.000005	-0.000013
1+1	-0.001361	-0.000002	—0. 002946	+0.000033
1 0	+0.022050	+0.003567	+0. 144114	+0.029971
I I	—o. 064916	0. 028157	—0. 86042 1	—o. 376306
1— 2	+0.002471	+0.001398	—0. 018055	0. 010215
1— 3	+0.000037	+0.000002	0. 000781	0. 000527
I— 4	0. 000000	0.000000	—0. 000039	—0. 000031
2+ 2			-0.000015	+0,000004
2+ I	-0.000134	—0. 000015	0.000277	0. 000029
2 0	+0.002511	+0.000765	+0. 013021	+0. 004689
2 I	o. 012658	o. oo7564	—о. 118937	0. 072881
2— 2	+0. 016137	+o. 01 7 327	+0. 210087	+0. 228385
2- 3	-0.000114	—0. 000158	+o. o10003	+0.013225
2— 4	0.000009	—o. ooooo8	+0, 000499	+0.000757
2— 5	+0.000001	0. 000000	+0. 000026	+ 0, 000042
3+ I	0, 000012	—0. 000002	0.000025	-0. 000004
3 o	+o. 000266	+0.000119	+0.001188	+0.000605
3— 1	0. 001785	-0.001391	—o. o13495	-0.010915
3— 2	+0.004115	+0.005618	+0.043179	+0.059822
3- 3	—0. 002390	o. oo6893	— 0. 030068	o. o8943 5
3 4	-o. 000041	0.000161	o. 001856	0. 007823
3- 5	0.000000	0, 000003	-0. 00009I	0. 000544
3— 6	0.000000	0.000001	0. 000004	0. 000036
4 0	+0.000027	+0.000016	+0.000109	+0.000071
4— I	0.000215	-0.000213	0, 001388	0.001441
4— 2	+0.000670	+0.001178	+0.005924	+0.010671
4 3	—o. 000623	0.002732	—o. 006751	—o. o3o542
4 4	—0. 000185	+0.002121	0.002719	+0.027020
4— 5	—o. 000021	+0.000112	o. ooo593	+0.003171
4— 6	0, 000002	+0.000005	—0.0000 66	+0,000262
4 7			—0. 000006	+0.000019
5 O			-0.000013	—0. 000006
5 1	0. 000023	—0. 000029	—0. 000133	-0. 000176
5— 2	+0.000085	+0.000199	+0.000654	+0.001593
5— 3	o. oooo76	0. 000662	0, 0 00700	—o. oo65o5
5— 4	-0.000192	+0.001005	0, 002289	+0.011529
5— 5	+0. 000293	-0.000520	+0.003788	-o. oo6447
5— 6	+0.000029	0, 000044	+0.000665	0. 000957
	·	1	1	1

Arg=i'g'+ig	$lpha^2rac{r^2}{a^2}$ ($\left(\frac{\mathbf{a}'}{\triangle}\right)^3$	$\frac{r'^2}{\mathbf{a}'^2}$ (<u>(a'</u>)3
	cos.	sin.	cos.	sin.
i' i 5— 7 5— 8	+0.000002	0, 000003	+0. 000073 +0. 000006	o. 000088 o. 000008
6— I 6— 2 6— 3 6— 4 6— 5 6— 6 6— 7 6— 8 7— 2 7— 3 7— 4 7— 5 7— 6	-0.000002 +0.000009 0.000000 -0.000084 +0.000200 -0.000017 -0.000001 +0.000001 +0.000002 -0.000024 +0.000074 -0.000097	-0.00004 +0.00029 -0.000125 +0.000277 -0.000287 +0.000094 +0.000010 0.000000 +0.000004 -0.000021 +0.000058 -0.000059	-0.000012 +0.000060 +0.000002 -0.000886 +0.002354 -0.001633 -0.000337 -0.000038 +0.000004 +0.000019 -0.000235 +0.000808 -0.001153	-0.00020 +0.000212 -0.001109 +0.002864 -0.003339 +0.001120 +0.000202 +0.000021 +0.000028 -0.000165 +0.000546 -0.000937 +0.000683
7— 7 7— 8 7— 9 8— 3 8— 4 8— 5 8— 6 8— 7 8— 8	+0.000041 +0.000007 +0.000001 0.000000 -0.0000006 +0.000021 -0.000035 -0.000011 -0.000002	0. 0000080. 000001 0. 0000000. 000003 +-0. 0000190. 00000190. 0000030. 000001	+0. 000497 +0. 000125 +0. 000017 +0. 000005 -0. 000050 +0. 000206 -0. 000428 +0. 000417 -0. 000117	-0. 000076 -0. 000013 -0. 000001 -0. 000023 +0. 000088 -0. 000194 +0. 000203 -0. 000045 -0. 000037 -0. 000009
9— 4 9— 5 9— 6 9— 7 9— 8 9— 9 9—10	-0.000001 +0.000004 -0.000011 +0.000014 -0.000011 +0.000001	+0.000001 -0.000003 +0.000004 0.000000 -0.000003 +0.000002	-0, 000010 +0, 000043 -0, 000117 +0, 000175 -0, 000123 +0, 000020 +0, 000006	+0.000013 -0.000032 +0.000043 -0.000003 -0.000041 +0.000022 +0.000005

Arg.	$\left({\stackrel{a'}{\scriptscriptstyle{\triangle}}} \right)^3 \frac{r'}{a'} \sin \left(f' + II' \right)$			
Aig.	sin.	6081		
i' i		-0. 040463		
0— 1	0. 2030405	+0. 4277100		
0— 2	-0.003162	-0.001314		
0— 3	-0.000076	+0.000079		
0 4	0. 000003	+0.000008		

For the computation of $a'\frac{r}{r'^2}H$ we have (page 63)

$\log h = 9.3949092n$	$\log l = 9.0364730$
$\log h_1 = 9.3939339n$	$\log l_1 = 9.0364229$
$\log P_0' = 9.1485126n$	
$\log P_{1}' = 9.9996414$	$\log Q_{1}' = 9.9998806$
$\log P_{2}' = 8.3697236$	$\log Q_{2}' = 8.3700426$
$\log P_{3}' = 6.9159173$	$\log Q_{3}' = 6.9162760$
$\log P_4' = 5.53591$	$\log Q_{4'} = 5.53629$
$\log P_{5}' = 4.1967$	$\log Q_5' = 4.1971$

There is then obtained

Arg.	$-\mathbf{a'} rac{r}{r'^2} \mathbf{H}$		Arg.	$-a'rac{r}{r'^2}\mathrm{H}$		
	cos.	sin.		cos.	sin.	
I+ 2 I+ I I 0 I- I I- 2 I- 3 I- 4 I- 5 2+ I 2 0 2- I 2- 2 2- 3 2- 4	+0.000027 +0.0001378 -0.0179504 +0.2477022 +0.0059715 +0.0002159 +0.000003 +0.000003 +0.000108 -0.0016835 +0.0232334 +0.0005600 +0.0000202 +0.0000009	-0. 0000004 -0. 0000080 -0. 0078673 +0. 1086316 +0. 0026188 +0. 0000041 -0. 0000002 -0. 0007380 +0. 0101892 +0. 00002456 +0. 0000089 +0. 0000004	3+ I 3 0 3- I 3- 2 3- 3 4 0 4- I 4- 2 5- I 5- 2 6- I 7- I	+0.0000007 -0.0001334 +0.0018387 +0.0000444 +0.0000016 -0.0000099 +0.0001363 +0.0000032 +0.00000097 +0.00000002 +0.00000007	0.0000000 -0.000585 +0.0008065 +0.0000195 +0.0000007 -0.0000043 +0.0000598 +0.0000014 +0.0000001 +0.0000001	

The logarithms of the factors proportional to the mass of Uranus are $\log \mu = 0.4249247 \qquad \qquad \log \left(\mu\alpha \sin J\right) = 7.9456112$

The following are the expressions for the forces:

Arg=i'g'+ig	$a\frac{d}{d}$	$rac{d\Omega}{dg}$	ar	$rac{d\Omega_{c}}{dr}$
	sin.	cos.	cos.	sin.
i' i	ll.	"	// +0. 10775	"
o— 1	—o. oo61113	+0.0004183	—o. 0143006	0. 0013396
0— 2	-o. oooo516	0. 0000564	+0.000019	+0.000092
o— 3	0, 000002	—o. 000002		
1+ 1	+0.00051	0, 00000	0. 00130	+o. 0000 t
1 0			+0. 02343	+0.00322
1 1	—0. 01934	+0.00810	o. o6oo3	—o. o2555
I— 2	o. oo346	+0.00440	0. 00261	—0. 00390
I — 3	0. 00029	+0.00038	-o. ooo18	o. 00026
1-4	-0.0002	+0.00003	u. 0000I	—0. 00002
2+ I	+0.00005	0.00001	-0. 00012	0,00002
2 0			+0.00359	+0.00187
2 I	—0. 01768	+0.01737	— 0. 03982	0. 03754
2 2	+0. 20276	0. 21971	+0, 20952	+o. 22679
2 — 3	+o. 01569	o. o1974	+0. 01092	+0.01455
2 4	+0.00104	-0.00144	+0.00055	+0.00084
2— 5	+0.00007	0.00010	+0.00003	+0.00005
3 0			+0.00045	+0.00034
3— 1	<u> </u>	+0.00336	o. oo676	-o. oo777
3— 2	+o. o3845	0. 05044	+0.04252	+0.05956
3— 3	0. 03021	+0.09161	-0. 03177	-0. 09452
3-4	0. 00275	+0.01093	-0. 00207	—o. oo882
3- 5	0. 00019	+0.00094	0. 00010	—o, ooo63
3— 6	-0,00001	+0.00007	0.00000	o. 00004
4 0			+0.00005	+0.00005
4— ī	0. 00036	+0.00046	—o. ooo84	-0.00116
4— 2	+0.00497	0.00803	+0.00576	+0.01062
4— 3	o. oo689	+0.02897	-0.00700	—o. o3216
4— 4	-0.00313	-0. 02854	—0. 00298	+0.02955
4-5	o. ooo76	-0.00428	— o. ooo68	+0.00364
4-6	0,00010	-0.00042	0.00008	+0.00031
4— 7	-0.00001	-0.00004	-0.00001	+0.00002
5— 1	-0.00004	+0,00006	0.00009	-0.00015
5— 2	+0.00053	0.00108	+0.00063	+0.00158
5— 3	-0.00081	+0.00573	—0. 00069	o. oo682
5— 4	-0.00218	-0. 01162	-0.00252	+0.01254
5 5	+0.00417	+o. oo688	+0,00423	-0.00720
5 6	+0.00087	+0.00127	+0.00077	0.00111
5— 7	+0.00011	+0.00014	+0.00009	-0.00010
5— 8	+0.00001	+0.00002	+0.00001	+o. ooooi

Arg=i'g'+ig	$a\frac{ds}{dt}$	$\frac{\Omega}{g}$	ar c	$rac{d\Omega}{dr}$
	sin.	cos.	cos.	sin.
i' i 6— 1 6— 2 6— 3 6— 4	0. 00000	+0.00001	-0. 00001	-0.00002
	+0. 00005	-0.00013	+0. 00006	+0.00021
	-0. 00004	+0.00091	+0. 00001	-0.00116
	-0. 00077	-0.00274	-0. 00097	+0.00310
6— 5	+0. 00242	+0.00349	+0. 00262	-0.00371
6— 6	-0. 00179	-0.00118	-0. 00185	+0.00127
6— 7	-0. 00044	-0.00026	-0. 00040	+0.00024
6— 8	-0. 00006	-0.00003	-0. 00005	+0.00003
7— I 7— 2 7— 3 7— 4 7— 5	0. 00000031 0. 00000 +-0. 000010. 00019 +-0. 00079	+0.0000064 -0.00002 +0.00013 -0.00050 +0.00095	0. 00000 +0. 00002 —0. 00026 +0. 00090	+0.00003 -0.00017 +0.00059 -0.00103
7— 6	-0.00122	-0. 00073	-0. 00130	+0.00077
7— 7	+0.00054	+0. 00007	+0. 00057	-0.00009
7— 8	+0.00016	+0. 00002	+0. 00015	-0.00001
7— 9	+0.00002	0. 00000	+0. 00002	0.00000
8— 3 8— 4 8— 5 8— 6 8— 7 8— 8 8— 9	0. 00000 -0. 00004 +0. 00019 -0. 00043 +0. 00045 -0. 00013 -0. 00004	+0.00002 -0.00008 +0.00019 -0.00005 +0.00005 +0.00001	+0.00010.0005 +0.000230.00048 +0.000480.000130.00004	-0. 00002 +0. 00009 -0. 00021 +0. 00023 -0. 00005 -0. 00004 -0. 00001
9— 4	-0.00001	-0.00001	-0.00001	+0.00001
9— 5	+0.00004	+0.00003	+0.00005	-0.00004
9— 6	-0.00011	-0.00004	-0.00013	+0.00005
9— 7	+0.00018	+0.00001	+0.00020	0.00000
9— 8	-0.00013	+0.00004	-0.00014	-0.00005
9— 9	+0.00002	-0.00002	+0.00002	+0.00003

Arg.	$a^2 \frac{c}{c}$	IQ IZ
	sin.	cos.
<i>i' i</i> o o	11	,, 0. 000357
0— I 0— 2	-0. 0017914 -0. 000028	+0.0037736 -0.000012

The expressions for the three multipliers, A, B, and C, have already been given (page 73). The resulting expressions for T and $\frac{1}{n}\frac{d\mathbf{R}}{dt}$ follow: in the latter the terms having the argument γ are alone retained, as the periodic perturbations of the latitude are quite insignificant.

Amorana Lilan Lia	7	ŗ.	Annual Had Lin		r.
$Arg = \varkappa_{\gamma} + i'g' + ig$	sin.	cos.	$Arg = \varkappa_{\gamma} + i'g' + ig$	sin.	cos.
и i' i п о— п	 0. 2141836	,, —0. 0000402	π i' i — I 3 ο	 0. 01077	,, +0. 01196
— I O O	-0.0213460	+0.0021751	o 3— I	+o. oo888	0.01008
0 0— 1	+0.0183339	-0, 0012549	I 3-2	0, 00484	+0.00648
I 0-2	-0.00312	0. 00049	— I 3— I	+o. 11826	0. 15634
— I O— I	+0.00031	-0.00022	o 3— 2	0. 11535	+0. 15132
0 0 2	+0.00015	+0.00017	I 3 3	+0.03893	-o. o5484
I 0 3	-0.00011	0, 00004	— I 3— 2	0. 09603	+0. 28318
— I I+ 2	1.0.00000	0.00006	0 3— 3	+0.09063	– 0. 27483
•	+0.00022	•	I 3—4	—0. 02840	+o. o8748
0 1+1	0. 00153 +0. 00178	0,00000	— r 3— 3	0.00470	+0. 02198
- 1 1+ 1	+0.02152	_0.00240	o 3 4	+0.00825	0. 03279
1 1-1	0. 01965	+0.00162	I 3 5	0.00340	+0.01289
_ I I O	-0. 09839	+0.00102	— 1 3— 4	-0.00023	+0.00140
0 1-1	+0.05802	-0, 02430	0 3-5	+0.00057	0. 00282
I I-2	+0.02129	0. 00989	1 3— 6	-0.00024	+0.00126
	o. oo867	+0.01236	- 1 3-5	0.00000	+0.00008
0 I-2	+0.01038	—0. 01320	o 3— 6	+0.00003	-0.00021
1 1-3	0.00333	+0.00442	1 3— 7	0.00002	+0.00010
_ i _ i _ 2	-0.00040	+0.00058			
o 1— 3	+0.00087	-0.00114	— I 4+ I	+0.00003	0,00002
I I—4	0.00038	+0.00050	I 4-I	+0.00001	-0.00004
— I I— 3	0. 00002	+0.00003	- I 4 0	-0.00130	+0.00169
o I— 4	+0.00006	_0.0008	0 4— I	+0.00108	0, 00138
I I-5	-0.00004	+0.00003	I 4— 2	-0.00061	+0.00100
ľ			- I 4 I 0 4 2	+0.01539 0.01491	0. 02530 +0. 02409
— I 2+ 2	+0.00003	-0.00001	·	+0.00518	—0. 00973
0 2+ 1	0, 00014	+0.00002	I 4-3 I 4-2	-0.02141	+0.08951
I 2 0	+0.00012	+0.00002	0 4—3	+0.02067	o. o8691
- 1 2+ I	+0.00249	-0.00090	1 4-4	o. oo635	+0.03003
I 2— I — I 2 0	0,00050	-0.00111 +0.06152	- I 4-3	-0. 00862	0. 08964
- I 2 0 0 2- I	-0.06519	-0.05211	0 4—4	+0.00939	+0.08562
1 2-2	+0.05304 - 0.02517	_	I 4— 5	-0.00319	0.02703
_ I 2— I	+0.61758	+0.02927 —0.66899	— I 4— 4	-0.00191	-0.00950
0 2— 2	-o. 60828	+0.65913	0 4-5	+0.00228	+0.01284
I 2~- 3	+0. 19461	-0. 21063	I 4—6	0.00083	-0.00487
_ i 2— 2	+0.02296	-o. o33o7	— I 4— 5	-0.00021	o. 0007 I
0 2— 3	-0.04707	+0.05922	0 4—6	+0,00030	+0.00126
I 2— 4	+0.02020	-0. 02462	I 4 7	-0.00011	-0.00054
— I 2— 3	+0.00101	-0.00169	<u>- 1 4- 6</u>	-0.00002	0. 00005
0 2-4	-0.00312	+0.00432	0 4 7	+0.00003	+0.00012
I 2 5	+0.00159	0. 00209	ı 4— 8	-0.00001	0. 00005
— I 2— 4	+0.00004	-0.00009			
0 2—5	0.00020	+0.00029	- I 5 0	-0.00013	+0.00020
1 2— 6	+0.00011	-0.00014	0 5 1	+0.00011	-0.00017
	i		I 5— 2	—0.00006	+0.00013
— I 3+ I	+0.00028 +0.00007	0.00017 0.00026	- I 5- I 0 5- 2	+0.00165	0.00348
1 3— 1		0.00020	0 5— 2	-0. 00159	+0.00324

A	т	1	A	Т	
$\mathbf{Arg} = \varkappa_{\gamma} + i'g' + ig$	sin.	cos.	$Arg = \varkappa \gamma + i'g' + ig$	sin.	cos.
и i' i I 5— 3	+0.00055	,, —0. 00144	κ i' i 1 7— 3	+0.00001	,, —0, 00005
— I 5— 2	-0.00247	+0.01781	- I 7- 2	+0.00003	+0.0004I
	+0,00243	_0.01719	0 7— 3	-0.00002	-0.00038
0 5— 3 1 5— 4	-0.0006I	+0.00636	I 7—4	+0.00001	+0.00014
	-0.00661	—0. 03602	_ I 7— 4	—o. ooo62	-0.00159
— I 5— 3	+0.00654		, , ,	+0.00057	+0.00150
0 5-4	—0. 00245	+0.03486	1 ' 1	-0.0002I	_0.00130 _0.00052
I 5— 5	1	-0.01173	'	+0.00246	+0.00301
— 1 5— 4	+0.01282	+0.02214	1 1		0. 00285
0 5-5	-0.01251	—0, 02064	0 7— 5	0.00237 +0.00082	+0.00095
1 5— 6	+0.00399	+0.00641	1 7— 6	. 1	
— I 5— 5	+0.00211	+0.00298	— I 7— 5	—o. oo383	0.00232
0 5—6	-0.00261	-0.00381	0 7—6	+0.00366	+0. 00219 0. 00066
I 5-7	+0.00098	+0.00140	1 7— 7	0.00120	
— r 5— 6	+0.00023	+0.00026	<u> </u>	+0.00181	+0.00032
0 5-7	—o, ooo33	-0.00042	0 7-7	-0.00162	-0.0002I
1 5— 8	+0.00013	+0.00017	1 7 - 8	+0.00047	+0.00007
— I 5— 7	+0.00004	+0.00002	— I 7— 7	+0.00039	+0.00004
o 5— 8	—o. oooo3	0. 00005	0 7-8	0.00047	—0. 0000 6
1 5-9	+0.00001	+0.00002	1 7— 9	+0.00017	+0.00003
— r 6— о	-0.00002	+0.00002	— I 7— 8	+0.00002	+0.00001
о 6— і	+0.00001	0.00002	0 7— 9	0.00006	o. 0000I
I 6— 2	o. oooo1	0. 00002	I 7—10	+0.00004	+0.00001
— 1 6— 1	+0.00016	-0.00043	<u> </u>	0,00013	0. 00026
0 6— 2	-0.00015	+0.00040	0 8-4	+0.00012	+0.00023
1 6-3	+0.00004	-0, 00020	ı 8— 5	0, 00005	0. 00008
<u> </u>	0.00012	+0.00281	— 1 8— 4	+0.00060	+0.00060
0 6-3	+0.00012	-0.00273	o 8— 5	—o. ooo57	-o. ooo57
ı 6— 4	+0.00002	+0.00106	r 8 6	+0.00020	+0.00021
— 1 6— 3	-0. 00240	—0. 00849	— 1 8 <u>—</u> 5	0,00136	0.00068
0 6-4	+0.00231	+0. 00822	o 8 6	+0.00129	+0.00063
1 6-5	0.00093	-0.00291	ı 8— 7	-0. 00044	0.0002I
<u> </u>	+0.00748	+0.01089	— 1 8— 6	+0.00144	+0.00018
o 6 5	0. 00726	-0.01047	0 8— 7	-0.00135	0.00015
ı 6 6	+0.00249	+0.00343	r 8— 8	+0.00044	+0.00003
— I 6— 5	-0.00569	0. 00399	_ I 8— 7	0, 00043	+0.00012
o 6 6	+0.00537	+o. oo354	o 8 8	+0.00039	-0.00012
ı 6— 7	-0.00168	-0.00106	ı 8— 9	0.00011	+0.00005
- I 6 6	0.00110	-0.00065	I 8 8	<u>_0.00005</u>	+0.00001
0 6 7	+0.00132	+0.00078	0 8-9	+0.00011	0. 00003
1 6-8	-0.00047	0. 00028	ı 8—10	-0.00007	+0.00002
_ I 6— 7	-0.00013	-0.00007		+0.00008	- +-0. 00006
0 6-8	+0.00018	+0,00010	- I 9- 4	—0. 00012	0.00009
1 6-9	-0.0007	_0.00003	0 9— 5 1 9— 6	+0.00009	+0.00007
ļ					—o. oooog
o 7 I	+0.00000094	0.00000192	— I 9— 5	o. 00036 b. 00033	+0.00012
- I 7- I	+0.000012	0,000053	0 9—6	-0.00012	-0.00012
D 7-2	-0.0001	+0.00005	I 9— 7	-0.0012	- 0.00009

$Arg = n\gamma + i'g' + ig$	ר	· .	Arc - 101 Life Lie	1	Γ.
Aig—n/+vy +vy	sin.		$Arg = n\gamma + i'g' + ig$	sin.	cos.
и i' i — I 9— 6 0 9— 7 I 9— 8	+0. 00057 0. 00054 +0. 00018	+0.00003 0.00003 +0.00001	π i' i - 1 9- 7 0 9- 8 1 9- 9	,,, -0.00043 +0.00039 -0.00013	+0.00009 -0.00012 +0.00009

$$\frac{1}{n}\frac{dR}{dt} = -0^{\prime\prime}.0008950 \cos(-\gamma) - 0^{\prime\prime}.0019103 \sin(-\gamma)$$

The logarithms of the integrating factors are contained in the following table:

Arg.	$\log \frac{n}{i'n'+in}$	Arg.	$\log \frac{n}{i'n'+in}$	Arg.	$\log \frac{n}{i'n'+in}$	Arg.	$\log \frac{n}{i'n'+in}$
i' i 0- I 0- 2 0- 3 I+ 2 I+ I I 0 I- I I- 2 I- 3 I- 4 2+ I 2 0 2- I 2- 2 2- 3 2- 4 2- 5	o. ooooon g. 69897n g. 69897n g. 52388n g. 66934 g. 94264 o. 85020 o. 06610n g. 73076n g. 54381n g. 41355n g. 89198 o. 54917 o. 14411n g. 76507n g. 56581n g. 42974n g. 3263n	i' i 3+ 1 3 0 3- 1 3- 2 3- 3 3- 4 3- 5 3- 6 4 0 4- 1 4- 2 4- 3 4- 4 4- 5 4- 6 5 0 5- 1	9. 84662 0. 37308 0. 23925n 9. 80233n 9. 58898n 9. 44655n 9. 33947n 9. 2537n 0. 24814 0. 36126n 9. 84307n 9. 61346n 9. 46404n 9. 35308n 9. 26478n 0. 15123 0. 53156n	i' i 5- 2 5- 3 5- 4 5- 5 5- 6 5- 7 6- 1 6- 2 6- 3 6- 4 6- 5 6- 6 6- 7 7- 1 7- 2 7- 3 7- 4	9. 88805n 9. 63940n 9. 48227n 9. 36713n 9. 27621n 9. 20107n 0. 81568n 9. 93822n 9. 66698n 9. 50129n 9. 38165n 9. 28795n 9. 21092n 1. 9325n 9. 9950n 9. 6964n 9. 5212n	i' i 7-5 7-6 7-7 7-8 8-3 8-4 8-5 8-6 8-7 8-8 8-9 9-4 9-5 9-6 9-7 9-8 9-9	9. 3967n 9. 3000n 9. 2210n 9. 1542n 9. 7280n 9. 5421n 9. 4122n 9. 3124n 9. 2313n 9. 1630n 9. 1040n 9. 5640n 9. 4284n 9. 3252n 9. 2419n 9. 1720n 9. 1119n

In the integration we put

$$k_0 = + \circ.$$
 $k_1 = - \circ.$ $k_2 = + \circ.$ $k_3 = + \circ.$ $k_4 = + \circ.$

Arg=i g'+ig		$\frac{\delta z}{dt}$	$rac{1}{n}rac{d u}{dt}$		
	208.	sin.	sin.	cos.	
i' i	"	"	п		
1 —0	-0.0213 +0.0021751nt	—0.0022 —0.0213460 <i>nt</i>	+0.0208 -0.0010875 <i>nt</i>	0.0019 0.0106730nt	
0— 2	-0.0004 +0.0000524 <i>nt</i>	0, 0000 0, 0005148nt	+0.0009 -0.0000524nt	0.0000 0.0005148nt	
0- 3	+0.0000018nt	o. 0000186nt	-0. 0000027nt	-0. 0000279nt	

$ ext{Arg} = i'g' + ig$	$\frac{d\delta}{d}$		$\frac{1}{n}\frac{d}{d}$	$\frac{\nu}{lt}$
	cos.	sin.	sin.	cos.
i' i	"	11	"	11
1+1	-0. 0120	+0.0007	0. 0069	-0.0003
I O	0.04146	-o. oo386	-0.00175	0.00024
1— 1	+0.7753	+0. 3305	-0. 3422	+o. 1458
I— 2	+0.0111	-0.0016	0. 0124	+0.0007
I — 3	+0.0004	0.0000	—o. ooo6	0.0000
2+ 1	-0.0003	+0.0001	-0.0002	0, 0000
2 0	0. 00293	+0.00051	+0, 00036	-o. ooo81
2— І	+0. 291 8	+0.2754	<u> </u>	+0.1155
2— 2	+o. 5838	+0.6315	— 0. 4000	+0.4325
2— 3	+0.0230	+0.0268	-0.0247	+0.0291
2 4	+0,0010	+0.0011	—o. 0016	+0.0018
3 0	0.0002	+0.0003	0, 0000	0. 0001
3 I	+o. o381	+0.0421	o. o138	+0. 0156
3— 2	+0. 1475	+0. 1 968	o. o955	+0. 1264
3-3	—o. 0287	0, 0910	+0. 0216	-0. 0710
3 4	0.0015	-0.0062	+0.0018	<u></u> 0. oo68
3— 5	0.0001	0.0004	+0.0001	0. 0006
4 1	+0.0045	+0.0056	-0,0012	+0.0017
4 2	+0.0272	+0.0452	—о. 0168	+0.0273
4- 3	-0.0073	-o. o339	+o. 0056	0.0256
4— 4	0.0019	+0.0164	+0.0018	+0.0140
4 5	0. 0004	+0.0016	+0,0003	+0.0018
5— I	+0.0006	+0.0008	-0.0001	+0.0001
5— 2	+ 0. 0046	+0.0099	0. 0027	+0.0056
5 — 3	0. 0009	-0.0078	+0.0007	-o. oo58
5— 4	0.0015	十0.0075	+0.0011	+0.0062
5- 5	+0.0017	-0. 0027	-0.0014	-0.0023
5— 6	+0.0003	0. 0004	-0,0002	-0.0004
6— т	+0.00007	+0.00016	0.00001	0.00000
6— 2	+0.0009	+0.0026	—o. ooo5	+0.0014
6— 3	0,0000	-0.0013	0,0000	0.0010
6 4	—0. 0006	+0.0019	+0.0004	+0.0015
6 5	+0.0011	-0.0016	<u> </u>	-0.0013
6— 6	— 0. 0006	+0.0004	+0.0005	+0.0003
6— 7	0.0001	+0.0002	+0.0001	0.0000
7— I	+0.000081	+0.000165		_
7— 2	+0.0010	+0.0045	—o. ooo5	+0.0023
7— 3	0.0000	-0.0002	0,0000	-0,0002
7— 4	0, 0002	+0.0004	+0.0001	+0,0004
7— 5	+0.0004	-0.0005	0.0003	-0.0004
7— 6	—o. ooo5	+0.0003	+0.0004	+0.0003
7 7	+0.0002	-0.0001	-0.0002	0.0000
10			L	

Arg=i''g''+ig	$n\delta$	Z		ν		u 8 i
	sin.	cos.	cos.	sin.	sin.	cos.
i'' i o— o	"	u	-0. 0353 -0. 0000263nt	"	11	+0.0000648nt
0— I	0.0000	0.0000	+0.0101	+0.0008		
1	-0.0021751 <i>nt</i>	-0. 0213460 <i>nt</i>	0.0010875 <i>nt</i>	+0.0106730nt	-0.0019103 <i>nt</i>	-0. 0008950nt
O— 2	+0.0002	-0.0001	+0.0001	0.0000		
	0. 0000262nt	-0.0002574nt	0. 0000262nt	+0.0002574nt	0. 0000461 <i>nt</i>	-0. 0000216nt
o— 3	-0.0000006 <i>nt</i>	-0.0000062nt	—0. 0000009nt	+0.0000093nt	—0.0000017 <i>nt</i>	-0. 0000008nt
1+ 1	-0. 0105	0.0006	+0.0060	0.0003		
1 0	0. 2936	+0.0273	+0.0124	—o. ∞17		
т— т	-0. 9028	+0. 3848	— 0. 3985	—о. 1698		
I— 2	-o. oo6o	-0.0009	—о. 0067	0, 0004		
I— 3	0.0001	0,0000	0. 0002	0,0000		
2+ I	0,0002	-0.000I	+ 0.0002	0.0000		
2 0	—0. 0104	-0.0018	-0.0013	-0.0029		
2— I	—о. 406 6	+0. 3837	—o. 1686	-0. 16 <u>10</u>		
2— 2	o. 3399	+o. 3676	0. 2329	—о. 2518		
2— 3	0.0085	+0.0099	-0. 009 I	0.0107		
2 — 4	-0.0003	+0.0003	0.0004	0.0005		
3 0	—o. ooo5	—o. ooo7	0.0000	0.0002		
3 - 1	o. o661	+0.0730	-0. 0239	-0.0271		
3— 2	-o. o936	+0. 1249	0.0606	0.0802		
3-3	+0.0111	—o. o353	+0.0083	+0.0276		
3-4	+0.0004	0.0017	+0.0005	+0.0019		
4— I	_o. o1o3	+0.0129	-0.0028			
		· -		-0. 0039		
4— 2	0. 0190	+0.0315	—0. 0117 +0. 0023	0.0190 +0.0105		
4-3	+0.0030 +0.0006	-0. 0139				
4-4	+0.0001	+0.0048	+0.0005	-0.0041		
4— 5		+0.0004	+0.0001	0. 0004		
5— 1	0. 0020	+0.0027	-0.0003	-0.0003		
5— 2	—o. oo36	+0.0076	-0.0022	-0.0043		
5— 3	+0.0004	0.0034	+0.0003	+0.0025		
5— 4	+0.0005	+0.0023	+0.0003	-0.0019		
5— 5	-0.0004	0. 0006	0. 0003	+0.0005		
6— 1	—o. ooo5	+0.0010	0. 0001	0.0000		
6— 2	-o. ooo8	+0.0023	0. 0004	0.0012		
6— 3	0,0000	-0.0006	0,0000	+0.0005		
6 4	+0.0002	+0.0006	+0.0002	0.0007		
6— 5	—0.0003	—0. 0004	-0.0003	+0.0004		
6— 6	+0.0001	+0.0001	+0.0001	1000.0-		
7 1	0,0069	+0.0141	`			
7— 2	0, 0010	+0.0045	-0.0005	0.0022		
7— 3	0, 0000	0.0001	0.0000	+0.0001		
7— 4	+0.0001	+o. 0001	0, 0000	+0.0001		
7 5	-o. ooo1	-0.0001	0.0001	+0.0001		
7— 6	+0.0001	+0.0001	+0.0001	-0.0001		

CHAPTER V.

PERTURBATIONS OF SATURN BY NEPTUNE.

In determining the action of Neptune on our two planets it will not be necessary to go beyond terms of the first order with respect to disturbing forces. Following the previous custom, no accents will be given to quantities pertaining to Saturn, and a single one to those belonging to Neptune.

The elements of Neptune employed are the following: *

Epoch 1850, Jan. o.o, Greenwich M. T.

These elements include the effect of the 4000-year inequality produced by the action of Uranus. Also, $\log a'$ includes the constant term of the perturbations of the logarithm of the radius vector. As the similarly corrected $\log a$ of Saturn is 0.9796819, we have here $\log \alpha = 9.5015405$.

The coefficients of the terms of the developments of the reciprocal of the distance between Saturn and Neptune and its odd powers are then functions of the following six elements:

$$\log \alpha = 9.5015405$$
 $J = 0.57 51.54$
 $e = 0.05605688$ $II = 192 9 3.80$
 $e' = 0.0084962$ $II' = 145 19 5.10$

 Π and Π' are measured from the ascending node of the orbit of Neptune on that of Saturn. The developments will be made first in terms of the eccentric anomaly of Saturn.

^{*}An Investigation of the Orbit of Neptune, with General Tables of its Motion. By Prof. S. Newcomb, p. 76.

The values of the auxiliary constants are

 $\mathbf{D} = 1.1002373 - [8.2302547] \cos \varepsilon' + [5.85845] \cos^3 \varepsilon' + [8.7486289] f \cos \mathbf{F}$

The circumference will be divided into twelve parts with reference to the mean anomaly of Neptune. For five points of the division we nave

We get the following table of values of D, log f, and F:

g'	D	$\log f$		F —	g'
0			0	,	,,
0	1. 1080847	9. 8038257	313	57	23.41
30	1. 1201363	9.8067290	313	58	o. 76
60	1. 1268758	9. 8081619	313	44	49. 23
90	1. 1265486	9.8077789	313	23	27.53
120	1. 1193373	9. 8059257	313	0	32.53
150	1. 1072172	9. 8033118	312	41	4. 15
180	1. 0933864	9. 8006159	312	28	10. 54
210	1.0814585	9. 7983207	312	24	18. 3 5
240	1.0745845	9. 7968135	312	31	3 5 · 97
270	1.0746535	9. 7965143	312	50	18. 03
300	1.0817412	9. 7977580	313	16	27. 68
330	1.0939957	9. 8004464	313	41	50. 59
s	6. 6040099	8. 8131007	1878	58	59. 36
s′	6. 6040098	8. 8131011	1878	58	59. 41

Employing the same procedure as in the preceding chapter, we have the following table of values of $\log \frac{1}{6} \alpha_i^{(n)}$:

	$\log \frac{1}{6} \alpha_0^{(1)}$	$\log \frac{\mathbf{I}}{6} \alpha_1^{(1)}$)	log	$\frac{1}{6} \alpha_2^{(1)}$	log	$g \frac{1}{6} \alpha_3^{(1)}$	1	og $\frac{1}{6}\alpha_4^{(1)}$	$\log \frac{1}{6} \alpha_5^{(1)}$
(0)	9. 2315543	8. 435723	31	7. 81	22246	7.	2335367		5. 6756563	6. 1298182
(1)	9. 2288883	8. 430807	73	7. 80	50982	7.	2242096	6	6. 6641326	6. 1161000
(2)	9. 2273807	8. 427832	28	7. 80	06822	7.	2183586	6	5. 6568491	6. 1073854
(3)	9. 2273991	8. 427530	10	7.80	00639	7.	2174261	6	6. 6556030	6. 1058260
(4)	9. 2289570	8. 430258	34	7.80	39425	7.	2224499	6	6. 6617699	6. 1131350
(5)	9. 2316935	8. 435644	ļ.2	7.81	19314	7.	2330302	6	5. 6749369	6. 1288863
(6)	9. 2349179	8. 442342	21	7.82	20415	7.	2465368	6	6. 6918337	6. 1491699
(7)	9. 2377498	8. 448288	So	7.83	10455	7.	2585846	6	6. 7069196	6. 1672911
(8)	9. 2393674	8. 451501	7	7.83	58261	7.	2649249	6	6, 7148166	6. 1767431
(9)	9. 2392929	8. 451013	33	7.83	49315	7.	2636260	6	5. 7131142	6. 1746376
(10)	9. 2375690	8. 447253	32	7.82	91720	7.	2558765	6	6. 7033784	6. 1629176
(11)	9. 2347227	8. 441628	39	7. 82	08196	7.	2448086	6	6. 6896001	6. 1464315
s	5. 3997463	80. 634911	13	76.90	38889	7 3.	4416834	70	0. 1043040	66. 8391692
S′	5. 3997463	80. 634911	8	7 6. 90	38901		4416851	70	0. 1043064	66. 8391725
	$\log \frac{1}{6} \alpha_6^{(1)}$	$\log \frac{\mathbf{r}}{6} \alpha_{\gamma}^{(1)}$	log	$\frac{1}{6}\alpha_8^{(1)}$	$\log \frac{1}{6}$	$\alpha_{0}^{(3)}$	$\log \frac{1}{6} \alpha_1^{(3)}$,	$\log \frac{1}{6} \alpha_2^{(3)}$	$\log \frac{1}{6} \alpha_3^{(3)}$
(0)	5. 591837	5.05938	4	. 5309	9. 319	0254	8. 978356	6	8. 5691675	8. 132783
(1)	5. 575927	5.04127	4	. 5106	9. 310	3118	8. 967616	6	8. 5562958	8. 117751
(2)	5. 565782	5. 02970	4	4975	9. 305	3264	8. 961308	8	8. 5485976	8. 108644
(3)	5. 563909	5.02752	4	. 4950	9. 305	2807	8. 960973	5	8. 5479578	8. 107696
(4)	5. 572360	5.03713	4	. 5058	9. 310	3224	8. 9670 7 0	6	8. 5551646	8. 116027
(5)	5. 590696	5. 05803	4	. 5294	9. 319	3733	8. 978508	1	8. 5691124	8. 132519
(6)	5. 614363	5.08510	4	. 5599	9. 330	1657	8. 992424	.9	8. 5863178	8. 153057
(7)	5. 635518	5. 10926	4	. 5871	9. 339	6806	9.004736	ī	8. 6015746	8. 171300
(8)	5. 646523	5. 12183	4	. 6012	9. 345	0617	9.011548	6	8. 6098959	8. 181151
(9)	5.644014	5. 11893	4	· 5979	9- 344	7009	9. 010816	8	8.6087730	8. 179631
(10)	5.630312	5. 10324	4	. 5802	9. 338	8572	9.003146	2	8. 5991772	8. 168084
(11)	5.611122	5. 08134	4	. 5556	9. 329	4120	8. 991205	7	8. 5846085	8. 150851
S	63. 621177	60. 43638		. 2755	5.948		3. 913855	- 1	1. 4683206	88. 85974
S'	63. 621186	60. 43635	57	. 2756	5.948	7503	3. 913856	8	1.4683221	88. 85975

	$\log \frac{\mathbf{I}}{6} \alpha_4^{(3)}$	$\log \frac{1}{6} \alpha_5^{(3)}$	$\log \frac{1}{6} \alpha_6^{(3)}$	$\log \frac{1}{6} \alpha_7^{(3)}$	$\log \frac{1}{6} \alpha_8^{(3)}$	$\log \frac{1}{6} \alpha_0^{(5)}$	$\log \frac{1}{6} \alpha_1^{(5)}$
(0)	7. 6817331	7. 2214931	6. 754952	6. 28383	5. 8093	9. 48476	9. 30965
(1)	7. 6645296	7. 2021118	6. 733389	6. 26008	5. 7834	9. 46928	9. 29264
(2)	7. 6540062	7. 1901681	6. 720023	6. 24529	5. 7671	9. 46037	9. 28273
(3)	7. 6527477	7. 1885985	6. 718141	6. 24309	5. 7646	9. 46015	9. 28229
(4)	7. 6622091	7. 1991932	6. 729870	6. 25595	5.7785	9. 46903	9. 29196
(5)	7. 6812582	7. 2208070	6. 754053	6. 28270	5.8079	9.48524	9. 31000
(6)	7. 7051480	7. 2480577	6. 784671	6. 31670	5.8452	9. 50472	9. 33183
(7)	7.7263934	7. 2723143	6. 81 1943	6. 34698	5. 8786	9. 52192	9. 35114
(8)	7. 7377828	7. 2852466	6. 826422	6. 36302	5.8962	9. 53158	9. 36188
(9)	7. 7358646	7. 2829285	6. 823703	6. 35990	5. 8926	9. 53081	9. 36083
(10)	7. 7223540	7. 2674493	6. 806251	6. 34047	5.8712	9. 52018	9. 34882
(11)	7. 7024422	7. 2448507	6. 780961	6. 31247	5.8405	9. 50324	9. 33000
S	86. 1632332	83.4116080	80. 622189	77. 80526	74. 9675	6. 97064	5. 9268
S/	86. 1632357	83. 4116108	80, 622190	77. 80522	74. 9675	6. 97064	5. 92690
	$\log \frac{1}{6} \alpha_2$	$\log \frac{1}{6} \alpha_3^{(5)}$	$\log \frac{1}{6} \alpha_4^{(5)}$	$\log \frac{1}{6} \alpha_5^{(5)}$	$\log \frac{1}{6} \alpha_6^{(5)}$	$\log \frac{1}{6} \alpha_7^{(5)}$	$\log \frac{1}{6} \alpha_8^{(8)}$
(0)	9. 02547	8. 68717	8. 31656	7. 92414	7. 51682	7.0977	6. 6697
(1)	9. 00651	8. 66618	8. 29338	7. 89886	7. 48884	7. 0675	6. 6373
(2)	8. 99537	8. 65374	8. 27969	7. 88403	7-47342	7.0507	6. 6191
(3)	8. 99465	8. 65271	8. 27829	7. 88227	7. 47089	7. 0478	6. 6158
(4)	9.00531	8. 66440	8. 29097	7. 89581	7. 48486	7. 0630	6. 6322
(5)	9. 02559	8. 68717	8. 31610	7. 92390	7. 51477	7. 0955	6. 6673
(6)	9. 05044	8. 71511	8. 34757	7. 95831	7. 55430	7. 1383	6. 7134
(7)	9.07237	8. 73990	8. 37508	7. 98894	7. 58678	7. 1738	6. 7519
(8)	9. 08445	8. 75340	8. 39001	8. 00521	7. 60417	7. 1928	6. 7725
(9)	9. 08307	8. 75168	8. 38800	8.00303	7. 60221	7. 1904	6. 7697
(10)	9. 06933	8. 73606	8. 37052	7. 98343	7. 58088	7. 1671	6. 7444
(11)	9. 04815	8. 71237	8. 34427	7. 95462	7. 54964	7. 1331	6. 7077
S	4. 23037	92. 20988	89. 99532	87. 65093	85. 21445	82. 7096	80. 1513
S'	4. 23034	92. 21001	89. 99512	87.65162	85. 21313	82. 7081	80. 1499

The values of the coefficients A for the development of $[D-f\cos{(\varepsilon-F)}]^{-\frac{1}{2}}$ are

	A (c)	A ₁ (c)	$A_1^{(s)}$		A	(c) 3		A ₂ ^(s)	A ₃ ^(c)	A ₃ ^(s)	A(c)
	8	8	п			8		В	В	8	8
(0)	+ 17043325	+ 1893009	+ 1963	249	2	23633		48539	— I 2 7497	+114274	— 4726 1
(1)	16939019	1872055	1940	٠	2	23018		37993	124727	111914	46026
(2)	16880322	1851866	1934		2	27631		31345	124321	108992	45205
(3)	16881035	1838527	1944		3	35425	1	30055	126060	106427	44963
(4)	16941700	1837025	1969	346	4	14214	6	35174	129654	105093	45453
(5)	17048788	1848624	2004		!	52362	(646415	134662	105412	46691
(6)	17175838	1869708	2042	2604		58556	6	61219	140131	107172	48420
(7)	17288199	1893150	2072	2893		61303	•	74934	144444	109700	50090
(8)	17352713	1911637	2084	1238		59085	(582662	145856	112243	51087
(9)	17349737	1920786	2071	1478		51548	6	81858	143575	114266	51068
(10)	17281004	1919800	2039	9070		40623	(573571	138437	115436	50144
(11)	+ 17168119	+ 1909907	+ 1998	3787	— ;	30088	+ 6	661257	132428	+115492	- 48731
s	+1.02674902	+11283045	+12033	3193	2	53742	+39	932510	—805896	+663210	-287570
S'	+1.02674897	+11283049	+12033	3195	-2	53744	+39	932512	805896	+663211	-287569
	A.(*)	A ₅ ^(c)	A ₅ ^(s)	$\mathbf{A}_6^{(c)}$		A ₆		A ₇ ^(c)	A ₇ ^(s)	A ₈ ^(c)	A(*)
	8	8	8	8		8					8
(0)	— 3449	— 8628	—10362	+ 42	26	— 38	884	+ 907	701	+ 336	+ 49
(1)	3325	8369	10032	40	07	3	744	869	673	321	47
(2)	3964	8012	9989	48	81	30	648	864	633	310	55
(3)	5072	7671	10196	61	14	36	612	886	592	305	70
(4)	6359	7451	10623	77	73	30	655	933	562	308	88
(5)	7615	7411	11230	93	36	3	783	1002	550	321	107
(6)	8644	7544	11911	10	78	39	971	1076	558	341	126
(7)	9175	7795	12462	110	60	4	162	1148	581	361	137
(8)	8910	8101	12651	113	35	4	283	1172	615	376	135
(9)	7766	8401	12366	25	89	4	293	1140	655	378	118
(10)	6070	8630	11717	7	67	4	199	1065	689	369	91
(11)	- 4444	8719	—1 0966	+ 5	55	4	046	+ 977	— 707	+ 353	+ 65
s	-37396	-48366	67253	+46	60	23	640	+6017	—3758	+2040	+544
s′	-37307	— 48366	67252	+460	61	23	640	+6022	—3758	+2039	+544

For the development of $\left[\mathrm{D}\!-\!f\cos\left(\epsilon\!-\!\mathrm{F}\right)\right]^{-\frac{3}{2}}$ they are

	$\mathbf{A_0^{(c)}}$	A ₁ ^(c)	A ₁ (a))	A ₂ ^(c)	1	A ₂ (*)	A ₃ ^(c)	A ₃ ^(*)	A ₄ ^(c)
	7	8	8		7		7	7	7	7
(0)	+ 2084613	+ 660368	3 + 6848	3712 -	- 13504	+	370578	-101099	+ 90614	47927
(1)	2043204	644358	8 6680	254	12980		359760	97612	87584	46068
(2)	2019884	632536	4 6608	3250	15464		353331	96567	84660	44910
(3)	2019671	627933	0 6642	2298	19824		352592	97915	82665	44669
(4)	2043254	632306	I 6778	3509	2 4934	1	358191	101476	82253	45499
(5)	2086283	645226	9 6996	5058	29936		369566	106840	83633	47376
(6)	2138778	663523	9 7248	3813	34029		384257	112994	86418	49927
(7)	2186153	681762	5 7464	1919	36142		397915	118145	89726	52388
(8)	2213409	694148	4 7568	3230	35119		405766	120269	92552	53861
(9)	2211571	697079	7 751	7678	30624		405075	118327	94173	53815
(10)	2182013	690476	733	3733	23921		396633	113099	94308	52384
(11)	+ 2135069	+ 677000	6 + 708	5054 -	— 1 74 66	+	383848	106665	+ 93024	— 50193
s	+1. 2681951	+3973359	6 +42386	5247 -	-146971	+2	268756	-645504	+530805	-294508
S'	+1. 2681951	+3973361	' ' "		146972	1	268756	-645504	+530805	-294509
	1	, , , , , ,								
	A ₄ ^(s)	A ₅ (c)	A ₅ (s)	A ₆ (c)	A(s))	$\mathbf{A}_{7}^{(e)}$	A ₇ ^(*)	A ₈ ^(c)	A(s)
	7	8	8	8	8		8	8	8	
(0)	— 3498	-106561	127975	+ 620	3 - 56	540	+ 15211	-11755	+ 6378	+ 936
(1)	3328	102018	122297	5844	4 53	807	14387	11147	6010	873
(2)	3939	96950	120862	686	7 520	032	14190	10397	5760	1018
(3)	5039	92813	123369	876	3 51	517	14555	9720	5669	1296
- (4)	6365	90839	129514	1111	3 52	525	15443	9302	5774	1648
(5)	7726	91581	138772	1362	9 55	101	16803	9234	6093	2041
(6)	8913	94724	149561	1595	58	782	18427	9506	6567	2423
(7)	9596	99273	158714	1740	7 62.	475	19838	10036	7070	2680
(8)	9394	104003	162417	1717.	4 64	817	20427	10718	7410	2666
(9)	8183	107804	158679	1495	5 64	935	19861	11406	7456	2321
(10)	6341	109779	149055	1150	4 62	968	18384	11903	7219	1774
(11)	— 4577	109364	—137554	+ 821	2 - 59	828	+ 16637	-12035	+ 6812	+ 1253
1 ' '				1	1			1	1	1
s	-38450	602856	839384	+688 ₁	2 -347	664	+102082	-6358r	+39108	+10465

For the development of $[\mathrm{D}\!\!-\!\!f\cos\left(\epsilon\!\!-\!\!\mathrm{F}\right)]^{-\frac{5}{2}}$ they are

	A ₀ (c)	A ₁ ^(c)	$\mathbf{A}_{1}^{(s)}$		$\mathbf{A_2^{(c)}}$		$\mathbb{A}_2^{(s)}$		A ₃ ^(c)	A ₃ ^(*)	A(c)
	6	6	5		5		5		5	Б	6
(0)	+ 30532	+14161	+146	86	386		+1059	7	- 3623	+ 3248	— 206 7
(1)	29463	13619	141		366		1014		3451	3096	1960
(2)	28865	13259	138	52	433		988		3388	2970	1897
(3)	28850	13159	139	20	554		986	2	3434	2900	1886
(4)	29446	13360	143	323	703		1009	9	3587	2908	1936
(5)	30566	13842	150	009	856	- 1	1057	2	3832	2999	2044
(6)	31968	14496	158	}	991		1118	8	4122	3152	2192
(7)	33260	15137	16	574	1069		1176	5	4375	3323	2333
(8)	34008	15552	16	955	1047		1210	I	4492	3457	2418
(9)	33948	15606	168	831	913		I 207	3	4417	3515	2415
(10)	33127	15304	16:	256	706		1170	9	4183	3488	2330
(11)	+ 31859	+14770	+15	457	— 5 08		+1116	ī	— 3886	+ 3389	2200
s	+1.87946	+86132	+91	909	<u>—4266</u>		+6557	8	23395	+19223	12840
S'	+1.87946	+86133	+91		4266		+6557	ł	-23395	+19222	-12838
	A(*)	A ₅ ^(c)	$\mathbf{A}_{5}^{(s)}$	$\mathbf{A}_{6}^{(c)}$		A ₆ (*)		A ₇ ^(c)	A ₇ (s)	A ₈ ^(c)	A ₈ ^(e)
	б	6	5	5		5		Б	δ	5	5
(0)	- 151	— 537	- 645	+ 3	6 _	- 327	, ⊣	- 99	- 77	+ 46	+ 7
(1)	142	507	608	3		306	- 1	90	72	43	6
(2)	166	479	597	3		295	1	91	66	40	7
(3)	213	458	609	5	1	292		93	62	40	9
(4)	271	452	644	6	3	299	1	99	60	41	12
(5)	333	462	700	7	9	318	3	109	60	44	15
(6)	391	486	767	9.		346		122	63	48	18
(7)	427	517	826	10.	1	372		133	67	53	20
(8)	422	546	852	10		389		138	72	56	20
(9)	367	566	833	9	1	390	- 1	134	77	56	17
(10)	282	571	775	6	i i	375		123	8o	54	13
(11)	— 20I	— <u>5</u> 60	— 7°5	+ 4	8 -	351	4	-110	— 80	+ 50	+ 9
s	-1683	-307 I	—4280	+40	3 -	-2031	r -	-672	—418	+285	+77
S'	—1683	-3070	<u>—4281</u>	+40.	4 -	-2029) -	-669	—418	+286	+76

The corrections to pass from the development of $[D-f\cos(\varepsilon-F)]^{-\frac{a}{2}}$ to that of $\left(\frac{a'}{\triangle}\right)^n$ are so small that it is deemed unnecessary to give the expressions for the former quantities, but we pass immediately to $\left(\frac{a'}{\triangle}\right)$ and $\left(\frac{a'}{\triangle}\right)^3$.

			(4)			
	<u>a</u> △	<u>′</u>	$\left(\frac{\mathbf{a}'}{\triangle}\right)^3$			
Arg=i'g'+i;	cos.	sin.	cos.	sin.		
i' i	1. 0267490		1. 2681946			
0 I	-0. 0031008	+0.0000 839	-0. 0272078	+0.0087021		
0— 2	+0.0000625	+0.0000001	+0.0007300	-0.0001262		
0 3	0, 0000003	+0.0000001	-0. 0000093	+0.0000041,		
1+ 2	-0. 0000004	0.0000012	— о. 0000046	0. 0000241		
1+ 1	+0.0002016	+0.0002385	+0.0007387	+0.0013937		
10	0. 003980 7	—o. 014058 7	— 0. 0163039	0. 0575499		
1— I	+0.2256609	+o. 2406638	+0. 7 946716	+0.8477242		
1 2	-0. 0005044	-0.0008631	o. oo95635	0. 0073459		
I — 3	+0.0000110	+0.0000139	+0.0002308	+0.0002017		
1— 4	-0.0000001	0.0000001	0. 0000034	0. 000002I		
2+ 1	+o. ooooo 43	—0. 0000046	+0.0000367	—о. 000 0368		
2 0	-0. 0001730	+0.0001609	—0. 0011676	+0.0012326		
2— I	+0 . 0 044940	-0. 0048541	+0.0252693	0. 0327933		
2— 2	0. 0050749	+0. 0786501	o. o293938	+0.4537504		
2-3	+0.0001437	0. 0003109	+0.0001228	0. 0048500		
2— 4	0.0000012	+0.0000053	0. 0000035	+0.0001197		
2— 5		•	0. 0000002	0. 0000015		
3+ 1			-0.0000011	0. 0000006		
3 0	+0.0000048	+0.0000019	+0. 00005 01	+0.0000174		
3— 1	-o. 0001257	-0. 0000449	<u> </u>	0.0003071		
3— 2	+0.0026027	+0.0000998	+0.0219110	0.0009048		
3— 3	0. 0161178	+o. o132642	—0. 1291000	+0. 1061610		
3 4	+0.0001148	0. 00002 69	+0.0015373	-0.0011111		
3-5	0.0000016	+0.0000007	—0. 0000359	+0.0000280		
3— 6			+0.0000004	0.0000005		
4 0			+0.0000001	-0.0000015		
4 I	+0.0000003	+0.0000032	+0.0000074	+0.0000397		
4— 2	-0.0000170	—0. 0000645	0. 0002713	-0.0007194		
4 3	+0.0006156	+0.0007381	+0.0070411	+0.0073737		
4 4	-0.0057514	-0.0007479	0. 0589015	0.0076895		
4 5	+0,0000322	+0.0000244	+0.0006986	+0.0001979		
4 6	-0.0000005	-0.0000003	0.0000164	0. 0000036		
5— 1		1	+0.0000011	-0.0000005		
5- 2	0.0000014	+0.0000013	-0.0000188	+0.0000179		
5 3	+0.0000183	-0.0000241	+0.0002167	-0.0003515		
5— 4	-0. 0000456	+0.0003394	-0.0003340	+0.0043736		
5— 5 r 6	0. 0009673	0.0013450	0. 0120572	0. 0167875		
5 6	+0.0000008	+0.0000139	+0.0001083	+0.0002509		
5— 7	0, 0000001	O, 000000I	-0. 0000029	0. 0000054		

$Arg=i'g'+i\varepsilon$	<u>a</u>		$\binom{\nabla}{3}_2$			
	cos.	sin.	cos.	sin.		
6' i 6- 3 6- 4 6- 5 6- 6 6- 7 6- 8	-0.000008 +0.000128 -0.0000976 +0.0000932 -0.0000032	-0. 0000002 -0. 0000006 +0. 0000686 -0. 0004728 +0. 0000033	-0.0000149 +0.0002016 -0.0014138 +0.0013761 -0.0000456 +0.0000008	-0. 0000029 -0. 0000272 +0. 0011020 -0. 0069533 +0. 0000905 -0. 0000021		
7— 4 7— 5 7— 6 7— 7 7— 8 8— 5 8— 6 8— 7 8— 8	-0. 0000002 +0. 000036 -0. 0000401 +0. 0001204 -0. 0000016 +0. 0000001 -0. 0000001 -0. 0000071 +0. 00000408	-0. 0000004 +0. 0000039 -0. 0000086 -0. 0000752 -0. 0000001 -0. 0000001 +0. 0000021 -0. 0000119 +0. 0000109	-0. 0000035 +0. 0000697 -0. 0006964 +0. 0020415 -0. 0000360 +0. 0000017 -0. 0000007 -0. 0001478 +0. 0007822	-0. 0000072 +0. 0000628 -0. 0001170 -0. 0012716 +0. 0000087 -0. 0000036 +0. 0000413 -0. 0002268 +0. 0002093		

These expressions are now changed into others in which ε is replaced by g; the formulæ and numerical data for this transformation have already been given (pages 52, 53).

Arg = i'g' + ig	<u>a</u>	<u>7</u>	$\left(\frac{\mathbf{a}'}{\triangle}\right)^3$			
gvy +iy	cos.	sin.	cos.	sin.		
i i o o I o 2 o 3 o 4	1. 0268359 0. 0031007 0. 0000245 0. 0000004	+0.0000838 +0.0000024 +0.0000002	1. 2689572 —0. 0272166 —0. 0000325 —0. 0000004 —0. 0000001	+0.0087058 +0.0001175 +0.0000073 +0.0000004		
I+ 3 I+ 2 I+ I I 0 I- I I- 2 I- 3 I- 4 I- 5	+0.000019 +0.0001128 -0.0103113 +0.2255119 +0.0058113 +0.0002480 +0.0000124 +0.0000007	+0.000020 +0.0001439 -0.0208108 +0.2405231 +0.0058732 +0.0002485 +0.0000124 +0.0000007	+0. 0000001 +0. 0000044 +0. 0004265 -0. 0385980 +0. 7945833 +0. 0126855 +0. 0006296 +0. 0000325 +0. 0000018	-0. 0000003 +0. 0000026 +0. 0010612 -0. 0813494 +0. 8474697 +0. 0163834 +0. 0007868 +0. 0000414 +0. 0000024		
2+ 2 2+ 1 2- 1 2- 2 2- 3	+0.0000025 -0.0002990 +0.0047751 -0.0049454 -0.0001354	-0. 0000033 +0. 0002971 -0. 0092579 +0. 0782935 +0. 0040783	+0.000006 +0.000270 -0.0018768 +0.0268967 -0.0286047 -0.0014899	-0.000007 -0.000272 +0.0021527 -0.0581990 +0.4518156 +0.0204783		

Ara-i/a/ ia	<u>a</u> <u>△</u>		$\left(\frac{\mathbf{a}'}{\triangle}\right)^3$			
Arg=i'g'+ig	cos.	sin.	cos.	sin.		
i' i 2 4	0, 0000048	+0.0002250	0. 0000837	+0.0011308		
2 5	0.0000002	+0.0000132	—0, 0000052	+0.0000661		
2— 6	0, 0000000	+0.0000008	—0, 0000003	+0.0000039		
3+ I			—o. oooooo8	0. 0000004		
3 0	+0.0000083	+0.0000032	+o. 0000844	+0.0000260		
3 I	-0. 0002904	-0. 0000349	—0. 0026025	0.0001311		
3-2	+0.0039446	-0.0010155	+0.0326512	—0. 0098267		
3-3	—0. 0158714	+o. 0131791	—0. 1271383	+0. 1054850		
3— 4	-0.0012251	+0.0010819	—0. 0091958	+0.0077667		
3— 5	-0.0000827	+0.0000753	- o. ooo6163	+0.0005255		
3 6	0. 0000054	+0.0000050	0. 0000408	+0.0000348		
3— 7	—0.0000003	+0.0000003	0. 0000027	+0.0000023		
4 0			—o. oooooo1	—o. ooooo26		
4 I	+0.0000021	+0.0000077	+0.0000318	+o. oooo888		
4— 2	0. 0000867	-0.0001285	—0. 0010463	0. 0013591		
4- 3	+0.0012530	+0.0008129	+o. o135606	+0.0081418		
4 4	0. 0056325	-o. ooo68o4	—o. o576734	0.0070069		
4 5	0. 0006032	0.0000547	—o. oo58103	0. 0006159		
4 6	-0, 0000496	—0. 0000036	o. 0 004666	0. 0000452		
4 7	0.0000038	-0.0000003	-0, 0000350	—0. 0000032		
4— 8			0, 0000026	0, 0000003		
5— 1			+0,0000025	—0. 0000019		
5— 2	—0. 0000029	+0.0000045	-0.0000370	+0.0000622		
5— 3	+0.0000175	—o. oooo694	+0.0001805	-0.0009354		
5— 4	+0.0000912	+0.0005205	+0.0013684	+0.0066298		
5 5	—o. ooo9535	-0. 0012834	—o. o118753	—o. o16o168		
5 6	-0.0001332	—o. ooo1691	o. oo15631	0. 0020339		
5— 7	—o. 0000131	-0.0000159	0.0001488	-0.0001885		
5— 8	-0,0000011	0.0000013	—0. 0000125	—o. oooo16o		
6 2	_		+0.0000020	0,0000000		
6 3	0.0000028	+0.0000004	—0. 0000459	+0.0000080		
6 4	+0.0000270	-0,0000146	+0.0004077	—0. 0002459		
6— 5	-0.0001098	+0.0001459	-0.0015937	+0.0022366		
6 6	+0.0000778	—o. ooo4506	+0.0011529	0. 0066235		
6— 7 6— 8	+0.0000110	-0.0000739	+0.0001638	-0.0010444		
6— 8	+0.0000010	0, 0000081	+0.0000160	—0. 0001123		
7— 3			+0. 0000009	+0.0000012		
7 4	-0.000011	-0.0000010	0, 0000205	-0.0000164		
7— 5	+0.0000118	+0.0000042	+0.0002117	+0.0000629		
7 6	—o. oooo618	+0.0000066	0.0010628	+0.0001411		
7— 7	+0.0001095	-0.0000736	+0.0018577	0.0012434		
7— 8	+0.0000208	-0.0000147	+0. 0003435	—o. 0002371		
8 4			-0.000001	+0.0000010		
8— 5 8— 6	0,0000000	-0,0000007	o, 0000008	-0.0000137		
8— 6 8— 7	+0.0000021 0.0000158	+0. 0000045 -0. 0000136	+0.0000427 0.0003143	+0.0000874 0.0002574		
8-8	+0.0000374	+0.0000081	+0.0007151	+0.0001563		
	5,1		L			

The expressions for the two factors by which $\left(\frac{a'}{\triangle}\right)^3$ must be multiplied are

$$\frac{1}{2} \left(\frac{r'^2}{a'^2} - \alpha^2 \frac{r^2}{a^2} \right) = \begin{cases} 19.65269181 \\ -2[7.6281908] \cos g' + 2[7.4505092] \cos (-g) \\ -2[4.9553] \cos 2g' + 2[5.5968] \cos (-2g) \\ +2[4.0441] \cos (-3g) \end{cases}$$

$$\frac{r'}{a'} \sin (f' + \Pi') = \begin{cases} -19.6139931 \sin g' + 2[9.4540858] \cos g' \\ -2[7.24218] \sin 2g' + 2[7.08227] \cos 2g' \\ -2[5.0465] \sin 3g' + 2[4.8866] \cos 3g' \end{cases}$$

The products are

Arg=i'g'+ig	$\frac{1}{2}\left(\frac{r'^2}{a'^2}-c\right)$	$\begin{pmatrix} \chi^2 r^2 \\ \mathbf{a}^2 \end{pmatrix} \begin{pmatrix} \mathbf{a}' \\ \overline{\triangle} \end{pmatrix}^3$	$\frac{r'}{\mathbf{a}'}\sin\left(f'+\Pi'\right)\left(\frac{\mathbf{a}'}{\triangle}\right)^3$		
	cos.	sin.	sin.	cos.	
i' i	1		La araare		
0 0	+0.0570160	10.0000774	+0.013258	10 56500	
0— 1	—o. oo68999	+0.0002754	—0. 122353	+0.567232	
0 2	-0.0000325	+0.0000025	0. 003952 0. 000185	+0.010369	
o— 3	0.0000011	+0,0000003		+0.000505	
1+ 2	0. 0000005	0, 0000004	0, 00008	0. 00006	
1+1	+o. 0000581	+0.0001562	0, 01182	+0.00629	
1 0	0. 0024662	0. 0043117	+o. 15198	— 0. 22056	
ı— ı	+0. 0275617	+0.0295937	+0.02166	+0.00201	
I— 2	-0.0009115	-0.0015739	o. 19389	+0.11675	
1— 3	0, 0000213	0. 0000506	0. 00917	+0.00512	
I— 4	о. 0000006	—0.0000023	—o. ooo5o	+0.00028	
2+ 2	+o. oooooo3	0. 0000002			
2+ I	+0.0000033	 0. 0000124	+0.00051	+0,00012	
2 0	o. 0001682	+0.0013487	-o. o5101	+0.00229	
2— І	+0.0025682	o. o277736	+0.57359	0. 08621	
2 2	o. 0106082	+o. 1636826	+0. 02389	+0.00678	
2 — 3	0. 0001487	+0.007 9848	0. 07902	-0. 02243	
2— 4	0,0000012	+0.0004384	—o. oo585	0.00170	
2- 5	+0.0000002	+0.0000254	-0.00041	0.00011	
2 — 6	+o. 0000001	+0.0000010			
3+ 1	0, 0000004	0.0000000			
3 0	+0, 0000404	+0.0000057	+0.00005	+0.00152	
3— I	0.0011111	+0.0001180	o. o1385	-o. o2796	
3— 2	+0. 0124610	o. oo55267	+0. 17770	+0. 13955	
3 3	-0. 0491933	+0. 04 06944	+0.00943	+0.01358	
3 4	0. 0036343	+0.0032734	-0.01303	-0.02541	
3— 5	0.000 24 29	+0.0002272	o. oo135	-0. 00259	
3 6	-o. oooo158	+0.0000152	o. 000 I I	-0.00020	
3— 7	-0.0000011	+0.0000010			

Arg = i'g' + ig	$\frac{1}{2}\left(\frac{r'^2}{a'^2}-a\right)$	$\left(\frac{a^2}{a^2}\right)\left(\frac{a^\prime}{\triangle}\right)^3$	$\frac{r'}{a'}\sin(f'-$	$+II') \left(\frac{\mathbf{a}'}{\triangle}\right)^{3}$
	cos.	sin.	sin.	cos.
i' i 4 0	—0. 0000003	0, 0000011		
4— I	+0.0000209	+0.0000329	0.00084	+0.00091
4 2	-0.0005291	-0, 0004864	+0.00598	-o. o1561
43	+0.0058429	+0.0027851	+0.00757	+0. 08205
4-4	-0. 0230505	0. 0028491	-o. oo135	+0.00849
4-5	-0. 0024204	-0.0002033	+0.00329	-0.00904
4— 6	-0.0001969	-0. 0000120	+0.00040	-0.00119
4-7	-0.0000148	—0. 000000 6	+0,00004	0,00011
4 8	-0.0000012	0, 0000000	1	
5— I	+0.0000009	-0,0000011		
5 2	0.0000105	+0.0000294	i	
5 3	+0.0000194	-0.0004030		
5 4	+0.0007797	+0.0027024		
5 5	-0. 0048298	—0. 0065511		
5— 6	-0.0006722	-o. ooo8468		
5 7	-0.0000659	-0.0000787		
5— 8	—0. 0000057	-0.000067	:	
6— 2	+0.0000010	—0. 0000003		
6 3	—0. 0000186	+0.0000067		
6— 4	+0.0001600	-0.0001252		
6 5	0.0006073	+0.0009807		
6 6	+0.0004864	0.0027402		
6 7	∔ 0.0000640	-0. 0004447		
6— 8	+0.0000058	—0. 0000486		.,
7— 3	+0.0000005	+0.0000005		
7 4	0, 0000098	-o. ooooo58		
7— 5	+0.0000931	+0.0000173		
7— 6	0. 0004461	+0.0000845		
7— 7	+0.0007789	—0.00051 69		
7— 8	+0.0001461	—0. 0001030		
8— 4	+0.0000001	+0.0000005		
8 – 5	0.0000012	о. 00000 60		
8 6	+0.0000218	+0.0000359		
8 7	—0. 0001392	0.0001030		
8— 8	+0.0003003	+0.0000665	:	

For the computation of $a' \frac{r}{r'^2}H$ we have (page 63)

 $\log h = 9.3366883$ $\log l = 9.3637535n$ $\log h_1 = 9.3359062$ $\log l_1 = 9.3644536n$

We have then

Arg=i'g'+ig	—a′	$\frac{r}{r'^2}$ H	Arg=i'g'+ig	—a′	$\frac{r}{r'^2}$ H
	cos. sin.			cos.	sin.
i' i i + 2 i + 1 i o i - 1 i - 2 i - 3 i - 4 i - 5 2 + i 2 o	-0. 0000022 -0. 0001080 +0. 0182556 -0. 2167446 -0. 0060702 -0. 0002550 -0. 0000127 -0. 0000007 -0. 0000018 +0. 0003102	-0. 0000019 -0. 0000975 +0. 0194612 -0. 2310759 -0. 0064716 -0. 0002718 -0. 0000135 -0. 0000017 +0. 0003307	i' i 2-1 2-2 2-3 2-4 3 0 3-1 3-2 3-3 4-1	0. 00368300. 00010320. 00000430. 0000002 +-0. 000005280. 00000010. 0000007	-0. 0039265 -0. 0001099 -0. 0000046 -0. 000002 +0. 0000047 -0. 0000563 -0. 0000016 -0. 0000001

In addition

$$-\frac{a'^2}{r'^2}\sin(f'+II') = +0.82229 \sin g' - 0.56900 \cos g'$$

$$+0.01397 \sin 2g' - 0.00967 \cos 2g'$$

$$+0.00020 \sin 3g' - 0.00014 \cos 3g'$$

The logarithms of the factors which depend on the mass of Neptune are $\log \mu = 0.5211900$ $\log (\mu \alpha \sin J) = 8.2488067$

The expressions for the forces are then

$ ext{Arg} = i'g' + ig$	$arac{d.\Omega}{dg}$		$arrac{d\Omega}{dr}$		$a^2rac{d\Omega}{dZ}$	
	sin.	cos.	cos.	sin.	sin.	cos.
i' i	"	"	,, +0. 189316	<i>''</i>	11	+0.000235
о— 1	-0. 010295	—0. 000278	0. 022910	+0.000914	+0.0100593	0. 0021698
0 2	o. ooo163	0.000016	0, 000108	+0.000008	+0.000184	0. 000070
0— 3	-0.000004	-0.000002	-0. 000004	+0.000001	0. 000009	0.000003
I+ 2	+0.000002	+o. ooooo1	0, 000002	0,000001		
1+1	0.000016	+0.000154	+0.000193	+0.000519	+0.000112	-0,000210
10			0.008189	-0. 014317	—0. 003911	+0.002695
I I	+0.029111	—o. o31368	+0.091516	+0. 098263	+0.000035	+0.000380
I— 2	0.001719	+0. 003974	0. 003027	—o. 00522 6	+0.002070	-0.003438
I— 3	— 0. 000070	+0.000232	0. 000071	0. 000168	+0.000089	-0.000163
1 4	0.000004	+0.000015	0, 000002	0.000008	0, 000000	-0.000009
2+ I	-0.000002	0.000017	+0.000011	-0.000041	0.000000	+0.000009
2 0			0.000558	+0.004478	+0.000041	-0. 000905
2— I	+0.003626	+0.043777	+0.008527	0. 092219	-0.001529	+0.010172

Arg=i'g'+ig	$a rac{d}{d}$	$rac{\Omega}{\log}$	ar_{-}^{a}	$rac{d\Omega}{dr}$	$a^2 rac{d_d}{d_d}$	$rac{\Omega}{Z}$
	sin.	cos.	cos.	sin.	sin.	cos.
i	"	"	"	"	n n	"
2— 2	-o. o33527	—o. 519201	-0.035223	+o. 5 43491	+0.000120	+0.000424
2— 3	-0.001392	-0. 040579	0.000494	+ 0. 026512	—о. 000398	0,001401
2— 4	0. 000066	0. 002986	0.000004	+0.001456	0. 000030	-0.000104
2 5	-0.000003	0.000219	+0.000001	+0.000084	0.000000	0.000007
2— 6	0.000000	0.000016	0.000000	+0.000003		
3 0			+0.000134	+0.000019	+0.000027	0.000000
3- 1	-0.001140	+ 0. 000303	—о. 003689	+0. 000392	—0. 00049б	0,000246
3— 2	+0.026185	+0.006754	+0.041375	—о. 018351	+0.002474	+0.003151
3-3	—0. 158099	0. 131279	—0. 163341	+0.135122	+0.000241	+0.000167
3— 4	0. 016271	— 0. 014369	0.012067	+0.010869	o. 000451	-0.000231
3- 5	-0.001373	-o. 001250	-0.000810	+0.000754	-0,000046	-0. 000024
3— 6	-0.000108	-0.000100	-0.00052	+0.000050		
3 7	—0. 000007	—0. 000007	-0.000004	+0.000003		
4 0			0.000001	-0.000004		
4 1	+0.000005	0.000023	+0.000069	+0.000109	+0.000015	-0.000015
4- 2	—o. ooo576	+0.000853	0.001757	0. 001615	0. 000277	+0.000106
4-3	 -0. 012481	-o. oo8o97	+0.019401	+0.009248	+0.001455	+0.000134
4— 4	— 0. 074808	+0.009034	0. 076537	0. 009460	+0.000151	0. 0 0 0024
4 5	-0.010014	+0,000908	-0.008037	0, 000675	o, ooo16o	+0.000059
4 6	0, 000988	+0.000072	—0. 000654	0, 000040	0.000021	+0.000007
4- 7	0,000088	+0.000007	0.000049	0, 000002		
4— 8			0. 000004	0.000000	ł	
5- 2	0.000019	0.000030	—0. 000035	+0.000098		
5— 3	+0,000174	+0.000691	+o.000064	0. 001338		
5 4	+0,001211	0.006912	+0.002589	+0.008973	1	
5— 5	0. 015831	+0.021307	0, 016037	0. 021752	ŀ	
5— 6	0, 002654	+ 0.003368	-0,002232	-0.002812		
5-7	0, 000304	+0.000370	—и. 000219	-0. 000261		i
5— 8	-0.000029	+0.000035	-0.000019	-0.000022		
6 3	0, 000028	-0.00004	—o. 000062	+0.000022	l	
6 4	+0.000359	+0.000194	+0.000531	-0. 000415	I	!
6— 5	0. 001823	-0.002423	0. 002016	+0.003255	l	
6— 6	+0.001550	+0.008976	+0.001615	0. 009098		
6 7	+0.000256	+0.001718	-0.000213	-0.001477	I	
6— 8	+0.000026	+0.000215	+0.000019	-0.000161		}
7 4	0.000015	+0.000013	0. 000033	0.000019		1
7— 5	+0.000196	0.000070	+0.000309	+0.000057		
7 6	0. 001231	0.000131	0. 001481	+0.000281		
7— 7	+0.002546	+0.001711	+0.002586	-0.001716		
7— 8	+0.000553	+0.000390	-+0.000485	-0.000342		
8— 5	0.000000	+0.000012	0, 000004	-0.000020	1	
8— 6	+0, 000042	0. 000090	+0.000072	+0.000118	1	}
8— 7	0. 000367	+0.000316	-0. 000462	0. 000342		
8— 8	+0.000994	-0.000215	+0.000997	+0.000221		
	1					1

The expressions by which these forces must be multiplied in order that we may obtain T and $\frac{1}{n} \frac{dR}{dt}$ have already been given (page 74), and the resulting developments are

$Arg = \varkappa \gamma + i'g' + ig$,	Г	Arg= u y + i'g' + ig	7	r
IIIg = 1/7 + 1/9 + 1/9	sin.	cos.	Mig// Try Try	sin.	cos.
κ i' i I 0— I	(1)	// 0,00001	$egin{array}{c ccccccccccccccccccccccccccccccccccc$	0. 00000	"
l .	-0. 37621	+0.00003	1		0.00019
—I 0 0	o. o329355	-0.0014737	0 2-5	+0.00001	+0.00066
0 0 1	+0. 03088	+0.00083	1 2— 6	-0.00001	0. 00042
I 0 2	0. 00823	+0.00036	I 3+ I	+0.00004	0.00000
—ı o— ı	+0.00037	—0. 00003	I 3— I	+0.00013	0.00001
0 0-2	+0.00049	+0.00005	_1 3 o	0. 00439	+o. ooo66
I 0— 3	-0. 00032	0, 00000	0 3— 1	+0.00342	0. 00091
—I 0— 2	+0.00001	0, 00000	I 3— 2	0. 00343	0. 00047
o o 3	+0.00001	+0.00001	—ı 3— ı	+o. 08492	+0.02437
I 0— 4	-0.00001	0, 00000	0 3 2	—о. 07855	0. 02026
-I I+ 2	+0.00006	+0.00005	1 3-3	+o. o3787	+0.01740
0 1+1	+0.00005	-0.00046	_1 3— 2	—o. 48361	0. 39943
110	+0.00001	+0.00043	0 3-3	+0. 47430	+0.39384
-ı ı+ı	<u></u> 0. 00480	+0.01068	I 3—4	-o. 15090	-0. 12563
1 I— I	+0.00153	0.00717	_r 3— 3	0. 02713	-0.02509
— I I O	+0. 14961	о. 16060	0 3-4	+o. 04881	+0.04311
0 I I	-o. o8733	+0. 09410	I 3— 5	—0. 02017	-0. 01760
I I— 2	-o. o3279	+0.03447	—I 3— 4	-o. oo162	0.00155
—I I— I	0. 00799	+0.01484	0 3-5	+0.00412	+0.00375
o I— 2	+0.00516	-0.01192	1 3-6	-0.00197	o. oo177
I I— 3	0.00214	+0.00456	_r 3— 5	-0.00010	-0.00009
—ı I— 2	-0.00006	+0.00022	0 3-6	+0.00032	+0.00030
o I— 3	+0.00021	0.00070	I 3— 7	0.00018	-0.00015
I I— 4	-0.00013	+0.00035	_1 4 0	+0.00004	-0.00011
_1 2+ 2	0, 00000	0. 00003	0 4— 1	o. 0000I	+0.00007
0 2+1	+0.00001	+0.00005	I 4-2	+0.00007	-0.00011
1 2 0	+0.00001	+o. oooo6	—I 4— I	—o. 00217	+0.00286
—I 2+ I	0. 00029	0.00172	0 4-2	+0.00173	-0.00256
I 2— I	-0.00019	0. 00425	I 4— 3	-0.00169	+0.00149
-ı 2 0	+0.01386	+0. 15007	I 4—_2	+0.04020	—0. 02503
0 2— I	o. oto88	_o. 13133	0 4-3	0. 03744	+0.02429
1 2- 2	+0.00445	-+o. o8 3 63	1 4-4	+0.01826	-0.00853
—I 2— I	-0. 10276	—r. 58983	—I 4— 3	—o. 22822	+0. 02851
0 2— 2	+0. 10058	+1.55760	0 4-4	+0. 22442	-0. 02510 -0. 02710
1 2-3	o. o3181	o. 4906o	I 4-5	—0. 22442 —0. 07174	+0.00850
-I 2 2	+0. 00044		-r 4-4	o. 0/1/4 o. 01981	+0.00150
		—0. 05033 —0. 12174	1		1
0 2-3	+0.00418		1 ' '	+0.03004	-0.00272
I 2— 4	—0. 00225	—o. o5367	1 4— 6	0.01181	+0.00111
—I 2— 3	+0.00006	0.00249	—I 4— 5	-0.00145	+0.00007
0 2 4	+0.00020	+0.00896	0 46	+0.00296	0.00022
1 2- 5	0.00015	0. 00466	I 4— 7	—o. 00134	+0.00011

	r	Г			r
Arg=xy+i'g'+ig	sin.	608,	Arg=\(\nu\nu+i'g'+ig\)	sin.	cos.
π i' i1 4 6 0 4 7 1 4 81 5 1 0 5 2 1 5 31 5 2	-0.00011 +0.00026 -0.00014 -0.00007 +0.00006 -0.00003 +0.00048	" 0.000000.00002 +-0.000010.00015 +-0.000090.00010 +-0.00233	π i i i i i i i i i i i i i i i i i i i	+0.00144 +0.00054 -0.00077 +0.00030 +0.00004 -0.00003	" +0.00861 +0.00393 -0.00515 +0.00191 +0.00039 -0.00064 +0.00029
0 5— 3 1 5— 4 —I 5— 3 0 5— 4 I 5— 5 —I 5— 4 0 5— 5 I 5— 6 —I 5— 6 I 5— 7 —I 5— 6	-0.00052 +0.00005 +0.00411 -0.00363 +0.00251 -0.04800 +0.04749 -0.01526 -0.00580 +0.00796 -0.00301 -0.00052 +0.00091	-0. 00207 +0. 00126 -0. 02168 +0. 02074 -0. 00847 +0. 06536 -0. 06392 +0. 02041 +0. 00721 -0. 01010 +0. 00387 +0. 00062 -0. 00111	-I 7-3 0 7-4 I 7-5 -I 7-4 0 7-5 I 7-6 -I 7-5 0 7-6 I 7-7 -I 7-6 0 7-7 I 7-8 -I 7-7	-0.00004 +0.00004 +0.00063 -0.00059 +0.00029 -0.00383 +0.00369 -0.00142 +0.00785 -0.00764 +0.00243 +0.00131	+0.00005 -0.00004 +0.00002 -0.00021 +0.00021 -0.00005 -0.00043 +0.00039 -0.00027 +0.00518 -0.00513 +0.00166 +0.00093
1 5—8 -1 5—7 0 5—8 1 5—9 -1 6—2 0 6—3 1 6—4 -1 6—3 0 6—4 1 6—5 -1 6—6 -1 6—5 0 6—6	-0. 00039 -0. 00005 +0. 00009 -0. 00004 -0. 00010 +0. 00008 -0. 00014 -0. 00114 -0. 00151 -0. 00563 +0. 00547 -0. 00189 +0. 00494 -0. 00465	+0. 00048 +0. 00005 -0. 00010 +0. 00005 0. 00000 +0. 00001 -0. 00003 +0. 00066 -0. 00058 +0. 00040 -0. 00727 -0. 00311 +0. 02743 -0. 02693	-1 /- / 0 7-8 1 7-9 -1 8-4 0 8-5 1 8-6 -1 8-5 0 8-6 1 8-7 -1 8-6 0 8-7 1 8-8 -1 8-7 0 8-8 1 8-9	-0.0013 -0.0000 0.0000 -0.0001 +0.00013 -0.00013 +0.00007 -0.00115 +0.00110 -0.00045 +0.00303 -0.00298 +0.00099	+0.0003 -0.00117 +0.0004 +0.00004 +0.00001 -0.00028 +0.00027 -0.00011 +0.00096 -0.00095 +0.00033 -0.00068 +0.00064 -0.00021

$\frac{1}{n}\frac{d\mathbf{R}}{dt}$ $\mathbf{Arg} = \mathcal{u}\mathbf{y} + \mathbf{i}'\mathbf{g}' + \mathbf{i}\mathbf{g}$			$Arg = \nu \nu + i'g' + ig$		$\frac{1}{n}\frac{d\mathbf{R}}{dt}$		
0 ,	, , , ,	cos.	sin.			008.	sin.
1	i' i o— I	// 	+0.00029	ж —I	i' i 2— 2	// 0. 0002I	+0.00072
I I	0 0 0 0 0 2	+0.0050243 -0.00500	+0.0011042 -0.00109	-i	2— 4 2— 3	+0.00020 a.00000	-0.00068 -0.00001
_1 _1	o— 1 o— 3	0.00033 0.00023	o. 00006 o. 00006	-I	2— 5 3+ I	+0.00003	-0.00007 0.00000
1	I+ 2 I 0	0, 00000 —0, 00022	+0.00006 -0.00021	I	3— I	-0.00003 -0.00022	+0.00001 +0.00008
I	I+ I	0.00195 0.00195	-0.00137 +0.00133	1 —1	3— 2 3— 1	+0.00035 +0.00126	0. 00025 0. 00158
—ı	I 0	+0.00021 +0.00013	-0. 00003 +0. 00037		3-3 3-2	-0.00122 +0.00001	+0.00156 +0.00005
_i	I— I I— 3	+0.00103 -0.00103	+0.00174 -0.00170		3-4 3-3	0.00017 0.00023	+0.00013
— 1	1— 2	—o. oooo5	0. 00006	ı	3-5	+0.00022	-0.00012
I	I— 4 2 0	o. 00007 o. 00000	-0.00013 +0.00004	1 -1	4 1 4 3	-0.00012 +0.00020	-0. 00005 +0. 00004
I	2+ I 2- I	o. 00000 a. 00008	+0.00031 0.00088	I	4— 2 4— 4	+0.00074 -0.00072	-0.00007 +0.00007
_1	2 0 2— 2		0. 00513 +0. 00505	i	4— 3 4— 5	+0.00002 0.00011	+0.00002 0.00001
I	2— I 2— 3	+0.00011 -0.00006	+0.00024 +0.00041	-ı	4— 4 4— 6	o. 00009 	o. 00003 +-o. 00003

The table of logarithms of the integrating factors follows:

Arg.	$\log \frac{n}{i'n'+in}$	Arg.	$\log \frac{n}{i'n'+in}$	Arg.	$\log \frac{n}{i'n'+in}$	Arg.	$\log \frac{n}{i'n'+in}$
i' i o- I o- 2 o- 3 I+ 2 I+ I I o I- I I- 2 I- 3 I- 4 I- 5 2+ 2	0. 00000n 9. 69897n 9. 5229n 9. 6618 9. 9286 0. 74772 0. 08553n 9. 73963n 9. 54956n 9. 4178n 9. 3168n 9. 6275	i' i 2-4 2-5 2-6 3+1 3-3-1 3-2 3-3 3-4 3-5 3-6 3-7	9. 43860n 9. 3332n 9. 2485n 9. 8135 0. 2706 0. 33375n 9. 83455n 9. 60841n 9. 46046n 9. 35031n 9. 2625n 9. 1895n	i' i 4— 5 4— 6 4— 7 4— 8 5— 1 5— 2 5— 3 5— 4 5— 5 5— 6 5— 7 5— 8 5— 9	9. 36806n 9. 2770n 9. 2017n 9. 1376n 0. 9740n 9. 9562n 9. 6765n 9. 5078n 9. 3866n 9. 2919n 9. 2142n 9. 1484n 9. 0912n	7— 3 7— 4 7— 5 7— 6 7— 8 7— 9 8— 4	9. 3074n 9. 2271n 9. 1594n 9. 1009n 9. 7574n 9. 5609n 9. 4261n 9. 3234n 9. 2404n 9. 1708n 9. 1108n 9. 5901n
2+ I 2 0 2- I	9. 8673 0. 44669 0. 19215 <i>n</i>	4 0 4— I 4— 2	0. 1457 0. 54525 <i>n</i> 9. 89112 <i>n</i>	6— 2 6— 3	0. 0327n 9. 7150n	8— 5 8— 6 8— 7	9. 4473n 9. 3401n 9. 2541n
2— 2 2— 3	9. 7 8450n 9. 57799n	4— 3 4— 4	9. 64112n 9. 48347n	6— 4 6— 5	9. 5335n 9. 4059n	8— 8 8— 9	9. 1924n 9. 1209n

25 AST----12

In integrating we put

 $k_0 = + \circ''.3763$ $k_1 = - \circ''.0492$ $k_2 = - \circ''.0025$ $k_3 = + \circ''.0025$ $k_4 = + \circ''.0005$ And we have

Arg=i'g'+ig		δz t	$\frac{1}{n}$	
gvy 49	cos.	sin.	sin.	cos.
<i>i' i</i> 0 0	11	"	"	" +0.0000207
0— І	-0. 0329	+0.0015	—0. 0162	+0.0014 +0.0164677 <i>nt</i>
0— 2	-0.0014737nt -0.0012	-0.0329355nt +0.0001	-0.0007368nt +0.0018	+0.0001
	-0.0000412nt	-0.0009224nt	-0.0000412nt	+0.0009224nt
1+ 1 1 0	0. 0000 +0. 00543	+0.0024 +0.01726	+0.0001 -0.00161	0.0014 0.00070
1— 1	-0.9611	-1.0316	+o. 4094	—0. 4394
I— 2	0. 0311	-o. o384	+0.0279	-0.0334
1-3	0.0012	-0.0016	+0.0018	-0.0022
2+ I	0,0000	+0.0002	0, 0000	o. ooo1
2 0	-0. 00002	+0.00413	-0, 00020	-o. 00284
2— I	o. o533	+0.5784	+o. o2o5	+0. 2302
2— 2	—о. 1118	+1.7242	+0.0751	+1.1559
2 — 3	0. 0032	+0.0690	+0.0042	+0.0779
2— 4	0. 0001	+0.0032	+0.0003	+0.0053
3 0	+0.0002	0.0000	0,0000	0.0000
3 1	+o. 01360	+0.00335	0.00491	+0.00060
3- 2	+o. 1438	— 0. 0448	o. o852	—o. o238
3 3	—o. 1765	+0. 1479	+o. 1382	+o. 1167
3— 4	0. 0105	+0.0092	+o. o122	+0.0106
3— 5	o. 0007	+0.0006	+0.0009	+0.0008
4— I	o. oooo8	o. ooo33	+0.00003	-0.00010
4— 2	о. 0068	—o. oo86	+o. oo36	0.0048
4 3	+o. o198	+0.0111	o. o131	+0.0082
4 4	0. 0475	0.005 8	+0.0405	-0. 0047
4— 5	0. 0040	0. 0005	+0.0047	0.0005
4— 6	+0.0002	0, 0000	+0.0007	0.0000
5— 2	 0. 0006	+0.0013	+0.0003	+0.0007
5— 3	+0.0002	0.0014	0.0002	0.0010
5— 4	+0.0013	+0.0055	-o. ooo8	+0.0041
5— 5	0. 0068	-0.009 <u>1</u>	+o, oo61	0. 0082
5— 6	—o. ooo6	0,0010	+o. ooo8	-0.0012
6— 4	+0.0003	0,0002	0.0002	-0.0001
6— 5	— 0. 0009	+0.0013	+0.0008	+0.0010
6 6	+0.0005	0. 0029	-0.0004	0. 0027
6— 7	0.0000	—0.0004	O. 000 I	0.0005
7- 5	+0.0001	0, 0000	-0.0001	0.0000
7- 6	-0.0004	0.0000	+o. 0004	+0.0001
7 7	+0.0008	-0.0004	0, 0006	-0.0004
7— 8	+0.0001	-0.0001	—o. ooo1	-0.0001
8— 7	-0, 0002	-0.0001	+0.0001	0.0001
8 8	+0.0001	0. 0000	0.0002	+0.0001

In fine we have the perturbations of Saturn by Neptune. Here we give a single accent to the symbols belonging to Saturn and three accents to the mean anomaly of Neptune.

$\mathbf{Arg} \! = \! \mathbf{i}'g''' \! + \! ig'$	$n'\delta z'$		ν	,,	u cos	_
g, , , ,	sin.	cos.	cos.	sin.	sin.	cos.
i' i o o	"	11		n .	"	// +0.0003 —0.0004230 <i>n't</i>
1 -0	0.0000	0.0000	-0.0327	0, 0007	0.0000	0.0000
	+0.0014737n't	-0. 0329355 <i>n't</i>	+0.0007363n't	+0.0164677 <i>n't</i>	+0.0011042n't	- -0.0050243 <i>n't</i>
0- 2	+0.0004	0.0000	+0.0007	0.0000	+0.0001	-0.0001
	+0. 0000206 <i>n't</i>	0. 000461 <i>2n't</i>	+0.0000206n/t	+0.000461 <i>2n't</i>	+0.0000309 <i>n't</i>	+0.0001407 <i>n't</i>
1+1	0.0000	0. 0020	-0.0001	0.0012	-0.0013	+0.0012
1 0	+0.0304	—o. o965	+o. 0090	+0.0039	- 0.0041	+0.0028
I — I	+1. 1703	—1.2561	+0.4984	+0.5350	+0.0013	+0.000I
f — 2	+0.0171	—o. o211	+0.0153	+o. 0183	0.0009	+0.0015
1 3	+0.0004	0.0006	+0.0006	+o. ooo8		
2 0	0.0001	—0. 011 6	+0.0006	0.0079	+0.0003	0. 0027
2 I	+0.0829	+ 0. 9001	+0.0319	—o. 3582	-o. oo26	+0.0175
2 2	+o. o681	+1.0498	+0.0457	7037	0.0003	+0.0008
2— 3	+0.0012	- 1-0. 0261	+ 0.0016	-0. o295		
2 4	0.0000	+0.0009	+0.0001	0. 0015		
3 0	- - 0. 0004	0.0000	0.0000	0.0000		
3— I	-0.0293	+0.0072	—0. 0106	-o. oo13	-0, 0004	0.0000
3- 2	-0. 0982	о. 0306	0. 0582	+0.0163	-0.0022	0.0028
3-3	+0.0716	+0.0600	+o. o561	0. 0474	<u> </u>	0.0001
3 4	+0.0030	+0.0027	+0.0035	0.0031		
3— 5	+0.0002	+0.0001	+0.0002	-0.0002		
4— I	+0.0003	-0.0012	+0.0001	+0.0004		
4 2	+0.0053	— о. 0067	+0.0028	+0.0037	+0.0004	-0.0002
4 3	-0.0087	+ 0.0049	-o. oo57	—о. 0 036	-0.0004	-0,0001
4 4	+0.0145	o. oo18	+0.0123	+0.0015		
4 5	+0.0009	-0.0001	+0.0011	+ 0.0001		
5— 2	+0.0005	+0.0012	+0.0003	0.0006		
5— 3	-0.0001	o. ooo7	0.0001	+0.0005		
5— 4	-0.0004	+0.0018	0.0003	-o. oo13		
5 5	+0.0017	-0.0022	+0.0015	+0,0020		
5— 6	+0.0001	0. 0 002	+0.0002	+0.0002		
6— 4	0.0001	0.0001	0.0001	0.0000		
6— 5	+0.0002	+0.0003	+0.0002	0.0003		
6— 6	_0.000 I	—o, ooo6	000 .0	+0.0005		
6 7	0.0000	-0,0001	0.0000	+0.0001		
7— 6	+0.0001	0.0000	+0.0001	0.0000		
7— 7-	`-o. ooo1	o. 0001	0.0001	+0.0001		

CHAPTER VI.

PERTURBATIONS OF JUDITER BY NEPTUNE.

In this case also first-order terms suffice. The elements of the two planets have already been given (pages 19, 161). The coefficients of the terms of the developments of the reciprocal of the distance between Jupiter and Neptune, and its odd powers, are functions of the six elements

$$\log \alpha = 9.2380919$$
 $J = 0.56 53.38$ $e = 0.04824277$ $\Pi = 196 4 4.53$ $e' = 0.0084962$ $\Pi' = 227 24 47.47$

 Π and Π' are measured from the ascending node of the orbit of Neptune on that of Jupiter. The developments will be made first in terms of the eccentric anomaly of the latter planet.

The values of the auxiliary constants are

		0	/	//
$\log k$	= 9.9999955	K = 31	20	50.47
$\log k_1$	= 9.9999450	$\mathbf{K}_1 = 3\mathbf{I}$	20	35-43
$\log p$	=9.2675773	P = 13	53	1.47
$\log v$	= 9.5387100	V = 31	22	43.86
$\log w$	= 9.5385860	$W = r_7$	26	35-35
$\log w_1$	= 9.5390766	$W_1 = 17$	28	47.54
$\log \frac{1}{2} \gamma$	= 5.5420182			

$$D = 1.0298308 - [8.2302547] \cos \varepsilon' + [5.8584494] \cos^2 \varepsilon' + [8.6834322] f \cos F$$

The circumference will be divided into eight parts with reference to g', the mean anomaly of Neptune. For three points of division we have

We get the following table of values of D, $\log f$, and F:

g'	D	$\log f$	F-g'		g'
ю				,	11
0	1. 0271856	9. 5383650	31	3	45.80
45	1.0217845	9. 5368144	31	33	22. 27
90	1.0211885	9. 5368308	31	56	48. 30
135	1.0257276	9. 5381879	31	56	6. 93
180	1.0326568	9. 5395481	31	33	35.96
225	1.0379352	9. 5403230	31	6	29.59
270	1. 0385560	9. 5405918	30	48	57. 11
315	1. 0341396	9. 5400099	30	47	8. 07
s	4. 1195869	8. 1553357	125	23	7. 17
S′	4. 1195869	8. 1553352	125	23	6.86

Employing the same method as in the preceding chapter, we have the following values of $\log \alpha_i^{(n)}$:

	$\log lpha_0^{(1)}$	$\log lpha_{1}^{(1)}$	$\log lpha_2^{(1)}$	$\log lpha_3^{(1)}$	$\log lpha_4^{(1)}$	$\log lpha_{5}^{(1)}$	$\log lpha_6^{(1)}$
(0)	0.0038932	8. 9430342	8. 0571682	7. 2167845	6. 397480	5. 59035	4. 79117
(1)	0. 0050731	8. 9450050	8. 0599259	7. 2203281	6. 401808	5. 59546	4. 79706
(2)	0. 0052126	8. 9454332	8.0606412	7. 2213302	6. 403097	5. 59705	4. 79894
(3)	0. 0042225	8. 9438341	8. 0584363	7. 2185203	6. 399684	5. 59303	4. 79431
(4)	0. 0026867	8. 9406253	8. 0535630	7. 2119846	6. 391486	5. 58317	4. 78279
(5)	0. 0015122	8. 9379116	8. 0493179	7. 2062100	6. 384182	5 · 57433	4.77243
(6)	0.0013828	8. 9377920	8. 0492080	7. 2061098	6. 384092	5. 57425	4.77235
(7)	0.0023676	8. 9401337	8. 0528997	7. 2111498	6. 390480	5. 58199	4. 78144
S	0. 0131753	5. 7668847	2. 2205804	88. 8562091	85. 576155	82. 34482	79. 14525
S'	0. 0131754	5. 7668844	2. 2205798	88. 8562082	85. 576154	82. 34481	79. 14524
	$\log \alpha_0^{(3)}$	$\log lpha_{\scriptscriptstyle 1}^{^{(3)}}$	$\log \alpha_2^{(3)}$	$\log \alpha_3^{(3)}$	$\log lpha_4^{(3)}$	$\log lpha_5^{(3)}$	$\log lpha_6^{(3)}$
(0)	0.0314812	9. 4412053	8. 7749893	8. 0790296	7. 368805	6. 64838	5. 92143
(1)	0. 0350934	9. 4455847	8. 7801476	8. 0855698	7.375529	6.65590	5. 92973
(2)	0. 0355384	9. 4463096	8. 7811567	8. 0868642	7. 377108	6.65776	5. 93188
(3)	0. 0325122	9. 4426928	8. 7769403	8. 0820459	7. 371687	6. 65172	5. 92523
(4)	0. 0277517	9. 4363094	8. 7689093	8. 0723610	7. 360346	6. 63873	5. 91058
(5)	0. 0240883	9. 4311526	8. 7622367	8. 0641668	7. 350628	6.62750	5. 89782
(6)	0. 0237010	9. 4307747	8. 7618684	8. 0638081	7. 350278	6. 62715	5.89748
(7)	0. 0267786	9. 4351689	8. 7675989	8. 0708801	7.358694	6. 63690	5. 90858
S	0. 1184723	7.7545990	5.0869237	92. 3026629	89. 456537	86. 57202	83. 66137
		1	5. 0869235	92. 3026626	89.456538		

The values of the coefficients A for the development of $[D-f\cos(\varepsilon-F)]^{-\frac{1}{2}}$ and $[D-f\cos(\varepsilon-F)]^{-\frac{3}{2}}$, no division by an integer being made, are

	A ₀ ^(c)	A ₁ ^(c)	A ₁		A	(c) 2		A ₂	A ₃ ^(c)
(o) (1) (2) (3) (4) (5) (6) (7) S	1.0090047 1.0117498 1.0120748 1.0097700 1.0062056 1.0034881 1.0031891 1.0054665 4.0304742 4.0304744	+ 751301 750774 748351 745694 743211 742136 744206 + 748465 +2987069 +2987069	466 464 456 447	6655 1791 5511 8830 3915 6919	+ 5 5 5 5 5 + 5 + 20	7 13332 1915 10598 10383 1147 12219 13214 13773 18291 18290		7 100834 102386 103254 102711 100903 199111 198548 199332 103539	7 916 1352 1694 1673 1329 932 686 — 669 —4625 —4626
	A ₃	A ₄ ^(o)	A ₄ ^(*)	1	(°)	A5(*)		A(c)	A ₆
(o) (1) (2) (3) (4) (5) (6) (7) S	— 16448 16553 16560 10455 16238 16050 16059 — 16247 — 65305	-7 -1406 1491 1550 1536 1456 1369 1328 -1343 -5740 -5739	7 —2064 2035 1999 1985 1987 1998 2025 —2058 —8075 —8076		7 354 365 371 367 355 342 337 343 1417	1; 1; 1;	49 37 36 45 55 64 68	-7 61 62 62 61 60 59 -60242242	+ 7 10 13 13 10 7 5 + 5 + 35 + 35
	A (°)	A ₁ ^(c)	A ₁		A	(c) -2		A ₂	A ₃ ^(c)
(o) (1) (2) (3) (4) (5) (6) (7) S	1. 0751800 1. 0841600 1. 0852715 1. 0777355 1. 0659865 1. 0570324 1. 0560902 1. 0636007 4. 2825282 4. 2825286	+2365838 2377329 2371275 2351904 2326990 2310597 2315666 +2339952 +9379778 +9379782	1394	5037 5940 9340 1294 1283 1093	+10	7 278487 272595 265858 263505 265562 269616 274592 278783 084499	— —	7 526537 537603 542528 537181 523905 511729 508519 514979 2101489 2101492	7 — 6681 9912 12429 12219 9638 6723 4946 — 4841 —33694 —33695

	A ₃ ^(e)	A ₄	$\mathbf{A_4}^{(s)}$	A ₅ ^(c)	Á ₅	A6(0)	A ₆
(0)		-13157	— ⁷	— ⁷ 4044	—1 ⁷ 859	⁷ 829	+ 93
(1)	121374	14031	19153	4192	1712	839	138
(2)	121508	14601	18832	4266	1575	837	173
(3)	120175	14405	18610	4205	1558	825	169
(4)	117736	13554	18492	4030	1645	803	132
(5)	115727	12677	18491	3861	1756	785	92
(6)	115721	12287	18731	3812	1852	787	67
(7)	117629	1 2 4 8 7	-19124	3893	—1905	 807	+ 67
s	—474903	 53599	75379	16152	—693 1	-3256	+465
S'	-474905	53600	75378	—16151	—6931	-3256	+466

The following are the formulæ for mechanical quadratures in the case of the division of the circumference into eight parts:

If

$$\begin{array}{lll} (0.4) = Y_0 + Y_4 & (\frac{0}{4}) = Y_0 - Y_4 \\ (1.5) = Y_1 + Y_5 & (\frac{1}{5}) = Y_1 - Y_5 \\ (2.6) = Y_2 + Y_6 & (\frac{2}{6}) = Y_2 - Y_6 \\ (3.7) = Y_3 + Y_7 & (\frac{3}{7}) = Y_3 - Y_7 \\ & (0.2) = (0.4) + (2.6) \\ & (1.3) = (1.5) + (3.7) \end{array}$$

Then

$$2(c_0 + c_4) = (0.2)$$

$$2(c_1 + c_3) = (\frac{0}{4})$$

$$2(c_0 - c_4) = (1.3)$$

$$2(c_1 - c_3) = \left[(\frac{1}{5}) - (\frac{3}{7}) \right] \cos 45^\circ$$

$$4 c_2 = (0.4) - (2.6)$$

$$2(s_1 + s_3) = \left[(\frac{1}{5}) + (\frac{3}{7}) \right] \cos 45^\circ$$

$$4 s_3 = (1.5) - (3.7)$$

$$2(s_1 - s_3) = (\frac{2}{6})$$

The quantity $\frac{1}{2}y_2$ is so small that we may neglect the terms multiplied by it, and thus may take $[D-f\cos{(\varepsilon-F)}]^{-\frac{1}{2}}$ as the equivalent of $\frac{\mathbf{a}'}{\triangle}$.

Annu-ilal Lin	<u>a</u>	<u>7</u>	$\left(\frac{\mathbf{a}'}{\triangle}\right)^3$		
$Arg=i'g'+i\varepsilon$	cos. sin.		cos.	sin.	
i' i o o o o - 1 o - 2 o - 3 I + 2 I + I I o I - I I - 2	1. 0076186 -0. 0007326 +0. 0000303 0. 0000000 +0. 0000001 +0. 0000937 +0. 0013995 +0. 1493534 -0. 0001261	-0.0000090 +0.0000021 0.0000000 +0.0000002 -0.000690 +0.0044427 -0.0909814 +0.0001343	1. 07063210. 0029278 +0. 00016070. 0000002 +0. 0002899 +0. 0045952 +0. 46898900. 0010542 +0. 0000440	-0. 0025664 +0. 0000170 -0. 0000005 +0. 0000018 -0. 0002370 +0. 0145895 -0. 2857182 +0. 0003051 -0. 0000217	
I— 3 I— 4		-0,000001	0, 0000001	0, 0000000	

Arg=i'g'+ie	i Z	7	(<u>ā</u>	r',) 8
	cos.	sin.	0087	sin.
i' i 2+ I 2 0 2- I 2- 2 2- 3 2- 4 3 0 3- I 3- 2 3- 3 3- 4 3- 5 4- 2 4- 3 4- 4	+0. 00000110. 0000134 +-0. 01041450. 0000045 +-0. 0000001 +-0. 0000001 +-0. 00000410. 0000310. 00000310. 00000310. 00004570. 00002870	+0. 0000002 +0. 0000003 +0. 0004056 -0. 0201770 +0. 0000399 -0. 0000002 +0. 00000066 -0. 0001271 -0. 0032652 +0. 0000074 -0. 0000003 +0. 00000011 -0. 0000609 -0. 0004038	+0. 00000510. 0000488 +0. 0068064 +0. 05422490. 0001415 +0. 0000015 +0. 0000049 +0. 00234600. 0016847 +0. 0000148 0. 0000000 +0. 0000193 +0. 00043750. 0026800	+0.000017 -0.0000359 +0.0029958 -0.1050745 +0.0002640 -0.000011 +0.0000406 -0.0005665 -0.0237452 +0.0000741 -0.000030 +0.0000132 -0.0004838 -0.0037689
4— 5 4— 6	+0.0000013	+0.0000008	+0.0000131 -0.0000003	+0.0000120 -0.0000006
5— 3 5— 4 5— 5 5— 6	+0.0000009 +0.0000014 0.0000708 +0.0000004	0. 0000003 0. 0000148 0. 0000304 0. 0000001	+0.0000088 +0.0000250 -0.0008076 +0.0000040	-0. 0000005 -0. 0001573 -0. 0003465 +0. 0000005
6— 4 6— 5 6— 6 7— 5 7— 6	+0. 0000002 -0. 0000013 -0. 0000121 0. 0000000 -0. 0000004	-0. 0000002 -0. 0000026 +0. 0000017 -0. 0000001 -0. 0000003	+0.0000022 -0.0000145 -0.0001628 +0.0000002 -0.0000066	-0. 0000017 -0. 0000334 +0. 0000233 -0. 0000008 -0. 0000045

These expressions are now changed into others dependent on the argument i'g'+ig. The formulæ and data for this transformation have already been given (pages 52, 53).

Arg=i'g'+ig	<u> </u>	v Ā	(<u>a'</u>)³		
	cos.	sin.	cos.	sin.	
i' i o o o o - 1 o - 2 o - 3 I + 2	1. 0076363 -0. 0007335 +0. 0000125 +0. 0000010	-0.0000091 +0.0000019 +0.0000001	1. 0707027 —0. 0029329 +0. 0000898 +0. 0000049 +0. 0000033	0. 0025664 0. 0000448 0. 0000019 0. 0000013	
1 0	+0.0000502 -0.0022054	o. 0000431 o. 0066390	+0.0001533 -0.0067243	-0.0001539 -+0.0214871	

<u></u>			1	-		
Arg=i'g'+ig		<u>a'</u> ∆	$\left(\frac{\mathbf{a}'}{\triangle}\right)$	$\left(\frac{\mathbf{a}'}{\triangle}\right)^3$		
Alg—ly Ţiy	cos.	sin.	cos.	sin.		
i' i						
I— I	+0. 1492726	—0. 0909350	+o. 4687669	—о. 2855666		
I 2	+0.0034722	-0.0020578	+0.0102446	-o. oo6578o		
I— 3	+0.0001299	-0.0000728	+0.0004016	0.0002558		
I— 4	+0.0000055	0. 0000034	+0.0000183	-0. 0000115		
2+ 1	+0.0000007	+0.0000001	+0.0000028	+0.0000013		
2 0	0. 0000506	—0. 0000095	0.0002131	0.0001082		
2 I	+0.0010373	+0.0013786	+0.0041871	+0.0080620		
2 2	+0.0104277	-0. 0201231	+0. 0542730	-0. 1047770		
2 — 3	+0.0004978	-0.0009306	+0.0024736	0.0047896		
2— 4	+0.0000246	-0.0000451	+0.0001224	-0.0002355		
2— 5	+0.0000013	-0.000022	+0.0000063	0.0000121		
3 o	0. 0000000	0.0000004	+0.0000014	o. 000002I		
3— т	0. 0000127	+0.0000099	-0. 0001097	+0.0000472		
3— 2	+0.0003605	+0.0001094	+0. 0024622	+0.0011523		
3— 3	-0.0002138	-0.0032549	0. 0015644	-0.0236554		
3 4	0. 0000123	0.0002282	-0.0001012	0.0016378		
3— 5	0. 0000007	0.0000138	-0.0000057	0. 0000991		
3— 6	0. 0000000	-0.000007	0. 0000003	—0.0000059		
4— I	0.0000000	—0. 0000002	—0. 0000004	0.0000013		
4— 2	0. 0000009	+0. 0000046	0. 0000186	+0.0000393		
4 3	+0.0000732	-0.0000216	+0.000694 1	0.0001179		
4— 4	0. 0002812	-0.0004045	0, 0026252	-0.0037701		
4 5	-0. 0000257	0.0000382	-0.0002419	0.0003512		
4 6	-0.0000018	0.0000027	0.0000172	0.0000252		
4— 7	į		-0.0000011	0. 0000017		
5— 3	+0.0000006	+0.0000010	+0.0000028	+0.0000131		
5— 4	+0.0000100	0.0000112	+0.0001223	-0.0001142		
5— 5	0 . 000069 7	-0.0000314	-0.0007941	0.0003567		
5— 6	—0. 00000 80	-0.000038	0. 0000923	0. 0000420		
5— 7	o. oooooo7	-0.0000003	-0.0000076	0.0000034		
6 4	+0.000004	+0.0000001	+0.0000028	+0.0000025		
6— 5	+0.0000004	-0.0000029	+0.0000093	0.0000365		
6— 6	0.0000121	+0,0000014	0. 0001611	+0.0000188		
6— 7	-0.0000017	+0.0000003	-0, 0000233	+0.0000029		

There are now computed certain values of the Besselian function $J_l^{(i)}$ corresponding to the multiples of half of the eccentricity of Neptune's orbit, by the method of page 52.

	Values of $\log J_i^{(i)}$								
i	$l=\frac{1}{2}e'$	l=e'	$l = \frac{3}{2}e'$						
o	9.9999922	9.9999686	9.9999295						
1	7.6281908	7.9292090	8.1052808						
2	4.9554	5.5574	5.9096						
3	2.1064	3.0095	3.5378						

With these we obtain the expressions for the two multipliers of $\left(\frac{\mathbf{a}'}{\Delta}\right)^{\mathbf{c}}$

$$\frac{1}{2} \left[\frac{r'^2}{a'^2} - \alpha^2 \frac{r^2}{a^2} \right] = \begin{bmatrix} 9.6857724 \end{bmatrix}$$

$$+ 2[6.85846] \cos (-g) - 2[7.62819] \cos g'$$

$$+ 2[4.9396] \cos (-2g) - 2[4.9553] \cos 2g'$$

$$\frac{r'}{a'} \sin (f' + II') = \begin{bmatrix} 7.97234 \end{bmatrix}$$

$$- 2[9.5293508] \sin g' - 2[9.5659853] \cos g'$$

$$- 2[7.15754] \sin 2g' - 2[7.19417] \cos 2g'$$

The expressions for the products are

Ann i/a l ia	$\frac{1}{2} \left[\frac{r'^2}{a'^2} - \epsilon \right]$	$2^2 \frac{r^2}{a^2} \left(\frac{a'}{\triangle} \right)^2$	$\begin{vmatrix} \mathbf{Arg} = i'g' + ig \end{vmatrix}$	$\frac{1}{2} \left[\frac{r'^2}{\mathbf{a}'^2} - c c^2 \frac{r^2}{\mathbf{a}^2} \right] \left(\frac{\mathbf{a}'}{\triangle} \right)^8$		
Arg=i'g+ig	DOB.	sin.	Aig, y 7-,y	cos.	sin.	
i' i o o o o o o o o o o o o o o o o o o	+0. \$193540 -0. 0018686 +0. 0000161 +0. 0000012 +0. 0000011 +0. 0000818 -0. 0120187 +0. 2273652 +0. 0050765 +0. 0001958 +0. 0000088 +0. 0000066 -0. 0000906 +0. 0000790 +0. 0262751 +0. 0012440 +0. 0000620 +0. 0000032 +0. 0000016 -0. 0000734	-0. 0000325 +0. 0000053 +0. 0000002 -0. 0000011 -0. 0000751 +0. 0102154 -0. 1385221 -0. 0029533 -0. 0001108 -0. 0000013 -0. 0000013 -0. 0050475 -0. 0507951 -0. 0022972 -0. 0001116 -0. 0000057 -0. 00000017 -0. 00000081	i' i 3-3 3-4 3-5 3-6 4-1 4-2 4-3 4-4 4-5 4-6 4-7 5-3 5-4 5-5 5-6 5-7 6-4 6-5 6-6 6-7	-0. 0007705 -0. 0000395 -0. 0000019 0. 0000000 +0. 0000200 +0. 0003415 -0. 0012736 -0. 0001158 -0. 0000005 -0. 0000005 -0. 0000014 +0. 0000699 -0. 0000446 -0. 0000037 +0. 0000009 +0. 0000078 -0. 0000114	-0. 0114533 -0. 0007946 -0. 0000479 -0. 0000029 -0. 0000009 +0. 0000151 +0. 0000123 -0. 0000123 -0. 0000008 +0. 0000070 -0. 0000397 -0. 0001714 -0. 000017 -0. 000017 -0. 0000162 +0. 0000013 +0. 0000014	
3— 2	+0.0009624	+o. ooog868				

Arg.	$\frac{r'}{a'}\sin\left(f'+\Pi'\right)\left(\frac{a'}{\triangle}\right)^{s}$			
	sin.	cos.		
i' i		+0.0052523		
0 1	+0. 2635842	0.0759927		
0— 2	+0.0061272	0.0014797		
o 3	+0.0002412	-0.0000582		
0— 4	+0.0000110	0. 0000027		

For the computation of $a' \frac{r}{r'^2}H$ we have

$$\log h = 9.1695601$$
 $\log l = 8.9536702$ $\log h_1 = 9.1690072$ $\log h_2 = 8.9542630$

And the expression for $a'\frac{r}{r'}H$ follows

Arg=i'g'+ig	-a'	$-{a'}_{r'2}^T$ H		$-a'rac{r}{r'^3}H$		
	cos.	sin.	Arg=i'g'+ig	CO8.	sin.	
i' i 1+ 2 1+ 1 1 0 1- 1 1- 2 1- 3 1- 4 1- 5 2+ 1	-0.000008 -0.0000497 +0.0106923 -0.1475785 -0.0035576 -0.0001286 -0.0000055 -0.0000003	+0.0000007 +0.0000360 -0.0065130 +0.0898888 +0.0021669 +0.0000784 +0.0000034 +0.0000002 +0.0000006	i' i 2 0 2— I 2— 2 2— 3 3 0 3— I 3— 2 4— I	+0.0001817 -0.0025076 -0.0000604 -0.0000022 +0.0000026 -0.0000360 -0.0000009	-0.0001107 +0.0015274 +0.0000368 +0.0000013 -0.0000016 +0.0000219 +0.0000005	

The logarithms of the factors which depend on the mass of Neptune are

$$\log \mu = 0.2576408$$
 $\log (\mu \alpha \sin J) = 7.7144717$

The expressions for the forces are

Arg=i'g'+ig	a ^c	$rac{d\Omega}{dy}$	ar	$rac{d\Omega}{dr}$
	sin.	cos.	cos.	sin.
i' i	"	,	,, +0.028117	11
o— 1	0.0013275	+0.0000165	-0.002718 2	+0.0000507
0— 2	+0.0000452	0. 0000069	+0.0000179	+0.0000079
1+1	-0.000001	0.000013	+0.000013	-0.000032
10			0, 000405	+0.000693
I I	+o. oo3o66	+0.001893	+0.009321	-0. 005730
1 2	0. 000309	0. 000395	—0. 000393	+0.000439
I 3	+0.000007	-0.000014	- -0.000004	+0.000010
2 0			+0.000211	0, 000443
2— I	0. 002661	0.005259	—o. oo5334	+0.010652
2— 2	+0. 037527	+0.072707	+o. o38008	0. 073655
2 — 3	+0, 002691	+0.005046	+0.001797	-0.003313
2 4	+0.000177	+0.000326	+0.000089	0.000161
2— 5	+0.000012	+0.000020	0, 000000	0. 000008

Arg=i'g'+ig	$a\frac{d}{d}$	$rac{d\Omega}{dg}$	ar	$rac{d\Omega}{dr}$
	sin.	cos.	cos.	sin.
i' i 3 0	"	"	+0.000008	,, o, 000006
3— 1	0, 000088	0. 000058	— 0. 000187	+0.000016
3— 2	+0.001302	—о. 000398	+0.001414	+o. oo 1688
3— 3	-0.001161	+0.017672	0 001201	—0. 017 7 83
3 4	—0. 0000 89	+0.001652	0. 000060	-0.001231
3— 5	о. 000006	+0.000125	0.000000	-0. 000074
3— 6	0.000000	+0.000007		
4 2	0.000003	0.000017	—o. oooo35	+0.000023
4— 3	+0.000397	+0.000117	+0.000552	+0.000093
4— 4	0. 002036	+0.002928	-0.002051	0. 002931
4 5	0.000233	+0.000346	—о. 000186	-0.000275
4 6	0. 000019	+0.000030	0.000013	-0.000020
5— 3	+0,000003	-0.000005	0.000000	+0.000012
5 4	+0.000072	+0.000081	+0.000117	0.000062
5 5	0. 000631	+0.000284	0. 000632	-0, 000282
5— 6	0. 000087	+0.000042	0. 000074	-0, 000034
5— 7	—0. 000009	+0.000004	—o. ooooo6	0, 000000
6— 4	+0.00000 3	0. 000001		
6— 5	+0.000004	+0.000026	+0.000014	-0.000027
6 6	0.000131	-0.000015	0.000130	+0.000015
6— 7	0 000021	0.000002	0.000019	0.000000

Arg.	a^2	$rac{d\Omega}{dZ}$
	sin.	cos.
i' i	n.	+0.000034
o— 1	+0.0013659	-0.0003937
0— 2	+0,000032	-0.00008
0— 3	+0.000001	0.000000

The expressions for the multipliers A, B, and C have already been given (page 73), and we obtain the following expressions for T and $\frac{1}{n} \frac{d\mathbf{R}}{dt}$:

Ana-witilal ta	7	r	A no	ا فاما ا فم		r
$Arg = \varkappa \gamma + i'g' + ig$	sin.	cos.	Arg=μγ	+ <i>i y</i> + <i>i y</i>	sin.	COS.
ж i' i I 0— I	,, —o. 05597	// 0. 00002		i' i 3— 2	o. 00391	+0.00119
_r o o	-0.0040184	+0.0000833		3-3	+0.00136	-0.00167
0 0— 1	+0.00398	-0.00005		3-2	—o. oo365	+0.05327
I 0— 2	-0.00131	-0.00002		3-3	+0.00348	—o. 05302
i o i	+0.00020	0.00004		3-3	-0.00111	+0.01739
0 0— 2	-0.00014	+0.00002		3-3	-0.00013	+0.00284
I 0-3	+0.00006	0.00000		3-3-4	+0.00027	-o. 00496
			H	3-5	-0.00012	+0.00206
-I I+ 2	+0.00001	0, 00002		3- 3	0. 00000	+0.00015
0 1+1	0,00000	+0.00004		3-5	+0.00002	-0.00037
IIO	0.00000	-0.00004	li .	3- 6	0.0000I	+0.00018
I I+ I	0.00012	-0.00050	1	, ,		,
I I— I	-0.00019	+0,00032	ł	4— I	0,00002	-0.00005
-I I O	+0.01544	+0.00949	0	4— 2	+0.00001	+0.00005
0 1—1	0. 00920	o. oo568	I	4-3	0,00001	0,00002
I I-2	-0.00313	-0.00187	-1	4 2	+0.00125	+0.00028
—I I— I	-0.00115	-0,00132	0	4-3	—0. 00119	o. ooo35
0 I— 2	+0.00093	+0.00118	1	4-4	+0.00055	-0,00010
1 I— 3	0.00038	0. 00044	1	4 3	—0. 00617	+o. oo88o
—I I— 2	+0.00004	0,00000	0	4-4	+0.00611	-0.00878
o I— 3	-0.00002	+0.00004	I	4- 5	-0.00200	+0.00288
I I 4	0, 00000	0.00002	-1	4 4	0. 00046	+0.00069
—I 2+ I	+0.00007	+0.00015	0	4- 5	+0.00070	-0.00104
I 2— I	+0.00024	+0.00046	1	4 6	0. 00028	+0.00041
—I 2 0	0.00883	0. 01766	1	4- 5	—0. 00002	+0.00005
0 2— I	+0.00798	+0.01578	0	4— 6	+o. oooo6	—o. oooog
I 2— 2	-o. 00545	-0.01045	1	4-7	0. 00004	+0.00004
—I 2— I	+0.11348	+0. 21990	I	5 3	+0.00024	+0.00023
0 2-2	-o. 11258	-0. 21812	0	5 4	-0.00022	-0.00024
I 2— 3	+o. o368o	+0.07128	1	5— 5	+0.00012	+0.00006
_1 2— 2	+0.00358	+0.00643	r	5— 4	0.00192	+0.00085
0 2-3	_o. oo8o7	-0.01514	0	5— 5	+0.00189	-0.00085
1 2-4	+0.00356	+0.00672	ı	5 6	0. 00062	+0.00028
I 2 3	+0.00017	+0.00028	∥ _ı	5 5	-0.00018	+0.00009
0 2-4	_o. ooo53	0. 00098		5 6	+0.00026	-0.00013
I 2— 5	+0.00028	+0.00051	1	5— 7	-0,00012	+0.00006
—I 2— 4	0.00000	+0.00001				1
0 2— 5	-0.00004	-0.00006	I	6— 4	+0.00001	+0.00008
I 2-6	+0.00002	+0.00004	II	6 5	-0.00001	0. 00008
				6— 6	+0.00001	+0.00002
—I 3 O	0,00031	-0.00016	11	6— 5	-0.00039	0.00005
o 3— 1	+0.00026	+0.00017	!!	6— 6	+0,00039	+0.00004
1 3-2	—o. ooo18	-0.00001	I	6— 7	0.00013	-0.00001
—1 3— 1	+0.00398	—o. oo162				
		<u> </u>]			<u> </u>

 $\frac{1}{n} \frac{d\mathbf{R}}{dt} = +0''.0006825 \cos{(-\gamma)} +0''.0001987 \sin{(-\gamma)}$

The logarithms of the integrating factors follow:

Arg.	$\log \frac{n}{i'n'+in}$	Arg.	$\log \frac{n}{i'n'+in}$	Arg.	$\log \frac{n}{i'n'+in}$	Arg.	$\log \frac{n}{i'n'+in}$
i' i o I O 2 O 3 I + I I O I - I I - 2 I - 3 2 - I	0. 00000n 9. 69897n 9. 52288n 9. 96981 1. 14275 0. 03245n 9. 71489n 9. 53343n 9. 94158	i' i 2 0 2— I 2— 2 2— 3 2— 4 2— 5 3 0 3— I 3— 2	o. 84172 o. 06751n 9. 73142n 9. 54424n 9. 41386n 9. 31372n 0. 66563 0. 10566n 9. 74860n	i' i 3-3 3-4 3-5 3-6 4-1 4-2 4-3 4-4 4-5	9. 55532n 9. 42204n 9. 32021n 9. 23777n 0. 14749n 9. 76649n 9. 56670n 9. 43039n 9. 32679n	i' i 6 5-3 5-4 5-5 5-6 5-7 6-4 6-5 6-6	9. 24321n 9. 5784n 9. 4389n 9. 3335n 9. 2487n 9. 1778n 9. 4476n 9. 3403n 9. 2542n 9. 1825n

In integrating we put

$$k_0 = + \circ''.0560$$
 $k_1 = - \circ''.0060$ $k_2 = + \circ''.0001$

$$k_2 = + 0''.0001$$

Arg=i'g'+-ig	$rac{d\delta}{dt}$		$\frac{1}{n} \stackrel{d}{\stackrel{d}{\stackrel{d}{\stackrel{d}{\stackrel{d}{\stackrel{d}{\stackrel{d}{d$	$rac{l u}{l t}$
	cos.	sin.	sin.	cos.
i' i	11	"	"	0.0000010
o— 1	0, 0040	0.0001	+0.0040	0.0000
	+0.0000833nt	0. 0040184 <i>nt</i>	-0.0000416nt	0.0020092nt
0— 2	0.0000	0.0000	0.0000	0. 0000
	+0.0000020nt	—0. 0000968 <i>nt</i>	—0. ∩000020 <i>nt</i>	—0. 0000968nt
1+1	0. 0000	-0.0005	0, 0000	+0.0003
1 0	-0.00013	0.00079	0.00020	0. 00008
1— 1	—o. 2259	+o. 1389	+o. 1064	+0.0654
I— 2	o. oo6o	+0.0042	+0.0057	+ 0.0038
r— 3	-0.0002	+0.0001	+0.0003	+0.0002
2 0	+0.00016	-0. 00029	+0.00012	+0.00023
2— 1	+0.0680	-o. 1361	-0.0319	-o. o635
2— 2	+o. o863	-o. 1674	-o. o614	0. 1189
2— 3	+0.0033	-o. oo62	0.0038	-0.0072
2— 4	+0.0002	0, 0002	-0.0002	-0.0003
3— 1	+0.0016	0. 0009	o. ooo8	-0.0004
3— 2	+0.0034	+0.0019	0. 0023	+0.0008
3 3	—o. ooog	o. o155	+o. ooo8	-o. o126
3 4	+0.0001	0.0008	0.0000	-0.0010
4— 3	+0.0004	-0.0001	-0.0003	0.0001
4— 4	0.0011	0.0014	+0.0009	-0.0013
4 5	0.0001	-0,0002	+0.0002	-0.0002

In fine, for the perturbations of Jupiter by Neptune we have

Arg=i'g'''+ig	n	5 <i>z</i>		ν	u cos i		
	sin.	cos.		sin.	sin.	cos.	
i' i	" "		 0. 0093	"	"	"	
1			-0.0000010nt			-0. 0000494 <i>nt</i>	
o— 1	0.0000	0.0000	+0.0020	0,0000			
l	o. 0000833nt	-0. 0040184 <i>nt</i>	0.0000416nt	+0.0020092nt	+0.0001987 <i>nt</i>	+0.0006825nt	
0 2	-0.0000010nt	0. 0000484 <i>nt</i>	-0.0000010nt	+0.0000484nt	+0.0000048nt	+0.0000165nt	
1+1	0. 0000	+0.0005	0.0000	+0.0003			
1 0	-0.0018	+0.0110	+ 0. 0028	-0.0011			
1 1	+0. 2434	+0. 1497	+o. 1147	0. 0705			
1 2	+0.0031	+0.0022	+0. 00 30	-0.0020			
2 0	+0.0011	+0.0020	 0. 00 08	+0.0016			
2 I	0. 0794	0. 1590	- 0. 0373	+0.0742			
2 2	— 0. 0465	-0.0902	o. o331	+0.0641			
2— 3	-0.0012	0. 0022	0.0013	- -0.0025			
3— 1	0. 0020	0.0011	o. oo1o	+0.0005			
3— 2	-0.0019	+0.0011	0, 0013	0, 0004			
3— 3	+0.0003	0.0056	+0.0003	+0.0045			
3 4	0.0000	0.0002	0.0000	+0.0003	!		
4— 3	0. 0001	0. 0000	-o. ooo1	0,0000			
4— 4	+0.0003	-o. ooo4	+0.0002	+o. 0 004			

CHAPTER VII.

PERTURBATIONS OF JUPITER AND SATURN BY THE FOUR INTERIOR PLANETS.

Here we need take account only of the secular terms, the constant terms of ν , and, in the action of Venus and the Earth, of the terms of $n\delta z$ and ν , which depend on the single multiple of the elongation of the disturbing planet from the disturbed. The terms to be derived are so few and small that they may most readily be got by an algebraical development of $\frac{\mathbf{a}'}{\triangle}$.

The elements of the interior planets for the epoch 1850,0 needed for the computation are

	Mercury.	Venus.	Earth.	Mars.
π	75° 7′ 13″.62	129° 27′ 42″.83	100° 21′ 39″.73	333° 17′ 51″.74
$oldsymbol{i}$	7° 0′ 7″.71	3° 23′ 35″.01	0 0 0	1° 51′ 2″.24
ស	46° 33′ 8″.63	75° 19′ 53″.08		48° 23′ 54″.59
e	0.20560476	0.00684311	0.01677114	0.09326803
776	5381016".260	2106641".357	1295977".416	689050".784
log a	9.5878217	9. 8593378	0.0000000	0.1828971
m	I		<u> </u>	I
***	5000000	425000	322800	3093500

Action of Mercury on Jupiter.

In this case

$$\log \alpha = 8.8715885 \quad \log b_{\frac{1}{2}}^{(0)} = 0.30163 \qquad \log b_{\frac{1}{2}}^{(1)} = 8.87249 \qquad \log \alpha b_{\frac{3}{2}}^{(1)} = 8.22481$$

$$\log \alpha \frac{db_{\frac{1}{2}}^{(0)}}{d\alpha} = 7.74588 \qquad \log \alpha \frac{db_{\frac{1}{2}}^{(1)}}{d\alpha} = 8.87430 \qquad \log \alpha^2 \frac{d^2b_{\frac{1}{2}}^{(0)}}{d\alpha^2} = 7.75129 \qquad \log \alpha^2 \frac{d^2b_{\frac{1}{2}}^{(1)}}{d\alpha^2} = 6.9720$$

The constant term of ν is given by the formula

$$\nu = \frac{1}{6} \frac{m}{\mu'} \left[b_{\frac{1}{2}}^{(0)} + \alpha \frac{db_{\frac{1}{2}}^{(0)}}{d\alpha} \right]$$

and in this case is

$$\nu = + o''.o138$$

We have also the following terms in $\frac{a'}{\triangle}$

$$\frac{a'}{\Delta} = [7.32172](e^2 + e'^2) - [7.92378]\sin^2\frac{1}{2}J - [6.59106]ee'\cos(\Pi' - \Pi)$$

In which we have

$$\log \sin \frac{1}{2} J = 8.7391$$
 $II' - II = 296^{\circ} 43'$

From this expression it is easy to find that the secular terms of $n\delta z$, ν , and $\frac{u}{\cos i}$ are

$$n\delta z = -0.000059nt \sin (-g) - 0.0000137nt \cos (-g)$$

$$v = -0.0000030nt \cos (-g) + 0.0000069nt \sin (-g)$$

$$\frac{u}{\cos i} = +0.0000080nt \sin (-g) - 0.0000171nt \cos (-g)$$

Action of Venus on Jupiter.

In this case

$$\log \alpha = 9.1431046 \qquad \log b_{\frac{1}{2}}^{(0)} = 0.30315 \qquad \log b_{\frac{1}{2}}^{(1)} = 9.14628 \qquad \log b_{\frac{1}{2}}^{(2)} = 8.16479$$

$$\log \alpha \frac{db_{\frac{1}{2}}^{(0)}}{d\alpha} = 8.29574 \qquad \log \alpha \frac{db_{\frac{1}{2}}^{(1)}}{d\alpha} = 9.15264 \qquad \log \alpha \frac{db_{\frac{1}{2}}^{(2)}}{d\alpha} = 8.46937$$

$$\log \alpha^2 \frac{d^2b_{\frac{1}{2}}^{(0)}}{d\alpha^2} = 8.31457 \qquad \log \alpha^2 \frac{d^2b_{\frac{1}{2}}^{(1)}}{d\alpha^2} = 7.79914 \qquad \log \alpha^2 \frac{d^2b_{\frac{1}{2}}^{(2)}}{d\alpha^2} = 8.48344$$

$$\log \alpha^2 \frac{d^3b_{\frac{1}{2}}^{(0)}}{d\alpha^3} = 7.43109 \qquad \log \alpha^2 \frac{d^3b_{\frac{1}{2}}^{(1)}}{d\alpha^3} = 7.83341 \qquad \log \alpha^2 \frac{d^3b_{\frac{1}{2}}^{(2)}}{d\alpha^3} = 7.47526$$

$$\log \alpha^4 \frac{d^4b_{\frac{1}{2}}^{(0)}}{d\alpha^4} = 7.48662 \qquad \log \alpha^4 \frac{d^4b_{\frac{1}{2}}^{(1)}}{d\alpha^4} = 7.20768 \qquad \log \alpha^4 \frac{d^4b_{\frac{1}{2}}^{(2)}}{d\alpha^4} = 7.52801$$

$$\log \alpha b_{\frac{1}{2}}^{(1)} = 8.77923 \qquad \log \alpha^2 b_{\frac{1}{2}}^{(0)} = 8.63965$$

$$\log \alpha^2 \frac{db_{\frac{1}{2}}^{(0)}}{d\alpha} = 8.41003 \qquad \log \alpha^2 \frac{db_{\frac{1}{2}}^{(1)}}{d\alpha} = 8.81022 \qquad \log \alpha^2 b_{\frac{1}{2}}^{(0)} = 7.54622$$

$$\log \alpha^2 \frac{d^2b_{\frac{1}{2}}^{(0)}}{d\alpha^2} = 8.46044 \qquad \log \alpha^2 \frac{d^2b_{\frac{1}{2}}^{(1)}}{d\alpha^2} = 8.14175 \qquad \log \alpha^2 \frac{db_{\frac{1}{2}}^{(2)}}{d\alpha} = 8.38980$$

The constant term of ν is

$$\nu = + 0''.1640$$

The non-periodic portion of $\frac{\mathbf{a}'}{\triangle}$ contains the following terms:

$$\frac{\mathbf{a}'}{\triangle} = [7.87614] (e^{2} + e'^{2}) \qquad -[8.47820] \sin^{2} \frac{1}{2} \mathbf{J} \qquad -[7.41622] ee' \cos (\Pi' - \Pi)$$

$$+ [8.53188] \sin^{4} \frac{1}{2} \mathbf{J} \qquad +[6.03454] e^{4} \qquad +[8.08876] e^{2} e'^{2}$$

$$+ [7.99054] e'^{4} \qquad -[8.69081] (e^{2} + e'^{2}) \sin^{2} \frac{1}{2} \mathbf{J} \qquad -[7.32535] e^{3} e' \cos (\Pi' - \Pi)$$

$$-[7.83041] ee'^{3} \cos (\Pi' - \Pi) + [8.48167] ee' \sin^{2} \frac{1}{2} \mathbf{J} \cos (\Pi' - \Pi) + [6.69417] e^{2} e'^{2} \cos 2(\Pi' - \Pi)$$

$$+ [8.89363] e^{2} \sin^{2} \frac{1}{2} \mathbf{J} \cos 2\Pi - [8.21647] ee' \sin^{2} \frac{1}{2} \mathbf{J} \cos (\Pi' + \Pi) + [6.93763] e'^{2} \sin^{2} \frac{1}{2} \mathbf{J} \cos 2\Pi'$$

$$-[7.41622] ee' \cos (\Pi' - \Pi)$$

In which we have

$$J = 2^{\circ} 15' 11''.34$$
 $II' = 310^{\circ} 4' 23''.11$ $II = 67^{\circ} 36' 52''.64$

From this expression we find

$$-\frac{1}{e'}\frac{d\left(\frac{\mathbf{a}'}{\triangle}\right)}{d\Pi'} = +0.0000158$$

$$-\frac{d\left(\frac{\mathbf{a}'}{\triangle}\right)}{de'} = -0.0007369$$

$$\frac{d\left(\frac{\mathbf{a}'}{\triangle}\right)}{dJ} = -0.0005933$$

$$\frac{1}{\sin J}\left[\frac{d\left(\frac{\mathbf{a}'}{\triangle}\right)}{d\Pi'} + \cos J\frac{d\left(\frac{\mathbf{a}'}{\triangle}\right)}{d\Pi'}\right] = +0.0000001$$

From these four quantities it is easy to conclude that the secular terms are

$$n\delta z = -0.0000153nt \sin (-g) - 0.0007144nt \cos (-g)$$

$$v = -0.0000077nt \cos (-g) + 0.0003572nt \sin (-g)$$

$$\frac{u}{\cos i} = +0.0002201nt \sin (-g) - 0.0001852nt \cos (-g)$$

The terms of $n\delta z$ and ν , which depend on the elongation of Venus from Jupiter, are*

$$n\delta z = + \circ''.0675 \sin(9 - 4) \qquad \qquad \nu = + \circ''.0675 \cos(9 - 4)$$

Action of the Earth on Jupiter.

In this case

$$\log \alpha = 9.2837668 \qquad \log b_{\frac{1}{2}}^{(0)} = 0.30511 \qquad \log b_{\frac{1}{2}}^{(1)} = 9.28988 \qquad \log b_{\frac{1}{2}}^{(1)} = 8.44939$$

$$\log \alpha \frac{db_{\frac{1}{2}}^{(0)}}{d\alpha} = 8.58591 \qquad \log \alpha \frac{db_{\frac{1}{2}}^{(1)}}{d\alpha} = 9.30214 \qquad \log \alpha \frac{db_{\frac{1}{2}}^{(2)}}{d\alpha} = 8.75728$$

$$\log \alpha^2 \frac{d^3b_{\frac{1}{2}}^{(0)}}{d\alpha^2} = 8.62181 \qquad \log \alpha^2 \frac{d^3b_{\frac{1}{2}}^{(1)}}{d\alpha^2} = 8.23752 \qquad \log \alpha^2 \frac{d^3b_{\frac{1}{2}}^{(2)}}{d\alpha^2} = 8.78433$$

$$\log \alpha^3 \frac{d^3b_{\frac{1}{2}}^{(0)}}{d\alpha^3} = 8.02093 \qquad \log \alpha^3 \frac{d^3b_{\frac{1}{2}}^{(1)}}{d\alpha^3} = 8.30187 \qquad \log \alpha^3 \frac{d^3b_{\frac{1}{2}}^{(2)}}{d\alpha^3} = 8.06368$$

$$\log \alpha^4 \frac{d^4b_{\frac{1}{2}}^{(0)}}{d\alpha^4} = 8.12288 \qquad \log \alpha^4 \frac{d^4b_{\frac{1}{2}}^{(1)}}{d\alpha^4} = 7.95070 \qquad \log \alpha^4 \frac{d^4b_{\frac{1}{2}}^{(2)}}{d\alpha^4} = 8.16093$$

$$\log \alpha b_{\frac{1}{2}}^{(1)} = 9.07533 \qquad \log \alpha^2 b_{\frac{1}{2}}^{(0)} = 8.96871 \qquad \log \alpha^2 b_{\frac{1}{2}}^{(2)} = 8.13844$$

$$\log \alpha^2 \frac{db_{\frac{1}{2}}^{(0)}}{d\alpha} = 8.85658 \qquad \log \alpha^2 \frac{db_{\frac{1}{2}}^{(1)}}{d\alpha} = 9.13378 \qquad \log \alpha^2 \frac{db_{\frac{1}{2}}^{(2)}}{d\alpha} = 8.78328$$

$$\log \alpha^3 \frac{d^2b_{\frac{1}{2}}^{(0)}}{d\alpha^2} = 8.94979 \qquad \log \alpha^3 \frac{d^2b_{\frac{1}{2}}^{(1)}}{d\alpha^2} = 8.74229 \qquad \log \alpha^3 \frac{d^2b_{\frac{1}{2}}^{(2)}}{d\alpha^2} = 8.88564$$

The constant term of ν is

$$\nu = + 0''.2189$$

^{*} For the formulæ of computation see Mécanique Céleste, Tome I, pp. 279, 280.

The non-periodic portion of $\frac{a'}{\wedge}$ contains the following terms:

$$\frac{\mathbf{a}'}{\triangle} = \begin{bmatrix} 8.17224 \end{bmatrix} (e^2 + e'^2) & -\begin{bmatrix} 8.77430 \end{bmatrix} \sin^2 \frac{1}{2} \mathbf{J} & +\begin{bmatrix} 7.53817 \end{bmatrix} e'^2 \sin^2 \frac{1}{2} \mathbf{J} \cos 2\Pi' \\ +\begin{bmatrix} 8.87474 \end{bmatrix} \sin^4 \frac{1}{2} \mathbf{J} & +\begin{bmatrix} 6.63508 \end{bmatrix} e^4 & -\begin{bmatrix} 7.85190 \end{bmatrix} ee' \cos (\Pi' - \Pi) \\ +\begin{bmatrix} 8.30292 \end{bmatrix} e'^4 & -\begin{bmatrix} 9.01985 \end{bmatrix} (e^2 + e'^2) \sin^2 \frac{1}{2} \mathbf{J} & +\begin{bmatrix} 8.41780 \end{bmatrix} e^2 e'^2 \\ -\begin{bmatrix} 8.28145 \end{bmatrix} ee'^3 \cos (\Pi' - \Pi) +\begin{bmatrix} 8.93970 \end{bmatrix} ee' \sin^2 \frac{1}{2} \mathbf{J} \cos (\Pi' - \Pi) -\begin{bmatrix} 7.79205 \end{bmatrix} e^3 e' \cos (\Pi' - \Pi) \\ +\begin{bmatrix} 9.20601 \end{bmatrix} e^2 \sin^2 \frac{1}{2} \mathbf{J} \cos 2\Pi -\begin{bmatrix} 8.67277 \end{bmatrix} ee' \sin^2 \frac{1}{2} \mathbf{J} \cos (\Pi' + \Pi) +\begin{bmatrix} 7.28650 \end{bmatrix} e^2 e'^2 \cos 2(\Pi' - \Pi) \end{bmatrix}$$

In which we have

$$J = 1^{\circ} 18' 42''.10$$
 $\Pi' = 92^{\circ} 59' 49''$ $\Pi = 181^{\circ} 25' 20''$

From this expression we find

$$-\frac{1}{e'}\frac{d\left(\frac{\mathbf{a}'}{\triangle}\right)}{d\Pi'} = +0.0001198$$

$$-\frac{d\left(\frac{\mathbf{a}'}{\triangle}\right)}{de'} = -0.0014394$$

$$\frac{d\left(\frac{\mathbf{a}'}{\triangle}\right)}{dJ} = -0.0006832$$

$$\frac{1}{\sin J}\left[\frac{d\left(\frac{\mathbf{a}'}{\triangle}\right)}{d\Pi} + \cos J\frac{d\left(\frac{\mathbf{a}'}{\triangle}\right)}{d\Pi'}\right] = -0.0000003$$

From these four quantities it is easy to conclude that the secular terms are

$$n\delta z = -0.0001530nt \sin(-g) - 0.0018372nt \cos(-g)$$

$$v = -0.0000765nt \cos(-g) + 0.0009186nt \sin(-g)$$

$$\frac{u}{\cos i} = -0.0004354nt \sin(-g) + 0.0000230nt \cos(-g)$$

The terms of $n\delta z$ and ν , which depend on the elongation of the Earth from Jupiter, are

$$n\delta z = + o''.1225 \sin(5 - 4)$$
 $v = + o''.1225 \cos(5 - 4)$

Action of Mars on Jupiter.

In this case

$$\log \alpha = 9.4666639 \qquad \log b_{\frac{1}{2}}^{(0)} = 0.31071 \qquad \log b_{\frac{1}{2}}^{(1)} = 9.48119 \qquad \log \alpha b_{\frac{3}{2}}^{(1)} = 9.48360$$

$$\log \alpha \frac{db_{\frac{1}{2}}^{(0)}}{d\alpha} = 8.97705 \qquad \log \alpha \frac{db_{\frac{1}{2}}^{(1)}}{d\alpha} = 9.51039$$

$$\log \alpha^2 \frac{d^2b_{\frac{1}{2}}^{(0)}}{d\alpha^2} = 9.05994 \qquad \log \alpha^2 \frac{d^2b_{\frac{1}{2}}^{(1)}}{d\alpha^2} = 8.83322$$

The constant term of ν is

$$\nu = + 0^{1}.0238$$

The non-periodic portion of $\frac{a'}{\triangle}$ contains the terms

$$\frac{a'}{h} = [8.58050](e^2 + e'^2) - [9.18256]\sin^2\frac{1}{2}J - [8.44029]ee'\cos(\Pi' - \Pi)$$

In which we have

$$\log \sin J = 8.3988$$
 $II' = 8^{\circ} 24'$ $II = 329^{\circ} 46'$

Whence we conclude that the secular terms are

$$n\delta z = +0.0002138nt \sin (-g) -0.0002217nt \cos (-g)$$

$$\nu = +0.0001069nt \cos (-g) +0.0001108nt \sin (-g)$$

$$\frac{u}{\cos i} = -0.0000186nt \sin (-g) -0.0001257nt \cos (-g)$$

Action of Mercury on Saturn.

In this case

$$\log \alpha = 8.6081398$$
 $\log b_{\frac{1}{2}}^{(0)} = 0.3012$ $\log \alpha \frac{db_{\frac{1}{2}}^{(0)}}{d\alpha} = 7.2171$

The constant term of ν' is

$$\nu' = + o''.o138$$

The non-periodic portion of $\frac{a'}{\wedge}$ contains the terms

$$\frac{a'}{\triangle} = [6.7918](e^2 + e'^2) - [7.3939] \sin^2 \frac{1}{2} J - [5.7977] ee' \cos (\Pi' - \Pi)$$

In which we have

$$\log \sin J = 9.0469$$
 $\Pi' = 64^{\circ} 18'$ $\Pi = 49^{\circ} 27'$

Whence we conclude that the secular terms are

$$n'\delta z' = 0.000000n't \sin g' - 0.000005n't \cos g'$$

$$\nu' = 0.000000n't \cos g' - 0.000002n't \sin g'$$

$$\frac{u'}{\cos i'} = + 0.000005n't \sin g' + 0.000002n't \cos g'$$

Action of Venus on Saturn.

In this case

$$\log \alpha = 8.8796559 \qquad \log b_{\frac{1}{2}}^{(0)} = 0.3017 \qquad \log \alpha \frac{db_{\frac{1}{2}}^{(0)}}{d\alpha} = 7.7621$$

The constant term of ν' is

$$\nu' = \pm 0''.1624$$

The non-periodic portion of $\frac{a'}{\wedge}$ contains the terms

$$\frac{a'}{\Delta} = [7.338\circ](e^2 + e'^2) - [7.94\circ 1] \sin^2 \frac{1}{2} J - [6.6153]ee' \cos(\Pi' - \Pi)$$

In which we have

$$\log \sin J = 8.5544$$
 $\Pi' = 61^{\circ} 44'$ $\Pi = 101^{\circ} 4'$

Whence we conclude that the secular terms are

$$n'\delta z' = + 0.00002n't \sin g' - 0.000235n't \cos g'$$

$$v' = - 0.000001n't \cos g' - 0.000117n't \sin g'$$

$$\frac{u'}{\cos i'} = + 0.000067n't \sin g' - 0.000036n't \cos g'$$

The terms of $n'\delta z'$ and ν' , which depend on the elongation of Venus from Saturn, are

$$n'\delta z' = + \circ'' \cdot \circ 369 \sin(9 - 9)$$
 $v' = + \circ'' \cdot \circ 369 \cos(9 - 9)$

Action of the Earth on Saturn.

In this case

$$\log \alpha = 9.0203181$$
 $\log b_{\frac{1}{2}}^{(0)} = 0.3022$ $\log \alpha \frac{db_{\frac{1}{2}}^{\frac{1}{2}}}{d\alpha} = 8.0460$

The constant term of ν' is

$$\nu' = + 0''.2147$$

The non-periodic portion of $\frac{a'}{\triangle}$ contains the terms

$$\frac{\mathbf{a}'}{\triangle} = [7.6236](e^2 + e'^2) - [8.2257] \sin^2 \frac{\mathbf{I}}{2} \mathbf{J} - [7.0413]ee' \cos (\Pi' - \Pi)$$

In which we have

$$\log \sin J = 8.6387$$
 $\Pi' = 157^{\circ} 46'$ $\Pi = 168^{\circ} 1'$

Whence we conclude that the secular terms are

$$n'\delta z' = + 0.00004n't \sin g' - 0.000579n't \cos g'$$

$$v' = - 0.000002n't \cos g' - 0.000289n't \sin g'$$

$$\frac{u'}{\cos i'} = + 0.000086n't \sin g' + 0.000212n't \cos g'$$

The terms of $n'\delta z'$ and ν' , which depend on the elongation of the Earth from Saturn, are

$$n'\delta z' = + o''.o672 \sin (a - b)$$
 $v' = + o''.o672 \cos (a - b)$

Action of Mars on Saturn.

In this case

$$\log \alpha = 9.2032152$$
 $\log b_{\frac{1}{2}}^{(0)} = 0.3038$ $\log \alpha \frac{db_{\frac{1}{2}}^{(0)}}{d\alpha} = 8.4190$

The constant term of ν' is

$$\nu' = + 0''.0226$$

The non-periodic portion of $\frac{\mathbf{a}'}{\triangle}$ contains the terms

$$\frac{\mathbf{a}'}{\wedge} = [8.0014](e^2 + e'^2) - [8.6035]\sin^2\frac{1}{2}\mathbf{J} - [7.6012]ee'\cos(\Pi' - \Pi)$$

In which we have

$$\log \sin J = 8.6153$$
 $II' = 113^{\circ} 5'$ $II = 356^{\circ} 19'$

Whence we conclude that the secular terms are

$$n'\delta z' = -0.000044n't \sin g' - 0.000172nt \cos g'$$

$$v' = +0.000022n't \cos g' - 0.000086n't \sin g'$$

$$\frac{u'}{\cos i'} = +0.000051n't \sin g' + 0.000022n't \cos g'$$

CHAPTER VIII.

PERTURBATIONS OF THE SECOND ORDER WITH RESPECT TO DISTURBING FORCES IN THE LONGITUDES AND RADII-VECTORES, ARISING FROM THE MUTUAL ACTION OF JUPITER AND SATURN—DERIVATION OF THE FACTORS OF ST AND ST.

Having completed the determination of all the perturbations of the first order with respect to the disturbing forces, we now arrive at the consideration of those of the second order. And, in the first place, we confine our attention to those of the fundamental arguments and radii-vectores which arise from the mutual action of Jupiter and Saturn. The more important part of these perturbations arises from attributing to the variables involved in T and T' no longer elliptical values but elliptical values augmented by the perturbations of the first order.

In a similar manner to Hansen's, we can put for Jupiter

$$\delta \mathbf{T} = \mathbf{A} n \delta z + \mathbf{B} \nu + \mathbf{C} \delta \frac{h}{h_0} + \mathbf{D} \frac{u}{\cos i} + \mathbf{E} \frac{u_1}{\cos i} + \mathbf{F} n' \delta z' + \mathbf{G} \nu' + \mathbf{H} \frac{u'}{\cos i'}$$

and for Saturn

$$\delta \mathbf{T}' = \mathbf{A}' n' \delta z' + \mathbf{B}' \nu' + \mathbf{C}' \delta \frac{h'}{h_0'} + \mathbf{D}' \frac{u'}{\cos i'} + \mathbf{E}' \frac{u_1'}{\cos i'} + \mathbf{F}' n \delta z + \mathbf{G}' \nu + \mathbf{H}' \frac{u}{\cos i}$$

Here u_1 and u_1' denote the differential coefficients of u and u' with respect to the time. In the present chapter we shall be engaged in determining the factors entering into the right members of these two equations.

Of these factors, two are very readily found, viz, A and F. For, evidently,

$$\mathbf{A} = \frac{dT}{dg} \qquad \qquad \mathbf{F} = \frac{dT}{dg'}$$

As to B, we have

$$\mathbf{B} = r \frac{dT}{dr}$$

Then, supposing T to have the form

$$\mathbf{T} = \mathbf{A}a \frac{d\Omega}{dq} + \mathbf{B}ar \frac{d\Omega}{dr}$$

(where the reader is asked not to confound this A and B with the same symbols denoting two factors of δT), we can suppose that B = V + X, where V denotes the portion of B which arises from making the forces in T variable with respect to r, and X the portion which arises from making the multipliers A and B so variable. Then it is plain that V has the expression

$$V = A \frac{d \cdot ar \frac{d\Omega}{dr}}{dq} + Bar \frac{d \cdot r \frac{d\Omega}{dr}}{dr}$$

In order to find X we take the expression

$$\mathbf{T} = \frac{a}{\cos \varphi} \left\{ \left[2 \frac{\rho}{r} \cos \left(f - \omega \right) - \mathbf{1} + 2 \frac{h^2 \rho}{h_0^2 a \cos^2 \varphi} \left[\cos \left(f - \omega \right) - \mathbf{1} \right] \right] \frac{d\Omega}{df} + 2 \frac{\rho}{r} \sin \left(f - \omega \right) r \frac{d\Omega}{dr} \right\}$$

whence

$$\mathbf{X} = -\frac{a}{\cos \omega} \left[z \frac{\rho}{r} \cos \left(f - \omega \right) \frac{d\Omega}{df} + z \frac{\rho}{r} \sin \left(f - \omega \right) r \frac{d\Omega}{dr} \right]$$

But we have

$$\frac{d\Omega}{df} = \frac{r^2}{a^2 \cos \varphi} \frac{d\Omega}{dg} - \frac{er \sin f}{a \cos^2 \varphi} r \frac{d\Omega}{dr}$$

Thus

$$\mathbf{X} = -\frac{2r\rho}{a^2\cos^2\varphi}\cos\left(f - \omega\right)a\frac{d\Omega}{dg} - \frac{2\rho}{a\cos^3\varphi}\left[\sin\left(f - \omega\right) - e\sin\omega\right]ar\frac{d\Omega}{dr}$$

Since, in computing the forces we have supposed $\log r$ to be augmented by the constant term of its perturbations, but in deriving the multipliers A and B have given to r its elliptic value, it follows that, calling the constant term of ν , c, we ought to write $B(\nu - c) + cX$ for $B\nu$.

Differentiating, partially with reference to $\frac{h}{h_0}$, the expression for T, we get

$$\mathbf{C} = -\frac{4\rho}{\cos^3 \varphi} \left[\cos \left(f - \omega \right) - \mathbf{I} \right] \frac{d\Omega}{df}$$

We note that

$$\bar{\mathbf{T}} = \frac{a}{\cos \varphi} \frac{d\Omega}{df}$$

Whence, it follows that*

$$C = 2[T + X + \overline{T}]$$

As to the other factor it can be got from either of the two equations;

$$\delta rac{h}{h_0} = - \left(rac{d\delta z}{dt} + 2
u
ight) \qquad \qquad \delta rac{h}{h_0} = - \int \overline{\mathbf{T}} n dt$$

We get D, E, and H from the following equations: ‡

$$D = A \frac{d \cdot a^2 \frac{d\Omega}{dZ}}{dg} + B \left[a^2 r \frac{d \cdot \frac{d\Omega}{dZ}}{dr} + a^2 \frac{d\Omega}{dZ} \right]$$

$$E = A a^2 \frac{d\Omega}{dZ}$$

$$H = A a a' \frac{d \cdot \frac{d\Omega}{dZ'}}{dg} + B a a' r \frac{d \cdot \frac{d\Omega}{dZ'}}{dr}$$

^{*}Auseinandersetzung, Abth. I, s. 128, gl. (69).

t Auseinandersetzung, Abth. I, ss. 128, 129, gl. (70), (71).

[‡] Auseinandersetzung, Abth. I, s. 130, gl. (72).

Lastly, we have*

$$G - V - T$$

In all these equations A and B denote the same multipliers as appear in T.

In these expressions four functions of the co-ordinates are present which did not appear in the determination of the first-order terms.

For Jupiter we have t

$$\frac{a}{\mu} \frac{d\left(r\frac{d\Omega}{dr}\right)}{dr} = \frac{3}{4} \left(\alpha^{2} \frac{r^{2}}{a^{2}} - \frac{r'^{2}}{a'^{2}}\right)^{3} \left(\frac{a'}{\Delta}\right)^{5} - \frac{r'^{2}}{a'^{2}} \left(\frac{a'}{\Delta}\right)^{3} + \frac{1}{4} \frac{a'}{\Delta} - a' \frac{r}{r'^{2}} H$$

$$\frac{d\left(\alpha^{2} \frac{d\Omega}{dZ}\right)}{dr} = -\frac{3}{2} \mu \alpha \sin J \left\{ \left(\alpha^{2} \frac{r^{2}}{a^{2}} - \frac{r'^{2}}{a'^{2}}\right) \left(\frac{a'}{\Delta}\right)^{5} + \left(\frac{a'}{\Delta}\right)^{3} \right\} \frac{r'}{a'} \sin (f' + \Pi')$$

$$aa' \frac{d\Omega}{dZ'} = \mu \alpha \sin J \left\{ -\left(\frac{a'}{\Delta}\right)^{3} + \left(\frac{a'}{r'}\right)^{3} \right\} \frac{r}{a} \sin (f + \Pi)$$

$$r \frac{d\left(\alpha a' \frac{d\Omega}{dZ'}\right)}{dr} = \mu \alpha \sin J \left\{ \frac{3}{2} \left(\alpha^{2} \frac{r^{2}}{a^{2}} - \frac{r'^{2}}{a'^{2}}\right) \left(\frac{a'}{\Delta}\right)^{5} + \frac{1}{2} \left(\frac{a'}{\Delta}\right)^{3} + \left(\frac{a'}{r'}\right)^{3} \right\} \frac{r}{a} \sin (f + \Pi)$$

For Saturn the similar quantities are

$$\frac{a'}{\mu'}r'\frac{d\left(r'\frac{d\Omega'}{dr'}\right)}{dr'} = \frac{3}{4}\left(\alpha^2\frac{r^2}{a^2} - \frac{r'^3}{a'^2}\right)^2\left(\frac{a'}{\Delta}\right)^5 - \alpha^2\frac{r^2}{a^2}\left(\frac{a'}{\Delta}\right)^3 + \frac{1}{4}\frac{a'}{\Delta} - a'\frac{r'}{r^2}H$$

$$r'\frac{d\left(\alpha'^2\frac{d\Omega'}{dZ'}\right)}{dr'} = -\frac{3}{2}\mu'\alpha\sin\int\left\{\left(\alpha^2\frac{r^2}{a^2} - \frac{r'^2}{a'^2}\right)\left(\frac{a'}{\Delta}\right)^5 - \left(\frac{a'}{\Delta}\right)^3\right\}\frac{r}{a}\sin\left(f + \Pi\right)$$

$$aa'\frac{d\Omega'}{dZ} = \mu'\alpha\sin\int\left\{\left(\frac{a'}{\Delta}\right) - \frac{1}{\alpha^3}\left(\frac{a}{r}\right)^3\right\}\frac{r'}{a'}\sin\left(f' + \Pi'\right)$$

$$r'\frac{d\left(aa'\frac{d\Omega'}{dZ}\right)}{dr'} = \mu'\alpha\sin\int\left\{\frac{3}{2}\left(\alpha^2\frac{r^2}{a^2} - \frac{r'^2}{a'^2}\right)\left(\frac{a'}{\Delta}\right)^5 - \frac{1}{2}\left(\frac{a'}{\Delta}\right)^3 - \frac{1}{a^3}\left(\frac{a}{r}\right)^3\right\}\frac{r'}{a'}\sin\left(f' + \Pi'\right)$$

For the principal multiplier involved in these expressions, from the data at page 59, we have

$$\alpha^{2} \frac{r^{2}}{a^{2}} - \frac{r^{\prime 2}}{a^{\prime 2}} = - [9.8490745]$$

$$+ 2[8.7484582] \cos g' - 2[8.1564087] \cos g$$

$$+ 2[6.8947428] \cos 2g' - 2[6.2375704] \cos 2g$$

$$+ 2[5.3420289] \cos 3g' - 2[4.6197410] \cos 3g$$

$$+ 2[3.9142411] \cos 4g' - 2[3.1268416] \cos 4g$$

^{*}Auseinandersetzung, Abth. I, s. 130, gl. (74).

t Auseinandersetzung, Abth. I, s. 120.

We then multiply the expression for $\left(\frac{a'}{\triangle}\right)^s$, given at pages 53-56, by this factor, and the product again by three-fourths of this factor, and thus obtain

Arg=i'g'+ig	$\left(\alpha^2 \frac{r^2}{a^2} - \frac{r'^2}{a'^2}\right) \left(\frac{a'}{\triangle}\right)^5$		$\left(\alpha^2 \frac{r^2}{\mathbf{a}^2} - \frac{r'^2}{\mathbf{a}'^2}\right) \left(\frac{\mathbf{a}'}{\Delta}\right)^5 \qquad \frac{3}{4} \left(\alpha^2 \frac{r^2}{\mathbf{a}^2} - \frac{r'^2}{\mathbf{a}'^2}\right)^2 \left(\frac{\mathbf{a}'}{\Delta}\right)^5$		$\frac{r'^2}{a'^2}$) ² $\left(\frac{a'}{\triangle}\right)^5$	$\left(\alpha^2 \frac{r^2}{a^2} - \frac{r'^2}{a'^2}\right) \times \left(\frac{a'}{\triangle}\right)^5 \frac{r'}{a'} \sin\left(f' + II'\right)$		$-\left(\alpha^2 \frac{r^2}{a^3} - \frac{r'^3}{a'^3}\right) \times \left(\frac{a'}{\triangle}\right)^5 \frac{r}{a} \sin\left(f + \Pi\right)$	
	cos.	sin.	cos.	sin.	sin.	cos.	sin.	cos.	
i' i									
0 0	-5. 02721		+2.59302			-0. 29	1	+0.35	
о— 1	- +0.5670 68	+1.175051	—0. 264241	o. 244635	-1.78	+4.07	+1.98	4 ⋅ 57	
0 2	+0.07576	—o. o6441	0. 01099	+0.01861	—o. 35	— 0. 27	+ 0. 46	+0. 39	
0 3	0.00476	o. oo399	+0.00103	+0.00051	+0.02	0.01	-0.04	+0.04	
0— 4	-0.00018	+0.00031	+0.00002	0.00005	ŀ				
1+ 3	-0.00080	+0.00015	+0.00014	0.00000					
1+ 2	+0.00431	+0.01246	0.00008	-0.00258	+0.02	— 0. 06	— 0. 03	+0.08	
1+1	+0.16021	-0. 09824	0. 04441	+0.00915	+0.63	+0.43	— 0. 76	o. 52	
1 0	-1.531692	<u>_1. 210440</u>	+0.401926	+0.535226	— 4. 01	+2. 8o	+3.66	—2. 50	
I I	1.825288	+8.852622	+0.925569	-4. 560 693	+o. 58	+0.42	0. 70	0. 49	
I 2	+ 0. 709941	o. 09778 1	—о. 075858	+0.075590	− 3·47	— о. 73	+4.40	+0.92	
1— 3	—0. 01743	0. 04487	+o. oo 869	+0.00836	+0.05	— 0. 24	-o. o8	+0.32	
1 4	0. 00255	+0.00146	+0.00053	—0. 00026	+0.01	+0.01	0.02	o. oı	
1— 5	+0.00013	+0.00014	0. 00003	-0, 00002	l				
2+ 3	0.00010	0. 00001	+0.00002	0, 00000					
2+ 2	0.00033	+o. oo168	+0.00013	-0.00028			0.00	+0.01	
2+ 1	+0.02574	-0.00012	0. 00526	-o. oo182	+0. 10	-o. oı	—0. 15	-0.01	
2 0	0. 094530	—о. 301683	-0.001913	+0.089814	-o. 38	+1.00	+0.44	-1.04	
2— I	-1.760858	+1.573472	+0.768184	-o. 486025	—3. IO	2 . 97	+2.44	+2.42	
z 2	+6.575664	+2.851119	-3. 383346	—1.442006	_o. 65	-j-0. 62	+0. 78	—o. 79	
2— 3	+0. 123630	-0. 299932	-0. 007497	0. 053802	+0.02	2.61	0, 01	+3.55	
2— 4	-0. 02072	+0.00326	+0.00634	-0.00731	+0.11	0.07	— 0. 17	+0.08	
2 5	+0.00024	+0.00146	+0.00013	—u. 00046	,	· .	,	,	
2— 6	+0.00010	-0.00002	_0.0000I	0.00000				i	
3+ 2	-0.00014	+0.00016	+0.00003	-0.00001					
3+ I	+0.00294	+0.00170	-0. 00044	—0. 00051	+0.01	0.01	-0.02	+0.02	
3 0	+0.01214	0. 04496	o. oo67o	+0.00934	+0.04	+0.17	-0.04	0. 21	
3— 1	-0. 443932	+0.054753	+0. 143260	+0. 019989	—I. 22	—0. 20	+1.14	+0. 24	
3— 2	+1.264647	+2.048382	—o. 422232	—0.897 606	+1.77	—2.8 1	1.33	+1.99	
3- 3	+3.04058	-4. 27059	—I. 53345	+2. 19691	-0.67	—о. 69	+o. 88	+o. 82	
3 4	—0. 02192	—0. 16314	-0. 12479	+0.01842	+1.76	0. 37	-2.55	+0.52	
3— 5	+0.00413	+0.00813	—о. 00839	—o. oo637	+0. 10	+0.01	-0. 14	о. оз	
3— 6	+0.00099	+0.00016	-0.00046	-0.00045					
3— 7	+0.00019	-0.00008	0.00011	+0.00001					
4+ 1	+0.00021	+0.00037	-0.00001	-o. oooo8					
4 0	+ 0 . 00469	-0.00445	-0.00133	+0.00054	+0.01	+0.02	-o. or	0. 02	
4— I	0. 065543	0. 032528	+0.014718	+0. 014596	0. 23	+0.10	+0. 24	0. 10	
4 2	—о. 02387 8	+0. 535892	+0.046419	0 . 183692	-o. oı	—I. 22	-o. o3	+1.02	
4 3	+2.030304	0. 783534	-0. 898122	+o. 263698	+2. 18	+o. 81	—1.43	0. 59	
4 — 4	2. 43782	2. 68073	+1.25694	+1.34814	+0.56	—о. 68	-o. 67	+0.90	

Arg=i'g'+ig	$(\alpha^2 \frac{\gamma^2}{a^2} -$	$\left(\frac{r'^2}{a'^3}\right)\left(\frac{a'}{\triangle}\right)^6$	$\frac{3}{4}\left(\alpha^2\frac{r^2}{a^2}-\right)$	$\left(\frac{r'^2}{a'^2}\right)^2 \left(\frac{a'}{\triangle}\right)^5$	$\left(\alpha_{ai}^{2^{r^{2}}} - \left(\frac{a'}{\triangle}\right)^{5} \frac{r'}{a'} \sin \alpha_{ai}^{r}\right)$)	$-\left(\alpha^2 \frac{r^2}{a^2}\right)^5 \frac{r}{a} \sin \frac{r}{a}$	
	cos.	sin.	cos.	sin.	sin.	cos.	sin.	cos.
i' i 4— 5	<u> </u>	0. 1218	-0. 0020	+0. 1438	+o. 5o	+1.10	 0. 73	—1. 63
4- 3	+0.0048	-0. 0082	0.0020	+0.0086	+0.04	+0.09	-0.06	-0. 12
	+0.0003	-0.0007	-0,0006	+0.0006		70.09	0.00	0.12
4 7				,				
5 0	+0.0009	-0.0003	0, 0002	+0.0001		,		
5 1	—o. oo569	-0.00939	+0, 00050	+0.00273	o. o3	+0.03	+0.03	-0. 04
5 2	o. o58167	+0.079796	+0.024204	—о. о19233	o. 17	-0. 24	+0.14	+0. 24
5— 3	+0. 551950	+0. 120960	—o. 197581	-0.077911	+1.08	—O. 22	0.83	+0.15
5— 4	0. 315926	-1.777410	+0.090186	+0.793893	—0. 2I		+0. 18	0.91
5— 5	—2 . 0842	+1.1902	+1.0454	0.6186	+0.63	+0.38	-0.84	-0.44
5— 6	o. 1657	+0.0437	+0.1291	+0.0264	0.62	+0.46	+0.95	0.70
5— 7 5— 8	0. 0105	0.0056	+0.0078 +0.0002	+0.0087 +0.0010	o. o6	+0.05	+0.07	—o. o7
	0.0006	—o. ooog	l '				,	
6— 1	0.0000	-0.0017	0.0000	+0.0004				
6— 2	0. 01517	+0.00584	+0.00460	0. 00023	0. 04	0, 02	+0.05	+0.02
6— 3	+0.08196	+o. o8361	—o. o2o69	—o. o3359	+0. 20	—0. 2I	—0. 2I	+0. 15
6— 4	+0. 2070	u. 49 77	о. 1060	+o. 1836	+0.34	+0.81	-o. 23	0. 59
6— 5	1.4045	—o. o319	+o. 6327	+0.0452	o. 95	+0.08	+0.49	-0,02
6— 6	+o. 4461	+1.4712	—o. 2381	0. 7361	-0. 22	+0.53	+0. 24	0.72
6— 7	-0.0121	+0.1528	+0.0421	-0. 0994	0. 36	0. 31	+0.58	+0.48
6— 8	0.0079	+0.0097	+0.0092	0.0053	—o. o6	— 0. 02	+0.09	+0.03
6— 9	0. 0009	+0.0005	+0.0009	0.0000				
7— 2	-0.0023	-o. ooo5	+0.0006	+0.0003				
7 3	+0.0042	+0.0206	+0.0004	—o. oo64	+0.02	— о. 05	—o. oı	+0.06
7— 4	+o. 1028	-0.0712	o. o4o7	+0.0183	+0.23	+ 0. 16	—o. 18	—о. 15
7— 5	—о. 3985	o. 2611	+0.1500	+0. 1229	-o. 55	+0.39	+o. 38	0. 24
7 6	—0. 2339	+1.0139	+0. 1248	-0. 4598	—о. 17	—o. 52	+0.06	+0.23
7— 7	十0.9557	—о. об13	—o. 4770	+0.0408	o. 4I	o. o8	+0.55	+0.08
7— 8	+o. 1159	+0.0451	o. o677	-0.0473	+0.12	0.24	—0. 2I	+0.42
7— 9	+0.0074	+0.0095	-o. oo31	-o. oo88	+o. o3	-0.09	0.00	+0.07
710	+0.0003	-0.0002	+0.0001	0.0002				
8— 3	0.0012	+0,0033	+0.0005	0.0008				
8— 4	+0.0248	-o, ooo8	0. 0079	0, 0016	+0.06	+ o . 01	—о. 06	0.00
8 5	-o. o513	0. 1116	+0.0124	+0.0439	o. 1o	+0.23	+0.07	—о. 17
8— 6	—0. 2767	+0. 2846	+0. 1260	0. 1082	0. 35	—о. 33	+o. 21	+0.22
8— 7	+o. 6718	+o. 3124	о. 3064	—о. 1539	+0. 27	о. 18	o. o6	+0.05
8— 8	+0. 1004	-o. 5741	0. 0430	+0. 2862	+0.02	—0. 30	o. o3	+0.41
8 — 9	+0.0544	0.0758	o. o433	+0.0407	+o. 13	+0.07	—o. 27	-0.04
8—10	+0.0091	-o. oo39	0.0073	+0.0009	+0.01	+0.02	о. 10	-0.02
8—11	+0.0009	+0.0001	-0.0007	-0.0004				
9— 4	+0.0039	+0.0022	0.0010	-o. ooog				
9— 5	+0.0036	0, 0267	-0.0030	+0.0087	+0.01	+o. o6	o. oI	o. o6
9— 6	0. 1095	+0.0279	+0.0433	0. 0050	0. 19	0. 04	+0.15	+0.03
9— 7	+0. 1783	+0. 2592	-o. o675	o. 116o	+0.17	0. 29	o. I2	+0. 18
					1		<u> </u>	l

Arg=i'g'+ig	$\left(\alpha^2 \frac{r^2}{a^2} - \right)$	$\left(\frac{r'^2}{a'^2}\right)\left(\frac{a'}{\triangle}\right)^5$	$\frac{3}{4}\left(\alpha^2\frac{r^2}{a^2}-\frac{1}{a^2}\right)$	$\left(\frac{r'^2}{a'^2}\right)^2 \left(\frac{a'}{\triangle}\right)^5$		$\left(\alpha^{2} \frac{r^{2}}{a^{3}} - \frac{r'^{2}}{a'^{3}}\right) \times -\left(\alpha^{2} \frac{r^{2}}{a^{3}} - \frac{r'^{2}}{a'^{3}}\right) \times \left(\frac{a'}{\triangle}\right)^{5} \frac{r'}{a'} \sin\left(f' + \Pi'\right) \left(\frac{a'}{\triangle}\right)^{5} \frac{r}{a} \sin\left(f + \Pi\right)$		
	cos.	sin.	cos.	sin.	sin.	cos.	sin.	cos.
i i 9— 8	+0. 3082	-o. 4072	—o. 1482	+o. 1864	+o. 14	+o. o8	+0.02	0. 02
9— 9	0. 3177	0. 1409	+o. 1585	+0.0652	+0. 10	+0. 18	o. 25	+0.04
9—10	-0. 0430	-o. o512	+0.0212	+0.0354	+0.11	-0. 02	+0.05	—0. 15
9—11	-0.0015	-o. oo8o	0. 0004	+0.0056	+0.03	0.00	+0.02	o. o1
912	+0. 0002	0.0007	0, 0004	+0.0005				
10 4	+0.0004	+0.0007	0, 0000	-0.0003				
10— 5	+0.0032	0. 0039	-0.0013	+0.0010				
10 6	o. o256	-o. oo81	+o. 0085	+0.0044	0, 05	+0.02	+0.05	0. 02
10- 7	+0.0059	+0.0980	+0.0024	о. 0388	0, 00	— 0. 15	о. оз	+0. 13
10 8	+0. 2205	-o. o938	o. 0980	+0. 0345	+0. 22	+o. o6	+o. 10	о. 13
10- 9	0. 2225	—о. 2608	+0. 1020	+0. 1243	0. 15	+o. 18	o. 25	+0.04
10—10	0. 1265	+o. 1594	+0.0595	0. 0796	+0.07	+0.01	+0.13	0.07
1011	-0.0415	+0.0202	+0. 0263	-o. oo86	0.00	o. o6	-o. o5	0. 09
1012	-o, oo63	0, 0005	+0.0040	+0.0014	+0.01	—o. oī	0.00	-0. 02
11- 5	+0.0009	0, 0004	-0. 0004	0,0000				
11 6	о. 0038	0. 0042	+0.0009	+0.0016				
11- 7	o. o118	+0.0223	+0.0055	—o. oo75	o. o3	0. 04	0.00	+0.05
11 8	+o. 080 7	+0.0108	—o. o32o	-0.0075	+o. 13	0.00	+0.07	o. o 6
11- 9	0, 0347	—о. 17 30	+0.0110	+0.0766	0. 17	+0.01	—0. 14	0. 03
11—10	— о. 1 989	+0.1047	+0.0943	-0. 0480	+0.04	+0.14	+0.06	+0.07
1111	+o. 0697	+0.0945	0. 0351	0. 0444	+0.02	—o. o5	0.01	0.09
1112	+0.0065	+0.0298	-0.0015	-o. o177	-0.04	-o. oı	0. 05	- 1 -0.01
12— 6	-0.0002	-o. oo1o	0,0000	+0.0003				
12 7	o. 005 I	+0.0028	+0.0020	-0.0007				
12- 8	+0.0181	+0.0148	-0. 0062	—о. 0067	+0.04	0.00	+0.03	0,00
12 9	+0.0225	-o. o634	-0. 0122	+0.0259	-0, 06	— 0. 06	-0.03	o. o5
12-10	—0. 1308	0.0035	+0.0602	+0.0055	0.05	+0.09	-o. o3	+0.08
12—11	+o. o358	+0. 1474	-o. o154	0. 0739	+0.05	+0.02	+0.06	-0.03
12—12	+0. 0701	-0. 0207	0. 0372	+0.0107	+0.01	+0.01	—o. o8	0. 01

In order to form the expressions for the forces in the second-order terms we still need developments for the two quantities

$$\left(\frac{\mathbf{a}'}{r'}\right)^3 \frac{r}{\mathbf{a}} \sin\left(f + \Pi\right) \qquad \qquad -\frac{\mathbf{I}}{\alpha^3} \left(\frac{\mathbf{a}}{r}\right)^3 \frac{r'}{\mathbf{a}'} \sin\left(f' + \Pi'\right)$$

The expression for $\left(\frac{a}{r}\right)^{s}$ is*

$$\left(\frac{\mathbf{a}}{r}\right)^3 = \frac{1}{\cos^3\varphi} + \left(\frac{3}{2}e + \frac{27}{16}e^3\right)\cos g + \left(\frac{9}{4}e^2 + \frac{7}{4}e^4\right)\cos 2g + \frac{53}{16}e^3\cos 3g + \frac{231}{48}e^4\cos 4g + \dots$$

with a similar formula for $\left(\frac{a'}{r'}\right)^3$

^{*}Auseinandersetzung, Abth. I, s. 179.

When the numerical values of e and e' are substituted we obtain

$$\left(\frac{\mathbf{a}'}{r'}\right)^3 = [0.00205] + 2[8.92625] \cos g' + 2[7.85050] \cos 2g' + 2[6.76604] \cos 3g'$$
$$\left(\frac{\mathbf{a}}{r}\right)^3 = [0.00152] + 2[8.86066] \cos g + 2[7.71983] \cos 2g + 2[6.57045] \cos 3g$$

The expressions for the factors $\frac{r}{a} \sin (f + \Pi)$ and $\frac{r'}{a'} \sin (f' + \Pi')$ have already been given (page 60), and we obtain the products

Arg=i'g'+ig	$\left(\frac{\mathbf{a}'}{r'}\right)^3 \frac{r}{\mathbf{a}} \text{ si}$	n (f+II)	Arg=i'g'+ig	$-\frac{\mathrm{I}}{\alpha^3}\left(\frac{\mathrm{a}}{r}\right)^3\frac{r'}{\mathrm{a'}}$	$\sin (f + \Pi)$
	sin,	cos.	A1g1 y + 1y	sin.	cos.
i' i 0 0 0 I 0 2 0 3 I + 2 I + I I 0 I - I I - 2 2 + I 2 0 2 - I 3 + I 3 - I	+0.415 +0.010 0.000 -0.001 -0.035 0.000 +0.035 +0.001 -0.003 0.000 +0.003	+0.066 -0.914 -0.022 -0.001 -0.002 -0.077 +0.011 -0.002 -0.006 +0.001 -0.006	i' i 0 0 1 0 2 0 3 0 -2 I I I I 2 I 2 2 2 2 2 2 2	-4. 984 -0. 140 -0. 006 +0. 010 +0. 360 0. 000 -0. 360 -0. 010 +0. 026 0. 000 -0. 026 -0. 001	-0. 308 +3. 657 +0. 102 +0. 004 +0. 007 +0. 264 -0. 045 +0. 007 +0. 001 +0. 019 -0. 003 +0.019 +0.001
ÿ			I- 3 I- 3	+0.002 0.002	+0.001 +0.001

We are now able to get the four functions severally for Jupiter and Saturn, the remaining data required being found in Chapters I and II.

Arg=i'g'+ig	$arrac{d\left(rrac{d\Omega}{dr} ight) }{dr}$		$a^2rrac{d^2\Omega}{drdZ}+a^2rac{d\Omega}{dZ}$		$aa'rac{d\Omega}{d\mathbf{Z}'}$		$aa'rrac{d^2\Omega}{drdZ'}$	
	cos.	sin.	sin.	cos.	sin.	cos.	sin.	cos.
i' i	// +21. 2696	"	11	// +0. 146	"	// —0. 0279	"	o. 150
1 —0	<u> </u>	— 3. 26268	+0.900	—2.060	—о. 1825	+0.4243	—о. 809	+1.890
0— 2	— o. 1675	+ 0. 2695	+0. 185	+0.149	-o. o5o7	—о. 0376	—o. 234	-0. 219
o— 3	+ 0.0170	+ 0.0087			+0.0015	0.0028	+0.023	—o. o23
0— 4	+ 0.0003	— o. ooto			+0.0001	+0.0001		
1+3	+ 0.0026	0.0000			0. 0003	-0. 0002		
I+ 2	- o. oo16	— 0. 04 01	0.008	+0.032	+0.0036	—о. 0066	+0.015	—o. o43
1+1	— o. 5939	+ o. 1297	-o. 333	—0. 224	+0. 07 67	+0.0442	+o. 38o	+0. 234
1 0	+ 4. 69009	+ 5.11622	+1.655	1. 139	o. 5o53	+0. 3533	—I.852	+1.269

Arg=i'g'+ig	$arrac{d\left(rrac{d\Omega}{dr} ight)}{dr}$		$a^2 r rac{d^2 \Omega}{dr dZ} + a^2 rac{d \Omega}{dZ}$		$aa'rac{d\Omega}{dZ'}$		$aa'rrac{d^2\Omega}{drdZ'}$	
	cos.	sin.	sin.	cos.	sin.	cos.	sin.	cos.
i' i I— I	" + 6.54843	//	o. 303	 0. 215	// +0.0995	,, +o. 0488	" +0. 372	+0. 215
I— z	— 1. 19864	-32.97927 + 1.65391	+1.798	+0. 379	_0. 6050	-0. 1315	-2. 22 8	0. 464
I— 3	+ 0. 1290	+ 0. 1624	0.030	+0. 128	_0.0052	-0.0301	+0.050	—0. 169
1— 4	+ 0.0096	- 0.1024 - 0.0032	0,030	1 0.120	+0.0008	-0.0001	+0.011	0.000
1— 5	- 0.0010	- 0.0003			'			0.000
2+ 3	+ 0.0003	0,0000						
2+ 2	+ 0.0019	0.0045			0,0000	0.0009		
2+ 1	- 0.0748	— o. o253	—o. o5o	+0.010	+0.0133	+0.0005	+0.076	0, 000
2 0	o. o8518	+ o. 98315	- - -0. 153	0. 486	0.0611	+0.1189	0. 222	+0.541
2— I	+10. 24927	— 3. 07938	+1.566	+1.503	-0. 2762	-0. 2742	—1. 265	—I. 258
2— 2	—48. 84956	—20. 69473	+0.332	-0.332	—o. 1062	+0.0811	-o. 395	+0.414
2— 3	+ 0.05380	— I. 03378	0.012	+1.377	+0.0018	-0.4024	0.000	—1. 84o
2— 4	+ 0. 1300	— O. 1239	<u> </u>	+0.033	+0.0105	0.0162	+0.091	— о. о38
2— 5	+ 0.0032	— o. oo77			0,0000	—o. ooo3		
3+ 1	— o. oo64	- o. oo77			+0.0016	-0.0007	+0.011	0.011
3 0	— 0. 0995	+ 0. 1011	-0. 027	o. o85	+0.0005	+0.0212	+0.023	+0.111
3— г	+ 1.91765	+ 0.79348	+0.627	+0.095	0. 1140	0. 0327	o. 5 98	—0. 123
3— 2	— 5. 14840	14. 27037	0, 916	+1.452	+0. 1231	0. 1900	+0. 702	-1.051
3— 3	—26. 1007	+37.5759	+0.359	+0.364	o. o8o6	0. 0941	0. 464	0. 426
3— 4	— 2. 4779	+ 0. 1749	0. 939	+0. 198	+0. 2420	-0.0515	+1.346	-0. 272
3— 5	— o. 1595	— 0. 1425	—u. o55	-0.005	+o. o155	-0.0011	+0.073	+0.019
3— 6	— o, oo83	— o. o1o3			+0.0006	-0.0003		
3- 7	- 0.0032	+ 0.0006						
4+ 1	0.0000	— o. oo13			+0.0001	0. 0002		
4 0	— 0.0193	+ 0.0042			+0.0015	+0.0026	0, 000	+0.011
4— 1	+ o. 17361	+ 0.27159	+0. 123	0.052	-0. 0229	+0.0052	—o. 127	+0.054
4- 2	+ 1.16692	2. 82988	+0.010	+0.640	+0.0072	0.0918	+0.015	—o. 541
4 3	—15. 95049	+ 3.61154	-1. 145	0. 430	+0.1154	+0.0437	+0.763	+0.318
4— 4	+24.0627	+25.6448	-0. 298	+0. 367	+0.0668	—0. 074 6	+0.353	-0. 479
4-5	— o. 180	+ 3.016	—o. 267	0. 596	+0.0612	+0. 1335	+0. 387	+0.870
4— 6	- o. 18o	+ 0.176	0. 021	0. 047	+0.0061	+0.0108	+0. 030	+0.065
4— 7	- o. o13	+ 0.013			+0.0006	+0.0005		
5 0	— o. oo3	+ 0.002			+0.0003	+0.0002		
т —2	- 0.0013	+ 0, 0446	+0.014	-0.014	-0. 0029	+0.0026	-0.015	+0.023
5- 2	+ 0.45743	- 0. 24968	+0.093	+0.128	o. 0091	-0. 0202	0. 076	0. 127
5— 3	— 3 38332	— I. 77554	—о. 576	+0.118	+0. 0649	0. 0082	+0.445	0.081
5— 4	+ 1.07637	+15. 35642	+0.112	o. 812	-o. oo83	+0.0623	-0. 100	+0.491
5 5	+21.509	—12. 841	o. 341	-0. 204	+0.0627	+0.0397	+0.452	+0. 234
5— 6	+ 2.839	+ 0.674	+o. 338	0. 249	—o. o674	+0.0519	-0. 514	+0.380
5— 7	+ 0. 170	+ 0.205	+0.032	-0. 027	—о. 0060	+0.0071	0. 038	+0.038
5— 8	+ 0.003	+ 0,026				+0.0007		
6 т	0.000	+ 0.006			0, 0002	+0.0005		
6— 2	+ 0.0796	+ 0.0109			0.0034	0. 0025	-0.027	—o. o11

$\mathbf{Arg} = i'g' + ig$	$ar \frac{d(r)}{r}$	$\left(\frac{r \frac{d\Omega}{dr}}{dr}\right)$	$a^2 r rac{d^2 \Omega}{dr d Z} \; .$	$+ a^2 \frac{d\Omega}{dZ}$	$aa'\frac{a}{a}$	$rac{d oldsymbol{Z'}}{d oldsymbol{Z'}}$	$aa'r\frac{d}{d}$	$d^2\Omega$
	cos.	sin.	sin.	cos.	sin.	cos.	sin.	cos.
i' i	"	"	"	"	"	, ,,	"	"
6— 3	o. 2936	— o. 6683	—о. 106	+0.112	+0.0153	-0.0109	+0.111	o. o81
6— 4	2. 355	+ 3.417	—о. 185	-o. 438	+0.0143	+0.0412	+0. 123	+o. 318
6 5	+13.074	+ 1.335	+0.513	-0.044	-0. 0291	+0.0037	—0. 268	-1 -0. ∞8
6— 6	— 5. 267	16. 052	+0.119	o. 287	0.0193	+0, 0482	—0. 127	+0. 391
6— 7	+ 1.023	— 2. 268	+0. 195	+0.172	о. 0376	-o. o3o5	—o. 314	o. 261
6— 8	+ 0.221	— o. 115	+0.032	+0.013	o. oo6o	-0. 0026	—o. o5o	o. o15
6— 9	+ 0.023	+ 0.003			—о. 0006	0.0000		
7— 2	+ 0.010	+ 0.006			0. 0007	o. ooo1	İ	
7-3	+ 0.026	— o. 115	—o. oo8	+o. o28	+0.0018	-o. oo37	0.000	—о. озо
7— 4	— o. 847	+ 0.279	—о. 125	-o. o83	+0.0108	+0.0100	- +0, 100	∔0. 081
7— 5	+ 2.977	+ 2.750	+ 0. 298	— 0. 209	-0.0234	+0.0149	—u. 207	+o. 130
7 6	+ 2.878	10.005	+o. o87	+0. 282	-0.0053	-0. 0109	—о. озо	o. 127
7— 7	—10. 879	+ 0.985	+0. 225	+0.041	-0.0344	— 0. 0060	—o. 299	<u></u> -0. 043
7— 8	— I. 595	1.158	o. o63	+0. 129	+0.0115	-0.0245	+0.115	0. 230
7 9	— o. o67	— o. 218	—o. o17	+0.04 6	+0.0006	-0.0044	0, 000	o. o38
7—10	+ 0.003	0.000			-0.0001	-0.0005		
8— 3	+ 0.010	— o. o13			0.0000	-0. 0008		
8 4	— 0. 154	- 0.051	-o. o33	0. 007	+0.0035	+0.0009	+0.030	0, 000
8 5	+ 0. 186	+ 0.943	+0. 054	-0. 123	0.0056	+0.0093	o. o38	+0.091
8— 6	+ 2.887	2. 256	+o. 181	+0. 182	<u> </u>	0.0121	0. 115	—o. 119
8— 7	— 6. 94 7	— 3.635	—0. 148	+0.098	+0.0021	0.0034	+0.034	0. 027
8— 8	— o. 979	+ 6.767	—о, от 1	+0. 179	-0. 0004	0. 0226	+0.019	—o. 226
8— 9	— I. 075	+ 0.982	-o. o72	0. 041	+0.0147	+0.0028	+0.150	+0.023
8—10	o. 183	+ 0.016		•	+0.0029	-0.0004	- +0. 058	+0.011
8—11	— o. o16	— o. o13			+0.0003	-0,0002		
9— 4	0.019	- 0.019			+0.0007	u. 0002		
9— 5	— o. o83	+ 0. 176	0. 006	— 0. 029	-0.0001	+0.0030	0, 000	+0.034
9— 6	+ 0.966	0. 051	+0. 102	+0.021	-0.0072	-0.0025	-o. o81	—o. o15
9 7	1.450	- 2.714	—o. o89	+o. 16o	+0.0053	0. 0083	+0.065	-c. 100
9— 8	- 3. 562	+ 4.366	—o. o78	0. 046	+0.0012	-0,0012	-0.011	+0.011
9— 9	+ 3.863	+ 1.562	0. 051	—о. 104	+0.0139	-0.0032	+o. 138	-0.023
9—10	+ 0.523	+ 0.892	0. 063	+0.013	+0.0005	+0.0081	o. o3o	+o. o81
9-11	- 0.013	+ 0. 141	0. 017	0.000	+0.0007	+0.0017	-0.011	0.000
9-12	- 0.010	+ 0.013			+0.0002	+0.0002		
10 4	0.000	— o. oo6			+0.0001	-0.0001		
10- 5	— 0.029	+ 0.019			+0.0003	+0.0006		
10— б	+ 0. 180	+ 0.112	+0.032	-0.011	0, 0024	+0.0004	—o. o27	+0.011
10— 7	+ 0.103	0.889	0.000	+0.083	+0.0006	-0.0052	+0.015	-0.072
10-8	2. 345	+ 0.754	0. 120	-o. o32	+0.0052	+0.0018	0. 062	+0.072
10— 9	+ 2.451	+ 3.048	- +0. 087	0. 098	+0.0019	-0.0003	+0. 142	0.023
10-10	+ 1.467	— 1. 98 <u>9</u>	o. o35	+0,006	+0.0038	+0.0080	o. o76	+0.034
1011	+ o. 670	- O. 212	0, 006	+0.035	0. 0041	+0.0015	+0.030	+0.050
10—12	+ 0. 103	+ 0.038	—о. 006	+0.006	0.0009	+0.0007	0.000	+0.011
	1)	•		•	!		1

Arg=i'g'+ig	$arrac{d\left(rrac{d\Omega}{d au} ight)}{dr}$		$a^2r \frac{d^2\Omega}{dr dZ} + a^2 \frac{d\Omega}{dZ}$		$aa'rac{d\Omega}{d\mathbf{Z}'}$		$aa'rrac{d^2\Omega}{drdZ'}$	
	cos.	sin.	sin.	cos.	sin.	cos.	sin.	cos.
i' i	"	11	11	"	"	"	"	"
11— 5	— 0. 010	0.000			+0.0001	+0.0001		
11 6	+0.013	+0.038			-0.0005	+0.0004		
11-7	+o. 138	— 0. 164	+0.017	+0.017	-o. ooo6	—o. oo17	0.000	-o. o27
11—8	—o. 751	<u> </u>	0.074	0,000	+0.0034	-o. ooo3	0. 042	+0. 034
11 9	+0.225	+1.867	+0.098	+0.006	-0. 0002	+0.0029	+0. 081	+0.015
11—10	+2.358	+1. 178	0. 029	-0.079	+0.0011	+0.0016	0. 034	0.043
11—11	о. 895	I. I2O	0. 017	+0.035	0, 0042	+0.0033	+0.008	+0.050
11-12	-o. o35	0. 459	+0.023	+0.006	-0.0013	-0.0020	+0.030	0.000
12— 6	0.000	+o. oo6			-0.0001	+0.0001		
12— 7	+0.048	—o. o13			-0, 0004	-0.0003		
12— 8	-o. 141	0. 170	-0.023	0.000	+0.0011	-o. ooo7	0.019	0.000
12- 9	 0. 324	+0.629	+0.035	+0.040	+0.0007	+0.0020	+0.015	+0.027
12—10	+1.521	+0.173	+0.023	-0.050	-0, 0014	+0.0003	+0.019	-0. 046
12—11	0. 375	-1.919	0.029	-o. o17	-0.0010	+0.0012	-0.034	+0.015
12-12	— 0. 985	+0. 282	0.006	0.006	-0.0023	-0.0017	+0. 046	+0.008

Arg=i'g'+ig	a'r'	$\left(r' rac{d\Omega'}{dr'} ight) \ dr'$	$a'^2r'\frac{d^2\Omega'}{dr'dZ'} + a'^2\frac{d\Omega'}{dZ'}$		aa' -	$rac{d\Omega'}{d\mathbf{Z}}$	$aa'r'rac{d^2\Omega'}{dr'dZ}$	
	cos.	sin.	sin.	cos.	sin.	cos.	sin.	cos.
i' i o o o I o o o o o o o o o o o o o o o	" +432.962 + 52.9395 - 1.0354 - 0.956 - 0.175 - 0.02 - 0.002 - 0.055	" +78. 1156 +11. 9696 + 1. 143 + 0. 057 + 0. 02 + 0. 010 + 0. 061	+14.46 + 1.74 - 0.14 - 0.03	+ 1.40 - 9.88 - 4.03 - 0.82 - 0.09	7. 536 +0. 049 -0. 020 -0. 009 -0. 002 -0. 001 -0. 006	" -0. 497 +5. 621 -0. 530 -0. 108 -0. 012 -0. 001 -0. 001	-27. 94 - 1. 86 + 0. 13 + 0. 04	- 1.86 +19.96 + 4.15 + 0.67 + 0.08
-2- I -I- I 0- I I- I 2- I 3- I 4- I 5- I 6- I -3- 2 -2- 2	- 0.637 - 5.362 - 20.9473 + 15.3859 +115.7133 + 20.7068 + 1.9290 + 0.031 0.00 + 0.004 + 0.014	+ 0. 205 - 1. 084 -83. 7676 -93. 2674 -51. 8406 + 5. 0202 + 2. 3042 + 0. 393 + 0. 06 0. 000 + 0. 037	+ 0. 58 + 2. 97 + 14. 01 - 2. 72 + 9. 37 + 4. 38 + 0. 92 + 0. 12	- 0. 05 - 2. 05 - 31. 68 - 1. 95 + 9. 37 + 0. 93 - 0. 36 - 0. 16	-0. 036 +0. 463 +1. 534 -1. 221 +2. 666 +0. 883 +0. 153 +0. 017 +0. 001	+0. 029 +0. 935 -3. 566 +0. 258 +2. 534 +0. 234 -0. 039 -0. 016 -0. 003	- 0. 36 - 1. 57 - 7. 04 + 1. 39 - 12. 30 - 4. 74 - 0. 89 - 0. 11	- 0. 01 + 2. 29 + 15. 98 + 2. 28 - 11. 71 - 0. 82 + 0. 37 + 0. 11
—I— 2 0— 2	- 0.030 - 0.372	+ o. 336 - 3. ∞3	- 0. 12 + 2. 36	+ 0.32 + 0.21	+0.046 +0.217	+0.023 +0.096	0.02 1.34	- 0. 18 - 1. 01

Arg=i'g'+ig	a'r'	$\left(\frac{r'\frac{d\Omega'}{dr'}}{dr'}\right)$	$a'^2r'rac{d^2\Omega'}{dr'd\mathbf{Z}'}$	$+ a'^2 \frac{d\Omega'}{dZ'}$	$aa'\frac{d}{a}$	$rac{\Omega'}{i\mathbf{Z}}$	$aa'r'\frac{d}{d}$	$rac{d^2\Omega'}{r'dZ}$
	cos.	sin.	sin.	cos.	sin.	cos.	sin.	cos.
i' i	"	11		"	,,	"	"	11
I — 2	17.0443	+ 68. 5236	+17.38	+ 3.64	+2.359	+o. 569	—13.51	2.79
2— 2	—562. 3187	-238. 6124	+ 3.09	- 3.03	+0.485	—о. 339	- 2. 54	+ 2.36
3- 2	— 64. <u>35</u> 81	-145.4312	5.06	+ 7.61	—I. 2II	+1.994	+ 6.85	10.90
4 2	+ 8.5789	— 28. 4054	— о. 13	+ 3.88	-0.045	+o. 784	o, oı	— 4. 69
5 — 2	+ 3.9135	_ 2.7124	+ 0.51	+ 0.90	+0.072	+0.150	— о. 63	— o. 92
6— 2	+ 0.700	+ 0.022	+ 0.19	+ 0.09	+0.023	+0.016	— о. 15	— o. o8
7 2	+ 0.08	+ 0.06			+0.004	0.000		
—2— 3	+ 0.004	0,000						
1	+ 0.004	+ 0.004	ļ		+0.005	+0.003		
-I- 3 0- 3			— o. og	+ 0.06			+ 0.07	— o. o4
1	L '	— 0. 350	— 0.09 — 0.28	+ 1.23	—0.005	+0.009	+ 0.16	— 0.04 — 0.90
I— 3	+ 0. 207	+ 6. 174 - 15. 3762	— 0. 20 — 0. 02		+0.022	+0. 117 +1. 531		
2 3	— 4. I224			+13.75	0.005		+ 0, 07	— 9.97
3— 3	—261. 3672	+373. 3284	+ 3.35	+ 3.21	+0.335	+0.434	2.53	— 2.65 L 2.66
4 3	—149. 9928	+ 41.4181	— 5. 39	- 2.20	1.310	-0.452	+ 8.34	+ 3.06
5— 3	— 31. 8426	— I3.774I	— 3. 13	+ 0.55	-0. 594	+o. o88	+ 4. 10	— o. 82
6— 3	- 3. 068	— 5. 57 I	0.79	+ 0.57	—0. I22	+0.092	+ 0.77	0.79
7— 3	+ 0.14	— I. oo	— 0.02	+ 0.23	-0,012	+0.028	+ 0.08	— o. 19
8— 3	+ 0.08	— O. 12			+0.001	+0.005		
0 4	+ 0.010	- 0.039						
1 4	+ 0.006	+ 0.356	0.07	0.04	0.003	+0.001	+ 0.04	+ 0.04
2— 4	+ 0.932	- I. 349	— 0, 64	+ 0.32	—о. 038	+0.063	+ 0.41	- o. 28
3— 4	— 25 . 880	+ 4.025	— 9· 73	+ 1.98	0. 893	+0. 194	+ 6.65	— 1 .40
4— 4	+217.452	+233.907	2.55	+ 3.39	— 0. 312	+0.312	+ 2.13	2.55
5 4	+ 13.7922	+135.5802	+ 0.65	— 3.39	+o. o86	о. 783	o. 78	+ 5.75
6 4	— 18.57	+ 30.46	— o. 85	— 2.21	-0. 149	—о. 399	+ 1.27	+ 3.06
7— 4	6.88	+ 2.81	— o. 67	— o. 57	0.095	0.084	+ 0.86	+ o. 61
8 4	— I. 28	- o. 33	— o. 15	0.00	-0.028	o. oo6	+ 0.22	+ 0.04
9— 4	— o. 15	o. 15			0. 005	+0.002		
10— 4	0,00	- 0.06			0.001	+0.001	1	
	- 0,010	+ 0.024						Ì
1— 5	1	- 0.024 - 0.083	0,00	— o. o4	0,000	+0.001		
2-5	+ 0.030 - 1.652	1		— 0.04 — 0.11	_o. o58	+0.001	+ o. 38	+ 0.03
3-5		— I.090 — 27.0I	— 0.54 — 2.76	- 6. 16	0.058 0.225	0.482	+ 0.38	+ 4. 12
4- 5	0.43	+ 27.91	- 2.76	— 0.10 — 1.66	0. 225 0. 266			
5-5	+183.95	—108.48	- 3. 14 - 1. 82	1	+0. 428	-0. 191	+ 2.35	+ 1.44 + 0.31
6 5	+109.92	+ 8.83	+ 1.83	0.09		0, 054	3.56	
7- 5	+ 25.44	+ 21.61	+ 1.41	0.90	+0.241	o. 155	2.06	+ 1.45 + 0.85
8— 5	+ 1.91	+ 7.53	+ 0.25	— v. 61	+0.049	—o. o86	— o. 38	
9— 5	— o. 57	+ 1.46	— 0.04	0. 23	+0.001	0. 025	+ 0.04	+ 0, 22
10— 5	— 0. 22	+ 0.15			0.003	-0.005		
11- 5	— o.o8	0,00			-0.001	0,001		
3— 6	— 0.089	0.087			-0.002	+0.001		
4— 6	— I. 42	+ 1.69	- 0, 25	— 0.46	— ¬. 023	—0. 039	+ 0.15	+ 0.34
5— 6	+ 24.48	+ 5.07	+ 3.57	— 2.64	+o. 238	о. 188	— 2. 3I	+ 1.72
6 6	42. 15	—130.96	+ 0.90	2.70	+0.095	0. 208	- o. 82	+ 1.97
7— 6	+ 22.44	80. 96	+ 0.22	+ 0.85	+0.083	+0.213	— o. 64	I. 94
95 A S/III	14			<u> </u>	l		1	

25 AST---14

Arg=i'g'+ig	a'r'	$\left(rac{r' rac{d\Omega'}{dr^i}}{dr'} ight)$	$a'^2r'rac{d^2\Omega'}{dr'dZ}$	$a_{i} + a'^{2} \frac{d\Omega'}{dZ'}$	aa' ⁻	$\frac{d\Omega'}{dZ}$	aa'r'	$rac{d^2\Omega'}{dr'd\mathbf{Z}}$
	cos.	sin.	sin.	cos.	sin.	cos.	sin.	cos.
i' i	. "	"	"	,,,	"	,,	"	"
8— 6	+22. 33	—18. 63	+0.77	+o. 81	+0. 133	+0.129	—1. 3o	—I. 23
9— 6	+ 7.53	— o. 73	+0.55	+0.13	+0.070	+0.022	—o. 71	—o. 15
10— 6	+ 1.44	+ 0.81	+ 0, 20	— 0. 07	+0.021	0. 004	—0. 19	+0.07
11— 6 12— 6	+ 0.14	+ 0.28			+0.004	-0.003		
12— 6	0.00	+ 0.06			0,000	-0,001		
4 7	— O. I2	+ 0.12			0.002	-0.002		
5 7	+ 1.51	+ 1.63	+0. 28	0. 28	+0.021	-0.025	0. 22	+0.19
6— 7	+ 7.99	—18. 6 <u>5</u>	+2. 17	+1.79	+o. 134	+0. 104	—1. 34	—1.14
7— 7	—85. 62	+ 7.18	+2.05	+0.32	+0. 148	+0.037	1.52	—o. 3o
8— 7	 54. 52	—27. 77	-0. 24	+0.19	-0, 094	+0.070	+1.00	o. 67
9 7	—II. 72	20.69	0.43	+0.65	—o. o62	+0.098	+o. 63	-1.07
10— 7	+ 0.55	— 6. 8 ₂	0. 10	+0.46	-0.005	+0, 052	0,00	o. 55
11-7	+ 0.98	— 1, 28	0, 00	+0.17	+0.006	-0. 015	0, 11	—0, 15
12 7	+ o. 35	— O. I2			+0.003	+0.003		
5— 8	+ 0.04	+ 0.19			+0.001	-0.002		
6— 8	+ 1.75	— I. oo	+o. 35	+0.13	+0.021	+0.009	— 0. 22	o. o8
7— 8	—12.65	— 8.91	— о. 78	+1.54	o. o38	+0.086	+0.44	-o. 89
8 8	7.87	+51.76	-0.11	+1.52	-0.004	—o. o 99	+0.07	-1.01
9— 8	—26. 85	+33.46	+o. o8	0. 08	0.047	0. 034	+0.52	+0.30
10— 8	-17.60	+ 6.02	+0. 28	0.46	—o. o67	0. 023	+o. 81	+0.22
11—8	— 5 . 68	— I. 42	+0.23	—0. 2I	o. o35	+0.004	+0.47	0, 00
12 8	— 1. o8	— I. 22	+0, 11	0.00	0.011	+0.007	+ 0. 14	0.00
6— 9	+ o. 17	0,00			+0.002	0,000		
7— 9	o. 59	1.67	0.00	+0.26	-0.002	+0.015	+0.10	-o. 32
8— 9	— 8. 14	十 7.59	1.00	—о. 16	-o. o51	o. oo8	+0.48	+0. 25
9 9	+28.83	+11.92	0, 94	⊹0. 16	-0.062	-0.010	+o. 38	+0.63
10— 9	_+18.41	+22.62	-0.91	+0.14	+0.008	o. o26	о. 53	+o. 65
11 9	+ 1.87	+13.85	— 0, 49	—о. 13	+0.004	-0. 042	60	+0.06
12—_9	— 2. 26	+ 4.64	— 0. 11	-0. 2I	0. 008	0. 025	0, 20	-0. 20
710	+ 0.02	0.04			0.000	+0.002		
8—10	— I. 37	+ 0.17	0. 37	0.07	-0.010	+0,002	+0.04	+0.07
9—10	+ 3.97	+ 6.65	+o. 18	0. 55	0. 003	0. 028	+0.39	— 0. 06
10—10	+10.92	—14. 53	+0.45	o. 28	-0.014	— о. 035	+0.25	+0.05
11—10	+17.27	— 8. 71	+o. 21	+0. 25	+0.013	-0.002	+0.13	+0.49
12—10	+11.02	+ 1.10	—0. 10	+o. 28	+0.031	-0. 002	—0. 19	+0.32
8—11	— o. I4	o. o8			-0.001	+0.001		
9—11	— o. o8	+ 1.06	+0.07	-0.04	-0.003	-o, oo6	+0.11	0.00
1011	+ 4.94	— 1. 59	- 0. 14	—0. 32	+0.014	о. 006	0, 01	—o. 21
11—11	6.43	— 8. 18	0, 00	о. 35	+0.019	-o. o13	+v. o6	—о. 17
12—11	2.77	—13.69	+0.21	0. 11	o. oor	+0.014	+o. 18	+o. o6
9—12	— o. o8	+ 0.10			0.001	0. 001		
10—12	+ 0.75	+ 0.28	0, 00	— 0. 07	+0.003	0. 002	+0.03	-o. o3
11—12	— o. 28	— 3. 32	—о. 18	+0.07	+0.005	+0.006	0. 14	-0.04
12—12	— 6. 94	+ 1.97	-o. 25	-0.04	+0.002	+0,003	+0.04	+0.03

Before we can write the expressions for the first eight factors of δT we have to pass through the intermediate stage of deriving V, X, and \overline{T} . It will be seen that in all cases, except that of X, the factors involving γ are the factors A and B, whose expressions have been given at pages 73, 74. In the case of X, putting

$$X = Ma \frac{d\Omega}{da} + Nar \frac{d\Omega}{dr}$$

we have

$$\mathbf{M} = -\frac{2r\rho}{\mathbf{a}^2 \cos^2 \varphi} \cos (f - \omega) \qquad \qquad \mathbf{N} = -\frac{2\rho}{\mathbf{a} \cos^3 \varphi} [\sin f \cos \omega - (\cos f + e) \sin \omega]$$

For a similar reason, as in deriving the expression for T, we can dispense with any direct computation of the terms of δT involving higher multiples of γ than the first, as all such terms in W are computed very readily by the formulæ of page 74. This abbreviation in determining T is applicable, no matter how far the approximation may be pushed; it is also true for each portion of T under restrictions which are readily seen. In consequence, availing ourselves of the quantities P and Q of page 63, in M and N, it suffices to put

$$\frac{\rho}{a}\cos\,\omega = \frac{1}{2}P_0 + P_1\cos\,\gamma \qquad \qquad \frac{\rho}{a}\sin\,\omega = Q_1\cos\,\phi\,\sin\,\gamma$$

and we also have

$$\frac{r}{a}\cos f = \frac{1}{2}P_0 + P_1\cos g + P_2\cos 2g + P_3\cos 3g + \dots$$

$$\frac{r}{a}\sin f = \cos \varphi \left[Q_1\sin g + Q_2\sin 2g + Q_3\sin 3g + \dots\right]$$

$$\frac{\cos f + e}{\cos \varphi} = \cos \varphi \left[Q_1\cos g + {}_2Q_2\cos 2g + {}_3Q_3\cos 3g + \dots\right]$$

$$\frac{\sin f}{\cos \varphi} = P_1\sin g + {}_2P_2\sin 2g + {}_3P_3\sin 3g + \dots$$

From these equations we derive

$$\begin{split} \mathbf{M} &= -\frac{\mathbf{P}_0}{\cos^2 \varphi} \left[\frac{\mathbf{I}}{2} \mathbf{P}_0 + \mathbf{P}_1 \cos g + \mathbf{P}_2 \cos 2g + \mathbf{P}_3 \cos 3g + \dots \right] \\ &- \frac{i = +\infty}{2} \left[\frac{\mathbf{P}_1 \mathbf{P}_i}{\cos^2 \varphi} \pm \mathbf{Q}_1 \mathbf{Q}_i \right] \cos \left(\gamma \mp ig \right) \\ \mathbf{N} &= -\frac{\mathbf{P}_0}{\cos^2 \varphi} \left[\mathbf{P}_1 \sin g + 2\mathbf{P}_2 \sin 2g + 3\mathbf{P}_3 \sin 3g + \dots \right] \\ &+ \sum_{i=0}^{i=\infty} i \left[\mathbf{Q}_1 \mathbf{Q}_i \pm \frac{\mathbf{P}_1 \mathbf{P}_i}{\cos^2 \varphi} \right] \sin \left(\gamma \mp ig \right) \end{split}$$

It is evident that M and N are connected by the equation

$$N = -\frac{dM}{dg}$$

Applying these formulæ to Jupiter we get

$$\begin{aligned} \mathbf{M} &= - & [8.0210889] & + 2[8.8601562] \cos \gamma & - 2[6.76559] \cos (\gamma + g) \\ &+ 2[8.8601562] \cos g & - 2[0.000005] \cos (\gamma - g) & - 2[5.06865] \cos (\gamma + 2g) \\ &+ 2[7.2422636] \cos 2g & - 2[8.3821499] \cos (\gamma - 2g) \\ &+ 2[5.8004832] \cos 3g & - 2[6.9403906] \cos (\gamma - 3g) \\ &+ 2[4.4324972] \cos 4g & - 2[5.5724173] \cos (\gamma - 4g) \end{aligned}$$

```
 N = + 2[8.8601562] \sin g + 2[0.0000005] \sin (\gamma - g) 
 + 2[7.5432936] \sin 2g + 2[8.6831799] \sin (\gamma - 2g) 
 + 2[6.2776045] \sin 3g + 2[7.4175119] \sin (\gamma - 3g) 
 + 2[5.0345572] \sin 4g + 2[6.1744773] \sin (\gamma - 4g) 
 - 2[6.76559] \sin (\gamma + g) 
 - 2[5.36968] \sin (\gamma + 2g)
```

And, similarly for Saturn, we get

```
M' = - [8.1518373]
      + 2[8.9255751] \cos g'
                                              N' = + 2[8.9255751] \sin g'
      + 2[7.3727757] \cos 2g'
                                                     + 2[7.6738057] \sin 2q'
      + 2[5.9960961] \cos 3g'
                                                     + 2[6.4732174] \sin 3g'
      + 2[4.6932130] cos 4g'
                                                     + 2[5.2952730] \sin 4g'
      + 2[8.9255751] \cos \nu'
                                                     + 2[0.0000000] \sin(\gamma' - g')
      -2[0.0000000]\cos(\gamma' - q')
                                                    + 2[8.7482885] \sin(\gamma' - 2q')
      -2[8.4472585]\cos(\gamma'-2g')
                                                    + 2[7.5477287] \sin(\nu' - 3g')
      -2[7.0706074]\cos(\nu'-3g')
                                                    + 2[6.3698013] \sin (\gamma' - 4g')
      -2[5.7677413]\cos(\gamma'-4g')
                                                    + 2[5.2047001] \sin(\gamma' - 5g')
      -2[4.5057301]\cos(\nu'-5g')
                                                    -2[6.89630] \sin(\gamma' + g')
      -2[6.89630]\cos(\gamma' + g')
                                                     -2[5.56550] \sin (\gamma' + 2g')
      -2[5.26447]\cos(\gamma'+2g')
```

We can now give the values of V and X. It is thought unnecessary to give the partial derivatives with respect to g or g' of any expression which has already been given, for the reason that they can so easily be formed. The expressions for B and G are appended:

A	rg=	V		Σ	X		3	G	
ну+	-i ⁷ g'+ig	sin.	cos.	sin.	cos.	sin.	cos.	sin.	cos.
и	i' i	"	11	"	+0.06138	"	+o. o6138	11	"
1	0-1	-42. 307	— 0. o66	+14.278	0. 025	28. 029	-0.091	+56.586	+0.082
—I	0 0	3.951	+4.621	+ 1.17913	—0. 84751	— 2.772	+3.773	+ 5.093	— 5. 638
0	o 1	+ 2.60940	-2.04419	— 1. 0 36 5 9	0. 00354	+ 1.57281	-2. 04773	— 3 . 5 3363	+2.54858
1	0 2	+ 0.478	—I. 882	+ o. 127	+0.510	+ o. 6o5	—1. 372	- o. 389	+2. 224
1	o— 1	— 0. 2 69	-0. 447	+ 0.035	+0.073	— o. 234	—o. 374	+ o. 318	+0.530
0	0 2	+ 0. 19153	+0. 26064	— o. oo889	— 0. 03706	+ 0. 18264	+0. 22358	— 0. 2 4191	-0. 31404
1	o 3	+ 0.059	+0.034	0.012	+0,004	+ 0.047	+0.038	— o. o58	о. озо
—1	0 2	+ 0.032	-0.015	— 0.004	+0.002	+ 0.028	o. o13	— o. o3б	+o. o18
0	o— 3	0.01704	+0.01396	+ 0.00088	-0.00020	— o. o1616	+0.01376	+ 0.01850	0. 01740
1	0 4	0.004	+0.002	0.000	0.001	0.004	+0.001	+ 0.005	0.001
-1	o— 3	+ 0.001	0.000			+ 0.001	0.000	0,001	0.000
0	0-4	— 0.00100	-0.00102	— 0.00004	+0.00003	- 0.00104	-0.00099	+ 0.00111	+0.00102
I	o— 5	+ 0.001	+0.001			+ 0.001	+0.001	0.001	-0.001
I	1+ 4	0,000	-0.007			0,000	-0.007	0.000	+0.007

A	ro=	v		X	:	В		(}
иу+	rg= $-i'g'+ig$	sin.	cos.	sin.	cos.	sin.	cos.	sin.	cos.
ж	i' i	11	"	11	"	"	"	"	11
٥	1+3	+ o. oo236	+ 0.01264	— o. ooo11	+ 0.00008	+ 0.00225	+ 0.01272	- 0.00259	- 0.01285
1	1+ 2	— o. oo5	— o. oo8	0,000	+ 0.001	— o, oo5	0.007	+ 0.005	+ 0.009
—I	1+3	— o. oo7	+ 0.012	+ 0.002	- 0.001	— o. oo5	+ 0.011	+ 0.007	- 0.012
٥	1+ 2	— 0.00704	+ 0.03441	— o. oo138	— o. oo381	- 0.00842	'		— o. o4o73
I	1+1	+ 0.006	— o. o63	0.000	+ 0.009	+ 0.006	0. 054	- 0.008	+ 0.073
_I	1+ 2	0. 230	— 0. 170	+ 0.018	+ 0.052	- 0. 212	o. 118	+ 0.249	+ 0.203
°	1+1	— 0. 36721	- 0.07128	+ 0. 10334	- 0. 05272		- 0. 12400	+ 0.47094	+ 0.08718
i .	IO	+ 0.726	+ 0.301	— o. 158	- 0.035	+ 0.568	+ 0.266	0.885	0, 364
—I	1+1	+ 4.870	- 4. 130	1.426	+ 0.719	+ 3.444	- 3.411	6. 254	+ 5.054
0	1 0	0.00000	0,00000	+ 0.16312	+ 0.78650			0,00000	0.00000
I	1 — 1	- 5.0412	+ 3.3090	+ 1.365	- I. 009	- 3.676	+ 2.300	+ 6.4715	3. 9986
-r	1 0	+ 9.922	+49. 739	- 2.095	10. 824	+ 7.827	+38.915	- 12.499	—62. 969
°	1— 1	— 4. 91261	-25. 32954	— o. o8o79	+ 0.00778				+32.55616
I	I— 2	— 3. 370 L 0700	-15. 844	+ 1.271	+ 5.956	— 2.099	— 9. 888	+ 4.173	+19. 399
-I	I— I	I.0709	- 3.6163	0.248 0.08917	+ 0.902	— I. 319	- 2.714	+ 0.5641	+ 4.7236
0	I— 2	— 0. 24520 - x 220	+ 2. 59490 - 0. 649		— o. 43467		+ 2. 16023	+ 0.96309	— 3. 47275
I	1— 3	+ 1.229	1	— 0. 12 5	+ 0. 205	+ 1.104	— 0. 444	— 1.633	+ 0.942
i	I 2	+ 0.257	— 0. 302	- 0.040	+ 0.046	+ 0.217	— 0. 256	— 0.316 - 0.32884	+ 0.370
°	1— 3	0.25009	+ 0. 30458	+ 0.00917	- 0.01476	- 0. 24092 + 0. 061	+ 0. 28982	+ 0.33884	— 0. 3924I
I	1— 4	+ 0.063	- 0, 045	0.002 0.000	+ 0.001		0.044	- 0.098	+ 0.072
-r	1-3	+ 0.017	+ 0.008	+ 0.00011		' '	+ 0.009	- 0.020	— 0.008
l °	1-4	- 0.02090	+ 0.00453	0.00011	- 0.00011	- 0.02079	+ 0.00442	+ 0.02744	— 0, 00854
I	1— 5	+ 0.004	- 0,005	0,000	0.000	+ 0.004 - 0.002	— 0.005	0.007	+ 0.007 0.000
_I	I 4	— 0.002	0,000	0, 00003	— 0. 00002	- 0.002 - 0.00041	+ 0.00002	+ 0.002	0.00028
0 1	ı— 5 ı— 6	- 0.00038 + 0.001	0.0005	- 0.00003	- 0,00002	+ 0.001	0.000	+ 0.00071 - 0.001	0.000
1 *	1 0	+ 0.001							
0	2+ 3	+ 0.00026	— o. ooog8			+ 0.00026	— o. ooog8		+ 0.00098
—I	2+ 3	— o. ooi	0,000	+ 0.001	0.001	0,000	0,001	+ 0.001	0.000
0	2+ 2	+ 0.00104	+ 0.00381	— o. ooo36	— 0. 00027	+ o. ooo68	+ 0.00354	- 0.00102	— 0. 00446
1	2+ I	— o. oo3	— o. oo7	0.000	+ 0.001	— o.oo3	0.006	+ 0.003	+ 0.007
_ı	2+ 2	- 0.042	— o. oo3	+ 0.005	+ 0.004	— o. o37	+ 0.001	+ 0.047	+ 0.004
0	2+ I	— 0. 03928	1	+ 0.00691	— o. o1064	- 0.03237	+ 0.00065	+ 0.04882	— o. o1335
I	2 0	+ 0.103	- 0.009	— o. o18	+ 0.005	+ 0.085	- 0,004	— 0. 123	+ 0.010
—I	2+ I	+ 0.171	— o. 874	— 0. 096	+ 0.146	+ 0.075	— 0. 728	- 0, 224	+ 1.044
°	2 0	0,00000		+ 0.23489	+ 0.05967		1		0.00000
I	2— I	— 0. <u>5469</u>	+ 0.8643	+ 0.079	- 0. 201 - 0. 828	— 0.468 — 11.413	+ 0.663	+ 0.7447	- 1.0511
I	2 0	+ 14.636	+ 4.668	- 3. 224		+ 11.412	+ 3.840	— 19.532 — 13.33044	- 5. 243 - 0. 01733
°	2— I	— 9.60269	I .	— 2. 38232	+ 1.03341	— 11.98501 ± 2.4712	— 0. 08053	1	+ 0.91722
I .	2 2	+ 1.5995	— 4. 6390	+ 0.8718 +32.814	+ 0.8956	+ 2.4713	— 3. 7434 ±26. 072	— 3.119 +167.6953	+ 6. 101
1—1	2 1	—119. 8230	+51.0393	— 0, 04681	-14.067 + 0.00420	— 87.009 +105.96987	+36.972		71. 5954 +64. 68104
°	2— 2	+106.01668					—45. 27521 —10. 252	—151.09782 ± 24.207	
I	2— 3	— 21. 930	+ 9. 193	— 2. 562	+ 1.159	— 24. 492 — 1. 3520	+10.352	+ 34. 297 - I 400	-14.464
i	2— 2	+ 1.5773	+ 3. 3876	- 0. 2253	- 0. 9535 - 0. 08052	+ 1.3520 + 2.52882	+ 2.4341	— 1.499 — 4.15522	— 5.02I — 7.02004
0	2- 3	+ 2.35012	I	+ 0. 18871	- 0. 08052				+ 7.92094 - 2.442
I .	2 4	— I. 3I3	+ 2.471	— 0. 143	+ 0.017	— 1.456 ⊥ 0.285	+ 2.488	+ 2. 193 - 0. 280	— 3· 443 — 0· 340
I	2 3	+ 0.329	+ 0.256	0.044	— o. o45	+ 0. 285	+ 0.211	— o. 380	0. 340
							·		

A	rg=	V		2	K	В		(3
ну+	i ⁷ g'+ig	sin.	cos.	sin.	cos.	sin.	cos.	sin.	cos.
и	i' i 2— 4	,, — 0. 15465	// 0.49077	" + 0.01045	0, 00100	// 0, 14420	o. 49177	" + 0. 11231	,, + o. 67980
ı	2 5	- o. o25	+ 0.213	- 0,004	+ 0.002	— 0. 029	+ 0.215	+ 0.068	— o. 300
_r	2— 4	+ 0.007	+ 0.015	- 0.002	— 0. 00I	+ 0,005	+ 0.014	0.009	— 0.019
0	2 5	— o. o1114	— 0. 03543		— 0, 000I4	- o. o1086	— o. o3557	+ 0.01030	+ 0.04823
ı	2 - 6	+ 0.004	+ 0.016	- 0.00I	0.000	+ 0.003	+ 0.016	- 0,002	- 0.022
0	2— 6	- 0.0063	— 0. 00167	+ 0.00003	- 0.00002	— o. ooo6o	0.00169	+ 0.00064	+ 0.00244
_1	3+ 2	— o. oo4	+ 0.003	+ 0.001	+ 0.001	— o. oo3	+ 0.004	+ 0.005	— o, oo3
0	3+ I	— o. oo325	+ 0.00302	+ 0.00007	— o. 00140	— o. oo318	+ 0.00162	+ 0.00398	— 0.00353
ı	3 0	+ 0.010	— o. oo8	_ 0.001	+ 0.001	+ 0.009	0.007	- 0.012	+ 0.009
—т	3+ I	— o. o48	— o. 110	0,002	+ 0.017	_ o. o5o	- 0, 093	+ 0.055	+ 0.130
0	3 0	0,00000	0.00000	+ 0.04330	- 0.01001	+ 0.04330	- 0.01001	0.00000	0.00000
1	3— I	— o. 014	+ 0. 151	- 0,004	— o. o26	- 0.018	+ 0. 125	+ 0.031	— o. 185
_1	3 0	+ 2.774	— o. 827	— o. 596	+ 0.138	+ 2. 178	o. 689	- 3.652	+ 1.145
0	3— I	— 1. 67802	+ 0.77926		+ 0. 44085	— 2. 02 4 36	+ 1. 22011	+ 2. 32527	I. 08947
1	3— 2	— o. 156	- 1.046	+ 0.196	+ 0.050	+ 0.040	- o. 996	— 0. 024	+ 1.418
i	3— I	—I4. 922	+28.851	+ 4.787	- 6. 057	—10. 135	+22. 794	+21.657	— 37. 882
0	3— 2	+12.87302	—24. 26454	— o. 99807	— 1.40617	+11.87495	-25.67073	—19. 23030	+ 32.41300
1	3-3	- 0. 237	+ 6.511	0. 474	+ o. 666	— 0. 711	+ 7.177	+ 1.382	— 9. 236
_r	3 2	69. 022	-99. 317	+13.584	+19.364	-55.438	-79.953	+89. 055	+127.729
0	3— 3	+64. 65315	+91.45689		- 0.04272	+64. 60081	+91.41417	—84. 13717	—118. 41682
1	3— 4	16. 577	-23. 474	— o. 8o6	— I. 074	—17. 383	-24. 548	+22, 261	+ 31.276
I	3— 3	- 6. 595	+ 1.056	+ 1.195	- o. o78	_ 5.400	+ 0.978	+ 8.559	— 0. 940
0	3-4	+ 9. 10247	+ 2.31940		+ 0.08122	+ 9. 15686	+ 2.40062	—11. 81818	— 3. 46238
I	3— 5	— 3. 450	- 1. 223	- 0.052	0.076	- 3.502	— I. 299	+ 4.476	+ 1.767
—I	3 - 4	0. 332	+ 0.407	+ 0.054	- 0.048	— 0. 278	+ 0.359	+ 0.434	— 0.469
0	3— 5	+ 0.71640	- 0. 26172		+ 0.00582	+ 0.72003	0. 25590	- 0. 93326	+ 0.26690
ı	3 6	- o. 319	+ 0.031	- 0.004	- 0.004	- o. 323	+ 0.027	+ 0.416	— o. o16
_1	3— 5	— 0. 014	+ 0.023	+ 0.004	- 0.003	- 0.010	+ 0.020	+ 0.019	- 0. 028
0	3 6	+ 0.04652	— o. o3167	+ 0.00027	+ 0.00021	+ 0.04679	— o. o3146	— o. o6108	+ 0.04687
I	3 7	- 0.024	+ 0.011	0.000	- 0.001	0.024	+ 0.010	+ 0, 031	- 0.112
I	3— 6	— o, oo4	+ 0.003			0.004	+ 0.003	+ 0,004	— o. oo3
0	3 7	+ 0.00216	l .	+ 0,00002	+ 0.00002		- 0.00283		+ 0.00326
—I	4+ 1	0.014	- 0.009	0,000	+ 0.002	— o. o14	- 0.007	+ 0.016	+ 0.011
0	4 0	0. 00000	0, 00000	+ 0.00501	- 0.00354	+ 0.00501	- 0.00354	0,00000	0.00000
1	4— 1	+ 0.009	+ 0.018	- 0.002	0.002	+ 0.007	+ 0.016	0.009	_ o. o23
—ı	4 0	+ 0. 294	- o. 312	o. o68	+ 0.049	+ 0. 226	— o. 263	— o. 390	+ 0.399
0	4— I	— 0. 15912	+ 0. 20917	- 0. 01243	+ 0.08450	— o. 17155	+ 0. 29367	+ 0. 22774	_ o. 27809
1	4- 2	— O. 1275	— o. 1234	+ 0.029	- o. oo8	— o. o98	- o. 131	+ 0. 1295	+ 0. 1795
—ı	4 I	+ 1.076	+ 5.719	+ 0. 173	— 1. 16 <u>5</u>	+ 1.249	+ 4. 554	÷ 0.913	− 7 · 434
0	4— 2	— o. 80131	- 4.64775	— o. 46277	- o. 23345	- I. 26408	- 4. 88120	+ 0.59118	+ 6. 16744
I	4-3	+ 1.113	+ 0.841	- 0.014	+ 0. 165	+ 1.099	+ 1.006	- I. 287	- I. 29I
-1	4 2	—37. 5113	-12.8716	+ 6.362	+ 3. 232	—3 1 . 149	— 9. 640	+46.9598	+ 17.4477
0	4— 3	+33.88113	+11.94483	l .	— 0. 79007	+34. 60310	+11.15476	—42. 76022	— 16. 35448
I	4 4	- 9. 727	— 1.061	- 0.463	- 0. 208	-10. 190	— 1. 269	+12.570	+ 1.919
_ı	4-3	+66. 142	70. 334	- 9· 953	+10.743	+56. 189	—59. 591	80. 770	+ 86. 232
0	4 4	-61.53333	+67. 26806				+67. 20284	+75. 35198	- 82. 84294
1	4-5	+17.070	—18. 743	+ 0. 422	— o. 498	+17.492	-19. 241	-21. 161	+ 23.418
		I	1		1	<u> </u>	1 .	l	1

Arg=	V	7	2	K	F	3	(3
$\mu\gamma + i^7g' + ig$	sin.	cos.	sin.	cos.	sin.	cos.	sin.	cos.
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	1. 666	- 7.835	+0. 157	// +1,109	 - 1.509	 — 6. 726	+ 1.786	" + 9.621
0 4-5	- o. 62573	+10. 33047	—o. o344o	+0.03220	— 0, 66013	+10. 36267	+ 1.16777	13.49758
I 4— 6	+ 0.541	- 3.759	+0.034	-0.049	+ 0.575	— 3. 8o8	— o. 762	+ 4.636
<u>-1</u> 4- 5	- o. 507	— o. 373	+0.053	+0.054	— o. 454	— o. 319	+ 0.584	+ 0.471
0 4-6	+ 0.44699	+ 0.80753	-0.00274	+0.00340	+ 0.44425	+ 0.81093	— o. 50166	— I. 00475
1 4-7	— o. 115	- o. 361	0.000	0.003	- o. 115	— o. 364	+ o. 126	+ 0.448
_r 4— 6	- o. o35	— o. o16	+0.005	+0.001	— o. o3o	- o. o15	+ 0.042	+ 0,020
0 4-7	+ 0.05370	+ 0. 04836	0. 00009	+0.00028	+ 0. 05361	+ 0.04864	— o. o6209	— o. o6136
I 4-8	— o. o24	- 0.019	0.000	0.000	0. 024	— o. o19	+ 0.027	+ 0.026
—I 4— 7	0,003	0.000			0.003	0.000	+ 0.003	0.000
o 4—8	+ 0.00746	+ 0.00266	+0.00002	+0.00004	+ 0.00748	+ 0.00270	— o. oo823	0.00341
0 5 0	0.00000	0, 00000	+0.00039	0.00062	+ 0.00039	— o. ooo62	0, 00000	0, 00000
_r 5 o	+ 0.014	0.054	—o. oo6	+0.008	+ 0.008	— o. o46	0.02I	+ 0.068
0 5— 1	- 0.00532	+ 0.03191	+0.00424	+0.01045	— 0. 00108	+ 0.04236		— 0. 04195
1 5 2	— o. o265	- 0.0022	+0.002	-0.004	0.024	o. oo6	+ 0.0302	+ 0.0075
—I 5— I	+ o. 658	+ 0.615	0. 059	—o. 143	+ 0.599	+ 0.472	o. 76o	— 0.820
0 5— 2	0. 50428	— o. 48746	—o. o9999	+0.00414	— 0. 60427	— o. 48332	+ 0.58105	+ 0.66878
I 5— 3	+ 0. 2505	— 0. 0502	+0.0121	+0.0258	+ 0. 2626	- 0.0244	— 0. 312	+ 0.019
—I 5— 2	8. 1002	+ 2.5012	+1.378	o. o55	— 6.722	+ 2.446	+10.1287	- 2.6538
o 5— 3	+ 7.20416	- 2.07513	+-0. 10788	-0.40042	+ 7.31204	- 2.47555	+ 9.09206	+ 2. 16585
1 5-4	— 1.698	+ 1.452	-0. 123	+0.013	1.821	+ 1.465	+ 2. 252 - 8. 396	— 1.669 +47.462
_1 5— 3	+ 6. 2989	—39. 2994 1 a6 6 7 7 7 7	1.5016	+5.5027	+ 4.7973	-33. 79 ⁶ 7 +36. 96884	- 8. 390 + 8. 05541	—44· 45554
0 5—4	— 6. 02469	+36.65055	1	+0.31829	— 5.47116 + 0.167	—11.066	— 0. 425	+13. 220
1 5 5	+ 0, 102	—10. 769	+0.065	-0. 297	+52.812	+31.826	— 0. 423 —71. 476	-42. 695
-I 5-4	+60. 330	+36. 232	—7. 518 +0. 05776	-4. 406 +0. 00303	58. 17801	-33. 4047 I	+69. 1 7473	+39.40340
o 5— 5 1 5— 6	-58.23577 +16.908	-33.40774 + 9.586	+0.03770 +0.285	+0.147	+17. 193	+ 9.733	-20, 242	—II. 368
1	+ 7.371	- 2. 620	o. 863	+0. 256	+ 6.508	- 2. 364	- 8. 749	+ 2.952
0 5— 6	— 9. 50437	+ 1. 35024	_	-0. 01457	— 9. 521 96	+ 1. 33567	+11.29325	— I. 4519I
I 5— 7	+ 3.415	0. 232	+0.035	+0.010	+ 3.450	- 0. 222	— 4. o68	+ 0. 225
_1 5-6	+ 0.348	- o. 581	0.043	+0.055	+ 0.305	o. 526	0. 42 5	+ o. 665
0 5-7	- 0. 73758	+ 0.61744		-0.00106		_	+ 0.88915	— o. 70284
1 5— 8	+ 0. 320	- 0. 203	+0.002	0.000	+ 0. 322	- 0. 203	— o. 386	+ 0. 230
5— 7	- 0.003	— o. o48	0.000	+0.005	0.003	- 0.043	0.000	+ 0.055
0 5—8	0.03542	+ 0.07007		+0.00002	— o. o3565	+ 0.07009		— o. o8o92
I 5— 9	+ 0.026	- 0, 025	0.000	+0.001	+ 0.026	0. 024	— o. o31	+ 0.029
_i 6 0	+ 0.002	_ o. oo7	0. 001	+0.001	+ 0.001	o. oo6	- o. oo2	+ 0.009
о 6— г	+ 0.00121	+ 0.00347	+0.00111	+0.00082	+ 0.00232	+ 0.00429	— o. 00112	0. 00460
I 6— 2	- o. oo7	+ 0.003	0.000	-0.001	— o. oo7	+ 0,002	+ 0.008	0.003
_1 6— 1	+ 0. 127	+ 0.018	-o. o15	0. 012	+ 0.112	+ 0.006	— o. 151	0.033
0 6— 2	o. o9454	- o. o1527	o. o1336	+0.00844	— 0. 1 0790	— o. oo683	+ 0.11348	+ 0.02895
r 6— 3	+ 0.023	o. o35	+0.004	+0.003	+ 0.027	0. 032	- 0.032	+ 0.037
_ı 6— 2	— o. 906	+ 1.187	+o. 183	o. 115	0. 723	+ 1.072	+ 1.170	- I. 373
o 6— 3	+ o.80735	— I. 00270	0. 02283	0. 09477	+ 0.78452	- I. 09747	1.05474	+ 1.16180
r 6— 4	o. o35	+ 0.421	0. 020	+0.014	— o. o55	+ 0.435	+ 0.085	— o. 506
	<u> </u>	1					·	

Arc	σ <u> </u>	v		X		F	3	G		
Arg ny+i	⁷ g'+ig	sin.	cos.	sin.	cos.	sin.	cos.	sin.	cos.	
	i' i 6— 3	" - 4. 312	// — 9. 070	" +o. 313	" +1.306	" — 3. 999		,, + 4.826	// +10.991	
o	6— 4	+ 3.83036	+ 8.40510	+0.30416	+o. o1677	+ 4. 13452	+ 8.42187	— 4. 28505	—10. 23334	
l .	6 5	- I. 86o	- 2. 128	0. 025	-o. o83	— 1.885	2. 211	+ 2.138	+ 2.657	
	6 4	+35.265	— o. 951	-4. 179	-0. 245	+31.086	- 1.196	-41.461	+ 0.666	
О	6— 5	—33. 42872	+ 0.92270	о. 10883	+0. 35440	33-53755	+ 1.27710	+39.40245	— 0. 66207	
•	6— 6	+ 9.919	— I.438	+o. 18o	+0.001	+10.099	— I. 437	11.775	+ 1.541	
_r	6— 5	15. 257	+45.748	+1.527	-4.810	— 13.730	+40. 938	+17.475	52.881	
	6— 6	+13.48590	44. 28526	+o. oo850	+0.04282	+13.49440	-44. 24244	—15.41530	+51.27238	
ı	6— 7	— 3.910	+13.158	-0.040	+o. 152	— 3. 950	+13.310	+ 4.470	—15. 305	
— I	6— 6	+ 3.285	+ 5.909	0. 297	— 0. 593	+ 2.988	+ 5.316	— 3. 710	— 6, 850	
0	6— 7	— 2. 74770	— 7.52 924	+o. oo664	-0.00916	— 2.74106	- 7.53840	+ 3.09747	+ 8. 73198	
1	6— 8	+ 0.790	+ 2.699	0, 000	+0.023	+ 0.790	+ 2.722	— o. 890	- 3. 135	
-1	6- 7	+ 0.609	+ 0. 242	0.052	— 0. 026	+· o. 557	+ 0.216	— о. 690	0, 293	
٥	6 8	— o. 70733	— o. 55988	+0.00034	-0.00159	— o, 70699	- 0. 56147	+ 0.80134	+ o. 66o34	
1	6— 9	+ 0. 246	+ 0.258	0.000	+0.001	+ 0.246	+ 0. 259	— o. 279	— 0. 302	
I	6 8	+ 0.054	— o. oog	0.005	-0.001	+ 0.049	0.010	— о. обт	+ 0.008	
0	6 9	- o. o8o84	— o. o2o53	0.00004	-0.00015	o. o8o88	— o. o2o68	+ 0.09182	+ 0.02593	
1	6-10	+ 0.033	+ 0.016	0, 001	0.000	+ 0.032	+ 0.016	0. 037	0.019	
1	6 9	+ 0.003	- 0.002			+ 0.003	- 0, 002	— o. oo3	+ 0.002	
0	6—10	— o. oo895	+ 0.00154	0.00000	+0.00001	— o. oo895	+ 0.00155	+ 0.00968	0.00141	
1	6-11	+ 0.007	0. 001			+ 0.007	- v. 001	— o. oo7	+ 0.001	
0	7 I	+ 0.00028	+ 0.00024	+0.00017	+0.00001	+ 0,00045	+ 0.00025	— o. ooo31	— 0. 00031	
1	7— 1	+ o. o16	— o. oo4	-0.003	0,000	+ 0.013	— o, oo4	0.019	+ 0,004	
	7— 2	- 0.01121	+ 0.00514	-0. 00103	+0.00196	— 0. 01224	+ 0.00710	+ 0.01384	— 0, 00493	
1	7— 3	- 0,002	— o. oo8	+0.001	0,000	- 0.001	- 0.008	+ 0.001	+ 0.009	
—1	7 2	— 0.011	+ 0. 229	+0.015	-0. 027	+ 0.004	+ 0. 202	+ 0.029	— 0. 27 I	
0	7-3	+ 0.01481	— o. 19650	-0. 0I232	-o. o1321	+ 0.00249	O. 2097I	- 0.03314	+ 0.23289	
1	7 4	+ 0.046	+ o. o6o	0.002	+0,004	+ 0.044	+ 0.064	— o. o48	0. 074	
—ı	7- 3	— I. 74I	- 1.015	+ 0. 169	+0. 183	— 1. 572	— o. 832	+ 2.003	+ 1.276	
0	7— 4	+ 1.55014	+ 0.95182	+0.07687	о. 03586	+ 1.62701	+ 0.91596	— 1. 7876 7	— I. 20325	
1	7 5	— o. 583	- 0.072	0.014	o. o13	— o. 597	— o. o85	+ o. 685	+ 0. 123	
—1	7— 4	+ 8.502	5. 904	1. 060	+0.490	+ 7.442	- 5.414	10. 056	+ 6.668	
	7- 5	- 8. 04741	+ 5.45171	+0. 03494	+0. 20882	8. 01247	+ 5.66053	+ 9.54307	— 6. 166 27	
1	7 — 6	+ 2.059	— 2. 206	+0.052	0. 028	+ 2.111	- 2. 234	- 2.484	+ 2.521	
_r	7— 5	+ 6.582	+27.992	o. 468	-2.869	+ 6.114	+25.123	— 7.312	-32. 241	
0	7— 6	— 6. 68419	—26. 75 840	—0. 210 33	-0.01411	— 6. 8 ₉₄₅₂	-26. 77251	+ 7.39450	+30.86979	
I	7 7	+ 3.059	+ 7.966	+0.048	+0. 102	+ 3.107	+ 8.068	— 3. 36 1	- 9. 232	
—I	7 6	—31. 422	— 3. o29	+2.852	+0. 222	—28. 570	2.807	+35.649	+ 3. 328	
	7— 7	+30.34215	+ 1.89095	0. 02985	+0.01298	+30. 31230	+ 1.90393	—34. 46121	2.02011	
	7-8	9. 126	— o. 464	-o. o77	+0.001	— 9. 20 <u>3</u>	— o. 463	+10. 398	+ 0.482	
	7— 7	- 4. 157	+ 3.443	+o. 362	o. 28o	— 3·795	+ 3. 163	+ 4.732	— 3.859	
	7— 8	+ 5. 26380	- 3. 32770	+0.00452	+0.00320	+ 5. 26832	- 3. 32450	— 5 . 990 72	+ 3.73716	
	7— 9	— 1. 883	+ 1.034	0.014	+0.005	— 1.897	+ 1.039	+ 2.145	— 1. 165	
—ı	7— 8	— o. 123	+ 0.581	+0.013	-0.045	- 0.110	+ 0.536	+ 0. 149	— o. 651	
٥	7— 9	+ 0. 34515	0. 70113	+0.00093	+0.00003	+ 0.34608	- 0. 70110	— o. 40059	+ o. 787o8	
1	710	— o. 163	+ 0.247	-0.003	+0.001	— о. 166	+ 0. 248	+ o. 187	— o. 278	
							,		!	

	.rg=	V		Σ		Е	;	(}
ну 	-i'g'+ig	sin.	cos.	sin.	cos.	sin.	cos.	sin.	cos.
ж —I	i' i 7— 9	+ 0.018	+ 0.031	+0.002	// 0, 004	,, + 0.020	// + 0.027	 0. 015	" — 0.038
0	7—10	— 0, 00414	— o. o8o76	÷0.00015	0. 00004	- o. oo399	o. o8o8o	- 0.00327	+ 0.09105
ı	, 7—11	0.001	+ o. o55	+0.001	0,000	0,000	+ 0.055	+ 0.006	0.059
I	7—10	+ 0.002	+ 0.002	, .		+ 0,002	+ 0.002	— 0.002	— 0. 002
0	7—11	- 0,00339	— o. oo688	-0.00014	_o. oooo1	— o. oo353	— o. oo689	+ 0.00285	+ 0.00793
1	7—12	+ 0.002	+ 0.006			+ 0.002	+ 0.006	- 0.002	— o. oo6
0	8 2	- 0,00081	+ 0.00125	+0.00001	+0.00028	— o. ooo8o	+ 0.00153	+ 0.00105	0. 00137
-I	8 2	+ 0.012	+ 0.029	-0.001	0.005	+ 0.011	+ 0.024	— о. от з	— o. o35
0	8— 3	0. 01377	0. 02428	0.00276	-0.00086	— o. o1653	— o. o2514	+ 0.01755	+ 0.02950
I	8 4	+ 0.016	+ 0.002	+0.001	+o. oor	+ 0.017	+ 0.003	— o. o17	— o. oo3
—1	8— 3	— o. 347	+ 0.022	+o. o38	+0.011	— o. 309	+ 0.033	+ 0.405	— o. oo7
0	8 4	+ 0.31115	- 0.01228	+0.01058	o. o146o	+ 0.32173	— o. o2688	— o. 3 6383	— o. oo347
I	8 5	— 0, 092	+ 0.061	0. 003	-0.001	— o. o95	+ 0.060	+ 0.111	— o. o64
-1	8— 4	+ 0.870	— 2. 1 66	0. 146	+0. 201	+ 0.724	- 1.965	— 1. o ₇ 8	+ 2.472
0	8— 5	0. 84496	+ 1.99985	+0.04055	+0.05451	— o. 80441	+ 2.05436	+ 1.04920	— 2. 28587
I	8— 6	+ 0.052	— o. 710	+0.009	−0. 012	+ o. o61	— 0.722	— o. o91	+ 0.819
_I	8 5	+ 6.8oı	+ 6.823	—0. 556	—o. 752	+ 6.245	+ 6.071	- 7.650	7. 924
0	8— 6	<u> </u>	— 6. 52929	—o. 13118	+0.05109	- 6.51932	- 6. 47820	+ 7. 20228	+ 7.59594
1	8 7	+ 2.315	+ 1.662	+0.023	+o. o3o	+ 2.338	+ 1.692	2. 629	— 1.959
— I	8— 6	19. 983	+ 9.035	+1.803	0. 694	18. 180	+ 8. 341	+22.650	10.093
0	8- 7	+19. 160 27	- 8.87404	-0. 01983	0. 11611	+19.14044	— 8. 990 1 5	-21.73985	+ 9.93193
1	8 8	5.693	+ 3. 208	0. 054	+0.024	5.747	+ 3.232	+ 6.480	— 3. 601
-1	8— 7	2.700	-19.744	+0.252	+1.574	- 2.448	-18. 170	+ 3.093	+ 22. 074
0	8— 8	+ 3.40236	+18.95337	-0. 01 <i>2</i> 87	—o. о1628	+ 3.38949	+18.93709	- 3. 89187	-21. 20181
1	8— 9	— 1. 123	— 5 . 738	-0.010	—о. 039	— 1. 133	- 5.777	+ 1.289	+ 6.431
-1	8 8	3. 127	— 2. 554	+0. 231	+0. 200	— 2. 896	2. 354	+ 3.476	+ 2.871
0	8 9	+ 3.23043	+ 3. 25042	0.00182	+0.00243	+ 3. 22861	+ 3. 25285	<u> </u>	3. 65134
1	810	- 1.053	— 1 . 169	0.004	—o, ооб	— 1. o57	<u> </u>	+ 1.174	+ 1.314
-1	8— 9	— o. 494	— o. oo7	+0.035	+0.003	— o. 459	— o. oo4	+ 0.549	+ 0.015
. 0	8— 1 0	+ 0.62087	+ 0. 14754	+0.00006	+0.00058	+ 0.62093	+ 0. 14812	0.69044	0. 17265
1	11—8	0. 228	— o. o83	-0.001	0.002	— O. 229	0. 085	+ 0.253	+ 0.095
_I	8—10	— o. o41	+ 0.030	+0.003	-0.001	— o. o38	+ 0. 029	+ 0.046	— o. o32
٥	8—11	+ 0.06913	0. 01641	+0.00006	+0.00007	+ 0.06919	— o. o1634	o. o7708	+ 0.01704
1	8—12	— o. o31	— o. oo3	+0,002	0,000	— o. o29	- 0.003	+ 0.034	+ 0.003
—ı	811	0,000	+ 0.001			0.000	+ 0,001	0.000	— o. oo1
0	8—12	+ 0.00508	- 0.00312	0.00000	+0.00001	+ 0.00508	- 0.00312	— o. oo577	+ 0,00369
1	9 2	+ 0.002	+ 0.001			+ 0.002	+ 0,001	0.002	- o. ooi
0	9- 3	— 0. 00332	- 0.00169	-0. 00042	+0.00008	- o. oo374	— o. oo161	+ 0.00371	+ 0,00220
1	9 4	+ 0.004	0, 000			+ 0.004	0.000	0, 004	0,000
—I	9 3	0. 047	+ 0.031	+0.006	-0.001	- o. o41	+ 0.030	+ 0.055	o. o33
٥	9 4	+ 0.03943	 0. 02830	+0.00037	-0. 00324	+ 0.03980	- 0. 03154	0.04714	+ 0.03019
1	9— 5	- 0,002	+ 0.020	0,000	0.001	— 0. 002	+ 0.019	+ 0.004	0, 022
—I	9— 4	— 0. 092	— o. 442	-0, 004	+0.045	— o. o96	- o. 397	+ 0.087	+ o. 5 09
0	9- 5	+ 0.07310	+ 0.40730	+0.01493	+0.00684	+ 0.08803	0.41414	— o, o6650	- 0. 47027
T	9— 6	- 0.078	— 0. 117	0,000	-0.003	0.078	— 0, 120	+ 0.084	+ 0. 138 - 0. 662
_r o	9— 5 9— 6	+ 2. 385 - 2. 23738	+ 0.530 - 0.53064	0. 206 0. 03406	0, 095 +0, 03874	+ 2. 179 - 2. 27144	+ 0.435 — 0.49190	- 2.695 + 2.53222	+ 0.66261
Ľ.	, ,	2.23/30	5, 55004	3, 03400	, 5, 530/4	2. 2/144	5, 49190	33222	' 3.33201
			-						

A	rg=	V		Σ		E	3	G		
иу-	$-i^7g'+ig$	sin.	cos.	sin.	cos.	sin.	cos.	sin.	cos.	
и	i' i	//	"	//	"	"	"	// v. 849	,,	
1	9- 7	+ 0.744	- 0.027	+0.010	+0.004	+ 0.754	- 0.023		+ 0,007	
	9— 6	— 4.694	+ 6.878	+0.470	—o. 532	- 4.224	+ 6.346	+ 5.380	— 7. 68o	
°	9- 7	+ 4. 52390	- 6. 57520	-0.05051	—o. 07551	+ 4.47339	- 6.65071	5. 18999	+ 7.35127	
I	9 8	— I. II2	+ 2. 276	-0.014	+0.018	- 1.126	+ 2.294	+ 1.291	— 2. 553	
ı	9-7	— 9. 439	—12.881	+0.688	+1.039	— 8. 751	—11.842	+10.476	+14.414	
°	9— 8	+ 9.29110	+12.33229	+0.05939	-0.02619	+ 9.35049	+12. 30610	—10. 32496 	—13. 80967	
I	9— 9	— 3. 165	- 3. 639	0, 020	-0.027	— 3. 185	- 3.666	+ 3.523	+ 4.085	
I	9— 8	+11.377	— 4· 479	—о. 805	+0.342	+10.572	— 4. I37	—12. 566	+ 4.999	
0	9— 9	—10. 77926	+ 4.88540	+0.00831	—o. 01058	10. 77095	+ 4.87482	+11.90855	— 5·45723	
I	9—10	+ 3.256	- 1.561	+0.016	0, 009	+ 3.272	1.570	3. 602	+ 1.748	
—I	9 9	+ 1, 340	2. 566	o. o95	+0.172	+ 1.245	— 2. 394	— I. 49I	+ 2.828	
0	9—10	- 1,73410	+ 2.73406	-0.00139	-0.00115	- I. 73549	+ 2.73291	+ 1.92700	— 3. 01675	
I	9—11	+ 0.628	— o. 908	+0.003	-0, 003	+ 0.631	0.911	0.698	+ 1.003	
1-1	9—10	— o. o64	— o. 384	+0.003	+0.025	— o, o61	— o. 359	+ 0.066	+ 0.424	
٥	9—11	— 0. 00942	+ 0.49580	0. 00032	+o. 00008	0.00974	+ 0.49588	+ 0.01515	- 0. 54704	
I	9—12	+ 0.020	— о. 188	0,000	0.000	+ 0.020	- o. 188	- 0.024	+ 0. 207	
—I	9—11	0, 026	— o. o32	+0.002	+0.002	— o. o24	- 0.030	+ 0.028	+ 0.035	
0	9—12	+ 0.02472	+ 0.05371	-0.00002	+0.00005	+ 0.02470	+ 0.05376	- 0.02646	- 0. 05914	
1	913	— o. oo6	— 0. 024	0.000	0,000	о. ооб	— 0. O24	+ 0.006	+ 0.026	
0	10- 3	— o. ooo47	+ 0.00003	-0. 00005	+0.00004	- 0.00052	+ 0.00007	+ 0.00054	0, 00000	
-1	10-3	— 0, 002	+ 0.010			0, 002	+ 0.010	+ 0.003	- 0.011	
0	10 4	+ 0.00266	- 0. 00662	0.00019	0. 00047	+ 0.00247	0.00709	- 0. 00342	+ 0.00737	
I	10— 5	0,000	0.000			0, 000	0, 000	0.000	0.000	
-1	10-4	— o. o53	- o. o56	+0.002	+u. 006	— o. o51	— o. o50	+ 0.058	+ 0.066	
0	10- 5	+ 0.04837	+ 0.05150	+0.00330	-0. 00027	+ 0.05167	+ 0.05123	— 0. 0 <u>525</u> 1	— о. обо8о	
r	10— 6	— o. o25	— o. oo6	0.000	0.000	— o. o25	- o. oo6	+ 0.028	+ 0.008	
—1	10 5	+ 0.484	— о. 178	— о. 0 46	+0.004	+ 0.438	0. 174	— o. 552	+ o. 186	
0	10— 6	— o. 45740	+ 0. 15826	-0.00316	+0.01357	— o. 46o56	+ 0. 17183	+ 0.52214	- o. 16399	
1	ro 7	+ 0.129	- o. 105	+0.002	0.000	+ 0.131	- o. 105	0. 149	+ 0.113	
—I	10— 6	o. o95	+ 2. 334	+0.044	—0. 187	- 0.051	+ 2. 147	+ 0, 154	2.614	
0	10- 7	+ 0. 12263	2. 22550	0. 03264	—о. 01831	+ 0.08999	<u> </u>	— o. 18224	+ 2. 49493	
I	ro 8	+ 0.114	+ 0.719	-0, 002	+0.007	+ 0.112	+ 0.726	— 0. 112	— o. 810	
—ı	10- 7	— 6. 23 6	2. 68 1	+0.448	+0.254	— 5. 788	- 2.427	+ 6.909	+ 3.048	
0		+ 6.01140	+ 2.57700	+0.03940	-0. 04143	+ 6.05080	+ 2.53557	- 6. 66624	- 2. 93199	
1	10- 9	_ 2.012	- o. 562	-0.014	-o. oo6	- 2.026	- o. 568	+ 2.236	+ 0.651	
—t	10-8	+ 7.428	- 8. 374	o. 543	+0.564	+ 6.885	— 7. 81o	— 8. 22 6	+ 9. 222	
0	10 9	— 7. o67	+ 8. 243	+0.02192	+0.02769	- 7.045	+ 8.271	+ 7.829	9. 086	
1	10-10	+ 2.057	- 2. 723	+0.012	-0.014	+ 2.069	_ 2.737	- 2. 282	+ 3,005	
—ı	10- 9	+ 4. 264	+ 5.929	-0. 289	—o. 375	+ 3.975	+ 5.554	— 4. 699	- 6.481	
0	10—10	- 4· 479	— 5· 497	+0.00774	+0.00358	- 4. 47 I	- 5.493	+ 4. 939	+ 6.008	
1	10-11	+ 1.420	+ 1.652	+0.007	+0.007	+ 1.427	+ 1.659	— 1. 5 68	- 1.807	
-1	10—10	+ 1.922	+ o. 528	—о. 118	0. 035	+ 1.804	+ 0.493	- 2. 103	— o. 584	
	10—11	- 2. 084	- o. 736	+0.00074	-o. ooo85	- 2.083	- 0. 737	+ 2. 282	+ 0.811	
1	1012	+ 0.703	+ 0. 280	+0.002	+0.001	+ 0.705	+ 0. 281	0. 770	- 0. 308	
	10—11	+ 0.703	- 0.113	-0. 017	+0.005	+ 0.259	— o. 108	- o. 303	+ 0.120	
0	10-12	— 0. 36150	+ 0.07393	-0.00021	-0.00009	- 0. 36171	+ 0.07384	+ 0. 39615	- 0.120 - 0.07774	
1	10—12	+ 0. 139	- 0.010	-0.001	-0.001	+ 0, 138	- 0.011	— 0. 39013 — 0. 152	+ 0.010	
<u></u>		1 0. 139	0.010			1 234		5.152	1. 0.010	

Arg=	V		Σ	Σ	В		G	1
$ \mu\gamma + i^{\gamma}g' + ig $	sin.	cos.	sin.	cos.	sin.	cos.	sin.	cos.
и 1 i о 11 — 4	0.00000	+0.00097	ıı .	11	0,00000	., +0. 00097	// +0.00004	0, 00110
-I II - 4	—о. 017	-0.004	+0.001	0,000	-0.016	-0.004	+0.018	+0.005
0 11— 5	+0.01059	+0.00241	+0.00049	0. 00033	+0.01108	+0.00208	-0.01184	—o. 00362
1 11—6	+0.001	+0.002	-0.001	0.000	0.000	+0.002	0, 000	0. 002
—ı II— 5	+0.057	-o.o78	-0.007	+0.005	+0.050	-o. o73	—o. o67	+o. o85
o 11— 6	—o. 05602	+0.07047	+0.00084	+0.00298	0. 05518	+0.07345	+0.06550	<u> </u>
1 11-7	+0.008	—0. 030	0,000	-0.001	+0.008	0.031	-0.010	+0.033
_1 II— 6	+o. 266	+0.472	0.012	0.042	+0. 254	+0.430	o. 285	—o. 533
0 11-7	o. 2459	-0.4521	0.01122	0, 00026	0. 2571	-0.4524	+0.2631	+0.5110
ı 11— 8	+0. 124	+o. I22	+0.001	+0.001	+0. 125	+o. 123	—о. 135	<u> </u>
—I II— 7	2. 076	+0.286	+o. 153	+0.004	—I. 923	+0.290	+2.306	o. 285
0 11—8	+1.998	-o. 2633	+0.00774	— 0.02506	+2.006	-o. 2884 ·	-2.221	+0. 2606
1 11—9	-o. 628	+0.214	-0.004	+0.001	—0. 632	+0.215	+0.700	<u> </u>
1 11 8	+1.081	—5. 217	-o. 108	+0.344	+0.973	-4. 87 I	I. 233	+5.732
0 11-9	—1.027	+5.007	- -0. 03033	+0.01796	— 0. 997	+5.025	+1.173	-5.510
1 11-10	+0. 142	—1. <u>5</u> 87	+0.002	0.008	+0, 144	-1.595	0. 171	+1.754
—ı 11 — 9	+6.645	+1.343	-0.412	o. 248	+6. 233	+1.095	7. 264	—1. 710
0 11—10	 6. 534	-3.462	-0.01132	+0.01530	— 6. 545	-3.447	+ 7. 147	+3.802
1 1111	+2.123	+3.331	+0.010	+0.005	+2.133	+3.336	-2. 324	-3.428
—I II—IO	-2.714	+3. 243	+o. 154	-0. 202	—2. 5 60	+3.041	+2.938	—3. 546
0 11—11	+2.412	3⋅395	-0.00101	+0.00503	+2.411	3. 390	2, 609	+3.707
I II—I2	—о. 711	+1.153	0.001	+0.005	0.712	+1.158	+o. 769	-1.252
-1 11-11	0.067	+1.303	+0.004	0.074	-o. o63	+1.229	+0.076	—1.416
0 11—12	+o. 1606	—1.430	+0.00019	-0.00052	+o. 1608	-1.43I	0. 1760	+1.555
1 11-13	-0. 070	+0.497	0,000	+0.002	0.070	+0.499	+0.076	—o. 541
—I I2— 5	_0.001	-0.013	0,000	+0.002	-0.001	o. oi i	0,000	-\ 0.015
o 12— 6	-0.00115	+0.01502	+0.00044	+0.00044	0.00071	+0.01546	+0.00207	—о. 01669
I 12 7	0.003	-o. oo6	0,000	0.000	-0.003	-o. oo6	+0.003	+0.007
<u> </u>	+0. 107	+0.052	-o. oo6	-o. oo6	+0. 101	+0.046	o. 116	o. o61
0 12— 7	<u>_0, 09298</u>	0, 05255	0, 00244	+0.00129	-0. 09542	-0.05126	+0. 10147	+0.06083
1 12— 8	+0.033	+0.005	0,000	0.000	+ o . 033	+0.005	o. o37	0.007
—ı 12 — 7	-0.424	+0.361	+0.034	-0.019	0. 390	+0.342	+0.474	0. 389
о 12— 8	+0.4020	-o. 3307	0.00166	-0.00862	+0.4003	о. 3393	—0. 4502	+0.3563
I I2 9	o. o95	+0.133	0.002	+0.001	-0.097	+0.134	+0. 109	o. 145
<u> </u>	-0.632	-1.759	+0.023	+0.119	0. 609	—r. 640	+o.669	+1.935
0 12 9	+0. 5847	+1.676	+0.01815	+0.00133	+ 0.6028	+1.689	—о. 6185	—1. 84 5
I I2I0	—o. 263	-0.482	-0.003	0, 004	0. 266	—о. 486	+o. 281	+0.534
—I I2— 9	+4. 171	-o. o89	— 0. 249	0.019	+3.922	—о. 108	4. 540	+0.064
0 12—10	−3.974	+0.081	0. 00626	+0.02100	3.980	+0. 102	+4. 330	-o. o58
I 12—11	+1. 190	-o. 126	+0.009	-o. oo3	+1.199	—o. 1 29	—I. 30I	+0. 128
—I I2—I0	—I. 357	+5.235	+0.090	o. 285	1. 267	+4.950	+1.485	5.656
0 12—11	+1.218	-4. 984	0.01046	— 0, 00288	+1.208	-4. 987	—I. 332	+5.391
I Į2—12	0. 314	+1.444	-0.001	+0.014	—0. 315	+1.458	+0.344	— 1. 567
—I I2—II	-2. 673	0. 881	+o. I34	+0.042	2. 539	—о. 839	+2.872	+0.940
0 12—12	+2.587	+0.664	+0.00034	—0. 00093	+2.587	+o. 663	—2. 782	—o. 7o6
1 12—13	— 0. 742	—о. 166	0.008	0,000	0. 750	о. 166	+o. 801	+0. 176
	<u></u>]	L	1				

In order to get the value of C we need that of \overline{T} . This can be got by making γ equal to g in the expression for T, taking care to derive the terms involving $\pm 2\gamma$, $\pm 3\gamma$, etc., by means of the process noted at page 74, or more readily by the equation

$$\bar{\mathbf{T}} = \frac{\mathbf{I}}{n} \frac{d}{dt} \left(\frac{d\delta z}{dt} + 2\nu \right)$$

For Jupiter we have the following expression:

A '/-/ \	ī		A :/-/ i	Ę	Ť
Arg=i'g'+ig	sin.	cos.	Arg=i'g'+ig	sin.	cos.
i' i	"		i' i 5— I	// o, ooo8	// o. oo85
o 1	+ 0.0380	+0. 1732	5— 2	+0.0747	+0. 0569
0— 2	— o. o148	-0.0094	5 3	—о. 6815	+0. 2266
o— 3	+ 0.0005	-0.0010	5— 4	+0.4213	—2. 7627
1+ 3	0.0003	0.0014	5 5	+3.6051	+2.0622
1+ 2	+ 0.0019	-0.0017	5— 6	+0.5123	0.0737
1+ 1	+ 0.0011	+0. 0281	5— 7	+0.0349	—o. o284
1 0	- o. o66o	o. 3208	5— 8	+0.0018	0. 0036
I— I	+ 0.4711	+2.4190	6— 1	-0.0007	0.0004
I— 2	+ 0. 2573	-o. 2053	6— 2	+0.0127	+0.0002
1— 3	+ 0.0197	0.0221	6— 3	0, 0702	+0.0997
1-4	+ 0.0014	0, 0004	6— 4	0. 2997	o. 6185
	+ 0.0020	+0.0034	6— 5	+2.0516	0. 0729
2+ I 2 O	- 0. 1181	—0. 0140	6— 6	—о. 6981	+2.3083
2	+ 2. 3998	—0. 5665	6 7	+o. 1288	+0. 3483
2— 1 2— 2	— 15. o620	-6. 4637	6— 8	+0.0296	+0.0223
2- 2	0. 3040	+o. 6788	6— 9	+0.0033	+0.0013
2- 3	+ 0.0073	+ o . o 396	7— 2	+0.0012	—o. 0007
2— 5	+ 0.0004	+0.0017	7— 3	+0.0001	+0.0183
			7— 4	—o. 1169	-o. o658
3+ 1	+ 0.0004	+0.0002	7— 5	- -0. 4829	o. 3396
3 0	- 0.0215	+0.0077	7— 6	+o. 3286	+1. 3851
3 I	+ 0. 3784	-0. 3219	7— 7	—1. 3668	0. 0836
3— 2	- 1.6395	+3.4109	7— 8	0. 2099	+0.1347
3— 3	- 6.4194	9. 0498	7— 9	-0.0111	+0.0253
3— 4 3— 5	0. 7658 0. 0466	-0. 1943 +0. 0133	710	0. 0022	+0.0029
3— 3 3— 6	- 0.0019	+0.0133	8 2	0.0000	-0,0004
			8- 3	+0.0012	+0.0020
4 0	- 0.0024	+0.0019	8 4	0.0228	+0.0026
4 I	+ 0.0272	-0.0643	8— 5	+0.0484	—0, 1220
4— 2	+ 0. 1581	+0.6183	8 6	+0. 3348	+0. 3331
4— 3	- 3. 3166	—I. 0972	8— 7	-0.8581	+0.4017
4 4	+ 4.6773	5. 1280	8 8	—o. 1352	—0. 7512
4-5	+ 0.0386	o. 6765	8— 9	-0.1156	-0.1161
4— 6	- 0.0233	-0.0439	8—10	-0. 0201	0,0041
4 7	— o. oo16	0.0016	8—11	-0.0016	+0.0016
5 0	— O. 0002	+0.0004			

Ang-ilal Lia	Ē	Ī.	Ana—i/a/ Lia	7	ī
Arg=i'g'+ig	sin.	cos.	Arg=i'g'+ig	81n	cos.
6' 6 9-3 9-4 9-5 9-6 9-7 9-8 9-9 9-10 9-11 9-12 10-4 10-5 10-6 10-7 10-8 10-9 10-10	" +0.0004 -0.0029 -0.0052 +0.1152 -0.1995 -0.3698 +0.3812 +0.0555 -0.0007 -0.0008 -0.0001 -0.0028 +0.0231 -0.0042 -0.2384 +0.2481 +0.1428	+0.0001 +0.0001 +0.0021 -0.0249 +0.0254 +0.2957 -0.4862 -0.1737 -0.0880 -0.0147 -0.0017 +0.0005 -0.0031 -0.0087 +0.0996 -0.1005 -0.2919 +0.1774	i' i 10—12 11— 5 11— 6 11— 7 11— 8 11— 9 11—10 11—11 11—12 12— 6 12— 7 12— 8 12— 9 12—10 12—11 12—12	+0.0104 -0.0008 +0.0030 +0.0111 -0.0786 +0.0347 +0.2095 -0.0703 -0.0045 +0.0002 +0.0043 -0.0158 -0.0200 +0.1224 -0.0345 -0.0652	" -0.0024 0.0000 -0.0035 +0.0206 +0.0111 -0.1764 +0.1142 +0.0986 +0.0386 -0.0008 +0.0020 +0.0130 -0.0567 -0.0016 +0.1382 -0.0172
1011	+0.0614	+0.0209			

The four factors C, D, E, and H for Jupiter have then the expressions

	1 2/ -/ 1 2	(C	I) ;	E		Е	
Arg=n	γ +i ′g′+ig	sin.	cos.	cos.	sin.	sin.	cos.	cos.	sin.
ж	i' i	"	+o. o736	//	"	"	o. III	11	· "
r	o 1	0,002	-0.082	+0.02	— о. 11	0.04	+0.21	0. 02	+0.14
-1	0 0	+0.074	+0.340	— 1.40	 3. 19	+o. 50	—1.13	+1.18	+2.73
	0 1	0. 1488	—0. 6692	+0.750	+1.694	<u>-0.720</u>	+1.694	— 0. 547	—1. 273
I	0 2	+0.076	+ 0. 336	+o. 41	+0.93	+o. 50	—1.13	0.45	<u>—</u> I. 02
-r	о— 1	0. 028	0. 020	0. 32	+o. 24	+0.04	+o. 10	+0.43	0. 37
o	0 2	+0. 0534	+o. o138	+0.212	<u>—</u> 0. 101	—0. 1 06	0.051	— 0. 304	+0. 225
I	0- 3	0. 026	0,000	+0,06	0, 04	+0.08	+ 0.02	0.05	+0.03
—т	0 2	0.000	0. 002	+0.01	+o. o1			0. 04	0.04
0	0- 3	0. 0012	+0.0044	-0.007	o. o13	+0.002	0,004	+0.014	+o. o25
I	0 4	-0.002	—o. oo4						
0	ı+ 3	-0. 0004	0.0022	0.002	+0.001				
I	I+ 2	0.000	0, 000						
-1	1+3	+0, 004	-0,002			0.00	+0.01	-0. 02	0,00
0	1+ 2	0, 0048	+0.0016	+0.015	+0.022	+0. ∞8	-0, 011	-0.022	0. 040
1	1+ 1	+0.004	-0.002	-0.02	 ∪. 04	+o. o1	+0.02	+o. o3	+0.07
1	I+ 2	-0.002	+o. o38	+o. 16	0. 15	-0. I 2	o. II	0. 19	+0. 17
0	1+1	+0,0014	0. 0810	+o. 188	<u></u> 0. 153	+o. 188	+0. 153	0. 230	+0. 133
1	1 0	+0.002	+0.056	-0, 42	+o. 35	о. 18	0.07	+0.49	o. 35
—r	r+ 1	o. o84	0.410	—1.63	—I. I7	+o. 76	o. 51	+1.82	+1.30

Ann	C		D		Е		Н	
$Arg = n\gamma + i'g' + ig$	sin.	cos.	cos.	sin.	sin.	cos.	cos.	sin.
κ i' i Ο Ι Ο	// + 0. 1942	" + 0.9314	0.000	0.000	 — I. II 9		,, 0, 000	0.000
1 I— I	— 0. 130	o. 638	+1.63	+1.17	+0.76	—o. 51	—1.82	—1. 30
—ı ı o	+ 0.964	+ 4.812	+0.32	— о. 35	0. 16	-0.09	-o. 45	+o. 32
0 I— I	<u> </u>	— 9. 5 996	—о. 183	+0. 178	+0. 183	+o. 178	+0. 299	—0. 147
I I— 2	+ 0.936	+ 4.802	0.00	+0.09	0. 16	0. 14	-0.07	0. 10
—ı ı— ı	+ 0.518	— o. 410	—3. 38	+0.72	+0.80	+o. 18	+4.65	— 0. 99
O I 2	<u> </u>	+ 0.4758	+2.379	—o. 513	—1. 184	—0. 256	—3. 63o	+0.789
1 I-3	+ o. 558	— 0. 176	+0.21	0.04	+0.79	+o. 17	+0. 20	-o. o7
—I I— 2	+ 0.038	0.044	+0,06	+0.23	0. 04	+0.03	O. I2	o. 33
o I— 3	— 0. 1196	+ 0. 1018	+0.039	—о. 167	-0. OI 2	o. o56	-0. 047	+o. 271
I I— 4	+ 0.066	0.052	0.04	о. оз	+0.02	+0.04	+o, o6	o. oı
_I I— 3	+ 0.006	+ 0.002	0.00	-o. oi			-0.02	+0.01
o I— 4	0.0100	+ 0.0070	—0 . 005	-0,001	+0.001	0,000	+0,009	+0.001
ı ı— 5	+ 0.006	— o. oo4					0, 00	0.00
—I 2+ 2	0,000	+ 0.006	+0.03	0.00	0.02	0.00	0, 04	+0.01
0 z+ I	— 0.0012	0.0102	+0.029	— 0. 006	+0.029	+0.006	-0, 040	+0.002
I 2 0	+ 0.004	+ 0.008	0. 07	0,00	0.02	+0.01	+0. 10	-0.01
I 2+ I	— o. o86	0.048	-0. 20	o. 44	+0.06	—0. 19	+0.26	+0.50
0 2 0	+ 0.2336	+ 0.0914	0, 000	0,000	o. o81	+o. 30 1	0,000	0,000
I 2— I	— o. 238	— o. o28	+0. 24	+ 0.40	0.00	—o. 25	-0. 28	—o. 48
I 2 O	+ 3.344	— o. 506	2.44	+2.32	+o. 88	+o. 83	+1.85	—1.78
0 2— I	7.4004	+ 1.3272	+1.316	—I. 23I	—ı. 316	—I. 23I	o. 828	+0.823
I 2— 2	+ 4.784	— 1.130	+o. 71	о, 65	+0.87	+0.83	— 0. 77	+0.68
I 2 I	—30. 116	+12.978	—o. 64	—о. 51	+0.11	—о. 15	+0.83	+0.66
0 2— 2	+59.9446	-25. 8674	+0.47 6	+0.333	—0. 238	+o. 166	—o. 637	—о. 487
I 2— 3	29. 858	+12.860	+0,04	-0.04	+0. 17	—о. 13	+0.01	+0. 12
—I 2— 2	— o. 6o8	+ 1.358	+0.01	+2.88	0. 01	+0.51	0. 03	-4. 27
o 2— 3	+ 3.3796	— 3. 6526	-0.007	-2. 248	+0.002	o. 749	+0.017	+3.622
1 2— 4	2.046	+ 1.978	0.00	+0.13	0.00	+0.50	0,00	0. 58
— 1 2— 3	+ 0.014	+ 0.078	+0.11	+0.05	0.01	—o, oī	o. 18	—o. o6
0 2—4	+ 0.1200	— o. 3008	-o. o74	—0. I 24	+0.019	0, 031	+o. 126	+o. 195
1 2— 5	— o. o94	+ 0. 178	-0.01	+0.04	-o. or	+0.03	0.00	—o. o8
—I 2— 4	0.000	+ 0.006			Į			
0 2— 5	+ 0.0030	0.0224	0,000	-0.003			+0.001	+0.004
ı 2— 6	- 0,006	+ 0.012			1			
—I 3+ 2	0,000	+ 0.002					-o. oI	-0.01
0 3+ 1	0,0004	- 0.0014	+0.003	+0.001	+0.003	-0.001	—o. oo5	-0.002
1 3 0	+ 0.002	0.000	١.		1		+0.01	+0.01
—i 3+ i	- 0.018	0,006	+0.01	-0.09	-0.01	-0.03	-0. OI	+0.11
0 3 0	+ 0.0436	- 0.0046	0,000	0,000	+0.013	+0.049	0,000	0.000
1 3— 1	0.042	4 0.016	+0.01	+0.09	-0.03	-0.03	0.00	-0. 11
—I 3 O	+ 0.564	0. 360	-0.89	+0.23	+0.28	+0.09	+0.80	-0.23
o 3— I	— I. 2302	+ 0.8582	+0.432	-0.114	0. 432	-0.114	0. 342	+0.098
I 3— 2	+ 0.752	0.644	+0.27	—0. 13 —2. 76	+0.30	+0.04	0. 32	+o. 13 —1. 83
—I 3— I	— 3. 896 — 7. 4304	+ 5.948	+1.70	+2.76	-0. 42	+0.65	—I. 17 —0. 728	1
o 3 2	+ 7.4394	—12. 2874	—I. 185	—I. 95I	+0.592	—0. 976	+0.738	+1.140

	(Ι)	F	ı	F	I
$\mathbf{Arg} = \kappa \gamma + i'g' + ig$	sin.	cos.	cos.	sin.	sin.	cos.	cos.	sin.
и i ' i	11	11	11	11	//	"	"	11
I 3— 3	— 3. 2 38	+ 6.782	o. o8	—0. 19	-0. 4I	+0.64	+0.16	+0.33
—I 3— 2	12. 898	—18.096	0. 69	+0.73	+0.13	+o. 10	+0.90	—1.00
o 3— 3	+26. 0246	+35.7348	+0, 492	—о. 636	—0. 164	-0, 212	o. 725	+o. 847
1 3— 4	12. 980	—17.752	—o. o7	+0.05	+0.13	+o. 15	+o. 18	—o. o8
—ı 3— 3	 1. 5 38	— o. 388	+z. I2	+0.43	0. 30	+0.05	-3. 3I	о. 66
0 3-4	+ 4.0086	+ 2.0598	-1.748	о. 379	+0.437	0. 095	+2.903	+o. 618
I 3— 5	— 2. <u>15</u> 6	1.240	+0.23	+0.04	0. 29	+0.06	-o. 58	0.14
—I 3— 4	- 0.096	+ 0.028	+0.09	0, 00	0,00	u. 00	о. 13	+0.03
0 3-5	+ 0.3478	+ 0.0278	-0. 141	-0. OI2	+0.028	0002	+0. 232	+0.017
ı 3— 6	0. 202	— o. o38	+0.03	+0.02	-0.02	0.00	0. 07	o. o3
—r 3— 5	0.002	+ 0.004	- O, OI	0.00			0.00	0.00
o 3— 6	+ 0.0258	0. 0048	-0.007	0, 004			+0.011	+0.006
I 3— 7	— o. o14	0.000					0. 01	0.00
—ı 4+ ı	0.004	0.000					0.00	+0.01
0 4 0	+ 0.0052	— 0.0032	0,000	0.000	+0.005	+0.006	0. 000	0.000
t 4— I	— o. oo4	+ 0.006					0.00	o. oi
— I 4 0	+ 0.056	— o. o76	о. 17	o. o3	+0.05	o. oi	+0. 18	+0.05
0 4 1	— 0. 1076	+ 0.1782	+0.075	+0.019	—о. 075	+0.019	—o. o69	<u> </u>
I 4 2	+ 0.054	— o. 128	+0.07	0, 01	+0.05	-0.03	—o. o8	-o. oı
—ı 4— ı	+ 0.020	+ 1.100	+0.07	+1.13	— 0. 02	+0. 26	—o. o8	o. 90
0 4— 2	— 0. 1892	2. 2696	0, 044	—0. 767	+0, 022	0. 384	+0.04300	+o. 55060
I 4 3	+ 0.320	+ 1.230	0. 07	0. 09	+0.02	+0.27	+0.05	+0. I4
—ı 4— 2	 6. 174	2. 688	+2.44	o. 87	-0.43	—u. 17	—I. 47	+0.57
0 4 3	+12.5690	+ 5.0446	1.924	+o. 663	+0.641	+0. 221	+1.039	o. 394
I 4— 4	6.612	- 2.132	+0.11	- o. o5	-0.42	- o. 16	+0.11	0.00
─ I 4─ 3	十 9.350	—IO. 3IO	+0.67	+0.78	—o. o7	+o. 11	o. 88	-1.05
0 4—4	—18. 2386	+20.7634	o. 611	—o. 611	+0.153	—о. 153	+0.801	+o. 895
I 4 5	+ 9.026	10. 346	-+0.07	+0.10	-0.11	+0.11	—0. I2	-0.23
—I 4— 4	+ 0.074	- I. 354	+o. 63	-1.40	0. 06	—o. 17	0.98	+ 2. 24
0 4-5	— o. 8048	+ 3.4620	—o. 551	+1.178	+0.110	+0. 236	+0.918	-2.003
1 4 6	+ 0.510	<u> </u>	+0.09	-0. 20	—o. o7	—о. 16	0, 22	+0.46
—I 4— 5	— o. o48	— o. o88	+0,06	—0. 09	-0.01	0.00	0.07	+0.13
0 4—6	+ 0.0574	+ 0.3134	—o. o66	+0.115	+0.011	+0.019	+0.111	-0. 194 - 0. 07
I 4 7	- 0.022	0. 180	+0.02	-0.03	0.01	-0.01	0, 04 0, 01	+0.07 0.00
—ı 4— 6	0,004	— 0.006	+0.01	0,00				-0, 010
0 4-7	+ 0.0134	+ 0.0234	—o. oo8	+0.006			+0.013 -0.01	+0.01
I 4— 8	— o. oo6	- 0.014				·	_0.01	70.01
050	+ 0,0004	0.0004	0.000	0,000			0.000	0.000
—ı 5 o	+ 0.002	— O. OI 2	—0. 02	-0. 02	+0.01	-o. oı	+0.03	+0.03
о 5— 1	— 0, 002 6	+ 0.0239	+0.008	+0.008	0. 008	+0.008	—o. oog	-o. oo8
I 5— 2	0. 004	— o. o18	0.00	0.00	+0.01	-0.01	_o. o1	o. oi
—ı 5— ı	+ 0.086	+ o. 124	-0. 12	+0.23	+0.02	+0.05	+0.11	O. 2I
0 5— 2	0. 2042	- o. 2405	+0.070	—0. 147	-o. o35	—0, 074	o. o54	+0. 121
r 5 3	+ 0.148	+ 0.114	-o. oī	-0, 04	+0.03	+0.05	0.01	+0.05
—ı 5— 2	— I. 302	+ 0. 196	+1.16	+o. 18	0. 19	+0.03	— 0. 84	-0. 11
0 5— 3	+ 2.6286	0.5290	0. 872	0. 130	+0. 29I	-0.043	+0.584	+0.074

A	C		Γ)	1	E	I	H
$Arg = \varkappa \gamma + i'g' + ig$	sin.	cos.	cos.	sin.	sin.	cos.	cos.	sin.
\varkappa i' i	"	,,	11	"	"	"	"	"
ī 5— 4	— 1. 354	+ 0.460	+0.01	+0.05	—o. 19	+0.05	+o. o6	 ∪. 01
—I 5— 3	+ 1.190	- 5. 320	0. 23	—1. 8 ₄	+0.04	—0. 26	∔0. 16	+1.00
0 5—4	<u> </u>	+10.7212	+o. 168	+1.533	-0. 042	+o. 383	0. 100	—o. 747
I 5— 5	+ 0.776	 5 . 496	-0.04	— 0. 19	+0.04	—0. 26	+0.03	-0.02
— I 5— 4	+ 7.256	+ 4. 114	+o. 76	—o. 48	-0.09	-0.04	—1. o6	+o. 63
0 5— 5	—14. 5522	— 7. 8410	0. 650	+ 0. 467	+0. 130	+0.093	+0.940	0. 596
ı 5— 6	+ 7.238	+ 3.858	+0.13	—o. o7	0.09	o. o6	0. 23	+0.12
—I 5— 5	+ 1.030	— o. 152	о. 83	о. 60	+0.09	0. об	+1.35	+0.99
0 5 6	2. 5884	+ 0. 0268	+ 0. 698	+o. 553	—о. 116	+0.092	-1.214	0. 935
I 5— 7	+ 1.376	+ 0. 034	0. 13	0. 12	+0.08	0. 06	+0. 29	+0, 22
—1 5— 6	+ 0.068	— o. o58	— 0. 06	—o. o8	+o. o1	-0,01	+0.09	+0.11
0 5-7	— o. 2384	+ 0.1118	+0.074	+o. o87	0. 011	+0.012	—0. 127	—0. 149
ı 5— 8	+ o. 136	— o. o54	-0.02	-0.02	+0.01	-o. o1	+0.05	+0,06
—ı 5— 7	+ o. oo6	— o. oo4					0.01	0.00
o 5— 8	0.0156	+ 0.0146	+0.003	+0.010			0.006	-0.017
1 5 9	+ 0.010	— o. oo6					0.00	+o. oi
_r 6 o	- 0.002	- 0,002						
о 6— г	+ 0.0006	+ 0.0030						
I 6— 2	- 0.002	— 0. 002						
—ı 6— ı	+ 0.018	+ 0,006	i		+0.01	+0. OI	+0.04	0,02
0 6-2	- 0.0394	— 0, 0102	+0. 023	-o. o16	_0. 01 I	-o. oo8	-0.020	+0.015
r 6-3	+ 0.026	+ 0,002	-0.02	0.00	+o. oī	+o. oı	-0, 02	0,00
—I 6— 2	— o. 162	+ 0. 142	+0. 24	+o. 18	-0.04	+0.03	-0. 20	0. 14
o 6— 3	+ 0. 3088	— o. 3084	-0.179	-0. 135	+0.060	-0.045	+0. 137	+0.098
ı 6— 4	- o. 140	+ 0. 198	-0. OI	+0.02	-0.04	+0.04	+0.02	0, 02
—r 6— 3	— 0. 402	— I. 230	+0.35	—о. 97	0.05	-0.13	-0. 22	+0.65
o 6 4	+ 0.9184	+ 2.4530	0. 291	+0. 781	+0.073	+0. 195	+0. 172	0.495
ı 6— 5	- 0, 606	— 1. 224	+0.05	-0.07	— 0. 06	-0.13	0, 02	+0.01
—ı 6— 4	+ 4.034	+ 0.080	—I. 2I	—0. 12	+o. 14	o. oɪ	+o. 56	+0.06
o 6— 5	— 8. o618	+ 0.0418	+1.048	+0.131	—o. 210	+0.026	-0, 437	-o. o56
ı 6— 6	+ 4.072	— O. 204	— 0. 19	0.02	+o. 14	0. 02	+o. o1	-0. o2
<u>-1</u> 6— 5	— I. 382	+ 4.646	-0. 28	0. 69	+o. o2	-o. o7	+0.37	+0.95
o 6— 6	+ 2.4796	9. 2720	+o. 280	+0.611	0, 047	+0. 102	0. 347	—о. 86 ₇
ı 6— 7	— I. 200	+ 4.598	— о. о5	-0.13	+o. o3	-0.07	+0.05	+0. 23
—ı 6— 6	+ 0.256	+ 0.696	0. 49	+0.42	+0.04	+0.03	+0.83	0. 71
o 6— 7	0. 4288	- I.7272	+0. 460	—о. 358	— о. о66	0.051	—0. 789	+0.64 0
ı 6— 8	+ 0.200	+ 0.918	0. 12	+o. o8	+0.04	+0.03	+0.21	—о. 17
—ı 6— 7	+ 0.058	+ 0.050	— 0. 07	+0.02	+0.01	0.00	+0.13	— 0. 04
o 6— 8	- o. 1282	— 0. 15 96	+0.084	-o. o35	-0.011	-0, 004	0. 145	+0.062
ı 6 9	+ 0.066	+ 0.090	—о. оз	+0.01	+0.01	0.00	+0.05	-0.02
—ı 6— 8	+ 0.004	0.000	-0.01	0.00			0,00	0,00
0 6— 9	— o. o154	— o. oo84	+0.010	0,000			0.016	+0.001
1 6—10	+ 0.006	+ 0.006					+0.01	0,00
—ı 7— ı	0,000	0, 000						
0 7— 2	— o. oo48	+ 0.0022	+0.004	0.000			-0. 0 04	+0.001
ı 7— 3	+ 0.004	— 0.002			l		ĺ ,	,
					<u> </u>			

	C		D		E		Ε	
$Arg = \varkappa \gamma + i'g' + ig$	sin.	cos.	cos.	sin.	sin.	cos.	cos.	sin.
u i' i	11	11	"	"	11	"	11	"
_1 7— 2	o. oo6	+0.030	+0.02	+o. o6	0.00	+0.01	0. 01	0. 05
o 7— 3	+0.0122	0. 0626	-o. o18	0. 041	+0,006	—o. 014	+0.016	+0. 033
1 7— 4	0,000	+o. o36	O. OI	+o. 01	0,00	+0.01	o. oı	+0.01
-ı 7- 3	—о. 186	—о. 156	+0.23	—o. 20	—o. oз	-o. oз	o. 18	+o. 16
0 7-4	+0. 3950	+0. 2994	—о. 187	+o. 165	+0.047	+0.041	+0. 130	0. 120
ı 7— 5	0. 232	—o. 128	+0.03	0.00	0.03	о. оз	o. or	0. 01
-ı 7— 4	+ 0. 988	-o. 548	0.70	-0.43	+0.08	—o. o5	+0.44	+o. 28
0 7— 5	— I. 9558	+1.1676	+0.590	+o. 378	0. 118	+o. 076	0. 351	—o. 223
1 7—6	+0.954	—o. 686	o. o8	o. o8	+0.08	0.05	+0, 02	+0.03
—I 7— 5	+0.524	+2.760	—o. 25	+o. 71	+0.03	+0.07	+0.11	—o. 2 7
0 7-6	— 1. 1840	-5. 4808	+0. 244	-o. 626	0.041	— 0. 1 04	0. 096	+o. 196
I 7-7	+0.700	+2.736	o. o3	+ 0. 14	+0.03	+0.07	0.02	+0.01
—1 7— 6	-2.750	- o. 154	o. 56	+0.11	+0.05	+0.01	+0.78	<u> </u>
0 7 7	+5.4450	+0.1170	+0.508	—о. 128	-0.073	-o. o18	-0. 722	+o. 126
ı 7— 8	2. 698	-0.034	− ∪. I2	+0.04	+0.05	+0.01	+0.19	0.01
—ı 7— 7	-0.426	+0. 272	+0.17	+o. 35	—о. оі	+0.03	—0. 32	—о. 61
0 7—8	+1.0430	-0. 5432	—0. 147	—o. 338	+0.018	-0. 042	+0. 277	+o. 587
x 7— 9	-0. 552	+0. 272	+0.05	+0.10	o. oı	+0.03	_o. o6	—о. 16
<u>—1</u> 7— 8	_o. o26	+0.050	+0.02	+0.09			0, 00	—o. 11
□ 7— 9	+0. 0904	-0, 1212	_o. oo8	o. o68	+0.001	o, oo8	+0.015	+0.119
1 7-10	-0.054	+0.064	-0. OI	0,00	'		-0.01	-0.03
—I 7— 9	-0.002	+0.006	0, 00	+0. or			0.00	0.01
0 7—10	+0.0107	0. 0149	+0.002	_o. oo8			-0.003	+0.014
1 7-11	-o, oo8	+0.008	'		l		0, 00	u, 0I
r 8 2	0.000	+0.002			1			
o 8— 3	-0. 0040	o. oo82	+0.001	0.008	1			
ı 8— 4	+0.004	+0.004	0.00	+o. oi			1	
—ı 8— 3	0. 040	0.008	+0.07	-0.02	0.01	0,00	<u> </u>	+o. o1
0 8-4	+0.0810	+0.0054	-o. o55	+0.012	+0.014	+0.003	+0.042	-0.011
r 8 5	0. 044	+0.004	+0.01	+0.01	-o. oī	0.00	0.00	0.00
—ı 8— 4	+0. 124	-o. 210	—о. 13	— 0. 26	+0.02	0. 03	+o. 10	+o. 18
o 8 5	—o. 2305	+0.4640	+0. 120	+0.211	0.024	+0.042	-0.084	-o. 140
r 8— 6	+0.096	0. 242	o. oI	0. 04	+0.02	—о. оз	+o. o1	+0.01
—ı 8— 5	+o. 586	+o. 698	-0.44	+0.44	+0.04	+0.04	+0. 26	0. 27
o 8— 6	—I. 22IO	— 1 . 3648	+0.392	—о. 379	-o. o65	—o. o63	—0. 2II	+0.217
r 8— 7	+o. 674	+0.654	-0.09	+0.06	+0.04	+0.04	+0.02	-0.02
r 8 6	-1.728	+0.728	+0.38	+0. 24	—o. o3	+0.02	—u. 07	0. 08
o 8— 7	+3.4034	-1.5446	0. 322	-0.239	+0.046	-0. 034	+0, 044	+0.072
ı 8 8	-I. 682	+0.834	+0.06	+0.08	0.03	+0.02	0,00	+0.02
_r 8— 7	—о. 2 82	1.512	+0.01	0. 09	0.00	-0.03	o. oi	0. 59
0 8—8	+0.6828	+2.9618	0.017	+o. 388	+0.002	+0.049	-0.010	+0.541
ı 8 9	-0. 352	-1.468	-0.01	-0.43	0, 00	-0.03	+0.05	0. 13
-ı 8-8	-0. 236	0. 234	+0. 22	0.04	0, 02	0.00	0. 4I	+0.09
o 8— 9	+0. 4964	+0.5744	0. 224	+0.034	+0.025	+0.004	+o. 396	-0.077
1 8—10	-0. 250	0. 302	+o. o8	+0.02	-0.02	0.00	0. II	+0.04
_1 8— 9	-0.040	-0.010	+0.02	+0.01	1		o. 10	0.00
	1				<u> </u>		<u> </u>	

25 AST——15

	C	;	D		E	1	F	H
$Arg = \mathcal{H} \gamma + i'g' + ig$	sin.	cos.	cos.	sin.	sin.	cos.	cos.	sin.
\varkappa i' i	"	11	"	11	,,	1,	"	"
0 8—10	+0.0992	+0.0432	0. 049	o. o o8	+0.005	-o. oo1	+o. o86	+0.012
1 8—11	—o. o52	0. 028					0.00	O. O2
—ı 8—ıo	-0, 004	+0.002					0. 01	0.00
0 8-11	+0.0128	+0.0022	o, oo6	0.003]	- 1
ı 8—12	-0.002	0,000					o. oı	0.00
—I 9— 3	-o. oo4	+0.002						
□ 9— 4	+0.0104	0.0060	0.010	-0.003			+0.009	+0.002
I 9-5	0. 004	+0.002	+0.01	0, 00				
—I 9— 4	+0.002	0. 044	+0.01	— о. 07	0.00	-0.01	0,00	+0.06
0 9—5	+0.0062	+0.0898	+0.001	+0.062	0.000	+0.012	-0.002	0. 045
ı 96	0.012	u. 048	0,00	-o. oı	0.00	10.0—	-0.01	0, 00
—ı 9— 5	+0. 208	0.074	—o. 24	+o. o6	+0.02	+o. 01	+o. 17	-o. o5
n 9—6	-0. 4274	—о. 1358	+0. 205	0. 065	0. 034	-0.011	0. 130	+0.045
1 9-7	+o. 230	+0.048	-o. o5	+0.01	+0.02	10.0+	+0.0I	0.00
r 9 6	-0.432	+0.540	+0. 24	+o. 38	-0. O2	+o. o3	0. 14	—0. 22
D 9—7	+0.8322	—1. 1118	-0.211	—о. 336	+o. o3o	0. 048	+0.111	+0. 173
ı 9—8	о. 386	+0.590	+0.04	+0.07	-0.02	+0.03	-o. oı	-o. o2
—ı 9— 7	0. 698	—о. 988	+0.19	0. 15	-0.02	-o. oı	0. 01	0.00
8 —9 ه	+1.4468	+1.9300	0. 182	+0. 134	+0.023	+0.017	+0.029	+0.030
1 9— 9	—o. 756	-0.946	+0.03	0.04	0. 02	-o. oi	0.01	-o. o3
—ı 9— 8	+'o. 768	—о. 356	+0. 22	_o. o6	-0.02	0.00	0. 39	o. o8
p 9—9	—1. 4796	+0.7750	_o. 273	—o. o45	+0. 030	-0.005	+0. 375	+0.087
I 9—10	+0.724	-0. 392	+0.13	+o. 14	-0.02	0.00	—о, 11	—o. o5
—ı 9— 9	+0.112	0. 180	+0.06	-o. o8	0.00	0. 01	+0.04	+0.24
ō 9—10	—o. 2776	+0. 3871	_o. o17	+o. 135	+0.002	+0.014	+0 , 016	0, 244
1 9—11	+0. 146	-0. t96	_o. o5	o. 10	0.00	-0.01	-0.04	+o. o8
-ı 9-10	+0.002	-0.030	+0.03	-o. oi			o. oı	+0.03
D 9—11	-0.0134	+0.0732	-0.014	+o. o31	+0.001	4-0.003	+0.024	o. o56
I 9—I2	+0.008	-o. o38	0.01	-0.02	,	,	o. o3	+0.04
_I 9—II	0.000	-0.002						
0 9—12	+0.0018	+0.0075	-0.004	+0.004				
ı 9—13	0.000	-0.004		•				
I 10 3	-0.002	+0.002						
o 10— 4	+0.0010	0.0016						
1 10 5	0.000	0, 000						
I 10 4	—o . 006	0.008					0.00	+0.01
0 10-5	+0.0092	+0.0118	0,006	+0.012	+0.001	+0.002		'
1 10— 6	-o. oo6	-0.004	0.00	_0.01	'	,	0,00	+0,01
—I IO— 5	+0.044	_o. oo8	o. o7	_0. O2	+o. o1	0.00	+0.06	+0.01
o 10—6	0. 0896	+0.0212	+o. o6o	+0.011	-0.010	+0.002	0.042	— υ. 007
1 IO 7	+0.044	-0.016	_o. o1	_o. o1	+0,01	0.00	0.00	o. o1
I IO 6	-0.030	+o. 186	+0.01	+0. 20	0.00	+0.02	o. o3	<u></u> 0. 14
o 10— 7	+0.0456	—o. 3762	-o. o17	0. 177	+0.002	-0.025	+0.013	+0. 108
ı 10— 8	-0.008	+0. 196	0,00	+0.04	0.00	+0.02	+0.02	0,00
_I IO 7	— 0. 450	o. 226	+0. 29	_o. 10	-0.02	_o. or	-0.02	+o. 10
n 10 8	+0.9116	+0. 4262	-0.261	+0.090	+0.033	+0.011	+0. 125	-0.042
	<u> </u>	<u> </u>	<u> </u>		. 33	· .		·

Amm-and ideal time	(0	1)]	E	1	H
$Arg = \kappa \gamma + i'g' + ig$	sin.	cos.	cos.	sin.	sin.	cos.	cos.	sin.
n i' i	11	"	"	"		"	11	"
1 10-9	o. 476	-0. 190	+0.05	0.03	0. 02	—о. от	<u> </u>	0. 04
—ı 10— 8	+0.510	о. 568	0. 12	—0. 18	0.00	o. oi	—0. 16	o. o3
0 10-9	—0. 9846	+1.1566	+0.034	+0.116	-0.004	+0.013	+0.052	+0.009
1 10—10	十0.474	0. 592	+0.07	十0.03	0.00	0. 01	+0.11	0.00
—I IO— 9	+0. 292	+0.354	+o. o8	o. 11	0.00	<u> </u>	+o. o1	+ 0. 19
0 10—10	—0. 6190	—o. 6598	—o. o7 I	+0. 17 6	+0.007	+0.018	+0. 114	— 0. 239
1 1011	+0.310	+0. 324	+0.02	0. 13	0.00	0. 01	—o. 18	+0.13
I IOIO	+0.126	+0.042	0.04	+0.02			+o. o6	+0.07
0 1011	0. 2710	-o. 1106	+0.074	+o. 032	0.007	+0.003	—о. 137	o. o48
I IO—12	+o. 138	+0.058	— о. об	o. o5			+0. 12	0. 02
—I 10—II	+0.020	-0.004	0.00	0.00			+0.01	+0.03
0 10—12	` —o. 0488	+0.0026	+0.018	+0.014			o. o33	—0. 025
1 10—13	+0.024	-0.002	0. 02	0, 02			+0.02	+0.01
—I II— 4	0.000	-0.002						
o 11— 5	+0.0020	+0.0012						
1 11— 6	0.004	0,000						i
—I II— 5	+o. oo 6	-0.004					+0.01	0.00
o 11— 6	0. 0114	+0.0122	+0.011	+0.009				
1 11-7	+0.004	o. oo8	—о. от	o, o1			+0.01	0.00
—ı ıı— 6	+0.014	+o. o38	0. 03	o, oı			+0.01	0. 05
0 11 7	—o. o 346	0. 0772	+0.021	+0.052	о. 003	+0.007	0. 014	+o. o3 5
1 11-8	+o. 02 4	+0.038	0.00	u. o <u>5</u>			+0.01	+0.01
—I II— 7	0. 154	+0.006	+0.16	10.0+	-0.0I	0.00	o. oI	+0.02
o 11-8	+0. 3044	—o. o226	—о. 138	—o. o16	+0.017	0. 002	+o. o81	+0.008
1 II— 9	—o. 152	+0.026	+0.02	+0.02	-o. oı	0.00	-0.09	0.04
-ı ıı— 8	+o. o88	-0.342	—0. 12	0. 11	0, 00	0.01	o. o8	+0.07
0 11-9	—o. 1614	+o. 6888	+0.019	+o. 184	0.002	+0.020	0.005	—o. o79
1 11—10	+0.062	—o. 350	+0.09	0.13	0, 00	o. o1	+0.08	+0.03
—I II— 9	+0.414	+0. 238	-0. OI	—o. o8			+o. or	o. oɪ
0 11—10	-0. 8298	0.4210	+0.062	+0.009	o. oo6	+0.001	+0.032	0.047
1 11—11	+0.422	+0.204	o. o 7	+0.07			o. o5	+0.07
—I II—IO	<u> </u>	+0. 202	—0. 05	-0.02			+0.08	+0.12
0 11—11	+0. 2514	-0.4176	+0.104	+0.070	0.009	+o. oo6	—о. 139	0.110
I II—I2	—о. 118	+0. 208	-0.09	—o. o8			+0.10	+0.02
- I IIII	-0.010	+0.078	-0.04	+0.03			0,00	—o. o5
0 11—12	+0.0222	0. 1746	+0.031	-o. o33			—0. 046	+0.071
1 11-13	0.012	+0.092	0.00	+0.01			+0.06	-o. o5
—I I2— 5	+0.002	0. 000						i
о 12— 6	—o. ooo6	+0.0026						
1 12— 7	0.000	-0.002						
— I I2 — 6	+0.006	+0.006		ļ			+o. o1	0.00
o 12— 7	-o. o132	0.0100	+0.011	-o. oog			_	
I 12 8	+0.008	+0.004	—o. or	+0.01			+0.01	0.00
—I I2— 7	0. 032	+o. 018	+0.05	+0.02			0,00	0.01
o 12— 8	+0.0614	-0.0424	0. 043	0. 028	+0.005	-0.004	+0.026	+0.017
1 12-9	0. 032	+0.026	+0.01	+0.02			-0.04	—0. OI
_1 12— 8	-o. o28	—o. 114	-o. or	o. o3	0,00	—o. oi	o. o3	+0.07

Anomara Lifet tim	С		D		E		Н	
$Arg = \varkappa \gamma + i'g' + ig$	sin.	cos.	cos.	sin.	sin.	cos.	cos.	sin.
n i' i 0 12-9 1 12-10 -1 12-9 0 12-10 1 12-11 -1 12-10 0 12-11 1 12-12 -1 12-11 0 12-12	+0. 0639 -0. 042 +0. 240 -0. 4802 +0. 240 -0. 076 +0. 1388 -0. 062 -0. 130 +0. 2610	" +0. 2280 -0. 112 +0. 012 -0. 0074 -0. 010 +0. 272 -0. 5438 +0. 274 -0. 034 +0. 0470	" -0. 035 +0. 06 -0. 12 +0. 150 -0. 08 +0. 04 -0. 005 -0. 03 0. 00 +0. 011	" +0.110 -0.11 -0.06 +0.010 +0.04 +0.03 -0.077 +0.07 0.00 -0.017	,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,	" +0.012 -0.01 0.00 +0.001 0.00 -0.007	" +0. 019 +0. 01 +0. 01 -0. 043 +0. 05 +0. 05 -0. 034 -0. 01 +0. 01 -0. 083	" -0. 055 +0. 01 -0. 04 -0. 010 +0. 06 +0. 05 -0. 041 +0. 01 -0. 03 +0. 060
I 12—13	—о. 134	-0.020	-0.02	+0.02		İ	+0.11	-o. o5

All the factors belonging to Jupiter having now been given, the similar quantities for Saturn are tabulated:

Arg=		v	71	X	,	В	,′		G ^r
$ \mu\gamma'+i'g'+ $	-ig	sin.	cos.	sin.	cos.	sin.	cos.	sin.	cos.
и i'	i o	"	11	"	 - 1. 2588	11		//	"
I I	0	+867.04	+ 2.74	+516.84	+ 1.90	+1383.88	+ 4.64	350.09	— I. 67
—I 2	0	+115.60	126.41	+ 60.57	-33.59	+ 176.17	— 160. 00	57.02	+83. 22
0 1	0	— 57. 3392	+ 73.0254	— 43. 5173	- o. 3053	— 100. 8565	+ 72.7201	+ 19.8580	44. 4869
1 0	0	— 39. o <u>5</u>	+ 29,64	6. 5936	+14.9534	— 45.64	+ 44.59	+ 30.42	-24. 29
—I 3	0	+ 2.12	- 27. 17	+ 4.03	6.87	+ 6.15	34.04	+ 0.90	+18.78
0 2	0	0.1210	+ 18.5562	5. 1065	+ 2.8158	— 5. 2275	+ 21.3720	— 2.1289	12.0027
I I	0	- 3.03	+ 5.23	+ 0.10	+ 1.72	— 2 . 93	+ 6.95	+ 2.22	- 4.49
—I 4	0	— I. 92	— 3. 36	0.02	— o. 88	τ. 94	- 4.24	+ 1.70	+ 2.35
0 3	0	+ 1.5755	+ 2.4063	- 0. 3401	+ 0. 5783	+ 1.2354	+ 2.9846	— I. 385I	- 1. 5718
I 2	0	- 0.07	+ 0.74	+ 0.11	+ 0.14	+ 0.04	+ 0.88	+ 0.01	— o. 64
—I 5	0	— o. 46	— o. 23	- 0.05	— 0. 08	— o. 51	— o. 31	+ o. 38	+ o. 15
0 4	0	+ 0.3615	+ 0.1704	+ 0.0007	+ 0.0736	+ o. 3622	+ 0.2440	— o. 2937	— o. o991
1 3	0	+ 0.04	+ 0.09	+ 0.02	+ 0.01	+ 0.06	+ 0.10	- 0.04	- o. o8
—1 6	0	- 0.03	0.00			— 0.03	0.00	+ 0.02	0, 00
0 5	0	+ 0.0520	- 0.0045	+ 0.0048	+ 0.0068	+ 0.0568	+ 0.0023	— 0.0416	+ 0.0076
I 4	D	- o.oı	+ 0.02			- 0.01	+ 0.02	⊹ 0.01	— 0. O2
0 6	٥	+ 0.0053	- 0.0032	+ 0.0009	+ 0.0005	+ 0.0062	- 0.0027	— 0.0042	+ 0.0030
0-4-	ı	- 0.0048	— 0.0132	— 0.0024	0.0019	— o. 0072	- 0.0151	+ 0.0038	+ 0.0114
_I-2-	1	— o. o6	- 0.03	- 0.01	— o. oı	— o. o7	- 0.04	+ 0.05	+ 0.03
0-3-	1	· - 0.0732	— o. o659	- 0. 0177	+ 0.0048	- 0.0909	— o. o611	+ 0.0598	+ 0.0564
1—4—	ı	+ 0.15	+ 0.10	+ 0.02	+ 0.01	+ 0.17	+ 0.11	— o. 13	- 0.09
-1-1-	1	— o. 51	— 0. 03	- o. o8	- o. oi	0.59	- 0.04	+ 0.43	+ 0.02
0—2—	I	o. 5963	- o. 1559	— о. 1161	+ 0.1176	— O. 7124	- 0.0383	+ 0.4790	+ 0.1294
1— 3—	I	+ 1.25	+ o. 18	+ 0.22	— o. o6	+ 1.47	+ 0.12	— I. 03	— o. 16

Arg=	V	7/	2	ζ′	F	3′	(G'
	sin.	cos.	sin.	cos.	sin.	cos.	sin.	cos.
ж i' i — I о— I		" + 2.80	" — 0.95	o. 76	,, 5. 06	+ 2.04	+ 3.12	
0—1—1	_ 2. 7934	+ 0.9512		+ 1.4648		+ 2.4160	+ 2.0982	— I. II75
I2 I	+ 7.94	- 3.48	+ 1.38	1.39	+ 9.32	- 4.87	— 6. 34	+ 3. 15
_1 1_1	47.620	- 42. 884	- 9.3 <u>5</u> 6	- 4.845	 5 6. 976	— 47·729	+ 49.88	+ 93.47
0 0— 1	0.0000	0,0000		+ 122.2131		+ 122.2131	0.0000	0.0000
1—I— I	+ 25.87	— 60.65	+ 4.62	17.37	+ 30.49	— 78. 02	15. 75	+ 69.20
1 z- I	+ 392.406	+1931.364	+ 79. 204	+ 393.671	+ 471.610	+2325.035	-423. o3	—2060. 97
0 1—1	— 575. 7289	-2765. 1410			— 573.7397	2763. 6644		+4344. 4247
1 0-1	+ 368.35	+1751.57	—304. 19	-1450.95	+ 64. 16	+ 300.62	782. 26	—3729. 4 7
I 3 I	+ 263.90	+ 253.95	+ 55.69	+ 66.67	+ 319.59	+ 320.62	20I.00	— 226.40
0 2— I	- 215. 5265	- 260. 4742		1 '			1	+ 301.0658
1 -1 I	+ 0.507	9. 840	— 14. 273	— 12 . 69 5	— 13.766	- 22.535	- 1.29	— 12.77
—I 4— I	+ 58.23	+ 4.33	+ 12.42	+ 4.56	+ 70.65	+ 8.89	— 43. 03	— 3.75
0 3— 1	— 48. 3766		— 4. 6698	_ 5.6234	53. 0464	i	+ 35.8158	+ 9.3200
I 2— I	— I. 773	- 4.097	— 2. 193	— o. 148	- 3.966	- 4. 245	+ 2.01	+ 2.31
—ı 5— ı	+ 7.27	4. 86	+ 1.72	- 0. 27	+ 8.99	- 5. 13	— 5. 21	+ 3.96
0 4—1	— 6. 1730	+ 4.0111	- I. 0443	o. 3889	— 7.2173	+ 3.6222	+ 4.3387	— 3. o443
1 3-1	— о. 65	— o. 56	— 0. 20	+ 0.13	— o. 85	- 0.43	+ 0.62	+ 0.35
—т 6— т	+ 0.43	— 1. 16	+ 0.15	— o. 15	+ 0.58	- 1.31	— o. 25	+ 0.94
0 5— 1	— o. 3672	+ 1.0038	— o. 1449	+ 0.0258	- 0.5121	+ 1.0296	+ 0, 2024	- o. 7907
1 4— 1	— O, I2	- 0.03	0.02	+ 0.03	- o. 14	0.00	+ 0.11	+ o. oı
_т 7— т	0.02	— o. 17	0, 00	- 0.02	0.02	- 0.19	+ 0.03	+ 0.14
о 6— г	+ 0.0358	+ 0. 1420	— o. or 34	+ 0.0130	+ 0.0224	+ 0. 1550	- 0.0413	- o. 110 7
1 5— 1	0.04	+ 0.02	0.00	— о. от	- 0.04	+ 0.01	+ 0.04	0.02
0 7— 1	+ 0.0132	+ 0.0136	о. 0006	+ 0.0022	+ 0.0126	+ 0.0158	0.0120	— o. o1o2
-I-I- 2	+ 0.01	- 0.03	İ		+ 0.01	- 0.03	o, oi	+ 0.02
0-2- 2	+ 0.0061	- o. o256	0,0042	0.0041	+ 0.0019	— o. o297	- o, oo61	+ 0.0205
1-3- 2	— o. oı	+ 0.07		i	— o. oı	+ 0.07	+ 0.01	— о. об
-1-0 2	0.02	- o. 21	— 0. O2	— o. 10	0.04	— о. 31	- 0.02	+ 0.07
O—I— 2	— o. o272	0. 0724	- 0.0512	- 0.0074	— o. o ₇ 84	o. o798	+ 0.0153	+ 0.0065
I2- 2	+ 0.11	+ 0.43	+ 0.06	+ 0.03	十 0.17	+ 0.46	— o. o8	- o. 33
-I I- 2	— 2. 97	- 7.89	- o. 31	0.48	- 3. 28	- 8. 37	+ 3.70	+ 12.62
0 0— 2	u, 0000	i .	+ 1.7529	1		1 .	1	1
I—I— 2	+ 1.69	+ 0.53	+ 0.61	+ 0.09	+ 2.30	+ 0.62	- 0.99	+ 1.50
—I 2— 2	+ 40.556		+ 11.04	- 0. 28	+ 51.60	+ 46.42	— 40. <u>3</u> 90	- 107.716
0 I— 2	— 45.25 69	- 191.3331					1	
ĭ 0— 2	+ 54.46	+ 193.37	20, 80	— 127.32	+ 33.66	+ 66.05	— 9 1 .41	— 379. 50
—I 3— 2	—1173.40		-244. 49	+ 104.88	-1417.89	+ 607.85	+835.77	— 363. 37
0 z- 2		— 410. 3923		l	+ 921.8298			+ 300. 2177
I I— 2	54.88	+ 26.72	+ 62.70	27.74	+ 7.82	- I. O2	+ 24.49	- 15.18
-I 4-2	— 206. 8 93	+ 353.200	50. 245	+ 62.573	— 257. 138	+ 415.773	+141.37	- 267.87
n 3— 2	+ 176.6016	l			+ 197.1868			
I 2— 2	+ 5.389	+ 28.123	+ 7.86	— II. 68	+ 13.25	+ 16.44	— 7· 524	— 18.749
—I 5— 2	+ 8.777	+ 85.869	— 2. <u>5</u> 80	+ 15.294	+ 6. 197	+ 101.163	— 11. 29	— 65.49
0 4- 2	7.2 696	- 75.7210		— 5. 2484				+ 57. 1032
I 3— 2	+ 6.31	+ 4.03	0.04	2.12	+ 6.27	+ 1.91	— 5·35	— 2. 33
I 6- 2	+ 9.93	+ 11.31	+ 0.84	+ 2.29	+ 10.77	+ 13.60	8.62	— 8. 37

Arg=	V	71		Χ']	3′	G	} '
$n\gamma'+i^{\gamma}g'+ig$	sin.	cos.	sin.	cos.	sin.	cos.	sin.	CO8.
u i' i	"	11	//	,,	,,	"	11	"
0 5— 2	— 8. 90733	— 10. 25910	+ 0.2205	— 1.2863	— 8.6868	— 11. 5454	+ 7.73073	+ 7.48003
I 4— 2	+ 1.445	- O. 202	— o. 171	— o. 231	+ 1.274	— o. 433	— 1. 15	+ 0.32
—ı 7— 2	+ 2.28	+ 0.58	+ o. 28	+ 0.22	+ 2.56	+ 0.80	- 1.91	— o. 32
0 6— 2	- 2. 08643	— 0.5 3294	— o. o715	— o. 1932	- 2.1579	- 0.7261	+ 1.73800	+ 0. 28121
I 5 2	+ o. 166	— о. 177	– о. оз	- 0.013	+ 0.131	— o. 190	— o. 13	+ 0.17
—I 8— 2	+ o. 3o	— о. 13	+ 0.04	0.01	+ 0.34	- O. 14	— o. 24	+ 0.13
0 7-2	— o. 2969	+ 0. 1057	0.0227	- o. o183	— o. 3196	+ 0.0874	+ 0. 2404	— C. 1101
ı 6— 2	0.00	- 0.04	0.00	0.00	0.00	- 0.04	0, 00	+ 0.04
— I 9— 2	+ 0.02	- 0.02			+ 0.02	— O. O2	_ 0. 02	+ 0.02
o 8— 2	0.0260	+ 0.0340	— 0.0038	— o. ooo4	— 0. 0298	+ o. o336	+ 0.0198	– ი. ივიუ
I 7— 2	+ 0.01	- 0.02			+ o. oi	- 0.02	— o. oı	+ 0.02
-1 o- 3	+ 0.03	+ 0.02			+ 0.03	+ 0.02	- 0.03	— o. o4
0 1 3	+ 0.0054	- o. o213	+ 0.0007	- 0,0014	+ o. oo61	— 0. 0227	— o. oo5o	+ 0.0163
1-2- 3	о. оз	+ 0.01			— o. o3	+ 0.01	+ 0.03	0, 00
II 3	+ 0.04	- o. 52	0.00	— O. O2	+ 0.04	0.54	+ o. o6	+ 0.93
0 0-3	0.0000	0,0000	+ o. 1737	+ 0.8449	+ 0. 1737	+ 0.8449	0, 0000	0.0000
1-1-3	— о. 18	— o. o6	0.00	+ 0.02	— o. 18	— o. o4	+ 0, 20	+ 0.22
—I 2— 3	+ 3.55	+ 2.68	+ 0.57	— o. 32	+ 4.12	+ 2.36	— 3.91	— 8. o6
0 1—3	— 3.9911	— 14.9472	- 0. 2141	— o. o749	- 4. 2052	- 15.0221	+ 6.9364	+ 31.0546
I 0— 3	+ 2.58	+ 16.28	- 2.06	- IO. O2	+ 0.52	+ 6.26	_ 5.83	— 31.36
—r 3 — 3	+ 1.51	+ 61.14	— 1.92	+ 13.38	— o. 41	+ 74.52	_ 5. 36	— 44. OI
0 2— 3	+ 16.7787	— 33· 3477	- 1.6199	2.1267	+ 15. 1588	— 35· 4744	— 9. 2355	+ 24. 2283
I I— 3	— 4. 6 <u>9</u>	+ 10.04	+ 2.53	+ 0.91	– 2. 16	+ 10.95	+ 3.06	- 8.23
—ı 4— 3	— 594. 32	852. 79	-95.33	—I 34. 35	—689. 65	-987.14	+459.59	+663.23
0 3— 3	+515.7983	+725.8970	— o. 5513	— I. 4375	+515.2470	+724. 4595	—396. 33 97	—560. 5710
I 2 3	— 8o. 76	112.87	+18.66	+ 25.56	— 62. 10	— 87. 31	+ 58.97	+ 82.65
—ı 5— з	392. 325	148. 624	- 57. 12	- 29. 23	449, 44	—177. 85	+312.688	+109.596
0 4-3	+349. 5288	+133.6786	+ 7.8778	+ 11. 3333	+357.4066	+145.0119	276. 9491	— 97. 6308
I 3— 3	— 51.65	— 3. 50	+ 8.46	+ 3.69	- 43. 19	+ 0.19	+ 39.56	+ 0.56
—r 6— 3	—101.33	+ 25.03	—15. 09	+ 0.44	—116.42	+ 25.47	+ 80.77	— 23.79
o 5-3	+ 92.8999	22. 1306	+ 4.7914	+ 2.4759	+ 97.6913	— 19. 6547	— 73. 6099	+ 21.2037
r 4— 3	— g. 6o	+ 8.37	+ 1.74	— o. 28	— 7.86	+ 8.09	+ 7.13	7.23
—r 7— 3	13.75	+ 15.44	2.39	+ 1.45	16. 14	+ 16.89	+ 10.60	— 13. 34
0 6— 3	+ 12.9321	— 1 4. 2449	+ 1.2702	 0. 0320	+ 14. 2023	— 14. 27 69		+ 12. 2941
I 5— 3	— o. 328	+ 2.509	+ o. 21	- 0. 20	·- 0. I2	+ 2.31	+ 0.097	- 2.084
—r 8— 3	- 0.47	+ 3.52	— O. 22	+ 0.38	- 0.69	+ 3.90	+ o. 21	- 2.98
o 7— 3	+ 0.4738	- 3. 3320	+ 0. 201 9	— 0. 1210		- 3.4530	— 0.2118	+ 2.8115
1 6-3	+ 0.24	+ 0.29	+ 0.01	- 0.04	+ o. 25	+ 0.25	- o. 23	— O. 2I
—ı 9— 3	+ o. 23	+ 0.51	+ 0.01	+ 0.06	+ 0.24	÷ 0.57	— O. 22	— 0.42
o 8— 3	— O. 2313	- 0.4824	+ 0.0184	— o. o331	— O. 2129	— o. 5155	+ 0. 2251	+ 0.3971
1 7— 3	+ 0.09	+ 0.01	0, 00	0.00	+ 0.09	+ 0.01	— o. o8	0.00
—ı 10— 3	+ 0.05	+ 0.03			+ 0.05	+ 0.03	— o. o5	о. оз
0 9— 3	— o. o68o	- 0. 0404	— 0.000 3	- o. oo55		– 0.045 9	+ 0.0611	+ 0.0308
1 8 3	+ 0.04	+ 0.01			+ 0.04	+ 0.01	— o. o4	0.01
0 10-3	- 0.0110	0.0000	— 0. 0 004	— o. ooo6	— o. o114	— o. ooo6	+ 0.0124	— o. ooo7

Arg=	v	.,	3	ζ′	В	3'	G	+′
$u\gamma'+i'g'+ig$	sin.	cos.	sin.	cos.	sin.	cos.	sin.	cos.
хi' i	"	"	"	"	"	"	, "	"
<u>-1</u> 1-4	0,00	- 0.02	0.00	0,00	0.00	- 0.02	+ 0.01	+ 0.05
0 0-4	0.0000	0.0000	+ 0.0143	+ 0.0656	+ 0.0143	+ 0.0656	0.0000	0.0000
1—1— 4	- 0.01	0.02	+ 0.01	0.00	0, 00	— 0. O2	+ 0.01	+ 0.03
—I 2— 4	+ 0.21	+ 0.36	+ 0.02	0,00	+ 0.23	+ 0.36	- o. 26	— o. 75
0 1—4	— o. 2895	 1, 1686	0,0016	— 0.0009	— o. 2911	— 1. 16 <u>9</u> 5	+ 0.5196	+ 2.3213
I 0— 4	+ o. 16	+ 1.12	o. 17	— o. 77	O, OI	+ 0.35	0.41	— 2. 28
—I 3— 4	+ 2.98	+ 3.42	+ o. 35	+ 0.69	+ 3.33	+ 4.11	- 2,60	- 2.52
0 2— 4	— o. 3590	— 2. 1539	0.0445	— o. 1286	0.4035	- 2. 2825	+ 0.5018	+ 1.6387
I 1-4	— o, 62	十 0.17	+ 0.01	+ 0.01	— о. 61	+ 0.18	+ 0.50	- O. I2
—I 4— 4	— 77. 68	+ 2.60	—12. 58	0, 82	— 90. 26	+ 1.78	+ 60.41	— 4·59
0 3 4	+ 54.3386	+ 15.9151	+ o. 8105	— 1.0164	+ 55. 1491	+ 14. 8987	41.8511	— 1o. 656o
I 2-4	12.19	— 4.86	+ 0.51	+ 1.55	— 11.68	- 3.31	+ 9.62	+ 3.39
—I 5— 4	+522.50	-561.53	+65.84	—72. 61	+588.34	634. 14	<u>-428. 27</u>	+457-45
0 4 4	—461. 9 5 41	+507.8785	+ 1.1622	0. 4024	460. 7919	+507.4761	+377.2372	414. 3948
I 3— 4	+ 94.13	—103. <u>3</u> 6	9.98	+11.37	+ 84. 15	91.99	 75⋅33	+ 82.37
—ı 6— 4	+ 66.73	371.03	+12.36	45-45	+ 79.09	416.48	50. 22	+306.90
0 5—4	— 6 1.7 309	+340.6751	— 5. <u>5</u> 801	+ 6.0077	67.3110	+346.6828	+ 46. 1689	—28o. 8633
I 4— 4	o. 17	— 61.37	— 1.23	+ 5.58	<u> </u>	55.79	+ 1.41	+ 49.83
—I 7— 4	— 42. 8 <u>5</u>	—IOO. 22	— 2. 96	-12.77	— 45. 81	112.99	+ 38. 29	+ 82,60
0 6— 4	+ 39.4048	+ 94. 1053	1.0552	+ 3.8132	+ 38. 3496	+ 97.9185	— 35. 22 35	- 77. 2929
1 5-4	— 10. 98	— 12.61	+ 0.44	+ 1.25	10. 54	11.36	+ 9.54	+ 10.05
—ı 8— 4	20.38	— 1 3.43	1.87	- 2.06	22. 25	— 15.49	+ 17.70	+ 10.67
o 7 4	+ 19.1792	+ 12.9092	+ 0.2466	+ 1.0752	+ 19.4258	+ 13.9844	— 16. 63o8	— 10. 2117
1 6-4	— 3.55	— o. 59	+ o. 18	+ 0. 14	— 3. 37	— o. 45	+ 3.02	+ 0.34
I 9 4	— 4. 6 ₃	+ 0.01	— o. 49	- o. 16	— 5. 12	- o. 15	+ 3.96	0.20
0 8 4	+ 4.4607	+ 0.0425	+ 0.1574	+ 0. 1749	+ 4.6181	+ 0.2174	— 3.8149	+ 0.1506
1 7-4	— u. 62	+ 0.32	+ 0.04	+ 0.02	— o. 58	+ 0.34	+ 0.52	— o. 3o
— I IO— 4	— o. 68	+ 0.43	— o. o8	+ 0.03	— о. 76	+ 0.46	+ 0.57	- 0, 40
0 9—4	+ o. 6501	— o. 4164	+ 0.0404	+ 0.0136	+ 0.6905	- o. 4028	— o. 5437	+ 0.3903
I 8 4	— 0.03	+ 0.12	u, 0 0	0.00	— o. o3	+ 0.12	+ 0.02	— o. 11
—I II— 4	0, 05	+ 0.14			— o. o5	+ 0.14	+ 0.05	o. 14
0 10 4	十 0.0525	— O. 1127	+ 0.0067	— o. oo13	+ 0.0592	- 0.1140	- o. o4o8	+ 0.1012
1 9—4	0.01	+ 0.04	1		0, 01	+ 0.04	+ 0.01	- 0.04
0 11 4	+ 0.0006	+ 0.0142	+ 0.0007	— o. ooo7	+ 0.0013	+ 0.0135	0,0000	- 0.0148
0 0- 5	0,0000	0.0000	+ 0.0009	+ 0.0048	+ 0.0009	+ 0.0048	0,0000	0.0000
-I 2-5	0.00	+ 0.03	0, 00	0.00	0,00	+ 0.03	0.00	- 0.06
o 1— 5	— o. o190	_ o. o86o	- o. ooo3	+ 0.0003	— o. o197	- 0.0857	+ 0.0363	, ,
I 0- 5	+ 0.02	+ 0.08	- 0.02	_ 0.06	0,00	+ 0.02	- 0.04	0. 17
-r 3 5	+ 0.16	+ 0.14	+ 0.02	+ 0.03	+ 0.18	+ 0.17	- o. 13	- o. 10
o 2— 5	- 0.0263	- 0. 1235	— o. oo34	- 0,0029	— o. o297	- o. 1264	+ 0.0293	+ 0.0968
1 I— 5	0.00	_ 0,02	0,00	0.00	0.00	- 0.02	0,00	+ 0.02
—I 4— 5	— 4. 19	+ 3.89	— o. 73	+ 0.46	4. 92	+ 4.35	+ 3.19	− 3.37
0 3-5	+ 3.4329	- 0.9817	+ 0.0596	- o. o658	+ 3.4925	_ 1.0475	_ 2.6351	1
I 2— 5	- 0. 70	- o. 31	+ 0.04	+ 0.03	- o. 66	- o. 28	+ 0.54	+ 0.24
5- 5	— II. 8I	- 77.78	- o. 81	-10. 10	— 12.62	— 87.88	+ 11.20	+ 63.54
0 4-5	- 5.0628	+ 62. 3156	+ 0.6043	+ 0. 2578	- 4. 4585	+ 62.5734	+ 3.0690	
<u> </u>	<u> </u>	1	"	1	1			

Arg=	v	71	2	K ′	F	3′	(3 ′
$ \mu\gamma' + i'g' + ig $	sin.	cos.	sin.	cos.	sin.	cos.	sin.	608.
и i' i 1 3— 5	" + 2.78	" — 14. 50		" + 0.75	+ 2.05	 13.75	// 2,00	,, + 11.81
—ı 6— 5	+456.97	+268.52		+ 3.73 $+$ 27.88	+506.40	+296.40	—38 5. 45	-228. 24
0 5— 5	-430.97 -424.0840	-241. 5061	+49·43 + 0.3585	+ o. 8537	 423. 7255	-240. 6524	+357.0214	+204. 8103
I 4 5	+ 98. 32	+ 56. 54	— 6. 47	- 3.49	+ 91.85	+ 53.05	- 82.01	— 47·45
-I 7-5	+309.64	- 4· 97	+32.60	— 3.49 + 1.76	+342.24	— 3. 2I	263. 24	+ 6.98
0 6-5	-289. 8739	+ 4.8711	— 4. 0926	2. 3865	-293. 9665	+ 2.4846	+245. 9267	- 6.7882
I 5— 5	+ 58.51	- 8.62	- 3· 43	- 0. 04	+ 55.08	— 8.66	— 49. 22	+ 8.01
-1 8-5	+ 85.86	- 56. 25	+ 9.56	- 4. 4I	+ 95.42	60.66	— 72. 55	+ 49.77
0 7-5	— 81.9068	+ 52. 9242	- 2.7370	o. 1633	84. 6438	+ 52.7609	+ 69.0697	— 46. 7912
1 6-5	+ 12.60	— I3. 20	- o. 81	+ 0.47	+ 11.79	— 12. 7 3	— 10. 44	+ 11.55
_I 9— 5	+ 10.49	- 23.42	+ 1.53	- 2.05	+ 12.02	- 25.47	- 8.46	+ 20.51
o 8— 5	— 10. 2918	+ 22.4218	— 0. 8052	+ 0. 3684	11.0970	+ 22.7902	+ 8. 2981	— 19. 6162
I 7— 5	+ 0.43	- 4· 34	— 0, 10	+ 0. 16	+ 0.33	- 4. 18	— o. 23	+ 3.76
1 10 5	— o. 85	- 5· 34	+ 0.04	- o. 51	— o. 81	_ 5.85	+ 0.91	+ 4.63
0 9 5	+ 0.7335	+ 5. 1892	— 0. 1279	+ 0.1716	+ 0.6056	+ 5. 3608	- 0.8062	- 4.4917
1 8— 5	- 0.45	- 0.75	- 0. 0I	+ 0.04	- 0.46	- 0.71	+ 0.42	+ 0.64
_1 11- 5	- 0.67	— 0.75	— o. o4	0.08	- 0.71	_ o. 83	+ 0.62	+ 0.64
0 10— 5	+ 0.6437	+ 0.7452	— 0. 0054	+ 0.0429	+ 0.6383	+ 0.7881	- u. 5929	- 0,6312
1 9-5	- 0.16	- 0.07	0.00	0.00	— 0. 16	- 0.07	+ 0.14	+ 0.06
_1 12— 5	- 0.20	- 0.04	0.00	0,00	O, 20	0.04	+ 0.18	+ 0.03
0 11- 5	+ 0.1623	+ 0.0454	+ 0.0029	+ 0.0070	+ 0.1652	+ 0.0524	- 0. 1454	— o. o331
1 10-5	+ 0.1023	— 0.01 — 0.01	+ 0.0029	+ 0.0020	+ 0.02	— 0. 0I	0.02	+ 0.01
0 12— 5	+ 0.0212	- 0.0071	+ 0.0010	+ 0.0007	+ 0.0222	— 0. 0064	— 0.0179	+ 0.0075
		1	`					
0 2—6	- 0.0013	0.0049	0.0004	— O. 0002	- 0.0017	- 0.0051	+ 0.0013	+ 0.0033
—I 4— 6	- 0.16	+ 0, 30	0,00	+ 0.02	— 0.16	+ 0.32	+ 0.12	- 0.25
0 3-6	+ 0.1872	- 0, 1092	+ 0.0013	— o. oo41	+ 0. 1885	— o. 1133	- 0. 1426	+ 0.0969
I 2 6	- 0.03	- 0.01	+ 0.01	0,00	- 0.02	- 0.01	+ 0.02	+ 0.01
—I 5— 6	4.80	- 4.22	— 0. 50	— o, 6o	- 5.30	- 4.82	+ 4.16	+ 3.35
0 4 6	+ 2.0503	+ 4. 1065	+ 0.0544	+ 0.0187	+ 2. 1047	+ 4. 1252	1.8269	- 3. 3004 + 0. 86
I 3— 6	- 0.06	I. o6	- 0.01	+ 0,06	- 0.07	I. 00	+ 0.06	+ 0.86 + 18.78
—I 6— 6	+ 66.21	- 21. 15	+ 7.22	- 1.89	+ 73.43	- 23.04	- 55.86 + 48.5565	('
0 5 6	— 57. 6 <u>95</u> 6	+ 7.4175	— o. o377	+ 0.3441	- 57.7333	+ 7.7616	1	
1 4— 6	+ 14.41	- 0.40	0, 64	— 0. 26	+ 13.77	- 0.66	— 12. 11	+ 0.50
—I 7— 6	—105.94 → 04.5054	+332.79	- 9. 02	+30.88	—114.96 ± 02.0458	+363.67	+ 92. 81 - 82. 6770	-287.80 +271.4960
0 6— 6	+ 94. 5054	—314. 3314 1 78 00	— 0. 5596 — 0. 05	+ 0. 3265	+ 93.9458	-314.0049 + 75.49	+ 21.22	- 67. 86
1 5— 6 —1 8— 6	— 24.42 — 52.65	+ 78.99	+ 0.95 + 3.63	- 3.50 +21.45	— 23.47 + 57.28	+ 75.49	+ 21. 22 - 48. 23	- 07. 80 -202. 02
i	+ 53.65	+232.74	¥.	t		1		1 1
o 7— 6 I 6— 6	— 52.8883 + 18.26	220.7926 + 48.00	+ 0.7951	— 2. 5592 — 1. 07	— 52.0932 — 17.78	-223. 3518 - 46.02	+ 47.8079 - 16.80	+191. 3864 - 41. 38
1	+ 18.36	+ 64.45	— 0. 58 — 4. 76	- 1.97 + 6.41	+ 17.78 + 66.60	+ 46.03	1	
—I 9— 6	+ 61.84		+ 4.76 0.2938	- 1.8018	— 59. 1664	+ 70.82 - 63.8921	— 54. 93 ± 52. 3177	- 55.45 + 56.3714
0 8 6	58.8726	— 62. 0903 — 10. 22			+ 13.46	I	+ 52. 2177 - 12. 17	- 8. 67
1 7— 6	+ 13.85	+ 10. 23	— 0. 39 — 1. 0f	— 0. 49 — 0. 00	+ 13.40 + 26.08	+ 9.74	- 12. 17 - 21. 35	
—I IO— 6	+ 24. 13	+ 6.12	+ 1.95 - 0.3086	+ 0.90		+ 7.02		- 4.9I - 4.8708
0 9-6	- 23. 2857	- 6.0930	— o. 3986	— o. 5393	- 23. 6843 - 4.40	— 6. 6323 — 0. 14	+ 20. 5747	
1 8— 6	+ 4.64	- 0.09	0. 15	— 0. 05	+ 4.49	— 0. 14 — 1. 82	— 4.07 4.78	+ 0.19
1 11 6	+ 5.45	1.78	+ 0.49	- 0.05	+ 5.94	— 1.83 — 1.7086	- 4.78 - 4.672T	+ 1.71 - 1.6173
o 10 6	- 5. 3346	+ 1.6757	0. 1644	0. 0771	— 5. 4990	+ 1.5986	+ 4.6731	— I. 6173

Arg=	V	71	X	,	В	3'	G	ł'
$n\gamma' + i^{7}g' + ig$	sin.	cos.	sin.	cos.	sin.	cos.	sin.	cos.
и i' i	"	"	11	"	"	11	11	11
1 9 6	+ o. 8 ₃	— 0.62	— o. o4	+0.01	+ 0.79	— 0.61	- 0.72	+ 0.57
—I I2— 6	+ 0.74	— 0. 90	+ 0.08	o. o5	+ 0.82	— o. 95	— о. 63	+ 0.82
o 11— 6	— o. 7335	+ 0.8634	— 0 , 0403	+0.0025	— o. 7738	+ o. 8659	+ 0.6271	— о. 7888
1 10— 6	+ 0.06	0, 20	0.00	+0.01	+ 0.06	— o. 19	0.05	+ 0.18
— 1 13— 6	+ 0.03	— O. 22			+ 0.03	0. 22	— o.o3	+ 0.22
0 12— 6	- o. o283	+ 0.2053	o, oo65	+0.0043	— o. o348	+ 0.2096	+ 0.0170	— o. 1848
1 11-6	+ 0.02	- 0.07			+ 0.02	- 0.07	0.02	+ 0.07
0 3—7	+ 0.0080	- o. oo86			+ 0.0080	— o. oo86	— o. oo56	+ 0.0074
—ı 5— 7	0.41	- o. 17	— o. o5	-o. o3	— o. 46	- 0, 20	+ 0.35	+ 0.13
0 4— 7	+ 0.2175	+ 0.2149	+ 0.0040	-0.0002	+ 0.2215	+ 0.2147	— о. 1881	— о. 1693
ı 3— 7	— o.o3	0.02	+ 0.01	0.00	- O. O2	- 0.02	+ 0.03	+ 0.01
—ı 6— 7	+ 3.58	- 5.32	+ 0.43	0. 51	+ 4.01	5.83	 2. 94	+ 4.64
o 5— 7	— 3. 8 ₉₃₇	+ 3.0776	+ 0.0011	+o. o368	— 3. 8926	+ 3.1144	+ 3. 2301	2. 7035
I 4— 7	+ 1.07	— o. 48	0.04	+0.01	+ 1.03	— o. 47	— o. 89	+ 0.43
—ı 7— 7	+ 26.43	+ 49.63	+ 2.24	+4.67	+ 28.67	+ 54.30	— 23. 38	— 42.85
0 6-7	— 1 6. 2761	45.8851	— о. 1860	+0.0386	— 16.4621	— 45. 8465	+ 14.4380	+ 39. 5650
ı 5— 7	+ 3.09	+ 12.22	+ 0.02	0.42	+ 3.11	+ 11.80	- 2.76	— 10. 52
_1 8— 7	220. 85	— 16.99	—17. 90	o. 86	—238. 75	17.85	+194.62	+ 15.74
o 7— 7	+211.2685	+ 12.3845	— o. 2789	0. 3532	+210.9896	+ 12.0313	—186. o16o	11.5928
r 6— 7	56. 18	3.88	+ 1.79	+0.05	— 54 · 39	— 3.83	+ 49. 29	+ 3.56
—ı 9— 7	—159. 11	+ 71.86	-13.02	+5.17	— 172. 13	十 77.03	+140.37	— 64. 2 5
0 8 7	+152.3186	69. 5874	+ 1.4855	+0. 1005	+153.8041	— 69. 4869	—134. 2451	+ 62. 1753
I 7 7	— 34. 8 5	+ 19.38	+ 1.08	-0.47	— 33·77	+ 18.91	+ 30.60	 17. 28
1 10- 7	42.07	+ 60.01	3.84	+4.35	— 4 5 . 91	+ 64.36	+ 36.71	— 53·7 ²
o 9— 7	+ 40.9072	- 57.9441	+ 1.0950	—o. 4257	+ 42.0022	 58. 3698	— 35. 6578	+ 51.8271
ı 8 7	6.92	+ 13.93	+ 0. 26	-0.34	— 6.66	+ 13.59	+ 5.95	- I2.42
I II 7	— I. 42	+ 22.40	o. 39	+1.69	— I. 8I	+ 24.09	+ o. 91	— 1 9. 99
0 10— 7	+ 1.5933	— 21.8425	+ 0. 3222	0. 3622	+ 1.9155	— 22. 2047	— 1.0710	+ 19.4824
I 9-7	+ 0.62	+ 4.46	+ 0.03	<u>—</u> 0. 12	+ o.65	+ 4.34	— o. 63	— 3.96
—I I2— 7	+ 2.60	+ 4.96	+ o. 13	+0.41	+ 2.73	+ 5.37	- 2.43	- 4.39
o 11— 7	2. 5381	- 4. 9204	+ 0.0339	—0. 141 9	- 2.5042	- 5.0623	+ 2.3719	+ 4.3525
1 10- 7	+ 0.76	+ 0.80	o. oi	o. o3	+ 0.75	+ 0.77	о. 70	— o. 7o
—I I3— 7	+ 1.11	+ o. 66	+ 0.06	+0. 06	+ 1.17	+ 0.72	— I. O2	— o. 57
0 12- 7	1.0693	— o.6373	— 0. 0094	—0. 0344	— I. 0787	- 0.6717	+ 0,9802	
1 11 — 7	+ 0.21	+ 0.04	0.00	0.01	+ o. 21	+ 0.03	0. 19	— o. o3
0 4—8	+ 0.0258	+ 0.0105			+ 0.0258	+ 0.0105	- 0.0234	— o. oo81
_r 6— 8	- 0.02	- 0.54	0.00	0.04	- 0,02	— o. 58	+ 0.04	+ 0.47
0 5—8	— o. 1711	+ 0.3098	+ 0.0012	+0.0028	— o. 1699	+ 0.3126	+ 0.1348	— o. 2681
1 4— 8	+ 0.05	- 0.02	0.00	0.00	+ 0.05	- 0.02	— 0.04	+ 0.01
-ı 7- 8	+ 5.36	+ 2.33	+ 0.45	+0.26	+ 5.81	+ 2.59	- 4.73	- 1.93
o 6— 8	— 3. 6846	— 3. 0367	— 0. 0223	+0.0083	— 3. 7 069	- 3. 0284	+ 3.2523	+ 2.5747
ı 5— 8	+ 0.75	+ 1.02	0.00	0.04	+ 0.75	+ 0.98	— о. 66	— o. 88
r 8 8	— 33. 15	+ 26.99	— 2.74	+2.09	35.89	+ 29.08	+ 29. 14	24. 07
o 7— 8	+ 32. 1359	20. 0470	0. 0544	-0.0945	+ 32.0815	— 20. 1415	— 28. 2365	+ 17.8507
1 6 B	- 9.00	+ 4.53	+ 0.26	o. o5	- 8. 74	+ 4.48	+ 7.90	- 4.02
_r 9— 8	21.89	—134. 67	— 1.92	<u>9.65</u>	— 23.81	-144. 32	+ 19.07	+120.47
		ļ	l		!		<u> </u>	l

Arg=	v	,	X	,	В	//	(3′
$n\gamma'+i\tilde{i}'g'+ig$	sin.	cos.	sin.	cos.	sin.	cos.	sin.	cos.
и i' i	"	"	"	11	11	"	"	11
o 8 8	+23.8594	+129. 9802	+ 0. 1968	-0. 2210	+24.0562	+129.7592	—20. 8 <u>5</u> 85	—116. 1964 —
ı 7—8	— 6. 11	36. 09	+o. 18	+o. 8 ₇	— 5 ⋅ 93	— 35.22	+ 5.34	+ 32. 19
—ı 10— 8	-72. 99	— 98 . 88	-4. 98	−7. 28	─77. 97	—106. 16	+65.72	+ 88. 37
o 9—8	+71.2107	+ 95. 2406	+0. 1408	+0.8024	+71.3515	+ 96.0430	—6 4. 0 803	— 85. 0511
ı 8— 8	—19. 23	— 22.60	+o. 39	+0.54	—18. 84	— 22.06	+17.28	+ 20. 12
—ı 11— 8	—52.45	— 23. OI	-3.55	-I. 99	— 56. oo	25.00	+47.32	+ 20. 24
0 10 8	+51.0787	+ 22.4700	+0.4113	+0.6128	+51,4900	+ 23.0828	<u>—46. 0609</u>	19. 7496
1 9— 8	12. 40	— 3⋅59	+0. 24	+0.13	—12, 16	3.46	+11.16	+ 3.10
—I I2— 8	—19. 05	+ 2.38	-1.35	-0.03	20, 40	+ 2.35	+17.14	- 2.39
0 11 — 8	+18.7200	2. 2004	+o. 2967	+0. 1672	+19.0167	 2. 0332	—16. 8 <u>3</u> 93	+ 2. 2242
1 10 8	3.94	+ 1.27	+0.09	0.00	— 3. 8 ₅	+ 1.27	+ 3.53	- I. 20
—ı 13— 8	— 4. 22	+ 3.44	0. 32	+0. 17	— 4⋅ 54	+ 3.61	+ 3.77	- 3. 19
0 12— 8	+ 4. 1429	- 3. 2712	+0.1114	+0.0031	+ 4.2543	— 3. 268 ₁	— 3. 699 5	+ 3.0360
1 11—8	— o. 65	+ 0.82	+0.02	-0.01	— o. 63	+ 0.81	+ 0.57	— o. 76
0 5— 9	— o, oo3o	+ 0.0207			— o. oogo	+ 0.0207	+ 0,0015	— o. o177
—ı 7 — 9	+ 0.49	— o, o6	+0.04	+0.01	+ o. 53	— o. o5	— o. 43	+ 0.07
0 6- 9	o. 3753	— o. 1059	-0,0018	+0.0014	— o. 3771	— o. 1045	+ 0. 3303	+ 0.0840
I 5 9	+ 0.08	+ 0.06	0, 00	0. 01	+ 0.08	+ 0.05	0.07	— o. o5
—ı 8— 9	1.18	+ 4.90	-O. 12	+o. 38	— I. 30	+ 5.28	+ 0.98	 4⋅37
o 7— 9	+ 1.9100	3. 7525	— 0. 0095	-0.0110	+ 1.9005	— 3. 7 625	1.6457	+ 3.3427
ı 6— 9	— o. 67	+ 0.86	+0.02	o. oi	— o. 6 5	+ 0.85	+ o. 59	— o. 76
—ı 9— 9	23.90	— 1 9. 5 6	—1. 68	—1.45	25. 58	<u> </u>	+21.50	+ 17.41
o 8— 9	+19. 5961	+ 19.8982	+0.0408	-0. 0484	+19.6369	+ 19.8498	17. 6041	— 17.7133
1 7— 9	— 4. 96	5.88	+0.07	+0.14	4.89	— 5⋅74	+ 4.45	+ 5.23
—I IO— 9	+75.25	— 32.42	+4.79	-2.32	+80.04	- 34⋅74	68. 15	+ 29.01
o 9— 9	-73.0070	+ 33.4570	+0. 1624	+0.0978	—72. 8446	+ 33.5548	+66. o839	— 29. 9 <u>5</u> 18
1 8 9	+21.01	9. 20	—о. 38	+0.20	+20.63	— 9.00	18.98	+ 8.23
—I II— 9	+55. 16	— 63. 10	+3.69	—3.96	+58.85	- 67.06	—49. 8 2	+ 57.27
o 10— 9	—53. 3262	+ 61.8900	0, 4010	+0. 1807	—53.7272	+ 62.0707	+47. 1332	<u> </u>
1 9 9	+12.97	- 16.74	-0. 24	+0.28	+12.73	— 16.46	—11.68	+ 15.17
1 12 9	+ 8.98	— 42.09	+o. 8o	-2.64	+ 9.78	— 44· 7 3	— 7.87	+ 38. 26
0 11— 9	- 8. 7822			+0.3297	— 9. o945	+ 41.6157	+ 7.6905	i
1 10-9	+ 0.98	— IO. I7	0.05	+0. 16	+ 0.93	- 10.01	— o. 81	+ 9.23
—I I3— 9	— 5.49	- 15. 55	-0.20	—I.00	— 5. 69	— 16.55	+ 5.19	+ 14.13
0 12— 9	+ 5.0559	+ 15.0834	-0.0679	1		+ 15.3028	ľ .	
1 II 9	— I. 57	- 3. 10	+0.02	+0.07	1.55	- 3.03	+ 1.47	+ 2.81
о 6—10	o. o358	+ 0.0053			— o. o358	+ 0.0053	+ 0.0331	— o. oo59
—ı 810	+ 0.13	+ 0.34	0.00	+0.03	+ o. 13	+ 0.37	— o. 14	- 0.29
0 7—10	+ 0.0140	— o. 3907	-0.0015	0.0007	+ 0.0125	— o. 3914	+ 0.0178	+ 0.3466
ı 6—10	— 0.02	+ 0.22	0.00	-o. ot	0.02	+ 0.21	0.00	- O. 2I
—ı 9—ıo	— 4. o3	0.14	-o. 28	0.04	- 4. 3I	— o. 18	+ 3.62	+ 0.08
о 8—10	+ 3.3860	+ 0.8470	+0.0056	-o. oo81	+ 3.3916		— 3 . 0446	— o. 7237
1 7—10	— o. 89	- 0.42	+0.02	+0.02	— o. 87	— 0.40	+ 0.80	+ 0.37
—I IO—IO	+ 9.90	- 19. 10	+o. 65	— 1. 23	+10.55	— 20. 33	— 8. 91	+ 17.33
0 9—10	-10.6321	+ 16.6454	+0.0361	+0.0164	—10. 59 60	+ 16.6618	+ 9.5680	- 15. 0857
1 8-10	+ 3.28	— 4· 49	—0. 07	+0.06	+ 3.21	— 4· 43	- 2.95	+ 4.07

Arg=	v	,	2	Κ′	В	′	(*/
$n\gamma' + i'g' + ig$	sin.	cos.	sin.	cos.	sin.	cos.	sin.	cos.
n i' i	<i>n</i>	"	"	"	"	"	11	11
—I II—IO	+29.57	+37.85	+1.86	+2.17	+31.43	+40.02	26.81	34. 65
0 10—10	30. 2760	<u>36.83</u> 80	—о. o39 7	+0.1117	—30. 3157	—36. 72 63	+27.4554	+33.7060
1 9—10	+ 8.64	+11.01	o. 14	-o. 17	+ 8.50	+10.84	— 7.83	10.06
—I I2—I 0	+48.89	+26.58	+2.86	+1.66	+51.75	+28.24	·44· 7 I	-24. 22
0 11—10	<u>—48. 2060</u>	25 . 6390	o. 1465	—о. 1824	48. 3525	-25.8214	+44.0714	+23. 3455
1 10—10	+13.14	+ 6.29	0. 19	-O. II	+12.95	+ 6.18	·I 2. 00	— 5.72
—r 13—10	+33.25	— o. 89	+1.87	+0.11	+35.12	— о. 78	—30. 5 3	+ 1.04
0 12-10	—31.8490	+ 0.4249	—o. 2339	0. 1371	-32, 0829	+ 0. 2878	+29. 2282	o. 5947
1 11-10	+ 7.50	- o. 62	u. i3	+0.01	+ 7.37	— 0.61	6.87	+ o. 62
—1 8—11	+ 0.03	+ 0.02		1	+ 0.03	+ 0.02	о. оз	0.02
0 7—11	- o. oi 12	0.0310			— o. oi 12	0.0310	+ 0,0133	+ 0.0268
—I 9—II	— o. 37	+ 0.21	-0.02	+0.01	o. 39	+ 0.22	+ o. 33	— o. 20
o 8—11	+ 0.3436	— o. o760	+0.0003	-0.0011	+ 0. 3439	— o. 0771	— 0. 3082	+ 0.0733
1 711	— o. 10	0. 03	0, 00	+0.01	o. 10	— O. O2	+ 0.09	+ 0.03
I IOII	— o. 49	 3. o6	+0.01	-0. 20	— о. 48	3. 26	+ 0.47	+ 2.77
0 9—11	— o. o759	+ 2.7440	+0.0057	+0.0012	— o. 0702	+ 2.7452	+ 0.0471	— 2 . 4869
1 8—11	+ 0.14	— o. 77	0.00	0.00	+ 0.14	- o. 77	0.12	+ 0.70
-I II-II	+14.01	+ 3.73	+0.82	+0.23	+14.83	+ 3.96	—12. 81	— 3· 37
0 10—11	<u>—12. 714</u> 0	- 4. 5200	-0.0032	+0.0246	—12.7172	- 4. 4954	+11.6130	+ 4.0997
1 9—11	+ 3.57	+ 1.53	-o. o3	_0, o2	+ 3.54	+ 1.51	3. 26	I. 39
—I 12—II	—16.52	+22. 11	о. 83	+1.26	—17. <u>35</u>	+23.37	+15.28	20. 23
0 11-11	+15.9920	—22. 730 0	-o. o716	_o. oo68	+15.9204	-22. 7768	16. 7842	+20.8142
1 10—11	 4. 98	+ 6.69	+o. o8	_0.09	4.90	+ 6.60	+ 4.60	— 6. 13
—1 1 3—11	9.05	+38.23	o. 55	+1.97	— g. 60	+40, 20	+ 8. 27	- 35⋅37
0 12—11	+ 8, 9080	—36. o750	+0.0682	o. o999	+ 8. 9762	<u>—36. 1749</u>	- 8. 1424	+33. 3516
1 11-11	— 2. 24	+ 9.08	+0.02	—o. 14	- 2. 22	+ 8.94	+ 2.05	— 8. 37
o 8—12	+ 0.0236	— o. o151			+ 0.0236	— o. o151	— 0 . 0209	+ 0.0127
I IOI2	— O. 24	— o. 27	0.00	-0. O2	O. 24	— 0.29	+ 0.22	+ o. 24
0 9—12	+ 0. 1216	+ 0.2719	+0.0008	-0,0002	+ o. 1224	+ 0.2717	— о. 1135	— o. 2470
1 8-12	0,00	— o. o7	u. 00	0.00	0.00	- 0.07	0.00	+ 0.06
-I II-I2	+ 2.14	о. 86	+0.13	0.04	+ 2.27	0.90	- 1.95	+ o. 81
0 10-12	2.0240	+ 0. 3954	0,0000	+o. oo36	— 2. 0240	+ 0.3990	+ 1.8470	— o. 3759
1 9-12	+ 0.62	+ 0.02	o. oı	0.00	+ o. 61	+ 0.02	o. 57	— O. O2
—I I2—I2	o. 3o	+ 9.30	о. оз	+0.50	o. 33	+ 9.80	+ 0.26	— 8. 56
0 11—12	+ 0.9865	- 8. 7420	0.0173	+0.0020	+ 0.9692	— 8. 7400	— o. 9001	+ 8.0373
I IO—I2	— o. 47	+ 2.56	+0.02	0.02	— o. 45	+ 2.54	+ 0.43	2. 35
—ı 13—12	18. 36	— 4. 69	—о. 8 ₇	—о. 18	19. 23	— 4. 8 ₇	+17.08	+ 4.41
o 12—12	+17.0600	+ 4. 3260	u. 00I2	-0.0432	+17.0588	+ 4. 2828	—15. 8618	- 4.0710
I II—I2	- 4. 38	— I.42	+0.07	+0.02	- 4.3I	- 1.40	+ 3.96	+ 1.33
	<u> </u>			Į.	L	<u> </u>	<u> </u>	

Next in order follows the expression for $\overline{\mathbf{T}}'$:

	Ī	ī,		F	T'
Arg=i'g'+ig			Arg=i'g'+ig	· · · · · · · · · · · · · · · · · · ·	1
	sin.	cos.		sin.	cos.
i' i	"	11	i' i	, 11	"
0 0		+ o. 1478	8 5	-0. 2953	+ 0.7502
10	+ 1.9899	+ 9.5637	9 5	+0.0321	+ 0. 1493
2 0	+ 0.8926	+ 0.9746	10- 5	+0.0194	+ 0.0174
3 0	+ o. 1482	+ 0.0426	11— 5	+0.0041	+ 0.0001
4 0	+ 0.0172	0.0044	4 6	+o. 1482	+ 0.2746
—2— I	+ 0.0058	— o. o188	5 6	-3. 1481	+ 0.4643
-I — I	+ 0.0502	+ 0. 1843	6— 6	+4.2774	—14. 1586
0— I	— 11.6426	55. 5290	7— 6	—2. 0135	8. 4942
1 1	+110.6520	+527.2337	8— 6	-2. 0513	- 2.0309
2 I	13. 3822	+ 9.8429	9— 6	0. 7069	— o. 1547
3— І	- 2.4227	+ 1.6236	10 6	o. 142 1	+ 0.0534
4 I	o. 1852	+ 0.3373	11 6	—0. 0163	+ 0.0230
5— 1	+ 0.0022	+ 0.0458	r	0. 2103	+ 0. 1760
—I— 2	+ 0.0161	+ 0.0358	5— 7 6— 7	0. 2103 0. 7856	- 2. 1291
0 2	— I. 0375	- 5. 2269	7-7	-0.7830 $+8.383$	+ 0.519
I 2	+ 10.9496	+ 61. 1107	8— 7	+5. 265	— 2. 455
2— 2	+ 92.6790	- 38. 1746	9-7	+1.224	— I. 82I
3 2	+ 10.0689	20. 8725	10-7	+0.0162	0.6112
4— 2	- 0.9708	— 3. 8o75	11-7	—o. o7o3	— o. 1186
5— 2	0.4612	o. 3546	12— 7	-o. o193	0.0139
6— 2	0.0792	- 0.0013	·		
7— 2	— o. oo84	+ 0.0057	6— 8	—о. 1831	— o. 1359
		,	7-8	+1.294	— o. 821
o— 3	0.0909	- 0.4232	8— 8	+0.829	+ 4.607
1 - 3	+ 0. 9394	+ 6.0984	9— 8 10— 8	+2. 258	+ 2.977
2 - 3	+ 1.8926 + 39.3716	- 4. 0378 + 55. 5085	11 8	+1.566	+ 0.602
3— 3 4— 3	+ 39.3710 + 20.3422	+ 6.7285	12— 8	+0.474	0. 082
5— 3	+ 4. 1889	— 1. 3921	12- 8	+0.096	- 0.072
6 3	+ 0.4345	0, 6126	7— 9	+0.073	·- o. 148
7 3	- 0,0004	- 0.1146	8— 9	+0.706	+ 0.724
8-3	— o. oog6	- 0.0133	9— 9	-2. 328	+ 1.046
9-3	- 0.0020	- 0.0007	10 9	-1.541	+ I.774
			11-9	—o. 223	+ 1.078
1-4	+ 0.0732	+ 0.3879	12-9	+0.120	+ 0.354
2— 4	0.0262	- 0. 2236	8—10	+0. 134	+ 0.044
3-4	+ 4.6982	+ 1.1890	9—10	—o. 355	+ 0.564
4-4	— 28. 6894	+ 29.4477	10—10	o. 888	— I. 077
5 4 6 4	- 2. 5835 - 1. 8410	+ 16.9438	11-10	—1. 275	— o. 674
7— 4	+ 1.8419 + 0.7184	+ 3.7988 + 0.4055	1210	0. 755	+ 0.010
7— 4 8— 4	+ 0.7184 + 0.1398	+ 0.4055 - 0.0133			
9-4	+ 0.1398	— 0.0133 — 0.0140	911	+0.004	+ 0.099
10— 4	+ 0.0008	- 0.0031	11-11	—o. 378 ⊥o. 444	— o. 135
1		-	12-11	+0. 444 +0. 237	- 0.617 - 0.854
3— 5	+ 0.2732	— o. o770	12-11	70.23/	— o. 854
4 5	- 0. 2338	+ 4. 1548	10—12	o. o51	+ 0.011
5— 5	— 22. 1066	12.6478	11-12	+0.015	— o. 248
6— 5	— 12.5826	+ 0.4445	12—12	+0.402	+ 0.114
7 5	— 2.9 72 1	+ 2.0845			
					1

The expressions for the factors C', D', E', and H' are:

$Arg = \varkappa \gamma' + i'g' + ig$		C'	Г) [']	E	,	F	I'
Alg_2/ +0 y +0 y	sin.	cos.	cos.	sin.	sin.	cos.	cos.	sin.
κ i' i ο ο ο	"	2. 2220	"	"	"	" + 0.981	u	"
-1 I o	0. 22	+ 1.66	+ 0.35	+ 2.61	+ 0.53	1.55	+ o. 85	- I. 63
—I 2 0	+ 3.98	+ 19.20	—20. 61	—14. 03	— 6. 16	+ 4.17	+12.91	+ 8.62
0 1 0	8. 0924	— 38. 56o2	+ 9.296	+ 6.423	+ 9.297	6. 422	+23.605	+16.862
100	+ 4.0750	+ 19.2066	+ 8.30	+ 5.60	— 6. 22	+ 4.40	43. 03	—31.24
-r 3 o	+ 2.02	+ 3,04	— 3⋅74	— 7. 27	— o. 84	+ 1.50	+ 2.64	+ 6.66
0 2 0	— 3. 92 80	— 5. 5 262	+ 2. 247	+ 4.361	+ 1.124	2. 181	— o. 293	— 3. 182
IIO	+ 1.82	+ 1.96	+ 1.09	+ 1.73	— o. 31	+ 1.16	— 1. 38	 1.83
—I 4 0	+ 0,40	+ 0.26	+ 0.06	— 1.75	0, 00	+ o. 28	0. 17	+ 1.48
0 3 0	— 0. 7646	— o. 4272	- 0.025	+ 1.171	— o, oo8	— o. 390	+ o. 181	0.973
I 2 0	+ 0.34	+ 0.08	+ 0.03	+ 0.35	+ 0.06	+ o. 16	— o. o5	0.29
— 1 5 о	+ 0.06	0, 00	+ 0.10	— O. 25	+ 0.02	+ 0.03	o. II	+ 0.21
0 4 0	— o. o998	— 0. 0042	— 0. 109	+ 0, 189	0.027	- o. o47	+ 0. 105	— o. 147
1 3 0	+ 0.04	0.00	+ 0,04	+ 0.03	+ 0.02	+ 0.01	0.02	o. o5
—I 6 о	+ 0.02	0.00	+ 0.02	— o. oı			— o. o2	+ 0.01
—I— 2— I	0.00	— 0. O2	- 0, 04	+ 0.04	0, 01	— o. oı	+ 0.08	o, o6 _
o 3 1			o. o95	+ 0.028	+ 0.032	+ 0.009	0.054	+ 0.013
1—4—1	1		+ o. 14	— o. o9	0.02	— o. oı	- o. oi	+ 0.03
—I— I— I	0.00	0,00	o. 39	— o. 10	O. IO	- 0.02	+ 0.60	+ 0.03
0 2 1	+ 0.0140	+ 0.2504	o. 532	- O. IIO	+ o. 266	— o. o55	— o. 217	- o. 175
I— 3— I	0.00	- o. 16	+ 1.05	+ o. 23	— O. 20	+ 0.04	— o. 28	+ 0.09
—ı o— ı	+ 0.08	+ 0.38	— 2. 28	- 2.05	— 1.66	+ 2.09	+ 0, 84	+ 4.63
o I I	+ 0.7236	+ 3.6308	— 1.657	— 1.355	+ 1.657	— I. 355	+ 1.388	- 2, 805
I— 2— I	0.44	- 2.12	+ 4.48	+ 3.84	o. 99	+ 0.67	— 2.7I	— o. 90
—I I— I	— 23. 2404	— 110. 8630	—14. 09	—31.76	+ 7.71	-16.98	+ 7.21	+16.18
0 0— 1	+ 28. 0898	+ 133. 3682	0,000	0.000	11.681	+25. 334	0,000	0.000
I I I	- 11.00	51.84	+13.98	+31.76	+ 7.89	-16.97	— 7. o3	16. 24
—ı 2 — ı	+219.72	+1046.56	+ 3.61	— 4. 00	+ 1.41	+ 0.96	- 4.04	+ 2.62
o I— I	<u>-438. 3416</u>	—2101. 1468	— 1. 586	+ 1.440	— 1. 586	— I. 440	+ 3.663	+ 0.774
1 — 0 — 1	+219.44	+1053.90	I. IO	+ 1.70	+ 0.46	+ 2.10	1.46	- 3.07
—ı 3— ı	14.42	+ 78.24	<u>—16. 02</u>	+15.91	- 3. 30	— 3. 3 1	+22.70	-21.73
O 2- I	+ 35.4446	— 127. 7548	+10.203	—IO. 000	+ 5. 102	+ 5.000	—15. 996	+15.204
I I I	— 2 6. 9934	+ 19.8396	+ 2.56	- 2.59	— 3.50	- 3.42	— 1.49	+ 1.56
—I 4— I	5.56	+ 7.96	8.89	+ 2.51	— I. 43	- 0.45	+10.49	- 2.70
o 3— I	+ 10.9366	- 13. 1390	+ 6.295	— I. 795	+ 2.099	+ o. 598	7· 947	+ 2. 106
I 2 I	- 4. 88	+ 3.30	+ 0.93	— o. 47	— 1.16	— o. 17	- 0.55	+ 0.45
—ı 5— ı	o. 68	+ 1.26	- 2. 23	— o. 55	0. 30	+ 0.04	+ 2.31	+ 0.62
0 4 1	+ 1.2096	2.0368	+ 1.688	+ 0.382	+ 0.422	- 0.096	1.830	0.468
1 3— 1	— o. 34	+ 0.68	+ 0.21	— o. oɪ	— o. 18	+ 0.08	— o. 17	+ 0.06
- т 6 т	o, o6	+ 0.14	— o. 36	- o. 33	- 0.04	+ 0.03	+ 0.34	+ 0.28
o 5 1	+ 0.0442	— o. 2830	+ 0. 264	+ 0. 236	+ 0.053	- 0.047	— 0. 252	— 0. 24I
I 4— I	— 0. O2	+ 0.10	+ 0.05	+ 0.03	0.02	+ 0.03	0.06	+ 0.02
—ı 7— ı	- 0.02	+ 0.02	o. oi	- 0.04			+ 0.01	+ 0.04
о 6— г			+ 0.020	+ 0.059			0.016	0.055
r 5— r	0.00	- 0,02	0,00	— o. o3]	+ 0.00	+ 0.03

Arg-world it all time	c	,	п)′	Œ	,	Н	[′
$Arg = \varkappa \gamma' + i'g' + ig$	sin,	cos.	cos.	sin.	sin.	cos.	608.	sin.
ж i' i	"	"	"	11	,,	"	"	"
—I— I— 2	0,00	+ 0.02	0,00	+ 0.03	0.00	0, 00		
0— 2— z			- 0.003	+ 0.030	+ 0.001	+0.015		
1— 3— 2	0.00	— 0. O2	0.00	— o, o6	0.00	o. or		
—I O— 2	+ 0.04	+ 0.08,	+ 0. 10	+ 0. 26	— o. o8	+0.13	- o. o3	— o. 16
O I 2	— o. o464	+ 0.1886	- 0.072	+ 0. 108	+ 0.072	+o. 108	+ o. 137	— o. o68
I — 2— 2	+ 0.06	0. 14	+ 0.02	— o. 40	— 0, 04	-o. II	o. 17	+ 0. 26
—I I— 2	- 2.08	— 10. 42	— 2. 32	+ 0.21	+ 1.01	—2. 8o	+ 1.39	I. OI
0 0 2	+ 1.4308	+ 11.0004	0,000	0.00	- 0.729	十4.353	0, 000	0.000
i- I- 2	— o. 18	— 3.88	+ 2.74	— O. 29	+ 0.39	—2. 92	1.64	+ 1.07
—I 2— 2	+ 21.74	+121.46	—24. 82	+ 5.32	— 7· 34	—1. 72	+18.24	— 3. 9 9
0 I— 2	59. 3036	-236. 9464	+11.139	2. 407	+11.137	+2.407	7.078	+ 1.707
I 0 2	+ 32.30	+117.62	+10.07	- 2.00	— 7·49	-1.40	8.87	+ 1.64
—I 3— 2	+186.28	— 69. 44	- 6.47	— 5. 18	— 1.51	+1.14	+ 5.25	+ 4. 13
0 2— 2	-374. 2492	+146.0158	+ 3.908	+ 2.986	+ 1.954	—ı. 493	— 2. 908	- 2.033
I I 2	+186.18	— 78. <u>5</u> 6	+ 1.41	+ 0.72	0.76	+1.08	I. 22	o. 71
—I 4— 2	+ 30.54	— 45.48	+ 9.44	+14.30	+ 1.48	-2. 24	—13. <u>99</u>	22. 50
0 3— 2	— 55. 7896	+ 89.9812	— 6. 7 93	—10. 486	— 2. 237	+3.495	+10.899	+17.946
1 2— 2	+ 19.98	— 42. 10	— o. 26	— 0.45	+ 1.60	2. 42	— o. 63	— 1.19
-ı 5— 2	— 0, 14	— 10. 18	+ 0.71	+ 8.65	+ 0, 12	—I. I4	0.67	—11.39
0 4— 2	+ 1.3874	+ 19.1238	— o. 527	6. 755	— o. 132	+1.689	+ o. 538	+ 9.408
I 3-2	- 2.00	— 7. 6 4	- 0. 24	0.09	— 0. O2	0. 97	+ 0.32	- 0.43
—I 6— 2	— 0.94 00	— I. 30	1.05	+ 2.31	0. 11	—0. 2 7	+ 1.32	2.64
0 5-2	+ 1.8718	+ 2.2764	+ 0.835	— I. 862	+ 0. 167	+0.372	I. 077	+ 2. 254
I 4— 2	- 0.96	— o.68	0.06	0.09	— O. I2	—о. 17	+ 0.11	- o. or
—I 7— 2	— o. 18	0.08	0.46	+ 0.33	- 0.04	o. o3	+ 0.46	— 0. 33
0 6— 2	+ 0.3954	+ 0.1144	+ 0. 372	— o. 279	+ 0.062	+0.047	0. 422	+ 0. 297
I 5— 2 —I 8— 2	— 0. I4	- 0.04	- 0.01	- 0, 02	0.03	-0.01	+ 0.06	+ 0.01
	- 0.04	- 0.02	— 0. 07	+ 0.01	— o. or	0.00	+ 0.06	— o. oı
0 7— 2 1 6— 2	+ 0.0508 0.00	— o. o164	+ 0.089	- 0.012	+ 0.013	+0.002	- 0.092	+ 0.009
o 8— 2	0.00	0.00	— o. o3	0.00	— o. oı	0,00	+ 0.04	0, 00
1	1						0.014	— o . 006
-ı o 3	0. 00	+ 0.04						
0-1-3			+ 0.005	+ 0.003			+ 0.016	— o. oo8
1-2-3	0.00	- 0.02						
—I I— 3	- 0.20	— o. 86	+ 0. 10	+ o. o6	+ 0.11	-O. 2I	— o. o7	— o. o5
0 0-3	+ 0.1656	+ 0.8434	0.000	0.000	— o. 166	+o. 357	0.000	0,000
1- 1- 3	- 0.04	— o. 28	— o. 10	— o. 10	+ 0.11	0. 25	+ 0.07	+ 0.08
—I 2— 3	+ 1.86	+ 10.12	+ 0.22	+ 1.30	— o. o5	-0, 02	O. I 2	— o. 98
o 1 3	— 4. 4400	— 20. 1 678	+ 0.096	— o. 553	+ 0.096	+0.554	o. o66	+ 0.351
1 o- 3	+ 2.38	+ 10.12	— o. 34	— I. II	0.06	o. 42	+ 0.20	+ o. 86
—ı 3— 3	+ 3.86	— 7.50	+ 0.20	+23.54	+ 0.09	4. 87	— о. 16	—16. o4
o 2 — 3	- 14. 5410	+ 5.9098	— o. o68	—14. 8o7	— o. o34	+7.405	+ 0. 0305	+ 9. 186
1 1-3	+ 8.32	- 1.80	+ 0.06	— 3.98	+ 0.01	-4.93	+ 0.02	+ 3.94
—ı 4— 3	+ 78.80	+110.42	6. 57	+ 7.31	— 1.09	—I. 27	+ 5.05	- 5.79
0 3— 3	—161. 27 66	—222. 5100	+ 4.448	- 5. 196	+ 1.483	+1.732	— 3.016	+ 3.902
I 2— 3	+ 80.90	+111.56	+ 0.31	o. 8o	o. 97	o. 8o	— o. 44	+ 0.71

. ,,,,,,	C	,	D'		E	′	Э	[/
$Arg = \varkappa \gamma' + i'g' + ig$	sin.	cos.	cos.	sin.	sin.	cos.	cos.	sin.
$ \begin{array}{cccc} & n & i' & i \\ & -1 & 5 - 3 \end{array} $	+ 45.04	,, + 19.60	+10.75	., -4. 21	+1.35	// + o. 53	" —18. 45	" + 6.60
0 4— 3	— 88. 7194	- 35. 9720	— 8. 494	+3.219	-2. 123	—o. 8o5	+15.720	5. 424
ı 3— 3	+ 41. 10	+ 13.26	+ o. 54	—о. 30	+1.50	+o. 62	- 2.32	+ o. 82
—ı 6— 3	+ 10.94	- I. 60	+ 7.29	+0.92	+o. 81	o. o8	—10. <u>3</u> 6	- 1.51
o 5— 3	20, 6194	+ 4.0212	— 5· 973	—о. 756	1.195	+0. 151	+ 8.906	+ 1.326
I 4— 3	+ 8.42	 2.84	+ 0.31	+o. 15	+0.70	-0.14	— о. 87	o. 43
—ı 7— 3	+ 1.52	— 1.30	+ 2.07	+1.40	+0. 20	—о. 13	- 2.43	— I. 90
o 6— 3	— 2.6574	+ 2.6124	— 1.685	—1. 208	—o. 281	+0. 201	+ 2. 197	+ 1.653
1 5— 3	+ o.88	— 1.24	— o. o3	+0.17	+0.13	— 0. 12	o. 17	— o. 23
ı 8 3	+ 0.08	— o. 32	+ 0.21	+o. 58	+0.02	o. o5	0. 29	o. 61
o 7— 3	— 0, 1210	+ 0.5698	— o. 228	— 0. 476	-o. o33	+o. o68	+ 0. 259	+ 0.582
ı 6 3	0.00	- 0, 24	+ 0.03	+0.01	+0.01	-0.04	+ 0.03	o. io
—ı 9— 3	0, 00	— o. o6	0,00	+o. o8	0.00	0. 01	+ 0.01	o. Io
o 8— 3	+ 0.0300	+ 0.0778	+ 0.907	O. II2	+0.001	+0.014	- 0.012	+ o. 125
I 7— 3	0.02	0.02	o. oi	+0.04	0.00	o, oı	+ 0.02	0.04
0 9— 3	+ 0.0092	+ 0.0068					— o. o13	+ 0.018
	0, 02	0.06			+o. o1	o. or		
—I I— 4	- 0.02	- 0.00	0.000	0.000	-0. 012	+0.022	0.000	0.000
0 0-4	+ 0.02	— 0. O2	0.000	0,000	+0.01	O. OI	0.000	0,000
I— I— 4		_	+ 0.08	<u> </u>	0.00	+0.01	— o. o5	+ 0.05
—I 2— 4	+ 0.14	,	— 0. 014	0.001	0.014	+0.001	+ 0.008	+ 0.002
0 I— 4	- 0.3170 + 0.16	- 1.5314 + 0.78	— 0.014 — 0.09	+0.04	+0.01	0.00	+ 0.05	o. o3
1 0-4	+ 0.16 - 0.06		+ 0.55	+0.64 +0.64	0.08	0. 16	0. 37	0.49
-1 3-4			- 0. 387	0. 5 97	o. 193	+0. 297	+ 0. 228	+ 0.380
0 2-4	0.4270 +- 0.26	+ 0.3300 - 0.08	— 0. 307 — 0. 53	+0.06	+0.17	-0. 21	+ 0.37	+ 0.05
I I— 4		+ 2.34	+18.52	+3.74	+2.91	o. 57	11.93	- 2.47
-I 4-4	+ 9.38 - 13.9576	— 10. 1730	—13. 356	-2. 842	-4.452	+0.947	+ 8.037	+ 1.743
0 3-4	+ 6. 16	+ 6.04	o. 88	o. 17	+2.97	-o. 63	+ 1.34	+ 0.32
I 2— 4	— 56.78	+ 62.94	+ 6.27	+7.30	+0.87	— 0. 98	— 4. 94	— 5. 5 1
-I 5-4 0 4-4	+114.3794	—128. 8768	— 4. 915	-5. 487	-1. 229	+1.372	+ 3.749	+ 3.748
1	- 57. 56	+ 64.72	— o. 18	+0. 14	+0.61	_o. 87	+ 0.19	+ 0.13
1 3— 4 —1 6— 4	- 8. 30	+ 37.36	1.09	-6. 93	o. 10	+0.71	+ 1.62	+13.25
0 5—4	+ 14.7968	— 73. 72 06	+ 0.763	+5.729	+0. 153	—1. 146	— 1. 289	—11. 745
1 4-4	- 4.94	+ 34. 24	- o. 16	o. 77	o. 16	+o. 8 ₃	+ o. 31	+ 2.30
—I 7— 4	+ 3.20	+ 9.70	+ 1.84	5 ⋅ 37	+0.17	+0.50	2. 97	+ 8.07
0 6-4	6. 7892	— 18.4008	— r. 584	+4. 553	—o. 264	— 0. 759	+ 2.677	— 7. 182
1 5-4	+ 3.76	+ 7.62	+ 0.26	-0.44	+0.19	+0.45	— o. 59	+ 1.03
—I 8— 4	+ 1.62	+ 1.40	+ 1.62	—I. 52	+o. 13	+0.13	— 2. 2 <u>5</u>	+ 1.93
0 7-4	_ 3. 1668	- 2. 4336	1.394	+1.288	_o. 189	—o. 184	+ 2,004	- I. 770
1 6-4	+ 1.42	+ 0.78	+ 0.16	_0, O2	+0.12	+0.08	- o. 31	+ 0.14
—I 9— 4	+ 0.36	+ 0.06	+ 0.53	0. 12	+0.04	+0.01	— 0.70	+ 0.18
0 8-4	- 0.6972	— o. o63o	- 0. 521	+0.131	-o. o65	o. o16	+ 0.676	_ o. 152
1 7—4	+ 0.28	0, 00	+ 0.12	-0.01	+0.03	0.00	_ O. I2	0.04
-I IO- 4	+ 0.06	0.00	+ 0.08	+0.02	+0.01	0.00	— o. 11	— o. o3
0 9-4	— o. o978	+ 0.0514	— O. I2O	-o. o32	0.013	+0.004	+ 0.143	+ 0.043
1 8— 4	+ 0.02	- 0.02	+ 0.06	+0.03	+0.01	0.00	o. o6	- 0.04
0 10-4	- 0.0084	+ 0.0142	- 0.018	-0.017			+ 0.020	+ 0.021
+			l		<u> </u>		<u> </u>	

Amos / 1 2/-/ 1 5	C		I)′	E	2'	H	[′
$Arg = \varkappa \gamma' + i'g' + ig$	sin.	cos.	cos.	sin.	sin.	cos.	cos.	sin.
и i' i —I 2— 5	0.00	+ 0.06	11	"	"	"	"	"
0 I— 5 I 0— 5	0, 00	+ 0.06						
—I 3— 5	- 0.02	— 0. O2	-0.02	— o. o3				
0 2-5			-0.002	0.010				
I I 5	0.00	0,00	-0.01	+ 0.06				
-1 4 5	+ 0.54	O. I2	+0.98	+ 0. 22	+0.14	O. 12	o. 65	—о. 16
o 3— 5	o. 9300	— o. 2480	—о. 854	— o. o62	0. 285	+0.021	+0.519	+0.043
I 2 5	+ 0.40	+ 0.20	-o. oı	+ 0.23	+0. 20	10.0+	+0.05	<u>—0. 12</u>
—ı 5— 5	0. 40	+ 8.28	+5.63	—12.61	+0.70	+ 1.61	—3. 58	+ 7.89
o 4— 5	+ 4.7286	—14. 4744	<u> </u>	+ 9.828	—1.126	2. 457	+2.704	5⋅779
I 3 5	— 3. O2	+ 6.88	+0.14	— o. 37	+o. 75	+1.65	+0.13	—o. 27
—ı 6— 5	44. 18	24. 80	+7.22	— 4· 34	+0.81	+o. 51	-5.36	+3.48
0 5 5	+90, 6290	+49.8034	<u></u> 5. 765	+ 3.652	—I. 153	—o. 731	+3.984	—2. 863
I 4— 5	—45.60	25. 16	+0.43	— o. 15	+0.71	+0.38	o. 15	+0.09
—I 7— 5	—27. 6o	— o. 50	3⋅74	0.40	0. 32	+0.05	+8.44	+0.92
o 6— 5	+54-5440	0.0498	+3.214	+ 0.412	+0.536	0.074	-7.710	—0. 964 Lo. 16
1 5 5	-25.44	+ 1.14	o. 67	+ 0.04	0.40	+0.02	+1.83 +5.57	+0.16 +3.56
—ı 8— 5	7.50	+ 4 14 - 8. 4236	-3.47	— 2. I4	—0. 30	+0. 17 0. 274	+5·57 -5.064	+3.30 −3.246
o 7— 5 I 6— 5	+14. 2560		+3.017	+ 1.917	+0. 431 0. 26	-0. 274 +0. 18	+o. 86	+0.67
I 6 5	— 5.94 — 1.00	+ 4.24 + 1.72	0. 40 0. 87	— 0. 35 — 1. 56	—0. 20 —0. 07	+0.11	+1.27	+2.28
0 8-5	+ 1.8064	- 3. 3740	+0.822	+ 1.374	+0. 103	0.172	—1. 176	-2.065
1 7—5	— o. 60	+ 1.48	—0. I2	— o. 17	-0.05	+0. 10	+0.11	+0.34
—I IO— 5	- 0.04	+ 0.40	+0.01	— o . 60	0, 00	+0.04	_0. 0I	+0.71
0 9-5	— o. o46o	- o. 7472	+0. 022	+ 0. 502	+0.002	—o. o56	0.014	—o. 683
I 8-5	+ 0.04	+ o. 30	0,00	— o. o3	0.00	+0.03	-o. oı	+0. 12
-I II- 5	+ 0.02	+ o. o6	+0.04	— o. og	0.00	+0.01	o. o5	+0.12
0 10 5	— o. o736	— o. 1074	o. o56	+ 0. 114	-o. o o6	-o. oi i	+0.075	0. 143
I 9— 5	+ 0.04	+ 0.02	+0.04	o. o5	0.00	+0.01	o. o <u>5</u>	+0.06
o 11— 5	0.0198	— o. o104	0.023	+ 0.016	-0.002	-0.001	+0.028	-o. o18
—I 4— 6	+ 0.08	— o. o6	+0, 01	+ 0.04	0.00	-o. oı		
o 3— 6			—о. озз	— o. o19	o. o1 1	+0.006	+0.020	+0.012
I 2— 6	+ 0.04	0,00	+0.01	+ 0.01	+0.01	0.00		
-ı 5— 6	+ o. 28	+ 0.54	+0.74	— o. 83	+0.14	+0.09	0, 44	+o. 58
o 4— 6	— v. 0416	1.0256	-0.452	+ 0.793	0. 113	—0. 198	+0. 271	0. 470
I 3— 6	- 0.02	+ 0.52	+0.09	— o. o3	+0.07	+0.14	o, o6	0, 04
—1 6— 6	6. 26	+ 0.96	—7. 64	5.69	o. 81	+0.60	+4.63	+3.50
0 5 - 6	+11.9066	+ 0.5800	+6. 203	+ 4.779	+1, 241	-0.956	3. 565	-2.824
1 4— 6	_ 5.88	— 0.72	—o. 58	- 0.46	0.84	+0.64	+0.08	+0.12
— 1 7— 6	+ 8. 22	-28. 22	2.46	- 6.42	-0. 24	+0.61	+2.00	+4.72
0 6 6	—16. 2212	+58.0064	+2.129	+ 5.316	+0.355	o. 886	-1.716	—3. 748
1 5 6	+ 8.30	-29. 26	-0.13	— o. 56	0. 17	+0.55	+0.10	+0.35
—r 8— 6	- 3.58	-18.54	0.67	+ 1.61	0.06	-0.11	+1.74	—4· 74
0 7—6	+ 7.7240	+36.7056	+0.685	1.403	+0.098	+0.200	—1. 746	+4. 479
ı 6 6	— 4. 28	<u> </u>	-0.11	+ 0.41	—o. o5	—0. 17	+0.42	—I. 27

	C ′		\mathbf{D}'		\mathbf{E}'		\mathbf{H}'	
$\mathbf{Arg} = \varkappa \gamma' + \mathbf{i}'g' + ig$	sin.	cos.	cos.	sin.	sin.	cos.	cos.	sin.
и i' i	"	11	11	11	"	"	"	"
— i 9— 6	4. 30	5. 10	—1 .91	+2.01	0. 13	-o. 15	+3.41	3.36
n 86	+ 8.6196	+ 9.7602	+1.725	—1.775	+0. 216	+0.222	-3. 203	+3.094
1 7—6	— 4. 14	— 4. 10	0. 32	+0. 29	0. 14	o. I4	+0.74	0. 59
—1 10— 6	— 1.66	— o. 62	—I. 37	+0.45	-0.09	о. оз	+2.02	0. 62
0 9 6	+ 3.2108	+ 1.0384	+r. 200	0.410	+o. 133	+0.046	—1. 882	+0.598
r 8— 6	— I.44	→ 0.30	—0. 15	+0.05	o. o8	-0.02	+ 0. 36	o. o8
—I II— 6	— o. 36	+ 0.04	-o. 52	—0. I2	0.03	0, 00	+0.63	+o. 14
o 10— 6	+ 0.7100	— 0. 1642	+0.434	+0.070	+0.043	-0.007	-o. 615	0. 114
1 9 6	o. 3o	+ 0.12	-o. oı	0.00	0. 02	0.00	+o. 11	⊹0.04
—I I2— 6	— o. o6	+ 0.06	0. 05	0.0 5			+0.10	+0.07
o 11—6	+ 0.0996	o. o982	+0.096	+0.074			<u>—0. 125</u>	-0. IO2
1 10— ¹ 6	- 0.02	+ 0.06	0. 05	-o. o5			+0.04	+o. o6
0 12 6							0.014	— о. 034
— I 5— 7	+ 0.02	+ 0,02	+0.05	0.00	+0.02	0.00		
0 4 7	·		0, 046	+o. o35	-0.011	-0.009	+0.027	0.021
I 3— 7	+ 0.02	+ 0.02	+0.03	-0.02	+o. o1	+0.01		
—ı 6— 7	— 0.42	+ 0.34	0. 52	о. 83	-0.04	+o. 12	+0.36	+0.51
o 5— 7	+ 0. 9088	o. 3226	+0. 555	+0.651	+0.111	0. 130	0. 322	—0. 382
1 4 7	— o. 44	+ 0.12	-0.07	о. 18	o. o8	+0.08	-o. o3	+o. o8
—ı 7— 7	— 1.62	— 4. 22	4.81	+3.98	0. 43	о. 36	+2.87	— 2. 36
0 6— 7	+ 1.7330	+ 8.4592	+4. 150	—3. 363	+0.691	+o. 5 60	-2.419	+1.879
1 5-7	— o. 62	— 4.24	-0. 5 4	+0.49	— 0. 46	о. 38	+ 0. 24	о. 13
—ı 8— 7	+16.66	+ 0.78	5. 11	+0.90	—0. 44	— 0. 08	+3.73	0. 81
o 7— 7	 34. 30	— I. 25	+4.426	—o. 772	+o. 632	+0.110	3. 114	+o. 7 87
ı 6— 7	+17.36	+ 0.74	о. 67	-o. o3	0.40	0.04	+0.42	-o. Io
—ı 9— 7	+11.44	— 4.88	+o. 31	+0.51	+0.02	-o. o3	—2. 37	—I. 72
o 8— 7	22. 65	+10.12	— 0. 309	o. 505	—0. 039	+0.063	+2.253	+1.678
ı 7— 7	+10.66	— 5. 14	+0.23	+0.09	+0.06	o. o3	—о. 68	о. 39
—ı 10— 7	+ 3.04	— 3.88	+1.02	+1.55	+0.06	—0. 10	—1.78	—2. 83
0 9—7	 5. 87	+ 7.73	o. 874	—I. 367	0.097	+0.152	+1.664	+2.647
1 8— 7	+ 2.46	— 3. 70	+0.14	+0. 22	+0.06	0. 10	0. 35	—о. 59
-I II 7	+ 0.24	1.44	+0.20	+1.11	+0.01	o. o6	—0. 15	— 1.66
o 10— 7	— o. 38	+ 2.78	-o. 11o	 0. 948	0.011	+0.095	+0.150	+1.546
ı 9— 7	+ 0.08	— I. 24	o. o8	+0.09	+0.01	o. o <u>s</u>	0.00	-o. 32
—I I2— 7	o. o8	— o. 32	0.09	+0.42	-o, oi	0.02	+ 0. 24	+0.15
o II— 7	+ 0. 2596	+ 0.6148	+0.131	0. 340	+0.012	+0,031	0. 205	—o. 500
1 10 7	0. 14	o. 26	—0. 10	+0.01	0.01	-0.02	+0.04	+0.57
—I I3— 7	— o. o6	o. o6	-o. o5	+0.05			+0.08	0.05
o 12— 7	+ 0.1208	+ 0.0774	+o. o83	-o. 07 I			—0. I2I	+0.100
1 11-7	0.04	0.04	0.04	+0.04			+0.07	0. 07
— 1 6— 8	— o. o4	+ 0.06	+0.01	0. 05	+0.01	+0.01		
o 5—8			+0,022	+0.064	+0,004	-o. o13	0.013	—o. o37
ı 4—8	— 0.02	+ 0.02	-0. OI	-0.04	0, 00	+0.01		
_r 7— 8	— o. 36	— 0. 28	o. 85	+0.21	-o. o8	0.01	+o. 51 ·	—o. 13
6 6— 8	+ 0.4538	+ o. 6688	+o. 668	—0. 286	+0.111	+0.048	—о. 386	+0.162
r 5—8	— о. 18	— o. 36	-0. 11	+0.05	0.07	-o. o3	+0.04	0.02

$Arg = \kappa \gamma' + i'g' + ig'$	C′		\mathbf{D}'		\mathbf{E}'		Ħʻ	
	sin.	cos.	cos.	sin.	sin.	cos.	cos.	sin.
arkappa = i' - i	"	"	"	"	11	"	- 11	"
—ı 8— 8	+2.55	— 1.67	+1.75	+3.55	+0. 15	0. 28	o. 95	2. 24
0 7—8	—5. 318	+ 2.562	—1.484	-3. 153	-o. 213	+0.450	+o. 788	+1.812
ı 6—8	+2.71	— I. I2	+0.25	+0.54	+o. 16	— 0. 30	-o. 11	o. 26
ı 9 8	+1.8o	+ 9.11	+0.09	+3.80	0.01	0. 28	o. 11	+0.50
o 8—8	—3. 95 0	— 18. 796	+0.060	-3. 322	+0.007	+0.415	+0.107	—2. 379
ı 7—8	+1.91	+ 9.55	-0. 24	+0.51	-0.02	-o. 26	+0.05	+2.72
—1 10—8	+4.59	+ 6.46	0.00	+o. 13	+0.01	-0.02	—1.2 8	+o.89
o 9—8	9. 462	-12. 820	-0, 199	-0. 204	-0, 022	+0.023	+1.258	-0, 923
ı 8 8	+4.68	+ 6.03	+0.23	+0.03	+0.01	0.00	o. 31	+0. 24
—ı ıı— 8	+3. 152	+ 1.554	+0.32	—o. 68	+o. o6	+0.02	2. I2	+v. 72
o 10— 8	6. 282	3.010	— 0. 956	+0. 323	—o. og6	-0.032	+1.998	—о. б93
1 9 8	+2.96	+ I. 24	+0.93	+0. 25	+o. o6	+0.02	-o. 45	+0.20
—I I2— 8	+1.11	0.04	+0.22	-o. 18	+0.04	0.00	1.28	-o. o6
o 11—8	2. 220	+ 0. 122	—о. 683	0. 071	o . 062	+0.006	+1.162	+o. 138
1 10—8	+0.99	— o. 13	+0.66	+0.29	+0.04	0.00	1 9	—о. 13
—I I3— 8	+0.26	o. 16	+0.05	+0.09			o. 41	o. 17
o 12—8	—o. 472	+ o. 332	—о. 2 42	—о. 158	-0, 020	+0.013	+0.392	+o. 261
1 11 8	+0. 19	— o. 15	+0.25	+0.11			o. o7	—о. 16
—ı 7— 9	0. 04	o. oı	0. 04	-0. O2				
0 6 9			+0.067	0,002	+0.011	0,000	—o. o39	+0.001
15-9	0. 02	0.04	0. 04	0.00				
—ı 8— 9	+0.15	o. 30	0, 02	+0.66	0.00	0.05	o. o8	o. 54
o 7— 9	0, 400	+ 0.502	-o. o73	—o. 569	-0.010	+0.081	+o. o38	+o. 326
1 6— 9	+o. 21	— O. 2I	+0.04	+0.12	+0.01	o. o5	+0.07	+0.09
—ı 9— 9	+1.44	+ 1.40	+2.36	o. 45	+0.17	+0.03	—I. 23	+0.39
o 8— 9	—2. 490	3.018	—2. 15 8	+0.417	0. 270	-0.052	+1.221	—о. 184
1 7-9	+1.16	+ 1.58	+0.44	0. 15	+o. 18	+0.03	—о. 33	-0. 12
1 10 9	-4. 61	+ 2.19	+2.54	+0.51	+o. 17	0. 04	-1.52	+0.43
0 9—9	+9.514	- 4.722	—2. 303	—о. 536	o. 256	+ 0. 060	+1.671	+o. 278
18—9	4. 82	+ 2.34	+0.44	+o. 21	+o. 16	-0.04	—о. 68	0. 85
—I II— 9	 3. 306	+ 3.732	+1.19	+0.22	+0.02	0.00	+o. 66	+1.13
0 10—9	+6.502	 7. 568	— 0. 354	-0.061	o. o35	+0.006	—о. 232	—0. 7 90
1 9— 9	3. 06	+ 3.69	о. 83	—о. 14	+0.01	0, 00	o. 31	0. 13
—I I2 — 9	-0. б2	+ 2.38	+0.48	-0.52	0.00	+0.04	+0.72	+o. 95
0 11—9	+1.114	- 4.718	+o. o38	+o. 5 93	+0.004	-0.054	—0. 139	—1. 378
1 10 9	— 0. 44	+ 2.19	—o. 57	o. 26	0.00	+0.04	— 0. 54	+0.81
—I I3— 9	+o. 21	+ 0.84	+0. 22	0. 52	+0.01	+0.03	+o. o3	+0.41
0 12-9	0. 448	- I. 624	0. 152	+0.451	0.013	-o. o37	+0. 290	0, 896
1 11— 9	+0.24	+ 0.73	-0.02	o. o6	+0.01	+0.03	0.42	+0.74
—ı 8—ıo	+0.02	— o. o5	-0.02	+0.04				
0 7—10			+0.015	—o, o59			-0.009	+0.034
1 6—10	+0.04	0.04	0.02	+0.04				
—I 9—IO	+ 0. 26	+ 0.04	+o. 65	+0.01	+0.04	-0.01	O. 2I	+0.02
o 8—10	-0.402	— o. 175	o. 424	-o. o58	-o. o53	+0.007	+0. 240	+0.03 7
1 7—10	+0. 21	+ 0.13	0.09	+0. 12	+0.04	0.00	-0.11	o. o8

Ann / Li/a/ Lia	(D'	I) [']	1	e'	F	I'
$Arg = \varkappa \gamma' + i'g' + ig$	sin.	cos.	cos.	sin.	sin.	cos.	cos.	sin.
и i' i	"	"	"	11	11	"	"	11
—I IO—IO	-2.09	+1.09	—0. 15	— I . 39	+0.01	+0.09	-0.44	+0.39
o 9—10	+1.490	—1.96o	-o. 091	+1.346	0.010	-o. 149	—o. o 93	o. 745
1 8—10	-2. 21	+0.97	+o. 23	о. 35	+0.01	+0.10	+o. 35	+0.57
—ı ıı—ıo	—1. 8o	-2.07	0.00	—I. 27	+0.05	+o. 10	—о. 57	+0.79
0 1010	+3.786	+4.334	о. 699	+1.469	—о. 070	0. 147	+0.433	—1. o82
1 9—10	—1. 9o	-2. 24	+o. 93	—о. 63	+0.05	+0.09	-o. o3	+0.63
—I I2—I0	—2. 64	-1.41	o. o6	+0.03	+0.01	+0.02	+o. 10	+o. 55
o 11—10	+5.426	+2.874	—0. 216	+0.318	0.019	-o. o29	0, 420	—o. o59
I 1010	-2. 65	1. 37	+o. 33	—о. 39	+0.01	+0.01	+0.44	o. 51
—I I3—I0	— 1 . 69	-0.07	-0. I2	+0. 24			+o. 93	+o. 38
0 12—10	+3.264	+0.086	+0.320	+0.074	+0.027	-o. oo6	-1.100	—о. 076
1 11—10	— 1. 52	+0.03	0. 31	— 0. 33			+o. 53	—0. 28
					1			
—I 9—II	+0.04	-0.01	+0.02	+0.03	i			
o 8—11			—o. o45	—o, o26			+0.025	+0.015
1 7—11	+0,02	+0.02	+0.03	+0.02				_
-I IO-II	+0.06	+o. 18	+0.05	-0, 22	1		0. 18	+0.08
0 9—11	+0,076	-0.314	o. 118	+0. 283	0.013	—o. o31	+0.070	—0. 157
I 8II	0, 03	+0.14	+0. 15	-o. 15			+o. o6	+0.11
-I II-II	− 0. 77	-0. 25	о. 33	-o. 47	o. o5	+0.02	+0. 26	o. 11
0 10—11	+1.440	+0, 620	+0.763	+0. 267	+0.076	-0. 027	-0.410	—o. 179
1 911	о. 68	0. 33	o. 66	+0.15	-o. o5	+0.02	+0.28	+0.32
I 12 II	+o. 82	-1.23	0. 59	—о. 79	-o. o5	+0.04	+0.37	+0.13
0 11—11	—1.672	+2.584	+o. 855	+0.672	+0.078	-o. o61	0. 637	o. 43o
1 10—11	+0.93	—I. 3I	0. 54	o. o9	0.05	+0.04	+0.47	+0.46
—ı 13—11	+0.47	—1. 78	—о. 36	-o. 29			—0. 19	-0. 29
0 12—11	0. 922	+3.538	0. 230	+o. 275	+0.019	0. 023	+0.033	+0.518
1 11—11	+0.43	—1.69	+o. 10	0.04			+0.13	-o. 43
—I IO—I2	+0.03	+o. o1	+ 0. 03	-o. oı				
0 9—12	' ' '	' '	-0.029	+0.029			+0.017	-o. o16
I 8—12	0.00	+o. o1	+0.02	-0.02			1 0.027	0.010
_I II—I2	o. 118	+0.024	0. 10	o. 18			+0.02	+0.03
0 10—12	+0. 252	-0.008	+0. 171	+0. 126	+0.017	-0.013	0.091	-0.074
I 9—12	-0. 12	0.00	-0. II	-0. 02	1 0.7	5.513	+0.09	+0.08
I I2I2	+0.02	-0.49	+0.03	+0.32			+0.26	—о. 16
0 11—12	—о. 176	+0.918	+0.260	0.400	+0.024	+o. o36	-0. 176	+0.184
I IO-12	+0.11	—0. 46	—o. 34	+0. 21	0.004	1 0.030	-0. 170 -0. 02	o. o8
-I I3-I2	+0.81	+0. 19	—0. 34 —0. 09	+0.21			0.00	
0 12—12				-0. 21 -0. 367	+0.043	±0.020	o. o66	—0.04 —0.103
I II—I2	—1. 594 →0. 78	—o. 368 ⊥o. 33	+0.512		70.043	+0.030		+0. 103
1 1112	+o. 78	+0. 22	—o. 58	+0. 27			+0.07	—o. o9

The second factors of δT and $\delta T'$ have all been given except $\delta \frac{h}{h_0}$, $\frac{u_1}{\cos i}$, and the similar quantities for Saturn. To complete the matter of this chapter these are now given:

			<u> </u>	
Arg=i'g'+ig	8	$\frac{h}{h_0}$		<u>t1</u> 8 i
	008	sin.	cos.	sin.
i' i	<i>"</i>	"	11	"
0 0	+ 4.7195		0. 0090	
O I	— o. o38o	+0.1732	+0. 1248	+0. 2825
O— 2	+ 0.0074	0.0047	+o. o188	-0. 0226
o— 3	0, 0000	-0.0004	+0.0001	-0.0010
1+ 3	0,0001	+ 0.0004		
1+ 2	+ 0.0008	+0.0007	+o. oo6o	+0.0014
1+ 1	+ 0.0008	-0.0200	+0.1379	-0.0417
1 0	— o. 1638	+0.7967	+0. 1799	+0. 1231
ı— ı	0. 7887	+4.0498	+o. 0694	0.0304
I— 2	— o. 1611	—o. 1285	+0.4137	-o. o936
1 3	 0. 0076	0. 0085	+0.0104	-0.0101
I— 4	— o. ooo4	-0.0001	+0.0004	+0.0004
2+ I	+ 0.0011	0.0019	+o. oo88	+0.0179
2 0	— o. 1467	+0.0174	—0. 0150	+0.3003
2— I	—12. 3301	-2.9105	0. 0902	+0.0855
2 2	+12.6079	+5.4106	+0. 1290	+0. 2279
2— 3	+ 0. 1385	+0.3093	+0.0031	—o. 1350
2— 4	— o. oo23	+0.0124	0. 0022	-0.0048
2— 5	0.0001	+0.0004	0.0008	-0.0004
3+ 1	+ 0.0002	—o. 0001	+0.0029	-0.0011
3 0	— o. o178	— 0. 0064	+0. 0405	-0.0498
3— г	+ 1.8188	+1.5474	+o. o394	+0.0061
3— 2	+ 2.0702	+4. 3071	+0. 4384	+o. 6888
3-3	+ 3.5824	—5. 0503	+0.0752	0. 0068
3-4	+ 0. 2743	—υ. 0696	-0.0575	-0.0112
3— 5	+ 0.0123	+o. ∞35	0.0030	0, 0000
3— 6	+ 0.0004	+0.0003		1
4— 0	0.0015	-0.0012	+0.0051	-0.0011
4— I	+ 0.0446	+0. 1053	+0.0250	+0.0167
4— 2	— 0. 4062	+1.5885	+0.0124	+0.0564
4 3	+ 2. 3874	—о. 7898	—о. 3186	+0. 1250
4— 4	— I. 9577	—2. 1463	0. 0344	-0. 0220
4 5	- 0.0114	0. 1996	0.0125	+0.0254
4— 6	+ c. 0053	-0.0100	0.0009	+0.0011
4— 7	+ 0.0003	0.0003		
5 O	- 0.0001	-0.0002	0.0032	0.0079
5— I	— o. ooo8	+o. o o84	0. 0710	0. 1649
5— 2	+ 5.5593	 4. 2341	+o. oo38	+0.0002
				·

Arg=i'g'+ig	δ	$\frac{h}{h_0}$	u co	8 i
	cos.	sin.	cos.	sin.
i' i	11	"	"	"
5— 3	+0.6908	+0. 2297	+3.5980	+0. 3498
5 4	-0. 2121	—1. 3907	+o. 1867	+0. 1039
5— 5	1. 2071	+o. 690 5	—о. 0066	+0.0140
5 6	—0. 1285	—o. o185	+0.0100	+o. oo88
5 7	0.0070	—o. oo57	+0.0010	+0.0010
5— 8	0.0003	—o. ooo6		
6— 1	o. ooo5	+0.0003	0, 0000	0, 0010
6— 2	+ 0. 0306	0.0005	+0.0030	0.0005
6 3	+0. 1202	+0.1707	+o. o188	+0.0102
6— 4	+0. 1892	o. 3905	-0.0223	+0.0698
6 5	0. 7940	0, 0282	+0.0315	+0.0054
6 6	+ 0. 1948	+0. 6441	+0.0051	+0.0100
6— 7	-0. 028I	+0.0760	+0.0050	-0.0041
6— 8	o. oo53	+0.0040	-0.0011	0.0000
6 9	—0. 0005	+0.0002		
7 2	+0.0015	+0.0009	+0.0024	+0.0010
7— 3	0, 0004	+0. 1008	+0,0009	+0.0004
7— 4	+0.0990	-o. o557	o. o435	+0.0553
7— 5	-0. 2214	—о. 1557	+0.0216	+o. o161
7 6	—o. 1033	+0. 4354	+o. oo48	—o. o124
7— 7	+0. 3269	0. 0200	+0.0067	-0. 0017
7— 8	+0. 0405	+0.0260	-0.0010	—o. oo26
7 9	+0.0018	+0.0041	i	
7—10	+0.0003	+0.0004		
8 2	0.0000	+0.0003		
8— 3	+0.0056	-0.0092	+0.0002	0.0002
8— 4	+0. 0293	+0.0021	+0.0086	0. 0030
8 5	0. 0272	о. 0686	+0.0076	+0.0112
8— 6	—0. 120 <u>5</u>	+0.1199	+o. oo86	o. oo86
8 7	+0. 2271	+0. 1063	- -0. 0045	0. 0034
8— 8	+0. 0283	—o. 1572	0,0000	+0.0033
8 — 9	+0,0200	0.0201	0.0017	+0,0006
810	+0.0029	0. 0006		
8—11	+0.0002	+0.0002		
9— 3	+o. ooo6	-0.0001		
9— 4	+0.0077	+0.0057	+0.0002	-0.0001
9— 5	+0.0038	-o. o181	— 0. 0003	+0.0066
9— 6	—o. 0485	+0.0107	+0.0059	0.0019
o 7	+0.0591	+0.0876	0, 0030	—o. ∞51
9— 8	+0.0845	-0.1111	-0.0018	+0.0013
9— 9	0.0709	-o. o323	-0.0011	0.0005
9—10	0. 0087	-o. or 38		
911	+0.0001	-0, 0020		
912	+0.0001	-0.0002		
)	<u></u>	I

Arg=i'g'+ig	δ	$\frac{h}{h_0}$	$\frac{u_1}{\cos i}$		
	cos.	sin.	cos.	sin.	
i' i 10— 4	,, —0. 0021	" —0. 0179	,,	"	
10 5	+0.0029	-0.0032	+0.0059	—o. 0147	
10— 6	—o. o117	-0.0044	+0.0024	_o. ooo6	
10— 7	+0.0014	+0.0335	—0. 0006	-o. oo33	
10 8	+0.0600	-0.0253	0, 0028	+0.0012	
10 9	0. 0499	—o. o587	+0.0005	+0.0010	
10—10	— 0. 0239	+0.0297			
1011	-o. oo88	+0.0030			
1012	0.0013	0, 0003			
11 5	+0.0014	0,0000			
11— 6	0.0019	—0. 0022	+o. ooo6	+0.0005	
11 7	-0.0043	+0.0080	+0.0005	+0.0013	
11 8	+0.0220	+0.0031	-0,0018	-0.0004	
11— 9	—0. 0076	o, o386	+0,0005	+0.0018	
1110	— 0. 0376	+0,0205			
11—11	+0.0107	+0.0150			
1112	+0.0006	+0.0051			
12 6	0.0002	0. 0007			
12— 7	-0.0020	+0.0009			
12— 8	+0.0050	+0.0041			
12- 9	+0.0048	<u> </u>		ļ	
12—10	-0.0237	0. 0003			
12—11	+0.0056	+0. 0224			
12—12	+0.0091	0.0024			

Arg=i'g'+ig	δ	$rac{h'}{h_0'}$	$\frac{{u_1}'}{\cos i'}$		
	cos.	sin.	cos.	sin.	
i' i o o o i o o o o o o o o o o o o o o	" -173.0111 + 1.9899 + 0.4463 + 0.0494 + 0.0003 - 0.0003 - 0.0144 + 4.6883 - 74.5932 + 27.6869 - 4.6889 - 0.1221	" - 9. 5637 - 0. 4873 - 0. 0142 + 0. 0011 - 0. 0004 - 0. 0042 + 0. 0529 - 22. 3609 + 355. 4266 + 20. 3654 - 3. 1427 - 0. 2223	" -0. 1347 +1. 6004 +0. 1788 -0. 0011 -0. 0031 -0. 0027 -0. 0206 -0. 1508 +1. 9041 +0. 9570 +0. 9911 -0. 3682 +0. 0769	" +1. 1383 +0. 4386 +0. 0529 +0. 0037 +0. 0005 -0. 0022 -0. 0996 +4. 0361 -0. 6482 -1. 0278 +0. 0102 +0. 0576	
5— I	+ 0.0009 + 0.0010	- 0.0182 - 0.0011	+0.0073 +0.0018	+0. 0096 +0. 0025	

COS. Sin. COS. Sin. COS. Sin.	Arg=i'g'+ig	$\delta_{ar{j}}$	$rac{h'}{\hbar_0{}'}$	$\frac{u}{\cos}$	<u>i'</u>
- 2 - 2		cos.	sin.	cos.	sin.
- 2 - 2	i/ i	"	"	"	"
0-2 + 0.2089 - 1.0524 +0.0452 +0.03 1-2 - 2.7604 +15.4062 -1.0007 +0.21 2-2 -31.2415 -12.8675 -0.2513 -0.20 3-2 -5.1200 -10.6134 +0.4513 +0.28 4-2 +1.0044 -3.9387 -1.0240 -8.62 5-2 -13.8298 +10.6323 -0.054 -0.02 6-2 -0.0766 +0.0013 +0.2446 -0.07 7-2 -0.0041 -0.0028 +0.0157 -0.00 8-2 -0.0001 -0.0003 +0.0157 -0.00 0-3 +0.0122 -0.0568 +0.0074 +0.01 1-3 -0.1456 +0.7903 -0.0052 +0.03 2-3 -0.3473 +0.7410 +0.0022 +0.46 3-3 8.8478 +12.4735 -0.1153 +0.3 4-3 5.8966 +1.9503 +0.2249 -0.08 5-3 -1.7097 -0.5683 +0.1305		0,0002	+ 0.0002		
1— 2 — 2. 7604 +15. 4062 — 1. 0007 +0. 211 2— 2 — 31. 2415 — 12. 8675 — 0. 2513 — 0. 20 3— 2 — 5. 1200 — 10. 6134 +0. 4513 +0. 28 4— 2 + 1. 0044 — 3. 9387 — 1. 0240 — 8. 62 5— 2 — 13. 8298 + 10. 6323 — 0. 0054 — 0. 02 6— 2 — 0. 0766 + 0. 0013 +0. 2446 — 0. 02 7— 2 — 0. 0041 — 0. 0028 +0. 0157 — 0. 00 8— 2 — 0. 0001 — 0. 0004 +0. 0157 — 0. 00 1— 3 — 0. 0002 + 0. 0003 — 0. 0056 +0. 0157 — 0. 00 1— 3 — 0. 0002 + 0. 0003 — 0. 0052 +0. 03 — 0. 0052 +0. 03 1— 3 — 0. 0122 — 0. 0568 + 0. 0074 +0. 01 +0. 01 +0. 01 +0. 01 +0. 01 +0. 01 +0. 01 +0. 01 +0. 01 +0. 01 +0. 01 +0. 01 +0. 01 +0. 02 +0. 02 +0. 08	_ I_ 2	o. oo27	+ 0,0060	о. 0036	+o. oo78
2- 2	0 2	+ o. 2089	— 1. 0 <u>52</u> 4	+0.0452	+o. o3o5
3-2	I— 2	- 2.7604	+15.4062	—1.000 7	+0. 2149
4-2 + 1.0044 - 3.9387 -1.0240 -8.62 5-2 -13.8298 +10.6323 -0.0054 -0.02 6-2 -0.0766 +0.0013 +0.2446 -0.07 7-2 -0.0001 -0.0028 +0.0157 -0.00 8-2 -0.0001 -0.0004 +0.0157 -0.00 -1-3 -0.0002 +0.0003 -0.0568 +0.074 +0.01 1-3 -0.1456 +0.7903 -0.0052 +0.03 2-3 -0.3473 -0.7410 +0.0022 +0.46 3-3 -8.8478 +12.4735 -0.1153 +0.13 4-3 -5.8966 +1.9503 +0.2249 -0.66 5-3 -1.7097 -0.5683 +0.2014 +0.02 6-3 -0.2996 -0.4225 +0.1305 +0.08 7-3 +0.0008 -0.2547 -0.0107 -0.01 8-3 -0.0175 +0.0241 -0.0017 +0.00 9-3 -0.0013 +0.0044 +0.009 -0.00 1-4 -0.00082 +0.0434 +0	2— 2	-31. 2415		0. 2513	—o. 2065
5-2 -13.8298 +10.6323 -0.0054 -0.02 6-2 -0.0766 +0.0013 +0.2446 -0.07 7-2 -0.0041 -0.0028 +0.0157 -0.00 8-2 -0.0001 -0.0004 +0.0157 -0.00 -1-3 -0.0002 +0.0003 -0.052 +0.01 1-3 -0.1456 +0.7903 -0.052 +0.03 2-3 -0.3473 -0.7410 +0.0022 +0.46 3-3 -8.8478 +12.4735 -0.1153 +0.13 4-3 -5.8966 +1.9503 +0.2249 -0.08 5-3 -1.7097 -0.5683 +0.2249 -0.08 6-3 -0.2996 -0.4225 +0.1305 +0.08 7-3 +0.0008 -0.2547 -0.0107 -0.01 8-3 -0.0175 +0.0241 -0.0013 +0.00 9-3 -0.0013 +0.0004 +0.0013 +0.00 1-4 -0.00082 +0.0434 +0.0009	3 2	— 5. 1200	—10. 6134	+0.4513	+0.2824
6 2	4 2	+ 1.0044	 3. 9387	— 1. 0240	8. 6226
7-2 -0.0041 -0.0028 +0.0157 -0.00 8-2 -0.0001 -0.0004 -0.0004 -0.0056 -0.0074 -0.01 1-3 -0.1456 +0.7903 -0.0052 +0.03 -0.0052 +0.03 2-3 -0.3473 -0.7410 +0.0022 +0.46 -0.46 3-3 -8.8478 +12.4735 -0.1153 +0.13 4-3 -5.8966 +1.9503 +0.2249 -0.08 5-3 -1.7097 -0.5683 +0.2014 +0.02 6-3 -0.2996 -0.4225 +0.1305 +0.08 7-3 +0.0008 -0.2547 -0.0107 -0.01 8-3 -0.0175 +0.0241 -0.0013 +0.001 9-3 -0.0013 +0.0004 -0.0013 +0.0004 0-4 +0.0007 -0.0032 +0.0095 +0.01 1-4 -0.0033 -0.0282 +0.0095 +0.01 3-4 +0.0033 -0.0282 +0.01 +0.01	5— 2	-13.8298	+10.6323	0, 0054	—o. o2o6
8- 2	6 2	o. o766	+ 0.0013	 -0. 2 446	—о. 0783
- 1- 3	7— 2	— o. oo41	— o, oo28	+0.0157	—0. 0039
0-3 + 0.0122 - 0.0568 + 0.0074 + 0.01 1-3 - 0.1456 + 0.7903 - 0.052 + 0.03 2-3 - 0.3473 - 0.7410 + 0.0022 + 0.46 3-3 - 8.8478 + 12.4735 - 0.1153 + 0.13 4-3 - 5.8966 + 1.9503 + 0.2249 - 0.08 5-3 - 1.7097 - 0.5683 + 0.2014 + 0.02 6-3 - 0.2996 - 0.4225 + 0.1305 + 0.08 7-3 + 0.0008 - 0.2547 - 0.0107 - 0.01 8-3 - 0.0175 + 0.0241 - 0.0013 + 0.00 9-3 - 0.0175 + 0.0024 - 0.0013 + 0.00 9-3 - 0.0015 + 0.0032 + 0.0013 + 0.00 1-4 - 0.0082 + 0.0434 + 0.0009 - 0.00 3-4 + 0.0033 - 0.0282 + 0.0712 + 0.07 4-4 + 4.8353 + 5.3003 + 0.0712 + 0.07 5-4 + 0.5238	8— 2	— 0. 0001	0.0004		
0-3 + 0.0122 - 0.0568 + 0.0074 + 0.01 1-3 - 0.1456 + 0.7903 - 0.0052 + 0.03 2-3 - 0.3473 - 0.7410 + 0.0022 + 0.46 3-3 - 8.8478 + 12.4735 - 0.1153 + 0.13 4-3 - 5.8966 + 1.9503 + 0.2249 - 0.08 5-3 - 1.7097 - 0.5683 + 0.2014 + 0.02 6-3 - 0.2996 - 0.4225 + 0.1305 + 0.08 7-3 + 0.0008 - 0.2547 - 0.0107 - 0.01 8-3 - 0.0175 + 0.0241 - 0.0013 + 0.00 9-3 - 0.0175 + 0.00241 - 0.0013 + 0.00 1-4 - 0.0082 + 0.0434 + 0.0009 - 0.00 2-4 + 0.0033 - 0.0282 + 0.01 + 0.01 3-4 + 0.6779 + 0.1715 + 0.2184 + 0.07 4-4 4 8353 + 5.3003 + 0.0712 + 0.07 5-4 + 0.5238	<u>- 1- 3</u>	o. 0002	+ 0.0003		
2-3	o 3	+ 0.0122	o. o568	+0.0074	+0.0156
3-3 -8.8478 +12.4735 -0.1153 +0.13 4-3 -5.8966 +1.9503 +0.2249 -0.08 5-3 -1.7097 -0.5683 +0.2014 +0.02 6-3 -0.2996 -0.4225 +0.1305 +0.08 7-3 +0.0008 -0.2547 -0.0107 -0.01 8-3 -0.0175 +0.0241 -0.0013 +0.001 9-3 -0.0013 +0.0004 -0.0013 +0.001 0-4 +0.0007 -0.0032 +0.0095 +0.01 1-4 -0.0082 +0.0434 +0.0095 +0.01 3-4 +0.0033 -0.0282 +0.0095 +0.01 3-4 +0.6779 +0.1715 +0.2184 +0.0712 +0.07 4-4 +4.8353 +5.3003 +0.0712 +0.07 -0.08 5-4 +0.5238 +3.4347 -0.0104 -0.08 6-4 -0.4683 +0.9656 +0.0240 -0.06 7-4 +0.0133 -0.005 +0.0133 -0.00 9-4 +0.0123 +0.0463	I— 3	— o. 1456	+ 0.7903	0. 0052	+0.0303
4-3 - 5.8966 + 1.9503 + 0.2249 - 0.08 5-3 - 1.7097 - 0.5683 + 0.2014 + 0.02 6-3 - 0.2996 - 0.4225 + 0.1305 + 0.08 7-3 + 0.0008 - 0.2547 - 0.0107 - 0.01 8-3 - 0.0175 + 0.0241 - 0.0013 + 0.00 9-3 - 0.0013 + 0.0004 - 0.0013 + 0.00 0-4 + 0.0007 - 0.032 + 0.003 + 0.0095 + 0.01 1-4 - 0.0082 + 0.0434 + 0.0095 + 0.01 + 0.01 3-4 + 0.0033 - 0.0282 + 0.095 + 0.01 + 0.01 3-4 + 0.6779 + 0.1715 + 0.2184 + 0.04 + 0.0712 + 0.04 4-4 + 4.8353 + 5.3003 + 0.0712 + 0.07 + 0.01 + 0.01 + 0.0240 + 0.06 5-4 + 0.5238 + 3.4347 + 0.0104 + 0.0240 + 0.0240 + 0.0258 + 0.0258 + 0.0258 + 0.0258 + 0.0258 + 0.0258 + 0.0258 + 0.0258 + 0.0376 + 0.037	2 3		0. 7410	+0.0022	+0.4682
5-3 - I. 7097 - 0. 5683 + 0. 2014 + 0. 02 6-3 - 0. 2996 - 0. 4225 + 0. 1305 + 0. 08 7-3 + 0. 0008 - 0. 2547 - 0. 0107 - 0. 01 8-3 - 0. 0175 + 0. 0241 - 0. 0013 + 0. 00 9-3 - 0. 0013 + 0. 0004 - 0. 0013 + 0. 00 0-4 + 0. 0007 - 0. 0032 - 0. 0003 - 0. 0032 1-4 - 0. 0082 + 0. 0434 + 0. 00095 + 0. 01 2-4 + 0. 0033 - 0. 0282 + 0. 0095 + 0. 01 3-4 + 0. 6779 + 0. 1715 + 0. 2184 + 0. 04 4-4 + 4. 8353 + 5. 3003 + 0. 0712 + 0. 04 4-5 + 0. 5238 + 3. 4347 - 0. 0104 - 0. 08 5-4 + 0. 5238 + 0. 1383 + 0. 0240 - 0. 06 7-4 - 0. 2448 + 0. 1383 + 0. 0258 - 0. 02 8-4 - 0. 0723 - 0. 0069 + 0. 0133 - 0. 00 <th>3 3</th> <th></th> <th>+12.4735</th> <th>0. 1153</th> <th>+0. 1384</th>	3 3		+12.4735	0. 1153	+0. 1384
6-3 - 0.2996 - 0.4225 + 0.1305 + 0.08 7-3 + 0.0008 - 0.2547 - 0.0107 - 0.01 8-3 - 0.0175 + 0.0241 - 0.0013 + 0.00 9-3 - 0.0013 + 0.0004 - 0.0013 + 0.00 0-4 + 0.0007 - 0.0032 + 0.0095 + 0.01 1-4 - 0.0082 + 0.0434 + 0.0095 + 0.01 3-4 - 0.6779 + 0.1715 + 0.2184 + 0.04 4-4 + 4.8353 + 5.3003 + 0.0712 + 0.07 5-4 + 0.5238 + 3.4347 - 0.0104 - 0.08 6-4 - 0.4683 + 0.9656 + 0.0240 - 0.06 7-4 - 0.2448 + 0.1383 + 0.0258 - 0.02 8-4 - 0.0723 - 0.0669 + 0.0133 - 0.00 9-4 + 0.0123 + 0.0463 - 0.0376 - 0.0376 10-4 + 0.00123 + 0.0463 - 0.0004 + 0.0004 2-5 + 0.0010 - 0.0008 + 0.0004 + 0.0004 + 0.0004 3-5	4 3	5.8966	+ 1.9503	+0. 2249	o. o828
7-3 + 0.0008 - 0.2547 - 0.0107 - 0.01 8-3 - 0.0175 + 0.0241 - 0.0013 + 0.00 9-3 - 0.0013 + 0.0004 - 0.0013 + 0.00 0-4 + 0.0007 - 0.0032 - 0.0032 - 0.00 1-4 - 0.0082 + 0.0434 + 0.0095 + 0.01 3-4 - 0.6779 + 0.1715 + 0.2184 + 0.04 4-4 + 4.8353 + 5.3003 + 0.0712 + 0.07 5-4 + 0.5238 + 3.4347 - 0.0104 - 0.08 6-4 - 0.4683 + 0.9656 + 0.0240 - 0.06 7-4 - 0.2448 + 0.1383 + 0.0258 - 0.02 8-4 - 0.0723 - 0.0069 + 0.0133 - 0.00 9-4 + 0.0123 + 0.0463 - 0.0376 - 0.0376 10-4 + 0.0123 + 0.0463 - 0.0004 2-5 + 0.0010 - 0.0008 + 0.0104 + 0.00 4-5 + 0.0278 + 0.4936 + 0.0463 - 0.03 5-5 + 2.9806 - 1.7054 <th>5 3</th> <th>— I. 7097</th> <th> o. 5683</th> <th>+0. 2014</th> <th>+0.0265</th>	5 3	— I. 7097	o. 5683	+0. 2014	+0.0265
8— 3 — 0. 0175 — + 0. 0241 — -0. 0013 — +0. 00 9— 3 — 0. 0013 — +0. 0004 0— 4 — +0. 0007 — -0. 0032 — +0. 0095 — +0. 01 3— 4 — 0. 06779 — +0. 1715 — +0. 2184 — +0. 04 4— 4 — +4. 8353 — +5. 3003 — +0. 0712 — +0. 07 5— 4 — +0. 5238 — +3. 4347 — -0. 0104 — -0. 08 6— 4 — -0. 4683 — +0. 9656 — +0. 0240 — -0. 06 7— 4 — -0. 2448 — +0. 1383 — +0. 0258 — -0. 02 8— 4 — 0. 0723 — 0. 0069 — +0. 0133 —-0. 00 9— 4 — -0. 0183 — -0. 0150 — -0. 0376 — -0. 03 10— 4 — +0. 0123 — +0. 0463 — -0. 0004 2— 5 — +0. 0010 — -0. 0008 3— 5 — 0. 0290 — -0. 0082 — +0. 0104 — +0. 0004 4— 5 — +0. 00278 — +0. 4936 — +0. 0463 —-0. 09 5— 5 — +2. 9806 — 1. 7054 — +0. 0527 —-0. 03 6— 5 — +1. 9609 — +0. 0693 —-0. 0289 —-0. 000	6— 3	— 0. 2996	— o. 4225	+o. 1305	+0.0854
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	7— 3	+ 0.0008	— o. 2547	—0. 0107	0. 0153
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	8— 3	— o. o175	+ 0.0241	0. 0013	+0.0016
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	9— 3	- 0.0013	+ 0.0004		
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	0— 4	+ 0.0007	- 0.0032		
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	1 4	- o. oo82	+ 0.0434	+0.0009	0, 0009
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	2— 4		0.0282	+0.0095	+0.0127
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	3 4		+ 0. 1715	+0. 2184	+0. 0464
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	4 4	+ 4.8353	+ 5.3003	+0.0712	+0.0795
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	5— 4		+ 3.4347	0. 0104	o. o8o9
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	6 4	— o. 4683	+ 0.9656	+ 0. 0240	− 0. 0692
$\begin{array}{cccccccccccccccccccccccccccccccccccc$		 0. 2448	+ 0. 1383		-0. 0243
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	8 4		1		-0.0048
$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$		-		0. 0376	—o. oo65
$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$			1	İ	
3-5 -0.0290 -0.0082 +0.0104 +0.00 4-5 +0.0278 +0.4936 +0.0463 -0.09 5-5 +2.9806 -1.7054 +0.0527 -0.03 6-5 +1.9609 +0.0693 -0.0289 -0.00	11— 4	— 0,0000	- 0.0004		
4-5 + 0. 0278 + 0. 4936 + 0. 0463 0. 09 5-5 + 2. 9806 - 1. 7054 + 0. 0527 0. 03 6-5 + 1. 9609 + 0. 0693 0. 0289 0. 00	2— 5			1	
5-5 + 2.9806 - 1.7054 +0.0527 -0.03 6-5 + 1.9609 + 0.0693 -0.0289 -0.00	3— 5			1	+0.0009
6— 5 + 1. 9609 + 0. 0693 -0. 0289 -0. 00					0. 0993
			1		0. 0341
7-5 + 0.5487 + 0.3849 -0.0276 -0.01				1	-0.0032
	7— 5				—o. o173
				•	—o. o137
			1	1	0.0058
					-0.0022
				+0.0010	-0.0010
12-5 -0.0007 -0.0006	12 5	0.0007	— 0,0000		

Arg=i'g'+ig	δ	$\frac{h'}{h_0'}$	u co	s i'
	cos.	sin.	cos.	sin.
i' i 3— 6	+0.0026	0.0010	"	"
4 6	-o. o136	+0.0252	+0.0044	-o. oo65
5— 6	+0.3180	+0.0470	-o. o426	-o. o327
6 6	o. 48o6	—I. 5908	-0.0133	-o. o338
7— 6	+0. 2549	1.0753	-0. 0047	+0.0095
8 6	+0. 2972	-0. 2957	-0, 0117	+0.0110
9— 6	+o. 1198	-0, 0262	-o. oo83	+0.0024
10— 6	+0.0290	+0.0109	-0.0029	0.0005
11— 6	+0.0042	+0.0059	o. ooo8	-0,0008
12— 6	+0.0002	+0.0016		
4 7	-0.0010	+0.0018	+0.0013	-0.0013
5— 7	+0.0170	+0.0142	-0.0037	-0.0037
6— 7	+0.0690	-0. 1870	-0. 0216	+0.0171
7-7	0. 8074	+0.0500	0. 0197	+0.0031
8— 7	0. 5610	o. 2616	+0.0009	+0.0028
9-7	o. 146o	0. 2172	+0. 0042 +0. 0015	+0.0067
10 7	-0.0022	0. 0828 0. 0186	—0. 0006	+0.0044
11— 7	+0.0110 +0.0036	-0. 0180 -0. 0026	-0.0011	+0.0032 +0.0005
· ·			-0.0011	70.0003
6 8	+0.0132	0.0098		_
7— 8	—0. 1006	o. o638	+0.0039	+0.0116
8 8	o. o698	+0. 3884	0.0012	+0.0107
9— 8	0. 2078	+0. 2740		
10 8	o. 1486	+0.0610		
11 8	0. 0 5 34	0. 0094	+0.0027	0, 0000
12— 8	-O. OI 22	0.0092		
7— 9	0. 0048	-0.0096		
8— g	0. 0492	+0.0504	+0.0057	0.0014
9— 9	+0. 1744	+0.0784	+0.0093	+0.0013
10 9	+0. 1248	+0.1436		
11- 9	+0. 0196	+0.0950		
12 9	—o. o116	+0.0342		
8—10	0.0080	+0.0026		
9—10	+0.0224	+0.0356		
1010	+0.0598	-0.0726		
11—10	+0.0922	—o. o488		
12-10	+0. 0588	+0.0008		
911	0.0002	+0.0054		
1011	+0.0218	-0.0078		
1111	-0.0272	o. o378		
12—11	-0.0154	o. o558		
1012	+0.0026	+0.0010		
11—12	-0.0008	-0. 0I32		
12—12	0. 0226	+0.0064		

CHAPTER IX.

CALCULATION OF THE TERMS OF ST AND ST' WHOSE ARGUMENTS ARE ν AND ν' .

Being now in possession of the several factors of the terms of δT and $\delta T'$, we could proceed immediately to the calculation of the terms, strictly of the second order, which arise from these quantities. But the more important parts of these functions are the terms coming from the secular variations of the elements. This prominence is kept up in the terms of the third, and apparently of all higher orders. And it is, perhaps, the most surprising instance in the planetary theories of a lack of convergence that the secular variations of the eccentricities and places of the perihelia of Jupiter and Saturn are augmented about a fourth part by the terms of the second order with respect to disturbing forces. Since the mass of Jupiter is less than $\frac{1}{1000}$ of that of the Sun it would naturally be supposed that the ratio of the second to the first-order terms would be somewhere in the neighborhood of this fraction. It is, however, 250 times larger.

By far the larger portions of these second-order terms arise from the terms of δT and $\delta T'$, having severally the arguments γ and γ' . By computing these portions at the outset, and annexing them to the first-order terms corresponding to the same arguments before proceeding to the general calculation of δT and $\delta T'$, we shall include in the determination of the second-order terms the more notable portion of the third-order terms. In like manner, on arriving at the general computation of the latter, we shall first compute the terms having the arguments γ and γ' , and annexing them to the second-order terms, shall then be able to include the more remarkable portion of the fourth-order terms in that of the third. The modifications which this mode of proceeding requires in the values of the second factors are readily perceived.

In this connection it will be interesting to see how much each set of terms of the second factors of δT and $\delta T'$ contributes to the terms under consideration. Hence, I enter into some details relative to them. Defining these sets of terms by the arguments on which they depend, the general form of which is i'g' + ig, I have arranged in the following table the component parts of the coefficients of $\sin \gamma$ and $\cos \gamma$ in δT and of $\sin \gamma'$ and $\cos \gamma'$ in $\delta T'$. The numbers given are in units of the seventh decimal of the second of arc for δT and in units of the sixth decimal for $\delta T'$. They arise from multiplying the terms in the second factors having the argument i'g' + ig by the terms of the first factors having the two arguments $\pm \gamma + i'g' + ig$ in the case of δT , or $\pm \gamma' + i'g' + ig$ in the case of $\delta T'$. Thus, it is plain that, since there are

eight terms in both δT and $\delta T'$, the numbers tabulated are the sums of thirty-two component parts. However, in many cases some of these have no significant values:

	δ	T	δ	\mathbf{T}'
Arg=i'g'+ig	sin (— γ)	$\cos{(-\gamma)}$	$\sin \gamma'$	cos γ′
i' i 0 0 0— 1 0— 2 0— 3	— 168 + 1900 + 1	+ 155 — 4860 — 7	— 6194 + 64527 + 315 + 1	— 9863 — 7326 — 41
1+ 1 1 0 1- 1 1- 2 1- 3	+ 31 + 10145 + 27548 - 508 + 1	— 64 — 5731 — 24944 — 275	— 51 — 9674 — 90608 + 1184 — 1	+ 56 + 24596 5216 + 6988 + 17
2— 0 2— 1 2— 2 2— 3 2— 4	+ 174 1618217 45163 + 5291 + 16	- 59 + 717049 + 10046 - 624 + 6	$ \begin{array}{rrrr} & - & 23 \\ & + & 63191 \\ & + & 28304 \\ & + & 374 \\ & + & 2 \end{array} $	+ 260 -365746 + 3690 + 1392 + 4
3 0 3— 1 3— 2 3— 3 3— 4 3— 5	— 1 — 18475 — 49846 — 9443 + 1050 + 4	- 7 + 4121 + 66600 + 12882 - 364	- 8 + 7070 + 59124 + 5280 + 53	+ 1 - 2983 - 68574 - 5075 + 184
4— r 4— 2 4— 3 4— 4 4— 5 4— 6	+ 9 - 303245 + 19018 - 2905 + 350 + 2	— 12 +1022420 — 63009 + 4524 — 189	— 10 +944393 — 57800 + 1506 + 2	+ 27 -508415 + 31889 - 1688 + 47
5— I 5— 2 5— 3 5— 4 5— 5 5— 6	0 — 236978 — 41087 — 1252 — 948 + 125	+ 1 + 700335 + 145928 - 13744 + 1581 - 73	+645280 +137249 13756 + 471	+ 1 -373622 - 71606 + 1566 - 573 + 14
6— 2 6— 3 6— 4 6— 5 6— 6 6— 7	+ 33 + 420 + 811 + 716 292 + 42	- 3 - 1516 - 2867 - 2499 + 508 - 22	+ 3 - 1414 - 2642 - 2290 + 136	+ 34 + 719 + 1364 + 1257 - 179 + 5

	δ	T	δ	T ′
Arg=i'g'+ig	$\sin (-\gamma)$	cos (— γ)	$\sin \gamma'$	cos γ'
i' i 7— 3 7— 4	—122 +165	+427 —601	+403 -563	-210 +283 +368
7— 5 7— 6 7— 7 7— 8	+225 +168 - 93 + 14	—729 —636 +163 — 8	—655 —598 + 40 — 1	+305 +322 - 55 + 2
8— 3 8— 4 8— 5 8— 6 8— 7 8— 8	- 1 + 29 + 66 + 36 - 27	+ 1 - 1 -105 -230 -163 + 51	+ 1 - 1 - 97210161 + 9	- 1 0 + 49 +109 + 82 - 18
8— 9 9— 4 9— 5 9— 6 9— 7 9— 8 9— 9	+ 5 - 10 + 5 + 11 + 20 + 9 - 8	- 5 + 38 - 10 - 35 - 77 - 41 + 18	+ 1 + 37 - 11 - 32 - 71 - 45 + 3	- 18 + 6 + 17 + 37 + 20 - 8
10— 4 10— 5 10— 6 10— 7 10— 8	- 4 - 2 0 + 5 + 9 - 1	+ 10 + 5 - 4 - 13 - 27 - 10	+ 9 + 5 - 4 - 12 - 24 - 14	- 5 - 3 0 + 5 + 12 + 7
11—10 11— 9 11— 8	o + 1 + 3	- 5 - 8 - 4	- 5 - 8 - 4	+ 4 + 5 + 4
12 9 1210	O 101	2 4	— I — 4	0

It will be perceived that the arguments 2g'-g, 4g'-2g, 5g'-2g, and 5g'-3g contribute the largest portions to these terms of the second order. In the case of the three latter arguments the cause of the largeness of the portions contributed is the division by the small divisor 5n'-2n or its square. But in the case of the first, 2g'-g, this cause does not operate, and yet for Jupiter this argument contributes the largest quota. Hence, it is hardly correct to say that the superior magnitude of the terms we are considering is due to the smallness of 5n'-2n. However, 2g'-g may be considered as an argument of long period, since $\frac{n}{2n'-n}$ is about 5. But the actual explanation of the magnitude of the coefficients, whose component parts have just been given, appears to be that the terms of T and T' having the arguments γ and γ'

are exceptionally small. This will be apparent when we write them in connection with the maximum terms, as follows:

$$T = - \frac{\pi}{1.142} \sin(-\gamma) + \frac{\pi}{1.017} \cos(-\gamma)
- 47.872 \sin(-\gamma + 2g'-g) + 20.556 \cos(-\gamma + 2g'-g)$$

$$T' = 8.631 \sin \gamma' - 5.350 \cos \gamma'
+ 413.905 \sin(\gamma' - g') + 1977.900 \cos(\gamma' - g)$$

With them may also be compared the largest terms of the factors G and G'

$$G = {}^{16}7.70 \sin (-\gamma + 2g' - g) - {}^{7}1.60 \cos (-\gamma + 2g' - g)$$

$$G' = -782.26 \sin (\gamma' - g) - 3729.47 \cos (\gamma' - g)$$

Adding the components of δT and $\delta T'$ given in the preceding table, we obtain

$$\delta \mathbf{T} = -0.2260338 \sin (-\gamma) + 0.2563282 \cos (-\gamma)$$

$$\delta \mathbf{T}' = +1.771981 \sin \gamma' -1.345783 \cos \gamma'$$

It is desirable to have the means of readily changing these expressions, so as to correspond to any new values of the masses of Jupiter and Saturn that may be adopted. Thus, by adding the five terms of δT involving the factors A to E, we find that the portion of δT proportional to $\left(\frac{m'}{r+m}\right)^2$ is

$$-\circ$$
".0351410 $\sin(-\gamma) + \circ$ ".0526059 $\cos(-\gamma)$

and by adding the three terms involving the factors F to H, we find that the portion of δT proportional to $\frac{m}{1+m'} \cdot \frac{m'}{1+m}$ is

$$-0''.1908928 \sin(-\gamma) + 0''.2037223 \cos(-\gamma)$$

In like manner, the portion of $\delta T'$ proportional to $\left(\frac{m}{1+m'}\right)^2$ is

$$+ 1''.337009 \sin \gamma' - 1''.066713 \cos \gamma'$$

and the portion proportional to $\frac{m}{1+m'} \cdot \frac{m'}{1+m}$ is

$$+ \circ''.434972 \sin \gamma' - \circ''.279070 \cos \gamma'$$

By joining the second-order terms, which arise from δT and $\delta T'$, to the principal secular terms of the first order of $n\delta z$ and $n'\delta z'$, obtained in preceding chapters, we have the following exhibit:

```
n\delta z
                                         -0.0000059nt \sin(-g) - 0.0000137nt \cos(-g)
Action of Mercury
Action of Venus
                                         -0.0000153nt \sin(-g) - 0.0007144nt \cos(-g)
                                         -0.0001530nt \sin(-g) - 0.0018372nt \cos(-g)
Action of the Earth
                                         + 0.0002138nt \sin(-g) - 0.0002217nt \cos(-g)
Action of Mars
Action of Saturn
                                         -1.0173636nt \sin(-g) - 1.1420391nt \cos(-g)
                                         -0.0021751nt \sin(-g) - 0.0213460nt \cos(-g)
Action of Uranus
                                         -0.0000833nt \sin(-g) - 0.0040184nt \cos(-g)
Action of Neptune
Terms factored by \left(\frac{m'}{r+m}\right)^2
                                         -0.0526059nt \sin(-g) - 0.0351410nt \cos(-g)
Terms factored by \frac{m}{1+m'} \cdot \frac{m'}{1+m}
                                         -0.2037223nt \sin(-g) - 0.1908928nt \cos(-g)
                                         -1.2759106nt \sin(-g) - 1.3962243nt \cos(-g)
      Sum
                                            n'\delta z'
                                                0.000000n't \sin g' - 0.000005n't \cos g'
    Action of Mercury
    Action of Venus
                                             + 0.000002n't \sin q' - 0.000235n't \cos q'
                                             + 0.000004n't \sin g' - 0.000579n't \cos g'
    Action of the Earth
                                             -0.000044n't \sin g' - 0.000172n't \cos g'
    Action of Mars
                                             -5.350080n't \sin g' - 8.631067n't \cos g'
    Action of Jupiter
    Action of Uranus
                                             + 0.085000n't \sin g' - 0.155652n't \cos g'
                                             -0.001474n't \sin g' - 0.032936n't \cos g'
    Action of Neptune
    Terms factored by \left(\frac{m}{1+m'}\right)^2
                                             -1.066713n't \sin g' - 1.337009n't \cos g'
    Terms factored by \frac{m}{1+m'} \cdot \frac{m'}{1+m}
                                             -0.279070n't \sin g' - 0.434972n't \cos g'
                                              -6.612375n't \sin g' - 10.592627n't \cos g'
```

The expressions actually used in Chapter XI for determining the portion of δT, which is factored by nt, are

Sum

$$n\delta z = -1.2759133nt \sin(-g) - 1.3962200nt \cos(-g)$$

$$n'\delta z' = -6.612298n't \sin g' - 10.592645n't \cos g'$$

The terms dependent on the arguments 2g, 3g . . . 2g', 3g' . . . can be found by the formulæ of page 102.

The secular terms of $\frac{u}{\cos i}$ and $\frac{u'}{\cos i'}$ are, in like manner, summed as follows:

```
Action of Mercury
                         + 0.0000080nt \sin(-q) - 0.0000171nt \cos(-q)
Action of Venus
                        + 0.0002201nt \sin(-g) - 0.0001852nt \cos(-g)
Action of the Earth
                         -0.0004354nt \sin(-g) + 0.0000230nt \cos(-g)
                         -0.0000186nt \sin(-g) - 0.0001257nt \cos(-g)
Action of Mars
Action of Saturn
                         + 0.2844315nt \sin(-g) + 0.1253514nt \cos(-g)
Action of Uranus
                         -0.0019103nt \sin(-g) - 0.0008950nt \cos(-g)
Action of Neptune
                         + 0.0001987nt \sin(-g) + 0.0006825nt \cos(-g)
      Sum
                         + 0.2824940nt \sin(-g) + 0.1248339nt \cos(-g)
                                  \frac{u'}{\cos i'}
    Action of Mercury
                             + 0.000005n't \sin q' + 0.000002n't \cos q'
                             + 0.000067n't \sin q' - 0.000036n't \cos q'
    Action of Venus
    Action of the Earth
                             + 0.000086n't \sin g' + 0.000212n't \cos g'
                             + 0.000051n't \sin q' + 0.000022n't \cos q'
    Action of Mars
                             + 1.106428n't \sin g' + 1.552265n't \cos g'
    Action of Jupiter
    Action of Uranus
                             + 0.032793n't \sin g' + 0.042895n't \cos g'
    Action of Neptune
                             -0.001104n't \sin g' + 0.005024n't \cos g'
          Sum
                             + 1.138326n't \sin q' + 1.600384n't \cos q'
```

The secular term of $\delta \frac{h}{h_0}$ is the same as the non-periodic secular term of -2ν .

CHAPTER X.

CALCULATION OF THE PORTION OF ST NOT FACTORED BY nt.

In determining the portion of δT , which follows, a table of limits for the retention of terms for each argument $\pm \gamma + i'g' + ig$ was computed from the formula

$$\frac{i'n'+in}{n} \cdot \frac{i'n'+(i\pm 1)n}{n} \times 0''.0005$$

and only those combinations were retained in which at least one coefficient exceeded this limit. It has been deemed advisable to give separately the eight products whose sum forms δT :

Aı	rg==	A	$n\delta z$	В(ν	c) + Xc	Fn	/δε/	$G(\nu'-c')$	
н γ+i	i'g'+ig	sin.	cos.	sin.	cos.	sin.	cos.	sin.	cos.
и	i' i	"	,,	"	//	"	"	"	//
٥	0 0		-0.00041718		+0,00039938		+0.00014725		0. 00015832
1		+0.0059	—0.00I2	+0.0145	-0.0006	-0.0104	-0.0051	+0.0433	—0.0019
1-1	0 0		+o. o386863	—o. oo85509			+0. 1637579		+ 0.0399 329
°	- 1	+0.0462	o. o588	+0.0127	0.0180	+0. 1348	—0. 1529	+0.0495	0.0410
I	0 2	o. o17	+0.025		+0.006	-0.029	+0.048	0. 013	+0.015
_1	о— і	—o. 07 I	o. o56	-0.010	0.007	-0. 324	0. 248	-0.069	—0. 045
0		+0.091	+o. o68	+0.011	+0.007	+o. 317	+0.236	+0.067	+0,040
I	0— 3		-0.022	0.003	0, 002	0, IOI	—0. 062	0, 020	0.014
-r		i '	—o. o81			+0.316	-0. 244	0.016	+0.007
0	o 3	l	+0. 101			—0, 296	+0. 247	+0.018	0. 006
I			o. o37			+0.094	0. 076		
—r		+0.003	0.019	·		+0.007	-0, 044		
°	0— 4	-0.010	+o. 02 7			-0.019	+0.053		
ı	0 5					+0. 01	0. 02		
—ı	1+4	+0.012	0.008			+0.019	-0.014	1	
0	1+3	0. 027	+0.017		'	0.052	+0.034	ŀ	}
1	1+2	+0.017	o. oo6			- +0. 043	o. o15		}
I	1+3	+0.035	0. 073			+0. 071	u. 138	ŀ	į l
0	1+2	0.094	+0. 193			— 0. 230	+0.465	+0.003	0, 022
I	1+1	+0.070	0. 152			+o. 227	o. 493	-o. 007	+0.021
_r	1+2	+0.029	+0.031	+0.003	+0.004	+o. o85	+0.090	+0.022	+0.020
0	1+1	o. o87	-0.072	—∪. OI 2	—o. oi i	—o. 317	0. 271	0. 073	_ ∪. 072
1	1 0	+0.0626	+o. o535	+o. 0108	+0.0103	+0. 3316	+0. 2838	+0.0790	+0.0749
<u>_1</u>	1+1	0. 0196	+0.0057	-o. oo83	+0.0042	o. o215	-0.0002	0.0124	+0.0043

Arg=	-	An	$\iota \delta z$	Β(ν	c) + Xc	Fn	'δz'	G(v'	-c')
$\mu_{\gamma}+i^{\gamma}g^{\prime}$		sin.	cos.	sin.	cos.	sin.	cos.	sin.	cos.
и i'	i	"	"	11	"	11	"	11	"
0 1	0	+0.0405	-0.0241	+o. o186	-0.0109	+0.0698	-0.0502	+0. 0209	-0.0218
I I-	_ ı	-0. 0218	+0.0117	-0, 0 1 21	+0.0079	-0.0815	+0.0572	<u> </u>	+0.0249
—I I	0	0. 0039	-o. 0141	0. 0032	0. 0178	-0.0143	+0.0450	0. 0274	-0. 1010
O I-	— ı	+0.0077	+0.0091	+0.0021	+0.0102	+0.0158	<u> </u>	+0.0210	+0.0650
1 1-	- 2	0.0007	0. 0005	+0.0020	+0.0040	+0.0027	+0.0074	+0.0015	+0.0145
-ı ı-	— I	—o. 0498	0. 0229	0. 0138	0. 0047	-0. 2019	—0. 1080	0. 0481	0. 0346
	z	+0.067	+0.031	+0.019	+0.007	+0. 193	+0. 104	+0.051	+0.036
I I-	- 3	0. 025	-0.011			— 0. об1	0. 022	0. 015	-o. oo8
—ı ı-	- 2	+o. o33	-0.072	+0.004	0.008	+o. 144	—о. 309	+0.022	o. o54
O I-	— 3	o. o39	+0.087	0, 004	+0.008	—о. 133	+0.303	0. 022	+0.053
1	— 4	+0.011	0. 034			+0.035	-o. o95	+0.007	-o. o17
	— 3	+0.075	+0.064			+0.214	+0. 174	-o. oo8	0.012
	4	—o. o89	-o. o7 I			—0. 214	0. 159	+0.007	+0,014
I I-	— 5	+0.04	+0.03			+0.07	+0.05		
I 2-	+ 3	+0.012	+0.009			+0.018	+0.014		
0 2-	+ 2	0. 022	0.021			0. 040	-0. 039		
I 2-	+ 1	+0.007	+0.014			+0.017	+0.034		
—I 2·	+ 2	+0.098	+0.023			+o. 177	+0.045	-0.007	+0,002
0 2-	+ 1	-0. 251	0. 060	+0.005	0.000	0.611	—0. 145	+0.024	0.000
I 2	0	+0. 1755	+0.0385	0. 0035	-0.0002	+0.6443	+o. 1391	-0. 0231	0. 0041
—I 2-	+ 1	0, 0250	+0.0311	-0.0031	+0.0060	—о. обо8	+0.0774	-0.0142	+0.0228
0 2	0	+o. o486	-o. o838	+0.0111	— 0. 0197	+0. 1744	0. 3078	+0.0600	о. 1063
I 2-	- I	-0.0292	+0.0502	-0.0089	+0.0164	—o. 1915	+o. 3287	o. o655	+0.1156
—I 2	0	+0.0017	0.0074	0. 0030	-0.0053	+0.0087	-0.0052	-0.0010	—o. o2o6
0 2-	1 —	+0.00899	+0.01147	+0.00725	+0.00839	-0.00175	+0.01928	+0.01229	+0.01990
I 2-	— 2	0. 0006	-0.0023	0. 0040	0.0053	+0.0017	-0. 0302	-o. o155	-0.0079
—I 2-	— ı	+0.0091	0.0097	+0.0154	-o. oo68	— 0. 0656	0.0 098	+o. 0823	0.0450
0 2-	— 2	0.0016	+0.0097	-0. 0098	+0.0055	+0.0603	+0.0108	-0. 06 11	+0. 0378
I 2-	- 3	+0.006	-0.007	—о, ооз	+0.001	-0.019	+0.003	0.001	0.002
—I 2-	— 2	+0.011	0. 053	+0.001	-0,016	+0.054	-0. 203	+ 0.02 0	-o. o51
0 2-	— 3	-o. o15	+0. 069	0, 002	+0.016	o. o51	+0. 199	-0. 021	+0.053
1 2-	— 4	+0.004	-0.015			+0.007	o. o59	+0.004	o. o16
— I 2-	- 3	+0.065	+0.015	+0.005	+0.001	+o. 260	+0.055	+0.039	+0.007
0 2-	4	-0.074	o. o16	-o. oo6	0.000	—0. 25 I	0. 043	-0.040	-0.007
I 2-	— 5	+0.023	+0.004			+0.078	+0.012	+0.012	+0.002
_ı 3-	+ 2	—o. oo5	+0.013			0.007	+0.015		
	+ 1	+0.013	-0.020			+0.019	o. o33	'	
1	+ 0	0.008	+0.003			-0.019	+0.009		
	+ 1	-0.001	+0.104			0,000	+0.171	0.000	0. 005
	0	+0.0033	—o. 2541	+0.0010	+0,0039	+0.0010	-0.6243	-0.0012	+0.0209
	— т	0, 0006	+0.1351	0.0001	-0.0029	-0.0005	+o. 6625	+0.0016	0. 0227
	_ o	-0.0110	-o. o164	-o. oo65	-0,0020	+0.0132	_0. 0215	+0.0096	+0.0051
	- I	+0.04018	+0. 02187	+0.02197	+0.00701	+0.02698	+0.04735	+0.02552	+0.00624
· ·	_ 2	-o. o185	-o. oo68	-0.0175	-0.0054	0. 0487	-0.0614	-0.0442	-0.0120
1	- 1	+0.0019	-o. ooog	+0.0031	0.0017	-0.0155	-0.0075	+0.0155	-0.0143
	_ 2	-0.0019	+ 0. 0 064	0.0051	+0,0030	+0.0110	+0.0072	-0.0119	+0.0186
ــــــــــــــــــــــــــــــــــــــ									,

A	rg=	An	δz	B(v-	o) + Xc	$\mathbf{F}n$	'δz'	G(u'	— c')
нγ∓	i'g'+ig	sin.	cos.	sin.	cos.	sin.	cos.	sin.	cos.
ж	i' i	"	"	"	//	"	"	"	//
ı	3-3	0.0007	+0.0017	+0.0033	—o. oo38	+0.0017	+0.0023	+0.0002	0.0148
—I	3— 2	+0.0092	+0.0019	+0.0075	+0.0090	-0.0057	0.0714	+0.0806	+0.0989
0	3— 3	-0.009	0. 003	-0.006	0,004	+0.006	+0.066	-0.072	—o. o85
I	3— 4	+0,010	+0.009	+0.003	+0.004	0.006	0.022	+0.017	+0.021
_I	3— 3	+0.046	0.000	+0.007	0.003	+0. 176	+0.001	+0.047	+0.004
°	3— 4	0. 056	0,000			—0. 167	+0.002	—o. o47	-0,004
I	3— 5	+0.013	0.000			+0.051	0.006	+0.013	-0,001
I	3— 4	0.000	+0.051			+0.007	+0. 191	0,000	+0.027
°	3— 5	0,000	0.051			-0.013	o. 186	-0.001	0. 026
I	3— 6	0.00	+0.02			0.00	+o. o6		
—ı	4+ I	+0.001	0.004			+0.001	0.003		
0	4 0	0.003	- -0.005			о. 003	+o. oo6		
1	4 1	+0.022	-0.023			+0.059	o. o46	—o. ∞5	+0.002
-1	4 0	+0. 0187	0. 0034			+0.0228	-0.0042	— 0. 0006	+0.0005
0	4— I	+0.0188	0.0051	-0.0004	0. 0004	+0.0452	—o. 0100	-0.0025	o. 0013
1	4-2	0.0001	+0.0004	+o. ooo6	+0.0002	0. 0829	+0.0173	+0.0041	+0.0010
_I	4— I	-0.0007	+o. 0064	0.0006	+0.0005	—0. 0128	+0.0078	-0.0025	+0.0342
۰	4 2	+0.0009	+0.0040	0.0010	+0.0062	+0.0093	+0.0005	-o. oo18	+0.0066
1	4- 3	—0. ∞18	+0.0048	+0.0007	+0.0083	-0.0015	-o. oo73	+0.0052	0. 0442
—I	4- 2	+0.0190	-0. 005 I	0.0003	+0.0015	+0.0926	-o. o532	0.0032	+o. 03 2 2
٥	4- 3	0. 031	+o. oo8	0.000	—о. 003	о. 089	+0.049	4-0.006	-0. 025
1	4— 4	+0.014	0,001	+0.002	+0.001	+0.023	—0. 013	+0.002	+0.006
-1	4 3	+o. 018	-0.012	0. 015	+0.019	+0.069	0.031	—o. o67	+o. o83
٥	4— 4	-0. ozo	+0.020	+0.021	—0. 023	—0. 070	+0.032	+0.061	o. o78
1	4— 5	+0.∞3	-0.004	0.005	+o. oo6	+0.014	0. 006	-o. o18	+0.020
_I	4— 4	+o. oo8	+0.030			+o. o31	+0, 130	+0.004	+o. o31
0	4 5	0.005	-0.030			-o. o32	0, 126	0.005	0. 030
I	4— 6	ļ				+0.014	+0.037	0.001	+0.004
I	4 5	—о. озз	+0.006			—0. 132	+0.030	—о. 017	+0.004
0	4— 6	+0.04	O. OI			+o. 13	0. 03	-0.02	0.00
I	4— 7					-o. o ₃	+o. oi		
_1	5 O	+0.0018	-0. 0003						
0	5— I	+0,0002	-0.0027			+0.0009	_o.ooo8		
I	5— 2	-0.000238		-0.000045	+0.000058	-o. oo1018	+0.000577	0.000465	+0.000250
1 —	5— I		+0. 034556	-0. 000364	—o. ooo530	-0. 004851	-0.001226	0. 000659	-0.002451
0	5— 2		+0.0000259		+0.0004938		-0.0011941		+0.0007744
г	5— 3	+0.014445	+0.034941	-0.000250	-0.000091	+0.000247	+0,003908	+0.000777	+0.001324
_ı	5— 2	-0.000892	-0. 004138	-0. 004603	+0.000805	+0.046018	_o. o3748o	-o. o39 5 62	+0.006578
0	5 3	—0. 0109	+o. oo68	-0.0019	-0.0004	-o. o352	+0.0335	+0.0194	0. 0039
ı	5 4	0. 0034	0.0023	+o. 0059	—o. ooo7	-0.0015	-0.0100	+0.0175	-0,0010
—1	5-3	+ 0.009	+o. o31	0. 002	-0,002	+0.071	+0.071	0.029	+0.016
0	5 4	_o. o13	-0. 045	0.001	+0.002	-0.072	0. 070	+0.033	0 . 01 6
ī	5- 5	+0.004	+o. o16			+0.020	+0.023	o. oo7	+0.001
—ı	5— 4		+o. o18	0. 024	o. o16	- -0. 046	+0.054	0. 067	_o. o33
0	5— 5	-0.027	 0. 024	l	+0.018	— 0. 047	-0.057	+o. o66	+o, o3o
		17			<u>.</u>				

A	rg=	An	δz	B(v	c) + Xc	$\mathbf{F}n'$	$\delta z'$	$\mathrm{G}(u'$	— o')
ку+	-i ⁷ g'+ig	sin.	cos.	sin.	cos.	sin.	cos.	sin.	cos.
н	i' i	"	//	11	11	"	"	"	11
1	5 6	+o. o16	+0.010	-0.007	-0.004	+0.002	+0.009	-o. o19	0. 010
—1	5— 5	-0.019	+0.007			—о. o88	+0.047	0. 020	+0.007
0	5 6	+0.021	-0.010			+o. o86	— о. 047	+0.020	-0.007
	5 7					-0.02	+0.01		
I	5— 6	-o. oı	0. 03			0. 04	— 0. 09		
0	5 7	+0.01	+0.03			+0.04	+o. o8		
I	5— 8					o. ot	O. O2		
1	6- 2					0.0002	0.0006		
—ı	6— і	+0.0036	+0.0023			—о. 0098	-o. oo57	-0.0002	0. 0001
۰	6 2	+0.0002	0.0000			+0.0005	0.0004		
1	6— 3	+0.0032	+0.0027			+0.0079	+0.0074	0.0001	—о. 0003
-I	6— 2	-0.0001	0. 0007	+o. ooo6	0, 0004	+0.0757	—o. o735	+0.0025	+0. 0183
٥	6— 3	—0. 0167	+0.0124	0. 0009	+0.0006	0.0412	+0.0468	-0,0024	0, 0070
1	6— 4	o. o16o	+0.0115	+0.0007	0. 0005	·—o. o236	+o. oo56	+0.0025	+o. oo46
_I	6— 3	+o. oo61	+0.0093	—0. 0031	0.0070	+0.0857	+0. 1768	0.0430	0. 1255
0	6— 4	-o. oog	-o. o17	+0.003	+0.004	0. 082	—о. 167	+0.040	+o. 116
I	6— 5	-0.001	-0, 004			+o. 02I	+0.044	0, 011	0. 028
—I	6— 4	—o. o27	+0.013	-0.002	0.002	0. 030	+o. 017	-0. 027	-0.024
٥	6 5	+0.034	-0.017	+0.007	0. 002	+0.030	-o. o8o	+0.027	+0.029
I	6— 6	0, 008	+0,006			o. o18	+0.018	0,000	о. 006
-1	6 5	0, 011	+0.018	+0.008	-0.021	-o. o33	+0.044	+0.011	—o. o49
0	6— 6	+0.007	-0.017	0.008	+0.022	+0.034	0. 044	o. o16	+0.048
I	6— 7	—0. 0I	+o. or				•	0. 00	-0.01
—I	6— 6	—0, 0I	0.00			0.04	o. o5		
0	6 7	+0.01	0,00			+0.04	+0.05		
I	7- 1	1				-0.0023	+0.0003		
0	7— 2	1				+0.0004	+0.0001		
1	7-3	+0.00065	+0.00029			+0.00257	+0.00138	0. 00037	-0. 00007
—т	7— 2	+0.00006	-0.00012	0, 00006	-0.00026	-0.01954	-o. o6615	+0.00007	+0.00057
0	7-3	+0.00427	+0.00898	+0.00002	+0.00028	+0.02252	+0.04730	-0. 00009	-0.00013
I	7— 4	—0, 0101	—u. 0043	+0.0001	-0.0001	—0. 0268	-o. o119	+0.0003	0.0000
—I	7-3	+0. 1015	+0.0949	0. 0004	+0.0011	+0.5323	+0.4937	-o. oo83	-0.0035
0	7— 4	—о. 19 06	0. 1775	0. 0002	0.0019	-0, 5002	0. 4658	+0. ∞75	+0.0039
1	7- 5	+0. 076	+0.073			+0.139	+0.125	-0.003	+0.001
1	7— 4	-0.017	+0.018	+0.014	-0.007	—о. 135	+0. 120	+0 .0 94	-o. o61
٥	7— 5	+o. o18	—o. o36	0.019	+0.008	+o. 111	—о. 133	-0.092	+0.062
1	7— 6	-0.001	+0.016	+0.005	-0.002	-0.027	+0.040	+ 0. 026	-o. o18
-1	7— 5	—o. o16	-o. o15	-0.002	0.002	о. обз	0.011	+0.016	0. 025
0	7— 6	+0.020	+0.024	4-0.003	+0.010	+0.068	+0.014	-0.020	+0.026
ı	7-7					0.017	0. 010		
-I	7— 6	0.017	-0.002	+o. o16	+0.003	-o. o39	o. o16	+0.034	+0.005
٥	7— 7	+0.03	0.00			+0.03	+0.02	o. o3	-o. oi
1	7— 7			į		+0.02	-0.03		
0	7— 8					-o. oı	+0.03		
L									

Arg=		An	δz	B(v -	c) + Xc	$\mathbf{F}n$	'δz'	$\mathbb{G}(u'$	— c')
$ uy+i^{7}g' $	'+ig	sin.	008.	sin.	cos.	sin.	cos.	sin.	cos.
и i' —1 8-	i 2	"	11	"	11	// 0, 0127	 o. 0138	"	"
o 8-	— 3	+0.00141	+0. co134	+0.00006	+0.00008	+0.01082	+0.00974	+0,00005	+0.00006
r 8-	 4	-0.0022	-o. ooo1			0. 0082	— υ, 000 4	0. 0001	0. 0001
—ı 8-	- 3	+0.0290	+0.0069	+0.0003	0.0000	+0. 2220	+0.0517	0. 0004	+0.0003
o 8-	- 4	0. 0522	—o. o139	—о. 0003	-0.0002	—0. 2024	0. 0519	+0.0001	0. 000 I
1 8-	- 5	+0.0232	0, 0001			+c. 0594	0. 00 10	0.0000	+0.0005
ı 8-	4	-o. 0982	+0. 1620	+0.0007	-0.0020	—о. 3806	+0.6353	+0.0064	o. o158
n 8-	- 5	+ 0. 139	o. 232	0.001	+0.003	+0.359	-0. 612	o. oo8	+0.019
ı 8-	6	o. o53	+0.090			-0. 099	+o. 178	0.000	—о. 006
—r 8-	5	-0. 024	0. 011	+o. o1 1	+0.014	-0. I2I	0. 067	+o. o63	+o. o63
n 8-	— 6	+0.037	+0.003	-o. o13	—о. 016	+0.124	+0.045	—о. об4	—0. 061
r 8-	- 7	0.012	+0.004			-0. 040	0. 007	+o. o16	+0.018
_r 8-	— 6	+0.001	o. oro	+o. oo8	-o. oo3	0.003	o. o48	+0.023	+0.006
o 8-	- 7	-0.002	+0.013	o. oo8	+0.004	+0.002	+0.048	0. 019	0.011
1 8-	8					0.00	o, oi		i
—ı 8-	- 7	_o. or	0. 02	0.00	+o. or			0.00	+0.02
o 8-	8	0.00	+0.02					0,00	o. oı
									- 1
—ı 9-	_ 2					—о. 0030	0.0013		- 1
0 9-	- 3					+0.0023	+0.0009		- 1
1 9-	- 4	-o. ooo3	+0.0001			0.0013	+0.0006		- 1
—ı 9-	— з	+0.0043	0. 0014			+0.0436	-0.0142	o. ooo1	0.0000
0 9-	- 4 l	0.00774	+0.00210	-0.00008	+0.00010	-0. 03947	+0.01114	-0.00009	+0.00004
1 9-	– 5	+0.0027	0. 0027			+0.0091	0.0091		
_r 9-	- 4	—υ. 0028	+0.0555	0.0001	0.000I	-0. 0112	+o. 2873	_o. ooo8	—0. 0029
0 9-	- 5	+0.005	-0.079			+0.013	—0. 269	+0.001	+0.001
1 9-	6	+0.004	+0.031			+0.009	+o. o8o	-0.001	0.002
—ı 9-	5	—0. 169	—o. o58	+o. oo6	+0.002	—0. 595	0. 202	+0.023	+0.004
0 9	6	+0. 217	+0.073	-o. oo6	0. 002	+0.574	+o. 188	-0. 020	0.007
1 9-	- 7	-o. o81	0. 026			0. 170	-o. o54	+0.010	+0.001
—I 9-	_ 6	-o. oo3	0. 017	0. 009	+0.012	+0.017	-0.092	o. o37	+o. o6o
0 9-	- 7	+0.013	+0.025	+o. o1o	-o. o13	+o. oo6	+0.096	+o. o33	o. o58
1 9	_ 8	-o. oo7	0.008			-0.008	-o. 029	-o. oi i	+0.015
—ı 9-	7	+0.002	—о. 007			+0.028	—o. oo8	-0. 004	+0.009
0 9-	_ 8	0.00	+0.01			0. 03	+o. or	+o. o1	0.00
	1								
-1 10-	- - 3	+0.00035	—u. 00041			+0.00491	-o. oo586	+0.00002	—0. 00002
0 10-	- 4	0. 0007234	+0.0007572	—о. 0000064	+0.0000076	o. oo45060	+0.0047523	—o. 0000156	+0. 0000140
1 10-	5	0. 00001	_o. ooo5o			+0.00011	-0.00230	+0.00001	-0.0000I
—I IO-	 4	+0.00504	+0.00965	0.00000	+ 0. 00005	+0, 03203	+0.06083	0. 00022	-0.00014
0 10-		o. oo65	_o. o133		'	0. 0274	-o. o56 7	+0.0001	0.0000
1	_ 6	+0.004	+0.004			+0.013	+0.013	[
—I 10-	- 5		+0.010	+0,001	0.000	—o. 286	+0.047	+0.004	-o. ooi
	_ 6	+o. o85	0. OI 2			+0. 274	-0.041	-0.003	0.000
I 10-		o. o31	+0.009			_o. o81	+0.023		
_I 10-	_	+0.017	-0. I42	o. oo i	+o. oo6	+0.053	-0. 476	0. 002	+0.021
		, ,		.,	<u> </u>	L		<u> </u>	

1 10— 8 —1 10— 7	sin. -0. 018 +0. 006 +0. 007 -0. 010 0. 00		sin. " 0.000 0.010 +-0.011		sin. // -0.039 +0.011	cos. // +0.462 -0.138	sin. +0.003	008. // 0. 020
0 10— 7 1 10— 8 —1 10— 7 0 10— 8 1 10— 9	-0.018 +0.006 +0.007 -0.010	+0. 175 -0. 059 -0. 006 +0. 016	0.000	o. 007 o. 005	-0.039 +0.011	+0.462	+0.003	
5 10— 8 1 10— 9	-0.010	+0.016				-1.25	0.000	+0.009
1 1	0.00	-0.01			+0.060 -0.060 +0.01	-0. 015 +0. 034 -0. 01	0. 045 +0. 038 0. 01	—0. 015 +0. 017 0. 00
					0.00	-0, 02	5, 51	5. 55
1 1	+0.0014	+0.0009 0.0013			-0.0002 +0.0109 -0.0097	+0.0009 +0.0068 -0.0065	+0.0001 +0.0002	o. 0000
-1 II- 5	+0.0010 -0.0123 +0.016	+0.0002 +0.0096 -0.011			+0.0037 -0.0632 +0.060	+0.0004 +0.0500 -0.046	+0.0003 0.001	0.0003 +0.001
i ii 6	-0.005 -0.023 +0.028	+0.006 -0.063 +0.073			0. 015 0. 093 +-0. 086	+0.018 0.241 +0.232	+0.002 -0.002	+0.004 0.004
-i ii- 7	-0. 012 +0. 106 -0. 124	—0. 026 —∪. 011 +0. 016	0.006	0.000	0. 034 +0. 338 0. 327	0. 068 0. 038 0. 046	-0. 019 +0. 025	+0.002 0.003
-1 11-8	+0.04 +0.01 -0.02	0.0I 0.0I			+0. 10 +0. 02 -0. 03	-0.01 +0.04 -0.03	0.00	0.03 +0.03
0 12-5	0. 00032	0, 00002			0. 00192 0. 0070	-0.00008 +0.0171	-o. oooo 1	0.00000
1 1	-0.0011 +0.0014	+0.0029 0.0033			+0.0062	-0.0141 +0.005		:
0 12- 7	-0.013 +0.017 -0.008	0. 012 +0. 014 0. 004			0. 062 0. 059 0. 020	0. 054 +0. 052 0. 012	+0.002	o. ooi
12— 8	+0.047 -0.055 +0.019	-0. 031 +0. 035 -0. 014			+0. 176 -0. 171 +0. 047	-0. 113 +0. 109 -0. 034	o. 003 o. 007	+0.002 0.004
—I I2— 8 D I2— 9	+0.024 -0.03 +0.01	+0.071 -0.08 +0.02			+0.078 -0.07 +0.02	+0. 218 -0. 20 +0. 05	-0. 006 +0. 01	-0.018 +0.02

A	rg=i'g'+ig	Cé	$\delta rac{h}{h_0}$	D _č	u cos i	$\mathbf{E}_{ar{\mathbf{c}}}$	u ₁	H-c	<u>u'</u> os i'
A)T	* y T *y	sin.	cos.	sin.	cos.	sin.	cos.	sin.	cos,
ж	i' i	"	"	"	"	"	"	"	"
°	0 0	0	+0.00002191		+0.00000013		-0.00000016		—0.00000005
1-1	0 0	+0.0008224	1	0.0000073	+0.0000180	0.0000001	-0.0000005	-0.0000052	+0.0000315
l °	0 I	-0.0020	+0.0004						
-r	1+1	+0,0002	-0.0002						
°	1 0	0.0007	+0.0003						
I	I— I	+0.0001	-0.0001						
-I	I 0	+0.0001	-0.0009	}					
°	I— I	0,0000	+0.0010						
1.	I— 2	-0,0002	0, 0006			·			
1-1	1—1	+0.0003	+0.0006	1.0.00001	L 0. 00000	0.00007	0.00007	La accesa	1.0.00000
l °	2— I	-0.0003 -0.0001	+0.00021	+0.00001	+0.00002	0.00001	0,00001	+ 0.00002	+0.00002
i	2— I		+0.0002						
l °	2— 2	+0.0014 0.00000	-0.0006						
l.°	3— 1	0,0000	+0.00009						
"	3— 1	_0, 0002	-0.0002 +0.0003]
i .	3-2	+0.0002	0.0000					•	
	4-2	+0.0002	-o. ooo6					1	
1	4— 2 5— 2	+0.000003	0.000007					1	
-1	5— 1	+0.000004	+0.000007					-0,000023	0.000043
	5— 2	-o. ooooog6	I '	-0.0000046	0.0000113	±0.0000072	+0.0000138	1	+0.000050
ľ	5 — 3	0. 000000	+0.000001	0,000040	0.0000113	7 0,00000/2	1 0.0000130	F0,0000032	7-0.0000030
]_1	5— 3 5— 2	+0.000053	0.000087					I	
	7-3	_0.00011	_0.00006						
	7 3	-0.0005	_0.000I						
0	10-4	-0.0000002							
				l				L	

CHAPTER XI.

CALCULATION OF THE PORTION OF ST FACTORED BY nt.

In determining the part of δ T having the factor nt a degree of precision 300 times greater than that used in deriving the part not multiplied by nt has been employed. In the following table the factor nt has been omitted, and for convenience all the coefficients have been multiplied by 100000:

Arg=	An	δz	Β(ν	— c)	Fn	'δz'	G(u'	— c')
$\begin{array}{c} \text{Arg} = \\ n\gamma + i'g' + ig \end{array}$	sin.	cos.	sin.	cos.	sin.	cos.	sin.	cos.
н i' i	"	,, + o. 4688	11	" + 0.5821	"	//	11	11
1 0— 1	+ 0. 2857	+ 0. 1514	+ 0. 5551	- o. 7368	— O. 1425	0, 0984	+ 0.4297	+ 0. 2221
-1 0 0 I	— 4. 3819	— 4. 8170	4. 2330	 4.7314	+15. 2806	+ 5.6172	—36. 2745	— 13. 3821
0 0— I					— 8.4	— 3. т	+18.7	+ 6.9
1 0 2	— 4. 406	— 4. 835	+ 4.307	+ 4.744	— 4. 162	— I. 536	+11.244	+ 4. 181
-ı o- ı			+ 1.0	— o. 1	— 1. 1	+ 0.6	+ 3.1	— 1.8
0 0 2					+ o.6	- 0,3	— 2 . o	+ I.2
1 0— 3	0.0	— 0.4	- 0. 2	+ 0.2	0.0	— o. i	+ 0.1	+ 0.5
_I I+2	+ o. i	— o. 8	+ o. 1	+ 1.1			- I.O	+ 0.9
0 1+1				,			— o. 8	+ 2.8
1 1 0	+ o. 21	0.70	+ 0.18	— o. 98	- 0.21	+ 0.08	+ 2.26	4.78
-ı ı+ı			— 7.80	— 4.70	— o. 28	— o. 33	-17.94	 28.80
0 1 0	+ 2.89	+ 1.82	+ 5.08	+ 3.14				
1 1-1	+ 2.91	+ 1.66	+ 1.97	+ 1.01	+ 0.13	+ o. 65	+18.03	+ 28.63
—I I O	— o. 53	+ 0.33	— o. 51	0. 14	+ 7.52	— 9· 44	4. 70	+ 8.14
o I— I	— o. 15	— 1. o3	— 0. 18	- o. 35	− 4. 39	+ 7 ⋅94	+ 2.42	7. or
I I— 2	— o. 7	+ 0.4	+ 0.9	+ 0.5	- 1.0	— 5.o	+ 1.1	+ 4.5
-ı ı- ı			+ 5.4	- 7⋅3	—19. I	+126. o	+16.6	—110. o
0 I— 2	+ 2.0	- 2.7	- 3.5	+ 4.8	+17.9	—118. 7	15. 1	+ 99.6
I I 3	+ 1.9	— 2. 7	— I.4	+ 1.9	5.1	+ 32.4	+ 3.6	— 22.4
—I I— 2			o. 3	+ 0.6	+ 1.6	+ 2.4	— o. 5	— o. 9
o 1— 3					— I.O	— 7.o	+ 0.3	+ 4.8
I I— 4					+ 1	+ 3	- 1	2
I 2 0					0.0	— O. 2	— o. 1	— o.6
_1 2+ I	+ 0.1	— o. 3	— 2. 2	+ o. 8	- 1.9	— o.8	5. I	— 2.4
0 2 0	+ 0.90	— o. 81	+ 1.65	— 1.42				
I 2— I	+ 0.13	+ 1.72	+ 0.30	+ 0.86	+ 1.71	+ 1.15	+ 4.59	+ 2.78
— I 2— 0	+ 7.77	-22. 53	+ 6.98	—20. 37	+12.73	— 14.54	+27.71	- 24. 59
0 2— 1	-14.743	+42.566	8. 649	+24. 918	— 6.893	+ 8.672	14. 455	+ 12.172
I 2— 2	+ 6.00	-17.48	+ 2.20	- 5⋅73	— 3.97	+ 1.84	— 8. o <u>5</u>	+ 9.01
								L

Arg=	An	δε	Β(ν-	- c)	$\mathbf{F}n'$	$\delta z'$	G(u')	— c')
κγ+i ⁷ g'+ig	sin.	cos.	sin.	cos.	sin.	cos.	sin.	cos.
κ i' i -1 2- 1	1. 06	1. o6	1.08	 — 2. 95	+ 13.59	" + 38.64	 11. 93	,, —22. 98
5 2— 2	— o. 4	+ 2.8	+ 1.6	+ 3.6	11.6	- 35.4	+10.0	+21.0
1 2-3	+ 1.7	_ 2.3	— 1, 2	- 0.4	+ 5.7	+ 8.7	_ 4.8	- 4.6
I 2 2	-21.8	— 9.8	+19.8	+ 9.0	127.5	+ 7.4	+95∙4	 5⋅3
0 2-3	+41.0	+18.5	—24. I	—1o. 8	+121.9	- 8.5	88.9	+ 5.8
1 2-4	—16.9	7.7	+ 5.6	+ 2.5	— 35. ²	+ 2.5	+23.4	- 1.4
_1 2-3	— T. I	+ 0.9			— 4.6	+ 4.4	+ 2.7	— 2.7
5 2-4	+ 4	0			+ 9	- 7	6	+ 3
I 2 5	l ' '				- 4	+ 2	+ 2	_ I
				105				100
—I 3+ I			— 0. 2	+ 0.5	— o. 5	+ 0.1	0.6	+ 0.2
0 3 0	+ 0.1	— 0. 3	+ 0.1	0.5	1 0 65	1 0 777		L C 12
I 3— I	+ 0.12	+ 0.31	+ 0.13	+ 0.13	+ 0.65	+ 0.17	+ 0.92	+ 0, 12
—I 3 0	0.60	- 5.02	— I. 75	— 5. 18	- 5.07	— 11.66	— 2. 78 ⊥ 3. 282	—12.19
0 3-1	+ 1.035	+ 9.281	+ 1.899	+ 5.889	+ 5.221	+ 7.980	+ 3.382	+ 7.340 + 0.63
I 3— 2	— I.49	- 3.66	0.92	— I. 23	— 5. 26	— I. 34	— 4. 27	1
-I 3- I	+31.64	+ 4.00	+21.74	+ 2.54	+110.99	+ 77.57	+87.33	+61.02
0 3— 2	—45·75	— 5. 36	25. 03	— 2. 86	104. 07	72.97	—79 . 19	—54. 96
1 3— 3	+18.0	+ 1.9	+ 6.7	+ 1.1	+ 29.2	+ 19.3	+17.5	+13.1
—I 3— 2	— 3·3	— I.4	+ 6.5	- 2.3	— 39. 9	+ 25.5	+28.0	18.9
0 3— 3	+ 4.5	+ 1.6	- 8.4	+ 2.4	+ 33.8	25.9	—29. 2 + 8. 0	+15.3
1 3— 4	+ 6.8	+ 0.4	+ 2.0	— I.4	— 7·7 — 28.4	+ 10. I —102. I	+19.1	— 5⋅3 +70⋅1
-i 3-3		-31. 2 +44. 8	— 4.9 L f f	+21.8	+ 28. 7	+ 97·3	—18. <u>5</u>	65. 7
0 3— 4 1 3— 5	— 9. 3	18	+ 5.5 - 1	—25.0 + 6	— 8	— 29	+ 5	—03.7 +19
, ,	+ 4	- 2		+ 0		— 29 — 5	+ 6	+ 2
-I 3-4	_ 2	l .	— I	— 2		+ 8	- 7	— 5
o 3— 5 1 3— 6	+ 1	+ 5			+ 9 - 3	— 3	+ 2	+ 1
] 1 3-0						3	T *	T *
1 4 1					+ 0.1	0.0		_
—I 4 0	— o. 5	— o. 6	- o. 9	o. 6	2.8	— 2. 2	— I. 9	— 1.8
0 4 1	+ 0.75	+ 1.14	+ 0.85	+ 0.64	+ 2.32	+ 1.57	+ 1.42	+ 1.05
I 4— 2	0. 57	— o. 28	— 0. 29	- 0.01	— 1.62	+ 0.15	— o. 86	+ 0.46
—ı 4— ı	+ 8.97	— 3.21	+ 6.40	— 3. 36	+ 43.91	+ 4.55	+28.44	+ 0.76
0 4— 2	—12.80	+ 4.47	— 7. 19	+ 3.65	 40. 16	- 5.09	—24.73	— 1.06
I 4— 3	+ 4.70	- 2.62	+ 1.81	— I. 38	+ 11.40	— I. 69	+ 5.66	— I. 72
—I 4— 2	+ 1.94	+30.08	+ 2.20	+17.88	55.09	+128.13	−34.49	+81.41
0 4-3	- 2.9	—38. 8	— 2.8	-19.9	+ 51.5	—122.7	+31.5	76.6
I 4— 4	+ 1.3	+14.7	+ 0.6	+ 6.0	— 13.9	+ 36.3	— 9. 2	+19.9
—1 4— 3	- 0.2	— 7. 2	+ 4.1	+ 7.9	— 32. o	- 30.8	+23.6	+25.3
0 4—4	+ 0.3	+ 8.7	— 5. I	- 9⋅3	+ 32.0	+ 25. 1	21.0	-27.2
1 4-5	— I	— 3	+ 2	+ 2	— I2	— 6	+ 7	+ 7
— I 4— 4	+30	0	19	— I	+ 69	— 37	-45	+23
□ 4— 5	-38	0	+21	0	66	+ 38	+42	-23
1 4— 6	+14	0	6	0	+ 20	- 11	—12	+ 6
— I 4— 5	+ 2	— 2			+ 2	_ 8	— I	+ 6
o 4— 6	5	+ 3			— 5	+ 9	+ 3	6
I 4-7					+ 2	— 3		
		1						

Arg=	Αı	$\imath\delta z$	Β(ν	— c)	$\mathbf{F}n'$	$\delta z'$	G(u'	— c')
$n\gamma + i^{\prime}g^{\prime} + ig$	sin.	cos.	sin.	608.	sin.	cos.	sin.	COH.
χ i' i I 5 ο	"	"	"	"	" 0, 6	" — 0. 2	" — 0. 3	,,, - 0, I
0 5— 1	+ o. 1	0.0			+ 0.5	+ 0.1	+ 0.2	0.0
1 5— 2	— o. o85	+ 0.022	— o. o34	+ o. o37	— 0. 252	+ 0. 160	- o. o76	+ 0.133
-1 5-1	+ 1. 222	_ I. 348	+ 0.721	_ I. 364	+ 8.316	— 3. 769	+ 4.320	- 2.772
0 5-2	— I. 75368		i e	+ 1.45203	- 7. 55126	+ 3.03722		+ 2. 20560
I 5— 3	+ 0.434	- 0.971	+ 0.076	— o. 486	+ 1.589	- I. 963	+ 0.424	— 1. 100
—I 5— 2	+ 6.034	+ 9.887	+ 4.687	+ 5.942	+ 4.911	+54.892	+ 4.939	+31.254
0 5— 3	− 7.7	-12.7	 5. 2	- 6.5	4.0	-51.7	- 4.3	-28.8
1 5-4	+ 3.6	+ 4.3	+ 1.9	+ 1.7	+ 4.0	+15.0	+ 2.5	+ 7.5
—ı 5— 3	-23.9	+ 5.8	—I2. 2	+ 5.0	—II7. 4	-23.7	—63.6	—I2. I
0 5-4	+28.9	− 7·4	+13.2	- 5.4	+113.2	+21.2	+60.5	+10.4
1 5-5	—10. 8	+ 3. I	— 4·3	+ 1.4	— 34⋅3	— 5. г	—16.8	3.5
—I 5— 4	+ 8.7	_ 2.7	— 7. o	+ 5.9	+ 18.7	—32. 2	18.8	+24.8
o 5— 5	11	+ 3	+ 8	— 7	14	+32	+21	22
ı 5— 6	+ 3	— I	- 2	+ 2	+ 1	-11	— 5	+ 7
—1 5— 5	+ 5	+23	— 3	14	+ 35	+42	21	—2 6
o 5— 6	- 7	28	+ 3	+15	36	39	+22	+25
ı 5— 7	+ 2	+10	1	— 5	+ 11	+11	- 7	- 7
i 5 6	+ 3	+ 1			+ 8	+ 1	— 5	0
o 5-7	- 3	— 4			8	— 3	+ 5	+ 1
-1 6- I	+ 0.03	- O. 29	— o. o7	— O. 29	+ 0.84	— 1.24	+ 0. 27	— o. 73
o 6— 2	- o. 11	+ 0.38	+ 0.02	+ 0. 29	o. 8o	+ 1.05	— 0.27	+ o. 59
ı 6— 3	— o. o6	— о. 18	— o. o6	0.08	— 0.02	— 0. 45	- o. II	o. 15
-ı 6- 2	+ 2.34	+ 1.36	+ 1.81	+ 0.65	+ 7.62	+11.08	+ 4.68	+ 5.18
o 6 3	- 2.91	— 1.76	- r. 95	0. 74	6. 8o	10.42	4.05	— 4. 76
ı 6 4	+ 1.3	+ 0.3	+ 0.7	0.0	+ 3.0	+ 2.4	+ 1.7	+ 0.9
-1 6-3	— 8. 5	+ 7.8	- 4.4	+ 5.1	 53⋅5	+15.9	27.7	+10.2
0 6-4	+10.0	— 9.5	+ 5.0	— 5.9	+ 51.3	15. 1	+26.3	- 9.2
ı 6— 5	— 3. 2	+ 4.0	I.4	+ 1.9	— 14.6	+ 6.7	- 6.9	+ 4. I
—ı 6— 4	— 7.2	—17. 1	— 5·5	— 6. 7	т. т	− 93. 3	— 1 .6	-43. 3
0 6 5	+ 8.7	+19.8	+ 6.2	+ 7.1	+ 2.8	+89. 9	+ 2.5	+41.6
1 6— 6	— 4	6	— 1	— 3	— 2	27	— I	12
—r 6— 5	+ 5	+ 7	— 5	 5	+ 28	+ 7	—24	-11
0 6-6	— 5	_ 8	+ 5	+ 6	— 26	5	+23	+12
ı 6— 7	+ 3	+ 4	<u> </u>	- 2	+ 8	+ 1	7	— 3
—ı 6— 6	—15	+ 7	+ 9	- 4	— 2I	+30	+14	-17
0 6-7	+18	- 9	9	+ 5	+ 20	—29	-12	+17
ı 6 8	— 6	+ 4			— 6	+ 9	+ 3	— 5
-ı 7- ı					0.0	— O. 2		
0 7— 2			!		- 0.02	+ 0.17		
	- 0.02	- 0.02	1000		- 0.05	o. o5	— o. oз	— 0.01
-I 7-2	+ 0.49 - 0.620	+ 0.01	+ 0.37	— 0.09 ⊥ 0.082	+ 2.32	+ 1.10	⊢ I.2I	+ o. 33
0 7— 3 1 7— 4	+ 0. 25	0.032 0.09	— 0. 395 + 0. 10	+ 0.082 u.09	- 2.084 + 0.76	— 1.094 + 0.01	— I. 039 — 0. 22	— o. 310
-I 7-3	— I. 03	+ 2.99	— o. 38	+ 2.01	— II. 08	+11.25	+ o. 33 - 4. 8o	- 0. 11 - 6. 14
0 7-4	+ 1.1	- 3.6	+ 0.2	- 2.3	+ 10.6	—10. 5	+ 4.5	- 5.6
1 7-5	0. 2	+ 1.5	+ o. i	+ 0.7	- 2.2	+ 3.7	— o. 7	+ 2.0

Arg=	An	δz	Β(ν-	— o)	$\mathbf{F}n'$	'δz'	G(u'	— o')
$n\gamma + i^{\gamma}g' + ig$	sin.	cos.	sin.	cos.	sin.	cos,	sin.	cos.
w i' i 1 74	,, — 8. 2		// -5.2			., —43. 9		// 21. 2
0 7—5	+ 9.6	+ 6.2	+5.6	+2.9	+23. o	+42.4	+12. I	+20.4
17-6	— 3·7	_ 2.0	— I. 9	0.7	— 8. 5	-12.0	— 4. 6	5.6
—ı 7— 5	+11.3	- 7.0	+2.8	—4. 9	+66.3	15. I	+26.3	— 6.7
o 7—6	12	+ 8	-3	+5	—63	+17	—2 6	+ 7
I 7— 7	+ 3	— 3	+1	-2	+19	6	+ 7	— 3
—1 7— 6	6	+ 6	+3	— 5	1	+20	+ 5	-19
0 7-7	+ 6	— 6	4	+5	_ 2	-19	5	+19
1 7— 8	— 2	+ 4			+ 2	+ 5	O	- 4
—I 7— 7	— 7	10	+4	+5	21	— 9	+12	+ 5
o 7— 8	+ 9	+10	— 5	— 5	+22	+ 8	-12	— 5
I 7— 9	— 3	- 3			— 7	- 3	+ 3	+ 1
—I 8— 2	+ 0.06	— o. o5	+0.04	0, 06	+ o. 38	o. o6	+ o. 15	··· 0. 07
o 8— 3	— o. o88	+ 0.042	0. 050	+0.047	— o. 373	+ 0.019	- o. 162	+ 0.049
ı 8— 4	+ 0.02	— о. оз			+ 0.09	— o. o8	+ 0.02	0, 04
—ı 8— 3	+ o. 11	+ o. 66	+o. 18	+0.43	o. 88	+ 3.30	— о. 16	+ 1.59
o 8 4	— o. 19	o. 81	— 0, 2 3	0.46	+ 0.91	3.08	+ 0.15	— 1.46
ı 8— 5	+ 0.1	+ o. 3	ŀ		+ 0.1	+ 0.9	+ 0. 1	+ 0.4
—ı 8— 4	— 3. 2	o. 3	—2, o	+0.2	—13.4	— 8. 7	— 6. 7	 3⋅4
0 8 5	+ 3.7	+ 0.3	+2. 1	о. І	+12.9	+ 8.6	+ 6.7	+ 3.5
ı 8 6	— I. 4	+ 0.1			- 4. 2	— I.7	2. I	— o. 5
— I 8— 5	+ 2.8	— 7 ⋅4	+1.4	-4.4	+31.2	26.8	+14. 1	-13.2
o 8 6	— 3. I	+ 8.4	—r. 5	+4.6	—29. 5	+25.6	—12.5	+12.7
ı 8— 7	+ 1	— 3			+ 8	— 8	+ 4	5
— I 8— 6	+ 5	+ 7	+3	+3	+20	+43	+ 8	+14
o 8— 7	— 7	— 9	4	—2	—2I	41	-10	—19
ı 8—8	+ 2	+ 1			+ 8	+13	+ 3	+ 5
—ı 8— 7	— 7	— 3	+4	+2	—14	+ 3	+14	+ 1
8 —8	+ 9	+ 4	— 5	2	+14	4	—14	— I
ı 89	ĺ				— 6		1	
o 9— 3			1		0.04	+ 0.03		
—1 9— 3	+ 0.08	+ 0.09	+0.08	+0.04	+ 0.17	+ 0.61	+ 0.13	+ 0.25
0 9-4	— o. 10	0. 11	o. o8	—o. o5	— 0. I3 — 0. I3	— o. 56	— 0.12 ± 0.07	- 0.23 + 0.04
I 9 5 I 9 4	0. 70	+ 0.32	-0. 4I	+0.30	+ 0. 13 3. 91	+ 0. 14 — 0. 26	+ 0.07 — 1.82	+ 0.15
0 9-5	+ 0.8	- 0.4	+0.5	—o. 3	+ 3.6	+ 0. 2	+ 1.5	— 0. 2 — 0. 2
r 96	'		l		— I. I	+ 0.3	- 0.4	+ 0.3
—ı 9— 5	— o. 3	— 2.9	0.4	—r. 7	+ 5.4	— 13.9	+ 2.0	— 7.0
o 9 6	+ 0.4	+ 3.3	+0.4	+1.8	 4⋅ 9	+12.9	1.6	+ 6.2
1 9-7	1.6		1.0	1.	La6	- 5 1 20	O 	— 2 8
—I 9— 6 o 9— 7	+ 6 7	— I	+3 -3	+1 -1	+26 25	+20 —19	-11 +11	+ 8 - 7
1 9— 8	j ′	_	,	_	+ 7	+ 4	+ 4	+ 2
—1 9—7	— 5	+ 4	-1	+3	—25	+20	6	+ 6
o 9—8	+ 1	- 5	ĺ		+24	21	+ 6	- 7
1 9— 9					— 5	+ 5	<u> </u>	+ 3
—1 9—8	+ 2	— <u>5</u>			5	—I2	+ 2	+ 7
o 9 9	— ı	+ 7	l		+ 5	+ 8	— 2	- 7
		·		•				·

Arg=	An	δz	Β(ν	— c)	Fn'	$\delta z'$	G(u'	-c')
	sin.	cos.	sin.	cos.	sin.	cos.	sin.	cos.
ж i' i —1 10— 3	+0.019	+0.005	// +0. 016		+ 0. 074	+ 0.071	+0. 039	+0. 023
0 10— 4	o. o2o68	o. oo889	-0.01523	0.00131	- o. o6526	— o. o7o65	o. o3376	-0.02171
I 10 5	+0.010	0.002	+0.005	-o. oo3	+ 0.031	+ 0.007	+0.012	—o. oo5
—I IO— 4	o. o98	+0.120	-o. o48	+0.093	— o. 727	+ 0.349	—o. 28o	+0. 205
0 10-5	+o. I	O. I			+ o.6	— o. 3	+0.2	0. 2
1 10— 6		_	1		0.2	+ 0.2	_	_
—I IO— 5	—o. 5	— 0. 6	-0. 4	-o. 3	o. 6	- 3⋅7	o. 6	—1. 6
0 10—6	+0.5	+0.7			+ o. 5	+ 3.5	+o. 5	+1.5
1 10-7					- 0.4	I. I		
—ı 10— 6	+2.3	—0. 8	+1.3	—о. б	+12.3	+ 1.9	+5.7	+o. 3
0 10 7	-3	+1	1	+1	—11	- 2	<u></u> 6	—I
1 10— 8					+ 4	0	+1	O
—I IO— 7	o	+4	0	+2	—to	+22	-3	+9
o 10— 8	—I	-4			+10	22	+4	— 9
1 10-9					— 2	+ 6	—I	+3
—ı 10— 8					17	-14	4	+1
0 10—9					+17	+14	+4	+1
—I II— 4			l		- o. o7	+ 0.11	O. OI	+0.05
0 11 5			<u> </u>		+ 0.07	— o. 10		
—I II— 5	o. I	—о. 1			o. 5	- 0. 2	0. 3	— 0. 2
0 11 6					+ 0.5	+ 0.7	+o. 3	+0.2
—ı 11— 6	+0.5	0.5			+ 3.3	I. 2	+1.3	_o. 8
o 11— 7					— 3. 2	+ 1.1	-I. 4	+0.7
1 11—8				,	+ 1	— I		
—I II— 7	+1	+1			ō	+ 9	0	+5
o 11—8	-2	_I			o	— 9	0	-4
1 11-9			ł		О	+ 3		
-ı ıı— 8	-3	+1			16	— 4	8	—I
o 11— 9					+16	+ 4	+8	+1
0 11—10					- 5	+12	—I	+5
0 12-5	o. oo1	0. 005			+ 0.001	- 0.020	0. 002	-o. oo7
—I I2— 5					o. 15	— o. o6	— о. об	0.00
I I2 6			ļ		+ 0.6	— o. 6	+0. 2	0. 3
0 12-7]				o. 6	+ 0.6	·	
—I I2— 7					+ 1.6	+ 2.6	+o.8	+1.1
0 12 8	1				- 2	— 3	I	_I
—ı 12— 8					— 7	+ 2	— 3	+1
0 12 9					+ 7	_ 2	+3	I
—I I2— 9					0	-10	-1	5
0 12—10	1				о	+ 9	0	+5
L	<u> </u>		<u> </u>	<u> </u>				

277+4'9'+ig sin. cos.	Arg=	C8	$\delta rac{h}{h_0}$	$D_{\overline{cc}}$	u os i	E	u ₁ 0s i	$_{ m H_{ m ar{c}}}$	u' os i'
	κγ+i'g'+ig	sin.	cos.	sin.	cos.	sin.	cos.	sin.	cos.
$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$		"		"		"	1	"	"
1	1 0 1	0.0000	0.0012	0.0003	о. 1848	o. ooo i	+o. 1850	0.0079	+0.0005
-I I I I I I I I I I I I I I I I I I I	-I O O	+0.0011	+0.0051	+0.0479	+0.0077	0, 002I	-0. 0169	+0. 1239	0. 0250
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	I 0 2	+0.001	+0.∞5	-0.011	0.000	+0.003	-0.007	-0.024	0. 022
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	-I I+I				•			+0.05	+0.09
0				-0,02	o. o3			o. oI	0, 04
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	—ı ı— o	+o. o1	+0.07	+o. 10	-0.02	—о. 13	+0.02	+0.07	-o. o3
$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$	0 I— I	o. o3	<u> </u>	о. 18	+0.03	+0.19	0. 04	-0.04	+0.01
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	I I 2			+o. t	o. 1			о. 1	0.0
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	_1 _1 _1					l		0, 0	+o. I
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	—I I— 2					1		0.7	o. 5
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	-ı 2+ ı			+0.3	+o. 1			+0.4	+0.2
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	0 2 0			—о. 13	0.05	+0.13	+0.05		
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	I 2— I			-0.07	-0.02	0. 0 9	-o. o3	0. 42	-o. 16
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	—I 2 0	+0.05	-o. oı	0.00	o. o3			o. o8	1 .
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	0 2— I	o. 111	+0.020	o, o18	+0.031	+o. o25	o. o37		' '
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	1 2-2	+0.07	0, 02	+o. o3	0. 02	Ì		I '	
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	—I 2— I	0.45	+0. 19		1	o. o5	O. I 2	I '	'
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	1			0. 1	—0, 2	İ		0. 2	—6. §
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	1 2-3	— 0. 4	+0.2						
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	I 3 I]						-0. 10	+0, 01
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	—I 3 o	Į		0, 04	+0. 24	+0.01	—0. 06	o. o 8	
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	· ·	0, 018	+0.013	+0.022	0. 170		1		
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	*	_	1.			· .			
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	_		1 1	+0.02	-0.02	0, 02	-0.02		
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	•			10.		İ		l	
$\begin{array}{cccccccccccccccccccccccccccccccccccc$		i .	. *	+0,1	0.0				
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	3-3	70.4	70.3						
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	— I 4— 0							l '	
$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$	1 '			-0,02	0.05				
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$				0.00	10.00		0.00		
$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$	1	0.00			1				
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	1				1		3.00		
$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$	į.	3.09	3.04						
$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$,		ł		ļ		
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$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$			l I		1 1				
$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$		4							
$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$		_0,019	75.003			70.005	+0.019		
$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$				0.0	70.1				
o 6-3 +0.04 +0.04 +0.05 +0.07									1
		1							
+0.2 +0.1				70.04	+0.04				
								+0.2	+0.1

$\begin{array}{c} \text{Arg} = \\ \varkappa_{\gamma} + i'g' + ig \end{array}$	$\mathrm{C}\deltarac{h}{h_0}$		$\mathrm{D}rac{u}{\cos i}$		$\mathbf{E}_{\overline{\mathbf{c}}}$	$\frac{u_1}{\cos i}$	$\mathbf{H} \frac{u'}{\cos i'}$	
27 T V Y T V Y	sin.	cos.	sin.	cos.	sin.	cos.	sin.	cos.
π i' i -1 7-2 0 7-3 -1 7-3 0 8-3 -1 8-3 0 10-4 -1 10-4	"	"	,,, —0. 03 +0. 018 +0. 04 0. 00 +0. 00068 +0. 004	., 0.00 +0.005 -0.05 -0.02 +0.00067 -0.003	u.	"	" -0.04 +0.030 +0.08 +0.007 +0.01 +0.00141 +0.009	" -0.01 +0.010 -0.10 -0.001 -0.05 +0.00132 -0.007

CHAPTER XII.

SECOND-ORDER PERTURBATIONS OF THE MEAN ANOMALY AND RADIUS-VECTOR OF JUPITER,
ARISING FROM THE MUTUAL ACTION OF THIS PLANET AND SATURN.

When the eight terms of δT , given in the two preceding chapters, are added the following expression is obtained:

Amaran Islah Isa	8	т
$Arg = \varkappa_{\gamma} + i'g' + ig$	sin.	cos:
κ i' i ο ο ο ι ο— ι —	+0.0533 + 1.1197nt -0.2260338-29.4310nt	" ",0.0000704+ 1.0520nt0.0088 0.4622nt +-0.2563282 17.3424nt
0 0— I I 0— 2 —I 0— I 0 0— 2	+0. 2412 +10. 3nt -0. 064 + 6. 952nt -0. 474 + 3. 0nt +0. 486 - 1. 4nt	-0. 2703 + 3. 8nt +0. 094 + 2. 530nt -0. 356 - 1. 1nt +0. 351 + 0. 9nt
I 0-3 -I 0-2 0 0-3 I 0-4 -I 0-3 0 0-4	0. 159 0. 1nt +-0. 408 0. 406 +-0. 140 +-0. 010	-0. 100 + 0. 2nt -0. 318 +0. 342 -0. 113 -0. 063 +0. 08
1 0-5 -1 1+4 0 1+3 1 1+2	-0.03 +0.01 +0.031 -0.079 +0.060	-0.02 -0.022 +0.051 -0.021
-I I+ 3 0 I+ 2 I I+ I -I I+ 2 0 I+ I	+0. 106 -0. 321 +0. 290 +0. 139 - 0. 8nt -0. 489 - 0. 8nt	-0. 211 +0. 636 -0. 624 +0. 145 + 1. 2nt -0. 426 + 2. 8nt
-1 1 0 1 0 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1	+0.4840 + 2.44nt $-0.0616 - 25.97nt$ $+0.1491 + 7.97nt$ $-0.1322 + 23.01nt$ $-0.0487 + 1.83nt$	+0. 4225 — 6. 38nt +0. 0138 — 33. 74nt -0. 1067 + 4. 96nt +0. 1016 +31. 88nt -0. 0888 — 1. 07nt
0 I— I I I 2 —I I— I	+0.0466 — 2.36nt +0.0053 + 0.3nt -0.3133 + 2.9nt	+0.0463 - 0.59nt +0.0248 + 0.3nt -0.1696 + 8.8nt

		δΤ
$Arg = \varkappa_{\gamma} + i'g' + ig$	sin.	608.
н i' i	п п	" "
0 I— 2	+0.330 + 1.3nt	+0.178 — 17.0nt
I I 3	-0.101 - 1.0nt	-0.041 + 9.2nt
—I I— 2	+0.203 + 0.1nt	-0.443 + 1.6nt
o 1— 3	0. 198 — 0. 7nt	+0.451 - 2.2nt
1 1-4	+0.053 ont	-0.146 + Int
—I I— 3	+0. 281	+o. 226
0 I—4	o. 296	o. 216
I I— 5	+0.11	+0.08
-ı 2+ 3	+0.030	+0.023
0 2+ 2	o. o62	0.060
I 2+ I	+0.024	+0.048
—I 2+ 2	+o. 268	+0.070
0 2+ 1	o. 8 ₃₃	0. 205
I 2 0	+0.7932 - 0.1nt	+0. 1733 — 0. 8nt
-ı 2+ I	-0. 1031 - 8. 4nt	+0. 1373 — 2. 4nt
0 2 0	+0.2941 + 2.55nt	—0. 5176 — 2. 23nt
I 2— I	-0.2951 + 6.15nt	+0.5109 + 6.30nt
—I 2 O	+0.0064 + 55.16nt	-0.0385 - 82.14nt
0 2— I	+0.02677— 44.811nt	+0.05928+ 88.390nt
I 2— 2	—u. 0184 — 3. 66nt	-0.0457 - 12.44nt
—I 2— I	+0.0411 — 0.78nt	-0.0711 + 12.15nt
0 2-2	—0.0108 + 0.2 <i>nt</i>	+0.0632 — 9.1 <i>nt</i>
I 2— 3	-0.017 + 1.0nt	0.005 + 1.6nt
—I 2— 2	+0.086 — 34.1nt	-0.323 + 1.3nt
0 2-3	-0.089 + 49.9nt	+0.337 + 5.0nt
I 2— 4 —I 2— 3	+0.015 - 23.1nt +0.369 - 3.0nt	-0.090 - 4.1nt
0 2—4	+0.369 - 3.0nt $-0.371 + 7nt$	+0.078 + 2.6nt -0.066 - 4nt
I 2— 5	-0.3/1 + 7m +0.113 - 2nt	+0.018 + 1nt
-ı 3+ 2	O. OI 2	+o. o28
0 3+ 1	+0.032	—o. o53
1 3 0	—0. 027	+0.012
-I 3+ I	-0.001 - 1.3nt	+0.270 + 0.8nt
0 3 0	+0.0041 + 0.2nt	0. 8536 0. 8nt
I 3— I	+0.0004 + 1.72nt	+0.7720 + 0.74nt
_1 3 o	+0.0053 — 10.31nt	-0.0348 - 33.34nt
o 3— 1	+0.11465+ 11.569nt	+0.08256+ 30.194nt
I 3— 2	-0. 1289 11. 91nt	-0.0856 - 5.85nt
—ı 3— ı	+0.0050 +251.76nt	-0.0246 +145.18nt
0 3- 2	-0.0081 -253.99nt	+0.0355 —136.31nt
ı 3— 3	+0.0045 + 71.4nt	-0.0146 + 35.4nt
—I 3— 2	+0.0916 — 9.2nt	+0.0384 + 3.0nt
0 3-3	-0.081 + 1.7nt	-0.026 - 6.5nt
I 3— 4	+0.024 + 0.9nt	+0.012 + 3.8nt
—ı 3— 3	+0.276 - 7.4nt	+0.002 - 41.4nt

	δТ		
$Arg = \varkappa \gamma + i'g' + ig$	sin.	cos.	
и i' i 0 3— 4		// // -0.002 + 51.4nt	
I 3— 5	+0.077 Ont	0.007 22nt	
—I 3— 4	+0.007 — 3nt	+0. 269 — 5nt	
0 3—5	-0.014 + 2nt	-0. 263 + 6nt	
I 3—6	0.00 — Int	+0.08 — $2nt$	
ŀ	0.00 - 1m		
—ı 4+ ı	+0.002	—0.007	
040	0.006	+0.011	
I 4 I	+0.0076 + 0.1nt	0.0067 ont	
-ı 4 0	+0.0409 — 6.0nt	-0.0071 - 5.1nt	
0 4— I	+0.0611 + 5.30nt	—0.0168 + 4.29nt	
I 4 2	-0. 0783 - 3. 36nt	+0.0189 + 0.26nt	
—I 4— I	—0.0166 + 87.10nt	+0.0489 — 1.22nt	
0 4— 2	+0.0076 — 84.49nt	+0.0173 + 1.91 <i>nt</i>	
ı 4— 3	+0.0026 + 23.57nt	0.0550 7.41 <i>nt</i>	
I 4 2	+0. 1089 — 85. 49nt	-0.0252 +257.49nt	
v 4 3	-0.114 + 77.3nt	+0.029 —258.0nt	
I 4 4	+0.041 — 21.2nt	—0.007 + 76.9nt	
-ı 4- 3	+0.005 — 4.5nt	+0.059 — 4.8nt	
0 4 4	-0.018 + 6.2nt	—0.049 — 2.7nt	
1 4 5	—0. 006 — 4nt	+0.016 ont	
—I 4— 4	+0.043 + 35nt	+0. 191 — 15nt	
0 4— 5	-0.042 - 41nt	-0. 186 + 15nt	
I 4—6	+0.013 + 16nt	+0.041 — 5nt	
— 1 4— 5	-0.182 + 3nt	+0.040 — 4nt	
0 4 6	+0. 15 — 7nt	-0.04 + 6nt	
I 4— 7	-0.03 + 2nt	+0.01 — 3nt	
—I 5 0 0 5— I	+0.0018 — 0.9nt +0.0011 + 0.8nt	-0.0003 - 0.3nt -0.0035 + 0.1nt	
I 5— 2	0.001763 0.462nt	+0.001130 + 0.335nt	
—I 5— I	+0.008734 + 14.351nt	+0.030313 - 9.125nt	
0 5— 2	+0.0040821— 13.66051nt	+0.0001070+ 8.46360nt	
I 5— 3	+0.015221 + 2.569nt	+0.040083 — 4.535nt	
—I 5— 2	+0.001014 + 20.443nt	-0.034322 +101.528nt	
o 5— 3	-0.0286 - 21.2nt	+0.0360 — 99.4 <i>nt</i>	
1 5 4	+0.0185 + 12.0nt	-0.0140 + 28.5nt	
—ı 5— 3	+0.049 —217.1nt	+0.116 — 25.0nt	
0 5-4	-0.053 +215.8nt +0.017 - 66.2nt	-0.129 + 18.8nt	
1 5— 5 —1 5— 4	+0.017 — 66.2nt -0.027 + 1.6nt	+0.040 — 4.1nt +0.023 — 4.2nt	
o 5-5	+0.025 + 4nt	-0.023 - 4.2ni -0.033 + 6nt	
1 5— 6	-0.008 - 3nt	+0.005 - 3nt	
—ı 5— 5	-0. 127 + 16nt	+0.061 + 25nt	
0 5 6	+0.127 — 18nt	-0.064 - 27nt	
ı 5— 7	-0.02 + 5nt	+0.01 + 9nt	
— 1 5— 6	-0.05 + 6nt	-0. 12 + 2nt	
o 5— 7	+0.05 — 6nt	+0.11 — 6nt	
1 5— 8	—o. oɪ	—0. 02	

	δΤ		
$Arg = \varkappa \gamma + i'g' + ig$	sin.	cos.	
и i' i 1 6— 2	,, ,, ,,, 0, 0002	,, ,, ,, ,, ,, ,, ,, ,, ,, ,, ,, ,, ,,	
- ·1 6— 1	0.0064 + 1.07 <i>nt</i>	-0.0035 - 2.55nt	
0 6- 2	+0.0007 1.15 <i>nt</i>	-0.0004 + 2.29nt	
1 6— 3	+0.0110 - 0.25nt	+0.0098 — 0.86nt	
-ı 6— 2	+0.0787 + 16.29nt	-0.0663 + 18.09nt	
o 6— 3	—u. 0612 — 15. 60nt	+0.0528 — 17.56nt	
1 6— 4	-0.0364 + 6.7nt	+0.0212 + 3.6nt	
-ı 6 <u>3</u>	+0.0457 — 93.9 <i>nt</i>	+0.0536 + 39.1nt	
0 6— 4	0.048 + 92.6nt	—0.064 — 39.7nt	
ı 6— 5	+0.009 — 26.1nt	+0.012 + 16.7nt	
-ı 6— 4	—0. 086 — 15. 4 <i>nt</i>	+0.004 —160.4nt	
o 6— 5	+0.098 + 20.2nt	-0.070 +158.4nt	
ı 6— 6	—0.026 — 8nt	+0.018 — 48nt	
1 6 5	-0.025 + 4nt	—0.008 — 2nt	
o 6— 6	+0.017 — 3nt	+0.009 + 5nt	
ı 6— 7	—0.01 + 2nt	0.00 ont	
1 6 6	-0.05 - 13nt	-0.05 + 16nt	
o 6— 7	+0.05 + 17nt	+0.05 16nt	
ı 6— 8	— 9nt	+ 8nt	
1 7 1	-0.0023 0.0nt	+0.0003 — 0.2nt	
0 7—2	+0.0004 — 0.02nt	+0.0001 + 0.17nt	
I 7— 3	+0.00285— 0.10nt	+0.00160- 0.08nt	
I 7— 2	-0.01947+ 4.32nt	—0.06596+ 1.34 <i>nt</i>	
0 7— 3	+0.02661— 4.090 <i>nt</i>	+0.05637— 1.339nt	
1 7— 4	-0.0365 + 1.44nt	-0.0163 - 0.28nt	
1 7— 3	+0.6246 — 17.17nt	+0.5861 + 22.24nt	
o 7— 4	-0.6835 + 16.4nt	—0.6413 — 22.0nt	
r 7 5	+0.212 3.0nt	+0.199 + 7.9nt	
—r 7— 4	-0.044 - 49.7nt	+0.070 - 73.5nt	
0 7-5	+0.018 + 50.3nt	-0.099 + 71.9nt	
1 7— 6	+0.003 — 18.7nt	+0.036 — 20.3nt	
—ı 7— 5	-0.065 +106.7nt	-0.053 - 33.7nt	
o 7— 6	+0.071 —104 <i>nt</i>	+0.074 + 37nt	
ı 7— 7	-0.017 + 30nt	-0.010 - 14nt	
— r 7— 6	-0.006 + 1nt	-0.010 + 2nt	
0 7 7	+0.03 — 5nt	+0.01 — 1nt	
r 7—8	0nt	+ 5nt	
-I 7— 7	+0.02 — 12nt	0.03 9nt	
o 7 - 8	-0.01 + 14nt	+0.03 + 8nt	
ı 7— 9	— 7nt	— 5nt	
-1 8— 2	-0.0127 + 0.63nt	-0.0138 - 0.24nt	
0 8 3	+0.01234— 0.666nt	+0.01122+ 0.156nt	
ı 8— 4	-0.0105 + 0.13nt	-0.0006 - 0.15nt	
i 8 3	+0. 2509 0. 74nt	+0.0589 + 5.91nt	
0 8 4	-0.2548 + 0.64nt	-0.0661 - 5.81nt	
l			

	δТ		
$Arg = \varkappa \gamma + i'g' + ig$	sin. cos.		
и i' i 1 8—5	"		
1 8 4	-0. 4717 -25. 3nt	+0.7795 —12.2nt	
0 8— 5	+0.489 +25.4 <i>nt</i>	-0.822 +12.3nt	
r 8— 6	-0. 152 - 7. 7nt	+0.262 — 2. Int	
—ı 8— 5	-0.071 +49.5nt	—0.001 —51.8nt	
o 8 6	+0.084 —46.6 <i>nt</i>	-0.029 +51.3nt	
ı 8— 7	—0.036 +13nt	+0.015 —16nt	
—ı 8— 6	+0.029 +36nt	-0.055 +67nt	
o 8— 7	-0.027 -42nt	+0.054 -71nt	
ı 8—8	0.00 + 13nt	—o. or —19nt	
—ı 8— 7	—o. oi — 3nt	+0.01 + 3nt	
o 8— 8	0.00 + 4nt	+0.01 — 3nt	
189	— 6nt	0 <i>nt</i>	
I 9 2	— 0. 0030	o. oo13	
0 9-3	+0.0023 0.04nt	+0.0009 + 0.03nt	
1 9—4	-0.0016	+0.0007	
—ı 9— 3	+0.0478 + 0.46nt	_0. 0156 + 0. 99nt	
0 9-4	-0.04738 - 0.43nt	+0.01338 — 0.95nt	
r 9— 5	+0.0118 + 0.20nt	-0.0118 + 0.18nt	
—ı 9— 4	-0.0149 - 6.84nt	+0.3398 + 0.51nt	
0 9-5	+0.019 + 6.4nt	-0. 347 - 0. 7nt	
1 9—6	+0.012 — 1.5nt	+0.109 + 0.6nt	
<u>—1</u> 9— 5	-0.735 + 6.7nt	—0. 254 —25. 5nt	
0 9-6	+0.765 - 5.7nt	+0.252 +24.2nt	
I 9— 7	-0. 24I ont	_0.079 _ 7nt	
—ı 9— 6	0.032 +46nt	-0.037 +30nt	
0 9— 7	+0.062 —46nt	+0.050 —27nt	
ı 98	-0.026 +11nt	-0.022 + 6nt	
—ı 9— 7	+0.026 -37nt	-0.006 +33nt	
o 9—8	-0.02 +31nt	+0.02 —33nt	
ı 9— 9	— 8nt	+ 8nt	
—r 9 — 8	— I <i>nt</i>	—Iont	
o 9— 9	+ 2nt	+ 8nt	
—ı 10— 3	+0.00528 + 0.148nt	-0.00629 + 0.098nt	
0 10—4	-0.0052516- 0.13299nt	+0.0055258— 0.10069nt	
1 10 5	+0.00011 + 0.058nt	-0.00281 - 0.003nt	
_1 10— 4	+0.03685 - 1.140nt	+0.07039 + 0.757nt	
o 10— 5	-0.0338 + 0.9nt	-0.0700 - 0.6nt	
I IO 6	+0.017 - 0.2nt	+0.017 + 0.2nt	
_1 10— 5	-0.348 - 2. Int	+0.056 - 6.2nt	
0 10—6	+0. 356 + 1. 5nt	-0.053 + 5.7nt	
1 10-7	-0.112 $-0.4nt$	+0.032 - 1.1nt	
_1 10 6	+0.067 +21.6nt	-0.591 + 0.8nt	
o 10-7	—0. 054 —21nt	+0.610 - 1nt	
1 10-8	-0.034 $-21m$ $+0.017$ $+5nt$	-0. 188 Ont	
_1 10— 3 _1 10— 7		-0.041 +37nt	
	+0.012 —13nt	-0.54x +3/m	

	δТ		
$Arg = \varkappa \gamma + i'g' + ig$	sin.	. cos.	
и i' i о 10—8	" " —0.021 +13nt	,, ,, +0.072 —35nt	
1 10— 9 —1 10— 8	0.00 — 3nt —21nt	—0.02 + 9nt —15nt	
0 10—9	0.00 +21 <i>nt</i>	-0.02 + 15nt	
0 11—4	—0. 0002	+0.0009	
—1 11— 4 0 11— 5	+0.0124 - 0.08nt $-0.0114 + 0.07nt$	+0.0077 + 0.16nt -0.0078 - 0.10nt	
1 11-6	+0.0047	+0.0006	
—ı ıı— 5	-0.0752 - 0.9nt	+0.0593 — 0.9nt	
o 11— 6	+0.075 + 0.8nt	—0. 056 + 0. 9 <i>nt</i>	
1 11-7	0. 020	 -0. 024	
—ı ıı— 6	-0.114 + 5.1nt	—0. 300 — 2. 5nt	
0 11-7	+0.112 - 4.6nt	+0.301 + 1.8nt	
1 11— 8	-0.046 + Int	—0.094 — Int	
II- 7	+0.419 + Int	-0.045 + 15nt	
o 11—8	o. 426 2nt	+0.059 —14nt	
1 11-9	+0. 14 Ont	-0.02 + 3nt	
—ı ıı— 8	+0.03 -27nt	0.00 — 4nt	
o 11—9	0.05 +24nt $6nt$	0.00 + 5nt	
		+17nt	
0 12 5	-0.00225- 0.002nt	—0. 00010— 0. 032nt	
—I I2— 5	-0.0081 - 0.21nt	+0.0200 — 0.06nt	
o 12— 6	+0.0076	o. o174	
1 12— 7	0,000	+0.005	
—I I2— 6	-0.073 + 0.8nt	0.067 0.9nt	
o 12 7 1 12 8	+0.076 0.6nt 0.028	+0.066 + 0.6nt 0.016	
1 12— 8 —1 12— 7	+0.220 + 2.4nt		
o 12— 8	-0.219 - 3nt	-0.142 + 3.7nt +0.140 - 4nt	
I 12— 9	—0. 219 — 3 <i>m</i> +0. 066		
_1 12— 9 _1 12— 8	+0.096 —Iont	+0.271 + 3nt	
0 12-9	-0.09 +10nt	-0. 26 ° - 3nt	
I 12—10	+0.03	+0.04	
—I I2— 9	— Int	—15nt	
0 12—10	ont	+14nt	

This expression for δT must be subjected to the same treatment as that we employed in Chapter II for deriving $\frac{d \cdot \delta z}{dt}$ and $\frac{d\nu}{dt}$ from T; that is, we must obtain $\overline{\delta W_0}$ and $-\frac{1}{2} \left(\frac{\overline{d \cdot \delta W_0}}{d\nu} \right)$ from δW_0 , the latter being given by the equation

$$\delta W_0 = \int \delta \mathbf{T} n dt$$

In deriving δW_0 from δT , in the terms whose arguments involve 5g'-2g or 10g'-4g, it seems advantageous to equate the motion of the argument. In this way

a more rapid approximation to the correct values of these terms is secured. Joining T and δ T together, and supposing that the argument is denoted by χ , let

$$T + \delta T = (a + bnt) \sin \gamma + (c + dnt) \cos \gamma$$

By means of the equations

these terms can be approximately expressed

$$T + \delta T = (A + Bnt) \sin (\chi + K + \mu nt)$$

and thence by integrating

$$W_0 + \delta W_0 = -\mu (A + Bnt) \cos (\chi + K + \kappa nt) + \mu^2 B \sin (\chi + K + \kappa nt)$$

where μ denotes the integrating factor for the argument $\chi + unt$. In the special cases we treat μ will be derived from either of the formulæ

$$\frac{1}{\mu} = \frac{5n' - 2n}{n} + \kappa \text{ or } \frac{1}{\mu} = \frac{10n' - 4n}{n} + \kappa$$

By developing the sine and cosine of the argument in powers of nt, and neglecting in the coefficients terms multiplied by n^2t^2 , we get

$$W_0 + \delta W_0 = -\mu[a - \mu B \sin K + (b - \mu \mu B \cos K)nt] \cos \chi$$
$$+ \mu[c + \mu B \cos K + (d - \mu \mu B \sin K)nt] \sin \chi$$

By subtracting from this the value of W_0 , found in Chapter II, we have the value of δW_0 .

In the five terms we treat by this process there has been found:

Arg.	log A	K	log B	log u	$\log\mu$
y + 5g' - 2g $5g' - 2g$ $-y + 5g' - 2g$ $10g' - 4g$ $-y + 10g' - 4g$	7. 8385 9. 2905882 0. 3077026 7. 81648 8. 8359	0 / // 217 19 24 248 8 38. 26 176 39 35. 74 133 13 55 62 10	4. 2156 5. 4424349n 6. 1611524n 3. 24871 4. 1369	6. 8991n 6. 9088766n 6. 7032188n 6. 40327 6. 2981	1. 8983560 1. 8989767 1. 8885772 1. 56683 1. 56770

By the aid of these quantities the terms of δW_0 in question have been found as follows:

A	78	W_0
$Arg = \varkappa \gamma + i'g' + ig$	cos. sin.	
κ i' i 1 5— 2 0 5— 2 —1 5- 2 0 10— 4 —1 10— 4	" +0. 1508 +0. 000372nt +0. 20521+0. 01077291nt +5. 7718 -0. 016254nt +0. 13735+0. 00004901nt -1. 3613 +0. 000421nt	" +0.0564 +0.000260nt -0.79420+0.00683789nt -1.3453 +0.078528nt +0.14799-0.00003718nt +2.6053 +0.000279nt

The expressions for $\overline{\delta W_0}$ and $-\frac{1}{2} \left(\frac{\overline{d \cdot \delta W_0}}{d \gamma} \right)$ follow:

$ ext{Arg} = i'g' + ig$	$\overline{\delta \overline{\mathrm{W}}_{\mathrm{o}}}$		
Alg='g+'g	cos.	sin.	
i' i o o	$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	" "	
о— 1	$+ 0.2093 +25646.6nt + k_1 - 8.6712n^2t^2$	$+$ 0. 2242 —22608. 5nt $+$ k_2 — 14. 7155 n^{2} 9	
0 2	- 0. 2832 + 620. 2nt +[8. 3821] k_1 - 0. 2090 n^2t^2	+ 0. 2146 - 544. 4nt +[8. 3822] k_2 - 0. 3548 n^2t^2	
o 3	$+ 0.0923 + 22.4nt + [6.9403]k_1 - 0.0076n^2t^2$	+ 0.0818 — 19.7 $nt+[6.9405]k_2— 0.0128n^2t^2$	
0— 4	$+ 0.0022 + 1.0nt$ $- 0.0003n^3t^2$	+ 0.0091 — 0.8nt — 0.0005n ² t ²	
I+ 4	— o. ooo7	— o. ooo6	
1+3	o. 0148	o. oo88	
I+ 2	— 0. 1337 — 0. 1 <i>nt</i>	0. 2170 0. 4nt	
1+ 1	- 0. 9173 - 4. 3nt	+ 0.8004 — 14.6nt	
1 0	- 0. 5479 $+$ 37. 25nt	— 0. 4234 — 65. 10nt	
1 I	+ 0. 2023 — 7. 86nt	— 0. 3128 — 2. 53nt	
I 2	-0.3533 + 5.2nt	+ 0.1841 — 7.7nt	
I— 3 I— 4	+ 0.0531 - 0.1nt + 0.0524	+ 0. 1508 — 0. 9 <i>nt</i> — 0. 0375	
2+ 2	o. o24I	+ 0.0141	
2+ 1	— 0.6558 + 0.9nt	+ 0.0635 1.8nt	
2 0	— 1.8249 + 33.0nt	— 3. 1885 — 36. 2nt	
2— I	+ 0.13729 — 301.67nt	— 0. 32321 — 545. 77nt	
2 2	+ 0.1974 - 5.7nt	+ 0.3142 - 58.0nt	
2— 3	+ 0.0420 13.0nt	+ 0. 1536 3. 7nt	
2 4	+ 0.0808 — 0.4nt	— 0.0123 — 0.2nt	
2— 5	+ 0.004	o, ∞i	

	8	$\overline{W_0}$
Arg=i'g'+ig	cos.	sin.
i' i	" "	"
3+ 1	+0.0117 — 0.2nt	+0.0841 + 0.1nt
3 0	-0.0084 - 8.3nt	+3.1295 + 3.5nt
3— I	-0.7115 - 61.14nt	+0.4816 + 124.44nt
3— 2	-0.0002 -1490.72nt	-0. 1013 + 849. 48nt
3— 3	+0.0798 — 39.8nt	0.0398 + 15.6nt
3— 4	+0.0804 — 3.2nt	-0.0002 + 11.0nt
3- 5	+0.0026 — 0.9 <i>nt</i>	0.0436 + 1.1 <i>nt</i>
4 0	0.0143 — 0.4n	-0.0081 0.0 <i>nt</i>
4 I	—0. 3265 — 13. 18 <i>nt</i>	—u. 0797 + 3. 30 <i>nt</i>
4— 2	+0.0483 — 342.81nt	+0.0721 2.44nt
4— 3	+0. 2313 — 176. 3nt	+0.0426 — 508.0nt
4— 4	+0.0018 — 8.1nt	—0.0254 — 11.3nt
4 5	+0.0089 + 5.8nt	-0.0353 + 2.4nt
4 6	-0.0247 + 0.1nt	-0.0065 + 0.6nt
5 0	+0.0036 + 0.9nt	+0.0013 + 0.6nt
5— 1	+0.1492 + 36.9nt	+0.0518 + 26.0nt
5— 2	+0.21209+1065.872nt	0.80459+ 679.033nt
5— 3	+5.7511 —1641.6nt	—1. 3745 +7939. Int
5— 4	+0. 1676 — 172. 9 <i>nt</i>	0. 0995 + 206. 5nt
5— 5	0.0011 5.4nt	0.0058 + 8.3nt
5— 6	-0.0149 + 1.9nt	o. 0065 3. 4nt
5— 7	-0.0053 + 0.4nt	+0.0111 + 0.5nt
6— 1	+0.0 010	-o. oo18
6— 2	+0.0210 + 1.67nt	0.0206 + 5.08nt
6 3	—o. 3163 — 61. 90nt	-0. 2629 + 71. 07nt
6— 4	+0.0478 — 113.5nt	—0. 0624 — 47. Int
6— 5	-0. 0223 - 8. ont	+0.0172 + 51.8nt
6 6	-0.0084 + 0.7 nt	+0.0004 + 1.7nt
6— 7	—0. 0033 — I. 5nt	+0.0032 — 2.4nt
7— 2	+0.0160 — 0.5nt	—0. 0084 + 0. 5nt
7-3	+0.1416 — 26.66nt	-0.3811 + 9.18nt
7— 4	+2.9728 82.5nt	-2.7899 - 107.5nt
7— 5	+0.0547 — 27.0nt	-0.1035 + 33.7nt
7— 6	-0.0095 + 22.3nt	-0.0007 + 8.5nt
7— 7	+0.0046 + 0.3nt	+0.0014 — 0.4nt
7— 8	+0.0029 — 1.8nt	+0.0013 + 1.4nt
8 3	-0.0577 + 2.66nt	+0.0399 + 0.67nt
8— 4	-1.4136 + 4.25nt	+0.3484 + 33.27nt
8— 5	—0.4131 — 20.8nt	-0.6273 + 10.3nt
8 — 6	—0.0349 + 13.6nt	-0.0168 + 15.2nt
8— 7	+0.0019 + 5.3nt	+0.0067 — 8.6nt
8 8	-0.0023 - 0.7nt	-0.0042 0.7nt

A 2/-/ 1 1-	$\overline{\delta \overline{\mathrm{W}_{\mathrm{o}}}}$		
Arg=i'g'+ig	cos.	sin.	
i′ i 9 3	" " -0.0066 + 0.1nt	" " " " " " " " " " " " " " " " " " "	
9— 4	—0. 1940 — 1. 75nt	-0.0531 + 3.98nt	
9— 5	-0. 0242 -14. Int	-0.6982 - 1.2nt	
9— 6	-0.2846 + 2.1nt	+0.0801 +10.4nt	
9— 7	-0.0139 + 8.4nt	+0.0094 5.6nt	
9— 8	+0.0022 — 4.5nt	0.0022 4. Int	
9— 9	+0.0002 — 0.1nt	0.0000 + 0.6nt	
10— 4	+0. 18928+ 4. 812nt	+0. 20046— 3. 622nt	
10— 5	—1.3884 +42.8nt	+2.6682 +28.4nt	
10— 6	-0.2477 - 0.5nt	+0.0224 + 4.6nt	
10 7	+0.0103 + 5.0nt	+0. 1425 + 0. 1 <i>nt</i>	
10— 8	-0.0007 - 1.4nt	+0.0069 · 5.4nt	
10 9	+0.0001 - 1.2nt	+0.0046 + 0.5nt	
11 4	+0.000 6	+0.0021	
11 5	-0.0461 + 0.3nt	+0.0310 + 0.6nt	
11 6	0.0928 1.0nt	o. 0766 + o. 9nt	
11 7	$-0.0444 + 1.7\pi t$	+0.0978 + 1.2nt	
11-8	+0.0725 — 0.1 <i>nt</i>	+0.0100 — 2.6nt	
11 9	+0.0014 — 2.4 <i>nt</i>	+0.0004 - 0.1nt	
11-10	— I. Int	— 3. Int	
12— 5	-0.0134 - 0.01 <i>nt</i>	+0.0008 + 0.19nt	
12— 6	—0.0420 — 1.3nt	-0. 1066 + 0. 4nt	
12— 7	-0.0370 + 0.4nt	+0.0294 + 0.5nt	
12 8	+0.0465 + 0.1nt	+0.0336 — 0.4 <i>nt</i>	
12— 9	+0.0172 — 0.8nt	—0. 0293 — 0. 3nt	
12—10	+0.0007 — 0.3nt	-0.0023 + 0.9nt	

Arg=i'g'+ig	$-rac{\mathrm{I}}{2}\Big(rac{\overline{d}\cdot\delta\overline{\mathrm{W}_0}}{d\gamma}\Big)$		
	sin.	cos.	
i' i	п п		
U— I	— 0.0160 —12814.7nt	+ 0.0229 —11301.1nt	
	$-\frac{1}{2}k_1$ + 4. 3356 n^2t^2	$+\frac{1}{2}k_3$ - $7.357.7n^2\ell^2$	
0 2	$+$ 0. 2114 $-$ 619. 4nt $-[8.3821]k_1+$ 0. 2090 n^2t^2	+ 0.1606 - 544.5nt $+ [8.3822]k_2 - 0.3548n^2t^2$	
o— 3	$\begin{array}{cccccccccccccccccccccccccccccccccccc$	+ 0.0740 - 29.6nt $+ [7.1165]k_2 - 0.0192n^2t^2$	
0— 4	$\begin{array}{rcl} - & 0.0049 & - & 1.9nt \\ + & 0.0006n^2t^2 \end{array}$	$\begin{array}{cccccccccccccccccccccccccccccccccccc$	

Arg=i'g'+ig	$-rac{1}{2}ig(rac{\overline{d}\cdot \delta\overline{W_0}}{d\gamma}ig)$	
	sin.	cos.
i' i	11 '1	n P
1+4	o. ooo8	+0.0008
1+3	o. 0155	+0.0116
I+ 2	—0. 1168 — 0. 1 <i>nt</i>	+0.1662 + 0.4nt
1+1	o. 5766 2. 3nt	—0.4918 + 9.4 <i>nt</i>
1 0	-0.1306 + 10.00nt	+0.0914 + 14.78nt
1— 1	—0.0607 + 1.90 <i>nt</i>	0, 1026 — 1. 81 <i>nt</i>
I— 2	+0.2402 2.5nt	+0.1278 — 5.7nt
1 3	-0.0437 - 0. Int	+0.1249 — 0.8nt
I— 4	—0. 0446	—o. o278
2+ 2	—o. o283	0.0121
2+ I	-0.4810 + 0.9nt	-0.0318 + 1.3nt
2 0	-0.7837 + 13.4nt	+1.3494 + 15.3nt
2— I	0. 00469+ 32. 59 <i>nt</i>	0. 04082 56. 20nt
2— 2	-0.1106 + 3.5nt	+o. 1799 — 33. 4nt
2 3	-0.0383 + 10.7nt	+0.1315 — 2.7nt
2— 4	-0.0726 + 1.2nt	—0. 0087 — 0. 6nt
2— 5	-0.004	-0.001
3+ 1	+0.0096 — 0.2nt	-0.0902 0.1nt
3 0	—0.0050 — 4.8nt	—1. 7968 — 1. 8nt
3— 1	—0. 0790 — 10. 83nt	-0.0651 - 17.00nt
3— 2	-0.0032 +624.74nt	-0.0346 + 358.12n1
3— 3	-0.0532 + 34.9nt	-0.0236 + 15.4nt
3— 4	-0.0696 + 3.9nt	-0.0023 + 9.4nt
3— 5	-0.0050 + 0.5nt	—0.0399 + 1.2nt
4 0	—0.0106 — 0.3nt	+0.0054 0.0nt
4— 1	-0.0879 - 5.77nt	+0.0211 - 1.35nt
4— 2	-0.0116 + 79.48nt	+0.0212 — 2.96nt
4- 3	-0. 1404 +108. 8nt	+0.0301 — 314.6nt
4 4	-0.0104 + 7.2nt	-0.0171 14.2nt
4- 5	-0.0081 - 5.1nt	-0.0363 + 1.7nt
4 6	+0.0236 — 0.6nt	—0. 0069
5 0	+0.0036 + 0.9nt	—0.0013 — 0.6 <i>nt</i>
5— 1	+0.0762 + 18.5nt	-0.0273 - 13.2nt
5 2	+0.01228+ 8.489nt	+0.03518— 6.460nt
5 — 3	-2.8808 +816.3nt	-0.6754 +3933.2nt
5— 4	—0. 1611 +138. Int	-0.0849 + 201.2nt
5— 5	-0.0024 + 6.6nt	-0.0097 + 11.1nt
5 6	+0.0195 — 2.2nt	o. 0096 3. 3nt
5— 7	+0.0065 — 0.9nt	+0.0130 — 0.5nt
6— I	+0.0007	+0.0011
6 2	+0.0066 + 0.27nt	+0.0075 1.58nt
6 3	+0.0825 + 21.46nt	-0.0725 + 22.98nt
		<u> </u>

Arg=i'g'+ig	$-rac{1}{2}\Big(rac{d\cdot\delta\overline{W_0}}{d\gamma}\Big)$	
	sin.	cos.
i' i	<i>u</i>	" "
6— 4	—0. 0336 +76. 2nt	-0.0487 -29.6nt
6— 5	+0.0223 + 7.6nt	-0.0012 +42.3nt
6 — 6	+0.0049 — 0.2nt	+0.0013 + 2.7nt
6— 7	+0.0072 + 1.0nt	+0.0071 — 1.5nt
7— 2	+0.0072 — 0.2nt	+0.0042 — 0.3nt
7 3	-0.0250 + 3.22nt	-0.0449 + 0.79nt
7— 4	—1. 6789 +46. 7nt	—1. 5758 —59. 7nt
7— 5	-0.0641 +20.6nt	-0. 1025 +24. 8nt
7— 6	+0.0093 —19.7 <i>nt</i>	+0.0054 + 7.5nt
7— 7	+0.0016 — 1.3nt	+0.0022 + 0.9nt
7— 8	-0.0024 + 0.9nt	+0.0036 + 0.6nt
8 3	-0.0108 + 0.34nt	-0.0059 - 0.17nt
8— 4	+0.5874 — 1.65nt	+0. 1348 +13. 77nt
8— 5	+0.3028 + 14.8nt	-0.4472 + 7.9nt
8 6	+0.0313 —11.4nt	-0.0215 + 12.8nt
8— 7	0.0035 5.9nt	+0.0076 — 9.3nt
8— 8	+0.0010 — 0.4nt	—0.0008 — 0.9nt
9 3	0.0028	+0.0003
9 4	+0.0427 + 0.42nt	-0.0157 + 0.86nt
9 5	+0.0224 + 8.8nt	-0. 4305 - 0. 6nt
9 6	+0.2324 - 2.0nt	+0.0588 + 8.2nt
9— 7	+0.0167 — 8.6nt	+0.0085 - 5.2nt
9— 8	-0.0028 + 4.5nt	+0.0016 — 4.5nt
9— 9	-0.0002 + 0.4nt	0.0000 + 0.9nt
10 4	+0.00278+ 0.097nt	-0.00428+ 0.049nt
10— 5	+0.6841 -21.2nt	+1.3071 +14.0nt
10 6	+0.1929 + 0.1nt	+0.0383 + 3.7nt
10 7	-0.0045 - 4.7nt	+0. 1281 0. ont
10 8	-0.0024 + 1.6nt	+0.0121 - 5.3nt
10— 9	-0.0001 + 2.7nt	+0.0007 + 1.6nt
11— 4	+o. ooo1	0.0000
11 5	+0.0157 — 0.1nt	+0.0093 + 0.2nt
11 6	+0.0624 + 0.7nt	—0. 0476 + 0. 8nt
11— 7	+0.0338 — 1.5nt	+0.0798 + 0.7nt
11— 8	-0.0644 - 0.3nt	+0.0111 — 2.6nt
11 9	-0.0081 + 3.8nt	+0.0004 + 0.4nt
12 6	+0.0239 + 0.6nt	-0.0586 + 0.2nt
12— 7	+0.0284 - 0.3nt	+0.0230 + 0.4nt
12— 8	-0.0415 - 0.5nt	+0.0280 — 0.8nt
12— 9	-0.0146 + 1.6nt	-0.0372 - 0.5nt
12—10	-0.0007 + 0.2nt	-0.0023 + 1.8nt

Calling the second-order terms, to be added to $n\delta z$ and ν , $n\delta^2 z$ and $\delta \nu$, they are determined by the equations*

$$\begin{split} \frac{d \cdot n\delta^2 z}{ndt} &= \overline{\delta W_0} + \left(\frac{\overline{dW_0}}{d\gamma}\right) n\delta z + \nu^2 \\ \frac{d \cdot \delta \nu}{ndt} &= -\frac{1}{2} \left(\frac{\overline{d \cdot \delta W_0}}{d\gamma}\right) - \frac{1}{2} \left(\frac{\overline{d^2 W_0}}{d\gamma^2}\right) n\delta z \end{split}$$

It therefore remains to find the three products, $(\frac{\overline{dW_0}}{d\gamma})n\delta z$, v^2 , and $-\frac{1}{2}(\frac{\overline{d^2W_0}}{d\gamma^2})n\delta z$. The factor $(\frac{\overline{dW_0}}{d\gamma})$ of the first has already been given in Chapter II, being equivalent to $-2\frac{d\nu}{ndt}$, and it is easy to square the value of ν there given. The expressions of the two products to be employed in determining $n\delta^2 z$ follow:

Arg=i'g'+ig	$\left(\frac{\overline{d}\overline{\mathrm{W}}_0}{d\gamma}\right)$	$\left(\frac{\overline{d \mathbb{W}_{0}}}{d\gamma}\right)n\delta z$	
	COS.	sin.	
i' i	н н	u u	
0 0	-0.2041+ 0.1395 <i>nt</i>		
	— 0.8677 <i>n</i> ² t ²		
0— 1	$+$ 0. 0363— 0. 0523 n^2t^2	+o. 3266	
0 2	—0. 0140— 0. 0804 n^2t^2	+0.0300— 0.8636n ³ t ²	
o— 3	$+$ 0.0110— 0.0049 n^2t^2	+0.0110— 0.0520n ³ t ²	
0 4	— 0, 0003 <i>n</i> ²ℓ³	— 0, 0029n ³ / ²	
I+ 2	0. 0180	—o. o310	
1+1	-0.0637+ 0.1nt	+0.0484— 5.8nt	
1 0	+0.0672+ 43.83nt	+0.0277— 26.99nt	
I I	+0.0200+ 6.05 <i>nt</i>	-0.0184 3.54 <i>nt</i>	
I— 2	-0.0128+ 30.5nt	+0.0102+ 41.1 <i>nt</i>	
I 3	+0.0030+ 2.9nt	+0.0080+ 2.7nt	
2+ 2	о. 0060	+0. 0030	
2+ I	-0.1070+ 1.9nt	+0.0160+ 0.6nt	
2 0	-0.0582+ 43.7nt	—0. 0971+ 48, 3 <i>nt</i>	
2— I	-0.0594+ 70.32nt	+0.0727+197.75 <i>nt</i>	
2 2	o. 0175 37. 2nt	—0. 0030+ 52. 5nt	
2— 3	+0.0010—192.4 <i>nt</i>	+0.0070+ 88.4 <i>nt</i>	
2— 4	+0.0040— 12.3nt	—0.0010+ 4.8nt	
3+ 1	+0.003	+0.034	
3 0	+0.0073+ 1.8nt	+0.6822+ 5.1nt	
3— т	+0. 1512+ 12. 17nt	-0.0371-62.55nt	
3 2	+0.0486+ 18.91 <i>nt</i>	-0.0159- 2.99nt	
3— 3	+0.041 + 64.1nt	-0.053 + 6.3nt	
3— 4	+0.004 + 9.0nt	-0.004 + 25.7nt	
3— 5	o, ont	+ 1. 2nt	

*Auseinandersetzung, Abth. I, s. 98, gl. (40).

Arg=i'g'+ig	$\left(\frac{\overline{d}\overline{W}_0}{d\gamma}\right)$	$n\delta z$
Ang—i y —iy	cos.	sin.
i' i 4 0		" " " " " " " " " " " " " " " " " " "
4— 1 4— 2	-0.0786 + 6.28nt +0.0085 + 17.25nt	$\begin{array}{ccccc} -0.0155 & - & 6.71nt \\ +0.0382 & + & 6.65nt \end{array}$
4— 3 4— 4 4— 5	+0.0577 + 8.8nt +0.082 - 4.7nt +0.004 + 7.7nt	+0.0402 — 2.6nt +0.087 + 17.7nt +0.005 + 0.6nt
5+ I 5 0	+ 1. 2nt + 22. 5nt	— 0. 4nt — 7. 9nt
5— I 5— 2	+0.0003 +464.0nt 0.000201 - 86.794nt	+0.0020 -167.4nt +0.003721-110.414nt
5— 3 5-— 4 5— 5 5— 6	$\begin{array}{rrrrr} -0.0064 & +205.4nt \\ -0.014 & +109.5nt \\ +0.022 & +11.0nt \\ & +0.8nt \end{array}$	-0.0076 +442.9nt -0.092 - 76.0nt -0.018 - 2.2nt - 2.5nt
6— I 6— 2 6— 3 6— 4 6— 5	$\begin{array}{rcl} -0.0002 \\ -0.0024 & -0.19nt \\ -0.0642 & +1.92nt \\ -0.0110 & 0.0nt \\ +0.007 & +0.7nt \end{array}$	+0.0014 +0.0030 — I.33nt -0.0466 — I.01nt +0.0321 — I.6nt -0.002 + 2.8nt
6— 6 6— 7 7— 2	$ \begin{array}{rcl} -0.002 & + & 1.0nt \\ & - & 1.0nt \\ -0.0029 & + & 0.2nt \end{array} $	$ \begin{array}{cccccccccccccccccccccccccccccccccccc$
7— 3 7— 4 7— 5 7— 6 7— 7	+0.0097 + 1.61nt +0.4458 + 0.5nt -0.135 - 0.4nt -0.008 + 0.7nt -0.002 - 0.4nt	$\begin{array}{cccccccccccccccccccccccccccccccccccc$
8— 3 8— 4 8— 5 8— 6	+0.0025 — 0.27nt -0.1461 + 0.04nt -0.037 -0.014	-0. 0015 - 0. 18nt +0. 0306 - 0. 20nt -0. 048 +0. 012
9— 3 9— 4 9— 5 9— 6 9— 7	+0.0005 -0.0077 + 0.06nt -0.0035 -0.048 0.000	+0.0001 -0.0027 - 0.05nt -0.0612 +0.014 +0.004
10— 4 10— 5 10— 6 10— 7	-0.00065 $-0.368nt$ -0.1824 $+0.6nt$ $+0.028$ $+0.004$	-0.00033 + 0.106nt +0.3525 0.0nt +0.022 +0.018
11— 5 11— 6 11— 7 11— 8	—0, 0019 —0, 0067 —0, 003 +0, 006	+0.0011 0.0050 +0.008 +0.001
12— 5 12— 6 12— 7 12— 8 12— 9	-0.0001 -0.0023 -0.003 +0.004 +0.001	0. 0000 0. 0057 +-0. 002 +-0. 003 0. 003

		2 ¹²
Arg=i'g'+ig	cos.	sin.
i' i	,, ,, ,, +0.0498 — 0.0025nt	и и
0 I	$+ 0.2171n^{3}t^{2}$ $+ 0.0143 + 1.5nt$ $+ 0.0200n^{3}t^{2}$	$+0.0094 - 1.6nt$ $-0.0104n^2t^2$
0 2	— 0.0188 n^2t^2	— 0. 2163n ² t ²
0— 3 0— 4	0. $0009n^2t^2$ 0. $0000n^2t^2$	- 0.0104 n^2t^2 - 0.0006 n^2t^2
1 + 1	-0.0008 0.5nt 0.018010.26nt	-0.0011 - 0.5nt -0.0074 + 6.30nt
ı— 1		+0.0060 + 1.19nt
I— 1 I— 2		-0.0007 + 9.6nt
I = 2 I = 3	+0.0015 + 7.2nt + 0.4nt	+ 0.3nt
2+ I	0. 0 <i>nt</i>	- 0. 4nt
2 0	-0.0034 - 5.7nt	—0.0073 — 7.6nt
2— I	+0.0150 —17.16nt	—0.0178 —47.44 <i>nt</i>
2— 2	-0.0023 - 7.7nt	-0.0026 + 4.0nt
2 3	—45. 7 <i>nt</i>	+20.7nt
2— 4	— 2. 5nt	+ 1. ont
3 0	0.0019 + 0.2nt	+0.0059 + 1.6nt
3 1	-0.0384 - 3.16nt	+0.0140 +15.86nt
3— 2	-0.0058 - 3.66nt	-0.0008 + 1.15nt
3— 3	+0.007 +16.1nt	-0.012 + 1.6nt
3 4	+ 1.4nt	+ 5. ont
4— I	-0.0012 - 1.36nt	-0.0009 + 1.28nt
4 2	-0.0007 - 3.91 <i>nt</i>	-0.0098 - 1.45nt
4— 3	+0.0047 + 1.2nt	+0.0062 + 2.4nt
4— 4	+0.019 — 1.2nt	+0.021 + 4.1nt
4 5	+ 1.3nt	+ 0. Int
5— 1	+ 5.3nt	— o. 2nt
5— 2	—0. 000049+21. 818 <i>nt</i>	-0.001044+27.546nt
5-3	-0.0012 - 0.2nt	-0.0039 - 3.1nt
5— 4	-0.005 +26.1nt	-0.019 -24.0nt
5— 5	+0.005 + 2.0nt	-0.004 - 0.8nt
6— 2	+ 0.04nt	+ o. 32nt
6 3	+0.0003 - 0.40nt	+0.0007 + 0.22nt
6— 4	-0.0027 + 0.5nt	+0.0102 + 0.1nt
6 5	+0.003 + 0.2nt	o. 000 + o. 4nt
7— 3	-0.0008 - 0.38nt	+0.0007 - 0.02nt
7 4	-o. o113	+0.0022
7 5	,o, o <u>3</u> 8	-0.020
8— 3	+ 0.06nt	+ o. o5nt
8 4	+0.0026	+0.0006
8— 5	+0.007	+0.012
8 6	0,002	+0.004
<u> </u>		

Arg=i'g'+ig		$ u^2$
Alg—vy +iy	cos.	sin.
i' i 9— 5 9— 6	,, ,, ,, o. oooo —o. oog	// // +0.0015 +0.002
10— 4 10— 5 10— 6	0.0005+0.093 <i>nt</i> +0.0023 +0.014	0.000310.026nt 0.0031 +-0.002

The expression for $-\frac{1}{2}\left(\frac{\overline{d^2W_0}}{d\gamma^2}\right)$ is obtained by differentiating, with respect to γ , the terms of $-\frac{1}{2}\frac{dW_0}{d\gamma}$, which has already been employed in Chapter II. However, in order not to have to return to this term when we compute the third-order terms, I have, before this differentiation, added to the latter quantity the expression for $-\frac{1}{2}\frac{d \cdot \delta W_0}{d\gamma}$, which has just been obtained. The expression for this factor, together with its product by $n\delta z$, is given in the following table:

Arg=i'g'+ig	$-rac{1}{2}\Big(rac{ar{d}^2 \overline{\mathrm{W}_0}}{ar{d} \gamma^3}\Big)$	
	cos.	sin.
i' i	'' '' '' -7. 1170+ 0. 7274nt	" "
o 1	-1.8280+63749nt	+ 1.3209—69810nt
	$-$ 4. 3356 n^2t^2	— 7. 3578n ² t ²
O— 2	-0.4480- 6153 <i>nt</i>	+ 0.1175 6732nt
	— 0.4180n ² t ²	— 0.7096n²t²
o— 3	+0.0828+ 500nt	+ 0. 1057— 548nt
	- 0.0340 n^2t^2	— 0.0577n ² t ²
0— 4	+0.0098+ 38nt	+ 0.0205— 42nt
o— 5	+ 3nt	— 3nt
1+ 3	—o. o327	— o. o26o
1+ 2	o. 2072 o. 2nt	— 0. 2038— 0. 8nt
1+1	—0. 9517—	+ 0.5677+ 5.5nt
10	—1.8045+ 28.53nt	0.8777- 38.79nt
ı— 1	—3. 4290— I. 30nt	+17. 3976— 2. 76nt
1— 2	-0.0850+ 2.0nt	+ 2.7063— 9.2nt
1-3	+0.0850+ 0.2nt	+ 0.4148— 1.4nt
1— 4	+0.0745	— o. o188
2+ 2	— 0. 0689	+ 0.0123
2+ 1	-0.6706+ 1.7nt	- 0.0492- 2.1nt
2 0	-1.2173+ 17.9nt	— 1.7481— 16.2nt
2— I	-2. 6878- 35. 58nt	+ 0.8470— 45.89nt

Arg=i'g'+ig	$-rac{\mathrm{i}}{2}ig(rac{ar{d}^2\overline{\mathrm{W}_0}}{ar{d}\gamma^2}ig)$	
	cos.	sin.
i' i	" "	11 11
2 2	126, 0048 5. 8nt	—53. 8071— 36. 5nt
2— 3	— 12.0046— 17.8nt	— 5.7615— 3.2nt
2 4	— 0.8632— 2.3nt	- 0.5154- 1. ont
2— 5	0.0646	0.0417
3+ I	+ 0.0177- 0.4nt	+ 0. 1977+ 0. 2nt
3 0	+ 0.0421— 4.6nt	+ 2.0173 + 2.4nt
3 т	- 0.3719- 1.32nt	+ 0.0860— 11.05 <i>nt</i>
3— 2	+ 15.7381—584.70nt	+21.0388+ 337.66nt
3— 3	— 12.0572— 64.5nt	+21.4071+ 31.6nt
3— 4	— 1.6844— 7.4nt	+ 2.0011+ 16.9nt
3— 5	— 0.1618— 0.8nt	+ 0.0908+ 2.1nt
3— 6	— o. o141	+ 0.0104
4 0	_ o. 0152— o. 5nt	0.0000 0.0 <i>nt</i>
4— I	- 0.1436 1.66nt	+ 0.0051— 1.74nt
4— 2	+ 0. 1546— 63. 06nt	+ 1.3338— 0.06nt
4-3	— 12. 5021—121. Ont	+ 6. 2950— 346. 8nt
4— 4	+ 4.7176— 14.4nt	+ 6.9776— 30.1nt
4 5	+ 0.4239+ 8. Int	+ 1.0265+ 0.9nt
4— 6	— 0.0093+ 1.4nt	+ 0.0960+ 1.3nt
4— 7	+ 0.0010	+ 0.0086
5 0	+ 0.0209+ 1.8nt	— 0.0162+ 1.2nt
5— 1	+ 0.2148+ 19.0nt	- 0. 1767 $+$ 13. Int
5— 2	- 0.0279- 5.548nt	+ 0.0780 - 2.898nt
5— 3	+ 78. 2787—812. Int	+ 5.0079+3918.6nt
5— 4	+ 8.7461—199.5nt	+ 4.9450+ 391.9nt
5— 5	+ 3.9404— 16.9nt	— 1.4236+ 30.6nt
5 6	+ 0.5961+ 3.2nt	— 0.0776— 5. Int
5— 7	+ 0.0550+ 1.0nt	+ 0.0236— 0.7nt
5— 8	+ 0.0051	+ 0.0015
	· · · · · · · · · · · · · · · · · · ·	0.0022
6 1	+ 0.0028	— 0. 0022 — 0. 0046—
6— 2	+ 0.0077— 0.39nt	
6— 3 6— 4	+ 0. 1920— 17. 98nt — 0. 4071— 87. 4nt	+ 0.1204+ 20.19nt + 1.7113- 34.1nt
6— 4 6— 5	+ 2. 1390 - 13. 7nt	+ 0.0531 + 54.1nt
6— 6	+ 2.1390— 13.7 n 1 — 0.3128 $+$ 0.2 n t	-1.6130+4.9nt
6— 7	+ 0.0345— 2.6nt	— 1.0135+ 4.9m — 0.2965— 2.9nt
6 8	+ 0.0151	— 0. 0352
6— 9	+ 0.0019	— 0.00352 — 0.0026
7— 2	+ 0.0082- 0.2nt	0.0019+ 0.1nt
7— 3	+ 0.0114— 2.1nt	- 0.0168+ 0.7nt
7— 4	+ 1.0385 - 48.5nt	- 0. 9331 - 62. 7nt
7— 5	+ 0.8054— 28.1nt	+ 0. 2358 $+$ 28. 5nt
7— 6	+ 0.2442+ 25.7nt	- 1.0804+ 12.0nt
7— 7	— 0.7700+ 2.5nt	- 0.0408+ 0.3nt

Arg=i'g'+ig	$-rac{1}{2}\Big(rac{d^2 \overline{ m W_0}}{d\gamma^2}\Big)$	
	cos.	sin.
$oldsymbol{i}' oldsymbol{i}$	11 11	и и
7— 8	-0. 1502- 1. 9nt	-0.0597+ 1.4nt
7— 9	· —o. 0161	o. o134
7—10	0.0013	0.0017
8 3	+0.0007 0.18nt	o. 0040 o. 05 <i>nt</i>
8 4	-0.4192+ 1.59nt	+0.0961+12.93nt
8— 5	0. 228817. 2nt	-0. 3266+ 9. 6nt
. 8— 6	+0. 2274+14. 0nt	-0. 3831+15. 8nt
8 7	-0.5384+ 9.2nt	0. 2468—12. 6nt
8 8	-0. 1121 - 0. 3nt	+0.3481— 1.4nt
8— 9	o. o539	+0.0721
810	—о. 0103	+0. ∞70
9— 4	-0.0280- 0.34 <i>nt</i>	-0.0087+ 0.71nt
9— 5	—0. 0172— 9. 4 <i>nt</i>	o. 3615 o. 8nt
9— 6	-0.1782+ 1.6nt	+0.0150+10.2nt
9 7	—0. 1926+11. 1 <i>nt</i>	—о. 1846— 6. 2 <i>nt</i>
9— 8	—0. 1963— 5. 0nt	+0. 2559— 6. 2nt
9— 9	+0. 1477— 0. 7 <i>nt</i>	+0.0952+ 0.7nt
9—10	+0.0305	+o. o383
9—11	+0.0023	+0.0072
10 4	-0.0019- 0.1nt	-0.0018 0.0nt
10— 5	-0.5885+21.0nt	+1.1161+14.0nt
10 6	—0. 2162+ 0. 9nt	+0.0804+ 4.6nt
10— 7	-0.0167+ 5.8nt	+0.0979+ 0.2nt
10 8	—о. 1329— 1. 9 <i>nt</i>	+0.0892— 7.1nt
10— 9	+0.1094— 2.8nt	+0.1364+ 1.3nt
10-10	+o. o634	—o. o56o
1011	+o. 0244	— 0. 0109
10—12	+ 0.0040	+o. ooo1
11 5	-0.0119+ 0.1 <i>nt</i>	+0.0073+ 0.2nt
11— 6	0.0627 0.7nt	-0.0478+ 0.8nt
11— 7	-0.0401+ 1.7nt	+0.0823+ 0.9nt
11 8	+0.0413+ 0.4nt	+0.0186— 3.2nt
11 9	+0.0329— 3.8nt	+0.0870+ 0.3nt
1110	+o. o846	-0.0411
11-11	—о. 0173	0. 0374
11-12	0. 0029	—o. or37
12— 6	—0. 0216— 0. 6nt	-0.0551+ 0.2nt
12 7	o. 0326+ o. 3nt	+0.0228+ 0.4nt
12 8	+0.0423+ 0.5nt	+0.0342— 0.8nt
12— 9	+0.0150— 1.6 <i>nt</i>	-0.0113- 0.5nt
1210	+0.0539— 0.3nt	-0.0057+ 1.8nt
12—11	o. oo82	o. o495
12—12	0. 0209	+0.0014

$\begin{array}{cccccccccccccccccccccccccccccccccccc$	Arg=i'g'+ig	$-rac{\mathrm{I}}{2}ig(rac{ar{d}^2}{d}$	$\frac{\overline{\mathrm{W}_0}}{\gamma^2} n \delta z$
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$		sin.	cos.
$\begin{array}{cccccccccccccccccccccccccccccccccccc$		" "	
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	0— I		
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	0— 2		_ ′
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	0 3	•	$\begin{array}{cccc} & - & 0.4311n^2t^2 \\ & + 0.000 & - & 0.3nt \end{array}$
$\begin{array}{cccccccccccccccccccccccccccccccccccc$		$+$ 0.0039 n^2t^2	— 0.0460n ² / ²
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	· ·		
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	1+ 2	—0.014 — 0.6nt	+0.021 — 1.7nt
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	1+1	—0. 0360 — 1. 2 <i>nt</i>	-0.0282 + 7.1nt
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	1 0		_ '
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	I I		0.0084 0.99nt
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	I— 2	+0.0073 — 15.9nt	+0.0055 + 21.3nt
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	r— 3	-0.002 - 2.4nt	+0.006 + 1.9nt
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	I— 4	—0. 004	-0.003
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	2+ 2	o. oo7	0.003
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	2+ I	-0.072 + 2.4nt	-0.007 + 5.3nt
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	2 0		+0.0571 — 20.9nt
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	2 I		1
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	2— 2		
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	2 — 3	-0.001 + 99.6nt	+0.004 + 47.0nt
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	2 — 4	-0.003 + 9.7nt	0.000 + 4.7nt
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	3+ I		-0.039 - 0.2nt
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	3 0		
$\begin{array}{cccccccccccccccccccccccccccccccccccc$		· ·	
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	-		i l
$\begin{array}{cccccccccccccccccccccccccccccccccccc$			i l
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	_		
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	4 0	-0.007 + 0.6nt	+0.003 + 0.8nt
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	4— I	-0.0504 + 3.71nt	+0.0101 + 6.13nt
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	4 2	-0.0016 - 2.71nt	+0.0009 + 1.08nt
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	4— 3	—0. 0329 — 4. 6nt	+0.0193 + 0.4nt
5 0 —0.001 + 25.2nt —0.001 + 9.1nt 5— 1 —0.0057 +259.3nt —0.0040 + 94.6nt	4— 4	-0.045 + 2.3nt	+0.045 + 9.3nt
5— 1 —0.0057 +259.3nt —0.0040 + 94.6nt	4 5	-0.004 - 4.8nt	+0.005 + 0.6nt
	5 0	-0.001 + 25.2nt	' '
	5 1		1
	5— 2	-0.015745- 3.290nt	-0.038551+ 2.342nt
. 5— 3 +0.0151 —114.5nt —0.0092 +248.1nt	· 5— 3	· · · ·	
5-4 $+0.006$ $-62.9nt$ -0.046 $-26.8nt$	5— 4		
5— 5 -0.014 8.7nt0.013 2.0nt		-0.014 8.7nt	-0.013 - 2.0nt
5— 6 — 0.7nt — 1.7nt	5— 6	0.7nt	— 1.7nt

Arg=i'g'+ig	$-rac{\mathrm{I}}{2}\Big(rac{\overline{d^2\mathbf{W}_0}}{d\gamma^2}\Big)n\delta z$	
	sin.	cos.
i' i 6— 1	,, +o. 0004	,, ,, ,, ,, ,, ,, ,, ,, ,, ,, ,, ,, ,, ,
6— 2	—0. 0038 — 0. 36nt	-0.0035 + 0.69nt
6— 3	+0.0418 2.99nt	-0.0297 - 3.06nt
6-4	+0.0092 + 0.9nt	+0.0158 — 1.7m²
6 5	-0.005 - 0.1nt	0.000 + 1.2nt
6— 6	+0.001 - 0.7nt	-0.004 - 0.7nt
6— 7	+ 0.6nt	— 0. 4nt
7— 2	-0.0061 - 0.3nt	-0.0013 + 0.6nt
7— 3	-0.0008 - 0.84nt	-0.0081 + 0.10nt
7— 4	-0. 2645 +17. 8nt	-0. 2776 +22. 4nt
7 5	+0.057 — 4.2nt	-0.068 - 2.7nt
7— 6	+o. oo6	—o. oo7
8— 3	-0.0001 + 0.08nt	-0.0009 - 0.09nt
8 4	+0.0765 + 0.68nt	+0.0162 - 7.75nt
8 5	+0.030 — 2.9nt	-0.036 - 1.6nt
8— 6	+0.011 0.0nt	+0.003 — 0.6nt
9— 3	-0.0002 + 0.05nt	0.0004 0.10nt
9— 4	+0.0038 — 0.18nt	-0.0011 - 0.39nt
9 5	+0.0023 — 3.8nt	-0.0377 + 0.3nt
9 6	+0.032 + 0.2nt	+0.008 — 2.2nt
9— 7	+0.001	+0.003
10— 4	-0.00002+ 0.181 <i>nt</i>	+0.00006+ 0.036 <i>nt</i>
10— 5	+0. 1034 +26. 0nt	+0. 2050 —16. 8nt
10-6	-0.007 + 2.3nt	+0.022 + 1.3nt
10— 7	-0.002 + 2.0 mt	+0.015 - 0.7nt
11-5	+o. ooc <u>5</u>	+0.0004
11- 6	+0.0041 — 0.5m2	-0.0031 - 0.5nt
11 7	+0.002 + 0.5nt	+0.006 — 0.4nt
11 8	0.004	+0.001
12— 5	+ 0.02nt	+ 0.03sst
12— 6	0.0023 0.0nt	+0.0066 + 0.1nt
12 7	+0.002	- 0.002

If we now add the three portions of $\frac{d \cdot n\delta^2 z}{ndt}$, which have just been given, we shall have the value of this quantity. In $\overline{\delta W_0}$ we give k_0 such a value that $n\delta^2 z$ may have no term proportional to t, and k_1 and k_2 are so assumed that the terms having the argument g may vanish. For this it is found necessary to put $k_1 = -0$.4862 and $k_2 = -0$.8170. In integrating the terms depending on the arguments 5g' - 2g and 10g' - 4g we have equated the motion of the latter, and have proceeded in a way precisely similar to that followed in deriving δW_0 from δT . By joining the first order

with the second order terms, it is found that, as far as these two arguments are concerned, we have

$$\frac{d \cdot n\delta z}{ndt} = \begin{bmatrix} " & " & " \\ [5.88438 + 0.01000896nt] \cos (5g' - 2g) + [-14.13462 + 0.00596165nt] \sin (5g' - 2g) \\ + [0.16091 + 0.00004537nt] \cos (10g' - 4g) + [-14.13462 + 0.00003542nt] \sin (10g' - 4g) \end{bmatrix}$$

Setting aside quantities of the third order this expression can be replaced by the following:

$$\frac{d(n\delta z)}{ndt} = \frac{(1.1849912) - (7.2193138)nt}{(9.37255) + (4.7058)} \cos \left[\frac{5g' - 2g + \frac{6}{7} 23}{23} \frac{51.22 - (6.8768938)nt}{51.22 - (6.3858)} \right]$$

The integrating factors for the equated arguments are given by

$$\log \mu = 1.8970002$$
 $\log \mu = 1.56699$

After neglecting certain quantities of the third order the integrated expression can be put under the form

$$n\delta z = \begin{bmatrix} 773.7148 + 0.785671nt \end{bmatrix} \sin(5g' - 2g) + \begin{bmatrix} 773.7148 + 0.785671nt \end{bmatrix} \sin(5g' - 2g) + \begin{bmatrix} 773.7148 + 0.001673nt \end{bmatrix} \sin(10g' - 4g) + \begin{bmatrix} 773.7148 + 0.001673nt \end{bmatrix} \sin(10g' - 4g) + \begin{bmatrix} 773.7148 + 0.001673nt \end{bmatrix} \cos(10g' - 4g)$$

By subtracting the corresponding terms of $n\delta z$, found in Chapter II, we get

$$n\delta^2 z = \begin{bmatrix} 51.3265 + 0.785671nt \end{bmatrix} \sin(5g' - 2g) + \begin{bmatrix} 77.3774 + 0.001308nt \end{bmatrix} \cos(5g' - 2g) + \begin{bmatrix} 6.9725 + 0.001673nt \end{bmatrix} \sin(10g' - 4g) + \begin{bmatrix} 7.3774 + 0.001308nt \end{bmatrix} \cos(10g' - 4g)$$

If we add the two portions of $\frac{d \cdot \delta \nu}{ndt}$ we have the value of this quantity. In integrating we are obliged to derive the constant term of $\delta \nu$ from another equation. It is known that this term is the same as that of the expression*

$$-\frac{1}{6} \left(k_0 + \frac{3}{2} \frac{e}{P_1} k_1\right) + \frac{1}{3} \left(\frac{d \cdot \delta z}{dt} + \frac{1}{2} \nu\right)^2 + \frac{3}{4} \nu^2$$

 k_0 is equivalent to the negative of the sum of the constant terms of $\delta \overline{W}_0$, $\left(\frac{d\overline{W}_0}{d\nu}\right)n\delta z$, and ν^2 ; that is, $k_0=+$ 0".1018. It has already been stated that $k_1=-$ 0".4862. In computing the constant term of $\left(\frac{d\cdot\delta z}{dt}+\frac{1}{2}\nu\right)^2$ it is necessary to take into account only the terms corresponding to the ten arguments having the largest coefficients. We make use of the expressions for $\frac{d\cdot\delta z}{dt}$ and ν given in Chapter II. It is found that this constant term is +0".1225. The constant term of ν^2 has already been found to be +0".0498. Thus, the constant term of $\delta \nu$ is +0".0671.

The values of $n\delta^2z$ and $\delta\nu$ follow. The proper number of decimals has been restored to the coefficients multiplied by nt and n^2t^2 :

	$n\delta^2 z$	
Arg=i'g'+ig	sin,	cos.
i' i	" "	" ", 000003182n2t3
		0000004153n ³ / ³
O I	—. 256776nt	—. 226275nt
	$+.000087035n^2t^2$	—. 000147259n ² t ²
0— 2	+0. 1531—. 003108nt	+0.1140—.002723nt
	+. 000001541 <i>n</i> ² <i>t</i> ²	$00007173n^{9}t^{9}$
o— 3	0. 0343 000075nt	+0.0307—.000066nt
_	+. 000000045 <i>n</i> ² <i>t</i> ²	$000000251n^2t^2$
0— 4	+0.0005000002nt	+0.0023—.000002nt
	$+.000000001n^9t^2$	—. $00000010n^2t^2$
I+ 4	-0, 0002	+0.0001
1+3	0. 0043	+0.0026
1+ 2	-0.0631 .000000 <i>nt</i>	+0.1032+.000002nt
1+ 1	-0. 7000 000034 <i>nt</i>	-0.6043+.000149nt
1 0	-1.2437+.001758nt	+1.0053+.002130nt
1— 1	-0.3651+.000049 <i>nt</i>	0. 5446 000082nt
I 2	+0. 2285—. 000269nt	+0. 1214+. 000269nt
I — 3	-0.021600001 <i>2nt</i>	+0.0611+,000008nt
I— 4	—o. 014 6	-0.0104
2+ 2	-o. o1o7	o. 006 1
2-1	-0.4225+.000016 <i>nt</i>	-0.0440+.000009nt
2 0	-2. 3423+. 000882nt	+4.0897—.000056nt
2— 1	—0. 5817+. 012769 <i>nt</i>	—I. 4442—. 020319nt
2 2	-0. 1487+. 000424 <i>nt</i>	+0. 2580—. 000013nt
2— 3	-0.0194+.001144 <i>nt</i>	+0.0727+.000480 <i>nt</i>
2 4	-0.0265+.000048nt	-0.0042+.000018nt
2— 5	0.0010	0,0002
3+ I	+0.0067—.000001 <i>nt</i>	0.0535 .000000nt
3 0	-0.0024000052nt	—3. 1601—. 000084nt
3— 1	—2.8597—.002506nt	-2. 2157 003737nt
3— 2	-0.0403+.018630 <i>nt</i>	-0. 1725+.010703nt
3— 3	0.0712000225nt	-0.0584+.000131nt
3— 4	-0.0301000026nt	-0.0015+.000149nt
3- 5	-0.0007+.000002nt	-0.0115+.000006nt
4 0	—0. 0138—. 000001 <i>nt</i>	+0.0075+.000001nt
4— I	0. 6652 000135nt	+0. 1571+. 000035nt
4— 2	—0. 1439+. 008464 <i>nt</i>	+0. 2365+. 000071nt
4— 3	-0.2140+.001197 <i>nt</i>	+0.0632—.003658nt
4— 4	0.0430+.000059nt	+0.0346+.000044 <i>nt</i>
4— 5	0.0038000044 <i>nt</i>	-0.0089+.000009nt
4— 6	+0.0056 .000000nt	-0.0015+.000001 <i>nt</i>

A :/-/ :	76	$a\delta^2z$
Arg=i'g'+ig	sin.	cos.
i' i	<i>11 11</i>	" "
5 0	+ 0.0018+.000116nt	— 0.0005+.000036nt
5— 1	+ 0. 1461+. 004996 <i>nt</i>	— 0.0482+.001397 <i>nt</i>
5— 2	+51. 3265+. 785671 <i>nt</i>	+118.2806477027nt
5— 3	— 5.7355+.014559nt	— 1.4196+.084928nt
5— 4	— 0.0745+.000188nt	— 0. 1061+. 000536nt
5— 5	0.0087000025 <i>nt</i>	— 0.0093+.000018nt
5— 6	+ 0.0037—.000007 <i>nt</i>	— 0.0016—.000015nt
5— 7	+ 0.0011—.000001 <i>nt</i>	+ 0.0022+.000001nt
6— т	+ 0.0006	+ 0.0003
6— 2	+ 0.0449+.000037nt	+ 0.0424—.000098 <i>nt</i>
6 3	+ 0.6533+.001034nt	— 0.5307—.001204 <i>nt</i>
6— 4	- 0.0217+.000713nt	- 0.0132000307nt
6 5	+ 0.0049+.000027 <i>nt</i>	+ 0.0059+.000213nt
6— 6	+ 0.0029000005nt	— 0.0018+.000002nt
6— 7	+ 0.0007+.000005 <i>nt</i>	+ 0.0007—.000006nt
7— 2	+ 0.0160000004nt	+ 0.0084+.000001 <i>nt</i>
7— 3	— 0.8276+.001403nt	— 2. 1955+. 000509nt
7— 4	— 2.8854+.000694 <i>nt</i>	— 2. 7617—. 000913nt
7— 5	+ 0.0543+.000126nt	— 0. 1058+.000164nt
7 6	+ 0.0055—.000072nt	— 0.0027+.000027nt
7— 7	— 0.0006 .000000nt	+ 0.0003—.000002nt
7 8	— 0.0006+.000003nt	+ 0.0003—.000001nt
8— 3	— 0. 2491+. 000111nt	0. 1729—. 000024nt
8 4	+ 2.0006000055nt	+ 0.4877+.000425nt
8— 5	+ 0.2492+.000117nt	— 0.3730+.000058nt
8— 6	+ 0.0183—.000049nt	— 0.0003+.000055nt
8— 7	0.0005000014nt	+ 0.0018000023nt
8 8	+ 0.0005+.000001nt	— 0.0009—.000001 <i>nt</i>
9 3	— 0.0098+.000002nt	+ 0.0016 .000000nt
9— 4	+ 0.5369+.000045 <i>nt</i>	— 0. 1485+. 000105 <i>nt</i>
9 5	+ 0.0201+.000102nt	— 0.5507—.000009nt
9 6	+ 0. 1413—. 000009nt	+ 0.0404+.000044 <i>nt</i>
9 7	+ 0.0041—.000025nt	+ 0.0040—.000017nt
9— 8	- 0.0005+.000010nt	0.0005000009nt
10— 4	+ 6.9725+.001673nt	- 7.3774+.001308nt
10 5	+ 1.6120—.000446nt	+ 3. 1014+. 000292nt
10 6	+ 0.1043+.000003nt	+ 0.0235+.000023nt
10 7	0.0048000017nt	+ 0.0540 .000000nt
10— 8	— 0.0002+.000004 <i>nt</i>	+ 0.0017000014nt
10 9	0.0000+.000002nt	+ 0.0009+.000001nt
11 4	+ 0.0014	0.0049
11 5	+ 0.0841000005nt	+ 0.0563+.000011nt
11— 6	+ 0.0634+.000006nt	0.0520+.000006nt
	<u> </u>	

	$n\delta^2z$							
Arg=i'g'+ig	sin.	cos.						
i' i 11— 7 11— 8 11— 9 12— 5 12— 6 12— 7 12— 8	+0.018400007nt -0.0220 .00000nt -0.003+.00005nt +0.0806+.00001nt +0.0379+.00001nt +0.018500002nt -0.0159 .00000nt	+0.0412+.00005nt +0.003100007nt +0.0001 .00000nt +0.0047+.000011nt -0.0962+.00003nt +0.0145+.00002nt +0.011600001nt						
12— 9 12—10	-0.0001+.000001nt	-0.0077000001nt -0.0004+.000002nt						

,,,,	8	ìv
Arg=i'g'+ig	cos.	sin.
<i>i' i</i> o o	,, +0.0671—.003098nt	" "
о— 1	$+.00000350n^2t^2$ +0.0845128514nt	+0.0628+.113101nt
o— 2	+. 000043692n ² t ² +0. 1134—. 003104nt	+. 000073493n³t² -0. 0852+. 002719nt
o 3	+.000001255n ² l ³ -0.0272000110nt	+. 000003929n ² t ² -0. 0273+. 000100nt
0— 4	$+.00000051n^2l^2$ 0.0012—.000005nt $+.00000003n^2l^3$	$+.000000217n^2t^2$ $-0.0032+.000004nt$ $+.00000013n^2t^2$
I+ 2	+0.0544+.000003nt	+0.0779+.000005nt
1+1	+0.4368+.000025nt	0. 3703+. 000118nt
1— I	+0. 3004—. 000460nt —0. 1165—. 000005nt	+0. 2230+. 000502nt +0. 1858+. 000047nt
I— 2	+0.1551—.000115nt	0. 0836 000098nt
I— 3 I— 4	0.0176000010nt 0.0135	-0.0504000004nt +0.0086
2+ 2	+0.0126	—o. oo54
2+ I 2 0	+0. 3063—. 000018nt +1. 0147—. 000471nt	-0. 0215+. 000037nt +1. 7470 000070nt
2 1	0.0342+.001342nt	+0.1801+.002001nt
2— 2	—0. 0977+. 000179nt —0. 0178+. 000503nt	0. 1557+. 000044nt 0. 0615 000202nt
2— 3 2— 4	-0.0237+.000022nt	+0.0027—.000007nt
3+ 1	-0.0053+.000020nt	-0.0585000001nt
3 0	0. 0000+. 000288nt +0. 3359+. 000465nt	—1. 8180+. 000009nt —0. 3171—. 000509nt

	δ	ν
Arg=i'g'+ig	cos.	sin.
i' i	11 11	n n
3— 2	-0.0209+.007833nt	+0.0744—.004512 <i>nt</i>
3— 3	-0.0424+.000015 <i>nt</i>	+0.0310000110nt
3— 4	0.025300009 <i>nt</i>	+0.0015—.000086 <i>nt</i>
3— 5	0.0013+.000001 <i>nt</i>	+0.0105—.000006 <i>nt</i>
4 0	+0.0109000002 <i>nt</i>	+0.0052+.000005 <i>nt</i>
4— I	+0.2265+.000034 <i>nt</i>	+0.0510+.000078 <i>nt</i>
4— 2	-0.0340+.00197 <i>2nt</i>	0.0519+.000048 <i>nt</i>
4— 3	-0.1263+.000750nt	-0. 0351+. 002262 <i>ni</i>
4— 4	-0.0232+.000040 <i>nt</i>	-0.0117+.000021 <i>nt</i>
4 5	—0. 0036—. 000029nt	+0.0092000007nt
4 6	+0.0054	+o.0016
5 0	-0.0015000130nt	-0.0012+.000042nt
5— 1	—0. 0688—. 002741 <i>nt</i>	—0. 0282+. 000803 <i>nt</i>
5— 2	+0.0195—.004003 <i>nt</i>	+0.0470—.003199 <i>nt</i>
5 3	—2.8617+.007113 <i>nt</i>	+0.7011—.042382nt
5 4	-0.0779+.000379nt	+0.0663—.000878 <i>nt</i>
5 5	o. 0055 000007 <i>nt</i>	+0.0076+.000030 <i>nt</i>
5— 6	+0.0049—.000007 <i>nt</i>	+0.0024+.00001 <i>3nt</i>
5— 7	+0.0013—.000002nt	0.0026+.000001 <i>nt</i>
6— 1	o. ooo8	o. oo15
6 2	-0.0068+.000002nt	+0.0096—.000021 <i>nt</i>
6 3	+0.2134+.000316nt	+0. 1756—. 000340 <i>nt</i>
6— 4	-0.0155+.000487 <i>nt</i>	+0.0211+.000198 <i>nt</i>
6— 5	+0.0068+.000029nt	+0.0005—.000168 <i>nt</i>
6— 6	+0.0017000003 <i>nt</i>	+0.0010000006nt
6— 7	+0.0016+.000003nt	-0.0015+.000004 <i>nt</i>
7— 2	-0.0013+.000006nt	+0.0035+.000004 <i>nt</i>
7-3	-0. 1421+. 000131 <i>nt</i>	+0. 2932—. 000049nt
7— 4	—1. 6456+. 000245 <i>nt</i>	+1.5693+.000316 <i>nt</i>
7— 5	0.0026+.000075 <i>nt</i>	+0.0782000101 <i>nt</i>
7— 6	+0.0047—.00006 <i>2nt</i>	+0.0005—.000024 <i>nt</i>
7— 7	+0.0004000003 <i>nt</i>	-0.0005000002nt
7— 8	—0.0005+.000002nt	-0.0007000001 <i>nt</i>
8 3	+0.0492—.000019 <i>nt</i>	0. 0306 00001 <i>2nt</i>
8— 4	+0.8527000012nt	0. 1940 000077 <i>nt</i>
8— 5	+0. 1871+. 000067 <i>nt</i>	+0. 2716—. 000035nt
8— 6	+0.0152000041nt	+0.0067—.000044 <i>nt</i>
8 7	-0.0009000016nt	-0.0020+.000021nt
8 8	+0.0002—.000001 <i>nt</i>	+0.0002+.000002nt
9 3	+0.0048—.000001 <i>nt</i>	0.0002000002nt
9— 4	+0. 1237+. 000007nt	+0.0447—.000013nt
9 5	+0.0179+.000036nt	+0.3402+.000002nt
	, ,,,	

A	δν						
Arg=i'g'+ig	cos.	sin.					
i' i 9— 6 9— 7	" " +0.1113—.000008nt +0.0052—.000025nt	" " -0.0281000025nt -0.0034+.000015nt					
9— 8 10— 4	—0.0006+.000010nt —0.0852—.000103nt	-0.0004+.000010nt -0.1306+.000032nt					
10— 5 10— 6	+0.8092+.000049nt +0.0942+.000012nt	—1. 5538+. 000029nt —0. 0306—. 000025nt					
10— 7 10— 8 10— 9	-0.002200009nt -0.0006+.00004nt 0.0000+.00005nt	-0.0481+.000002nt -0.0030+.000013nt -0.000100003nt					
11— 5 11— 6	+0.0284—.000002nt +0.0423+.000001nt	-0.017000003nt +0.0323+.00001nt					
11 7 11 8 11 9	+0.0139—.000004nt -0.0192—.000001nt -0.0018+.00008nt	-0.0334000001nt -0.0034+.000007nt -0.0001000001nt					
12— 6 12— 7	+0.0185+.000005nt +0.014000001nt	+0.0445000003nt					
12— 7 12— 8 12— 9	-0.013100002nt -0.0035+.000004nt	-0.011500002nt -0.0088+.00003nt +0.0089+.00001nt					
12—10	-0.000I .000000nt	+0.0004—.000003nt					

CHAPTER XIII.

CALCULATION OF THE PORTION OF ST' NOT FACTORED BY n't.

We have now to go through the same processes for Saturn as, in the three preceding chapters, we have gone through with for Jupiter. In determining the portion of $\delta T'$, which follows, a table of limits for the retention of terms for each argument $\pm \gamma' + i'g' + ig$ was computed from the formulæ

$$\frac{i'n'+in}{n'}\cdot\frac{(i'\pm 1)n'+in}{n'}\times 0''.0005$$

and only those combinations were retained in which at least one coefficient exceeded this limit. It has been deemed advisable to give separately the eight products whose sum forms $\delta T'$:

A	rg=		Α′	$n'\delta z'$	Β'(ν'	c') + X'c'	. F'	$n\delta z$	G'(1	v — c)
жγ'+	$ u\gamma'+i'g'+ig $		sin.	cos.	sin.	cos.	sin.	cos.	sin.	cos.
и	i'	<i>i</i> 0	"	,, —0. 1065891	"	,, +0. 1095091	"	// 0, 0118202	"	// +0.0118041
-1	1	o	—о. 3380	-0.043029	+0.9159	-0. 100097	-0. II20	-0.001867	+0. 3291	-0.001759
—I	2	О	0. 005	0.003	+0. 288	-0. 275	+0.002	+0.721	+0.061	-0. 309
0	I	o	o. 2784	—1. 1850	—0. 5461	+o. 9867	0. 2507	o. 4566	-0.1331	+0.3765
1	0	О	+1.018231	—о. 376723	+0. 337326	—0. 723162	+0. 320340	0. 088791	+0. 114485	0. 190184
_I	3	0	+ 0. 106	-0. I I 2	+0.026	0. 008	+0.050	0.074	+0.047	+0.018
٥	2	О	—1. 376	+2.281	0. 409	+0.555	o. 352	+o. 666	о. 103	+0.072
1	I	0	+2. 220	—3. 923	+0.571	0. 890	+0.411	—o. 770	+o. 084	—0. 105
-1	4	О	0.008	0. 207	+0.048	+0.032	0.021	—о. 175		l l
0	3	o	+o. 377	+3.904	—o. 149	0. 183	+0.044	+1.561	0,005	-0.022
1	2	0	0. 267	7. 003	+0.047	+0.245	0.019	—1. 8 <u>93</u>	+0.003	+0.031
-1	5	О					0. 97	+o. 18		
0	4	О	+1.17	-0. 24	+0.03	0,00	+0.95	—о. 18		
1	3	٥	0. 713	+ 0. 298	— 0. 006	0, 004	0. 294	+0. 120		i
١.			0.70	—0, O2						
i_			-0. 10 -0. 25	-0, 02 -0, 20			-0. 12	0. 03 0. 08		
			+0.05	-0. 20 +0. 14			0, II	+0.08		
	•	- 1	+5.699	-1. 268	— 0. 206	10.005	+0.05		0.001	10.001
—ı—	2	- 1	-3. 76	+0.87	+0.14	+0.025	+1.757		0.031	+0.001
			+0.46	-0. II	TV-14	0, 01	—r. 53	+0.35	+0.02	0.00
	3— o—	- 1	+3. 321	—0. 11 —2. 701	+o. 585	0. 602	+0. 29 +0. 715	0. 07 0. 567	+0.080	-o. o83

Arg=	A'n'	$\delta z'$	B'(v'-	(c') + X'c'	F'	$n\delta z$	G'(1	· - o)
$\mu\gamma'+i^7g'+ig'$	sin.	cos.	sin.	cos.	sin.	cos.	sin.	008.
κ i' i	"	"	"	. "	"	"		, "
0 1 1	— z. 373	+1.807	-0.441	+0.495	—o. 68o	+0.430	0.091	+0. 107
I- 2- I	+ 0. 229	o. 272	+o. o68	0. 082	+0.110	+0.025	+0.023	—o. o36
-I I— I	+ 1.544	—1.833	+0.457	—о. 379	+o. 369	-o. 473	+0.078	0. 143
0 0— 1	— o. 956	+1.234	—o. 36 5	+0.423	0. 403	+0.446	—o. o <u>5</u> 8	+0. 227
1 1 1	+ 0.041	-0. 124	+0.082	— 0. 174	+o. 138	-0. 143	+0.004	—о. 108
—I 2— I	+ 0. 2334	<u> </u>	+0. 3490	+1.3286	+0. 2540	+o. 9889	0. 174 0	0. 8917
o I— I	— o. 193	+0. 198	—o. 147	—0. 189	-0. 204	—0. 781	+0. 197	+1.037
1 0— 1	+ 0.106	+0. 200	—о. 239	—1.342	+0.006	+o. o76	o. 10 4	—o. 497
-ı 3- ı	+ 0.4920	-o. 0761	—о. об79	+0. 2581	o. 2312	—o. 2533	+o. 2597	+0. 2936
0 2 1	+ 0.0391	о. 3377	o. 358 1	-0. 2419	+0. 1212	+0. 1052	о. 3089	—o. 3249
1 1-1	+ o.7886	+o. 6734	+0.5047	+0.0995	+0. 0591	+0.0750	+0. 1532	+0. 1772
—I 4— I	+ o. o283	-o. o7o4	+o. 3058	+0. 1104	o. o986	+0, 0204	+0.0549	+0.0067
o 3— 1	+ 2.6870	+0. 2307	2. 0576	<u> </u>	o. 10 7 0	o. 1974	—о. 1688	0. 0505
I 2— I	+ o. 5773	+0.7208	+1.6494	+0.5672	+0.4009	+0. 2232	+0. 1629	+0.0441
—ı 5— ı	+ 0.003	_o. o58	-o. o91	+0.025	<u>—5. 161</u>	+o. 886	o. o98	+o. 104
0 4 1	+10.082	—1. 976	+0.431	o. o65	+4. 118	—о. 677	+o. 111	—о. 108
1 3— 1	— 1.5994	+0.3047	—o. 3264	+o. o36o	o. 3432	+0.0126	-o. o557	⊹ 0. 0386
_т 6— т	o. o ₇₃	0. 043	+0.002	-0.001	+o. o31	+o. 015		1
0 5— 1	0. 004	+0.009	-o. o16	+o. oo8	0,000	0,000		
1 4— 1	+ 0.313	O. 122	+0.014	-0.007	+0. 125	0. 045	+0.004	-0.002
<u>—</u> I 7— I	- 0.004	-0.021						
I I_ 2	+ 0. 22	o. 38			+0.09	—о, 16		
0— 2— 2	— o. 18	+o. 18			0. 10	+0. 10		
I— 3— 2	+ 0.03	u. O2				'		
r o 2	+ 1.87	+3.95	0.05	—о. 17	+0.61	+1.31		
0- I- 2	- I. 4I	_2.88	+0.03	+0.12	— 0. 57	_1. I9		
I— 2— 2	+ o. 23	+0.49	, ,	·	+0, I2	+0.27		
_I I— 2	+ 2.93	+2.21	+0.49	+0.31	+o. 66	+0.52	+o. o6	+o. o 5
0 0-2	- 2. 25	-1.70	_o. 39	0. 24	o. 66	-0.50	-0.07	0.05
I- I- 2	+ o. 37	+0. 23	+0.08	+0.05	+0.13	+0.08	+0.01	+0.01
1 z 2	+ 1.977	+1.000	+0.451	+0. 271	+0.512	+0. 249	+0.107	+0.013
o I— 2	— 1. 463	_o. 706	-0. 379	-0. 200	-0. 479	_0. 219	-0.119	-0.013 -0.018
I 0-2	+ 0.21	+0.05	+0.09	-o. o3	+0.09	+0.03	+0.01	0.00
_I 3— 2	+ 0.766	+0. 125	-1.500	+0.751	_u. 009	+o. o88	+0.069	-o. oo6
0 2-2	— 0. 511	_0.052	+1. 361	o. 686	o. 273	+0.046	0. 312	+0.113
I I 2	+ 0.032	-0. 028	-0. 02 I	+0.022	+0.359	_0. 136	+0. 327	0.113
_I 4— 2	+ 0.1255	_o. 3283	-0. 4340	-0. 2016	—o. o636	+0.0545	+0. 0266	
0 3-2	+ 0. 294	+1.536	+0. 453	+0.429	+0. 129	+0.416	+0.0200	— 0. 1177 — 0. 172
I 2— 2	— 0. 248	+0. 247	0. 076	-0. 03I	-0. 127	_0. 571		+0.173
1	+ o. o9308	+0. 247 +0. 87656	+0.09341	0. 96932	+0.11520	1	-0.059	-0. 130
0 4-2	+ 0.09308	-0. 1189	0.0007	0. 90932 0. 0308	_0.0515	—0. 73773 —0. 6485	o. 09099	+0.71614
1	- 0. 3124	+1.6932	-0. 1003	+1.0233	_0.0313 _0.0423	t I	+0.0918	o. 8377
· ·	1	1	-0. 1003 -0. 01846	1		—0. 1092	0, 0299	+0.4125
_1 6— 2	+ 1.47830	+3.23313		+0.02240	—o. 00039	-0.00314	+0.00594	+0.00330
0 5— 2	- 0. 0843226		+0.0460054			+0.0091938		
I 4-2	+ 1.29547	+3.02602	—o. o5540	—0. 12780	-0.00279	+0.01556	+0.00668	-0.02291
—I 7— 2	+ o. 850	+0. 483	+0.003	+0.003	0, 004	0. 004	+0.004	0.000
								1

Arg=	$\mathbf{A}'n$	'δz'	$\mathbf{B}'(\nu'-a)$	(') + X'c'	$\mathbf{F}'i$	$\iota \delta z$	G'(<i>v</i>	— c)
$\mu\gamma'+i'g'+ig$	sin.	cos.	sin.	cos.	sin.	cos.	sin.	cos.
и i' i o 6— 2	,, —0. 2755	,, —o. 1396		.,, 0. 0085	+0.0025	// +0. 0034	o. 0028	.,, —0.0027
I 5— 2	-o. oo363	0. 00284	+0.00553	+0.00452	+0.00231	-0.00128	—0. 00030	+0.00247
I 8 2	+0. 177	-0.010	+0.001	0.000				' "
0 7— 2	_o. o95	+0.008	0.000	0.001				
ı 6— 2	+0.003	-0.002	+0.003	0.000				
_I 9— 2	+0.022	-o. o15						
0 8 2	0. 014	+0.009						
—r o— 3	+0.43	+0. 16			+0.17	+0.06		
o_ i_ 3	o. 25	—о. 17			0. 13	_o. o8		
I— 2— 3	+0.04	+0.03						
-I I-3	—2. 38	+1.90	+0.13	0.07	o. 85	+o. 65		
o o- 3	+1.85	—1.50	-o. 1o	+0.05	+0.78	0.62		
I I 3	0. 37	+0. 29			-0. 19	+o. 15		
— I 2— 3	-1.17	+2.62	—о. 13	+0.38	—о. 30	+o.65	-0, 02	+o. o5
o 1— 3	+0.95	-2. I2	+o. 12	o. 32	+o, 28	0. 62	+0.02	o. o5
I 0— 3	—o. 15	+0.39	-o. o3	+0.07	0, 05	+0.14		
—т 3— з	-0.42	+1.84	0. 19	+0.44	—o. o7	+0.50	0.00	+o. 13
0 2-3	+o. 3o	—1.45	+0. 23	0. 39	+0.02	-0.44 -	-0. 02	—o. o8
I I 3	-0. 02	+0.23	-o. o3	+0.07	+0.06	+0.05	+0.02	-o. or
—I 4— 3	+o. o6o	+0.572	0. 783	о. 966	<u> </u>	0. 125	0. 302	—o. 419
0 3— 3	+0.01	-o. 27	+o. 5 8	+0.70	+o. 53	+0.76	+o.64	+o. 95
I 2- 3	+o. o3	+0.09	-o. o3	-0.04	— 0. 5 8	—0. 91	о, 6о	о. 87
—ı 5— 3	-1.062	+0.528	-0. 204	—o. 372	0. 209	+0.071	+0.111	+o. o36
0 4-3	+o. 604	-o. 263	+0. 271	+0.313	о. 078	0. 152	o. 271	—0. 096
I 3— 3	0, 021	0.007	— 0. 069	0.032	+o. 323	+o. 155	+0.279	+0.132
—ı 6— 3	0. 157	+0.529	+1.724	— 0. 207	0. 203	+o. 138	+0.098	—о. 016
o 5— 3	-2. 364	0,060	—2. 123	+0.237	+0,004	—o. об9	—o. o6 7	+0.006
I 4— 3	+0.020	<u> </u>	+0. 247	-o. o2 5	+0.062	+0.036	0. 024	-0.001
-I 7-3	+1.1923	—0. 5 863	+0.0136	-o. o131	+0. 2669	—о. 1755	0.0212	+0.0144
o 6— 3	—8. 529	+5.648	+0.043	·o. 084	-3.448	+2.391	+0.069	-0.064
I 5— 3	+0.043	+0.005	0. 039	+0.029	+4. 336	—3. o21	0. 074	+0.072
—ı 8— 3	o. o188	+1.4384	-0,0059	0,0013	-0.0011	+0. 1820	o. oo36	+0.0055
o 7— 3	—о. 6786	—0. 3236	 -0.0093	0,0028	—о. 1373	-0. 0510	+0.0052	o, oo8o
1 6— 3	+o. 1335	-0.0518	o. 0045	+0.0035	+0.0537	o. o256	-0.0007	+0.0017
— I 9— 3	+0. 1468	+o. 3839	0.0012	+0.0004	+0.0142	+0.0372	+0.0002	+0.0006
o 8— 3	o. 1457	0, 2097	4-0.0007	0. 0065	—o. o196	0. 0285	-0.0001	0, 0015
I 7 3	+0.0224	o. oo59	+0.0001	+0.0050	+0.0044	-0.0002		
—I IO— 3	+0.054	+0.051			0.000	0.002		
0 9—3	— о. 036	0. 022			-0.001	+0.002		
o 10—3	+0.024 0.008	0, 041 0, 002	0.005	0. 006	+0.005	0. 003		
-1 I— 4	o. o ₇	+0.40			0. 03	+o. 16		
0 0 4	+0.09	_0. 48 _0. 28						
_1 2— 4	—1. 59	—0. 23 —1. 23	+ 0. υ6	+0.09	+0.05	-0. 13		
o I— 4	+1.32	+0.99	—0. 02		—0. 57 —0. 55	-0.47 +0.43		
- 4	1 3	1 5. 33	0.02	0. 04	+o. 55	1 5. 43		

I Arc	σ <u></u>	$\mathbf{A}'n$	'δz'	$B'(\nu'-c')+X'c'$		$\mathbf{F}'n\delta z$		$G'(\nu-c)$	
Arg κγ'+i	i'g'+ig	sin.	cos.	sin.	cos	sin.	cos	sin.	cos.
н 1	i' i 0-4	// 0. 29	 0. 23	"	"	// —0. 14		"	"
_ı	3- 4	-2.09	-0.42	— 0. 32	—o. o6	-0.54	0. I2	+0.04	0.00
0	2— 4	+1.73	+o. 3o	+0. 25	+0.04	+0.52	+0.11	+0.03	0.00
I	I 4	0. 34	0.07	0.06	O. OI	o. 11	0.02	'	
— 1	4 4	—1. 5o	+0.04	0. 40	-0. O2	0.43	-0.02	0. 05	-0.02
О	3 4	+1.20	0, 06	+o. 32	+0.02	+0.45	+0.11	+o. 11	+0. 10
I	2— 4	— 0. 22	+0.02	0.04	+0.01	0. 10	o. 15	o. o6	_o. o8
—r	5 4	о. 64	+0.34	+o. 56	-o. 71	o. 25	+0.21	+o. 21	_O. 22
0	4 4	+0.50	0. 23	o. 38	+0.50	+0.11	_o, 1o	o. 26	+0.22
1	3— 4	-o. o6	+0.03	+0.07	-o. o8	+0.12	-0.02	+o. 11	-o. o6
1	6— 4	o. 52	— 0. 55	+o. 33	— о. 26	_O. 12	—о. 32	+o. oi	-o. o5
0	5— 4	+0.18	+o. 38	-o. 37	+o. 22	+0.06	+0.33	_0. 04	+0.08
1	4— 4	-0.04	0.06	+0.07	-0.04	+0.02	-o. 13	+0.02	0.09
-1	7 4	0. 232	—2. 157	+0.374	+1.039	+o. 196	—0. 204	+0. 119	+o. 378
0	6— 4	о. 383	+1.716	-0. 249	— 0.673	0. 870	+0.073	-0, 229	— 0. 793
1	5 4	-0.05	0.06	+o. o1	0.00	+1.02	+0.17	+0.20	+o. 68
-1	8— 4	—5. 631	—5. 352	+0.130	+o. o8o	—1. 43o	-1. 359	+0.029	+0.027
o	7-4	+3. 138	+3.031	—о. 108	-0.072	+1.150	+1.108	-o. o23	0. 045
I	6— 4	о. 183	—о. 155	+0.014	-0.008	0. 110	-o. 106		
—I	9— 4	-2.837	0. 704	+0.022	-0.002	0. 561	о. 139	0, 001	o. 00 0
О	8 4	+1.870	+0.482	-0. 029	+0.002	+0.481	+0. 124	0,000	0.001
r	7— 4	0. 130	+0.026	+0.002	-0.005	-0.042	+0.011		
— г	10-4	0. 66417	+· o. 19695	+0.00305	-0.00174	0. 10326	+0.03050	-0.00217	+o. 00 050
О	9— 4	+0. 4863	-o. 1374	-0.0016	+0.0016	+0.0958	0. 0267	+0.0025	0. 0009
1	8— 4	-0.026	+0.033	-0.003	0.000	0. 006	+0.008		
—ı	11 4	-0.09116	+0.09913	0.00010	0.00017	-o. o1165	+0.01256	-0.00009	+0.00014
0	10-4	+0.069759	o. o73644	-0.000101	+0.000255	+0.011093	-o . 011 609	+0.000080	—0. 000113
1	9— 4	-0.00293	+0.01166	+0.00029	0.00031	-0.00005	∔0.00168	+0.00005	0.00000
0	11 4	+0.0038	-0.0167			+0.0005	-0,0022		
Ι.									
I	2 5	o. 33	0,00			—o. 13	0,00		
0	1 5	+0.25	+0.04			+0.12	+0.02		
	3— 5	+0.51	—1. 16			+0.21	0.43		
0	2— 5	-0.41 +0.10	+1.00			-0. 19	+0.42		
_I	1 — 5 4 — 5	o. o6	—0. 23 —1. 48	0.07	-0.79	+0.05	-0. II		
1		±0.06		_0.0I	—o. 18	-0.01	0.4I		
D	3 5	· ·	+1.28	+0.01	+o. 16	10.0—	+0.35		
_I	2— 5 5— 5	0. 02 0. 29	—0. 27 —1. 05		_0.20	—0.0I	0, 09		
1	5 5			—0. 05 ⊥0. 03	—0. 29 ⊥0. 20	-0.07	-0. 24		
0	4 5	4 -0. 26 0. 06	+0.90 0.19	+0.02	+0. 20	+0.04	+0.21		
_i	3— 5 6— 5	0.00 0.44	_0. 19 _0. 49	+0.53	+0.24		0.00		
1		1	—0. 49 +0. 41		-0. 24 -0. 17	0. 22	0. 20	+0. 19	+0.11
0	5— 5 4— 5	+0.37 -0.01	—0. 04	0.35 +-0.08		+0.19	+0.17	0. 2I	—0. 12
_r		+0.24	_0. 6 ₇	1	+0.05 +0.20	—0. 05 ±0. 31	o. o3	10.05	
i .	7— 5 6— 5	-0. 24 -0. 22	- 1	+0. 26 -0. 23	+0.20	+0. 21	-0.09	+0.06	+0.03
°	- 1	+0.06	+0.55 -0.06		—0. 17 —0. 02	0. 33 0. 16	+0.05	-0. I2	-0.07
'	5 5	T-0.00	0.00	0.00	+0.03	+o. 16	+0.04	+0.03	+0.07

Arg=	$\mathbf{A}'n'\delta z'$		$B'(\nu'-c')+X'c'$		$\mathbf{F}'n\delta z$		$\mathbb{G}'(\nu-c)$	
<i>μγ'</i> + <i>i</i> ⁷ <i>g'</i> + <i>ig</i>	sin.	cos.	sin.	cos.	sin.	cos.	sin.	cos.
n i' i	"	11	"	11	11	11	"	"
—ı 8— 5	+1.03	I. IO	o. 71	+0.49	+o. 21	0. 25	-0, 14	+0.07
0 7—5	o. 76	+o. 88	+o. 55	o. <u>3</u> 8	0. 20	+0.22	+0. 12	o. o7
I 6- 5	+0.12	0, 11	o. o8	+0.04	+0.02	-0.01		
—ı 9— 5	+3.429	5. 790	0. 084	+o. 185	+1.004	-1.672	—o. o14	+o. o33
0 8 5	—2. 28	+3.89	+0.08	-o. 18	—о. 85	+1.45	+0,02	-0.02
1 7— 5	+0.25	0.48	0.00	+0.03	+0.15	0. 25		
I IO 5	+o. 135	—3. 060	+0.009	+o. o35	+0.038	-0.710	+0.001	+0.004
0 9— 5	—0. 110	+2. 248	0.001	— 0. 028	0, 038	+0.649	-0.001	-0.004
1 8 5	0. 044	o. 252			0. 016	—o. o 96		
-I II- 5	—о. 380	7 49	+0.003	+0.007	o. o73	o. 146	-0.001	-0.002
0 10 5	+0. 284	+0.579	0.005	-o. oo8	 -0. 066	+o. 1 36		
ı 9— 5	0. 052	— 0. 047			0. 016	-0.015		
—I I2— 5	—0. 148 8	0, 0959	+0.0003	+0.0002	-0. 0244	-o. o161	+0,0004	+0.0001
o 11— 5	+0. 109	+0.074	0,000	0.000	+0.018	+0.013		
1 10— 5	-0.015	-0. 002			+0.002	+0.003	i	
—r 13— 5	-o. o341	0. 0006	0.0000	0.0000	0. 0050	0.0001		
0 12 5	+0.0275		0.0001	+0,0001	+ 0. 0046	+0.0001		
1 11 5	0.0025	+0.0014			—0. 0005	+0.0003		
_r 3— 6	o. o6	_o. 25			o, o3	—o. 10		
0 2-6	0.0	+0.2						
—ı 4— 6	+o. 81	+0.17			+0. 29	+0.07	l	
o 3—6	0.71	-0.14			-0, 29	0.05	l	
1 2-6	+0.17	+0.04			1		1	
—1 5— 6	+1.00	-0. 24	+o. 11	-o. o3	+ 0. 26	o. o5		
0 4-6	-o. 8 ₇	+0.21	— 0. 10	+0.03	_o, 26	+0.06		
I 3— 6	+o. 16	-0.04				'		
— 1 6— 6	+0.70	—о. 38	+0. 1 4	-o. o6	+0.14	_o. o8		
o 5— 6	0.60	+0.34	-0. 12	+0.06	—o. 14	+ 0.08		
1 4— 6	+0.06	0.06		·	i i	'		
—ı 7 6	+o. 28	—0. 43	—о. o8	+0.34	+0.10	-o. 18	-0. o5	+0.15
o 6— 6	0, 24	+0.31	+0.04	-0. 23	—0. 04	+0.11	+o. o5	-0.14
r 8 6	+0.49	-0.02	0. 10	+0.26	+0. 14	+0.14	+0.01	+0.03
0 7—6	-0.42	0. 05	+o. 10	0. 19	0. 12	_o. 13	-0.02	0.07
ı 6— 6	+0.07	+0.04	'				1	
— I 9— 6	+0.99	+0.41	0.47	— 0. 43	+0.20	+0.03	-0. 12	0. Із
0 8—6	_o, 81	0.34	+0.37	+0.34	-0, 22	-0.04	+o. o8	+0.09
1 7—6	+0.15	+0.06	_o. o6	o. o7	+0.02	+0.03	I ' '	'
I IO 6	+4.95	+1.63	-0. 24	0.06	+1.50	+0.50	0.06	-0.02
0 9 6	—3. 65	—I. I7	+0.19	+0.05	—I. 37	-0.45	+0.05	+0,02
1 8-6	+o. 58	+0.19		'	+0. 28	+0.09	l	'
-1 11-6	+2.73	-0.44	—0. 04	+0.02	+0.71	0. 10	0. 02	0.00
0 10—6	—2. I2	+0.33	+0.04	-0.01	—o. 66	+0.09	+0.01	0.00
1 9-6	+o. 30	0. IO	,		+0, 12	—0. 04		
_1 12 <u></u> 6	+o. 683	-0. 532	-o. oo5	+0.004	+0.151	-o. 118		
o 11— 6	—0. 561	+0.423	+0.004	-0.004	0. I45	+0. 109		
1 10— 6	+0.05	-0. 07	,		+0.01	-0,02		
" "	1 0.03	/			1		<u> </u>	

Arg=	$\mathbf{A}'n$	′δz′	B'(v'-	(c') + X'c'	F'1	ιδε	G'(1	· e)
$ \mu\gamma'+i'g'+ig $	sin.	cos.	sin.	cos.	sin.	cos.	sin.	cos.
$oldsymbol{arkappa} oldsymbol{i}' oldsymbol{i}'$	1,	"	11	"	1,	"	"	"
—ı 13— 6	+0.073	-0. 2 00	0.000	+0.004	+0.016	0. 037		
o 12— 6	-0.070	+0. 160			<u> </u>	+ 0. 036	•	1
1 11 6	0.001	-0.023			0,000	0, 006		
—I 4— 7	+o. 2	o. I						
0 3-7	o. I	+o. 1						
—ı 5— 7	0.0	+0.5			0.0	+o. 2	ľ	
0 4-7	0.0	o. <u>5</u>			0.0	-0. 2		ŀ
—ı 6— 7	+0. 29	+0,60			+0.08	+0.17		}
D 5-7	0. 27	—о. 53			-0.07	0. 16		
-I 7- 7	+o. 38	+0.40			+0.07	+0.06		
o 6— 7	о. 33	о. 35			-0.07	o. o5		
_1 8— 7	+0. 32	+0.14	0. 23	0, 02	+0. 15	+0.01	—o. 11	—o, o2
0 7-7	0. 25	—0. 1 2	+0.20	+0.02	0. 18	-0, 02	+0.11	-0.01
—ı 9— 7	+0.06	+o. 36	-0, 22	-0.04	+0.01	+o. o8	—o. o6	+0.03
o 8— 7	0.04	—o. 31	+0.13	+o. o6	0.01	0.07	+o. o6	o. o3
1 7-7	-0.02	+0.07				_		
<u> </u>	-0.03	+0.68	+0. 26	-0.43	+0.02	+o. 18	+0.07	-0. 10
0 9-7	+0.04	0, 63	-0. 21	+0.37	0. 01	0. 20	—0 . 06	+0.09
1 8 7	0.00	+0.12	+0.05	0. 07				,
	o. 37	+3.70	+0.03	-0.19	—0. I 2	+1.17	+0.01	—o, o6
o 10-7	+0. 26	-2.91	0. 02	+0.17	+0.11	-r. 09	—o, oı	+0.05
1 9-7	—o. o6	+0.54	0.00	-0.04	-o. o3	+0. 25		
<u> </u>	+0.82	+2.12	-0.02	-0.04	+0. 23	+0.60		
0 11-7	0.67	—1.74 +0.26	+0.01	+0.03	-0. 21	0. 57		
i io 7	+0. 14 +0. 61	+0. 20 +0. 53	-0, 02	O. OI	+0.06	+0.11		
0 12— 7	-0. 51	+0.53 -0.45	—0. 02 —0. 02	-0. OI	+0. 15 0. 14	+0. 13 —0. 12	1	
1 11 7	+0.09	+0. 06	-0.02	-0.01	+0. 03	—0. 12 +0. 02		
		,			70.03	70.02		
-r 6-8	0.3	+o. 1						
0 5—8	+0.3	—о. 1						
-1 7— 8	—o. 3	+0.2			—o. 1	+0. 1		
. U U U	'	-0. 2			+o. 1	o. 1		
-x 8— 8 o 7— 8	—o. 13	+0.30						
1 .	+0. 1 0. 06	—0. 2 →0. 07	-0.07	_0.70	10.00	10.70	0.07	0.00
o 8— 8	0.00	+0.07	+0.01	-0. 10 +0. 09	+0.02	+0.13	o. or	—o. o8
-1 10-8	0. 21	+o. o8	+0.01	-0. II	0. 02 0. 01	—0. 12 —0. 07		
o 9— 8	+0. 19	0. o5	0. 02	+0.06	+0.01	+0.07 0.06		
-1 11-8	—0. 42	+0.17	+0.32	+0. 10	0. 04	+0.07	+0.07	+0.03
n 10—8	+0.42	-0, 16	—0. 23	-0. 10	+0.07	-0.07	—0.07 —0.07	-0.03 -0.03
1 9-8	-0.07	+0.01	+0.06	+0.03	1,	0/	""	5.03
_1	-2. 53	+0.33	+0.16	-0.01	-o. 82	+0. 10	+0.05	0.00
0 11—8	+2.07	0.30	—o. 17	+0.02	+0.77	—o. 1o	—o. o5	0.00
ı 10— 8	-0. 43	+0.05	,		o. 18	+0.02		3.30
_1 13 8	—ı. 48	+0.97	+0.03	-0.02	-0, 4I	+0.27		
1 11-8	-0.21	+0.15	' /-5		0, 09	+0.06		
		1 - 3			-7.79	1 00		

Arg=	$\mathbf{A}'n'\delta z'$		$\mathbf{B}'(\nu'-c')+\mathbf{X}'c'$		$\mathbf{F}'n\delta z$		$G'(\nu-c)$	
$egin{align*} \mathbf{Arg} = \\ \mathbf{\varkappa} \gamma' + i'g' + ig \end{aligned}$	sin.	COS	sin.	cos.	sin.	cos.	sin.	cos.
κ i' i -1 7-9 -1 8-9 0 7-9 -1 11-9 0 10-9 -1 12-9 0 11-9	-0. 10 +0. 02 -0. 24 +0. 22	-0. 2 -0. 2 +0. 2 -0. 11 +0. 11 -0. 20 +0. 21	-0. 03 +0. 03	+o. 18 -o. 16	o. o7 +-o. o8	0.00 +0.02	"	"
-1 13-9 0 12-9 1 11-9 -1 13-10 0 12-10	+0. 47 —0. 09	-1.57 +1.29 -0.24 -0.13 +0.2	+0. 04 0. 06 0. 11 +0. 1	+0. 14 -0. 13	0. 19 +0. 18 0. 04 0. 06	0. 52 +0. 51 0. 12 0. 08		

Δι κγ'+	g=		C,	$\delta rac{h'}{h_0'}$	D	$\frac{u'}{\cos i'}$	E	$\frac{u_1'}{\cos i'}$	Н	cos i
μγ'+	ı' g' -	⊢ <i>1</i> g	sin.	cos.	sin.	cos.	sin.	cos.	sin.	cos.
и	i' 0	i 0	"	,, 0. 0023032	11	,, —0, 0000019	"	+0.0000019	"	//
_ı	I	0	+0.0011	+0.001441	—0. 000 6	+0.000003	0,0000	-0.000001	+0.0001	-0.000003
_ı	2	0	<u> </u>	+o. o33					,	
0	I	o	+0.0372	-0. 0677						
—1	3	0	-0.012	-0.024						
٥	2	0	+o. o26	+0.052						
1	I	o	o. oi i	0. 029						1
—r	4	o	+0.004	+0.008						
0	3	0	-0.009	_o. o15					:	
I	2	0	+0.004	+0.007						
-1	0-	- I	+o. 004	+0.009						
0-	- I-	- I	0, 002	-0.020						
1	- 2 -	- I	0. 004	+0.010					1	
—т	1-	- I	+o. oo8	+0.092						
0	0-	- I	0. 004	-0. II4						
1	- I-	- I	-0.002	+0.049						
—ı	2-	- 1	—0. 1625	0. 7965						
0	I—	- I	+0.321	+1.601						
1	0-	- I	—о. 165	—о. 8o8						
—I	3-	- I	+0.0124	0.0553						
0	2-	- I	-0.0294	+0.0870	-0,0002	0,0002				i
I	1-	- I	+0.0218	-0.0095						
-1	4-	- I	+0.0017	—o. oo69						
0	3-	- I	0.0077	+0.0146	^					
I	2—	- I	+0.0039	o. oo55						
-r	5-	- 1	+0.034	—0. 02 9						

Ar	g=i'g'+ig	C′δ	$\frac{h'}{h_0'}$	$\mathbf{D}'\frac{1}{\mathbf{c}\mathbf{c}}$	u' os i'	$\mathbf{E}'\frac{1}{\mathbf{c}}$	$\frac{u_1'}{\cos i'}$	$\mathbf{H}'_{\mathbf{c}}$	и 08 і
ny +	ig +ig	sin.	cos.	sin.	cos.	sin	cos.	sin.	cos.
н	i' i 4— I	 0. 073	// +o. o63	"	"		И	11	"
ı	3— І	+0. 0362	-0.0313						ľ
0	5— I	+0.004	-o. oo3						
ı	4— I	-0.004	+0.003						
1	,	· ·							:
0	0— 2	+0.02	0.00						
ı	2- 2	0. 159	0, 023						
0	I— 2	+o. 268	+0.076						
' '	0 2	-0. I3	o. o6						
-r	3 2	+0.631	-0. 295						
0	2— 2	—1. 259	+0.573						
I	I— 2	+o. 638	-0. 279						•
_I	4— 2	+0. 1033	+0.1164						
o .	3— 2	—o. 183	-0. 241						
I	2 2	+0.069	+0.135						
-r	5 2	+0.00157	+0.01056	0.00006	+0.00019	+0.00003	+0.00001	-0.00001	+0.00012
0	4— 2	0,0000	-0.0180						
I	3— 2	-o. 0037	+0.0048						
_T	6 2	+0.00095	+0.00130		+o. 00061		-0.00014	, ,	+0.00014
0	5— 2	—0. 0017004		0. 0001555			+0.0002169	0.0000312	
1	4— 2	+0.00080	+0.00049	—u. 00010	- 0. 00019	0.00007	0.00014	o. oooo7	-0.00013
0	6— 2	+0,0006	+0.0018						
X	5— 2	+o. 0015	—o. ooo8o	-0.00004	-0.00002	-0.00002	—0. 0000I	0. 00004	—0, 0 0002
—I	3- 3	+o. 14	-o. o6						1
٥	2 — 3	—о. 28	+0.10			,			
1	I — 3	+o. 13	-o. o7						•
—1	4- 3	o. 236	—o. 351						
٥	3 3	+0.50	+0.70						
X	2 — 3	0. 26	0. 36						
-1	5— 3	O. I24	-0.072						
٥	4 3	+0. 234	+0.128						
I	3— 3		0.048	ì					
1-1		o. o37	+0.010						
0		+o. o68	0.018						
1		-0. 031	+0.012					1	ļ !
-1		+0.0157	0. 0381					ł	
٥		-0.031	+0.076						
I		+0.020	0. 041					{	
1—		+0.0021	0.0022					1	
O		0.0038	+0.0029						
I		+0.0014	0.0000						
О	8 3	-0.0007	+0.0001						
1	7— 3	+0.0002	0.0000						
-ı	5— 4	+0. 17	_0. 19			1			
0		0. 34	+0. 39	1					
1		+0.20	_0. 2I						
						<u> </u>		<u> </u>	

A	rg= $-i'g'+ig$	$\mathrm{C}'\deltarac{h'}{h_0{'}}$		D' c o	$\mathbf{D}' \frac{u'}{\cos i'}$		$\mathbf{E}' rac{u_1{}'}{\cos i'}$		$\mathrm{H'}rac{u}{\cos i}$	
<i>κ</i> γ'- 	-i'g'+ig	sin.	cos.	sin.	cos.	sin.	cos.	sin.	cos.	
ж I	i' i 6 4	// +0.02		"	"	"	"	11	"	
0	5— 4	o. o5	+0.23							
I	4 4	0,00	o. II							
1	7— 4	0.009	-0. 024							
٥	6— 4	+0.018	+0.064							
-I	8— 4		0.003							
0	7— 4		+0.005							
1	6— 4	-o. oo8	-0, 002							
—ı	9— 4	-0,002	+0.001							
0	8— 4	+0.004	-0,002							
_ı	10— 4		+0.00030	0, 00005	+0.0000I					
٥		+0.0005	0.0007							
_I	11-4	0,00000	+0.00006							
٥	10— 4	+0.000013	-0.000131	+0.000003	0.000004			-0.000001	+0.000004	
-1	6 5	+o. 12	+o. o8							
٥	5— 5	0. 26	o. 14							
1	4 5	+0.11	+0.06							
_r	7— 5	+o. o5	0.00							
٥	6— 5	o. 1 4	0,00							
1	5 — 5	+o. o3	0.01							
٥	7— 5	0, 02	+0.01							
I	7— 6	o. oī	+0.04							
	6— 6	+0.03	-0.14							
0	7 — 6	-o. oI	-o. o5			,				

CHAPTER XIV.

CALCULATION OF THE PORTION OF δT' FACTORED BY n't.

In determining the part of $\delta T'$ having the factor n't a degree of precision 200 times greater than that used in deriving the part not multiplied by n't has been employed. In the following table the factor n't has been omitted, and to avoid multiplicity of zeros all the coefficients have been multiplied by 10000:

$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	Ar	g=		$\mathbf{A}'n$	l'δz'	В	'v'	F'	$n\delta z$	G	ľv
1	ну′+	i ⁷ g′⊣	-ig	sin.	cos.	sin.	608.	sin.	cos.	sin.	cos.
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$		-		"		"	i e	11	"	11	"
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	1	1	0	+ 3.47	1	2.39		+ 2.93	+ 3.5127	- 2.9I	- 4. 8233
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	—ı	2	0	+ 87.61	+139.28	+107.14	l	— 13.46	1	+103.02	
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	٥	I	О		3.45	+ 2.17	+ 3.04	_	+ 93.79		128.93
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	1	0	О	+ 83.0235	+132.8585	110. 8643	—177. 1608		i .	+187. 1815	+111.0051
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	—ı	3	0	+ 43.3	+ 18.6	+ 37.0	+ 14.5	+ 6.8			+ 1.4
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	0	2	0	— 14.0	- 5.3	— 16.9	— 7.0	+ o.8	+ 5.5	— 19. I	- 5.0
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	1	I	0	+ 1.13	+ 1.82	- 12.41	— 7.22	— 1.99	— I.58	+ 0.62	+ 0.43
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	-1	4	0	+ 8.8	- 1.4	+ 6.0	- 1.4	+ 1.1	- 1.5	+ 1.8	2.2
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	0	3	0	- 4.4	I.O	— 3.6	+ 0.8	0.9	+ 1.1	- 1. 9	+ o.8
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	1	2	0	— 0. 3	ο. υ	— I.5	— o. 1	— 0. 2	- o. 1	— O. 2	0.0
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	-1	5	0	+ 1.0	— o. 9	+ 0.4	- 0.4	+ o. 1	- 0.3	+ 0.1	— 0.3
$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$	0	4	٥	— o. 5	+ 0.5	- 0.4	+ 0.4	υ, ο	+ 0.3	- O. 2	+ 0.2
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	I	3	0	— o. 1	0,0	- o. ı	+ o. 1				
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$		1—	. т	- 0.2	_ o. 1	0.0	+ 1.o			- 0.1	+ 0.3
$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$	o—	2		- 0.3	+ 0.1	0. 0					
$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$	1—	3—	. 1	,	- 0.9	- o. r	I.9	— o. 1	— o. 1		·
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	_ı	0—	I	— 12.4	— 7. I	— 1.3	+ 6.9	+ 2.4	- 1.4		
$ \begin{array}{ c c c c c c c c c c c c c c c c c c c$	0	1	1	- 6.4	- 2.2	+ 6.7	+ 2.3	I. 9	+ 1.2		
$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$	1	2-	ı	+ 3.7	— I.4	- 6.3	- 9.4	+ 0.1	- o. I		_ 4. I
$ \begin{array}{ c c c c c c c c c c c c c c c c c c c$	—ı	1—	. 1	+ 75.7	+ 26.4	+337.2	+124.8	+ 0.9	+ 0.6	+ 12.8	
$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$	o	0	I	-458.7	168. 2	402.9	—147. 7				
$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$	1	ı —	1	o. 6	— 0.6	+ 44.9	+ 16.2	+ 0.3	+ 0.2	— 13.6	- 14.8
$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$	—ı	2-	1	64. 24	+ 44. 10	+ 70.56	— 16. 26	- 10.25	- 9.42	_	
$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$	0	I —	ı	- 8. 75	32.47	71.87	+ 5.80	+ 36.08	+ 22.05		
$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$	I	o—	ı	+ 6.5	— o. б	+ 8.7	- I.O		- 22.4		,
0 2-1 -348.270 -327.391 +301.613 -290.252 + 24.222 -63.753 + 11.406 - 38.695	—1	3—	1	+ 46.223	41.866	—252. 421	+239.612	<u>- 28. 371</u>	+ 78. 277		
	0	2—	1	—348. 270	<u>—327. 391</u>	+301.613	-290. 252	+ 24. 222	— 63. 75 3	+ 11.406	
	1	<u>ı</u> —	1	+ 0.85	+ 0.63	— 34. o ₃	+ 32.33	- 2.72	l i	- 0.57	+ 1.72

Arg=	A'n	'δz'	В	'ν'	F'	$n\delta z$	G	ŀν
$\kappa \gamma' + i'g' + ig$	sin.	cos.	sin.	cos.	sin.	cos.	sin.	cos.
ж i' i —I 4— I	+ 9.31	+ 64. 27	22. 47	+ 72.12	+ 3.33	+ 24.01	+ 4.84	+ 15.94
0 3— 1	— 37. 649	— 4. 062	+ 28. 187	— 5 9. 11 7	— 2. 69 5	— 21. 1 98	- 4.051	— I3. 379
1 2— 1	+ 5.859	 3⋅747	+ 0.727	— 2. 613	+ 1.095	+ 1.782	+ 0.907	+ 0.408
—ı 5— ı	+ 9.3	+ 17.4	+ 3.5	+ 12.0	+ 2.7	+ 3.6	+ 2.8	+ 2.2
0 4— 1	— 8. 76	— 8. 7 8	— 1.67	— 9.44	— 2.42	— 3· 39	- 2.41	1.93
1 3— 1	+ 1.11	+ 0.50	+ 0.22	— o. 89	+ 0.40	+ 0.13	+ 0.27	- 0.09
— 1 6— 1	+ 3.1	+ 2.1	+ 1.6	+ 1.1	+ o.6	+ 0.4	+ o.6	0.0
o 5 1	- 2.3	- I. 4	— I.2	— o.8	o. 6	- · o. 3	— o. 5	- o. i
I 4— I	+ 0.2	— o. ı			0,0	0.1		
—ı 7— ı	+ 0.5	1.0 +	+ 0.2	0.0	+ 0.7	+ 0.3	+ 0.7	o. r
о 6— 1	— O. 4	0.0	— o. ı	0,0	— o. ı	+ o. I	— o. 1	+ 0.1
I 0 2	_ o. 8	- 0.4	_ 1.7	- 0. I + 2	0. 0	+ 0.2	- o. 3	0.0
0- I- 2 I- 2- 2	1.	0	+ 1	+ 2	ľ		1	
-I I - 2	+ I + 32.0	+ 15.2	+ 9.2	+ 3.6	+ 4.2	— 4.0	+ 2.3	– 5⋅3
0 0-2	- 52.8	— 17.6	1 ' '	_ 12. 8	T 4.*	4.0	T 2.3	_ 3.3
1-1-2	+ 0.2	- 17.0 - 0.1	- 27.7 + 11.1	+ 1.0	- o. ı	— 1.6	+ 3.2	2.4
_1	+ 53.2	1	1	11	— IO. O	+ 11.5	— 69. 5	+ 97.3
0 1-2		<u>-327.9</u> ⊥170.2	— 33.5 — 10.1	+231.6	+111.8	—146. 4	+146. o	—206. 6
	32. 2	+179.2	+ 19.1	152. 4 0. 5	—139. O	+184. I	—124. 9	+177.9
1 0-2	+ z.2	— IO. 2	+ 0.9	+ 79.5	+ 0.9	— 2. 5	— I. 4	+ 19.3
-1 3-2 0 2-2	— 14.6 — 11.5	-141.7	+ 24.9 + 0.4	— 73.6	+ 5.7	- 3.9	+ 6.5	- 21. O
I I - 2	— 4. I	+119.4 - 4.1	— 2.6	+ 9.2	_ I.7	+ 2.6	— 0. 2	+ 1.0
_I 4— 2	—293. 69	—212. 79	—179. 32	_123.93	— 80. o5	_ 10.97	— 44· 37	3.65
0 3-2	+162.6	+122.7	+117.4	+ 77.5	+ 70.4	+ 8.8	+ 38.0	+ 2.5
I 2— 2	- 9· 7	_ 6.o	+ 1.4	+ 0.6	— 12.8	- I.4	— 5.8	_ 0.9
-I 5- 2	— 139. 230	— 16. 103	— 76.712	3. 260	— 28. 507	+ 10.214	— 16. 302	+ 8. 259
0 4— 2	+ 92.09	+ 11.50	+ 56.70	+ 2.86	+ 26.12	9.22	+ 14.49	7. 30
i 3-2	- 5.87	+ 2.05	- 1.02	+ 2.84	- 3.57	+ 2.23	— 1.55	+ 1.44
i 6 2	— 30. 975	+ 13. 247	— 14. 433	+ 8.550	- 4.644	+ 5. 163	- 2. 28I	+ 3.959
0 5-2	+ 22.75472			1 .	+ 4.41582	1	l .	1
1 4-2		+ 1.643	+ 0.222	+ 1.010	- 0. 322	+ 0.839	- 0.018	+ 0.526
1 7— 2	, ,	+ 5.14		+ 2.66	_ 0. 27	+ 1.21	+ 0.04	+ 0.93
0 6-2	+ 3.02	_ 3.96	+ 1.10	2. 18	+ 0.29	1.16	— o. o7	_ o. 86
1 5-2		+ 0.413	+ 0. 157	+ 0.157		+ 0.151	+ 0.067	+ o. o83
	- 0.2	+ 1.0	+ 0.1	+ 0.4	0.0	+ 0.2	+ 0.1	+ 0.1
ŀ	+ 0.1	- 0.7	- 0. I	_ 0.4	0.0	- 0.2	_ o. 1	_ o. I
1 6-2	ľ	+ 0.05	+ 0.03	0,00	+ 0.02	+ 0.02	+ 0.02	0.00
-I I-3	+ 3	+ 2	o	_ I	+ 1	_ r	+ 1	o
0 0-3	1	_ r	2	0				
I- I- 3			+ 1	+ 1				
—1 2— 3	7	11	+ 4	+ 6	— 10	+ 9	— 5	+ 8
o 1— 3		+ 7	0	- 5	+ 28	3 5	+ 16	22
I 0-3			+ 1	+ 1	27	+ 37	- 15	+ 23
_	+285.4	- 19.8		+ 11.6	+ 75.7	+ 35.4	- 47.2	- 20.6
95 4 97					<u> </u>		1	

Arg=		A'n'	'δz'	В	'v'	F'4	$n\delta z$	G	ľv
$\kappa_{\gamma'} + i'g' +$	⊢ig	sin.	cos.	sin.	cos.	sin.	cos.	sin.	cos.
\varkappa i'	i	11	11	,,	"	//	11	"	"
	- 3	189.4	+ 16.4	+137.3	— 10.9	61.5	30. г	+37.4	+15.0
1 1-	- 3	+ 23	— I	17	+ 2	+ 7	+ 3	2	О
-I 4-	- 3	+ 99.2	— 66. і	— 71.7	+ 45.4	+18.4	+ 3.1	-19.7	+ 5.9
0 3-	- 3	- 76.7	+ 52.7	+ 55.5	— 32. 3	-15.9	— I.O	+16.6	— 4.0
I 2-	- 3	+ 7.3	— 8. o	— 5·4	+ 5.7	+ v.6	— о. 1	— I. I	+ 1.1
-r 5-	- 3	+125.9	-292.8	+ 63.2	—151. 2	— 2.3	—66. 5	— 5.8	-32.9
0 4-	- 3	— 84. 2	+197.1	44.8	+110.7	+ 2.7	+60.4	+ 5.4	+29.3
I 3-	- 3	+ 8.9	— 24. I	+ 6.4	13.4	— I. I	—13. 3	— о. б	— 6. т
-ı 6-	- 3	12.5	-145.2	— 1o. 8	— 73. г	—15. 7	—26. 2	10. 7	—13.4
0 5-	- 3	+ 8.6	+106.6	+ 8.3	+ 58.0	+14.5	+24.3	+ 9.6	+12.3
1 4-	- 3	— 3⋅7	— II.6	— 3.0	— 5·7	— 3⋅4	— 4.0	— 2. I	— I.9
—I 7-	- 3	22.61	— 33.69	— I2. 52	- 14.64	<u> </u>	— 4. 20	4. 66	- 1.72
o 6–	- 3	+ 17.40	+ 26.51	+ 10. 24	+ 12.30	+ 6.72	+ 4.06	+ 4.33	+ r. 64
1 5-	- 3	 3.0	_ 2.0	I.7	— 0.6	— 1.3	- o. 3	— o. 8	o. ı
-1 8-	- 3	- 7.819	- 3.890	- 3.738	— I. I42	— 1.726	— o. o51	1.089	+ 0. 230
0 7-	- 3	+ 6.343	+ 3.269	+ 3.190	+ 1.031	+ r.665	+ 0.073	+ 1.028	0. 209
I 6-	- 3	- o. 8o	+ 0.01	— o. 35	+ 0.16	- o. 25	+ 0.08	— o. 13	+ 0. 10
_1 9-	- 3	— I. 59	+ 0.10	— o. 66	+ 0.17	- o. 26	+ 0.14	o. 15	+ 0.15
0 8-	- 3 l	+ 1.351	— o. o65	+ 0.581	— o. 151	+ o. 268	- o. 135	+ 0. 147	— o. 141
1 7-	- 3	— 0. 124	+ 0.089	— o. o18	+ 0.053	0. 028	+ 0.035	— 0.011	+ 0.031
—I IO-	- 3	— 0. z	+ o. i	o. I	0, 0				
0 9-	- 3 l	+ o. 18	— 0. 12	+ 0.06	0.08	+ 0.02	o. o5	0, 00	— o. o3
ı 8–	- 3	0.00	+ 0.02	0.00	+ 0.01				
_I 2-	_ 4	I	o	+ 1	o	- I	+ 1		
	- 4			-	_	+ 3	-4	+ 1	I
	- 4					- 3	+ 4	<u> </u>	+ 1
	- 4	+ 14	I4	- 8	+ 9	+ 6	— 2	— 3	+ 1
1	- 4	_ 10	+ 5	+ 7	- 3	_ <u>5</u>	— I	_ 2	
1 I	- 4	+ 2	I	— I	+ 1	_			
1	- 4	+ 58	+205	 36	-128	-17	+78	+10	44
1	- 4	 45	—149	+ 29	+101	+14	—68	- 9	+39
	- 4	+ 7	+ 24	5	— 18	-3	+12	+ 1	— 5
_r 5—	- 4	+ 74.3	+ 68.3	— 52. 7	57.4	+ 2.4	+23.9	— 9.8	20. O
1	- 4	— 63	— 55	+ 40	+ 47	- 4	-2I	+ 8	+19
	- 4	+ 11	+ 7	_ 8	— 5	+ 1	+ 3	- 2	2
i	- 4	+246.0	+ 49. I	+110.5	+ 19.4	+49.5	— 9.8	+20.5	—10. 6
1	- 4	-182.4	35-4	— 86.6	— 13.9	45.9	+ 9.5	18.7	+ 9.9
1	- 4	+ 29.7	+ 4.6	+ 15.9	+ 3.5	+11.0	— 3. I	+ 4.6	— I. 7
—I 7—	- 4	+126.7	— 37.8	+ 59.4	- 21.3	+20.0	18. o	+ 8.9	—11. I
	- 4	- 99. 2	+ 29. I	— 49. 1	+ 17.6	—19. I	+17.1	8.4	+10.2
1 5-	- 4	+ 13.9	— 6.6	+ 7.2	- 4·3	+ 3.6	4.0	+ 1.6	2. 2
	- 4	+ 29.7	— 29. 7	+ 12.2	15. o	+ 2.8	— 7·9	+ 0.8	- 4.6
0 7	- 4	- 24.4	+ 24. I	— 10.5	+ 12.7	- 2.7	+ 7.6	- o.8	+ 4.4
ı 6—		+ 2.4	- 4.3	+ 0.6	— 2.3	+ 0. 1	— I. 5	- o. I	o. 8
_r 9—	- 4	+ 2.74	- 9.77	+ 0.57	— 4.40	— 0. 33	- 1.98	- 0.44	— 1.13
	- 4	_ 2.3	+ 8.1	— o. 5	+ 3.8	+ 0.3	+ 1.9	+ 0.4	+ 1.2
								•	

Arg=	A'n	'δε'	В,	'v'	F'1	$\imath \delta z$	G	′ν
$n\gamma'+i'g'+ig$	sin.	cos.	sio.	cos.	sin.	cos.	sin.	cos.
κ i' i	11	11	,,	"	"	11	"	11
7— 4	o. I	— т.о	- O. 2	— o. 4	— o. 1	o. 3	— O. 2	o. I
— I IO— 4	— 0. <u>5</u> 02	2.000	— o. 361	— o. 783	o. 251	— o. 311	0. 204	— o. 149
0 9 4	+ 0.40	+ 1.74	+ 0, 31	+ 0.71	+ 0.23	+ 0.31	+ 0, 20	+ 0.16
I 8— 4	o. 15	— o. 17	0.09	- 0.05	 0.06	— 0.03	0.05	0,00
I II 4	- 0. 253	- 0. 259	— 0. 130	0.082	o. o64	- o. o26	0.049	— o. oo6
D 10— 4	+ 0.2240	+ 0. 2395	+ 0.1174	+ 0.0789	+ 0.0639	+ 0.0268	+ 0.0460	+ 0.0048
1 9-4	0. 040	— o. o13	0.019	+ 0.005	- 0.011	+ 0.002	o. oo8	+ 0,002
o 11 4	+ 0.05	+ 0.01	+ 0.01	0, 00	+ 0.02	— o. oı	+ 0.01	o. oı
— I 3 5	0	_ ı	- I	+ 1				
o 2 5	0	+ 1				_		
—I 4— 5	+ 16	+ 11	10	— 6	+ 3	+ 8	— I	- 4
0 3 5	— 9	— 10	+ 6	+ 7	- I	<u> </u>	+ 1	+ 3
I 2— 5	_ 2	0	— 2	— I	+ 1	+ 1		
— I 5— 5	—I34	+ 71	+80	—43	<u>—</u> 64	o	+35	Ö
0 4 5	+102	<u> </u>	66	+36	+58	— I	-3I	0
I 3— 5	— 19	+ 11	+14	_ 8	-13	0	+ 6	0
— I 6— 5	38	+ 69	+39	—52	-23	+ 8	+17	—13
D 5-5	+ 32	— 61	34	+41	+21	— 8	17	+11
1 4- 5	8	+ 14	+ 5	— 9	0	+ 3	+ 2	— 3
—ı 7— 5	+ 3	+184	+ 4	+72	+12	+35	+10	+10
o 6— 5	- 4	-145	— 4	<u>58</u>	12	-32	—10	- 9
I 5— 5	+ 2	+ 28	— I	+13	+ 4	+ 8	+ 2	+ 4
r 8 5	+ 53.4	+ 96.6	+25.9	+42.3	+17.7	+13.4	+10.0	+ 4.8
0 7 5	— 42.6	— 78.8	—22. 4	—36. I	—16.8	-12.9	— 9. 5	— 4·4
1 6-5	+ 9	+ 13	+ 4	+ 6	+ 4	+ 2	+ 3	+ r
—I 9— 5	+ 32.7	+ 21.5	+15.4	+ 8.2	+ 7.8	+ 1.0	+ 4.2	0, 2
o 8— 5	27.5	— 18. 3	—13. 6	- 7.5	— 7.6	- 1.0	4. I	+ 0. 1
1 7- 5	+ 4.9	+ 2.0	+ 2.5	+ 0.7	+ 1.6	- 0.3	+ 0.9	- 0.2
—1 10— 5	+ 10.4	+ 0.8	+ 4.5	— 0. 2	+ 1.9	- 0.8	+ 1.0	— o. 7
5 9-5	9.2	- 0.8	— 4.0	+ 0.2	- 1.8	+ 0.8	- 1.0	+ 0.7
1 8-5	+ 1.2	- 0.2	+ 0.5	— o. 3	+ 0.3	- 0.3	+ 0.2	0. 2
	+ 2.0	— I.O	+ 0.8	- 0.7	+ 0.3	— o. 3	+ 0.1	- 0.3
0 10-5	- 1.8	+ 0.8	0.8	+ 0.6	— o. 3	+ 0.3	— o. i	+ 0.3
I 9-5	+ 0.2	- 0.2	+ 0.1	- 0. 2	+ 0.1	— 0. I	0.01	0.06
—I I2— 5	+ 0.27	- 0.38	+ 0.07	- 0.17	+ 0.01	— 0.09 — 0.08	0.01	0.06
0 11-5	- 0. 24	+ 0.33	— 0.07	+ 0.15	0.01	+ 0.08	+ 0.01	+ 0.06
—I I3— 5	+ 0.007	- 0.080	0.018	- 0.034	— 0.003 — 0.003	— 0.015 — 0.016	— o. oo8	0.010
0 12 5	0.008	+ 0.075 - 0.01	+ 0.004	+ 0.029	+ 0.003	+ 0.016	+ 0.007	+ 0.008
1 11-5	— 0.0I							
-ı 4-6	+ 2	0	— т	+ 1				
0 3-6	— I	I	— I	О	,		1.	
—ı 5— 6	— 6	+ 17	+ 4	10	<u> </u>	+ 5	+ 3	2
o 4— 6	+ 7	- 11	— 5	+ 7	+ 6	— 3	— 2	+ 2
1 3— 6	— 2	+ 4	+ 1	<u> </u>	— I	+ 1		
— I 6— 6	— 6 ₇	— 77	+40	+44	10	45	+ 5	+25
		<u> </u>						<u> </u>

$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	sin. '' +11 - 4	cos.	sin.	cos
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	+11			uvoi .
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	·	+42	"	"
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	- 4		- 5	—2 3
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$		-10	+ 1	+ 5
$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$	—11	19	+13	+13
$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$	+11	+17	12	—12
$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$	- 3	— 3	+ 2	+ 2
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	23	+10	— 3	+ 8
$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$	+22	12	+ 2	— 9
$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$	- 6	+ 4	- 4	+ 2
$ \begin{vmatrix} 1 & 7-6 & -9 & +9 & -5 & +5 \\ -1 & 10-6 & -12.5 & +31.6 & -4.1 & +14.1 \\ 0 & 9-6 & +11 & -27 & +4 & -13 \\ 1 & 8-6 & -1 & +5 & 0 & +3 \\ -1 & 11-6 & +1.2 & +9.8 & +1.0 & +4.1 \\ 0 & 10-6 & -0.9 & -8.8 & -0.9 & -3.6 \end{vmatrix} $	<u>- 8</u>	+15	— I	+ 7
$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$	+ 8	— 15	+ 1	— 7
$ \begin{vmatrix} 0 & 9 - 6 \\ 1 & 8 - 6 \\ -1 & 11 - 6 \\ 0 & 10 - 6 \end{vmatrix} + \begin{vmatrix} 11 & -27 \\ +5 & 0 \\ +1.2 & +9.8 \\ -8.8 & -0.9 \end{vmatrix} + \begin{vmatrix} 4 & -13 \\ +3 \\ +1.0 \\ -3.6 \end{vmatrix} $	- 1	+ 4	0	+ 2
$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$	+ 0.3	+ 6.9 6	+ 0.9	+ 3.4
$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$	- I 0	- 6 + 2	+ I	— 3 o
0 10-6 - 0.9 - 8.8 - 0.9 - 3.6	+ 1.1	+ 2 + 1.6	+ 0.8	+ 0.8
	_ i.i	— 1.6	— o. 8	— 0. 5 — 0. 7
	+ 0.3	+ 0.3	+ 0.2	— 0.7 + 0.2
-1 12-6 + 1.6 + 1.9 + 0.8 + 0.8	+ 0.4	+ 0.2	+ 0.3	+ 0.2 + 0.1
0 II-6 - I.5 - I.7 - 0.7 - 0.7	- 0.4 - 0.4	0.2	— 0.3	— 0. I
1 10-6 + 0.3 + 0.2 + 0.2 + 0.1	+ 0.1	+ 0. 1	_ 0.3	0.1
$\begin{bmatrix} -1 & 13 - 6 \end{bmatrix} + 0.4 \end{bmatrix} + 0.2 \end{bmatrix} + 0.2 \end{bmatrix} = 0.0$	+ 0.2	— o. 1		
0 12-6 - 0.4 - 0.2 - 0.2 0.0	- 0. I	+ 0.1		
$\begin{bmatrix} -1 & 6-7 & -15 & -3 & +9 & +1 \\ 0 & 5 & 7 & +26 & +3 & +3 & +3 \end{bmatrix}$	6	— 4	l	
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	+ 4	+ 5		
$\begin{bmatrix} -1 & 7-7 & +37 & -52 & -21 & +30 \\ 0 & 6-7 & -29 & +44 & +19 & -26 \end{bmatrix}$	+29	—I4	-15	+ 7
	-27 + 7	+14	+14	- 7
$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$	+13	- 3 -12	— 6	-1-10
0 7-7 0 +38 +8 -32	-13	-12 +17	+ 6	+10
1 6-7 + 1 -10 -1 +6	+ 2	⊤ */ 4		9
$\begin{vmatrix} -1 & 9-7 & -38 & -80 & -13 & -21 \end{vmatrix}$	10	— 4 —14	_ 6	0
0 8-7 + 33 + 67 + 11 + 18	+10	+13	+ 6	_ ı
1 7-7 -9 -15 -4 -7	-3	2	, ,	•
$\begin{bmatrix} -1 & 10 - 7 & -51 & -37 & -21 & -14 \end{bmatrix}$	-11	— т	- 7	o
0 9-7 + 43 + 32 + 18 + 12	+11	+ 1	+ 6	o
1 8-7 -9 -6 -5 -2	-	·	,	_
-I II-7 -27 -5 -12 -I	- 5	+ 1	- 3	+ 1
0 10-7 + 24 + 4 + 10 0	+ 5	— I	+ 3	— I
1 9-7 -4 0 -3 0				
$\begin{bmatrix} -1 & 12 - 7 & -8 & +3 & -3 & +2 \\ & & & & & & & & & & & & & & & & & & $	- I	+ 1		
$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$	+ 1	— I		
$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$				
0 12-7 + 1.3 - 1.5				
$\begin{bmatrix} -1 & 7-8 & -1 & -12 & +1 & +7 \\ 0.6 & 8 & 0.0 & +0.0 \end{bmatrix}$				
0 6-8 0 +9				

Arg=	A'n	′δz′	В	'v'	$\mathbf{F}'n$	δz	G	'ν
$ \mu\gamma' + i'g' + ig $	sin.	cos.	sin.	cos.	sin.	cos.	sin.	cos.
π i' i -1 8-8	+37	+14	// 2I	" — 9	+13	+16		9
o 7— 8 1 6— 8	-32 + 8	—12 + 3	+19 - 5	+ 7 - 2	— 14	— 15	+7	+8
o 8— 8	+28 -26	— 6 + 6	—27 +24	— 2 + I	+14 —14	+ 7 7	- 8 +8	—4 +4
7—8 —1 10—8 0 9—8	+ 8 +46 -39	— 1 —35 +33	+10 — 8	—10 + 8	+ 9 9	— 7 + 7	+2	— 4
o 10-8	+ 6 +19 -17	5 42 +36	+ 5 + 6 - 4	4 16 +15	0	- 8 + 8	0	4
1 9— 8 —1 12— 8 0 11— 8	+ 2 - 1 + 1	- 7 -19 +17	+ 1 - 1 + 1	— 4 — 9 + 9	- 2 + 2	- 4 + 4		
1 10— 8 —1 13— 8 o 12— 8	- 1 - 4 + 3	$ \begin{array}{c c} -4 \\ -6 \\ +5 \end{array} $	— 2 + 2	- 3 + 2				
-I 8-9 -I 9-9 0 8-9 -I 10-9 0 9-9 -I 11-9 0 10-9	+ 8 2 + 2 + 9 8 + 30 27	- 3 +23 -21 +16 -15 +23 -21	+ 2 - 2 - 4 + 4 + 5 - 6	-13 +12 -13 +12 + 2 - 2	- 8 + 7 - 3 + 3	-11 +11 -10 +11	+4	— 6
1 9-9 -1 12-9 0 11-9 1 10-9	$\begin{array}{c} +5 \\ +31 \\ -28 \\ +6 \end{array}$	+ 3 + 7 - 6 + 1	+14 —12	+ 3 - 2	+ 5 5	— 2 + 1		
-I 13-9 0 12-9	+14	- 4 + 4	+ 7 — 6	- 3 + 2				
-I 10-10 0 9-10 -I 11-10 0 10-10 -I 12-10 0 I1-10 -I 13-10 0 12-10	+13 -15 +13 -10 +8 +1	+ 2 - 2 + 8 - 8 + 23 - 20 + 18 - 16	+ 8 7 + 1	- 5 + 4 + 3 + 5 8				
-1 12-11 0 11-11 -1 13-11	+ 7	- 9 + 7						

$\begin{array}{c} \text{Arg} = \\ \varkappa \gamma' + i'g' + ig \end{array}$	C′8	$\frac{h'}{h_0'}$	$\mathbf{D}'_{\overline{\mathbf{c}}}$	$\frac{u'}{\cos i'}$	$\mathbf{E'}_{\mathbf{c}}$	$\frac{u_1'}{\cos i'}$	$\mathrm{H}' rac{u}{\cos i}$	
ny +1 y +1y	sin.	cos.	sin.	cos.	sin.	cos.	sin.	cos.
н i' i	"	// + 0.0200	n	" +o. 5438	"	" —0. 5438	"	."
-ı ı o	0.00	- 0.0149	+0.01	— 0. 7200	0. OI	+0.7234	0.00	0. 0005
-I 2 0	+0.04	— o. 17	+0.02	0. 27	+0.11	+0.07	+0.04	0.03
0 1 0	+0.07	+ 0.35	+0.07	+o. 17	0. 14	o. o8	0.01	0,00
1 0 0	—о. 0367	- o. 1728	0. 0931	+0.0882	+0.0826	+0.0011	+0.0191	+0.0678
_1 3 o			—1.2	-0.4	0.4	0. I	о. 6	-0.2
0 2 0	0,0	- 0.2	+0.5	+0.2	+0.2	+0.2	+0.4	+0.2
1 1 0	-0.02	- 0.02	+0.45	+0.17	—о. 33	-0. I2	+0.04	+0.02
—ı 4 o			-0.4	+o. I	-o. I	0.0	-0.2	∔0. I
0 3 0	1		+o. 3	0.0	+o. 1	0. І	+o. I	-o. I
1 2 0			+o. 1	0.0				
-I 5 O			—о. 1	0.0				
_i i i	1		0.0	-0. 2	+0.1	+0.2		
0 2 I	1		-o. I	+o. 1	—о. 1	о. 1	0.0	—o. т
I— 3— I			0.0	+0.3			0.0	+0.1
—ı o— ı	1		-o. 8	-1.4	— 0. 5	0.8	o. 5	o. 8
o— I— I					+0.7	+1.2	+o. 3	+0.5
1— z— 1			+o. 8	+1.4	-o. 5	о. 8	+o. 1	+0.2
—ı ı— ı	+0.2	+ 1.0	0. 3	+o. 1	o. I	o. I		
0 0 1	l	-	0.0	— 0. 2	0.0	+0.2		
I— I— I	+o. 1	+ 0.5	+o. I	0.0	+0. r	+o. 1		
—I 2— I	—1. 98	— 9.41	-0. <u>5</u> 2	+0, 12	+o. 6 5	о. 13	o. o 6	+0.02
o I— I	+3.94	+18.90	o. 68	+0.14	— 0. 97	+o. 19	+0. 64	0. 14
I 0— (2.0	− 9. 5	+1.4	0.4	+o. 7	0. 2	-o. 7	+o. 1
—ı 3— ı	+0.130	- 0.704	+0.138	+0.087	—o. oo6	+o. 115	+0.05 8	0.016
0 2— 1	—0. 319	+ 1.149	—о. 168	+0.027	+0.021	—о. 153	o. 010	+0.018
1 1-1	+0.24	o. 18	+0.05	—o. o8	—o. o6	+0.11	-0.02	0.00
-1 4- I	+0.05	- 0.07	+0. 20	—I. II	+0.03	-O. 2I	+0.08	o. 53
0 3— 1	0. 098	+ 0.118	—0. 125	+0.707	-0, 044	+0.312	-0.054	+0.415
I 2— I	+0.044	0.030	-0. 031	+0.170	+0.032	-0, 216	-0.001	0, 020
-1 5- I			—0. I	-0.4	0.0	—o. 1	-0. I	-0. 2
0 4— 1	10.00	+ 0.02	+0.10	+0.32	+0.04	+0.12	+0.05	+o. 16
I 3— I	0.00	- 0.01	+0.01	+0.05	-0.02	0. 06	-0.01	—o. oı
-I 6- I			-0. I	-0. I +0. I				
_I 0— 2			+0.1	0. I	о. 1	—o. 1	0.0	
-I I-2	0.0	1.0 +	+0.9		-0. 1 -0. 3		0,0	-0.1
0 0-2	-0.4	+ 0.3	+0.4	o. 3	J. 3	+0.3	+0, 2	0. 2
I I 2			-0.4	+0.3	0. 3	+0.3	0.2	+ 0. 2
_I 2— 2	-0.2	— I. I	o. I	-o. 3	+0.1	0.0	_0. I	0.0
0 I— 2	+0.5	+ 2. I	0.0	+0.2	0.0	o. 1	+o. I	0.0
I 0— 2	-o. 3	- I.I	+o. 1	+o. 1	+o. 1	_o. 1	0.0	+0.1
—I 3— 2	—ı. 7	+ 0.6	— 0. 2	0.3	-0.2	-o. 5	+0.1	+0.3
0 2-2	+3.4	— I.3	0.0	—о. 1	+o. 2	+0.7	-0. I	_0. 2
I I— 2	—I. 7	+ 0.7	+0.2	+o.5	0. 2	-o. 5	0.0	+o. 1
								,

Ar	:g=	C'8	$\frac{h'}{h_0'}$	$\mathbf{D}' \frac{\mathbf{C}}{\mathbf{C}}$	$\frac{u'}{\cos i'}$	$\mathbf{E}' \frac{u_1'}{\cos i'}$		$\mathrm{H}'rac{u}{\cos i}$	
μγ+	i'g'+ig	sin.	cos.	sin.	cos.	sin.	cos.	sin.	cos.
ж	i ' i	11	"	"	"	"	11	//	11
t	4— 2	—0. 27	+0.41	o. 16	+0.07	—о. 13	-o. o8	+0.05	+0.09
0	3— 2	+0.5	о. 8	0.0	о. 1	+o. 3	+o. 1	0.0	0.0
1	2 2	-0. 2	+0.4	0, 0	+o. 1				
-1	5 2	+0.001	+0.092	+o.866	-o. o15	+0.111	0.009	+ 0.421	-0, 022
٥	4— 2	0.01	—о. 17	o. 6 5	+0.01	0. 19	+0. or	o. 35	+0.03
1	3— 2	+0.02	+0.07	о. оз	0.00	+0. I2	-0.01	+0.05	O, OI
—I	6 2	+0.008	+0.012	+o. 389	-0.214	+0.052	-0.025	+o. 177	0, 102
0	5 2	-o. o1684	-0.02048	—0. 30202	+0. 16809	0. 07626	+0.04104	-0. 1517 4	+o. 0878 1
1	4- 2	+0.009	+0.006	-0.010	-o. oo8	+0.043	-0.028	+o. oi i	0.012
—ı	7— 2			+0.07	-0.11	+0.01	-0, 01	+0.03	o. o5
0	6— 2			0, 06	+0.07	0, 01	+0.02	—о. оз	+o. o 5
I	5 2	+0.001	0.000	-0.004	0.001	+0.006	-0.012	+0.001	—o. oo5
_1	2— 3			+1	+1				
	1-3			_i	0				
_I	3— 3	0. 0	+0.1	+0.4	-0. I			+o. 1	1 .0
0	2-3	+o. 1	_o. I	-0, 2	+o. I	+o. 1	-o, I	'	
-1	4 3	_o. 7	—I. O	+0.4	0.3	+0.2	0.0	0. 2	+0.2
	3 3	+1.5	+2.0	_o. 3	+0.2	0.4	+0.3	+0, 3	O. 2
1	2— 3	-0.7	_I. o	0. 2	+0. I	+0.2	0, 2	` `	
—ı	5 3	-0.4	—o. 2	—о. 1	-0.3	'		0.0	+o. 1
0	4-3	+o.8	+0.3	+o. 1	+0.2	-0. I	+0. I	0,0	—о. 1
1	3-3	0.4	o. I			İ			
-1	6— 3	0. 1	0.0	+o. 1	+o. 6	0, 0	—о. 1	+o, 1	+0.2
0	5 3	+o. 2	0.0	o. I	-o. 5	O. I	-o. I	0. I	0. 2
1	4 3	о. 1	0.0		1	0.0	+o. 1		
-1	7— 3	0.01	+0.01	+0.24	+o. 26	+0.02	+0.03	+o. 11	+0.12
0	6 3	+0.02	-0.02	0, 20	—о. 23	0.04	-0.05	0. 10	o. 1o
-1	8— 3	o. ooi	+0.003	+0.117	+0.049	+0.011	+0.006	+0.055	+0.018
0	7-3	0.001	0, 005	-0. 100	0. 040	-o. o18	-0.009	0.047	0.015
1	6 3			+o. o1	0, 00	0.00	+0.01	+0.01	0.00
-1	9-3			+0.03	-0.01			+0.01	-0.01
0	8— 3			0.026	+0.003	0, 004	+0.001	-0.012	+0.001
1	7— 3			+0.001	+0.001	+0.002	0.001	+0.002	-0.002
_ı	3— 4			_ı	+1				
0	2— 4	İ		0	I		1		
-1	5- 4	+o. 5	o.6	+0.3	+0.4	+o. 1	+o. 1	— о. 3	0.2
0	4— 4	—ī	+1	0	I	ļ [']			
I	3— 4	+1	I						
-1	6— 4	+o. 1	—o. з	+0.2	0.0			-0.2	_о. т
0	5 4	0.0	+0.7	0.1	0.0	0.0	o. I	+0.2	+o. 1
1	4 4	0, 0	—o. 3						
_I	7 4	0.0	—о. т	-0. 4	+0.3			—o. I	+o. 1
0	6 4	+0.1	+0.2	+0.3	-0.3			+o. I	o. I
1	5 4	0.0	o. I						
		L	<u> </u>	<u> </u>	<u></u>	<u> </u>	<u> </u>	1	

$egin{arg} ext{Arg}= \ arkappa \gamma' + i'g' + ig \end{array}$	$\mathrm{C}'\deltarac{h'}{h_0'}$		$\mathrm{D}' rac{u'}{\cos i'}$		$\mathbf{E}' \frac{{m{u_1}'}}{\cos{m{i}'}}$		$H'\frac{u}{\cos i}$	
$\kappa \gamma' + i'g' + ig$	sin.	cos.	sin.	cos.	sin.	cos.	sin.	cos.
π i' i —I 8— 4 0 7— 4 —I 9— 4 0 8— 4 —I 10— 4 0 9— 4 —I 11— 4 0 10— 4 I 9— 4 0 5— 5 —I 8— 5 0 7— 5 —I 9— 5 0 8— 5 —I 10— 5 0 9— 5	+0.000I -I -0. I -0. I		" -0. I +0. 2 -0. 03 +0. I +0. 009 0. 00 +0. 003 -0. 0046 +0. 003 -0. 2 +0. 2 -0. 2 +0. 2 -0. 1 +0. I	" +0. 2 -0. 2 +0. 10 -0. 1 +0. 026 -0. 02 +0. 003 -0. 0045 +0. 001 -0. 1 +0. 1 0. 0 0. 0 0. 0	+0.001 -0.0006	+0.001 -0.0005	" -0. I +0. I 0. 00 +0. 004 -0. 01 +0. 002 -0. 0021 +0. 001	" +0. I -0. I +0. 05 +0. 012 -0. 01 +0. 002 -0. 0019 -0. 001

CHAPTER XV.

SECOND-ORDER PERTURBATIONS OF THE MEAN ANOMALY AND RADIUS-VECTOR OF SATURN, ARISING FROM THE MUTUAL ACTION OF THIS PLANET AND JUPITER.

When the eight terms of $\delta T'$, given in the two preceding chapters, are added the following expression is obtained:

	δτ΄	
$Arg = \varkappa \gamma' + i'g' + ig$	sin.	cos.
μ i' i ο ο ο	// // // // // // // // // // // // //	+0.0000741+ 4.6131 <i>n't</i> -0.145312 + 16.6354 <i>n't</i>
-1 2 0 0 1 0	+0.330 +284.440n't -1.1711 - 59.600n't	+0. 167 +366. 21n't -0. 3461 - 35. 11n't
1 0 0 —1 3 0	+1.771981 - 39.0494n't +0.217 + 101.7n't	$\begin{array}{cccc} -1.345783 & -50.7489n't \\ -0.200 & +32.0n't \end{array}$
0 2 0	$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	+3.626 — 11.4 $n't$ — 5.717 — 6.50 $n't$
-I 4 0 0 3 0 I 2 0	+0.023 + 17.0n't +0.258 - 10.3n't -0.232 - 2.1n't	$ \begin{array}{cccccccccccccccccccccccccccccccccccc$
1 5 0 0 4 0 1 3 0	-0.97 + 1.5n't +2.15 - 1.1n't -1.013 - 0.2n't	+0.18 $-1.9n't-0.42$ $+1.4n't+0.414$ $+0.1n't$
0— 4— I —I— 2— I	0. 22 0. 36	-0. 05 -0. 28
o 3 1 1 1	+0.10 +7.219 — 0.2n't	+0. 22 -1. 638 + 1. 2n't
0 2 I I 3 I I 0 I	$ \begin{array}{rcl} -5.13 & -0.6n't \\ +0.75 & +0.5n't \\ +4.705 & -17.4n't \end{array} $	$ \begin{array}{cccccccccccccccccccccccccccccccccccc$
0— I— I I— 2— I	$\begin{array}{rrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrr$	+2.819 + 2.4n't -0.355 - 14.2n't
0 0— I —I I— I	+2. 456 +426. 4n't -1. 786 -861. 9n't	$\begin{array}{cccc} -2.734 & +167. \text{ on}'t \\ +2.216 & -317. \text{ In}'t \end{array}$
I— I— I —I 2— I	+0.263 + 31.3n't +0.4999 + 6.72n't	-0.500 + 1.6n/t +0.0123 + 14.49n/t
0 I— I 1 0— I —I 3— I	-0.026 $-64.75n't-0.396$ $-3.6n't+0.4650$ $-249.915n't$	+1.866 — 3.68n't -2.371 — 16.7n't +0.1670 +324.289n't
0 2— I I I— I	-0.5363 - 11.505n't +1.5274 - 36.26n't	-0.7127 - 64.268n't $+1.0156 + 41.42n't$

$Arg = \varkappa \gamma' + i'g' + ig$	$\delta { m T}'$	
	sin.	cos.
μ i' i -1 4- I	,, ,, ,, ,, ,, ,, ,, ,, ,, ,, ,, ,, ,,	,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,
0 3— 1	+ 0.3459 - 16.529n't	-0.7243 - 96.204n't
I 2— I	+ 2.7944 + 8.632n't	+1.5498 — 4.266n't
-1 5- I	-5.313 + 18.1n't	+0.928 + 34.5n't
0 4— 1	+14.669 - 15.08n't	-2.763 $-22.92n't$
I 3— I	-2.2885 + 1.98n't	+0.3606 — 1.38n't
—ı 6— ı	-0.040 + 5.8n't	-0.029 + 3.5n't
0 5 1	0.016 4.6n't	+0.014 - 2.5n't
1 4-1	+ 0.452 + 0.2n't	-0. 173 - 0. 2n't
-1 7- 1	-0.004 + 2.1n't	-0.021 + 0.3n't
о 6— г	- 0.7 $n't$	+ 0. 2n't
— I—· I—· 2	+ o. 31	
0— 2— 2	+ 0.31 - 0.28	0. 54 +0. 28
I- 3- 2	+ 0.03	+0.20 -0.02
-1 0-2	+ 2.43 - 2.8n't	+5.09 — $0.6n't$
0— I— 2	- 1.95 0.0n't	-3.95 + 2n't
I— 2— 2	+ 0.35 + 1n't	+0.76 on't
-I I-2	+ 4.14 + 48.5n't	+3.09 + 8.8n't
0 0-2	-3.35 $-80.5n't$	-2.49 $-30.4n't$
I— I— 2	+ 0.59 + 13.5n't	+0.37 — 2.3n't
—I 2— 2	+ 2.888 — 60. In't	+1.510 + 11.1n't
0 I— 2	-2.172 +245.3n't	—1. 067 —324. 0 <i>n't</i>
I 0- 2	+ 0.27 -260.9n't	-0.01 +350.3n't
-1 3-2	-0.043 + 7.8n't	+0.663 - 45.3n't
0 2- 2	0.994 4.6n't	-0.006 + 20.0n't
I I— 2	+ 1.335 - 10.3n't	-0.558 + 9.5n't
—I 4— 2	— 0. 2422 —597. 94 <i>n't</i>	-0. 4767 -350. 85n't
0 3— 2	+ 0.713 +389.2n't	+2.313 +210.7n't
I 2 2	- 0.441 $-$ 27. $1n't$	o. 350 7. 2n't
—I 5— 2	+ 0.21223 -259.352n't	-0. 1034 7 - 0. 844 <i>n't</i>
0 4— 2	+ 0.1153 +188.20n't	-0. 3569 - 2. 28n't
I 3— 2	- 0. 4886 $-$ 11. 85 $n't$	+3.0246 + 8.61n't
—I 6— 2	+ 1.46667 - 51.707n't	+3.25760 + 30.590n't
O 5— 2	- 0.0460094+ 40.27460 <i>n't</i>	+0.0201528— 24.10504n't
I 4— 2	+ 1.24452 - 1.015n't	+2.89090 + 3.976n't
—I 7— 2	+ 0.853 - 5.25n't	+0.482 + 9.77n't
o 6— 2	-0.2822 + 4.24n't	-0. 1456 - 8. 02n't
I 5— 2	+ 0.00396 + 0.318n't	+0.00202 + 0.786n't
—I 8— 2	+ 0.178 0.0 <i>n't</i>	-0.010 + 1.7n't
0 7— 2	- 0.095 - 0.1n't	+0.007 — I.4n't
1 6— 2	+ 0.006 + 0.12n't	-0.002 + 0.07n't
—I 9— 2	+ 0.022	o. o15
o 8— 2	— 0. 0I4	+0.009
—ı o— 3	+ 0.60	+0.22
o— I— 3	- o. 38	—o. 25
I— 2— 3	+ 0.04	+0.03

	δι''		
$Arg = n\gamma' + i'g' + ig$	sin.	cos.	
и i' i —1 1— 3		,,, ,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,	
o o— 3	+ 2.53 - 6n't	-2.07 — $In't$	
1-1-3	-0.56 + 1n't	+0.44 + In't	
-1 z-3	-1.62 - 17n't	+3.70 + 13n't	
o 1— 3	+ 1.37 + 43n't	-3.11 - 55n't	
I 0-3	- 0. 23 - 41n't	+0.60 + 61n't	
_r 3— 3	-0.54 + 130.8n't	+2.85 + 6.5n't	
0 2—3	+ 0.25 - 76.2n't	-2.26 - 9.7n't	
I I— 3	+ 0.16 + 11n't	+0.27 + 4n't	
—I 4— 3	-1.406 + 25.9n't	—1. 289 — 12. 8n't	
0 3-3	+ 2.26 - 19.4n't	+2.84 + 17.7n't	
I 2— 3	-1.44 + 0.7n't	-2.09 - 2.4n't	
—I 5— 3	- 1.488 +180.5n't	+0. 191 -543. 8n't	
0 4-3	+ 0.760 —120.1n't	-0.070 +398.0n't	
I 3 3	+ 0.397 + 13.2n't	+0.200 - 57.0n't	
—ı 6— 3	+ 1.425 — 49.6n't	+0.454 -257.2n't	
o 5— 3	-4.482 + 40.9n't	+0.096 +200.4n't	
I 4-3	+ 0.274 - 12.3n't	—0. 039 → 23. I <i>n't</i>	
-r 7-3	+ 1.4673-46.54n't	o. 7986 53. 83n't	
o 6 3	-11.896 + 38.37n't	+7.967 + 44.11n't	
ı 5— 3	+ 4. 286 $-$ 6. 8n't	-2.956 - 3.0n't	
r 8 3	0.0273- 14.190 <i>n't</i>	+1.6244- 4.777n't	
o 7— 3	— 0.8052+ 12.060n't	-0.3825+4.095n't	
r 6 3	+ 0. 1834 1. 51n't	-0. 0722+ 0. 36n't	
—1 9— 3	+ 0. 1600— 2. 62n't	+0.4221+0.54n't	
o 8— 3	— 0. 1654+ 2. 305n't	—0. 2461— 0. 487 <i>n't</i>	
ı 7— 3	+ 0.0271- 0.176n't	-0.0011+0.206n't	
—I IO— 3	+ 0.054 - 0.3n't	+0.049 + 0.1n't	
o 9— 3	-0.037 + 0.26n't	-0.020 - 0.28n't	
ı 8 3	+ 0.024 0.00n't	-0.050 + 0.03n't	
0 10—3	o. oo8	0.002	
I 4	— o. 10	+o. 56	
0 0—4	+ 0.14	—o. 41	
—I 2— 4	-2.10 - 1n't	-1.61 + 1n't	
0 I—4	+ 1.85 + 4n't	+1.38 - 5n't	
I 0— 4	-0.43 - 4n't	-0.35 + 5n't	
r 3 4	-2.91 + 8n't	—0.60 — 5 <i>n't</i>	
0 2-4	+ 2.53 - 10n't	+0.45 on't	
1 I— 4	-0.51 + 1n't	—o. 10 on't	
—I 4— 4	-2.38 + 15n't	-0.02 + 111n't	
D 3 4	+ 2.08 — IIn	+0.17 - 77n't	
I 2— 4	— 0.42 on't	-0.20 + 13n't	
— 1 5— 4	+ 0.05 + 14.8n't	-0.57 + 14.5n't	
0 4—4	- 0.37 - 20n't	+0.78 — 10n't	
1 3-4	+ 0.44 + 3n't	-0.34 + 2n't	
— I 6— 4	-0.28 +426.6n't	-1.28 + 47.7n't	
	·	·	

	δ T ′		
$Arg = \varkappa \gamma' + i'g' + ig$	sin.	cos.	
н l'i	,, ,,	" "	
0 5— 4	-0.22 $-333.5n't$	+1.24 - 29.0n't	
I 4— 4	+0.07 + 61.2n't	-0.43 + 3.0n't	
—I 7— 4	+0.448 +214.5n't	-0.968 - 87.9n't	
0 6— 4	-1.713 -175.3n't	+0.387 + 73.8n't	
I 5— 4	+1.18 + 26.3n't	+0.79 — 17.2n't	
—ı 8— 4	-6.910 + 45.3n't	-6.607 - 56.9n't	
0 7— 4	+4.714 - 38.1n't	+4.027 + 48.5n';	
1 6-4	-0.287 + 3.0n't	—0. 271 — 8. 9 <i>n't</i>	
—I 9— 4	-3.379 + 2.51n't	-0.844 - 17.13n't	
0 8 4	+2.326 - 2.0n't	+0.605 + 14.9n't	
I 7— 4	-0. 170 - 0. 6n't	+0.032 — I.8n't	
—1 IO— 4	-0.76701 - 1.304n't	+0. 22652 — 3. 204n't	
0 9—4	+0.5835 + 1.13n't	-0.1641 + 2.89n't	
1 8— 4	-0.035 - $0.35n't$	+0.041 — 0.25n't	
-I II- 4	-0. 10300 - 0. 491 <i>n't</i>	+0.11172 — 0.368n't	
0 10— 4	+0.080846+ 0.4441n't	-0.085242+ 0.3430n't	
9-4	-0.00264 - 0.074n't	+0.01303 — 0.004n't	
0 11—4	+0.0043 + 0.09n't	—0.0189 — 0.01 <i>n't</i>	
—1 2— 5	—o. 46	0.00	
0 I— 5	+0. 37	+0.06	
—I 3— 5	+0.72 - In't	—1.59 on't	
0 2-5	_0.60	+1.42 + 1n't	
1 1-5	+o. 15	0. 34	
—I 4— 5	-0.08 + 8n't	-2.07 + 9n't	
□ 3— 5	+0.06 — 3n't	+1.79 - 6n't	
1 2-5	-0.03 - 3n't	—0. 36 on't	
—ı 5— 5	-0.41 - 83n't	-1.58 + 28n't	
0 4 5	+0.32 + 63n't	+1.31 - 22n't	
I 3 5	-0.06 - 12n't	-0.19 + 3n't	
—ı 6— 5	+0.18 - 5n't	-0.26 + 12n't	
o 5— 5	-0.26 + 1n't	+0.15 - 17n't	
I 4— 5	+0.13 — 1n't	+0.04 + 5n't	
—I 7— 5	+0.82 + 29n't	-0.53 +301n't	
o 6 5	-1.04 - 30n't	+o. 36 —244n't	
I 5 5	+0.28 + 7n't	+0.07 + 53n't	
—ı 8— 5	+0.39 +106.7n't	-0.79 + 157.0nt	
o 7-5	-0.31 - 91.2n't	+0.66 —132.0 <i>n't</i>	
1 6— 5	+0.06 + 20n't	-0.08 + 22nt	
—I 9— 5	+4.335 + 59.9n't	-7.244 + 30.5nt	
0 8 5	-3.03 - 52.6n't	+5.14 - 26.7n't	
1 7— 5	+0.40 + 9.9n't	-0.70 + 2.2n't	
—1 10— 5	+0.183 + 17.7n't -0.150 - 15.9n't	-3.731 - 0.9n't	
ō 9— 5	-0.150 - 15.9n't -0.060 + 2.2n't	+2.865 + 0.9n't	
1 8— 5		-0.348 - I. on't	
—I II— 5	-0.451 + 3.2n't +0.345 - 3n't	-0.890 2.3n't	
n 10— 5	+0. 345 — 3n't	+0.707 + 2n't	

	δ	\mathbf{T}'
$Arg = \varkappa \gamma' + i'g' + ig$	sin.	cos.
n i' i	u u	" "
I 9— 5	-0.068 + 0.4n't	—0. 062 — 0. 5n't
—I 12— 5	-0.1725+0.34n't	-0.1117- 0.70n't
0 11- 5	+0.127 - 0.31n't	+0.087 + 0.62n't
I 10— 5	—о. 013	+0.001
—I I3— 5	-0.039I- 0.022n't	-0.0007 0.139n't
0 12 5	+0.0320+ 0.022n't	+0.0008+ 0.128n't
1 11-5	o. 0030 o. 01 <i>n't</i>	+0.0017— 0.01 <i>n't</i>
—1 3— 6	0.09	—o. 35
o 2— 6	0.0	+0.2
—r 4— 6	+1.10 + 1n't	+0.24 + 1n't
o 3— 6	-1.00 - 2n't	-0. 19 - 1n't
I 2-6	+0.17	+0.04
—1 5— 6	+1.37 - 5n't	-0.32 + 10n't
o 4— 6	-1.23 + 6n't	+0.30 - 5n't
1 3— 6	+0.16 - 2n't	-0.04 + 3n't
i 6 6	+0.98 - 32n't	-0.52 - 53n't
0 5—6	-0.86 + 29n't	+0.48 + 41n't
ı 4—6	+0.06 — 6n't	_0.06 _ 9n't
—ı 7— 6	+0.24 - 7n't	0.08 on't
o 6— 6	-0.16 + 11n't	-0.09 In't
1 5 6	— 3n't	+ 3n't
—r 8— 6	+0.54 —195n't	+0.41 + 59n't
o 7— 6	-0.47 + 163n't	−0.49 − 58n't
ı 6— 6	+0.07 - 42n't	+0.04 + 14n't
—ı 9— 6	+0.60 - 99n't	-0.12 + 104n't
8 — 6	-0.58 + 87n't	+0.05 — 93n't
1 7— 6	+0.11 - 15n't	+0.02 + 20n't
—ı 10— 6	+6.15 - 15.4n't	+2.05 + 56.0n't
u 9—6	-4.78 + 13n't	-1.55 - 49n't
ı 8— 6	+0.86 on't	+0.28 + 10n't
—I II— 6	+3.38 + 4.1n't	-0.52 + 16.3n't
o 10— 6	-2.73 - 3.7n't	+0.41 — 14.7n't
1 9 6	+0.42 + I.4n't	-0.14 + 2.4n't
—I I2— 6	+0.829 + 3.1n't	-0.646 + 3.0n't
o 11— 6	-0.702 - 2.9n't	+0.528 - 2.7n't
1 10— 6	+0.06 + 0.6n't	-0.09 + 0.4n't
—I I3— 6	+0.089 + 0.8n't	-0.233 + 0.1n't
o 12— 6	-0.086 - 0.7n't	+0.196 — 0.1 <i>n't</i>
1 11— 6	-0.001	0. 029
—ı 4— 7	+0.2	o. 1
o 37	o. I	+0. r
ı 5— 7	0.0	+0.7
0 4— 7	0.0	—o. 7
<u> </u>	+0.37 - 12n't	+0.77 - 6n't
□ 5— 7	-0.34 + 9n't	-0.69 + 7n't
		<u> </u>

	$\delta \mathbf{T}'$	
$Arg = \varkappa \gamma' + i'g' + ig$	sin.	ens.
ν i' i	// // // // // // // // // // // // //	11 11
-1 7-7	+0.45+30n't	+0.46— 29n't
0 6— 7	-0.40-23n't + 10n't	-0.40 + 25n't - $7n't$
1 5— 7 —1 8— 7	+0.13-2n't	+0.11-6n't
3 7 0 7 7	-0.12 + 1n't	-0.15 + 14n't
ı 6— 7	+2n't	-8n't
i 9 7		+0.43-115n't
0 8-7	+0.14+60n't	-0.35 + 97n't
1 7-7	-0.02-16n't	+0.07 - 24n't
_r ro— 7	+0.32-90n't	+0. 33— 52n't
0 9-7	-0.24+78n't	-0.37 + 45n't
8— 7	+0.05-14n't	+0.05-8n't
i ii 7	-0.45-47n't	+4.62-4n't
0 10-7	+0.34+42n't	-3.78+2n't
1 9-7	0.09 7n't	+0.75 $on't$
_1 12- 7	+1.07-12n't	+2.68+6n't
0 11-7	-0.87+11n't	-2.28-6n't
1 10-7	+0.20— In't	+0.37+ 1n't
-i i3-7	+0.74- 2.0n't	+0.65+ 2.3n't
0 12-7	-0.67 + 1.3n't	_0.58_ 1.5n't
1 11-7	+0.12	- -o. o8
	,	•
—ı 6— 8	-0.3	+0. I
o 5 8	+0.3	—0. I
—ı 7— 8	-0.4 on't	+0.3 - 5n't
o 6— 8	+0.3 on't	-0.3 + 9n't
—ı 8— 8	—o. 13+23n't	+0.30+ I2n't
0 7-8	+o. I —20n't	-0.2 - 12n't
ı 6— 8	+3n't	+ In't
_1 9— 8	-0.06+ 7n't	+0.02 - 5n't -0.03 + 4n't
o 8— 8	—0. 0I — 8n't	-0.03 + 4nt $- In't$
1 7-8	+8n't	-1nt $+0.04-56n't$
—I 10— 8	-0. 20+67n't +0. 18-56n't	+0.04 - 50nt -0.05 + 48n't
□ 9— 8 ■ 8— 8	$+0.18-50n^{2}t + 11n^{2}t$	-0.05 + 40nt -9n't
1 8—8 —1 11—8	-0.07+25n't	+0.37— 70n't
D 10-8	+0.19-21n't	-0.36 + 59nt
1 9-8	-0.01 + 3n't	+0.04— 11n't
1 <u>9</u> 8	$\frac{-3.14-4n't}{}$	+0.42- 32n't
o 11—8	+2.62+4n't	-0.38 + 30n't
1 10— 8	_0.61 in't	+0.07-4n't
_r 13— 8	1.86 6n't	+1.22 9n't
0 12—8	+1.57+5n't	-I.00+ 7n't
1 11—8	0.30	+0.21
	—о. 1	—0. 2
—ı 7— 9 —ı 8— 9	-0.1 -0.2 + 8n't	-0.2 $-0.2 - 3n't$
0 7-9	+0.2	+0.2
- / /		

	δ	T'
$Arg = \varkappa \gamma' + i'g' + ig$	sin.	cos.
n i' i	<i>II</i>	" "
—ī 9 — 9	-4n't	+15n't
o 8— 9	+7n't	—19n't
—I 10— 9	+ 2n't	+14n't
0 9—9	- In't	—14n't
—I II— 9	-o. 10+35n't	-0.11 + 25n't
o 1 0— 9 _.	+0.02-33n't	+0. 11—23n't
1 9 9	+ 5n't	+ 3n't
—I I2 — 9	-0.34+50n't	-0.02+ 8n't
0 11—9	+0.33-45n't	+0.07— 7n't
I 10 9	+6n't	+ In't
—1 13— 9	0.75+21n't	—1.95— 7n't
0 12—9	+0.59—19n't	+1.67+6n't
1 II— 9	o. I3	—о. 36
I IOIO	—14n't	+ 2n't
o 9—10	+13n't	2n't
—1 11—10	-7n't	+ 3n't
0 1010	+6n't	- 4n't
—I 12—IO	-9n't	+26n't
0 11—10	+8n't	20n't
—1 13—10	-0.19+ 1n't	-0.21 + 23n't
0 12—10	+0.1 - 2n't	+0.224n't
I I2II	— 8n't	— 9n't
0 1111	+7n't	+7n't
1 1311	-8n't	on't

In deriving $\delta W_0'$ from $\delta T'$ it has been deemed advantageous to equate the motion of the arguments in the terms involving 5g'-2g and 10g'-4g. The formulæ for this have already been given (p. 275). In the two terms we treat by this process there has been found:

Arg.	log A	K	log B	log u	$\log \mu$
5g'—2g 10g'—4g	o. 4798525 9. 0047121	0 / " 68 0 23.25 313 9 56.7	6. 8614088 <i>n</i> 4. 7292	7. 1863943 <i>n</i> 6. 7424	1. 4973782 1. 1722875

By the aid of these quantities the terms of $\delta W_{0}{'}$ in question have been found as follows:

Arg.	$\delta \mathrm{W_o}'$	
	cos.	sin.
5g'—2g 10g'—4g	,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,	.,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,

The expressions for $\overline{\delta W_0}'$ and $-\frac{1}{2} \left(\frac{\overline{d \cdot \delta W_0}'}{d \gamma'} \right)$ follow:

	$\overline{\delta \mathrm{W_0}'}$		
Arg=i'g'+ig	cos.	sin.	
i' i		" "	
I O	$+ k_0 + 2.3065n'^2t^2 + 0.9868 - 13541.60n't$	— 0. 2596 +17867. 41 <i>n't</i>	
ł	$+ k_1 - 25.3745n'^2t^2$	$+ k_2 - 19.5247n'^2t^2$	
2 0	-2.2418 - 374.62n't	-3.9742 + 494.75n't	
]	$+[8.4472]k_1$ — 0.7106 $n^{2}t^2$	$+[8.4473]k_2-$ 0.5469 $n'^{2}t^{2}$	
3 0	- 0.0621 - 15.26n't	-2.8029 + 20.16n't	
	+[7.0705] k_1 — 0.0298 n'^2t^2	$+[7.0707]k_2$ — 0.0230 $n^{2}t^2$	
4 0	0.0064 0.71n't	-0.0583 + 1.05n't	
	$+[5.77]k_1$ — 0.0015 n'^2t^2	$+[5.77]k_2$ — 0.0011 n'^2t^2	
4— I	— o. o336	+ 0.0102	
—3— I	-0.0018 + 0.01n't	+ 0.0376 — 0.02n't	
—2— I	+ 1.1202 + 0.06n't	+ 0.2798 0.07n't	
—ı— ı	+ 1.0070 + 1.32n't	+ 0.9110 - 0.81n't	
0— 1	+ 1.0456 — 49.69n't	+ 1. 1018 + 14. 64n't	
ı 1	+ 0.8434 - 17.39n't	- 0. 3182 $-$ 3. 18 $n't$	
2— І	-0.8913 + 435.49n't	+ 1.0414 + 736.12n't	
3— 1	+ 4.9768 + 52.02n't	- 4.5791 - 62.76n't	
4— I	2.9691 0.66 <i>n't</i>	— 0.8452 — 3.82n't	
5— I	— 0. 1495 — 0. 04 <i>n't</i>	— 0. 1011 — 0. 18n't	
6— ı	- 0.0022 - 0.26 $n't$	— 0.0070 + 0.13 <i>n</i> / <i>t</i>	
-3- 2	+ 0.002 $0.00n't$	+ 0.002 0.00n't	
-2- 2	+ 0.0305 - 0.01n't	+ 0.0232 $0.00n't$	
—I— 2	+ 0. 2429 $-$ 0. 10 $n't$	- 0. 4942 + 0. 06 $n't$	
0— 2	+ 0. 4969 $-$ 2. 29 $n't$	- 0. 3576 + 4. 22 $n't$	
I— 2	+ 0.4814 - 11.03n't	- 0. 2504 + 8. 50n't	
2— 2	- 0.0352 $-$ 6.72 $n't$	-0.2132 + 22.06n't	
3— 2	0. 2412 212. 09n't	-1.3520 + 257.39n't	
4— 2	-6.6128 + 7966.41n't	-27.4774 - 26.42n't	
5— 2	- 1.07047 - 1212.911n't	+ 4.50831 - 742.402n't	
6— 2	0. 1609 11. 09 <i>n't</i>	+ 0.0999 + 20.41n't	
7— 2	— 0. 0179 — 0. 34 <i>n't</i>	-0.0028 + 0.60n't	
8— 2	- 0.0011 $-$ 0.04 $n't$	-0.0009 + 0.05n't	
-2- 3	+ 0.001	— o. oo1	
—ı— 3	+ 0.027	— o. o15	
o 3	- 0. 2158 + 0. 03 $n't$	— 0. 1786 — 0. 06n't	
1— 3	- 0. 1215 $-$ 1. 12 $n't$	— 0. 2962 — 2. 08n't	
2— 3	- 0.0638 + 17.27 $n't$	— 0. 2591 — 0. 17n't	
3— 3	- 0. 1792 + 5. 33 $n't$	+ 0.1154 + 6.58n't	
4— 3	- 0. 2802 + 40. 74 $n't$	- 0.0963 + 124.48n't	
5— 3	-0.6832 $-23.88n't$	— 0. 2908 + 105. 96n't	
6 3	-3.2151 $-79.14n't$	-2.4514 + 90.41n't	

,,,,	δ	$\widetilde{\mathbf{W_0}'}$
Arg=i'g'+ig	cos.	sin.
i' i	u n	11 11
7— 3	-1.5666 + 51.53n't	+3.8956 - 17.98n't
8 3	+ 0. 2626 — 2. 92n't	-0. 1688 - 1. 01n't
9- 3	— 0.0390 — 0.06n't	0. 0843 0. 10n't
10 3	十 0.0020	0. 0033
— I— 4	0.000	o. 002
0— 4	— o. oo4	—o. 016
I— 4	- 0. 113 $-$ 0. 1 $n't$	+0.086 0.0n't
2 4	- 0. 1704 $+$ 0. 10 $n't$	+0.0423 + 0.19n't
3 4	-0.1553 + 1.15n't	+0.0081 9.33n't
4 4	+ 0.0080 + 3.20n't	+0.0435 — 1.88n't
5— 4	0. 1018 +53. $25n't$	+0. 1627 5. 89n't
6— 4	- 0. 1474 $+$ 34. $85n't$	+0.1720 +15.52n't
7— 4	-2.3082 + 11.45n't	+2.1392 + 15.71n't
8— 4	-2.1577 + 2.04n't	+0.6759 + 9.96n't
9 4	+12.0354 +20.58n't	+3.5243 -51.00n't
10 4	— 1.11130— 6.224n't	-I. 17797+ 4. 770n't
11 4	-0.0041 - 0.08n't	-0.0181 - 0.01n't
1— 5	— 0.010	0.000
2- 5	+ 0.031 0.0n't	+0.070 — 0.1n't
3- 5	- 0.008 0.0n't	+0.098 — 0.5n't
4 5	-0.022 - 5.0n't	+0.079 — 1.6n't
5— 5	+ 0.0127 - 0.63n't	+0.0195 - 1.74n't
6 5	+ 0.0319 + 2.32n't	+0.039725.72n't
7— 5	+ 0.0774 + 10.97n't	+o. 1305 —15. 06n't
8 5	+ 0.6569 + 7.75n't	+1. 1297 — 3. 39n't
9— 5	+ 0.0109 + 3.28n't - 0.2064 + 1.17n't	+0.8058 + 0.37n't
10 5		+0.3637 + 0.99n't
11-5	-0.3286 + 0.60n't + 0.1417 + 0.08n't	+0.2073 + 1.23n't -0.0043 - 0.47n't
12 5	,	
2— 6	o. oo4	+0.013
3 6	+ 0.034 - 0.2n't	-0.008 + 0.1n't
4 6	+ 0.041 - 0.3n't	+0.009 - 0.5n't
5— 6	+ 0.028 - 1.2n't	+0.015 + 2.7n't +0.018 - 0.4n't
6— 6 7— 6	+ 0.014 - 0.2n't + 0.0311 - 12.81n't	$+0.018 - 0.4n^{2}$ $-0.0020 - 3.29n^{2}t$
7— 0 8— 6	+ 0.0311 - 12.81nt + 0.0681 - 6.29n't	-0.0020 - 3.29nt -0.0011 - 7.04n't
9— 6	+ 0.5948 - 0.96n't	-0.1924 - 4.76n't
10— 6	+ 0.3945 - 0.96nt + 0.3925 + 0.56n't	+0.0785 — 1.66n/t
11 6	+ 0. 1216 $+$ 0. 47 $n't$	+0. 1097 — 0. 43n't
12 6	+ 0.0172 + 0.17n't	+0.0630 - 0.02n't
	+ o. oo8	-0, 002
3-7	+ 0.001	0.002 0.008
4— 7 5— 7	+ 0.001 + 0.006 - 0.3n't	- 0.013 0.0n't
6 7	+ 0.000 - 0.3nt + 0.008 + 1.7n't	-0.003 $0.0nt$ $-0.009 + 1.2n't$
7— 7	$+ 0.001 - 0.1n^{t}$	+0.001 + 0.4n't
, - ,	0.70	1 3.4

	δν	$\overline{{ m V_0}'}$
Arg=i'g'+ig	cos.	sin.
$oldsymbol{i}'$ $oldsymbol{i}$	n n	// //
8 7	-0.011-3.4n't	-0.022+5.9n ^t
9— 7	+0.017-4.6n't	-0.026+2.5n't
10— 7	0.0292.7n't	-0. 315+0. 3n't
11 7	+0.095—0.7 <i>n't</i>	-0. 198-0. 4n't
12— 7	+0.065-0.3n't	o. 053o. 2n't
5— 8	0.003	—o. oo1
6 8	—o. 009+o. 1 <i>n′t</i>	—0. 002—∪. 2n′t
7— 8	-o. 003+0. 5n't	0.0100.2n't
8— 8	-0.007+0.7n't	+0.001+0.5n't
9 8	-0.003+2.6n't	0.000+2.3n't
10— 8	-0.001+1.0n't	-0.011+3.0n't
11— 8	0. 1740. 2 <i>n't</i>	-0.022+1.1n't
12— 8		o. 075+0. 4n't
6 9	0. 006	+0.013
7— 9	-0.001+0.5n't	+0.001+0.2n't
8 9	+0. 2n't	+0.2n't
9— 9	+0. I <i>n't</i>	—o. 1 <i>n't</i>
10— 9	-0.007+0.8n't	+0.001-0.5n't
11-9	-0.006+1.4 <i>n't</i>	+0.002—0.3n't
12 — 9	0. 034+0. 4 <i>n't</i>	+0.080+0.2n't
910	—o. I <i>n't</i>	\circ , $\circ n't$
10—10	—o. I <i>n't</i>	+0. I <i>n't</i>
11—10	o. In't	-o. 6n't
12—10	-0,008-0. In'	+0.003 0.0n't
11—11	o. I <i>n't</i>	+0. 2 n 't
12-11	0. 5n't	0.0n't

Arg=i'g'+ig	$-rac{1}{2}ig(rac{ar{d}\cdot\delta \mathbb{W}_0ar{i}}{d\gamma'}ig)$		
	sin.	cos.	
i' i o o i o o i o o o o o o o o o o o o	$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	$\begin{array}{cccccccccccccccccccccccccccccccccccc$	

$\mathbf{Arg} = i'g' + ig$	$-rac{1}{2}(rac{d\cdot dW_0'}{dy'})$		
	sin.	cos.	
i' i - 4 1	,,, ,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,	,, ,, + 0.0027	
— 3— I	-0.0215 0.02n't	+ 0.0474 - 0.02n't	
- 2- I	-1.0238 - 0.14n't	+ 0. 2665 — 0. 66n't	
_ I _ I	-0.9422 4.94n't	+ 0.8056 — 4.86n/t	
0— 1	0. 8188 — 140. 51n't	+ 0.8569 — 55.88n't	
т— т	-0.5757 - 20.98n't	- 0. 4865 - 0. 55n't	
2— I	+0.9016 — 254.16n't	+ 0.4326 +330.83n't	
3— I	+2.9518 + 6.92n't	+ 1.6489 + 54.17n't	
4— 1	+1.3220 + 2.19n't	-0.0737 + 8.01n't	
5— 1	-0.0205 + 0.68n't	+ 0.0390 + 0.61n't	
6— 1	-0.0009 + 0.23n't	- 0.0003 + 0.03 $n't$	
— 3— 2	0.002	+ 0,001	
- 2- 2	-0.0396 0.00n't	+ 0.0138 0.00n't	
I 2	-0.2504 + 0.05n't	- 0.4805 - 0.01n't	
0— 2	-0.4984 - 4.42n't	- 0. 4322 - 0. 98n't	
I— 2	-0.4541 - 15.99n't	-0.2651 + 34.67n't	
2— 2	+0.2013 — 1.16n't	-0.2731 + 24.83n't	
3- 2	+0. 2620 + 86. 66n't	- 0.5827 +179.81n't	
4— 2	+3. 1325 —3892. 97n't	—12. 3561 — 9. 69n't	
5— 2	+1.35685— 25.805n't	+ 3.11867+ 17.113n't	
6— 2	+0.2229 - 6.10n't	+ o. 1602 — 9. 33n't	
7— 2	+0.0276 — 0.33n't	+ 0.0021 0.41n't	
8— 2	+0.0026 - 0.05n't	0.0017 0.06n't	
- 2- 3	o. oor	0.002	
<u> </u>	—o. o24	0. 025	
o 3	+0.2158 0.29n't	— 0. 1863 — 0. 01 <i>n't</i>	
1 3	+0.1353 - 2.02n't	- 0. 3148 $+$ 2. 87 $n't$	
2— 3	+0.0845 — 14.33 <i>n't</i>	- 0. 2861 $+$ 0. 30 $n't$	
3— 3	+0.0875 - 5.64n't	- 0.0060 + 8.25 $n't$	
4 3	+0.3122 - 34.21n't	$-0.0312 + 109.73n'\ell$	
5 3	-0.5342 + 18.25n't	- 0. 1081 + 88. 29 $n't$	
6— 3	-0.7411 + 49.51n't	+ 0.3556 + 58.74n't	
7— 3	+0.0912 — 13.56n/t	+ 1.4233 - 4.25n't	
8— 3	+0.0889 — 1.08n't	+ 0.1319 + 0.41n't	
9— 3 10 3	-0.0091 - 0.07n't	+ 0.0547 0.00 <i>n't</i> + 0.0025	
		, -	
— I— 4	0, 000	— d. 002	
0— 4	+0.013	— 0. 025	
1— 4	+0.122 - 0.1n't	+ 0.085 + 0.2n't	
2— 4	+0.1914 - 0.63n't	+ 0.0370 — 0.15n't	
3 4	+0.1722 - 1.53n't +0.0268 - 4.45n't	- 0.0074 - 8.63n't	
4 4		+ 0.0424 1.57n't	
5— 4 6— 4	+0.0453 - 51.14n't +0.1493 - 34.27n't	+ 0. 1417 $-$ 4. 91 $n't$	
0— 4 7— 4	+1.8380 - 11.29n't	+ 0.3419 + 14.10n't + 1.7084 + 13.90n't	
/ +	1 5,500 *** ******	T 1. 7004 T 13. 90%	

Arg=i'g'+ig	$-\frac{1}{2}$	$\frac{\vec{x} \cdot \delta \vec{W}_{0}'}{dy'}$
	sin.	cos.
i' i	" "	" "
8 4	+1.4611 — 1.96n't	+0.5513 + 7.44n't
9— 4	—5. 7269 — 9. 88n't	+1.6971 —24.11n't
10— 4	-0.05028- 0.274n't	+0.05993- 0.179n't
11-4	0.0001	+0.0004
1— 5	+0.020	-+-0. 005
2- 5	o. o31	+o. o76
3— 5	+0.006 - 0.3n't	+0.111 - 0.6n't
4 5	+0.024 + 5.0n't	+0.096 — 1.8n't
5— 5	-0.0110 + 0.10n't	+0.0248 - 2.21n't
6— 5	—0. 0615 — 2. 90n't	+0.0628 -25.22n't
7 5	0. 072310. 99n't	+0. 1459 —16. 11n't
8— 5	—0. 5985 — 7. 97 <i>n't</i>	+1.0395 4.15n't
9— 5	-0. 0329 — 3. 42 <i>n't</i>	+0.7472 + 0.13n't
10— 5	+0.1597 — 1.08n't	+0.3103 + 0.80n't
11 5	+0.2020 - 0.41n't	+0.1337 + 0.83n't
12- 5	-0. 0347 - 0. 02n't	0.0000 — 0.12n't
2 6	+0.001	+0.014
3— 6	-o. o47	_o. oo8
4 6	-0.065 + 0.3n't	+0.016 - 0.2n't
5 6	-0.052 + 1.5n't	+0.026 + 2.6n't
6 6	-0.017 + 1.4n't	+0.003 0.0n't
7- 6	-0.0403 + 12.26n't	-0.0277 - 3.99n't
8 — 6	-0.0805 + 7.40n't	-0.0001 - 7.83n't
9— 6	-0.5898 + 1.49n't	-0.1847 - 5.04n't
10 6	-0. 4024 - 0. 54n't	+0.0623 - 1.88n't
11— 6	-0. 1359 - 0. 47n't	+0.1049 - 0.46n't
12 6	-0.0231 - 0.21n't	+0.0571 - 0.03n't
3— 7	—o. oo7	
4— 7	0.001	—o. o31
5— 7	-0.017 + 0.4n't	-0.035 + 0.4n't
6- 7	-0.022 - 1.0n't	-0.022 + 1.1n't
7— 7	-0.006 + 0.4n't	-0.007 + 0.4n't
8 7	+0.011 + 3.5n't	-0.007 + 0.4nt $-0.024 + 5.8n't$
9— 7	-0.017 + 5.6n't	-0.024 + 3.0nt -0.039 + 3.1n't
10— 7	+0.024 + 3.4n't	-0.331 + 0.3n't
11— 7	-0.091 + 1.1n't	$\begin{array}{cccccccccccccccccccccccccccccccccccc$
12 7	-0.074 + 0.2n't	$-0.025 - 0.5n^{2}t$ $-0.067 - 0.3n^{2}t$
5 8	+0.012	
6 8	+0.012 +0.015 - 0.1n't	0.005
7— 8	+0.005 - 0.9n't	-0.013 + 0.2n't
7— 8 8— 8		-0.013 - 0.5n't
	+0.003 - 0.5n't	-0.001 + 0.4n't
9— 8	+0.010 - 3.0n't	-0.003 + 2.6n't
10— 8	+0.015 - 1.3n't	-0.020 + 3.5n't
11 8	+0.176 + 0.1n't	-0.028 + 1.8n't
12— 8	+0.116 + 0.4n't	-0.077 + 0.6n't

$\mathbf{Arg} = \mathbf{i}'g' + \mathbf{i}g$	$-rac{\mathrm{I}}{2}\Big(\!rac{ec{d}\cdot\delta\mathrm{W}_0{}'}{d\gamma'}\!\Big)$	
	sin.	cos.
6' 6 6 9 7 9 8 9 9 9 10 9 11 9 12 9 9 10 10 10 11 10 12 10	+0.003 +0.007—0.3n't +0.1n't -0.1n't +0.004—1.3n't +0.018—2.3n't +0.034—1.1n't +0.4n't +0.3n't +0.3n't +0.3n't +0.008 0.0n't	+0.006 $+0.007+0.1n't$ $-0.6n't$ $-0.6n't$ $+0.005-1.0n't$ $+0.007-0.4n't$ $+0.088+0.4n't$ $-0.1n't$ $-1.0n't$ $+0.009-1.0n't$
11—11 12—11	+0. 3n't +0. 3n't	+0. 3n't 0. 0n't

In obtaining the products $\left(\frac{\overline{dW_0'}}{d\gamma'}\right)n'\delta z'$ and ν'^2 the secular terms of the second order have been included in the values of the factors, so that, as far as these terms are concerned, we have

The expressions of the two products to be employed in determining $n'\delta^2z'$ follow:

Arg=i'g'+ig	$\left(\frac{d W_o'}{d \gamma'}\right)$	$n'\delta z'$
	cos.	sin.
i' i		и и
1 0	$-3.2193+0.97n't \\ -0.2650n'^2t^2$	-1. 3312-0. $79n^{t}t$ 0. $0000n^{t}t^{3}$

Arg=i'g'+ig	$\left(rac{d \operatorname{W}_{q'}}{d \gamma'} ight)$	$n'\delta z'$
	cos.	sin.
i' i 2 0	,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,	" (1) (1) (1) (1) (1) (1) (1) (1) (1) (1)
3 0	$\begin{array}{cccc} & - & 1.6748n'^3t^2 \\ & + 0.0407 + & 1.32n't \\ & - & 0.1170n'^2t^2 \end{array}$	$ \begin{array}{cccccccccccccccccccccccccccccccccccc$
4 0	$\begin{array}{cccc} & -0.1176n^{2}t^{2} \\ & +0.1174 + 0.11n^{t}t \\ & -0.0079n^{t^{2}t^{2}} \end{array}$	$+0.0663 + 0.08n't$ $-0.0160n'^2t^2$
5 0	$-0.0016 + 0.01n't - 0.0004n'^2t'^2$	+0.0031 0.00n't 0.0010n'2t2
3 I 2 I	-0.0020 -0.3850 + 0.30n't	0.0180 0.0960 0.44n't
	$-0.2592 + 8.35n^{t}$	-0. 2343 6. 93n't
0— 1	-0.2592 + 0.35nt -0.2289 + 145.09n't	-0.2343 - 0.93nt $-0.2146 - 67.55n't$
1-1	-0.0347 - 80.01n't	-0.0075133.76n't
2— 1	+0.0837 + 121.31n't	+0.9138 + 93.09n't
3— I	+0.5664 + 85.64n't	+0.4607 —137.93n't
4— 1	+3.3627 + 16.98n't	+0.7575 - 12.05n't
5— 1	+0.0862 + 1.13n't	+0.0728 — 0.88n't
6— 1	+0.0014 + 0.06n't	+0.0070 — 0.03n't
2 2	—o. or 18	0.0052
—I— 2	—0. 0698 — 0. 04 <i>n't</i>	+0.1449 0.26n't
0— 2	-0.1122 + 3.99n't	+0.0852 — 5.09n't
I— 2	-0. 1146 - 10. 07 <i>n't</i>	+0.0575 — 64.56n't
2— 2	-0.0302 - 3.35n't	+0.0401 — 20.72n't
3— 2	0. 0387 —290. 00n't	+0.5806 +212.61n't
4 2	+0. 1589 <i>−</i> 754. 93 <i>n′t</i>	+0. 1844 +112. 92n't
5— 2	- -0. 04490—348. 440 <i>n't</i>	-0.00059162.108n't
6— 2	+0. 1656 —468. 79 <i>n't</i>	—0. 0409 —658. 50 <i>n't</i>
7— 2	+0.0223 - 26.84n't	+0.0039 — 36.41 <i>n't</i>
8— 2	+0.0019 1.71n't	+0.0012 2.29n't
—ı— 3	— 0. 007	-
o— 3	+0.0548 + 0.25n't	+0.0438 — 0.15n't
1 3	+0.0265 - 0.68n't	+0.0587 - 0.91n't
2— 3	+0.0152 - 20.81n't	+0.0565 — 1.43n't
3- 3	-0.0194 - 9.22n't	+0.0810 — 6.97n't
4— 3	+0.2010 — 10.09n't	+0.0822 - 23.96n't
5-3	+1.0324 + 1.16n't	+0.1191 — 15.57n't
6 3	+2.7298 + 2.02n't	+1.0753 - 2.67n't
7— 3	+0.3574 + 3.37n't	-0.7091 - 1.62n't
8— 3	+0.0653 — 1.82n't	-0.0450 - 0.23n't
9— 3	+0.0070 — 0.16n't	-0.0078 - 0.07n't
0— 4	+0.002	+0.005
1— 4	+0.026	-0.020
2— 4	+0.0312 - 0.65n't	-0.0062 - 0.05n't
3— 4	+0.0260 — 2.42n't	-0.0007 + 7.92n't

Arg=i'g'+ig	$\Big(rac{d \mathbb{W}_0{}'}{d \gamma'}\Big)$	$n'\delta z'$
	cos.	sin.
i' i	<i>''</i>	" "
4 4	+0.0254 -3.56n't	+0.0180 +2.82n't
5— 4	+0.0773 -9.87n't	-0.0414 + 1.70n't
6 4	+0.2600 -5.47n't	—∪. 2947 —I. 63 <i>n't</i>
7— 4	+0. 9499 —1. 56 <i>n't</i>	-0. 9325 -1. 51 <i>n't</i>
8— 4	-0.4847 + 0.13n't	+0.0015 +0.45n't
9 4	-3.7810 -0.18 <i>n't</i>	-1.0946 + 0.79n't
10— 4	-0.01472-0.795 <i>n't</i>	o. o1383+o. 744 <i>n't</i>
11 4	0.00541.06 <i>n't</i>	+0.0056 +0.28n't
2— 5	—o. oo6	0.014
3— 5	—0. 00I —0. 2n't	-0.013 + 0.3n't
4— 5	-0.001 +3.1n't	-0.005 + 1.7n't
5— 5	+0.0008 +0.76n't	-0.0038 + 1.88n't
6— 5	-0.0117 -0.12n't	-0.0200 +4.48n't
7 5	0.08911.30n/t	-0.0735 + 2.39n't
8 5	-0. 2345 -0. 90n't	-0.3985 +0.59n't
9— 5	-0.0131 -0.35n't	-0.2439 + 0.03n't
10— 5	+0.0486 —0.10n't	-0.0976 -0.06n't
11-5	+0. 0368 -0. 01 <i>n't</i> -0. 0084 0. 00 <i>n't</i>	-0.0265 -0.01n't -0.0006 -0.02n't
12— 5	0.0084 0.00m1	
3— 6	0.007	+0.002
4— 6	+0. In't	+0.2n't
5 6	+1. In't	—I. In ⁱ t
6— 6	+1. in't	-0. 2n't
7 6	-0.0098 + 2.04n't	+0.0057 +0.51n't
8 6	-0.0387 + 1.06n't	+0.0183 +0.93n't
9— 6 10— 6	-0.1750 + 0.21n't	+0.0589 + 0.54n't -0.0154 + 0.17n't
10— 6	-0. 1034 -0. $03n^{t}t$ -0. 0309 -0. $02n^{t}t$	-0.0134 + 0.17nt $-0.0233 + 0.04n't$
12— 6	-0.0369 -0.02nt -0.0046 -0.02nt	$-0.0107 + 0.01n^{t}$
5— 7	+0. I <i>n't</i>	—0. I <i>n't</i>
6 7	-0.4n't	—0. 6n't
7— 7	0. on't	—0. 5 <i>n't</i>
8— 7	+0.001 +0.5n't	+0.005 -0.9n't
9— 7	+0.001 +0.6n't	+0.014 -0.4n't
10— 7	+0.008 +0.3n't	+0.082 -0.1n't
11 7	-0.017 + 0.1n't	+0.048 0.0n't
12 7	o. o14	+0.012
6— 8	o. o <i>n't</i>	—0. I <i>n't</i>
7 8	0. 3n't	+0. In't
8 8	—0. 3n't	0. 2n't
9 8	—0. 5n't	-0. 4n't
10— 8	+0.006 —0.1 <i>n't</i>	+0.002 -0.4n't
11— 8	+0.037 $0.0n't$	
12— 8	+0.020 0.0 $n't$	+0.013 -0.1n't

Arg=i'g'+ig	$\left(rac{d \widetilde{\mathbb{W}}_{0}'}{d \gamma'} ight)$	$n'\delta z'$
	cos.	sin
i' i 8— 9	11 11 0. on ¹ t	" " +0. In't
9 — 9	o. on't	+0.2n't
10— 9	-o. 3n't	+0. In't
11 9	o. 2n't	$0. \ On't$
12— 9	+0.006—0.1 <i>n't</i>	-0.014 0.0n't
1010	0. On't	+0. In't
12—10	0. On't	+0. I <i>n't</i>

	ν'	2
Arg=i'g'+ig	cos.	sin.
i' i	11 11	II il
0 0	+0.4048 - 0.6096n't	i
1 0	$+$ 0. 9461 $n^{2}t^{2}$ $-$ 0. 0981 $+$ 27. 53 $n^{t}t$	0.1600 44.000/4
1 ' '	-0.0981 + 27.53nt + 0.0826 $n^{12}t^2$	-0. 1633 -44. 23n't - 0. 0476n'2t'
2 0	-0.0268 + 3.22n't	-0.0284 - 0.85n't
	$-0.4120n^{12}t^{2}$	$-0.8502n^{2}t^{2}$
3 0	-0.0047 + 0.32n't	+0.0076 + 0.05n't
	$- 0.0232n'^2t^2$	$-$ 0. 0477 n'^2t^2
4 0	$0.0000 + 0.02n^{t}t$	0.0000 + 0.01n't
,	— 0.0013n'2t'2	- 0.0027n'213
-ı- ı	+0.0079 + 2.09n't	+0.0075 — 1.36n't
0 1	+0.0139 +50.14 <i>n't</i>	+0.0060 —20.91 <i>n't</i>
ı— 1	+0.0523 -17.66n't	-0.1469 -32.69n't
z I	o. 116341. 53n't	-0.2007 -33.21n't
3— 1	0. 2684 —21. 39n't	+0.1101 +27.92n't
4— I	+0.0377 + 2.67n'i	+0.0124 — 0.61n't
5— 1	+ 0.15n't	0.05n't
0— 2	+0.0028 + 0.59n't	-0.0019 - 0.75n't
I— 2	+0.0016 — 1.44 <i>n't</i>	0.0056 9.31n't
2 2	—0.0994 — 2.30n't	—0.0401 — 4.89 <i>n't</i>
3.− 2	0. 027482. 49 <i>n't</i>	+0.0868 +65.78n't
4— 2	+0.0724 + 9.85n't	+0.2583 + 3.87n't
5— 2	+0.00550+87.527n't	0. 04049+40. 333n't
6— 2	-0.0004 - 5.41n't	+0.0012 -12.35n't
7— 2	— 0. 26n't	- 0.21n't
8— 2	— o. oi <i>n't</i>	-0.02n't
1— 3	0. 00n't	— 0.07 <i>n't</i>
2- 3	— 2. IIn't	— 0. I5n't
3 3	o, 0186 1. 35n't	+0.0271 - 0.67n't
4-3	+0.0037 + 0.34n't	+0.0189 + 1.21n't

	$ u^{r_2}$	
Arg=i'g'+ig	cos.	sin.
i' i	<i>n</i>	Н И
5— 3	+0. 2831 —0. 11 <i>n't</i>	+0.0229 +0.71n't
6 3	-0. 0492 -0. 72n't	-0.2102 + 1.04n't
7— 3	-0.0241 -0.76n't	+0.0424 +0.39n't
8— 3	+0.0027 +0.37n't	-0.0001 + 0.07n't
2— 4	—Q. 05 <i>n't</i>	+0.01n't
3 4	-c. 20n't	+0.63 <i>n't</i>
4 4	+0.0069 -0.31n't	+0.0075 +0.35n't
5— 4	+0.0079 +0.42n't	+0.0018 -0.02n't
6— 4	+0.0162 +0.37n't	-0.0443 + 0.13n't
7— 4	+0.0111 +0.13n't	-0.0200 +0.14n't
8 4	-0.2421 + 0.11n't	+0.0622 +0.36n't
9 4	+0.0750 +0.01n't	+0.0280 +0.01n't
10 4	—0. 00350+0. 198 <i>n′t</i>	-0. 006200. 189 <i>n't</i>
11— 4	-0.04n't	+0.01n't
4- 5	+0. 2n't	+0. In't
5 5	+0. IIn't	+0. 15n't
6 5	+0.03n't	—0. IOn't
7— 5	-0.0095 + 0.07n't	0.00530.12n't
8— 5	-0.0041 + 0.06n't	—0. 0068 —0. 03 <i>n't</i>
9— 5	-0.0005 +0.03n't	-0.0043 -0.01 <i>n't</i>
10 5	+0.0023 +0.01n't	-0.0036 + 0.01n't
11— 5	o. oo17	+0.0010
12— 5	+o. 0004	0.0000
7— 6	o. o5n't	-0.02n't
8— 6	0. 04 <i>n't</i>	0.04n't
9— 6	o. oI <i>n't</i>	-0.04 <i>n't</i>
10— 6	+o. oi $n't$	—o. oi <i>n't</i>

There follow the expressions of $-\frac{1}{2}\left(\frac{\overline{d^2W_0'}}{\overline{d}\gamma'^2}\right)$ and its product by $n'\delta z'$, which forms the second part of $\frac{d\cdot\delta\nu'}{n'dt}$:

Arg=i'g'+ig	$-\frac{1}{2}(\tilde{d})$	$\frac{d^2 \overline{W} o'}{d \gamma'^2}$
	cos.	sin.
i' i	// // 260. 121	и и
1 0	+ 36. 323—3. 3061n/t	+11.655+5.2963n't
2 0	+ 2.009—0.3703n't	+ 1.121+0.5934n't
3 0	+ 0.073-0.0350n't	+ 0.067 + 0.0561n't
4 0	— 0.001—0.0031 <i>n't</i>	o. 000+0. 0050n't

Arg=i'g'+ig	$-rac{1}{2}\left(rac{d^2W_0'}{d\gamma'^2}\right)$	
gy 149	cos.	sin.
i' i	"	"
—3— I	+ 0.004	+ 0.004
—2— I	+ 0.039	+ 0.037
—I— I	+ 0.326	+ 0.237
0 I	+ 1.962	+ 2.972
1— 1	+121.718	535. 167
2— І	+ 71.015	— 78. 902
3— I	+ 5.720	 7. 090
4— I	+ o. 438	— 0. 274
5— 1	+ 0.020	+ 0.003
6 I	— o. oor	+ 0.005
2- 2	+ 0.007	— 0.002
—ı— 2	+ 0.074	- 0. OI 2
O— 2	+ 0.784	+ o. oo8
I— 2	+ 13.625	 24 . 844
2— 2	+ 93.486	+ 36.557
3— 2	+ 30.517	+ 11.437
4— 2	— 37. 653	305. 118
5— 2	+ 0.47137	— 1. 30389
6 2	+ 0.743	+ 0.107
7— 2	+ 0.086	+ 0.025
8— 2	+ 0.008	+ o. oo3
o— 3	+ 0.019	— 0.02I
1— 3	+ 0.521	1. 58 7
2 — 3	+ 2.949	— I. 210
3 3	+ 23.441	— 31. 12 5
4 3	+ 18.666	— 8. 533
5 3	+ 8.008	+ 0. 782
6 3	+ 3.57 r	+ 2.373
7 — 3	— o. 230	— o. 46o
8— 3	— о. ооб	— o.o15
1— 4	+ 0.019	- o. o88
2— 4	+ 0.04I	- 0.077
3— 4	+ 0.526	— 1. 53I
4 4	11.114	— 1 3.018
5— 4	— 2. 259	— 9.639
6— 4	+ 0.979	 3. 469
7— 4	+ o. 8o6	— o. 79 9
8 4	+ 0.292	— o. 12 7
9— 4	— o. 8o2	— O. 212
10— 4	— o. oo477	— o. oo4o4
11 4	+ o. oo45	+ 0.∞52
3 5	+ 0.005	o. o5o
4- 5	— o. 669	— o. 571
	1	

Arg=i'g'+ig	$-rac{1}{2} \left(rac{d^2 \overline{W_0}'}{d\gamma'^2} ight)$	
	cos.	sin.
i' i	, , , , , , , , , , , , , , , , , , , ,	"
5 5	 7. 044	+3.673
6— 5	5. 190	+0. 120
7 5	—ı. 788	 0. 909
8— 5	o. 342	<u> </u>
9 5	O. OI2	—o. 172
10 5	+0. 023	0. 045
11— 5	- 0. 021	-0. 014
4— 6	 0. 025	—o. o37
5— 6	 0. 596	+0.212
6— 6	+0.934	+3.668
7— 6	—о. 532	+2.747
8— 6	0. 731	+0.921
9— 6	—о. 348	+0. 145
10— 6	o. 101	0. 011
11— 6	o. o19	-o. o15
5 7	—o. o39	+0.004
6— 7	+0. ∞9	+0. 390
7 7	+1.824	<u></u> 0. 023
8— 7	+1.396	<u>+</u> 0. 600
9— 7	+0.440	+0.540
10 7	+0.044	+0. 234
11-7	0.022	<u>+</u> 0.06 5
12 7	0.011	+0.011
6— 8	0. 009	+0.024
7 8	+o. 222	+o. o68 _*
8 8	+o. 206	<u></u> о. 863
9— 8	+0.486	 0. 670
10— 8	+0.370	0. 190
11 8	+0. 151	+0.004
12 8	+o. o38	+0.021
7— 9	 -0. 016	- 0. 011
8— 9	+0.072	0. 121
9— 9	о. 383	0. 200
10 9	0. 297	—о. 338
11— 9	<u></u> 0. 064	0. 237
12- 9	+0.020	 0. 093
8—10	- -0. 011	—o. oog
910	 0. 055	<u> </u>
to—to	—о. 143	+0. 156
11—10	0. 215	+0.115
12-10	0. 141	+0.008

Arg=i'g'+ig	$-rac{1}{2}\Big(rac{d^2\overline{W_0'}}{d\gamma'^2}\Big)n'\delta z'$	
	sin.	cos.
i' i	<i>"</i>	" "
0 0		+0.088806— 11.2139n't
1 0	—1. 8383 — 83. 45n't	+1.5115 —134.52n't
	— 0. 1856n ¹² t ²	0.0000n ² t ²
2 0	+0.0686 — 10.00n't	-0. 2856 - 9. 33n't
3 0	— 0. 8493 <i>n'</i> 2 <i>t</i> 3 —0. 0537 — 0. 67 <i>n't</i>	+ 1.6978n'2t ⁹ -0.6626 - 0.49n't
'	— 0. 1064n'st2	$+$ 0. 2140 $n^{/9}t^{2}$
4 0	-0. 1796 — 0. 03 <i>n't</i>	-0.0179 - 0.01 <i>n</i> ′ <i>t</i>
	- 0. $0!05n^{/2}t^2$	$+$ 0.0212 n'^2t^2
5 0	-0.0020 - 0.0010 $n^{/2}t^{2}$	$-0.0046 + 0.0018n'^2t^2$
-3- I	+ 0.014	—o. 014
2 I	+0.2422 — 0.18n't	0.0646 0.09n't
—ı— ı	+0.1606 + 0.61n't	-0. 1008 - 1. 68n't
о— 1	+0.1144 + 161.88n't	-0.0928 + 47.69n't
ı— ı	-0.0410 + 67.76n't	-0.0061 - 60.56n't
2— I	-0.7129 + 120.84n't	+0. 1874 —121. 78n't
3— 1	-1.5367 + 42.91n't	-0.4746 + 23.05n't
4 I	-3.4478 + 9.51n't	+0.6212 + 5.14n't
5— 1	+0.123 + 0.88n't	-0.205 + 0.66n't
6 1	+o. oo6	-0. 025
-2- 2	+0.010	+0.001
—I— 2	+0.0486 + 0.13n't	+0.0976 0.20n't
0 2	+0.0766 + 9.13n't	+0.0532 — 0.38n't
I— 2	+0.0446 + 7.33n't	+0.0377 - 34.73n't
2— 2	-0.0184 + 18.82n't	+0.0167 — 12.26n't
3— 2 4— 2	-0. 0992 +173. 13n't -0. 0240 +389. 46n't	-0.5991 +112.58n't
4— 2 5— 2	-1.32222 5. $303n't$	-1.1671 + 56.68n't
6— 2	-0. 1662 -236. 60n't	-3.11372 + 2.580n't -0.1938 + 329.73n't
7 2	-0.0116 - 26.79n't	-0.090 + 36.65n't
8— 2	-2.51n't	+ 3.49n't
-ı- 3	+0.002	+0.006
0-3	-0.0391 + 0.49n't	+0.0321 + 0.12n't
ı— 3	-0.0180 + 0.76n't	+0.0419 — 0.57n't
2— 3	-0.0064 + 13.08n't	+0.0329 — 1.47n't
3 3	-0.0412 + 5.59n't	-0.0514 - 4.77n't
4 3	-0.1540 + 5.12n't	+0.0082 - 12.69n't
5— 3	+0.8008 - 0.70n't	-0.0780 - 7.37n't
6 3	+3.0147 - 0.70n't	-2.4513 - 0.78n't
7— 3	+0.2875 — $0.54n't$	—0. 6490 — 0. 25 <i>n't</i>
8— 3	+0.0269 - 0.57n't	-0.0556 + 0.08n't
9— 3	-0.0020 - 0.09n't	-0.0072 + 0.01n't
1— 4	0. 020	0.014
2— 4	-0.0234 + 0.48n't	-0.0046 + 0.11n't
		1

Arg=i'g'+ig	$-rac{1}{2}(rac{d^2}{d\eta})$	$\frac{N_{0'}}{r^{\prime 2}} n' \delta z'$
	sin.	cos.
i' i	и и	и и
3— 4	-0.0187 + 1.64n't	-0.0003 + 5.22n't
4 4	-0.0081 + 2.57n't	-0.0023 + 1.86n't
5— 4	+0.0154 + 5.89n't	-0.0541 + 1.00n't
6— 4	+0.0422 +2.98n't	o. 3339o. 97n't
7— 4	-0.4838 + 0.75n't	o. 5260o. 78n't
8— 4	+0.3339 -0.09n't	-0.0270 + 0.18n't
9— 4	+1.8881 +0.11n't	-0.5424 + 0.45n't
10— 4	+0.01006-0.026n's	-0.00958-0.022n't
11 4	-0.0025 -0.52n't	-0.0041 -0.12n't
2 5	+0.005	0.011
3— 5	0.001	o. oto
4 5	-2. 07n't	+1.22n't
5 5	—0. 56n't	+1.36n't
6 5	+0.0223 +0.13n't	-0.0245 +3.01n't
7— 5	+0.0604 +0.80n't	-0.0633 + 1.35n't
8— 5	+0.1419 +0.52n't	-0.2495 + 0.31n't
9— 5	+0.0038 +0.18n't	-0. 14570. 01 <i>n't</i>
10- 5	o. o28o	o. o515
11— 5	 0. 0142	-0.0101
12 5	+0.0042	+0.0003
5— 6	—0. 79n't	-o. 83n't
6— 6	—o. 8on't	o. 30n't
7 6	+0.0071 —1.45n't	+0.0040 +0.39n't
8— 6	+0.0313 -0.62n't	+0.0134 +0.58n't
9 6	+0.1188 -0.12n't	+0.0381 +0.34n't
10 6	+ 0. 0678	o. o1 16
11— 6	+0. 0179	-0.0144
12 6	+0.0027	—о. 0067
6— 7	+0. 3n't	-0.5n't
7 7	0. On't	—o. 5n't
8— 7	—o. 3n't	_0. 5n't
9 7	0, 0010. 4n't	+0.012 -0.3n't
10— 7	0.005	+0.058
11 7	+0.012	+0.030
12— 7	+0.009	+0.008
10— 8	o. oo6	-0.002
11— 8	—o. o24	+0.004
12— 8	—o. o15	+0.010
12— 9	0, 005	-o. oi i

If we add the three portions of $\frac{d \cdot n' \delta^2 z'}{n'dt}$, which have just been given, we shall have the value of this quantity. In $\overline{\delta W_0}'$ we give k_0 such a value that $n' \delta^2 z'$ may have no term proportional to t, and k_1 and k_2 are so assumed that the terms having the

argument g' may vanish. For this it is necessary to put $k_0 = +1$ ".5316, $k_1 = +0$."5432, and $k_2 = +0$ ".3989.

In integrating the terms depending on the arguments 5g'-2g and 10g'-4g we have equated the motion of the latter, and have proceeded in a way precisely similar to that followed in deriving $\delta W_0'$ from $\delta T'$. By joining the first order with the second order terms, it is found that, as far as these two arguments are concerned, we have

Setting aside quantities of the third order this expression can be replaced by the following:

$$\frac{d(n'\delta z')}{n'dt} = [(1.9644830) - (8.3669461)n't] \cos [5g' - 2g + 247 26 44.14 - (7.2640621)n't] + [(0.1504991) + (5.88018)n't] \cos [10g' - 4g + 133] 0 34.7 + (6.78501)n't]$$

The integrating factors for the equated arguments are given by

$$\log \mu = 1.5015038$$
 $\log \mu = 1.1719199$

After neglecting certain quantities of the third order the integrated expression can be put under the form

$$n'\delta z' = \begin{bmatrix} -1143.2024 - 4.660293n't \end{bmatrix} \sin(5g' - 2g) + \begin{bmatrix} -2691.4278 + 2.782008n't \end{bmatrix} \cos(5g' - 2g) + \begin{bmatrix} -14.3434 - 0.010128n't \end{bmatrix} \sin(10g' - 4g) + \begin{bmatrix} 15.3517 - 0.007920n't \end{bmatrix} \cos(10g' - 4g)$$

By subtracting the corresponding terms of $n'\delta z'$, found in Chapter II, we get

$$n'\delta^2z' = \begin{bmatrix} -114.0044 - 4.660293n't \end{bmatrix} \sin(5g' - 2g) + \begin{bmatrix} -273.6868 + 2.782008n't \end{bmatrix} \cos(5g' - 2g) + \begin{bmatrix} -16.8155 - 0.010128n't \end{bmatrix} \sin(10g' - 4g) + \begin{bmatrix} 17.8091 - 0.007920n't \end{bmatrix} \cos(10g' - 4g)$$

If we add the two portions of $\frac{d \cdot \delta \nu'}{n'dt}$ we have the value of this quantity. In integrating we get the constant term of $\delta \nu'$ by the aid of the formula given at page 289. The constant term of $\frac{1}{3} \left(\frac{d \cdot \delta z'}{dt} + \frac{1}{2} \nu' \right)^2$ is +0''.2374. Thus, the constant term of $\delta \nu'$ is found to be +0''.2781.

In integrating the term depending on the argument 5g'-2g the motion of the latter has been equated. The first-order terms being included, we have

$$\frac{d\nu'}{n'dt} = [-\circ''.76834 - \circ''.\circ\circ311\circ8n't \sin(5g' - 2g) + [-1''.51690 + \circ''.\circ\circ19693n't] \cos(5g' - 2g)$$

$$= [(\circ.23\circ5490) - (6.54556)n't] \sin[5g' - 2g + 243° 8' 12''.78 - (7.33352)n't]$$

The logarithm of the integrating factor is 1.5059163, and we obtain

$$v' = [24''.9523 + o''.o99369n't] \cos (5g' - 2g) + [-48''.4634 + o''.o63826n't] \sin (5g' - 2g)$$

By subtracting the corresponding terms of ν' , in Chapter II, we get

$$\delta v' = [\circ''.8754 + \circ''.99369n't] \cos(5g' - 2g) + [-2''.8311 + \circ.''\circ63826n't] \sin(5g' - 2g)$$

The values of $n'\delta^2z'$ and $\delta\nu'$ follow:

	$n'\delta^2z'$			
Arg=i'g'+ig	sin,	cos.		
i' i	и и	"00013045 n'^2t^2 0001767 n'^3t^3		
1 0	—1. 355224 <i>n't</i> — . 00255569 <i>n'</i> ² t ³	$-1.787350n't + .00195723n'2t^{1}$		
2 0	$\begin{array}{cccccccccccccccccccccccccccccccccccc$	$+ 1.5631024799n't + .00023963n'^3t^3$		
3 0	- 0.0087000461n't 00000567n'2t2	+ 0.5428— .000690 $n't+ .00001028n'^2t^2$		
4 0	$+ 0.0277000016n't0000027n'^3t^2$	- 0.0020000028 $n't$ + .0000049 n'^9t^2		
5 0	— 0. 0003	- 0.0006		
-4- I -3- I	+ 0.0052 + 0.0007	+ 0.0016 + 0.0036		
2 I	0. 1640 000008n't	+ 0.0410000011n't		
-I- I 0- I	- 0.2170000338n/t - 0.3357005861n/t	+ 0.1965— .000261n't + 0.3621— .002973n't		
I I	- 0.5882+.007757n't	- 0. 3238 011436n't		
2— I 3— I	+ 2.2522106611n't + 10.1442 + .022503n't	+ 3.8506+ .164691n't + 7.8013+ .033438n't		
4— I	+ 0.2837+.001252n't	+ 0.0504+ .001087n't		
5— I 6— I	- 0.0252+.000049n't - 0.0002000006n't	+ 0.0112+.000044n't 0.0000000003n't		
z 2	- 0.0027	+ 0.0026		
—I— 2	- 0.0290+.000002n't	— 0.0585— .000003 <i>n't</i>		
0 2	- 0.0780000046n't	— 0.0552— .000033n ^t t		
I— 2 2— 2	$\begin{array}{cccccccccccccccccccccccccccccccccccc$	— 0.0501— .001648n't		
3- 2	+ 0.0555 + .00041/n + 0.1701 + .029724n't	- 0.0720000120n't - 0.3633+.027242n't		
4-2	+ 6.6113— .747047n't	$-27.1947 + .009349n^{t}t$		
5— 2	—114. 0044—4. 660293 <i>n't</i>	-273.6868+2.782008n't		
6— 2	— 0.0567— .046962 <i>n't</i>	— 0. 1037+ . 062944 <i>n't</i>		
7— 2	+ 0.0013— .001350n't	- 0.0012 $+$.001771 $n't$		
8— z	+ 0.0003— .000058n't	- 0.0001 + .000074 $n't$		

	n	$\delta^2 z'$
Arg=i'g'+ig		
	sin.	CO8.
i' i	11 11	" "
— I— 3	o. oo24	0.0011
o— 3	+ 0.0216000004n't	— 0.0181—.000003 <i>n't</i>
1 3	+ 0.0147 + .000028n't	— 0. 0368—. 000047 <i>n't</i>
z— 3	+ 0.0089+.000104 <i>n't</i>	— 0.0372—.000032n't
3— 3	+ 0.0488 $+$.000118 $n't$	+ 0.0502—.000024n't
4 3	+ 0.0228—.000898n't	+ 0.0017+.002949n't
5- 3	0. 2566+. 000928n't	— 0.0611+.003718n't
6 3	+ 0.3728 + .005367n't	- 1.0977+.006121 <i>n't</i>
7— 3	+ 2.7313—.012031n't	+ 7. 2025—. 004269n't
8— 3	+ 0.6006—.000794 <i>n't</i>	+ 0.3875+.000213n't
9— 3	0.0206—.000014 <i>n't</i>	+ 0.0594+.000011n't
10-3	+ 0.0008	+ 0.0013
0— 4	+ 0.0002	— o. ooi i
1-4	+ 0.0097 $+$.000001 $n't$	+ 0.0074 .000000n't
2 4	+ 0.0175 + .000008n't	+ 0.0045+.000002n't
3 4	+ 0.0187+.000021n't	+ 0.0011000011n't
4 4	— 0.0068+.000011n't	+ 0.0116+.000022n't
5— 4	+ 0.0034000888n't	+ 0.0252000085n't
6— 4	— 0. 0326—. 000774 <i>n't</i>	- 0.0422+.000356n't
7— 4	+ 0.4595—.000342n't	+ 0.4047+.000489n't
8— 4	+ 1.4923000118n't	+ o. 3826+.000557n't
9 4	- 8. 9304 002187n't	+ 2.6357005379n't
10 4	—16. 8155—. 010128n't	+17.8091007920n't
11-4	- 0.0089000111 <i>n't</i>	+ 0.0116—.000026n't
1— 5	+ 0.0009	0,0000
2 5	— 0.0024 .000000 <i>n't</i>	+ 0.0054000001n't
3 5	+ 0,0009+.000002n't	+ 0.0090000002n't
4 5	+ 0.0027 $+$.000020 $n't$	+ 0.0088—.000002n't
5— 5	— v. 0018—, 000003n/t	+ 0.0021+.000004n't
6— 5	0.0032000035n't	+ 0.0031—.000333n't
7— 5	+ 0.0039000180n't	+ 0.0095—.000236n't
8— 5	— 0.0947—.000154 <i>n't</i>	+ 0.1640—.000064 <i>n't</i>
9— 5	+ 0.0008—.000087 $n't$	+ 0.1632+.000011n't
10 5	+ 0.0643 $-$.000045 $n't$	+ 0.1086+.000039n't
11 5	+ 0. 2071 $-$. 000042 $n't$	+ 0.1283+.000086n't
12- 5	0. 3212 000019n't	0.0118000118n't
2 6	+ 0.0003	+ 0.0010
3— 6	- 0.0023 $+$.000002 $n't$	- 0.0005+.000001n't
4 6	-0.0038+.000002n't	+ 0.0008000003n't
5 6	- 0.0028+.000001 <i>n't</i>	+ 0.0015+.000016n't
6 6	0.0016000010n't	+ 0.0020—.000007n't
7— 6 8— 6	$\begin{array}{lll} - & 0.0027 + .000137n't \\ - & 0.0043 + .000076n't \end{array}$	+ 0.0005—.000035n't
9— 6	-0.0043+.000070nt 0.0711+.000013n't	+ 0.0025—.000089n't — 0.0226—.000072n't
10— 6	- 0.0590000011n't	+ 0.0129—.000031n't
11— 6	- 0.0233000012n't	+ 0.0221—.000010n't
12 6	— 0. 0043—. 000005 <i>n't</i>	+ 0.0180 .000000n't

	$n'\delta^2z'$			
Arg=i'g'+ig	sin.	cos.		
i' i	и и	11 11		
3— 7	-0.0005	-0.0001		
4 7	o. ooo1	0. 0006		
5— 7	—0.0005+.000002n't	—0.0010—.000001 $n't$		
6 7	0.0007000011n't	-0.0008+.000005n't		
7 7	0.0001+.000001 <i>n't</i>	+0.0001—.000001 <i>n't</i>		
8— 7	+0.0011+.000031n't	-0.0018 + .000053n't		
9— 7	-0.0021 + .000048n't	-0.0014 + .000025n't		
10 7	+0.0028+.000033n't	-0.0316+.000003n't		
11 7	-0.0122+.000009 <i>n't</i>	o. 0235 000006 <i>n't</i>		
12— 7	-0.0095+.000006n't	o. 0076 000004 <i>n't</i>		
5 8	+0.0002	-0,0001		
6— 8	+0.0006000001 <i>n't</i>	—0.0001—,000002 <i>n't</i>		
7— 8	+0.0002+.000002n't	—0.0008—.000001 $n't$		
8 8	+0.0006—.000003n't	+0.0001+.000003n't		
9-8	+0.0003—.000019n't	0.0000 + .000017n't		
10 8	-0.0005000009n't	-0.0009+.000026n't		
11— 8	+0.0154+.000002 <i>n't</i>	-0.0020+.000011n't		
12 8	+0.0111+.000004n't	-0.0079+.000004n't		
6— 9	+0.0004	+o. 0008		
7 9	+0.0001—.000003n't	+0.0001 + .000001n't		
8— 9	o. 0000 00000In't	o. 0000+. 000002n't		
9— 9	o. 0000—. 000001 <i>n't</i>	0. 0000+. 000001 <i>n't</i>		
10 9	+0.0006000004n't	+0.000100003n't		
11 9	+0.0005—.000011 <i>n't</i>	+0.000200003 <i>n't</i>		
12— 9	+0.0027—.000003 <i>n't</i>	+0.0064+.000002 <i>n</i> ′ <i>t</i>		
12—10	+0.0006+.000001 <i>n't</i>	+0.0002+.000001n't		

Arg=i'g'+ig		δ	· · · · · · · · · · · · · · · · · · ·
		cos.	sin.
i' o	í o	+. 00011252n'2t ²	" "
I	0	$+$ o. 6169 $+$. 676008 $n't$ $+$. 00128728 n'^2t^2	+0. 6757—. 892752 <i>n't</i> +. 00097623 <i>n'</i> 2 <i>t</i> ²
2	0	$+$ 0. 7470 $+$. 018297 $n't$ $-$ 1. 00007799 n'^2t^2	+1.2544—. $024933n't+.00011223n'2t^2$
3	0	+0.0292+.000710n't $+.00000504n'^2t^2$	+0.5359—. $001080n't+.00000828n'^2t^2$
4	o	+0.0276+.000034n't +.0000034n'2t2	+0.0154000058n't $+.00000059n'^2t^2$
5	o	+0.0004+.000001n't $+.0000002n'^2t^3$	-0.0009000003 $n't$ +.00000004 n'^2t^2

	$\delta u'$			
Arg=i'g'+ig	cos.	sin.		
š' š	11 11	11 11		
- 4- I	0.0003	0.0004		
— 3— I	0.0014	0.0061		
— 2— I	0. 1744 000007n't	- 0.0450+.000017n't		
_ i_ i	-0. 2245 000124n't	- 0.2023+.000188n/t		
o— 1	-0.2838+.000861 <i>n't</i>	- 0.3074+.000330n't		
ı— ı	-0.4186+.003154n't	+ 0.3343+.004120n't		
2— I	+0.4800—.027584n't	— 1. 3399—. 04325 <i>2n't</i>		
3— т	2. 7100 009645n't	+ 2.2915 + .014945n't		
4— I	+1.4022000771n't	+ 0.3615 + .000867n't		
5— I	+0.0033000062n't	+ 0.0074+.000050n't		
6— 1	+0.0001—.000007 <i>n't</i>	— 0.0008+.000001 <i>n't</i>		
— 2— 2	o. 0042	o. oo21		
— I— 2	o. 0338+. 000003n't	+ o. o642+. ooooo4n'i		
0 2	-0. 0849+. 000095n't	+ 0.0763+.000027n't		
I— 2	0. 1032—. 000218n't	+ 0.0572 $+$.000002 $n't$		
2— 2	+0.0618+.000595n't	+ 0.0866—.000424 <i>n't</i>		
3— 2	+0.0904+.013210n't	+ o. 6076—. 014867 <i>n't</i>		
4— 2	+3. 2207—. 362438n't	+13.6148 004861 <i>n't</i>		
5 2	+0.8754+.099369n't	— 2.8311+.063826n't		
6— 2	0.0249+.023487 <i>n't</i>	— 0.0552+.031006n't		
7— 2	-0.0070+.001334n't	-0.0041+.001782n't		
8— 2	o. 0009+. 000084n't	— 0.0006+.000113n't		
- I— 3	—0. 0026	+ 0.0022		
o— 3	+0.0237+.000003n't	+ 0.0207—.000001 <i>n't</i>		
1— 3	+0.0182000020n't	+ 0.0423—.000036n't		
2— 3	+0.0143—.000023n't	+ 0.0464+.000021n't		
3-3	+0.0104000001 <i>n't</i>	+ 0.0129—.000078n't		
4- 3	+0.0467000843n't	+ 0.0065—.002813n't		
5 3	+0.1102+.000716n't	+ 0.0762—.003302n't		
6 3	+1.5708+.003366n't	+ 1.4476—.003996n't		
7— 3	+0.8394003134n't	— 1.7277+.001000n't		
8 3	-0. 2103+. 000300n't	+ 0.1382+.000089n't		
9 3	+0.0072+.000010n't	+ 0.0306+.000001n't		
10-3	+0.0004	+ 0.0010		
0 4	+0.0013	+ 0.0025		
I— 4	+0.0114000001n't	0. 0079 000002n't		
2 4	+0.0212000002n't	- 0.0041 $+$.000001 $n't$		
3— 4	+0.0221+.000002n't	+ 0.0011+.000049n't		
4-4	+0,0032—,000032n't	— 0. 0068—, 000005 <i>n't</i>		
5— 4	+0.0123000917n't	0.0180+.000079n't		
6— 4	+0.0488—.000795n't	- 0.0022000334n't		
7 4	+0. 4619—. 000359n't	- 0.4032000447n't		
8-4	+0. 9286—. 000106n't	-0.4032000447nt $-0.2713000394n't$		
9— 4	-4. 1159—. 001047n't	1		
10— 4	+0. 5985+. 000450n't	— I. 2383+. 002535n't		
		+ 0.7483—.000301n't		
11-4	+0.0024+.000049n't	— 0.0035—.000011n't		

	82'			
Arg=i'g'+ig	6087	sin.		
4/ 4	,, ,, +0.0018	" "		
1-5		-0.0004		
2— 5	-0.0025	0.0062		
3— 5	+0.0005—.000003n't	-0.0107+.000006n't		
4 5	+0.0029+.000035n't	-0.0114+.000007 <i>n't</i>		
5— 5	o. 0015 000006n'i	-0.0033+.000011n't		
6— 5	-0.0055000043n't	-0.0056+.000346n't		
7-5	-0.0023000188n't	-0.0153+.000272n't		
8— 5	-0. 1034 000169n't	-0. 1789+. 000087n't		
9— 5	—0. 0852—. 000095 <i>n't</i>	—0. 1760—. 000004 <i>n't</i>		
10-5	+0.0545—.000045n't	—0. 1071—. 000033 <i>n't</i>		
11-5	+0.1325—.000029n't	o. 0872 000059n't		
12- 5	o. 0733 000006 <i>n't</i>	-0.0007+.000029n't		
2— 6	+o. ooo r	0.0011		
3— 6	—o. oo39	÷0.0007		
4 6	-0.0060+.000003n't	-0.0015 + .000002n't		
5— 6	-0.0053 + .000007n't	-0.0026000018n't		
6— 6	-0.0019 + .000007n't	0.0003+.000003n't		
7 6	-0.0042+.000137n't	+0.0030+.000046n't		
8 6	-0.0071 + .000098n't	-0.0019 + .000105n't		
g— 6	-0.0798+.000023n't	+0.0248+.000080n't		
10— 6	-0.0683000011n't	—0. 0103+. 000038n't		
11 6	0. 0303, 000012n't	-0.0232+.000012n't		
12— 6	o. 0070 000007n't	-0.0174+.000001n't		
3— 7	0.0005	-0. 000I		
4 7	0,0001	+0.0023		
5 7	-0.0014+.000003 <i>n't</i>	+0.0028—.000003n't		
6 7	-0.0019000011n't	+0.0019000005n't		
7— 7	0.0006+.000004n't	+0.0007+.000001n't		
8— 7	+0.0012+.000034n't	+0.0026—.000056n't		
9— 7	-0.0021+.000062n't	+0.0032000033n't		
10 7	+0.0026+.000046n't	+0.0370—.000004n't		
11 7	-0.0124+.000017n't	+0.0305+.000008n't		
12 7	-0.0121+.000004 <i>n't</i>	+0.0110+.000006n't		
5— 8	+ 0.0008	+0.0003		
6— 8	+0.0011—.000001 <i>n't</i>	+0.0009—.000001n't		
7— 8	+0.0004000007 <i>n't</i>	+0.0010+.000004n't		
8— 8	+0.0003000004n't	+0.0001—.000003 <i>n't</i>		
9— 8	+0.0009000028n't	+0.0003000024n't		
10— 8	+0.0009—.000013 <i>n't</i>	+0.0022000035n't		
11 8	+0.0171+.000001n't			
12— 8	+0.0128+.000005 <i>n't</i>	+0.0085—.000008 <i>n't</i>		
6— 9	+0.0002	—0. 0002		
7— 9	+0.0005—.000002n't	-0.0005000001n't		
8— 9	+.000001n't	+.000004n't		
9— 9	—. 000001 <i>n't</i>	+. 000004n't		
10— 9	+0.0003—.000011n't	o. 0003+. 000008n't		
11 9	+0.0016—.000020 <i>n't</i>	o. 0006+. 000004n't		
12- 9	+0.0028000011n't	o. 0074 000004n't		
12—10	+0.0006 .000000n't	-0.0007+.000008n't		

CHAPTER XVI.

PERTURBATIONS OF THE THIRD ORDER WITH RESPECT TO DISTURBING FORCES IN THE LONGI-TUDES AND RADII-VECTORES, ARISING FROM THE MUTUAL ACTION OF JUPITER AND SATURN— DETERMINATION OF THE FACTORS OF δ°T AND δ°T′.

The corrections to be applied to T and T', on account of terms of three dimensions with respect to disturbing forces, will be denoted by δ^2 T and δ^2 T'. In determining them it is important to reject all parts of the formulæ which afford insignificant terms, and thus reduce the very onerous labor involved. In this connection it will be seen, on referring to the previous elaboration of the second-order terms, that those involving the factors u and u' are generally insignificant and in the remaining cases quite small. As, in the third-order terms, these factors should give rise to still smaller terms, it is thought allowable to entirely neglect them. For like reasons, all terms arising through the consideration of δh and $\delta h'$ will be neglected. Thus, we will consider only the four augmentations, $n\delta z$, ν , $n'\delta z'$, and ν' .

Then, applying Taylor's theorem, extended to any number of variables, to the functions T and T', we have

$$\begin{split} \delta^2 \mathbf{T} &= \mathbf{A} n \delta^2 z + \mathbf{B} \delta \nu + \mathbf{F} n' \delta^3 z' + \mathbf{G} \delta \nu' \\ &+ \frac{\mathbf{I}}{2} \frac{d \mathbf{A}}{dg} (n \delta z)^2 + \frac{d \mathbf{A}}{dg'} (n \delta z) (n' \delta z') + \frac{\mathbf{I}}{2} \frac{d \mathbf{F}}{dg'} (n' \delta z')^2 \\ &+ \frac{d \mathbf{B}}{dg} (n \delta z) \nu + \frac{d \mathbf{B}}{dg'} (n' \delta z') \nu + \frac{d \mathbf{G}}{dg} (n \delta z) \nu' + \frac{d \mathbf{G}}{dg'} (n' \delta z') \nu' \\ &+ \frac{\mathbf{I}}{2} r^2 \frac{d^2 \mathbf{T}}{dr^2} \nu^2 + r r' \frac{d^2 \mathbf{T}}{dr dr'} \nu \nu' + \frac{\mathbf{I}}{2} r'^2 \frac{d^2 \mathbf{T}}{dr'^2} \nu'^2 \\ \delta^2 \mathbf{T}' &= \mathbf{A}' n' \delta^2 z' + \mathbf{B}' \delta \nu' + \mathbf{F}' n \delta^2 z + \mathbf{G}' \delta \nu \\ &+ \frac{\mathbf{I}}{2} \frac{d \mathbf{A}'}{dg'} (n' \delta z')^2 + \frac{d \mathbf{A}'}{dg} (n \delta z) (n' \delta z') + \frac{\mathbf{I}}{2} \frac{d \mathbf{F}'}{dg} (n \delta z)^2 \\ &+ \frac{d \mathbf{B}'}{dg'} (n' \delta z') \nu' + \frac{d \mathbf{B}'}{dg} (n \delta z) \nu' + \frac{d \mathbf{G}'}{dg'} (n' \delta z') \nu + \frac{d \mathbf{G}'}{dg} (n \delta z) \nu \\ &+ \frac{\mathbf{I}}{2} r'^2 \frac{d^2 \mathbf{T}}{dr'^2} \nu'^2 + r r' \frac{d^2 \mathbf{T}'}{dr dr'} \nu \nu' + \frac{\mathbf{I}}{2} r^2 \frac{d^2 \mathbf{T}'}{dr^2} \nu^2 \end{split}$$

The four factors, A, B, F, and G, of the first line of each of these two expressions are the same as the factors, denoted by these symbols, employed in the computation of the second order terms, and the first factors of the two following lines are obtained from those just mentioned by partial differentiation with respect to g or g'. Thus,

eleven out of fourteen quantities involved in each of these expressions are determined in the easiest manner possible; a notable advantage resulting from the employment of Hansen's variables. But the first factors of the three terms in the last line of each expression must be specially computed. They all have the form

The readiest method of obtaining them appears to be the following: Derive, in the first place, the two quantities

$$a_{0}\left(r\frac{d}{dr}\right)^{3}\Omega = \mu \left\{-\frac{15}{8}\left(\frac{a'}{\triangle}\right)^{7}\left(\alpha^{2}\frac{r^{2}}{a^{2}} - \frac{r'^{2}}{a'^{2}}\right)^{3} + \left(\frac{a'}{\triangle}\right)^{5}\left[\frac{9}{8}\left(\alpha^{2}\frac{r^{2}}{a^{2}} - \frac{r'^{2}}{a'^{2}}\right)^{2} + \frac{9}{2}\frac{r'^{2}}{a'^{2}}\left(\alpha^{2}\frac{r^{2}}{a^{2}} - \frac{r'^{2}}{a'^{2}}\right)\right] - \frac{1}{2}\left(\frac{a'}{\triangle}\right)^{3}\frac{r'^{2}}{a'^{2}} - \frac{1}{8}\left(\frac{a'}{\triangle}\right)^{3}\left(\alpha^{2}\frac{r^{2}}{a^{2}} - \frac{r'^{2}}{a'^{2}}\right) - \frac{1}{8}\frac{a'}{\triangle} - \frac{a'r}{r'^{2}}H\right\}$$

$$a_{0}'\left(r'\frac{d}{dr'}\right)^{3}\Omega' = \mu'\left\{\frac{15}{8}\left(\frac{a'}{\triangle}\right)^{7}\left(\alpha^{2}\frac{r^{2}}{a^{2}} - \frac{r'^{2}}{a'^{2}}\right)^{3} + \left(\frac{a'}{\triangle}\right)^{5}\left[\frac{9}{8}\left(\alpha^{2}\frac{r^{2}}{a^{2}} - \frac{r'^{2}}{a'^{2}}\right)^{2} - \frac{9}{2}\alpha^{2}\frac{r^{2}}{a^{2}}\left(\alpha^{2}\frac{r^{2}}{a^{2}} - \frac{r'^{2}}{a'^{2}}\right)\right] - \frac{1}{2}\left(\frac{a'}{\triangle}\right)^{3}\alpha^{2}\frac{r^{2}}{a^{2}} + \frac{1}{8}\left(\frac{a'}{\triangle}\right)^{3}\left(\alpha^{2}\frac{r^{2}}{a^{2}} - \frac{r'^{2}}{a'^{2}}\right) - \frac{1}{8}\frac{a'}{\triangle} - \frac{a'r'}{r^{2}}H\right\}$$

To save labor, it must be remembered that

$$\left(\frac{\mathbf{a}'}{\triangle}\right)^5 \left(\alpha^2 \frac{r^2}{\mathbf{a}^2} - \frac{r'^2}{\mathbf{a}'^2}\right)^2 \text{ and } \left(\frac{\mathbf{a}'}{\triangle}\right) \left(\alpha \frac{r^2}{\mathbf{a}^2} - \frac{r'^2}{\mathbf{a}'^2}\right)$$

have been computed in our work on the second-order terms, and that

$$\left(\frac{\mathbf{a}'}{\triangle}\right)^3 \left(\alpha^2 \frac{r^2}{\mathbf{a}^2} - \frac{r'^2}{\mathbf{a}'^2}\right), \quad \left(\frac{\mathbf{a}'}{\triangle}\right)^3 \alpha^2 \frac{r^2}{\mathbf{a}^2}, \quad \left(\frac{\mathbf{a}'}{\triangle}\right)^3 \frac{r'^2}{\mathbf{a}'^2}, \quad \frac{\mathbf{a}'}{\triangle}, \quad \frac{\mathbf{a}'r}{r'^2} \mathbf{H}, \text{ and } \frac{\mathbf{a}'r'}{r^2} \mathbf{H}$$

have been computed for the first-order terms.

In the second place, derive Y and Y' from the equations

$$\mathbf{Y} = \mathbf{M} \frac{d}{dg} \left(a_0 r \frac{d\Omega}{dr} \right) + \mathbf{N} a_0 \left(r \frac{d}{dr} \right)^2 \Omega$$

$$\mathbf{Y'} = \mathbf{M'} \frac{d}{dg'} \left(a_0' r' \frac{d\Omega'}{dr'} \right) + \mathbf{N'} a_0' \left(r' \frac{d}{dr'} \right)^2 \Omega'$$

M, N, M', and N' have been used in deriving the quantities denoted X and X' in the second-order terms. Also, $\frac{d}{dg}\left(a_0r\frac{d\Omega}{dr}\right)$, etc., have already been obtained in computing V and V' in the second-order terms.

Then

$$r^{2}\frac{d^{2}\mathbf{T}}{dr^{2}} = \mathcal{A}\frac{d}{dg}\left[a_{0}\left(r\frac{d}{dr}\right)^{2}\Omega\right] + Ba_{0}\left(r\frac{d}{dr}\right)^{3}\Omega - \mathbf{B} - \mathbf{X} + 2\mathbf{Y}$$

$$r'^{2}\frac{d^{2}\mathbf{T}'}{dr^{2}} = \mathcal{A}'\frac{d}{da'}\left[a_{0}'\left(r'\frac{d}{dr'}\right)^{2}\Omega'\right] + B'a_{0}'\left(r'\frac{d}{dr'}\right)^{3}\Omega' - \mathbf{B}' - \mathbf{X}' + 2\mathbf{Y}'$$

We have already used

$$a_0 \left(r \frac{d}{dr}\right)^2 \Omega$$
 and $a_0' \left(r' \frac{d}{dr'}\right)^2 \Omega'$

in computing V and V'. The quantities, for the sake of distinction, denoted \mathcal{A} , \mathcal{B} , \mathcal{A}' , and \mathcal{B}' are the same as A, B, A', and B' in the formulæ of the first-order terms

$$\begin{split} \mathbf{T} &= \mathbf{A} a_0 \frac{d\Omega}{dg} + \mathbf{B} a_0 r \frac{d\Omega}{dr} \\ \mathbf{T}' &= \mathbf{A}' a_0' \frac{d\Omega'}{dq'} + \mathbf{B}' a_0 r' \frac{d\Omega'}{dr'} \end{split}$$

After $r^2 \frac{d^2 \mathbf{T}}{dr^2}$ and $r'^2 \frac{d^2 \mathbf{T'}}{dr'^2}$ have been obtained, we get the four remaining factors from the equations

$$r^{2}\frac{d^{2}T}{dr'^{2}} + rr'\frac{d^{2}T}{drdr'} = -2B - X + Y$$

$$rr'\frac{d^{2}T}{drdr'} + r'^{2}\frac{d^{2}T}{dr'^{2}} = -2G - X - Y$$

$$r'^{2}\frac{d^{2}T'}{dr'^{2}} + rr'\frac{d^{2}T'}{drdr'} = -2B' - X' + Y'$$

$$rr'\frac{d^{2}T}{drdr'} + r^{2}\frac{d^{2}T'}{dr^{2}} = -2G' - X' - Y'$$

These equations result very simply from the consideration that T and T' are homogeneous functions of r and r'.

If, then, we make the two following multiplications, viz.,

$$\left(\frac{\mathbf{a}'}{\triangle}\right)^7 \text{ by } \frac{15}{8} \left(\frac{\mathbf{r}'^2}{\mathbf{a}'^2} - \alpha^2 \frac{\mathbf{r}^2}{\mathbf{a}^2}\right)^3$$
$$\left(\alpha^2 \frac{\mathbf{r}^2}{\mathbf{a}^2} - \frac{\mathbf{r}'^2}{\mathbf{a}'^2}\right) \left(\frac{\mathbf{a}'}{\triangle}\right)^5 \text{ by } -\frac{9}{2} \alpha^2 \frac{\mathbf{r}^2}{\mathbf{a}^2}$$

we shall be able, by the aid of the products, together with expressions previously obtained, to get the quantities $a_0 \left(r\frac{d}{dr}\right)^3 \Omega$ and $a_0' \left(r'\frac{d}{dr'}\right)^3 \Omega'$, and that through simple additions or subtractions.

By raising the value of $\frac{r'^2}{a'^2} - \alpha^2 \frac{r^2}{a}$, given on page 201, to the third power, we have

$$\frac{15}{8} \left(\frac{r'^2}{a'^2} - \alpha^2 \frac{r^2}{a^2}\right)^8 = [9.83735] - 2[9.19885] \cos g' + 2[8.0107] \cos 2g' - 2[5.61] \cos 3g' + 2[8.6105] \cos g + 2[7.1181] \cos 2g + 2[5.57] \cos 3g - 2[7.8045] \cos (g' - g) - 2[7.8045] \cos (g' + g) - 2[6.1481] \cos (g' - 2g) - 2[6.1481] \cos (g' + 2g) + 2[6.2142] \cos (2g' - g) + 2[6.2142] \cos (2g' + g)$$

Also

$$-\frac{9}{2}\alpha^2 \frac{r^2}{a^2} = -\left[0.12783\right] + 2\left[8.8096\right]\cos g + 2\left[6.89\right]\cos 2g$$

The derived products are:

Arg=i'g'+ig	$\frac{15}{8} \left(\frac{\mathbf{a}'}{\triangle}\right)^7 \left(\frac{\mathbf{a}'}{\mathbf{a}}\right)^{-1}$	$\frac{r^2}{r^2} - \alpha^2 \frac{r^2}{a^2}$	$\frac{9}{2} \left(\frac{\mathbf{a}'}{\Delta}\right)^5 \left(\frac{\mathbf{r}'^2}{\mathbf{a}'^2} - \alpha^2 \frac{\mathbf{r}^2}{\mathbf{a}^2}\right) \alpha^2 \frac{\mathbf{r}^2}{\mathbf{a}^2}$	
	cos.	sin.	cos.	sin.
i' i				
0 0	+17.678		+6.785	.0
0— I	2. 853	— 3. o58	-1.404	— I. 582
0 2	— o. 149	+ 0. 294	o. o73	+ 0.162
o— 3	+ 0.017	+ 0.007	+0.011	+ 0.002
0 4	+ 0.001	0.000		
I+ 4	0.000	+ 0.001		
1+3	+ 0,006	+ 0.002	+0.001	+ 0.001
I+ 2	+ 0.003	— o. o45	+0.003	0. 024
1+ 1	— o. 591	+ 0.127	0. 315	+ 0.062
1 0	+ 4.033	+ 4.930	+1.949	+ 2.190
I I	+ 6.615	—32. 8o5	+2.397	—11.966
I— 2	— I. 728	+ 1.241	-1.073	+ 0.698
r— 3	+ 0.133	+ 0. 128	+o. o68	+ 0.061
1— 4	+ 0,006	— o. oo7	+0.003	— o. oo5
1— 5	0.010	+ 0.001		
2+ 3	— o. oo3	— 0.009		
2+ 2	+ 0.003	— o. oo7	+0.002	0,002
2+ I	o. o81	o. o35	0.042	— o. o18
2 0	o. oo3	+ 1.021	+0.020	+ o. 509
2 I	+ 6.925	- 4. 278	+2.782	1.947
2 2	—26. 604	—II. 248	8. 932	 3⋅743
2— 3	+ 0.333	+ 0.459	+0. 256	+ o. 588
2 4	+ 0.097	— 0. 066	+0.041	O. O2I
2 5	+ 0.008	0.006	0.001	— 0. 002
3+ 2	+ 0.001	0.001		
3+ 1	o. oo8	- 0.007	0.003	— o. oo5
3 0	— o. o89	+ 0.122	- —0. 044	+ 0.066
3— 1	+ 1.493	+ 0.234	+o. 681	+ 0.053
3 2	— 3. 576	8. 298	—1. 531	- 3.020
3— 3	13. 154	+19.067	4. 000	+ 5.853
3— 4	— o. 464	— o. o34	+0. 226	— o. o53
3— 5	0, 062	- o. o87	0, 004	— 0.025
3— 6	— o. oo6	- o. oo2	-0.001	+ 0.001
4+ 1	+ 0.002	— o. oo6		
4 0	O. O2I	+ 0.007	-0.010	+ 0.004
4— 1	+ 0. 171	+ 0. 175	+0.088	+ 0.079
4— 2	+ 0.569	— т. 868	+0. 157	— 0.774
4 3	— 8. 723	+ 2.196	2. 884	+ 0.914
4— 4	+12.065	+12.722	+3. 396	+ 3.539
4 5	— 0.092	+ 0.964	0, 002	- 0.011
4 6	o. o85	+ 0.059	o. o15	+ 0.001
4— 7	+ 0.002	+ 0.004	l	
L	<u> </u>	<u> </u>	<u> </u>	1

Arg=i'g'+ig	$\frac{15}{8} \left(\frac{a'}{\triangle} \right)^7 \left(\frac{r'^2}{a'^2} - \alpha^2 \frac{r^2}{a^2} \right)^3$		$\frac{9}{2} \left(\frac{\mathbf{a}'}{\triangle}\right)^5 \left(\frac{\mathbf{r}'^2}{\mathbf{a}'^2} - \alpha^2 \frac{\mathbf{r}^2}{\mathbf{a}^2}\right) \alpha^2 \frac{\mathbf{r}^2}{\mathbf{a}^2}$	
22.6—19 19	cos.	sin.	cos.	sin.
i' i				
5 0	0.003	+0.001	0. 001	-0.001
5— 1	+ 0.006	+0.039	+0.004	+0.018
5— 2	+ 0.290	-0. 201	+0.114	—о. 101
5— 3	— 2.032	-o. 959	—o. 767	-o. 27 I
5 4	+ 0.611	+8. 191	+o. 326	+2.471
5— 5	+10.806	-6. 581	+2.766	-1.709
5— 6	+ 1.087	+0. 290	+0.087	+0.017
5— 7	+ 0.010	+0.099	+0.001	+0.012
5 8	0.005	+0.025	0.000	+0.001
6— г	— 0, 004	+0.003	o. oo1	+0.002
6— 2	+ 0.058	+0.001	+0.025	-0.003
6— 3	- O, 212	-0.406	0.099	-0. 144
6 4	— 1.317	+1.951	0. 364	+0.672
6— 5	+ 6.967	十0.757	+1.927	+0. 106
6— 6	2.838	-8. 305	—0. 691	1.967
6— 7	+ 0.463	o. 9 66	+0.043	-o. 1 09.
6— 8	+ 0.112	-0,024	+0.010	-0.002
6 9	+ 0.019	+0.013	1	
7— 2	+ 0.007	+0.004	+0.003	+0.002
7- 3	+ 0.015	o. o8o	+0.001	—o. o33
7 4	0. 505	+0. 169	—0. 164	+0.081
7— 5	+ 1.662	+1.556	+o. 528	+0.410
7— 6	+ 1.655	-5.417	+0.350	1. 382
7 7	 5.855	+0.623	-1. 291	+0. 150
7— 8	— o. 723	-0. 549	0, 094	0. 065
7 9	— 0.010	-0. 109	0. 002	-0.010
8— 3	+ 0.005	-0.010	+0.004	-0.004
8 4	— o. o97	0. 032	o. o36	o. oo6
8 5	+ 0.094	+0.567	+0.053	+o. 169
8— 6	+ 1.651	—1. 246	+0.411	0. 369
8— 7	— 3.853	2. 049	-0. 914	 0. 438
8— 8	— o. 432	+3.777	—o. o88	+o. 785
8— 9	— o. 589	+0.478	o. o67	+o. o66
9— 3	+ 0.003	0.001	+0.001	-o. oo i
9— 4	— o. o15	o. o15	-0. 005	-o. oo5
9— 5	- o. o55	+o. 126	-0.012	+o. o ₃ 8
9— 6	+ 0.653	0.005	+o. 158	0. 022
9- 7	o. 832	—1. 861	0. 226	0. 372
9— 8	- 2.604	+2.770	-0. 423	+0.554
9 9	+ 2.698	+1.384	+0. 446	+0. 163

Thence are derived the following expressions for $\frac{a_0}{\mu} \left(r \frac{d}{dr} \right)^3 \Omega$ and $\frac{a_0'}{\mu'} \left(r' \frac{d}{dr'} \right)^3 \Omega'$:

d' i cos. sin. cos. sin. d' i 0 0 -1.820 -7.663 -8.88 0 - 1 -0.184 -0.308 + 1.171 +0.888 0 - 2 -0.023 +0.043 +0.068 -0.135 0 - 3 +0.002 +0.003 -0.004 -0.004 1 + 3 +0.004 +0.001 -0.005 -0.001 1 + 2 0.000 -0.009 0.000 +0.011 1 - 1 -0.065 +0.021 +0.219 -0.054 1 - 0 +0.151 +0.137 -1.579 -2.043 1 - 1 -0.339 +1.593 -3.685 +18.109 1 - 2 -0.296 +0.198 +0.499 -0.132 1 - 3 +0.024 +0.028 -0.058 +0.093 1 - 4 +0.001 -0.001 -0.002 +0.002 2 + 2 0.000 -0.003 +0.001 +0.002 2 + 1 -0.015 -0.008 +0.018	Arg=i'g'+ig	$\frac{a_0}{\mu} \left(r \frac{d}{d} \right)$	$\left(\frac{l}{r}\right)^{3}\Omega$	$rac{a_{0'}}{\mu'} \left(r' rac{d}{d ilde{r'}} ight)^{3} \Omega'$	
0	**** 5 ***	cos.	sin.	cos.	sin.
0- I -0.184 -0.308 + I.17I + 0.888 0- 2 -0.023 + 0.043 + 0.068 - 0.135 0- 3 + 0.002 + 0.003 - 0.004 - 0.004 I+ 3 + 0.004 + 0.001 - 0.005 - 0.001 I+ 2 0.000 - 0.009 0.000 + 0.017 I+ 1 - 0.065 + 0.021 + 0.219 - 0.054 I- 0 + 0.151 + 0.137 - 1.579 - 2.043 I- 1 - 0.339 + 1.593 - 3.685 + 18.109 I- 2 - 0.296 + 0.198 + 0.499 - 0.132 I- 3 + 0.024 + 0.028 - 0.058 - 0.029 I- 4 + 0.001 - 0.001 + 0.028 - 0.058 - 0.029 I- 4 + 0.001 - 0.003 - 0.001 + 0.005 2+ 2 0.000 - 0.003 - 0.001 + 0.005 2+ 1 - 0.015 + 0.078 + 0.018 - 0.356 2- 1 + 0.477 <td></td> <td>- 0</td> <td></td> <td></td> <td></td>		- 0			
0-2 -0.023 +0.043 +0.068 -0.135 0-3 +0.002 +0.003 -0.004 -0.004 1+3 +0.004 +0.001 -0.005 -0.001 1+2 0.000 -0.009 0.000 +0.017 1+1 -0.065 +0.021 +0.219 -0.054 1-0 +0.151 +0.137 -1.579 -2.043 1-1 -0.339 +1.593 -3.685 +18.109 1-2 -0.296 +0.198 +0.499 -0.132 1-3 +0.024 +0.028 -0.058 +0.032 1-4 +0.001 -0.001 +0.028 -0.058 -0.002 2+2 0.000 -0.003 -0.001 +0.005 2+1 -0.015 +0.028 +0.032 +0.014 2-0 -0.015 +0.078 +0.018 -0.36 2-1 +0.477 +0.070 -3.137 +1.798 2-1 +0.477 +0.070 -3.137 +1.79					1 0 888
0-3			· ·		
1+3 +0.004 +0.001 -0.005 -0.001 1+2 0.000 -0.009 0.000 +0.017 1+1 -0.065 +0.021 +0.219 -0.054 1 0 +0.151 +0.137 -1.579 -2.043 1-1 -0.339 +1.593 -3.685 +18.109 1-2 -0.296 +0.198 +0.499 -0.132 1-3 +0.024 +0.028 -0.058 -0.029 1-4 +0.001 -0.001 -0.001 -0.002 +0.002 2+2 0.000 -0.003 -0.001 +0.005 2+1 -0.015 -0.008 +0.032 +0.014 2-0 -0.015 +0.078 +0.018 -0.396 2-1 +0.477 +0.079 -3.137 +1.798 2-2 -1.625 -0.663 +13.083 +5.559 2-3 +0.114 +0.120 +0.094 +0.045 2-4 +0.027 -0.063 +0.004 +0.001					
I+ 2 0.000 -0.009 0.000 + 0.017 I+ I -0.065 +0.021 + 0.219 -0.054 I 0 +0.151 +0.137 -1.579 -2.043 I- I -0.339 +1.593 -3.685 +18.109 I- 2 -0.296 +0.198 +0.499 -0.132 I- 3 +0.024 +0.028 -0.055 -0.029 I- 4 +0.001 -0.001 -0.001 +0.002 2+ 2 0.000 -0.003 -0.001 +0.005 2+ 1 -0.015 -0.008 +0.032 +0.014 2 0 -0.015 -0.008 +0.032 +0.018 2- 1 +0.477 +0.079 +0.018 -0.032 +0.018 2- 1 +0.477 +0.079 +0.132 +0.014 +0.079 +0.043 +5.559 2- 3 +0.114 +0.120 +0.090 +0.044 +0.034 +0.044 +0.034 +0.044 +0.034 +0.034 +0.034 <td< td=""><td>↓ · · · · ·</td><td>+0.002</td><td>+0.003</td><td>- 0.004</td><td>- 0.004</td></td<>	↓ · · · · ·	+0.002	+0.003	- 0.004	- 0.004
1+ 1 -0.065 +0.021 +0.219 -0.054 1 0 +0.151 +0.137 -1.579 -2.043 1- 1 -0.339 +1.593 -3.685 +18.109 1- 2 -0.296 +0.198 +0.499 -0.132 1- 3 +0.024 +0.028 -0.058 -0.029 1- 4 +0.001 -0.001 -0.002 +0.002 2+ 2 0.000 -0.003 -0.001 +0.005 2+ 1 -0.015 -0.008 +0.032 +0.014 2 0 -0.015 +0.078 +0.018 -0.396 2- 1 +0.477 +0.070 -3.137 +1.798 2- 2 -1.625 -0.663 +13.083 +5.559 2- 3 +0.114 +0.120 -0.009 +0.042 2- 5 +0.008 -0.002 -0.004 +0.034 2- 5 +0.008 -0.002 +0.004 +0.001 3- 1 +0.129 +0.097 -0.625 -0.146	r+ 3	+0.004	+0.001	0.005	- 0.001
I 0 +0. 151 +0. 137 -1. 579 -2. 043 I-1 -0. 339 +1. 593 -3. 685 +18. 109 I-2 -0. 296 +0. 198 +0. 499 -0. 132 I-3 +0. 024 +0. 028 -0. 058 -0. 029 I-4 +0. 001 -0. 001 -0. 002 +0. 004 2+2 0. 000 -0. 003 -0. 001 +0. 005 2+1 -0. 015 -0. 008 +0. 032 +0. 014 2 0 -0. 015 +0. 078 +0. 018 -0. 396 2-1 +0. 477 +0. 070 -3. 137 +1. 798 2-2 -1. 625 -0. 663 +13. 083 +5. 559 2-3 +0. 114 +0. 120 -0. 090 +0. 045 2-4 +0. 027 -0. 100 -0. 047 +0. 034 2-5 +0. 008 -0. 002 -0. 004 +0. 001 3-1 +0. 129 +0. 021 +0. 036 -0. 044 3-1 +0. 129 <td< td=""><td>1+ 2</td><td></td><td>-0.009</td><td>0, 000</td><td>+ 0.017</td></td<>	1+ 2		-0.009	0, 000	+ 0.017
1	1+1	o. o65	+0.021	+ 0.219	— o. o54
1 - 2	1 0	+o. 151	+o. 137		-
1-3	ı— 1	—о. 339	+1.593		
1— 4 +0.001 —0.001 —0.002 +0.004 2+ 2 0.000 —0.003 —0.001 +0.005 2+ 1 —0.015 —0.008 +0.032 +0.014 2 0 —0.015 +0.078 +0.018 —0.396 2- 1 +0.477 +0.070 —3.137 +1.798 2- 2 —1.625 —0.663 +13.083 +5.559 2- 3 +0.114 +0.120 —0.090 +0.045 2- 4 +0.027 —0.010 —0.047 +0.034 2- 5 +0.008 —0.002 —0.009 +0.003 3+ 1 —0.003 0.000 +0.004 +0.001 3- 0 —0.013 +0.021 +0.036 —0.044 3- 1 +0.129 +0.097 —0.625 —0.146 3- 2 —0.027 —1.038 +1.489 +4.058 3- 3 —1.941 +2.882 +7.037 —10.183 3- 4 —0.109 —0.033 +0.045 +0.058	I— 2	—0 . 296	+o. 198		
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2+ I -0.015 -0.008 + 0.032 + 0.014 2 0 -0.015 +0.078 + 0.018 - 0.396 2- I +0.477 +0.070 - 3.137 + 1.798 2- 2 -1.625 -0.663 + 13.083 + 5.559 2- 3 +0.114 +0.120 + 0.090 + 0.045 2- 4 +0.027 -0.010 - 0.047 + 0.034 2- 5 +0.008 -0.002 - 0.047 + 0.034 2- 5 +0.008 -0.002 - 0.099 + 0.003 3+ 1 -0.003 0.000 + 0.004 + 0.001 3- 0 -0.013 + 0.021 + 0.036 - 0.044 3- 1 + 0.129 + 0.097 - 0.625 - 0.146 3- 2 -0.027 - 1.038 + 1.489 + 4.058 3- 3 - 1.941 + 2.882 + 7.037 - 10.183 3- 4 - 0.109 - 0.069 + 0.508 + 0.008 3- 5 - 0.019 - 0.033 + 0.045 + 0.005 3- 6 - 0.005 + 0.001 + 0.	I— 4	+0.001	0. 001	— 0. 002	+ 0.004
2+ I -0.015 -0.008 + 0.032 + 0.014 2 0 -0.015 +0.078 + 0.018 - 0.396 2- I +0.477 +0.070 - 3.137 + 1.798 2- 2 -1.625 -0.663 + 13.083 + 5.559 2- 3 +0.114 +0.120 + 0.090 + 0.045 2- 4 +0.027 -0.010 - 0.047 + 0.034 2- 5 +0.008 -0.002 - 0.047 + 0.034 2- 5 +0.008 -0.002 - 0.099 + 0.003 3+ 1 -0.003 0.000 + 0.004 + 0.001 3- 0 -0.013 + 0.021 + 0.036 - 0.044 3- 1 + 0.129 + 0.097 - 0.625 - 0.146 3- 2 -0.027 - 1.038 + 1.489 + 4.058 3- 3 - 1.941 + 2.882 + 7.037 - 10.183 3- 4 - 0.109 - 0.069 + 0.508 + 0.008 3- 5 - 0.019 - 0.033 + 0.045 + 0.005 3- 6 - 0.005 + 0.001 + 0.	2+ 2	0. 000	-0.003	o. oo1	+ 0.005
2 0		0. 015	1		
2— I +0.477 +0.070 — 3.137 + 1.798 2— 2 —1.625 —0.663 +13.083 + 5.559 2— 3 +0.114 +0.120 — 0.090 + 0.045 2— 4 +0.027 —0.010 — 0.047 + 0.034 2— 5 +0.008 —0.002 — 0.009 + 0.034 2— 5 +0.008 —0.002 — 0.009 + 0.034 3— 1 —0.003 0.000 + 0.004 + 0.001 3— 1 +0.129 + 0.097 — 0.625 — 0.146 3— 2 —0.027 —1.038 + 1.489 + 4.058 3— 3 —1.941 + 2.882 + 7.037 — 10.183 3— 4 —0.109 —0.069 + 0.508 + 0.008 3— 5 —0.019 —0.033 + 0.045 + 0.052 3— 6 —0.002 —0.001 + 0.004 + 0.005 4— 1 + 0.013 + 0.027 — 0.065 — 0.005 4— 2 + 0.199 — 0.224 — 0.344 + 0.848 4— 3 — 1.622 + 0.029 + 4.601<					
2— 2	2— I			ľ	1
2- 3	2 2]
2-5 +0.008 -0.002 -0.009 +0.003 3+1 -0.003 0.000 +0.004 +0.001 3 0 -0.013 +0.021 +0.036 -0.044 3-1 +0.129 +0.097 -0.625 -0.146 3-2 -0.027 -1.038 +1.489 +4.058 3-3 -1.941 +2.882 +7.037 -10.183 3-4 -0.109 -0.069 +0.508 +0.008 3-5 -0.019 -0.033 +0.045 +0.052 3-6 -0.002 -0.001 +0.004 +0.002 4-0 -0.005 +0.001 +0.009 -0.002 4-1 +0.013 +0.027 -0.065 -0.076 4-2 +0.199 -0.224 -0.344 +0.848 4-3 -1.622 +0.029 +4.601 -0.928 4-4 +2.794 +2.881 -6.912 -7.300 4-5 -0.083 +0.308 +0.087 -0.065 4-6 -0.035 +0.017 +0.058 -0.003 <td< td=""><td>2— 3</td><td>+0. 114</td><td></td><td>1</td><td>1</td></td<>	2 — 3	+0. 114		1	1
3+ I -0.003 0.000 +0.004 +0.001 3 0 -0.013 +0.021 +0.036 -0.044 3- I +0.129 +0.097 -0.625 -0.146 3- 2 -0.027 -1.038 +1.489 +4.058 3- 3 -1.941 +2.882 +7.037 -10.183 3- 4 -0.109 -0.069 +0.508 +0.008 3- 5 -0.019 -0.033 +0.045 +0.052 3- 6 -0.002 -0.001 +0.004 +0.002 4- 0 -0.005 +0.001 +0.009 -0.002 4- 1 +0.013 +0.027 -0.065 -0.076 4- 2 +0.199 -0.224 -0.344 +0.848 4- 3 -1.622 +0.029 +4.601 -0.928 4- 4 +2.794 +2.881 -6.912 -7.300 4- 5 -0.083 +0.308 +0.087 -0.768 4- 6 -0.035 +0.017 +0.058 -0.045 4- 7 +0.005 +0.001 -0.002 -0.002	2— 4	+0.027	0.010	- 0.047	+ 0.034
3 0	2— 5	+ 0. 008	0.002	0. 009	+ 0.003
3— I +0. 129 +0. 097 — 0. 625 — 0. 146 3— 2 —0. 027 —I. 038 + I. 489 + 4. 058 3— 3 —I. 94I +2. 882 + 7. 037 —I0. 183 3— 4 —0. 109 —0. 069 + 0. 508 + 0. 008 3— 5 —0. 019 —0. 033 + 0. 045 + 0. 052 3— 6 —0. 002 —0. 001 + 0. 004 + 0. 002 4— 0 —0. 005 +0. 001 + 0. 009 — 0. 002 4— 1 +0. 013 +0. 027 — 0. 065 — 0. 076 4— 2 +0. 199 —0. 224 — 0. 344 + 0. 848 4— 3 —I. 622 +0. 029 + 4. 601 — 0. 928 4— 4 +2. 794 +2. 881 — 6. 912 — 7. 300 4— 5 —0. 083 +0. 308 + 0. 087 — 0. 768 4— 6 —0. 035 +0. 017 + 0. 058 — 0. 045 4— 7 +0. 005 +0. 001 — 0. 003 — 0. 003 5 —0. 001 +0. 008 — 0. 001 — 0. 001	3+ 1	-0.003	0, 000	+ 0.004	+ 0.001
3-2 -0.027 -1.038 +1.489 +4.058 3-3 -1.941 +2.882 +7.037 -10.183 3-4 -0.109 -0.069 +0.508 +0.008 3-5 -0.019 -0.033 +0.045 +0.052 3-6 -0.002 -0.001 +0.004 +0.002 4-0 -0.005 +0.001 +0.009 -0.002 4-1 +0.013 +0.027 -0.065 -0.065 -0.076 4-2 +0.199 -0.224 -0.344 +0.848 4-3 -1.622 +0.029 +4.601 -0.928 4-4 +2.794 +2.881 -6.912 -7.300 4-5 -0.083 +0.308 +0.087 -0.768 4-6 -0.035 +0.017 +0.058 -0.045 4-7 +0.005 +0.001 -0.003 -0.003 5 -0.001 +0.001 +0.002 -0.002 5-1 0.000 +0.008 -0.001 -0.001	3 0	o. o13	+0.021	+ 0.036	— o. o44
3-3 -1.941 +2.882 +7.037 -10.183 3-4 -0.109 -0.069 +0.508 +0.008 3-5 -0.019 -0.033 +0.045 +0.052 3-6 -0.002 -0.001 +0.004 +0.002 4 0 -0.005 +0.001 +0.009 -0.002 4-1 +0.013 +0.027 -0.065 -0.076 4-2 +0.199 -0.224 -0.344 +0.848 4-3 -1.622 +0.029 +4.601 -0.928 4-4 +2.794 +2.881 -6.912 -7.300 4-5 -0.083 +0.308 +0.087 -0.768 4-6 -0.035 +0.017 +0.058 -0.045 4-7 +0.005 +0.001 -0.003 -0.003 5 0 -0.001 +0.001 +0.002 -0.002 5-1 0.000 +0.008 -0.001 -0.001	3— 1	+o. 129	+0.097		— o. 146
3-4 -0. 109 -0. 069 + 0. 508 + 0. 008 3-5 -0. 019 -0. 033 + 0. 045 + 0. 052 3-6 -0. 002 -0. 001 + 0. 004 + 0. 002 4 0 -0. 005 + 0. 001 + 0. 009 - 0. 002 4-1 + 0. 013 + 0. 027 - 0. 065 - 0. 076 4-2 + 0. 199 - 0. 224 - 0. 344 + 0. 848 4-3 - 1. 622 + 0. 029 + 4. 601 - 0. 928 4-4 + 2. 794 + 2. 881 - 6. 912 - 7. 300 4-5 - 0. 083 + 0. 308 + 0. 087 - 0. 768 4-6 - 0. 035 + 0. 017 + 0. 058 - 0. 045 4-7 + 0. 005 + 0. 001 - 0. 003 - 0. 003 5 0 - 0. 001 + 0. 001 + 0. 002 - 0. 002 5-1 0. 000 + 0. 008 - 0. 001 - 0. 001	3— 2	o. o27		+ 1.489	
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	3— 3 `	-1.941			
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	3— 4	—o. 109			1
$\begin{array}{cccccccccccccccccccccccccccccccccccc$		0. 019	-0.033		
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	3— 6	0, 002	-0.001	+ 0.004	+ 0.002
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	4 0	—o. oo5	+0.001	+ 0.009	- 0.002
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	4— I	+o. o13	+0.027	0. 065	— o. o76
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	4— 2	+o. 199	-0. 224	— 0. 344	+ 0.848
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	4 3	-1.622	+0.029	+ 4.601	- o. 928
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	4— 4		+2.881	- 6.912	- 7.300
4-7 +0.005 +0.001 -0.003 -0.003 5 0 -0.001 +0.001 +0.002 -0.002 5-1 0.000 +0.008 -0.001 -0.017	4 5	-o. o83	+0.308		— o. 768
5 0 —0.001 +0.001 + 0.002 — 0.002 5— 1 0.000 +0.008 — 0.001 — 0.017	4— 6	-o. o35	+0.017	+ 0.058	
5— 1 0.000 +0.008 — 0.001 — 0.017	4 7	+0.005	+0.001	o. oo3	0.003
5— 1 0.000 +0.008 — 0.001 — 0.017	5 0	-0.001	+0.001	+ 0.002	0.002
	5— I	0.000	+0.008	- 0.001	0.017
5- 2 +0.063 -0.009 -0.143 + 0.075	5— 2	+0.063	0. 009	— o. 143	+ 0.075
5-3 -0.335 -0.329 + 0.996 + 0.577	5 — 3	—о. 335	-o. 3 2 9	+ 0.996	+ 0.577

Arg=i'a'+ia	$a_0 \left(r rac{d}{dr} ight)^3 \Omega$		$rac{a_0'}{\mu'}\Big(r'_{ar{d}}$	$\binom{d}{r'}^3\Omega'$
	cos.	sin.	cos.	sin.
i' i				-
5— 4	—0. 14 6	+2.011	—о. 167	-4. 613
5— 5	+3. 176	1. 994	—6. 566	+4.000
5— 6	+0. 403	+0. 153	-o. 814	0. 234
5— 7	—o. o28	+0.047	+0.003	-o. o74
5— 8	o, oo6	+0.019	+0.005	0.023
6 1	0. 003	0. 000	+0.003	0, 000
6 2	+0.011	+0.005	—o. o27	-0. 004
6— 3	—o. o15	—o. 105	+0.086	+0. 216
6— 4	— 0. 463	+0.418	+o. 8o3	—1.0 2 6
6 5	+2.096	+0.446	4. 150	—о. 583
6— 6	-1.044	—2. 925	+1.808	+5. 294
6— 7	+0. 22 6	—о. 398	— 0. 359	+0.713
6— 8	+0.060	+0.003	—o. o88	+0.014
6— 9	+0.015	+0.013	0, 018	—о. 013
7— 2	+0.001	0, 000	0.003	0.002
7-3	+0.013	o. o18	-O, OI 2	+0.041
7— 4	0. 152	+0.001	+o. 284	0. 064
7— 5	+0.435	+0.577	—o. 925	-o. 972
7— 6	+0.728	-1. 902	1. 127	+3.383
7— 7	2. 358	+0. 285	+3.884	-o. 415
7— 8	—о. 318	—0. 266	+o. 531	+0.415
7 9	+0.006	o. o57	+0. ∞3	+0. 086
8— 3	0, 001	0, 002	0,000	+0.005
8 4	-0.024	-0.018	+0.050	+0. 024
8 5	0.017	+0. 195	0. 023	о. 336
8 — 6	+o. 658	—o. 374	—1. 060	∔ 0. 725
8— 7	—I. 52 4	-0.901	+2. 502	+1.390
8 8	-0. 145	+1.673	+o. 283	—2. 582
8— 9	—0. 323	+0. 225	+0.459	0. 353
9— 4	0.005	0. 006	+0.009	+0.009
9— 5	0, 029	+0.047	+0.039	o. o76
9— 6	+0. 294	+0.042	0. 434	-0.023
9 7	—o. 293	0. 954	+0.511	+1.324
9— 8	1. 498	+1.357	+1.968	—1. 948
9 — 9	+1.523	+0.921	-2. 023	1. 126

In the next place we obtain the expression of Y:

Ana-10, 18/4/ 184	: Y	7	Angeres I ilal Lia	Y	
$Arg = \varkappa \gamma + i'g' + ig$	sin.	cos.	$Arg = \varkappa \gamma + i'g' + ig$	sin.	cos.
χ i' i	"	,, + 0. 29	χ i' i I 2 2	— 1.83	 — 1.77
I 0 I	+42. 30	— o. 13	0 2— 3	+ 0.97	- o. 42
_I 0 0	+ 4.11	- 3.93	I 2— 4	— o. 65	— 0. 14
0 0— 1	- 3.07	— 0. O2	_1 2— 3	o. 25	o. 16
I 0— 2	- o. 32	+ 2.57	0 2—4	+ 0.05	+ 0.02
-ı o- ı	+ 0.20	+ 0.41	1 2-5	0.00	+ 0.01
0 0-2	+ 0.02	- 0. 19	—1 2— 4	0.00	o. oı
I 0— 3	— o. 14	— 0. 04	0 2— 5	0.00	0.00
—I 0— 2	- 0.02	+ 0.01	ı 2— 6	0.00	+ 0.01
0 0-3	+ 0.01	+ 0.01			·
1 0-4	+ 0.01	- 0.01	-ı 3+ ı	+ 0.01	+ 0.09
			0 3 0	+ 0.15	— o. o3
-I I+ 3	+ 0.02	— o. oı	1 3— 1	— o. o6	— o. 13
0 I+ 2	— o. oı	- 0.04	-ı 3 o	— 2. 04	+ 0.30
1 1+1	+ 0.01	+ 0.05	o 3— 1	— o. 81	+ 1.45
—I I+ 2	+ 0.22	+ 0.26	I 3 2	+ 1.08	+ 0.10
0 1+1	+ 0.36	— O. 24	—I 3— I	+11.27	-19. 84
I I O	— o. 71	— o. 17	o 3— 2	— 3⋅53	— 4. 98
-1 1+1	- 5.05	+ 3.33	I 3— 3	— 2. 34	+ 3.94
0 1 0	+ 0.64	+ 3.00	—I 3— 2	+47⋅54	+68. 68
1 I— 1	+ 4.79	- 4· 5 ²	o 3— 3	O. I2	— o. 19
I I O	— 8. 13	-41. 32	I 3— 4	— 4.93	— 6. 64
0 I — I	- 0.44	+ 0.10	— I 3— 3	+ 3.97	1.27
I I 2	+ 5.15	+24.23	0 3—4	+ 0.34	+ 0.50
—I I— I	+ 1.23	+ 3.13	I 3— 5	— O. 22	— O. 44
5 1- 2	o. 35	— I. 77	—I 3— 4	+ 0.17	- 0. 29
1 I— 3	- 0.98	+ o. 58	o 3— §	+ 0.01	+ 0.03
—ı I— 2	- 0. 20	+ 0. 22	ı 3— 6	— O. O2	o. oı
o 1— 3	+ 0.08	— o. o5	I 4 0	0. 24	+ 0. 17
I I— 4	+ 0.01	o. o4	0 4 1	+ 0.03	+ 0.30
—I I— 3	— o. oɪ	— o. oı	I 4— 2	+ 0.16	— o. o9
o I— 4	0.00	+ 0.02	—I 4— I	- 0.48	 4.03
1 1-5	+ 0.01	- 0.01	0 4— 2	— 1.87	- 0. 69
—I 2+ 2	+ 0.04	+ 0.01	I 4— 3	+ 0.07	+ 1.01
o 2+ 1	+ 0.03	o. o6	—I 4— 2	+25.61	+ 9.49
1 2 0	- 0.09	+ 0.02	0 4— 3	+ 3.28	— 3· 57
-1 2+ I	- o. 32	+ 0.76	I 4— 4	— 3. I2	— 1. 16
0 2 0	+ 0.75	+ 0.35	—I 4— 3	-45· 37 + 0.13	+48. oi
I 2 I	+ 0. 19	— o. 96	0 4-4 1 4-5	+ 3.07	0. 27 3· 54
_I 2 0	-10. 24	4.81	I 4— 5 —I 4— 4	+ 3.07	+ 4.85
o 2— I	— 6. 12	+ 2.66	0 4— 5	- 0. 23	+ 0. 24
I 2 2	+ 4.49	+ 3.75	1 4-6	+ 0. 24	0.31
I 2 I	+84.45	—35. 8 ₅	—I 4— 5	+ 0.35	+ 0.19
0 2— 2	— 0. 20	— o. 15	0 4-6	- 0.01	+ 0.02
1 2— 3	—I 3. I7	+ 5.88	I 4-7	+ 0.01	- o. o3
	, , , , , , , , , , , , , , , , , , ,		1	<u> </u>	

	Y			Y	
$Arg = \varkappa \gamma + i'g' + ig'$	sin.	208.	$Arg = \varkappa \gamma + i'g' + ig$	sin.	cos.
н i' i	"	"	и i' i	"	"
-r 5- o	0.01	+ 0.04	—ı 6— 8	— o. o3	0.00
0 5— 1	+ 0.03	+ 0.04	0 6— 9	0.00	+ 0.01
I 5 2	+ 0.01	0. 02	I 6-10	— o. oı	o. oı
—ı 5— ı	— o. 41	- 0.47			
0 5— 2	- o. 43	+ 0.11	-I 7— 2	+ 0.01	— o. 16
I 5— 3	+ 0. 12	+ 0.15	0 7-3	o. o9	— o, o5
—I 5— 2	+ 5.61	— I. 47	1 7—4	- 0.01	+ 0.03
o 5— 3	+ 0.35	— I.96	—I 7— 3	+ 1.16	+ 0.73
I 5 4	— o. 83	+ 0.19	0 7—4	+ 0.43	— o. 29
—ı 5— 3	4.78	+26.74	1 7-5	- 0. 14	— 0. IO
0 5— 4	+ 3.04	+ 1.79	—I 7— 4	— 5. 8 ₅	+ 3.86
1 5 5	+ 0.38	— 2, 26	0 7— 5	+ 0.30	+ 1.40
—I 5— 4	40. 99	—24. 83	1 7— 6	+ 0.45	0.28
0 5 5	+ 0.32	+ 0.01	-1 7— 5	4. 16	18.98
ı 5— 6	+ 2.32	+ 1.22	0 7—6	— I. 58	0. 14
—I 5— 5	— 4.62	+ 1.93	1 7— 7	0.00	+ 0.94
o 5— 6	— o. 15	— o. 11	-1 7— 6	+21.27	+ 2.17
1 5— 7	+ 0.26	+ 0.09	0 7— 7	— 0. 20	+ 0.10
—ı 5— 6	— O. 19	+ 0.39	ı 7 8	- 0.80	— o. oı
o 5— 7	0.03	0.00	-I 7-7	+ 2.61	— 2. 34
ı 5— 8	+ 0.02	0.00	0 7—8	+ 0.06	+ 0.04
—r 5— 7	+ 0.01	+ 0.04	1 7— 9	— 0. I2	+ 0.06
o 5— 8	+ 0.01	0,00		+ 0.06	- o. 37
1 5— 9	0.00	0.02	o 7— 9 1 7—10	+ 0.01	0.00 + 0.02
—ı 6— ı	o. o8	— o. o3	1 7—10	- 0.01	+ 0.02
o 6— 2	— o. o5	+ 0.06	8 2	0.00	o. o2
ı 6— з	+ 0.03	0.00	0 8— 3	0.02	0.00
—ı 6— 2	+ 0.66	— o. 77	1 8-4	0.00	0.00
0 6 3	— 0. 20	- o. 45	1 8-3	+ 0.22	+ 0.01
1 6-4	— o. 13	+ 0.14	0 8-4	+ 0.04	o. II
_r 6— 3	+ 2.72	+ 6.25	ı 8— 5	0.03	0.00
0 6-4	+ 1.74	0.03	—ı 8— 4	— o. 64	+ 1.44
ı 6— 5	- 0. 26		o 8 5	+ 0.33	+ 0.34
1 6 4		— o. 64	1 8— 6	+ 0.05	o. 11
	—23. 94	+ 0.30	—ı 8— 5	— 4.52	- 4.7I
0 6 5	— o. 75	+ 2.29	o 8— 6	- o. 97	+ 0.44
ı 6 6	+ 1.52	- 0.04	ı 8 7	+ 0.30	+ 0.26
—r 6— 5	+10.51	−31.00	_r 8_ 6	+13.57	5.95
0 6—6	+ 0.06	+ 0.28	o 8— 7	— o. 14	— o. 98
ı 6 7	— o. 35	+ 1.41	ı 8 8	— o. 55	+ 0.27
— 1 6— 6	— 2. 29	— 3. 7o	—ı 8— 7	+ 1.73	-+13.38
o 6— 7	+ 0.05	— O. 12	o 8— 8	— O. I2	 0. 14
ı 6—8	0, 00	+ 0. 18	1 8— 9	o. 10	o.4I
—ı 6— 7	— o. 39	— o. 13	_1 8—8	+ 2.07	+ 1.60
□ 6—8	+ 0.01	o. oı	0 8-9	+ 0.01	+ 0.03
ı 6— 9	0.00	+ 0.02	1 8—10	- o. o2	— o. o7
			<u> </u>		

$ ext{Arg} = \kappa \gamma + i' g' + i g$	Y		A		. у	
	sin.	608.	$Arg = \varkappa \gamma + i'g' + ig$	sin.	cos.	
ν i' i -1 9-3 0 9-4 1 9-5 -1 9-4 0 9-5 1 9-6 -1 9-5 0 9-6 1 9-7	" +0.030.010.01 +0.03 +0.110.011.600.24 +0.11	" -0.02 -0.02 0.00 +0.31 +0.02 -0.03 -0.41 +0.33 +0.02	π1 0 11 0 11 0 1	i' i 9-6 9-7 9-8 9-9 9-8 9-9 9-10	+3. 24 -0. 06 -0. 13 +6. 27 +0. 57 -0. 23 -7. 76 -0. 51 +0. 17	

In like manner we have the expression of Y':

Y'				Υ'	
A / 1 #/-/ 1 #-	Υ'		A ==== = (Υ'	
$Arg = \varkappa \gamma' + i'g' + ig$	sin.	cos.	$Arg = \varkappa \gamma' + i'g' + ig$	sin.	cos.
π i' i 0 0 0 -I I 0 -I 2 0 0 I 0 I 0 0 -I 3 0 0 2 0 I I 0 -I 4 0 0 3 0 I 2 0 -I 5 0 0 4 0 I 3 0 -I I I I 0 - I I I 1 0 - I I 1 - I I I 1 - I	sin. // -433.8 -120.3 + 73.0 + 33.7 - 6.0 + 10.3 - 0.6 + 1.2 + 0.5 - 0.5 + 0.4 - 0.1 - 0.1 + 0.5 + 0.6 - 1.2 + 4.5 + 2.0 - 7.6	+ 4.6 - 5.8 + 101.6 + 1.1 - 54.4 + 23.2 - 8.6 - 8.0 + 3.1 - 2.0 - 0.7 + 0.3 - 0.3 - 0.0 + 0.2 - 0.5 + 0.1 - 0.7 - 5.3 + 5.4	κ i' i —I 4— I 0 3— I 1 2— I —I 5— I 0 4— I I 3— I —I 6— I 0 5— I I 4— I —I 0— 2 —I 2 I —2 2 —I 1— 2 —I 2— 2 —I 2— 2 —I 2— 2 —I 3— 2 —I 3— 2 —I 3— 2 —I 3— 2 —I 3— 2 —I 3— 2 —I 3— 2	sin. - 45.4 + 16.1 + 10.7 - 6.1 + 3.8 + 1.1 - 0.4 + 0.5 + 0.1 - 0.0 + 0.3 - 0.2 + 1.3 + 4.7 - 3.4 - 24.1 + 21.5 - 55.1 + 865.8 + 4.7	- 3.9 + I4.4 - 0.1 + 3.5 + 0.2 - 0.8 + 0.8 - 0.3 - 0.2 + 0.2 + 0.1 - 0.3 + 2.6 + I0.4 - 1.9 + I6.1 - 9.7 - 122.3 - 365.0 - 6.2
-I I- I 0 0- I I- I- I -I 2- I 0 I- I I 0- I -I 3- I 0 2- I I I- I	+ 37.5 + 14.3 - 25.0 - 200.0 - 8.2 - 171.9 - 192.3 + 16.1 + 60.9	- 6.2 + 69.9 + 63.3 -1012.4 - 3.1 - 827.9 - 169.7 + 85.4 + 42.2	I I— 2 —I 4— 2 — 3— 2 I 2— 2 —I 5— 2 — 4— 2 I 3— 2 —I 6— 2	- 4.7 -255.3 +163.7 - 73.1 - 31.0 - 3.1 - 13.8 + 1.7 - 7.0	+ 112.6 -260.1 + 29.8 + 57.9 - 65.3 + 21.8 + 11.5 - 9.1

$Arg = \kappa \gamma + i'g' + ig$	Y'			Y'	
	sin.	cos.	$Arg = \mathcal{H} \gamma' + \mathbf{i}'g' + \mathbf{i}g$	sin.	008.
Arg=xy+i'g'+ig	+ 0.3 + 1.2 - 1.7 + 0.6 + 0.3 - 0.2 + 0.1 - 0.1 + 0.2 + 0.1 - 2.2 + 0.3 - 1.8 - 4.9 + 8.1 - 8.6 +424.0 + 4.5 - 95.1 +283.3 - 34.7	+ 5.5 + 1.2 - 0.6 + 0.7 + 0.1 0.0 0.0 - 0.1 + 0.1 + 0.9 - 0.1 + 1.8 + 0.7 - 11.6 - 46.7 + 10.9 - 9.4 +610.3 + 5.2 -131.5 +114.2 - 51.8	x i' i 1 3-4 -1 6-4 0 5-4 1 4-4 -1 7-4 0 6-4 1 5-4 -1 8-4 0 7-4 1 6-4 -1 9-4 0 8-4 1 7-4 -1 10-4 0 9-4 1 8-4 -1 3-5 0 2-5 1 1-5 -1 4-5 0 3-5 1 2-5	sin. + 62.0 - 51.9 + 31.4 + 5.6 + 28.8 + 4.6 - 4.2 + 14.5 - 2.4 - 1.7 + 3.5 - 1.2 - 0.8 + 0.5 - 0.2 - 0.1 - 0.1 - 0.1 - 0.1 + 3.0 - 0.5 - 0.2	- 69. 5 +264. 4 - 32. 4 - 37. 1 + 73. 3 - 22. 3 - 8. 6 + 10. 4 - 6. 1 - 1. 0 + 0. 1 - 0. 8 - 0. 1 - 0. 3 0. 0 + 0. 1 - 0. 0 + 0. 1 - 0. 0 + 0. 1 - 0. 1 - 0. 0 + 0. 0 + 0
I 3—3 —I 6—3 —I 6—3 —I 7—3 —I 7—3 —I 8—3 —I 8—3 —I 8—3 —I 9—3 —I 9—3 —I 9—3 —I 2—4 —I 3—4 —I 3—4 —I 3—4 —I 4—4 —I 4—4 —I 4—4 —I 4—4 —I 4—4 —I 4—4 —I 5—4 —I 5—4 —I 5—4 —I 5—4 —I 5—4	- 48.9 + 75.2 - 23.7 - 10.5 + 10.8 - 6.3 - 1.3 + 0.5 - 1.0 - 0.1 - 0.2 0.0 0.0 - 0.1 - 0.1 - 2.3 + 0.5 + 57.0 - 5.0 + 57.0 - 5.3	- 16.6 - 15.7 - 9.9 + 3.1 - 10.9 + 1.3 + 1.6 - 2.5 + 1.0 + 0.3 - 0.4 + 0.2 0.0 + 0.1 - 0.8 - 2.6 + 0.6 - 0.1 - 5.2 + 6.0 - 7.4 +393.9 + 3.5	-I 5-5 0 4-5 I 3-5 -I 6-5 0 5-5 I 4-5 -I 7-5 0 6-5 I 5-5 -I 8-5 0 7-5 I 6-5 -I 9-5 0 8-5 I 7-5 -I 10-5 0 9-5 I 8-5 -I 4-6 0 3-6 I 2-6 -I 5-6 0 4-6 I 3-6	+ 10.8 - 4.1 + 4.1 -317.3 - 3.1 + 46.3 -218.5 + 26.2 + 25.8 - 62.1 + 18.3 + 6.1 - 8.0 + 5.2 + 0.7 + 0.5 + 0.7 - 0.1 + 0.1 - 0.0 + 3.7 - 0.4 + 0.1	+ 55.4 - 1.9 - 3.3 -186.9 - 4.6 + 25.6 + 0.6 + 16.1 - 1.1 + 38.6 + 0.2 - 4.4 + 16.6 - 3.2 - 1.6 + 3.9 - 1.3 - 0.4 - 0.2 0.0 - 0.0 - 0.2 - 0.1

Argentol Lila Lia	Y'		A	3	7'
$\mathbf{Arg} = \varkappa \gamma' + i'g' + ig$	sin.	cos.	$Arg = \kappa \gamma' + i'g' + ig$	sin.	cos.
κ i' i -1 6-6 0 5-6 1 4-6 -1 7-6 0 6-6 1 5-6 -1 8-6 0 7-6 1 6-6 -1 9-6 0 8-6 1 7-6 -1 10-6 0 9-6 1 8-6 -1 5-7 0 4-7 1 3-7 -1 6-7 0 5-7 1 4-7 -1 7-7 0 6-7 1 5-7 -1 8-7	sin. - 46.3 + 0.3 + 3.8 + 73.2 + 3.6 - 8.1 - 35.1 - 6.7 + 2.9 - 42.9 + 4.4 - 17.2 + 3.6 + 1.4 + 0.3 - 0.0 + 0.1 - 2.4 - 0.0 + 0.2 - 19.4 + 1.6 - 0.2 + 151.1 + 2.6	1008. 11	# i' i -1 10-7 9-7 1 8-7 -1 6-8 0 5-8 1 4-8 -1 7-8 0 6-8 1 5-8 -1 8-8 1 6-8 -1 9-8 1 6-8 -1 9-8 1 8-8 -1 10-8 9-8 1 8-8 -1 7-9 1 6-9 1 6-9 -1 9-9 8-9	sin. +30. 2 - 9. 3 - 2. 3 0. 0 + 0. 1 0. 0 - 3. 9 + 0. 2 + 0. 2 + 22. 5 + 0. 4 - 2. 1 + 14. 9 - 1. 6 - 1. 6 + 51. 1 - 1. 2 - 3. 8 - 0. 4 - 0. 1 + 0. 7 + 0. 2 + 0. 2 + 16. 6 - 0. 4	
1 6— 7 —1 9— 7 0 8— 7	- 16.4 +111.0	- 0.7 - 49.0	1 7— 9 —1 10— 9	0.8 52.4	- 1.3 +23.7
1 7— 7	- 12.5 - 9.9	- 1.2 + 5.0	1 8— 9	- 1.5 + 4.0	- I. o - I. 3

The developments of the three factors, which must be specially computed for $\delta^2 T$, follow:

$\mathbf{Arg} = \varkappa \gamma + i'g' + ig$	$r^2rac{d^2\Gamma}{dr^2}$		$rr'rac{d^{2}\Gamma}{drdr'}$		$r'^2rac{d^2\mathbf{T}}{dr'^2}$	
	sin.	CONT	sin.	cos.	sin.	coa.
и i' i	,,,	" +0.46	"	— o. 35	"	"
1 -0 1	+216.02	-0.46	—131. 94 — 13 88	+ 0.53 -16.22	-37.81	0.54
0 0 1	- 5.4I + 3.0I	+5.60 -7.78	+ 13.88	+11.86	-29.36 +19.36	+32.28 -16.93
I 0 2	+ 0.95	+2.74	— 2.6o	+ 2.06	+ 3.58	— 9. <u>59</u>

$Arg = \nu \gamma + i'g' + ig$	$r^2 \frac{d}{d}$	12T dr ²	rr' d	$rac{d^2 ext{T}}{dr dr'}$	gn/S	$rac{d^2 \Gamma}{dr'^2}$
	sin.	608:	sin.	cos.	sin.	cos.
 κ i' i -I 0- I 0 0- 2 I 0- 3 -I 0- 2 0 0- 3 I 0- 4 -I I+ 3 	- 0.56 + 0.87 - 0.10 + 0.11 - 0.11 + 0.07	" - 1.49 + 1.06 + 0.02 - 0.09 + 0.09 + 0.05	+ 1.19 - 1.20 - 0.13 - 0.19 + 0.16 - 0.06 + 0.01	+ 2.57 - 1.65 - 0.14 + 0.12 - 0.10 - 0.06	2.07 + 1.67 + 0.40 + 0.28 0.21 + 0.04	- 4. 12 + 2. 51 + 0. 23 - 0. 17 + 0. 12 + 0. 07
0 I+ 2 I I+ I -I I+ 2 0 I+ I I I 0 -I I+ I 0 I 0	- 0.02 0.00 - 0.16 - 0.90 + 1.33 - 7.49 + 0.96	+ 0.13 - 0.31 + 0.07 - 0.70 + 0.45 + 4.47 + 4.43	+ 0.03 - 0.01 + 0.78 + 1.68 - 3.02 - 3.01 - 0.80	- 0.23 + 0.45 + 0.38 + 0.75 - 1.13 + 4.96 - 3.79	- 0.04 + 0.02 - 1.52 - 3.09 + 5.66 + 22.00	+ 0.35 - 0.66 - 1.10 - 0.63 + 2.06 - 19.12
I I— I —I I O O I— I I I— 2 —I I— I O I— 2 I I— 3	+ 6.58 - 19.95 - 15.45 + 35.53 - 11.34 + 6.91 + 2.16	- 8.66 - 96.21 - 73.41 +170.25 - 10.15 + 4.65 + 3.25	+ 4.21 - 1.75 + 25.07 - 27.45 + 15.46 - 6.51 - 5.22	+ 0.55 - 12.11 +124.14 -132.20 + 17.80 - 10.31 - 1.99	- 23. 30 + 36. 97 - 37. 07 + 12. 68 - 17. 57 + 5. 01 + 9. 60	+ 12.98 +190.20 -189.36 + 63.22 - 31.29 + 19.46 - 0.68
-I I-2 0 I-3 I I-4 -I I-3 0 I-4 I I-5	+ I. 02 - 0. 77 + 0. 14 0. 00 - 0. 10 + 0. 11 - 0. 20	- 0.98 + 1.07 + 0.01 + 0.07 0.00 0.00 + 0.17	- 1.62 + 1.32 - 0.25 - 0.05 + 0.14 - 0.10	+ 1.67 - 1.71 + 0.03 - 0.10 + 0.02 - 0.01	+ 2.49 - 2.09 + 0.44 + 0.10 - 0.19 + 0.10	- 2.67 + 2.55 - 0.13 + 0.13 - 0.02 + 0.01
0 2+ I I 2 0 -I 2+ I 0 2 0 I 2- I -I 2 0	- 0.14 + 0.40 - 0.60 + 1.03 - 0.36 + 3.54	- 0. 17 - 0. 03 - 0. 21 - 0. 34 + 0. 58 - 0. 20 - 7. 26	+ 0.32 + 0.22 - 0.63 + 0.24 - 0.98 + 1.41 - 33.38	- 0.16 - 0.02 + 0.23 + 2.41 - 0.41 - 1.88 - 4.40	- 0.45 - 0.36 + 0.99 + 0.63 - 3.17 + 85.91	+ 0. 14 + 0. 12 - 0. 28 - 5. 40 + 5. 14 + 20. 53
0 2— I I 2— 2 —I 2— I 0 2— 2 I 2— 3 —I 2 2	- 28.62 + 23.91 - 25.48 + 186.78 - 142.94 + 9.77	- 4.87 + 13.31 + 9.13 - 79.19 + 61.66 - 7.13	+ 48.86 - 25.23 +251.14 -398.87 +181.31 - 14.07	+ 6.66 - 2.98 -104.85 +169.60 - 77.64 + 1.45	- 66. 99 + 26. 11 -703. 79 +701. 32 -234. 17 + 19. 13	- 12. 18 - 13. 87 +297. 96 -298. 81 + 99. 53 + 11. 32
0 2-3 1 2-4 -I 2-3 0 2-4 I 2-5	- 1. 27 - 4. 22 + 1. 25 - 1. 33 + 0. 09	- 4.48 + 7.69 + 0.36 - 0.96 + 0.64	- 3.03 + 6.63 - 2.02 + 1.65 - 0.03	+ 15.30 - 12.83 - 0.90 + 1.96 - 1.05	+ 10. 18 - 10. 22 + 3. 08 - 1. 93 - 0. 10	30. 64 + 19. 84 + 1. 79 3. 34 + 1. 64

$Arg = \mu \gamma + i'g' + ig$	$r^2rac{d}{d}$	*T	ry'-	$d^2 T \over dr dr'$	90/9	$rac{d^2 \Gamma}{dr'^2}$
	sin.	cos.	sin.	cos.	sin.	cos.
и i' i —1 2— 4 0 2— 5 1 2— 6	+ 0. 25 - 0. 04 - 0. 24	+ 0.06 - 0.08 + 0.02	0.25 + 0.06 + 0.24	- 0.09 + 0.16 - 0.05	+ 0. 28 - 0. 08 - 0. 24	+ 0. 14 - 0. 26 + 0. 08
-I 3+ 2 0 3+ I I 3 0 -I 3+ I	- 0. 10 - 0. 02 + 0. 11 - 0. 21	- 0.04 + 0.02 + 0.01 - 0.47	+ 0.10 + 0.02 - 0.13 + 0.32	+ 0.04 - 0.02 + 0.01 + 0.72	- 0.11 - 0.03 + 0.15 - 0.44	- 0.03 + 0.03 - 0.03 - 1.09
0 3 0 I 3— I —I 3 0 0 3— I I 3— 2	+ 0.21 - 0.01 + 1.94 - 5.00 + 2.89	- 0.04 + 0.50 - 2.24 + 3.62 - 1.55	- 0. 19 - 0. 01 - 7. 74 + 8. 58 - 2. 09	+ 0.04 - 0.84 + 3.78 - 5.05 + 3.60	+ 0.02 + 17.67 - 12.08 + 0.86	+ 1.37 - 6.51 + 5.34 - 6.59
-I 3- I 0 3- 2 I 3- 3 -I 3- 2 0 3- 3	+ 2.87 + 12.96 - 12.33 - 81.31 +170.11	+ 29. 16 - 68. 50 + 39. 74 - 122. 95 + 246. 40	+ 23.87 - 39.23 + 11.88 +226.15 -299.38	- 88. 52 +116. 27 - 50. 83 +332. 17 -429. 37	- 83. 24 + 82. 22 - 11. 83 -465. 38 +467. 82	+190. 18 -174. 71 + 64. 69 -675. 68 +666. 44
I 3-4 -I 3-3 0 3-4 I 3-5	- 85.07 - 3.27 + 21.21 - 13.53	-120.85 + 8.82 + 0.62 - 3.74	+115.71 + 16.85 - 39.24 + 20.36	+164. 38 11. 97 5. 00 +- 5. 98	—154. 50 — 39. 13 + 62. 48 — 29. 04	219. 21 + 15. 20 + 11. 34 8. 99
-I 3-4 0 3-5 I 3-6 -I 3-5 0 3-6	- 0.53 + 1.69 - 0.85 - 0.08 + 0.08	+ 1.74 - 1.83 + 0.25 + 0.05 - 0.13	+ 1.21 - 3.12 + 1.47 + 0.11 - 0.19	- 2.70 + 2.37 0.32 - 0.10 + 0.20	- 2.30 + 4.98 - 2.28 - 0.16 + 0.32	+ 3.98 - 2.93 + 0.36 + 0.17 - 0.28
I 3— 7 —I 4 0 0 4— I I 4— 2 —I 4— I	0.00 + 0.26 - 0.28 - 0.11 + 6.40	+ 0.11 - 0.56 + 1.04 - 0.56 + 6.66	+ 0.04 - 0.89 + 0.66 + 0.44 - 9.55	- 0.11 + 1.20 - 1.40 + 0.74 - 18.63	- 0. 10 + 1. 97 - 1. 14 - 0. 89 + 11. 69	+ 0.11 - 2.22 + 1.58 - 1.00 + 38.70
0 4— 2 I 4— 3 —I 4— 2 0 4— 3 I 4— 4	- 9.02 + 4.36 - 67.54 +114.79 - 53.17	- 13. 25 + 6. 33 - 2. 47 + 15. 00 - 7. 01	+ 10. 13 - 6. 48 +149. 09 -181. 43 + 70. 89	+ 22.55 - 7.50 + 28.01 - 40.08 + 8.60	-8.98 $+8.99$ -274.98 $+262.95$ -92.45	- 33.96 + 8.90 - 75.63 + 77.15 - 11.07
-I 4-3 0 4-4 I 4-5 -I 4-4	+149.90 226.88 + 91.46 9.71	—152. 38 +239. 96 98. 39 — 14. 64	-297. 70 +350. 01 -123. 79 + 14. 04	+308.83 -374.56 +133.83 + 31.84	+514. 56 -500. 86 +162. 62 - 19. 24	-540. 04 +540. 59 -176. 63 - 57. 03 + 80. 98
o 4— 5 r 4— 6 —r 4— 5 o 4— 6 r 4— 7	+ 2.92 + 1.09 - 2.13 + 2.77 - 0.88	+ 35·33 - 17·18 - 0·44 + 2·40 - 1·36	- 1.80 - 2.02 + 3.33 - 3.66 + 1.11	- 55.84 + 24.54 + 1.22 - 4.00 + 2.05	0.00 + 3.27 - 4.91 + 4.68 - 1.37	+ 80.98 - 33.45 - 2.40 + 5.99 - 2.92

25 AST-23

$Arg = \kappa \gamma + i'g' + ig$	$r^2rac{\dot{d}}{\dot{d}}$	$rac{d^2 ext{T}}{dr^3}$	rr' d	$rac{d^{2} ext{T}}{drdr'}$	$r'^2 rac{d}{d}$	² T _{r^{/2}}
	sin.	cos.	sin.	cos.	sin.	608.
π i' i -1 4-6 0 4-7 1 4-8 -1 5 0 0 5-1 1 5-2 -1 5-1 0 5-2 1 5-3 -1 5-2 0 5-3	+ 0.15 - 0.02 - 0.32 + 0.03 + 0.06 - 0.12 + 1.99 - 2.90 + 1.27 - 14.44 + 23.73	- 0.06 - 0.04 - 0.16 - 0.20 + 0.16 + 0.07 + 0.30 - 0.80 + 0.12 + 12.90 - 17.02	- 0.07 - 0.08 + 0.36 - 0.05 - 0.03 + 0.17 - 3.54 + 3.77 - 1.68 + 32.11 - 38.11	+ 0.09 - 0.07 + 0.20 + 0.33 - 0.21 - 0.07 - 1.57 + 1.87 + 0.04 - 19.22 + 20.42	- 0.03 + 0.20 - 0.41 + 0.10 - 0.03 - 0.25 + 5.53 - 4.40 + 2.17 - 59.36 + 55.83	" - 0. 15 + 0. 20 - 0. 25 - 0. 51 + 0. 24 + 0. 09 + 3. 82 - 3. 33 - 0. 29 + 26. 05 - 22. 39
I 5-4 -I 5-3 0 5-4 I 5-5 -I 5-4 0 5-5 I 5-6 -I 5-5 0 5-6 I 5-7 -I 5-6 0 5-7 I 5-8 -I 5-9	- 9.72 - 2.88 - 1.92 - 1.59 +190.17 -263.84 + 98.32 + 21.64 - 41.86 + 18.21 - 0.92 - 2.89 + 3.07 - 0.28 - 0.02 + 0.26	+ 7.98 -103.08 +150.54 - 60.95 +121.17 -159.18 + 57.77 - 13.33 + 10.55 - 2.55 - 2.77 + 3.69 - 1.14 - 0.77 + 0.55 + 0.19	+ 12.65 - 10.00 + 15.35 + 1.57 -329.26 +380.46 -130.66 - 38.42 + 60.77 - 24.88 + 0.15 + 4.34 - 3.69 + 0.29 + 0.11 - 0.32	- 10.72 +191.92 -223.01 + 81.13 -205.25 +225.99 - 76.16 + 19.72 - 13.37 + 3.07 + 4.17 - 4.93 + 1.54 + 0.89 - 0.69 - 0.17	- 16. 20 + 33. 07 - 35. 05 - 1. 17 + 520. 72 - 519. 19 + 168. 54 + 61. 40 - 83. 19 + 32. 72 + 0. 93 - 6. 09 + 4. 44 - 0. 30 - 0. 21 + 0. 38	+ 13. 86 -319. 08 +309. 81 -105. 01 +319. 87 -304. 80 + 97. 54 - 27. 81 + 16. 37 - 3. 62 - 5. 94 + 6. 34 - 2. 00 - 1. 05 + 0. 85 + 0. 13
-I 6- I 0 6- 2 I 6- 3 -I 6- 2 0 6- 3 I 6- 4 -I 6- 3 0 6- 4 I 6- 5 -I 6- 4 0 6- 5 I 6- 6 -I 6- 5 0 6- 6 I 6- 7 -I 6- 6 0 6- 7 I 6- 8	+ 0.36 - 0.46 + 0.12 - 0.90 + 1.48 + 0.02 - 21.36 + 27.31 - 12.14 + 122.64 - 163.95 + 61.07 - 69.52 + 81.42 - 27.54 + 17.44 - 18.67 + 6.07	- 0. 15 + 0. 19 - 0. 17 + 4. 22 - 5. 72 + 2. 45 - 22. 37 + 32. 50 - 11. 79 - 19. 71 + 22. 95 - 11. 58 + 189. 75 - 244. 11 + 86. 15 + 23. 11 - 40. 32 + 16. 57	- 0.65 + 0.64 - 0.15 + 2.82 - 3.22 - 0.03 + 31.77 - 34.13 + 15.66 -204.58 +230.39 - 79.93 +105.96 -108.35 + 35.13 - 25.41 + 24.19 - 7.65	+ 0.11 - 0.23 - 7.02 + 7.56 - 3.18 + 42.83 - 49.39 + 15.65 + 22.65 - 23.57 + 14.42 - 297.82 + 332.83 - 111.51 - 36.86 + 55.29 - 21.85	+ 1.05 - 0.80 + 0.17 - 6.01 + 5.56	0.00 - 0.01 - 0.30 + 10.66 - 9.33 + 4.04 - 72.37 + 69.88 - 20.24 - 24.03 + 22.24 - 17.46 + 439.39 - 435.70 + 140.56 + 54.85 - 72.62 + 27.92

Arg=μγ+ i 'g'+ig	r² <u>đ</u>	$rac{r^2}{dr^2}$	$rr'rac{\dot{\phi}}{da}$	$rac{d^2\mathbf{T}}{rdr'}$	$r'^2rac{d^2}{dr}$	T
	sin.	cos.	sin.	cos.	sin.	608.
π i' i -1 6-7 - 6-8 -1 6-9 -1 6-8 - 6-9 -1 6-10	+ 3.51 - 4.58 + 1.34 + 0.62 - 0.54 - 0.14	" - 0.32 - 2.23 + 1.79 - 0.58 + 0.13 + 0.34			+ 6.79 - 7.62 + 2.40 + 0.90 - 0.88 + 0.01	+ 0.96 4.65 + 2.87 0.62 + 0.02 + 0.44
-I 7-2 0 7-3 I 7-4 -I 7-3 0 7-4 I 7-5 -I 7-4 0 7-5 I 7-6 -I 7-6 1 7-7 -I 7-6 0 7-7 I 7-8 -I 7-8 I 7-9 -I 7-8	+ 0.40 - 0.40 + 0.20 - 7.21 + 9.32 - 3.72 + 26.86 - 36.08 + 11.97 + 38.84 - 47.86 + 19.08 - 162.06 + 197.79 - 67.44 - 19.75 + 33.12 - 13.62 + 0.49	+ 0.72 - 0.92 + 0.24 - 0.89 + 1.89 - 0.21 - 30.38 + 38.18 - 16.05 + 121.90 - 153.55 + 53.95 - 21.37 + 18.97 - 5.55 + 20.23 - 24.40 + 8.84 + 3.61	- 0.40 + 0.32 - 0.29 + 11.34 - 12.23 + 4.79 - 46.53 + 52.37 - 15.79 - 54.75 + 60.27 - 25.35 + 237.62 - 258.58 + 85.12 + 29.58 - 43.60 + 17.31 - 0.22	- 1. 25 + 1. 30 - 0. 33 + 3. 10 - 3. 98 + 0. 28 + 44. 57 - 48. 31 + 20. 26 - 188. 25 + 206. 96 - 69. 25 + 28. 94 - 22. 68 + 6. 46 - 28. 61 + 31. 08 - 10. 86 - 5. 02	+ 0.32 - 0.15 + 0.41 - 16.68 + 15.29 - 6.00 + 73.55 - 71.80 + 20.26 + 74.00 - 73.27 + 32.02 - 333.04 + 327.73 - 105.05 - 42.02 + 55.51 - 21.46 - 0.15	+ 1.98 - 1.71 + 0.45 - 6.56 + 6.71 - 0.42 - 62.26 + 59.03 - 25.00 +274.58 -268.55 + 86.67 - 37.99 + 26.61 - 7.41 + 38.95 - 38.60 + 13.12 + 6.73
7-9 1 7-10 -1 8-3	+ 1.49 - 1.28	- 5. 19 + 1. 91 + 0. 73	- 2.18 + 1.61 + 2.05	+ 6.59 - 2.39 - 0.79	+ 2.97 - 1.96 - 3.12	- 8.16 + 2.93 + 0.78
0 8— 4 1 8— 5 -1 8— 4 0 8— 5 1 8— 6 -1 8— 5 0 8— 6 1 8— 7 -1 8— 6 0 8— 7 1 8— 8 -1 8— 7 0 8— 8 1 8— 9	+ 1.60 - 0.53 + 0.37 - 1.37 - 0.15 + 38.62 - 47.25 + 18.87 - 104.69 + 126.47 - 42.74 - 10.46 + 19.86 - 8.65	- 0.80 + 0.49 - 10.41 + 12.73 - 4.60 + 26.01 - 33.29 + 10.15 + 56.36 - 69.18 + 27.18 - 121.53 + 143.20 - 48.52	- 2.21 + 0.68 - 2.30 + 3.26 + 0.07 - 55.06 + 59.45 - 23.27 + 152.82 - 164.87 + 53.74 + 16.84 - 26.75 + 10.82	+ 0.76 - 0.61 + 15.57 - 16.54 + 5.94 - 42.11 + 46.64 - 13.30 - 78.30 + 86.30 - 33.39 + 169.68 - 181.20 + 59.69	+ 2.89 - 0.87 + 5.25 - 5.73 + 0.05 + 75.44 - 72.75 + 28.20 - 213.49 + 208.51 - 66.09 - 25.01 + 34.66 - 13.29	- 0.62 + 0.74 - 22.16 + 20.75 - 7.46 + 63.42 - 62.32 + 16.93 + 105.13 - 105.06 + 40.30 - 228.78 + 223.75 - 72.11
—I 8— 8 Ø 8— 9 I 8—IO	22.09 + 25.80 8.03	$ \begin{array}{r rrrr} & - & 14.33 \\ & + & 23.32 \\ & - & 9.45 \end{array} $	+ 29.73 - 32.25 + 10.13	+ 20.43 - 29.79 + 11.73	- 38. 98 + 39. 43 - 12. 45	- 27.97 + 37.06 - 14.29

Arg=ny+i'g'+ig		$r^2 rac{d^{y} \Gamma}{dr^{s}}$		$rr'rac{d^{3}\Gamma}{drdr'}$		$r'^2 rac{d^2 \Gamma}{dr'^2}$	
<u> </u>	sin.	cos.	sin.	cos.	sin.	COR	
" i' i -1 9-3 0 9-4 1 9-5 -1 9-4 0 9-5 1 9-6 -1 9-5 0 9-6 1 9-7 -1 9-6 0 9-7 1 9-8 -1 9-8 1 9-9 -1 9-8		+ 0. 21 - 0. 24 + 0. 09 - 2. 29 + 2. 26 - 0. 21 - 0. 68 + 0. 19 - 0. 99 +51. 70 -51. 55 +10. 84 -87. 80 +92. 04 -21. 12 -44. 99	+ 0.30 - 0.26 - 0.07 + 1.48 - 1.45 + 0.93 - 21.12 + 19.89 - 4.49 + 32.97 - 34.98 + 7.66 + 104.62 - 95.38 + 17.73 - 123.61	" - 0. 29 + 0. 28 - 0. 13 + 3. 36 - 3. 07 + 0. 42 - 0. 50 + 1. 08 + 1. 05 - 68. 45 + 64. 29 - 15. 22 + 119. 20 - 116. 86 + 28. 19 + 55. 82	" - 0.45 + 0.36 + 0.07 - 1.67 + 1.45 - 1.09 + 28.31 - 24.68 + 6.07 - 47.44 + 45.35 - 10.09 -132.53 + 115.40 - 24.53 + 157.31	+ o. 38 - o. 32 + o. 17 - 4.73 + 3.99 - o. 67 + 2.33 - 2.77 - 1.09 + 88.92 - 78.28 + 20.10 - 157.83 + 144.73 - 36.03 - 69.05	
0 9—9	94. 56 +18. 20	+37.38 + 3.15	+115.58 — 24.59	— 47. 08 — 0. 03	—138.90 + 31.61	+ 57.98 - 3.43	

And in a similar manner we have the developments of the three factors specially computed for $\delta^2 T'$:

$Arg = \kappa \gamma' + i'g' + ig$		$r'^2rac{d^2\Gamma'}{dr'^2}$		$rr'rac{d^2\Gamma'}{drdr'}$		$r^2rac{d^3\mathrm{T}'}{dr^2}$		
			sin.	cos.	sin.	C08/	sin.	009.
ν ο σ σ σ σ σ σ σ σ σ σ σ σ σ σ σ σ σ σ	i' 0 1 2 1 0 3 2 1 4 3 2 5 4 3	6 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0	" -5796. I - 979. 6 + 449. 2 + 409. 4 - 28. 5 + 24. 7 + 18. 2 + 16. 6 - 8. 5 - 2. 9 + 4. 7 - 2. 7 - 1. 2	" + 11.7 - 27.0 +954.2 -304.5 -415.9 +226.5 -113.2 - 77.0 + 30.4 - 17.9 - 9.8 + 2.3 - 1.6 - 0.7	" +2077.7 + 446.3 - 130.9 - 277.9 + 6.3 + 1.1 - 13.1 - 11.6 + 6.9 + 2.3 - 3.3 + 1.8 + 0.9	" - 3.3 + 10.1 -497.0 +160.5 +257.3 -128.4 + 59.0 + 53.5 - 18.0 + 9.3 + 7.2 - 1.3 + 0.8 + 0.5	" -1460.6 - 272.6 + 61.8 + 190.0 - 6.1 - 2.0 + 9.2 + 7.0 - 4.2 - 1.9 + 2.1 - 1.1 - 0.8	" - 2.9 +264.6 - 72.3 -169.3 + 74.4 - 29.2 - 38.2 + 11.0 - 4.8 - 5.4 + 0.8 - 0.3 - 0.3
1— 0 1	6 5 4	o o o	+ 0.6 - 0.4 - 0.3	- 0.2 - 0.3 + 0.6	- 0.6 + 0.2 + 0.3	+ 0.2 + 0.3 - 0.6	+ 0.6 - 0.1 - 0.3	- 0.2 - 0.3 + 0.6

$Arg = \varkappa \gamma' + \mathbf{i}'g' + \mathbf{i}g$	7'9 <u>'</u>	$rac{d^2\Gamma'}{dr'^2}$	$rr'rac{d}{dt}$	$\frac{r^{2}T'}{rdr'}$	902.	$rac{ar{t}^2 ext{T}'}{dr^2}$
	sin.	сов.	sin.	cos.	sin.	cos.
ж i' i —I— 2— I	+ 1.0	0, 0		// O. O	+ 0.7	
0— 3— 1	+ o.6	+ o.6	— o. 4	0.4	+ 0.3	+ 0.3
I 4 I	 1.6	_ o.8	+ 1.2	+ 0.6	— I.O	- 0.4
-ı- ı- ı	+ 7.4	+ I.9	_ 5.6	I. 7	+ 4.3	+ 1.5
0— 2— I	+ 5.8	+ 0.1	— 3· 7	— o.7	+ 2.2	+ 0.7
I— 3— I	— 14.7	2.7	+ 10.3	+ 2.7	— 7⋅3	- 2.4
—ı o— ı	+ 54.1	- 15.8	— 38. 5	+ 11.9	+ 28.8	- 2.9
0 1 1	+ 23.7	- 17.8	— 14.9	+ 6.2	+ 9.1	— о. 1
I— 2— I	85. 3	+ 38.9	+ 57.7	— 22. 3	— <u>3</u> 8.8	+ 12.0
-1 I- I	+ 354.9	— 222. 2	194. o	+ 316.2	+ 66.1	— 492. I
1 —0 O	— 2 2. 8	— 104. 6	— 4o. o	— 1 92. 1		
I I I	295.8	+ 494.7	+ 205.2	258. o	153.3	+ 73.7
-I 2- I	1685. 8	—8498. 2	+ 463.4	+2442. I	+ 503.5	+ 2298.6
0 I—I	+ 601.5	+3035.7	+ 535.7	+2487. 1	2344. 6	11174.2
1 o— 1	+ 595.8	+2887.3	— 59 1 . 9	2865. 5	+2632.4	+12603.3
—ı 3— ı	— 1 856. 7	-1392.6	+ 969.5	+ 515.0	— 43 0. 9	+ 40.8
0 2— 1	+ 954.9	+ 808.5	 488. 3	— 102.8	+ 122.8	— 551.6
1 I— 1	+ 328.6	+ 378.9	— 225.8	— 279. o	+ 181.8	+ 275.0
-1 4— I	— 445∙3	+ 19.6	+ 246.3	45.9	— 127.2	+ 52.7
0 3—1	+ 276.2	+ 1.7	— 1 49. 4	+ 43.1	+ 66.3	— 7 0. 5
I 2— I	+ 76.3	+ 29.8	55.4	- 21.4	+ 42.9	+ 17.0
—ı 5— ı	— 57.2	+ 46.2	+ 31.4	— 32. 2	16.6	+ 21.0
0 4— I	+ 38.9	30.4	— 19.7	+ 23.8	+ 8.2	17.5
1 3 1	+ 12.7	- 0.7	9.8	+ 0.6	+ 7.7	— o. 7
—т 6— т	- 2.7	+ 10.9	+ 1.0	- 7.4	— о. з	+ 4.8
0 5 1	+ 2. I	 7⋅5	— o. 5	+ 5.2	— о. з	_ 3. 3
I 4— I	+ 1.7	1.5	1.4	+ 1.3	+ 1.1	— r. r
—ı 7— ı	+ 0.6	+ 1.1	— o. 6	- 0.7	+ 0.5	+ 0.4
o 6 1	0.0	— 1.3	0.0	+ 0.9	+ 0.1	- o. 8
1 5 1	— o. 6	+ 0.3	+ 0.6	+ 0.3	— 0. 7	+ 0.3
—I— I— 2	- o. I	+ 1.0	+ 0.1	— 1.0	o. 1	+ 1.0
0- 2- 2	— o. 1	+ 0.2	+ 0.1	— O. 2	- O. I	+ 0.2
1-3-2	+ 0.3	— I. 3	- o. 3	+ 1.1	+ 0.3	- I.O
-1 O- 2	+ o. 3	+ 4.1	— o. 3	- 3.2	+ 0.3	+ 3.0
0- 1- 2	+ 0.9	+ 1.3	0.3	— 1.0	+ o. 1	+ 0.9
I 2 2	- I. 5	— 5.6	+ o.8	+ 4.3	o. 5	— 3·4
_1 I— 2	+ 20.0	+ 31.9	— 11.8	12.0	+ 3.4	— 15. 3
0 0— 2	+ 5.8	- o. 6	— 6. 5	21.1		
I- I- 2	— 27.5	— 29. I	+ 18.9	+ 25.9	— 1 4. I	27.1
—I 2— 2	— 63.6	+ 186.3	- 74.7	— 2 62. 7	+ 168.6	+ 462.3
0 I— 2	+ 47.7	38. 3	+ 80.1	+ 404.2	257.6	1143.4
I 0— 2	— 228. 5	— 54.9	+ 126.8	72.1	+ 131.9	+ 1080.8
—ı 3— 2	+8208.7	-3452. I	—4262. 6	+1766.8	+1969.8	— 779.9
0 2— 2	4284. 6	+1827.5	+2447.3	1015.9	—116 0. о	+ 420.7
I I— 2	— 913. 7	+ 393.2	+ 58o. 1	— 25 0. 9	436.5	+ 196.4

$Arg=\mu\gamma'+i'g'+ig$	$r^{\prime 2}rac{d^{2}\Gamma^{\prime}}{dr^{\prime 2}}$		$rr'rac{d}{d}$	$r^2 T'$	$r^3 \frac{d}{d}$	$rac{dr^2}{dr^2}$
	sin.	cos.	sin.	CO8.	sin.	cos.
 μ i' i -I 4-2 0 3-2 I 2-2 -I 5-2 0 4-2 I 3-2 -I 6-2 0 5-2 I 4-2 -I 7-2 0 6-2 	+1421.5 943.1 219.1 126.9 +- 74.1 38.8 94.4 +- 67.8 2.9 21.3 +- 16.1	" -2704.8 +1685.1 +136.2 -676.6 +470.6 +46.4 -85.3 +64.5 +11.3 -2.3 +1.9		+1550.5 -1030.8 - 99.4 + 393.6 - 281.6 - 36.6 + 46.7 - 34.7 - 9.1 - 0.1 + 0.4	+ 297.2 - 166.4 - 115.6 - 85.7 + 75.9 - 18.9 - 41.7 + 34.3 - 0.5 - 8.9 + 7.0	- 817.3 + 560.3 + 90.7 - 212.6 + 151.2 + 31.9 - 23.2 + 15.4 + 7.5 + 1.1
I 5— 2 —I 8— 2 0 7— 2 I 6— 2 —I 0— 3	+ 0.9 - 2.7 + 2.4 + 0.1	+ 2.2 + 1.3 - 1.4 + 0.2	- 0.8 + 1.9 - 1.6 0.0	- 1.7 - 1.1 + 1.2 - 0.3 + 0.2	+ 0.9 - 1.2 + 0.9 - 0.1 - 0.9	+ I.3 + 0.8 - I.0 + 0.3
0- I- 3 I- 2- 3 -I I- 3 0 0- 3 I- I- 3 -I 2- 3	- 0.1 + 1.0 - 1.3 0.0 + 1.4 - 22.6	0.0 + 0.2 + 0.8 + 0.2 - 1.1 + 23.6	+ 0.1 - 1.0 + 1.2 - 0.4 - 0.9 + 11.6	0.0 - 0.2 + 0.3 - 1.7 + 1.0 - 26.3	- 0.1 + 0.9 - 1.2 + 0.4	0.0 + 0.2 - 2.2
0 I— 3 I 0— 3 —I 3— 3 0 2— 3 I I— 3	+ 5.6 + 8.6 - 80.2 - 22.1 - 0.4	- 2.0 - 14.9 - 352.3 + 151.7 - 109.3	+ 3·3 - 9·3 + 78.0 + 1.4 - 6.3	+ 32.8 + 0.7 + 143.2 - 67.7 + 77.1	- 2.2 - 17.3 + 24.9 - 60.5 + 10.6 + 5.3	+ 40.9 - 93.5 + 83.6 - 21.9 + 10.5 - 52.2
-I 4-3 0 3-3 I 2-3 -I 5-3 0 4-3 I 3-3	+4530.9 -2857.9 + 27.9 +3225.4 -2234.6 + 82.1	+6572. 2 -4072. 6 + 40. 2 +1044. I - 756. 8 - 100. 2	$ \begin{array}{r} -2632.4 \\ +1832.6 \\ -17.5 \\ -1986.2 \\ +1477.2 \\ -53.1 \end{array} $	-3853.4 +2630.2 - 22.7 - 545.1 + 403.7 + 79.5	+1384.5 -1043.8 - 24.0 +1134.6 - 896.5 + 14.4	+2050. 91512. 9 36. 7 + 240. 9 167. 9 67. 7
-I 6-3 0 5-3 I 4-3 -I 7-3 0 6-3 I 5-3	+ 839.3 - 627.6 - 1.7 + 105.6 - 83.3 - 10.5	- 292. 4 + 204. 0 - 53. 9 - 153. 6 + 117. 2 - 10. 4	$ \begin{array}{rrrr} & -516.2 \\ & +403.7 \\ & +5.3 \\ & -60.2 \\ & +47.1 \\ & +9.2 \end{array} $	+ 225.3 - 177.0 + 41.1 + 107.5 - 87.3 + 7.6	+ 294.6 - 237.6 - 10.8 + 30.6 - 22.5 - 8.3	162.5 + 142.1 29.4 71.4 + 61.5 4.8
-1 8-3 0 7-3 1 6-3 -1 9-3 0 8-3 1 7-3	- I.O + O.I - 3.I - I.9 + 2.I - I.I	- 33·7 + 26.7 + 0.3 - 4.9 + 3.7 + 0.3	+ 3. I - 2. 7 + 2. 6 + 1. 3 - 1. 7 + 0. 9	+ 23.0 - 18.6 - 0.4 + 3.2 - 2.5 - 0.3	- 3.8 + 3.9 - 2.0 - 0.7 + 1.2 - 0.7	- 14.9 + 12.2 + 0.6 2.1 + 1.5 + 0.3

Arg=κγ'+i'g'+ig	$r'^2rac{d}{d}$	$\frac{rT'}{r'^2}$	$rr'rac{d}{dt}$	$P^{2}T^{\prime}$	$r^2 \frac{d}{d}$	72T' 1r2
	sin.	cos.	sin.	cos.	sin.	cos.
π i' i —I 2— 4			+ 0.3		+ 0.3	+ 2.0
0 1—4	+ 0.1	+ 0.3	+ 0.4	+ 2.2	_ I.3	6.9
1 o— 4	+ 0.7	+ 0.4	— 0, 6	_ I.O	+ 1.7	+ 7.2
—I 3— 4	- 29.3	23.8	+ 20. I	+ 12.3	12.9	— 5.4
0 2 4	+ 6.2	+ 11.7	— 5⋅3	6.4	+ 4.2	+ 2.6
I I 4	+ 7.5	+ 0.1	5.8	o. 6	+ 4.3	+ 0.9
—I 4— 4	+ 556.0	80.0	305.8	+ 72.0	+ 140.6	— 56.8
0 3-4	- 298.8	38. г	+ 182.8	+ 15.3	— 94·9	+ 1.0
I 2-4	+ 81.0	1.4	<u> </u>	– 0, 9	+ 38.2	— о. 1
—I 5— 4	4480. 7	+4737.3	+2870.5	-3002.6	—1712. 0	+1766.4
0 4—4	+3058.4	3307.0	—2143. 3	+2296.9	+1392.9	—I474. 2
I 3—4	344.7	+ 369.5	+ 248.5	— 266.4	— 149. 8	+ 159.8
—I 6— 4	438.8	+3303.9	+ 216.3	2161. 1	76.4	+1328.4
o 5— 4	+ 342.6	-2451.2	— 171. 0	+1719.4	+ 52.9	-1131.3
I 4-4	+ 67.5	+ 252.7	— 57⋅9	183.8	+ 50.7	+ 115.6
— I 7— 4	+ 477.5	+ 885. 1	— 354. 1	— 573. o	+ 251.7	+ 347.3
0 6— 4	362.3	— 694. 5	+ 291.4	+ 472.6	- 224.5	299.5
I 5 4	+ 77.1	+ 36.4	— 6o. 7	— 23.4	+ 45.3	+ 10.7
<u>—</u> 1 8— 4	+ 211.7	+ 103.2	— 150.9	59.7	+ 102.8	+ 30. I
0 7— 4	- 169.0	— 86.4	+ 127.6	+ 51.2	— 92. ī	— 25.8
1 6 4	+ 20.4	- 6.3	15.5	+ 6.0	+ 11.1	- 5.9
—I 9— 4	+ 46.1	— 8. ı	— 31.9	+ 8.6	+ 21.0	— 8, 2
0 8— 4	— 37·9	+ 6.0	+ 27.3	7.4	- 18.6	+ 7.7
I 7-4	+ 1.2	- 4.4	— o.8	+ 3.7	+ 0.6	- 3.0
—I IO— 4	+ 7. I	— 5.8	— 4·9	+ 4.5	+ 3.4	— 3·5
0 9-4	— 5 ⋅3	+ 4.6	+ 3.7	— 3.8	- 2.4	+ 3.0
I 8— 4	— o. 8	— o. 5	+ 0.7	+ 0.4	— o.6	— o. 3
—I 3— 5	— 2. 7	— I. I	+ 2.2	+ 0.6	- 1.8	- 0.4
D 2— 5	0.0	+ 0.6	- 0. I	- 0.4	+ 0.1	+ 0.2
I I 5	1.4	+ 0.6	— I.5	0.5	+ 1.6 + 8.5	+ 0.4
-1 4-5	+ 30.7	39. 2	— 17. z	+ 27.0		— 17.6 + 6.9
0 3 5	— 19.5 — 7.6	+ 11.5 + 3.6	+ 11.9	— 9. I — 2.0	- 6. 2 - 0. 5	+ 6.9 + 2.3
1 2-5	+ 1.6 + 148.8	+ 3.6 + 637.4	- 0.4 - 112.0	- 2. 9 - 396. I	+ 79.6	+ 2.3 + 223.7
-1 5-5 0 4-5	+ 140.0 - 9.5	+ 037.4 - 401.7	+ 13.8	+ 274.3	+ 79.0 - 16.4	+ 223.7 - 171.4
D 4-5 I 3-5	+ 3.3	+ 86.4	+ 13.6 - 2.5	- 63. o	+ 3.2	+ 41.9
-1 5-5 -1 6-5	+ 3·3 -4256.3	—2569. 7	+2876. 8	+1762. I	—1838. o	—1146.6
D 5—5	+3176.5	+1857.6	-2332. 6	—1381. 7	+1621.3	+ 975.9
1 4— 5	7 - 538. o	— 318. 3	+ 407.2	+ 241.4	— 283. o	— 168. 6
-1 7— 5	— 535. 0 —2992. 0	+ 170.8	+ 407.2	— 165. 6	— 203. 0 —1344. 1	+ 149.2
o 6— 5	+2328.2	— 126.8	-1709. 9	+ 140.3	+1196.0	— 1 40. 4
I 5— 5	- 337.6	+ 94.6	+ 256.6	- 78.3	— 18o. 6	+ 63.5
_1 5— 5 —1 8— 5	- 809. 6	+ 633.7	+ 547. I	— 76.3 — 469.3	— 349· 4	+ 335.7
-1 8- 5 0 7- 5	+ 658.0	— 506. I	+ 347·1 - 467·8	+ 400.9	- 349.4 + 314.1	— 307·4
i 6— 5	— 58. o	+ 104.2	+ 41.3	— 83. 7	— 25·7	+ 64.5
. 0_ 3]	1 204.2	1 44.3	3.7	I -3.7	1 -4.5

$Arg = n\gamma' + i'g' + ig$	7'8 <u>0</u>	$\frac{l^2 T'}{lr'^2}$	**************************************	d ² T' lrdr'	9-2	$d^3 T' \over dr^3$
	sin.	cos.	sin.	cos.	sin.	cos.
и i' i 1 05	76.8	"	,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,	— 186. 3	"	,,
		+ 255.9 - 210.4	+ 43.3	+ 161.2	- 19.9 + 18.9	+ 130.8
		l	- 39.9	— 22, I	1	- 119. 2 + 16. 1
, ,	+ 5.1		— 4.9 — 16.9		+ 4.8 + 14.6	+ 30.5
-1 10-5 0 9-5	+ 19.0	+ 59. 2 - 47. 5	+ 14.1	- 43.2 + 35.2	1	— 25. I
o 9— 5 1 8— 5	— 14.5 + 5.1	+ 0.7	- 4.2	+ 35.2 + 0.3	— 13. 1 + 3. 6	— I. 2
— 1 4— 6	+ 1.2	— 2.4	— 0.7	+ 1.6	+ 0.4	- 0.9
o 3 6	— 1.2	+ 0.9	+ 0.7	- 0.7	— o. 3	+ 0.5
1 2—6	— o. з	— o. 1	+ 0.3	+ 0.1	 0.3	- o. i
—ı 5— 6	+ 48.6	+ 31.6	— 33.8	— 18.4	+ 22.3	+ 9.3
o 4— 6	20.0	24.8	+ 15.3	+ 16.4	— II.2	— 9 .6
1 3— 6	+ 1.1	+ 5.4	- o. 8	3.6	+ 0.6	+ 1.9
-ı 6— 6	603.8	+ 236.4	+ 403.5	- 171.9	- 252.7	+ 119.6
o 5— 6	+ 425.6	— 89.4	— 309.9	+ 70.9	+ 212.5	— 54.6
1 4— 6	- 94.2	+ 15.9	+ 71.0	12.3	5o.o	+ 9.7
—ı 7— 6	+1141.1	—3407. o	828. 9	+2419.6	+ 579.2	—1645.8
o 6— 6	— 844. 7	+2665.7	∔ 661. 1	2040. 6	— 498. 7	+1499.9
ı 5— 6	+ 180.3	— 548. ı	— 142. 3	+ 429.0	+ 107.1	318. 2
1 8 6	— 631.8	—2437. 8	+ 478.5	+1744.9	— 35o. 6	—1199. 3
0 7—6	十 509. 2	+1964.2	412.5	—1495. 9	+ 322.8	+1096.9
1 6— 6	— 148. 8	— 340. 2	+ 116.7	+ 266, 8	85.4	— 198. 6
—ı '9— 6	— 726.6	646. 5	+ 545.7	+ 452.2	— 397.7	301.4
o 8— 6	+ 601.0	+ 539.9	— 479∙4	— 396. ₇	+ 372.4	+ 278.2
1 7—6	— 124.4	59. 1	+ 102.2	+ 44.1	— 82. o	30.2
-1 to- 6	294.9	— 35⋅4	+ 223.6	+ 15.8	165.7	- 2.2
0 9-6	+ 234.7	+ 34.5	— 183. 3	- 16.9	+ 138.9	+ 3.7
т 8— 6	— 20.9	+ 8.0	+ 13.4	— 7⋅5	6.6	+ 6.8
-1 5-7 0 4-7	+ 2.5 - 1.6	+ 1.2 - 1.8	— I. 2	— o. 7	+ 0.3	+ 0.3
3 4 7 1 3 7	+ 1.6	- 1.0 + 0.2	+ I.2 - I.3	+ 1.3	— o.8	- 0.9
_1 3— 7 —1 6— 7		+ 56.9	- I.3 + 8.3	- 0.2	+ 1.3	+ 0.2
0 5-7	- 19.1 + 26.6	— 28.2	— 18.8	— 40.9 + 21.7	— 0.9	+ 28.2
I 4— 7	— 16.2	+ 2.9	+ 14.4	— 1.9	+ 12.3	— 16.0
—I 7— 7	299. 3	— 496. o	+ 220.3	+ 348.6	— 12. 7 — 158. 4	+ 1.0 - 233.5
0 6-7	+ 163.6	+ 381.2	— 128.8	289.7	+ 98.5	+ 210.6
I 5— 7	- 32.6	— 91.3	+ 26.2	+ 71.1	- 20.5	1
—ı 8— 7	+2473.7	+ 241.4	-1827.3	— 193. o	+1304.9	- 52.7 + 150.4
0 7-7	—2003. 5	- 157. 2	+1584.4	+ 136.2	—1214. 6	— 115. 2
1 6-7	+ 462.5	+ 42.7	- 371.9	- 35.8	+ 287.9	- 115. 2 + 29. 3
—I 9— 7	+1800.0	- 876.8	—1331.8	+ 668.6	+ 953. I	- 496. 2
0 8-7	— 1488. 8	+ 733.5	+1167.2	— 595.8	— 887. 7	- 490. 2 + 472.6
1 7— 7	+ 288. 2	- 186.9	- 23I. 6	— 595.6 + 154.6	+ 179.3	+ 472.6 124.5
—I IO— 7	+ 449.3	— 801.4	- 323.9	+ 625.8	+ 179.3 + 223.9	- 480. 3
0 9-7	— 378. I	+ 625.4	+ 283.7	— 504. 2	+ 223.9 204.2	
1 8— 7	+ 37.4	- 79·7	- 26. 6	- 504. 2 + 56. 2	+ 16.8	+ 397.0
. ,	1 3/-4	17.1	20.0	30.2	7 10.0	— 34·5

$Arg = \varkappa \gamma' + i'g' + ig$	r'2 d	YT' T'2	rr'	d ² T' drd r '	$r^2 rac{\dot{c}}{c}$	$rac{d^2 \Gamma'}{dr^2}$
	sin.	cos.	sin.	cos.	sin.	cos.
π i' i -1 6-8 0 5-8 1 4-8 -1 7-8 0 6-8 1 5-8 -1 8-8 0 7-8 1 6-8 -1 9-8 0 8-8 1 7-8 -1 10-8 0 9-8 1 8-8 -1 7-9 0 6-9 1 5-9	*in. " + 1.6 + 1.0 - 1.2 - 61.8 + 35.6 - 4.5 + 357.5 - 296.8 + 78.8 + 219.8 - 216.3 + 53.4 + 1060.6 - 798.7 + 96.6 - 7.5 + 3.4 + 1.6	*** *** *** *** *** *** *** *** *** *** *** *** ** *** *** *** *** *** *** *** *** *** *** *** *** ** *** *** *** *** *** *** *** *** *** *** *** *** ** *** *** *** *** *** *** *** *** *** *** *** *** ** *** *** *** *** *** *** *** *** *** *** *** *** ** *** *** *** *** *** *** *** *** *** *** *** *** ** *** *** *** *** *** *** *** *** *** *** *** *** ** *** *** **	sin. - 1.6 - 0.5 + 1.2 + 45.9 - 28.0 + 3.3 - 260.5 + 233.1 - 63.8 - 155.4 + 166.3 - 43.4 - 848.5 + 654.6 - 63.2 + 6.1 - 2.7 - 1.7	COS. '' - 6.9 + 2.7 + 2.6 + 7.1 - 15.1 + 8.0 + 241.0 - 167.9 + 40.1 - 1249.9 + 1110.5 - 285.4 - 975.7 + 814.9 - 119.3 - 3.8 + 0.1 + 2.4	sin. " + 1.5 + 0.1 - 32.9 + 21.3 - 2.2 + 182.5 - 177.0 + 49.8 + 103.3 - 123.2 + 34.1 + 671.0 - 525.5 + 32.0 - 4.9 + 2.2 + 1.7	*** *** *** *** *** *** *** *** *** *** *** *** ** *** *** *** *** *** *** *** *** *** *** *** *** ** *** *** *** *** *** *** *** *** *** *** *** *** ** *** *** *** *** *** *** *** *** *** *** *** *** ** *** *** *** *** *** *** *** *** *** *** *** *** ** *** *** *** *** *** *** *** *** *** *** *** *** ** *** *** *** *** *** *** *** *** *** *** *** *** ** *** *** *** *** *** *** *** *** *** *** *** *** ** *** *
—I 8— 9 0 7— 9 I 6— 9 —I 9— 9 0 8— 9 I 7— 9 —I 10— 9 0 9— 9 I 8— 9	+ 5.0 - 13.9 + 7.7 + 306.7 - 215.8 - 46.6 - 1103.5 + 848.0 - 145.0	- 59.6 + 39.1 - 7.4 + 230.1 - 201.2 + 54.1 + 524.7 - 357.5 - 11.2	- 1.6 + 10.3 - 6.7 - 237.2 + 176.2 - 37.7 + 886.3 - 704.1 + 108.2	+ 45.0 - 31.4 + 6.0 - 173.7 + 162.0 - 44.1 - 429.3 + 289.2 + 27.7	- 1.0 - 7.2 + 5.6 + 179.3 - 140.6 + 29.5 - 702.4 + 573.2 - 73.8	- 33. I + 24. 6 - 4. 6 + 127. I - 126. 9 + 34. 8 + 349. 9 - 228. 4 - 43. I

We have in the next place to attend to the following factors of $\delta^2 T$ and $\delta^2 T'$. As the multiplications by which these quantities are formed naturally divide themselves into three sections independent of each other, according as the terms produced are independent of the factors nt or n't, or involve the first power of these factors, or in the last place their squares, we will divide the consideration of the second factors of $\delta^2 T$ and $\delta^2 T'$ into corresponding portions.

Of these fourteen factors four, viz., $n\delta^2 z$, $n'\delta^2 z'$, $\delta \nu$, $\delta \nu'$, have already been given; but from $\delta \nu$ and $\delta \nu'$ must be subtracted the constants which have virtually been supposed to belong to these quantities in Chapter I, when we derived the value of α . Now, from the present investigation, it appears that the value +1''.622 of the constant term of l(r'), given by Hansen,* is six times too large. Thus it is necessary to attribute to the constant terms of $\delta \nu$ and $\delta \nu'$ severally the values +0''.0665 and -1''.387.

^{*} Gegenseitige Störungen des Jupiter und Saturn, s. 167.

We have next to form the ten squares and products of the four quantities $n\delta z$, $n'\delta z'$, ν , and ν' . In doing this it will be more accurate to employ for $n\delta z$, $n'\delta z'$, etc., not their values, as given by considering first-order terms only, but as they are after $n\delta^2 z$, $n'\delta^2 z'$, etc., have been added to them. In this connection it is plain that the values, which ought to be attributed to the constant terms of ν and ν' , are the same as those just given in the case of $\delta \nu$ and $\delta \nu'$. It is convenient to give these squares and products the factor $\frac{1}{2}''(\log \pm 4.38454)$, as, on multiplication by the first factor of $\delta^2 T$ or $\delta^2 T'$, the resulting product is in seconds of arc as we desire it.

The following tables contain the developments of the portions of these squares and products which are independent of the factors nt or n't or their powers. The coefficients are uniformally carried to nine places of decimals; and the decimal point is omitted:

Arg=	$(n\delta z)$	$)^2 \times \frac{\mathbf{I}''}{2}$	$(n\delta z)(n$	$(\delta z') \times \frac{1}{2}''$	$(n'\delta z)$	$(2)^2 \times \frac{\mathbf{I}''}{2}$	$(n\delta z)$	$\nu \times \frac{1}{2}^{\prime\prime}$	$(n'\delta z')$	$\nu \times \frac{1}{2}^{"}$
i 'g'+ig	cos.	sin.	cos.	sin.	cos.	sin.	sin.	cos.	sin.	cos.
i' i 0 0 1 0 2 0 3 0 4 0 -3-1 -2-1 -1-1 0-1 1-1 2-1 3-1 4-1 5-1 6-1 7-1 -2-2 -1-2 0-2 1-2 2-2 3-2 4-2 5-2 6-2 7-2 8-2 0-3 1-3	+9121 + 73 + 540 - 6 + 21 - 3 + 222 + 199 - 496 - 120 + 82 + 411 + 1105 - 15 - 3 + 2 + 5 + 26 + 7 + 21 - 18 - 169 - 103 - 65 + 122 + 80 - 24 - 24 - 4	+ 160 + 967 -2764 + 8 + 40 + 35 + 132 -1997 + 27 - 434 - 1468 + 244 - 12 - 16 - 4 + 3 - 53 - 40 - 23 - 40 + 220 + 220 + 94 - 97 - 16 - 9 - 10 - 14	-21153 - 4805 - 228 - 2 - 45 + 5 - 315 - 310 + 444 + 56 + 357 - 2395 - 1375 + 103 + 6 - 35 - 48 - 47 - 53 + 347 + 298 + 154 - 135 - 77 + 33 + 18 + 6	-3011 - 379 +3576 - 9 - 49 - 64 - 195 + 2305 + 778 + 993 + 4739 - 253 + 47 + 22 + 6 - 4 + 68 + 71 + 51 + 24 - 285 - 273 - 207 + 114 + 17 + 12 + 16 + 21	+54062 +20252 - 454 + 24 + 95 + 216 + 167 + 203 - 155 - 1149 + 5976 + 28 - 392 - 2 + 1 + 3 + 48 + 47 - 16 - 94 - 1007 - 434 - 151 - 81 - 11 - 17 - 7	+11864 - 1119 - 1115 + 50 + 122 + 193 + 113 - 4427 - 13326 - 201 - 142 - 12 - 4 + 2 - 59 - 35 - 29 - 87 - 103 + 300 + 589 + 101 + 14 - 4 - 14 - 20	+ 17 + 121 0 + 7 + 2 - 81 - 64 + 137 + 16 + 3 + 183 - 5 - 1 + 1 - 3 - 12 + 1 - 5 + 3 + 15 - 1 + 17 - 6 + 5 + 4	- II - 20 -213 +789 - 3 + 2I + 12 + 42 -508 + 2 - 25 +124 - 42 + 8 + 5 + 2 + I - 2I - 17 - 6 + 3 + 46 + I + I + I2 + 4 + 3 - 5 - 4	-264 - 85 - 3 - 18 - 3 + 189 + 176 - 205 - 1 - 14 - 240 - 437 + 15 + 1 - 2 + 7 + 24 + 32 + 30 - 30 - 176 - 56 + 1 - 31 - 38 + 17 - 11 - 5	+ 26 + 205 + 144 1884 + 6 51 39 109 +1145 + 398 12 352 + 96 25 13 3 3 + 41 + 57 + 35 + 17 99 40 17 35 10 7 + 11 + 15
2— 3 3— 3 4— 3	— 4 — 104 — 190	0 + 150 - 140	+ 40 + 504	+ 27 - 29 + 166	- 4 - 13 - 264	- 22 + 5 - 43	+ 2 + 44 + 66	+ 64 - 54	— 2 — 22 —274	+ 18 - 12 + 89

Arg=	$(n\delta z)$	$\frac{1}{2} \times \frac{1}{2}^{\prime\prime}$	$(n\delta z)(n$	$(\delta z') \times \frac{1}{2}^{"}$	$(n'\delta z$	$()^2 \times \frac{\mathbf{I}''}{2}$	$(n\delta z)$	$\nu \times \frac{\mathbf{I}^{\prime\prime}}{2}$	$(n'\delta z')$	$\nu \times \frac{1}{2}^{\prime\prime}$
i'g' + ig	cos.	sin.	cos.	sin.	cos.	sin.	sin.	cos.	sin.	cos.
6' i 5-3 6-3 7-3 8-3 9-3 10-3	+ 121 + 930 - 651 - 176 - 4 + 2	+ 70 + 659 + 1621 + 76 - 3 + 7	- 398 - 1216 + 1907 + 433 + 4	— 100 — 1363 — 4801 — 152 — 0	- 457 + 452 - 5497 - 1052 - 1	- 230 + 3576 + 13674 + 278 - 1	27 144 + 54 18 2	+ 27 +103 +109 - 7 0	+ 163 + 376 - 122 + 43 + 2 - 2	- 63 - 341 - 250 + 19 - 1 + 4
I— 4 2— 4 3— 4 4— 4 5— 4 6— 4 7— 4 8— 4 10— 4 II— 4	- 4 - 4 - 3 - 144 + 39 + 34 1756 +1160 + 235 +5932 + 1	+ 3 + 1 + 6 - 150 + 219 - 128 + 1909 - 273 + 60 + 6184 + 4	+ 7 + 6 + 9 + 26 + 211 + 1951 - 1291 - 4961 - 14390 - 7	- 5 - 2 - 4 + 25 - 44 - 811 - 2259 + 279 - 1384 - 14957 + 2	- 7 - 9 - 9 - 5 - 26 - 938 + 1820 +22658 +34894 + 32	+ 5 + 3 + 2 - 2 + 320 + 929 - 362 + 6332 + 36150 - 27	$ \begin{array}{r} + 2 \\ + 2 \\ + 4 \\ + 81 \\ - 21 \\ - 15 \\ + 472 \\ - 240 \\ - 27 \\ + 42 \end{array} $	+ 2 + 1 + 3 - 86 + 106 - 54 + 533 - 55 + 9 - 62	- 4 - 5 - 8 - 21 - 14 - 123 - 1058 + 614 + 30 - 102	- 3 - 1 - 3 + 13 - 26 - 449 - 1210 + 133 - 6 + 147 + 1
2— 5 3— 5 4— 5 5— 5 6— 5 7— 5 8— 5 9— 5 10— 5 11— 5 12— 5 13— 5	+ I - 5 - 27 - 12 + 318 + 43 + 14 + 1021 + 6 - 11	+ 2 + 1 - 3 + 22 + 1 + 202 + 64 + 179 - 2039 - 7 - 34 - 5	- I - 0 + I + 9 - I - 51 - 23I + 20 - 122I + 20 + 32 - 2	- 3 - 4 - 2 - 6 - 17 - 80 - 341 + 360 + 2451 - 1 + 98 + 13	+ I	+ 3 + 4 + 3 + 1 + 10 + 33 + 225 + 181 + 120 + 31 - 275 - 28	0 0 + 3 + 17 + 9 -168 - 8 - 5 -248 - 2 + 1	+ I + I - 4 + I3 - 2 + I06 + 7 + 5I - 497 0	+ I 0 - I - 6 - 4 + 2I + 14I - 3 + 6I3 + 2 - 3	- 2 - 2 - 6 - 17 - 63 - 203 + 164 + 1225 + 3 + 6
6— 6 7— 6 8— 6 9— 6 10— 6 11— 6 12— 6	+ 3 + 9 + 19 + 83 - 107 + 18 - 24 - 6	+ 8 + 7 - 20 - 27 - 37 + 13 - 44 + 32	0 - 3 - 18 - 87 - 78 - 12 + 29 + 6		+ 3 + 13 + 73 + 49 + 13 - 12 - 2	— 29	+ 7	+ 6 + 8 - 12 - 14 - 21 + 4 - 15 + 6	+ 1 + 2 + 15 + 57 + 54 + 6 - 15 - 4	- I - 2 + 3 + 24 + 24 - 3 + 28 - 16
7— 7 8— 7 9— 7 10— 7 11— 7 12— 7 13— 7	+ 2 + 2 - 1 - 6 + 5 - 5	0 — II — 5 — 2I — 15 + 5 — I	- I - 2 + 2 + I - 6 - 5 + I2 + 2	+ 1 + 5 + 28 + 18 + 2 - 1	+ 1 - 2 - 2 + 7 + 5 - 5	- 26 - 17 - 5 - 3	- 2 - 1 + 2 + 4 - 2 + 5 - 2 + 1	- 3 - 10 - 6 + 3 + 1	+ I - I 0 + 4 + 2 - 8 - I	+ I + 6 + 2I + II + 4 - I + I
10— 8 11— 8 12— 8	- 2 - 8 - 5 - 1	- I - 3 + 3	+ 2 + 10 + 5 + 1	+ 1 + 4	_ ii	- I - 4	+ 3 + 2	+ 1 - 1	- 6 - 4 - 1	+ I + 3 - 2

$\begin{array}{c} \mathbf{Arg} = \\ \mathbf{i}'g' + \mathbf{i}g \end{array}$	$(n\delta z)$	$\nu' \times \frac{1}{2}''$	$(n'\delta z')$	$\nu' \times \frac{1}{2}''$	ν^{3}	× ¹ / ₂	יעע'	× ¹ / ₂	v'9	× 1"
• 9 7•9	sin.	cos.	sin.	cos.	cos.	sin.	008.	sin.	cos.	sin.
i' i o o I o 2 o 3 o 4 o	1846 169 + 1 + 17	+ 17 +922 +198 -278 - 10	+5028 - 89 - 15 - 38	- 33 2572 + 421 + 535 + 24	+122 45 8 5	—19 —19 +14	— 12 — 47 +116 + 1	— 14 +195 — 36	+945 255 75 11 + 1	-426 76 +- 22
-3- I -2- I -1- I 0- I I- I 2- I 3- I 4- I 5- I 6- I	+ I + 63 + 16 - 141 - 83 - 7 - 84 + 1223 + 18 + I	- 2 - 7 + 7 + 95 -549 +355 -765 -275 - 18 - 2	- 2 - 122 - 86 - 77 + 63 + 120 + 10 - 3002 - 54 - 3	+ 4 + 28 + 69 + 63 - 28 - 525 + 1798 + 698 + 48 + 9	- 4 + 35 - 10 + 41 - 96 - 4	+ 3 +23 +11 -47 +36 - 2	0 + 11 13 95 48 + 38 24 2 + 2	+ 1 - 4 - 16 - 70 + 279 + 8 - 1 - 3 + 2 + 1	- 6 + 12 + 33 + 67 - 46 - 698 + 95 + 2	+ I + 22 + 26 - 3 - 496 + 26I + 30 - I
-I- 2 0- 2 I- 2 2- 2 3- 2 4- 2 5- 2 6- 2 7- 2 8- 2	+ 7 + 4 - 8 - 79 + 131 - 122 + 3 + 80 + 9 + 3	+ 17 + 9 - 5 + 17 + 48 +215 + 11 + 20	- 16 - 24 - 33 + 11 - 2 + 351 - 23 - 195 - 39 - 6	- 33 - 20 - 13 - 38 - 486 - 70 + 21 - 35 0 + 2	- I + 6 + 4 + I - I6 - I 0	+ 2 - 2 - 1 - 7 - 1 - 21 - 2 0	0 - 4 - 11 - 23 + 63 - 22 + 3 - 4 + 3 - 1	- I - 2 + II + 2 + 17 - 88 + 4 + 2 0	- 1 + 6 + 2 -173 - 30 + 95 - 45 + 2	+ 1 - 2 - 6 - 70 +234 - 30 + 17 + 5
0-3 1-3 2-3 3-3 4-3 5-3 6-3 7-3 8-3 9-3	- 4 - 1 - 2 + 105 - 227 + 140 - 1060 - 375 + 78 + 3	+ 3 + 1 + 2 +157 + 16 - 57 +488 -720 + 26 + 2	+ 10 + 4 + 1 - 9 + 112 + 834 +2429 + 861 - 188 - 6	- 8 - 11 - 11 - 34 - 42 - 69 - 417 + 1668 - 62 - 6	+ 1 + 17 + 8 - 6	- I -27 +14 - 9 + 2	+ I	+ 2 + 2 - 89 - 13 + 28 + 33 - 15 + 1	- I - 7 - 38 + 14 +717 -120 - 67 + 7 - I	- 3 - 4 + 58 + 42 + 52 - 526 + 99 - 2
1— 4 2— 4 3— 4 4— 4 5— 4 6— 4 7— 4 8— 4	- 2 - 1 + 3 - 37 - 17 - 175 + 112 - 125	- I - I + 6 + 37 + 2 -546 - 16 - 58	+ 3 + 5 + 4 + 8 + 24 + 112 + 452 1000	+ 3 + 1 + 1 - 7 + 15 + 167 + 461 - 168	+ 1 + 45 - 11 - 4 - 29 + 6	2 +48 49 +25 +6 +2	+ 1 + 3 - 24 - 8 - 84 + 133 - 4	- 5 - 23 - 4 +297 - 65 - 4	- I - 2 + 14 + 22 + 36 + 29 -642	+ 2 + 15 + 6

Arg=	$(n\delta z)$ 1	$v' \times \frac{1}{2}''$	$(n'\delta z')$	$\nu' imes rac{1''}{2}$	$ u^2 angle$	<\frac{1''}{2}	νν'	$\times \frac{\mathfrak{l}''}{2}$	$ u'^2 imes$	$\langle \frac{\mathbf{I}''}{2}$
∛ g′+ig	sin.	cos.	sin.	cos.	cos.	sin.	cos.	sin.	cos.	sin.
i' i 9— 4 10— 4 11— 4	+2271 247 4	-645 +298 - 3	-5306 + 598 + 9	+1480 - 721 + 8	ø	I	—19 + 2	- 9 + 3	+198 - 9	+74 16
4— 5 5— 5 6— 5 7— 5 8— 5 9— 5 10— 5 11— 5 12— 5 13— 5	- II - 8 + 53 + 54 - I5 - 34 + 3 - 4 - I	- 5 - 13 - 33 - 80 + 288 - 61 + 4 + 15 - 1	+ I + 3 + I - 33 - 76 - 8 + I5 + 9 + 8	+ 2 + 4 + 7 + 28 + 127 + 101 + 41 - 19 - 35 + 5	+ 2 +10 + 8 -95 +19 - 1 + 6	+ 3 - 9 + 2 -48 +29 + 5 - 8	- 7 - 8 +32 +16 - 8 -13	+ 6 + 12 + 16 + 21 - 161 + 21	+ 7 + 4 - 22 - 8 - 1 - 5 + 9 - 1	- 3 - 3 - 14 - 14 - 9 + 6 + 5 - 3
6 6 7 6 8 6 9 6 10 6 11 6 12 6	+ I + I + II + 2I + I7 - 4	- 4 - 3 + 8 + 12 - 3 + 4 - 6 + 6	0 2 10 43 30 7 +- 5 +- 2	+ I - I - 8 - I5 + 4 + 5 - I6 + I4	- 2 - 4 - 7 - 9 +38	- 5 - 3 + 9 + 3 + 5	+ I + 2 + 6 + 4 + 2 - 5 - I	+ 2 + 3 - 7 - 6 + 1 - 5 + 3	- I - I - 6 - 5 - 2 + 2 + 2 + 2	- 2 - 1 + 5 + 2 0 + 1 + 3 - 13
7— 7 8— 7	+ 1	0	o	- I	— I	0			I	o
9-7 10-7 11-7 12-7 13-7	- 2 0 + 2 + 2 - 3	+ 4 + 8 + 5 + 2	+ I + 2 - 4 - 4 + 3	- 6 - 15 - 10 - 3	+ 2 + 2 	+ 2 + 2 + 1 - 3	- 2 0 0	— 3 — 2 — I	0 + 1	+ 3 + 2 + I
14— 7	+ 7	— 4	+ 3	o			+ 5	+ 1		
10— 8 11— 8 12— 8	— 2 — 4 — 2	+ 1 + 1	+ I + 6 + 4	— I — I — 3	+ 1	ס	— т	0	+ 1	0
I2 — 9	0	_ I	+ 1	+ 2						

We are now in possession of all the quantities needed for the calculation of the portions of $\delta^2 T$ and $\delta^2 T'$ which are not multiplied by the factors nt, n't or their powers. Hence, proposing to stop the approximation with the terms of three dimensions, we avail ourselves of the possibility of obtaining a higher degree of precision by computing the terms of these quantities which depend severally on the arguments γ and γ' , and applying the resulting corrections to $n\delta z$, $n\delta^2 z$, ν , $\delta \nu$, $n'\delta z'$, $n'\delta^2 z'$, ν' , and $\delta \nu'$. This course of proceeding is exactly similar to that we employed with the second-order terms in Chapter IX

There has been found

$$δ^2T = -0.0038635 \sin(-\gamma) + 0.0080094 \cos(-\gamma)$$

$$δ^2T' = +0.100156 \sin \gamma' -0.059616 \cos \gamma'$$

On integration these equations give

$$n\delta^{3}z = -0.0080094nt \sin(-g) - 0.0038635nt \cos(-g)$$

$$n'\delta^{3}z' = -0.059616n't \sin g' - 0.100156n't \cos g'$$

If these corrections are applied to the complete values of $n\delta z$ and $n'\delta z'$, obtained previously, we get

$$n\delta z = -1.284368nt \sin(-g) - 1.400329nt \cos(-g)$$

 $n'\delta z' = -6.681432n't \sin g' - 10.708152n't \cos g'$

The values used in the computation of the third-order terms, however, were

```
n\delta z = -1.284370nt \sin(-g) - 1.400324nt \cos(-g)
       -0.015494nt \sin(-2g) - 0.016877nt \cos(-2g)
       -0.000373nt \sin (-3g) - 0.000407nt \cos (-3g)
       -0.000012nt \sin (-4g) - 0.000013nt \cos (-4g)
   \nu = - 0.015507nt
       -0.642311nt \cos(-g) + 0.700126nt \sin(-g)
       -0.015490nt\cos(-2g) + 0.016872nt\sin(-2g)
       -0.000557nt\cos(-3g) + 0.000612nt\sin(-3g)
n'\delta z' = -6.681439n't \sin g' - 10.708170n't \cos g'
       -0.092997n't \sin 2g' - 0.149736n't \cos 2g'
       -0.002549n't \sin 3g'
                               - 0.004189n't \cos 3g'
       -0.000094n't \sin 4g'
                               - 0.000158n't \cos 4g'
   \nu' = + 0.093349n't
       +3.339074n't\cos g' - 5.352962n't\sin g'
       + 0.092870n't \cos 2g' - 0.149869n't \sin 2g'
       + 0.003852n't \cos 3g'
                               - 0.006330n't \sin 3g'
       + 0.000191n't \cos 4g'
                               - 0.000319n't \sin 4g'
```

In order to have the proper values of $n\delta^2 z$, $n'\delta^2 z'$, $\delta \nu$, and $\delta \nu'$ the values employed for $n\delta z$, $n'\delta z'$ ν , and ν' in computing the second-order terms ought to be subtracted from those just given. With regard to $n\delta z$ and ν the values were not quite the same in computing $\delta T'$ as in computing δT . Hence, in deriving $\delta^2 T$ we employ the terms

$$n\delta^{2}z = -0.008457nt \sin(-g) - 0.004104nt \cos(-g)$$

$$-0.000116nt \sin(-2g) - 0.000046nt \cos(-2g)$$

$$-0.00002nt \sin(-3g) - 0.000001nt \cos(-3g)$$

$$\delta \nu = -0.00015nt$$

$$-0.004354nt \cos(-g) + 0.002016nt \sin(-g)$$

$$-0.000112nt \cos(-2g) + 0.000041nt \sin(-2g)$$

$$n'\delta^2z' = -0.069141n't \sin g' - 0.115525n't \cos g'$$
 $-0.000416n't \sin 2g' - 0.001386n't \cos 2g'$
 $+0.000044n't \sin 3g' - 0.000034n't \cos 3g'$
 $\delta v' = +0.000574n't$
 $+0.032925n't \cos g' - 0.056640n't \sin g'$
 $+0.000289n't \cos 2g' - 0.001519n't \sin 2g'$
 $-0.000037n't \cos 3g' - 0.000098n't \sin 3g'$

But in deriving $\delta^2 T'$ we substitute for the first two the following:

$$n\delta^{2}z = -0.008008nt \sin(-g) - 0.003859nt \cos(-g)$$

$$-0.00097nt \sin(-2g) - 0.000047nt \cos(-2g)$$

$$-0.00002nt \sin(-3g) - 0.00001nt \cos(-3g)$$

$$\delta\nu = -0.00097nt$$

$$-0.004004nt \cos(-g) + 0.001930nt \sin(-g)$$

$$-0.00097nt \cos(-2g) + 0.000047nt \sin(-2g)$$

$$-0.00003nt \cos(-3g) + 0.00002nt \sin(-3g)$$

The remaining terms of these quantities are the same as those given at pages 290-294, 335-339. In computing δT it is convenient to have n always accompany t as a factor, and with $\delta T'$ to have n' accompany the same variable. Hence, we take occasion to make some multiplications by $\frac{n'}{n}$, $\frac{n'^2}{n^2}$ or the reciprocals of these factors.

The following tables contain the portions of the ten factors which are multiplied by nt or n't. The coefficients are expressed in units of the eleventh decimal:

Arg=	$(n\delta z)$) ² × ¹ / ₂	$(n\delta z)(n^{i}$	$(\delta z') \times \frac{1}{2}''$	$(n'\delta z')$	$(1)^2 \times \frac{\mathbf{I}''}{2}$	$(n\delta z)$	$\nu \times \frac{\mathbf{I}''}{2}$	$(n'\delta z')$	$)\nu \times \frac{\mathbf{I}''}{2}$
i 'g'+ig	nt cos.	nt sin.	nt cos.	$nt \sin$.	n't cos.	n't sin.	nt sin.	nt cos.	nt sin.	nt cos.
ť i 0 0	—18 6		+421		-2572					6
0— 1	— 2 5	+ 45	193	+ 33	+ 129	+ 144	51	+10	+ 60	+ 4
0— 2	— 3	— I	— 11	14	+ 36	— 6	4	+ 1	+ 6	8
1+2	— 2	+ 3	+ 6	- 2	- 14	+ 2			+ 3	+ 1
1+1	+ 7	+ 36	— 10	18	10	— 6 ₇	— 4	-13	— 2	+ 7
10	164	+ 96	+176	— 98	— 1 897	+1367	62	8	+ 6	- 7
1-1	— 30	+ 10	200	316	+3402	+5127			+ 29	— 51
1-2	-107	143	92	562	+ 67	+ 468	+ 43	-13	+ 52	318
1 3	5	- 3	+ 1	_ 6					2	8
2.⊹ I	6	+ 32	+ 10	— 10	+ 1	十 ` 34	I	-11	+ 1	+ 4
2 0	249	— 1 88	+339	+344	_ 2	+ 48	38	+33	+175	-171
2 I	 144	407	171	159	+ 38	+ 481	— 82	—1 3	+ 75	— 62
2— 2	+178	-210	—401	+583	+ 69	+ 316	63	39	+197	+273
2— 3	+398	-181	- 85	+ 18	+ 99	+ 9	-211	+95	+ 55	+ 11
2— 4	+ 11	— 5					— 9	+ 3		

$\begin{array}{c} \text{Arg} = \\ i'g' + ig \end{array}$	$(n\delta z)$	$^{2}\times\frac{I^{\prime\prime}}{2}$	$(n\delta z)(n')$	$(\delta z') imes rac{{f I}^{\prime\prime}}{2}$	$(n'\delta z')$) ² × ¹ / ₂	$(n\delta z)$	$\nu \times \frac{\mathbf{I}''}{2}$	$(n'\delta z')$	$\nu \times \frac{\mathbf{I}''}{2}$
<i>i y +iy</i>	nt cos.	nt sin.	nt cos.	nt sin.	n't cos.	$n't \sin$.	nt sin.	nt cos.	$nt \sin$.	nt cos.
i' i 3+ I 3 0 3- I 3- 2 3- 3 3- 4	+ 10 + 241 + 60 - 40 - 183 - 12	- 6 + 29 + 232 - 30 - 17 - 35	- 7 - 293 - 78 + 442 - 18 - 2	+ 2 + 1 - 431 - 293 + 3 + 17	+ 167 - 1274 + 8065 + 52 + 8	+ 30 + 6239 - 6246 + 22 - 27	60 21 30 +- 85 +- 7	+ 2 7 I 0 + 2	- 5 - 154 - 52 - 240 + 20 + 2	0 + 1 - 40 - 177 - 22 + 12
4 0 4 I 4 2 4 3 4 4 4 5	- 48 - 34 - 28 + 9 - 8	+ 2 + 104 - 15 - 12 - 32	+ 13 + 564 -3786 + 834 + 4 + 5	- 7 - 700 + 590 + 829 + 18 + 2	- 3 - 456 +42475 + 60 + 14	+ 18 + 170 - 6746 + 120 - 12	- 2 - 21 + 8 - 5 + 5	- 16 0 + 1 + 3 + 1	+ 10 + 266 + 70 - 411 - 6	+ 7 + 325 + 18 + 406 + 16
5 0 5— 1 5— 2 5— 3 5— 4 5— 5 5— 6	- 33 -2541 + 238 - 917 - 274 - 12 - 1	+ II + 902 + 280 -2449 + 22I + 3 + 3	+ 37 + 880 - 71 832	— 13 —1084 — 21 +2920 + 41	+ 45 + 9414 + 62 + 39	- 79 + 4247 + 31 - 7	$ \begin{array}{r} - 15 \\ - 623 \\ + 108 \\ + 278 \\ + 134 \\ + 8 \end{array} $	— 5 —227 — 21 —626 — 14	+ 37 + 1537 + 33 - 680 - 4 - 3	+ 13 + 545 + 44 + 1454 + 37 + 3
6— 2 6— 3 6— 4 6— 5	+ 9 61 + 5	+ 16 + 64 + 3 - 5	—2077 — 174 + 27	-2971 + 312 + 19	+25050 485 19	+35598 + 76 + 4	+ 7	II	- 16 + 113 - 12	+ 30 + 170 + 12
7— 2 7— 3 7— 4 7— 5	+ 2 - 144 - 123 - 12	+ 10 - 60 - 149 + 5	- 33 + 416 + 145	- 50 + 185 + 158	+ 367 - 3095 - 167	+ 469 - 1229 - 188	+ 13 + 35 + 7	+ 6 + 50 + 1	— 3 — 18 — 77	+ 5 + 15 + 84
8— 2 8— 3 8— 4 8— 5	+ 2 - 10 + 12 - 3	$ \begin{array}{rrr} - & 3 \\ - & 21 \\ + & 121 \\ - & 2 \end{array} $	+ 14 5 + 29	+ 58 - 113 - 15	+ 12 - 91 + 9 - 43	+ 11 - 447 + 404 + 20	3	— 13	+ 5	— 56 — 9
9-3 9-4 9-5 9-6	+ I - 9 - 18 + 2	0 + 22 - 3 + 7	+ 257 — 48	— 595 + 2	+ 2 - 2850 - 47	— 18 + 6635 — 6	+ 6	— I	3 + 22	- 5 + t
10— 3 10— 4 10— 5 10— 6	0 —1065 + 264 + 4	- 13 + 762 + 165 - 19	— 1 +2535 — 315	+ 15 1834 195	—15188 — 41	+11120 — 27	— 12 — 50	o - 7	+ I + 20 + I55 + 3	- 7 + 10 - 97 - 6
11-4 11-5 12-5			+ 47 - 3	+ 10	- 566 - 20 + 30	+ 132 - 6 + 43			+ 4	- 5

$ m_{\it i'g'+ig}^{Arg=}$	$(n\delta z)i$	√'× ¹ / ₂	$(n'\delta z')$	$\nu' imes rac{{f I}''}{2}$	$ u^{2}\rangle$	< 1''	νν':	$\times \frac{\mathbf{I}''}{2}$	v'^2	×1"
i'g'+ig	$nt\sin$.	$nt\cos$.	$n't \sin$.	n't cos.	nt cos.	nt sin.	nt cos.	nt sin.	n't cos.	n't sin.
i' i 0 0 0— I 0— 2	+ 103 + 7	+ 69 + 38 - 8	+ 1187 - 2	— 360 + 554 + 16	— 2 — I	+ 1	+ 1 + 33 + 3	— 14 + 4	- 43 +1226 + 13	— 516 — 19
I+ 2 I+ I I O I- I I- 2 I- 3	6 + 243 + 92 + 166 + 4	- 3 + 165 - 140 - 443 - 8	- 6 - 38 - 426 - 1231 - 55	- 1 + 20 - 358 +2069 + 345	0 2 24 4 +- 17 +- 2	+ I - 3 + I5 + 3 + 23 + I	- 87 + 6 + 87 + 3	6 + 58 + 23 +239 + 7	+ 53 + 12 - 425 - 36	+ 37 - 35 - 146 - 228
2+ I 2 0 2- I 2- 2 2- 3 2- 4	89 87 7 + 145 + 56	+ 81 + 98 + 13 + 202 + 15	+ 1 - 49 + 934 - 45 - 76	- 24 - 13 - 905 + 156 + 6	+ I 14 45 20 111 6	$ \begin{array}{rrr} - & 3 \\ - & 19 \\ - & 115 \\ + & 9 \\ + & 51 \\ + & 2 \end{array} $	+ I + 37 2I + 70 + 34	- r + 52 - 13 - 92 - 8	+ 3 + 81 - 934 - 62 - 52	+ 4 - 4 - 829 - 114 - 4
3+ I 3 0 3- I 3- 2 3- 3 3- 4	- 33 + 42 + 281 + 41	- 11 + 193 + 187 + 1 + 12	+ 73 + 13 - 4114 - 45 - 6	— 11 — 707 —3169 + 27 — 22	- 2 - 2 - 6 - 9 + 39 + 4	+ I + 4 + 34 + I + 4 + I3	$ \begin{array}{c} + 8 \\ + 16 \\ +135 \\ + 24 \\ + 2 \end{array} $	- 5 - 13 - 95 + 1 - 8	+ 13 - 567 -2121 - 33 - 5	+ 1 - 5 ² +1701 - 15 + 15
4 0 4— I 4— 2 4— 3 4— 4 4— 5	— I — 252 +1673 — 421 — I — 4	- 8 - 363 + 278 + 450 + 14 + 1	— 1 — 7 —10889 — 25 — 10	+ 9 + 481 2104 + 52 - 12	- 3 - 8 + 2 - 3 + 3	+ 3 - 4 + 6 + 10 + 1	+ 1 +117 - 59 -217 - 2 - 4	- 5 -142 - 3 -233 - 11 - 1	+ 4 + 57 - 335 + 6 - 6 + 5	+ 2 + 28 + 483 + 30 + 9 + 3
5— I 5— 2 5— 3 5— 4 5— 5 5— 6	— 22 — 3 — 67	- 61 + 58 + 33	53 30 14	— 317 — 66 — 4	+ 12 + 56 + 66 + 5 + 1	+ 69 9 61 3 1	+ III - 5 - 32 - 2 - 2	- 28 - 3 - 20 - 2 - 2	+ 8 +2243 - 25 + 11 + 2	+ 3 +1036 + 109 - 1 + 4
6— 2 6— 3 6— 4 6— 5 6— 6	—1035 — 92 — 30	+1476 - 121 + 13	+ 5861 178 + 11	—8835 — 419 — 15	I	- I	+ 7 71 19	+ 14 + 96 - 5	+ 466 + 153 + 25 + 1	+ 62 - 5 + 10 - 3
7— 2 7— 3 7— 4 7— 5	- 29 - 70 - 3 - 3	+ 39 + 26 - 10 - 3	+ 182 + 341 + 85	- 237 - 186 - 100	+ 2 0 + 3	— r — 7	- 2 + 4 - 2	+ 3 + 12 + 3	+ 10 - 18 + 20 + 3	+ 5 - 20 + 11 - 6

$\begin{array}{c} \text{Arg} = \\ i'g' + ig \end{array}$	$(n\delta z)i$	$y' imes rac{1''}{2}$	$(n'\delta z')$	$\nu' imes rac{\mathbf{I}''}{2}$	$ u^2 angle$	< 1"	νν',	$\times \frac{1}{2}^{"}$	$ u'^2$	×1"
1 y +1y	nt sin.	nt cos.	n't sin.	n't cos.	$nt \cos$.	$nt\sin$.	nt cos.	nt sin.	n't cos.	$n't \sin$.
6' 6 8— 2 8— 3 8— 4 8— 5 9— 3 9— 4 9— 5 9— 6 10— 4 10— 5 10— 6	+ 5 - 6 - 10 -117 + 33 + 26 - 4	- 16 + 12 - 6 -270 0	+ 8 - 25 - 3 + 20 - 4 +680 + 22 - 1 -161 + 14 + 2	- 8 + 78 + 244 + 12 + 8 + 1591 - 2 + 60 - 9 + 60	- I - 3 - 2 - 1	- I · + 2	+ 1 + 2 + 19	+ 2 - 3 - 1	- I - 26 + 5 - 32 + 3	- 15 170 - 3 + 24 0
11— 4 11— 5 12— 5	+ 24 4	+ 3 + 6	—144 + 4 — 5	- 31 - 8 + 6			_ I	— 3	+ 5	+ 2

In like manner the portions of the ten factors multiplied by n^2t^2 or n'^2t^2 follow; the coefficients are expressed in units of the thirteenth decimal when multiplied by n^2t^2 , but in units of the twelfth decimal when multiplied by n'^2t^2 :

$\begin{array}{c} \text{Arg} = \\ i'g' + ig \end{array}$	$(n\delta z)$) ² × ¹ / ₂	$(n\delta z)(n$	$(\delta z') \times \frac{1}{2}^{"}$	$(n'\delta z'$) ² × ^{1''} / ₂	$(n\delta z)$	$\nu \times \frac{\mathbf{I}''}{2}$	$(n'\delta z')$	$\nu \times \frac{1}{2}^{"}$
* g' + i g	$n^2t^2\cos$.	n^2t^2 sin.	$n^2t^2\cos$.	n^2t^2 sin.	$n^{/2}t^2\cos$.	$n'^2t^2\sin$.	n^2t^2 sin.	n^2t^2 cos.	$n^2t^2\sin$.	$n^2t^2\cos$.
6' 6 0 0 0— 1 0— 2 0— 3	+261 + 1 + 18 + 1	— 9 +211 + 6	— 5 9 + 4	+ 11	+1112		+ 3 - 10	+ 1 +106	— 2	+ 6
I+ 2 I+ I I O I- I I- 2	o - 1	+ 1 - 1	+258 + 92 - 11	-5^{2} $+275$ $+6$	+ 71 0	+ 24 + 17			+ 6 +279 + 5 - 76 + 1	$\begin{array}{c} + & 1 \\ + & 52 \\ + & 8 \\ + & 275 \\ + & 8 \end{array}$
2+ I 2 0 2 I 2 2 3 0 3 I 3 2	+ 3 + 3 + 4 + 1 - 5 + 1	- 5 - 2 - 1 - 1 - 2 + 1	- 12 + 16 + 6 + 8	+ 4 + 12 + 7 + 12	+ 412 - 5 + 11 - 31 + 28	+840 - I + 24 - 16 + 80	- I - I - I	+ 2 - 1 0	+ 3 - 3 - 1 + 4	- 6 + 3 + 3
3-3	+ 1	— 3	- 11	+ 12			I	_ I		

$ m Arg = \it i'g' + \it ig$	$(n\delta z)$	$^{9}\times_{\hat{2}}^{1^{\prime\prime}}$	$(n\delta z)(n$	$(\delta z') \times \frac{1}{2}^{\prime\prime}$	$(n'\delta z')$) ² × ^{1''} / ₂	$(n\delta z)$	$\nu \times \frac{1}{2}^{\prime\prime}$	$(n'\delta z')$	$\nu \times \frac{\mathbf{I}''}{2}$
* g' + ig	n^2t^2 cos.	n^2t^2 sin.	$n^2t^3\cos$.	$n^2t^2\sin$.	$n'^2t^2\cos$.	$n^{/2}t^2\sin$.	n^2t^2 sin.	$n^2t^2\cos$.	$n^2t^2\sin$.	$n^2t^2\cos$.
i' i 4— 1 4— 2 4— 3	- I + I	— I	+ 6 + 18 + 3	+ 3 - 73 - 6	— 3 — 12	— 7 +690			+ 14	— I3 + I5
5 ° 5— 1 5— 2 5— 3 5— 4	- 2 - 55 - 15 + 173 - 9	- 4 220 + 14 54 13	+ 42 7 88	+143 5 + 32	— 71	+130	- 1 14 5 44 + 1	+ 1 +55 - 1 -13 + 5	+ 2 + 34 +101	- 3 -131 + 33
6— 2 6— 3 7— 2 7— 3	o	— 3	+187 - 20 + 8	— 98 — 15 — 1	-815 - 32 - 2	+425 + 7 - 13			+ 12	— 9
8— 4 9— 4 10— 4 10— 5	- 3 - 1 - 23 - 6	0 - 44 + 7	+ 8 + 27 + 4	+ 4 + 5 ² - 5	39 82	— 25 —153	+ 1	+ 2	— 4	- 5

$ \begin{array}{c} \text{Arg} = \\ i'g' + ig \end{array} $	$(n\delta z)$	$\nu' \times \frac{\mathbf{i}''}{2}$	$(n'\delta z')$	$\nu' \times \frac{\mathbf{I}''}{2}$	$ u^2 angle$	$<\frac{1}{2}''$	νν'	× ½"	$v^{\prime 2}$	$\times \frac{\mathbf{I}''}{2}$
<i>vg</i> + <i>ig</i>	n^2t^2 sin.	n^2t^2 cos.	$n'^2t^2\sin$.	$n'^2t^2\cos$.	n^2t^2 cos.	$n^2t^2\sin$.	$n^2t^2\cos$.	n^2t^2 sin.	$n'^2t^2\cos$.	n'^2t^2 sin.
i' i 0 0 0— I 0— 2 0— 3	8 + 2	- I + 2 + I	2	+ 3	+53 + 4 - 5 o	— 3 —53 — 2	— 3	+ 3	+234 — 2	_ 2
I+ 2 I+ I I 0 I- I I- 2	+279 -5 $+84$ $+21$	+ 52 + 4 -271 + 2	+ 11 o	— 19 + 3			- 3 -140 - 3 + 38 + 3	+ 26 + 4 + 136 + 4	+ 17 0	— 12 — 3
2+ I 2 0 2- I 2- 2 2- 3	+ 8 0 + II - 4	+ 2 + 4 - 3 + 1	+206 - 3 + 4	-420 - 3 + 1	+ 1	+ 1 - 1	- 3 - 1 + 1 + 3	0 - I + 4 + 2	-102 + 2 + 1	-2I0 - 2 0
3 0 3-1 3-2 3-3	+ 13 + 4	— 8 — 11	+ 8 - 2 - 19	- 18 + 6 + 41	- I	+ 1 - 1	+ 1	+ 2	— 6 — 5 — 10	- 12 - 2 - 18

$\operatorname*{Arg=}_{i'g'+ig}$	$(n\delta z)\nu'\times\frac{\mathbf{I}''}{2}$		$(n'\delta z') u' imes rac{1}{2}^{"}$		$ u^2 imes rac{1}{2}^{\prime\prime}$		$\nu \nu' imes rac{1}{2}''$		$v^{\prime 2} \times \frac{1}{2}^{\prime \prime}$	
<i>i'g'+ig</i>	n^2t^2 sin.	$n^2t^2\cos$.	$n^{\prime 2}t^2\sin$.	$n'^2t^2\cos$.	n^2t^2 cos.	n^2t^2 sin.	$n^2t^2\cos$.	$n^2t^2\sin$.	$n^{\prime 2}t^2$ cos.	$n^{\prime 2}t^2\sin$.
i' i 4 0 4- I 4- 2 4- 3 5- I 5- 2 5- 3 5- 4 6- I 6- 2 6- 3 7- 2 7- 3 8- 4 9- 4	- 13 - 26 + 9 - 1 + 11 - 6 +222 - 23 + 13 - 2	+ 10 - 16 + 8 - 5 + 15 - 2 + 118 + 19 + 4 + 2	$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	- 2 - 108 - 2 - 1 - 6	-4 —2	+3 +3	+6 +9 -1 -3 +1 0 -6	+7 -2 -6 -3 +1 -5	-18 + 7 + 3	- I + 8 + 3I - I
10— 4 10— 5 11— 4	+ 1	- 2	- 2 0	+ 4						

CHAPTER XVII.

CALCULATION OF THE SEVERAL PORTIONS OF 8°T.

The fourteen parts of the portion of $\delta^2 T$ not factored by nt or $n^2 t^2$ are as follows:

Aı	·o=	An	$\iota \delta^2 z$	В	δν	$\mathbf{F}n'$	$'\delta^2z'$	Ge	$\delta u'$
μ γ+1	g = i'g' + ig	sin.	cos.	sin.	cos.	sin.	cos.	sin.	cos.
ж o	i' i	11	o. 0000551	"	o. 0000128	"	o. 0001186	,n	., -0.0000415
1	0— і	1	+0.0000052		+0.0000008	-0.0006	-0.0000791		+0.0000109
-1	o o		+0.0013445	—0. 000007 6	+o. ooo3655		+0.0076775	l .	+0.0013968
°	0 I	+0.0007	-0,0016			+0.0028	0.0069	+0.0002	-0.0015
1	0— 2	0.000093	+0.000746		+0,000122	-0.000056	+0.002351		+0.000490
-1	о— 1	0.006	0, 005	l		0.026	0, 020	-0.004	-0.002
°	0 2	+o. oo8	+0.006			+0.028	+0,021	+0.004	+0.002
1	o — 3					0, 008	-0.004		
-1	1+ 2	+0.002	+0.003	l					
0	1+1	0.007	_o. oo6	1		0. 025	O. O2I	—о. 00 3	-0.004
1	1 0	+0.0051	+0.0048	+0.0003	+0.0005	+0.0255	+0.0226	+0. 0040	+0.0051
—ı	1+1	0. 0005	+0.0001			-0.0020	+0.0001	0, 0003	0.0001
0	I o	+0.0012	— 0, 0006	+0.0002	0.0000	+0.0054	0.0033	+0, 0014	0. 0004
ı	1-1	0. 0008	+0.0002	-0. 0002	0.0000	-0.0062	+0.0033	o. 0014	+0.0002
—т	I o	0. 0000	+0.0002			+0.0003	+0.0016	+0.0001	+o. ooo8
0	ı— 1	0.0000	-0.0003			-0.0004	-0.0013	-o. 0002	0. 0003
—т	1— 1	o. o o19	0. 0003			-0.0091	o. oo16	0.0016	+0.0001
o	I— 2	+0.002	0.000			+0.011	+o. ooi	+0.001	0,000
1	I 3	<u>,</u>			!	0, 002	0,000		
—т	I 2	+0.003	0. 007			+0.012	-0.030	1	
٥	I — 3	-0.004	+0.009			-0.012	+0.028		1
1	1-4					+0.003	_o. oo7		
_1	2+ 2					+0.020	+0.005		
0	2+ 1					0.069	-0. 017		
ı	2 0					+0.0728	+0.0164		
	2+ 1	—0. 0019	+0.0020				+o. 0104 +o. 0060	o, ooo8	+0.0010
0	2 0	l	_0.0020 _0.0065	+o. ooo6	-o. ooo5	—0.0055 ±0.0140	o. 0248	+0.0033	_0.0015 _0.0045
1	2 U	+0.0042 -0.0027		_0.0006		+0.0149	+0.0262	o. oo38	+0.0053
	2 0	+0.0002	+0.0038		+0.0005	-0.0163	o. 0006	0.0000	-0.0003
_I		1	-0.0003	±0.00076	10.0000#	+0.0010		+o. oooo6	+0.00051
0	2 1	+0.00026	+0.00056	+0.00016	+0.00027	-0.00024	+0.00185	0.0000	-0.00051
I	2— 2	-0.0001	-0.0001	0.0001	0.0002	0.0000	0, 0026		l . '
-I	2— I	—0.0003	+0,0001			-0.0020	+0.0005	-0,0012	+0.0004
٥	z 2	ł				+0. 0024	-0.0010	+0.0010	0.0004
									272

Aı	rg=	An	$\delta^{2}z$	В	δν	Fn	$'\delta^2z'$	G	$\delta u'$
жу+-	i ^v g'+ig	sin.	cos.	sin.	cos.	sin.	cos.	sin.	cos.
ж — г	i' i 2— 2	// O. 000		"	"	// 0.002		"	"
0 1 0	2— 3 2— 3 2— 4	+0.006 0.008	+0.002 -0.002			0.000 +0.021 -0.020	+0.008 +0.005 -0.005		
0 I	3+ I 3 o					+0.002 +0.002	-0.003 +0.001		
	3 0	0.000 0.0001	+0.013 -0.0306			0.000 +0.0008	+0.019 -0.0705		
-1 1	3— I 3— I	+0.0001 0.0000 +0.00193	+0. 0163 -0. 0016 +0. 00206	0. 0002 +0. 00086	-0.0001 +0.00063	0.0013 +0.0013 +0.00235	+0.0744 -0.0026 +0.00528	+0.0002 +0.0006 +0.00153	0. 0007 0. 0003 0. 00054
1 T	3- 2 3- 1	o. 0009 o. 0000	—0. 0006 —0. 0002	0, 0005	-0.0004	-0. 0043 -0. 0004	-0. 0066 +0. 0009	0.0026 0.0000	-0.000I
-1 I O	3- 2 3- 3 3- 2					0,0017	0. 0024		
-I 0	3-3 3-3 3-4	:				+0.008 -0.008	-0, 002 +0, 002		
—I	3— 4 3— 5					o. 000 o. 000	+0.002 +0.016 —0.016		
-1 I	4— I 4 0	+ 0, 0022	0. 0004			—0, 0022 +0, 0026	-0. 0024 -0. 0005	—o. 0007	—o. ooo1
I II	4— I 4— z 4— I	+0.0023 0.0001	+0.0011			+0.0051 -0.0092 -0.0003	-0.0008 +0.0017 +0.0010	+0.0006 -0.0003 -0.0005	-0.0002 -0.0001 -0.0018
0	4— 2 4— 3	+0.0001 0.0000	—0, 0008 —0, 0005	-o. ooo1	-0.0001	0.0000 +0.0002	+0.0002 -0.0012	+0.0004	+0.0004 +0.0019
o -I	4- 2 4- 3					-0.0013 0.000	-0.0009 +0.001	+0.0004	+0.0004
-1 -1	4- 3 4- 4 4- 5					+0.002 +0.003 -0.012	-0.002 +0.006 +0.002		
0 I	5— I 5— 2	+0.000485	o. ooo695	+o. 000241	-0.000215	o. 0008 +o. 000877	+0.0025 0.002763	o. 0000 +o. 000039	+0.0007 0.000867
I —	5— I 5— 2 5— 3	+0.001427 +0.0006399 +0.001489	+0.003366 +0.0015326 +0.003311	—0. 000211 —0. 0004766 —0. 000269	-0.000510 +0.0011381 -0.000639	0. 000005 0. 0000225 +0. 000108	-0.000172 +0.0002158 +0.000036		-0.000659 +0.0009613
—I	5— 3 5— 2 5— 3	-0.001379 -0.0019	-0.00076 +0.0001	—o. ooo648	-0.000031	-0. 002065 +0. 0029	-0. 00036 -0. 000908 +0. 0007	-0.000207 -0.002835 +0.0025	-0.000504 -0.000527 -0.0005
-I	5— 4 5— 3	0. 0008	0.0001			-0.0010	—0. 0002	+0.0006	+0.000I
I I	5— 4 5— 5 5— 4		,						
0	5— 5								

Aı	rø=	An	$\delta^2 z$	Ва	δν	$\mathbf{F}n'$	5°22'	Gå	ìν'
ну+	rg = i'g' + ig	sin.	cos.	sin.	cos.	sin.	cos.	sin.	cos.
κ I	i' i 6— 2	"	"	u	H	"	11	"	
I	6— 1	+0.0005	+0.0003			-0.0010	-0.000 6		
٥	6— 2	-0.0004	-0,0002			0. 0007	-0.0004	-0.0001	+0.0001
1	6 3	+0.0008	+0,0006			+0,0006	+o. ooo6	-0.0001	0.0000
_ı	6— 2	+0.0002	-0.0002	+0.0004	0.0002	+o. oo76	-o. oo58	+0,0002	⊹ 0, 0004
	6— 3	0.002I	+0,0018	0, 0004	+0.0003	_o. oo35	+0.0032	—u, 0002	0.0001
1	6— 4	-0.0018	+0.0014		, ,	0.0022	+0.0015		
—т	6 3	0.0006	0.0013			+o. 0005	+o. oo38	0,0009	0. 0074
	6 4					0.003	-0.004	+0.001	+0.006
_ı	6— 4	1							
	6— 5								
_r	6— 5	1							
0	6 6								
1					1				
I	7— 3	+0.00085	+0.00011						
—I	7— 2	+0.00004	-0,00022	+0.00004	-0.00014	-0.00212	o. oo68 5	+0.00005	o. ooo16
0	7 — 3	+0.00048	+0.00115	0,00004	+0.00010	+0.00270	+0.00489	0.00000	+0.00026
1	7— 4	-0.0012	-0, 0005	1	i	—о. 0030	-0.0010	-0.0001	+0.0003
—I	7— 3	+0.0119	+0.0109	+0.0002	+0.0001	+0.0549	+0.0528	-0.0002	0.0003
0	7 4	0. 0223	-0.0211			-o. o513	-0.0497	+0.0002	0.0000
1	7— 5	+0.010	+0.009			+0.014	+0.013		
—r	7— 4					0.003	+0.001	+0.005	⊸ 0. 002
٥	7— 5	-0.002	-0.002			+0.002	0. 004	0, 005	+0.002
-1	8— 2	0, 0000	+0.0004			0.0013	0.0014		
0	8 3	+0.00017	-0.00071	—o. oooo3	—o. ooo46	+0.00146	+0.00056	-0.00004	0. 00034
1	8— 4	0,0002	+0.0005			0, 0012	+0,0006	+0.0001	+0.0006
—ı	8 3	+0.0036	+0.0008	+0.0001	0,0000	+0.0236	+0.0059	+0.0004	0. 0003
0	8— 4	0, 0063	-0.0016	İ		-0.0219	-o. oo61		
I	8— 5	+0.0027	0,0000			+0.0064	0,0000		
1	8 4	— 0. 0113	+0.0186	1		 0. 0406	+0.0649	+0.0003	0,0005
0	8— 5	+0.016	-0.027			+0.040	0. 063		
I	8— 6	o, oo6	+0.010			o. oi i	+0.017		
_I	8 5	1				0.001	-0.001	+0,002	+0.004
٥	8— 6	0.000	-0.004			+0.003	0.001		
-I	9 — 3	+0.0005	0.0002			+0.0049	0.0013	+0.0006	-0.0002
٥	9— 4	—0. 00092	+0.00027	<u> </u>		0, 00432	+0.00099	+0.00010	-0.00003
1	9— 5	+0.0003	0.0003			+0.0010	-0.0010	0.0006	+0.0002
-1	9 4	0,0003	+0.0065			0.0030	+0.0291	+0,0006	+0.0006
0	9 5	+0.001	0.010			+0.004	0. 027		
т	9— 6	0, 000	+0.003			+0.001	+0.009		
-1	9— 5	0.019	0.007			0. об1	-0.023		
0	9 — 6	+0.025	+0.008			+o. o56	+0.020		
1	9— 7	0.010	-0.003			o. o17	—0. 006		}
1	9— 6	-0, 002	+0,001			0, 002	0,000	1	
0	9— 7	+0.003	0,000	1		+0.003	+0.002		
		<u> </u>	<u> </u>	<u> </u>	1			<u> </u>	l

Arg		An	$\delta^2 z$	Bě	δν	$\mathbf{F}n'$	$\delta^{2}z'$	Gå	īν'
Arg:	g'+ig	sin.	cos.	sin.	cos.	sin.	cos.	sin.	608.
	i' i 0— 3	// 	// 0. 00032	"	"	// +0.00059	// 0. 00057	.,, —0. 00005	// +0.0000I
	0— 4		+0.0000983	o. 0000001	+0.0000053	, ,,	+0.0004872		+0.0000247
	o— 5	+o. oooo1	0.00006		33	+0.00003	-0, 00025	+0.00004	-0.00006
	0-4	+o. 00055	+0.00124			+0.00248	+0.00618	+0.00034	+0.00052
1	0— 5	-0.0008	0.0016			-0.0029	_o. oo62		
1	ю— 6					+0.002	+0,002		
-I I	0 5	-o. oo8	+0.001			-0.029	+o, oo2		
0 1	0 6	+0.010	_0.002			+0.029	_0.004		
1 1	io— 7	-0.004	+0.002			0.00 8	+0.002		
—I I	o— 6	+0.002	-0.016			+0.006	_0, 046		
0 1	10— 7	0.002	∔0.020			_o. oo5	+0.044		
1 1	o 8	0,000	-0.007			+0.001	o. o13		
							_		
-I I	11 4	+0.0002	+0.0002			∔ 0. 0002	+0,0004	+0.0002	0.0000
0 1	11— 5	0. 0002	0.0001			0.0006	_o. ooo5		
i i	11— 5	0.0015	+0.0011	l		o. oo67	+0.0044		
0 1	11 6	+0.002	0, 002			+o. oo6	0.005		
1 1	11— 7			1		-0.002	+0,002		
—I I	11 6	-0.003	-o. oo7			0.009	_0, 02 5		
0 1	r— 7	+0,004	+0,009			+0.009	+0.024		
1 1	8 — r		ĺ			0.003	-o. oo7		
_I I	11— 7	+0.011	0,001			+0.032	0, 003		
0 1	11— 8	0.013	+0.002			—0. 031	+o. oo 3		
0 1	12 5	+0.00002	o. oo oo8			+0.00012	0.00041	0,00000	0.00000
-I I	12— 5	+0.0003	-0.0009			-o. ooo7	+0.0017		
0 1	12— 6					+0.0007	_o. oo16		
-1 1	2— 6	-0, 002	-o. 0 02			—o. ooუ	-o, oo6		
0 1	2 7					+o, oo6	+0,006	i '	
-1 1	2— 7	+ 0,006	-0. 004			+0.019	0, 011	ļ ,	
0 1	2 8	—о. ооб	+0.004			-o. o18	+0.011		
-1 1	2— 8	+0.002	+0.007			+0.007	+0.019		
0 1	12— 9					o. or	-0. O2	l	
			1	<u></u>			l		!

$egin{align*} ext{Arg}= & \ ext{} arphi \gamma + i'g' + ig \end{aligned}$	$\frac{1}{2}\frac{dA}{dg}$	$n\delta z)^2$	$rac{d{f A}}{dg'}(n\delta z)$	$(n'\delta z')$	$rac{1}{2} rac{d ext{F}}{d g'} (au)$	$(\delta z')^2$	$rac{d\mathrm{B}}{dg}(n)$	$\delta z) u$
**/ T* 9 T*9	sin.	cos.	sin.	cos.	sin.	cos.	sin.	cos.
κ i' i	11	11	11	"	11	11	11	11
0 0 0		+0.0000064		+0.0000019		—0. 0000921		+0.0000037
1 0— 1		-0.0000052		-0. 0000098		+o. 0001557		—o. ooooo 18
I 0- 2		—o. oooo57		0. 000209		—o. 000170		—o. 000051
o 1+1					0, 000	+0.001	:	
-i i+ i			0,0003	0. 0009	+0,0005	0. 0016		
0 1 0			0.0004	+0.0001				
1 1—1	1		4,1114		+0.0001	+0.0001		
					-0.0007	-0.0010		
o I— I						+0.0004		
-1 I- I					+0.0038	-0.0010		
I 2 0					+0.0023	—o. ooo8		
I 2— I	l				+0,0004	+o. ooo8		
_I 2 0					-0.0013	0, 0002		
0 2— 1	+0.00010	+0,00012	+o. 00045	+0.00032	+0.00105	0.00005	+o. oooo3	+o. 00004
I 2— 2	1 0.000	, 0, 00012	1 01 00045	1 0,00032	-0.0003	+0.0003	,5	
_I 2— I			+0.0043	-0.0017	+0.0117	0.0054		
0 2- 2			_o. 0076	+0.0033	-0.0107	+0.0046		
0 3 0					0.0009	_o.oo16		
I 3— I			+0.0005	+0.0003		+0.0028		
-I 3 O					_o. ooo6	+0.0003		
0 3— 1	-0.00014	-0.00005	-0.00014	~-o. 00027	+0.00076	-0.00044	-0.00011	-0.00004
I 3- 2		1			0. 0005	+0.0003		:
—ı 3— ı	1		+0.0016	_o. 0019	+0.0049	0. 0067		
0 3-2	1		-0.0028	+0.0035	-0. 0044	+0.0059		
I 3-3	1	1			⊹о. оо об	_o. oo13	1	
—1 3— 2	+0.0007	+0.0010			+0.0109	+0.0154		
0 3-3	-0, 002	-0.002			-0.010	_o. o13		
1 4-1					+0.0041	+0.0041		
5 4— I					+0.0009	-0.0010	1	
I 4— 2	1				-0,0014	+0.0013		
_r 4— r			+0.0001	-o. ooo7	+0.0002	-0. 0027]
0 4— 2	0,0000	+0.0002	_0.000I	+o. ooo8	-0.0003	+0.0023		
I 4— 3	1				0.0002	-0.0004		
—I 4— 2	+0.0003	+0.0002	+0.0048	+0.0022	+0.0120	+0.0062	1	
0 4-3			0. 006	-0, 002	0. 011	0. 005		
o 5— 1			+o. ooo5	0. 0014	+0.0022	-o. oo35		
I 5— 2	-o. ooo156	+0.000169		+0.001571	-o. oo26o9	+0.003926	0.000079	+0.000079
_1 5— 1	+0.000080		+0.000263	+0.000440	0.000161	—0. 0 00688		+0.000141
0 5-2		-0. 0004691	ı	-0. 0009403	1	+0.0007807	-0. 0001234	-o. 000325 7
ı 5— 3	+0.000087	1	I .	+0.000468	-0.000408	0, 000546		+0.000123
	<u> </u>		<u> </u>	!	1	I	<u> </u>	1

	$\frac{1}{2}$	$rac{d ext{A}}{d g} (n \delta z)^2$	$rac{d\mathbf{A}}{dg'}(n\delta z)$	$)\left(n^{\prime }\delta z^{\prime } ight)$	$\frac{1}{2} \frac{d\mathbf{F}}{dg'}$	$n'\delta z')^3$	$rac{d\mathbf{B}}{dg}(n$	$\delta z) u$
<i>*Y</i> + <i>t y</i> +	sin.	cos.	sin.	cos.	sin.	cos.	sin.	cos.
π i' -1 5- 0 5-	1 ·	+0.000026	+0. 002108 -0. 0027	+0. 000288 -0. 0006	,, +0. 005902 -0. 0054	,,, +0,000863 0,0007	// +o. 000075	+0.000005
I 5-	- 4		-0.001	+0.005	+0.0007 0.003	—0. 0003 +0. 015		
1 5	- 4 - 5 - 4		+0.002 -0.009	o. 007 o. 005	+0.004 0.000 0.015	0. 015 +0. 003 0. 009		
0 5-	- 5 - 2		+0.011	+0.006	+0.015	+0.008 +0.0075	:	
n 6	+0.0001 - 3		+0.0007 0.0002	+0.0005 -0.0002	-0.0025 +0.0014 -0.0018	+0.0010		
o 6_	- 2 -0.0003 - 3 +0.0003		-0.0003 +0.0002 +0.0001	+0.0003 -0.0004 +0.0032	+0.0016 -0.0017 +0.0005	0. 0005 +0. 0004 +0. 0081	-0.0001 +0.0002	+0.0001 -0.0002
o 6-	- 4 - 4		o. ooo —o. oo6	0. 002 0. 000	o. 000 —o. 016	0. 008 0. 001		
r 6-	- 5 5 6		+0.008 +0.003 -0.003	-0.000 -0.009 +0.011	+0.012 +0.004 -0.004	+0.001 -0.014 +0.013		
	- 2 - 3 -0.000	-0.00002	+0.0029 -0.00181	+0.0003 -0.00025	+0.0045	+0.0006	0.00011	-0.00001
0 7-	- 2 - 3 - 4	-0.00006	-0.00013 -0.00008	+0.00027 -0.00006	+0.00030 0.00052 +0.0004	-0.00030 +0.00019 -0.0001	+0.00001	—o. oooo6
-I 7-	- 3 - 4 +0.000	+0.0003	0. 0002	+0.0005	0.0010	+0.0025	+0.0001	0, 0001
	- 4 - 5		-0.002	+0.001	0. 009 +0. 004	+0.002 -0.002		
—ı 8– —ı 8–	- 3 +0.000 - 3 -0.000 - 4 - 6		-0.0009 -0.0004 +0.005	+0. 00058 0. 0000	-0.00029 +0.0004 -0.0028 +0.009	+0.00033 +0.0004 +0.0022 -0.004	+0.00001	+0.00012
	- 3 - 4		+0.00016	-0, 00004	+0.0001 0.00004	+0.000I		
-1 10-	- 4 +0.000	0014 -0.0000006	+0.000029	_o. oooo3o1	+0.00002 -0.0000468 +0.00004	+0.00005 -0.0000532 -0.00001	+0.0000011	-0.0000019
—I IO—		-0.00004	-0. 00029 +0. 00010	-0. 00009 -0. 00012	-0.00101 +0.00033	-0.00021 -0.00035	-0.00002	-0,00002
—I I2-	- 5		+0.0008 -0.0014	-0.0020 +0.0038	+0.0021	-o. ∞63		

Arg ny+i's	;= a/ 1 ÷ a	$rac{d\mathrm{B}}{dg'}(n')$	$\delta z') u$	$rac{d\mathrm{G}}{dg}(n\delta)$	δz)ν'	$rac{d\mathrm{G}}{dg'}(n')$	$\delta z') u'$	$\frac{1}{2}r^2\frac{d^2}{dr}$	$rac{\Gamma}{2} u^2$
hy+rg	y +1y	sin.	cos.	sin.	cos.	sin.	cos.	sin.	cos.
ı	i' i o o o o I o 2	"	// +0.0000153 -0.0000119 -0.000059	u.	+0. 0000173 -0. 0000068 -0. 000210	"	0. 0000316 0. 0000258 0. 000317	"	+0.000001 +0.000012 -0.000012
-1 0 -1	I 0 I 1 I 1 I 1 I 1 I 1 I 1 I 1 I 1 I 1	+0.0001	0, 0000			-0.0011 +0.0002 +0.0002 -0.0021	0. 0006 0. 0004 0. 0002 0. 0002		
I	2— I 2 O 2— I 2— I	+0.0002 0.0001 +0.00003	-0.0003 -0.0002 +0.00013	0.00010	—o. 00009	+0.0007 -0.0002 -0.00009 -0.0006	-0.0003 -0.0003 -0.00003 +0.0004		
o -i	3- I 3 0 3- I 3- 2 3- I 3- 2 3- 2	+0.0002 -0.00023 +0.0002 +0.0003 -0.0003	-0. 0004 -0. 00015 +0. 0003 -0. 0002 +0. 0003	—o. 00023	—o. ooo15	+0.0006 -0.0002 -0.00045 +0.0005 +0.0012 -0.0012 -0.0008	+0.0009 0.00000.00041 +0.00040.0015 +0.00140.0009		
0 1 	4— I 4— I 4— 2 4— I 4— 2 4— 2 4— 3	o. 0000 o. 0000	0, 000I 0. 000I			+0.0014 -0.0006 +0.0006 0.0000 -0.0001 +0.0023 -0.002	+0.0013 -0.0002 +0.0006 -0.0008 +0.0005 +0.0012 -0.001		
-1 0 1 -1	5— I 5— 2 5— I 5— 2 5— 3 5— 3 5— 3	-0.000359 +0.000197 -0.0003058 +0.000130 +0.000297	+0.000415 -0.0007671	+0.000011 0.0000245 0.000047	+0.000325 -0.000028 -0.0001270 -0.000038 +0.000088	+0.0008 -0.001096 +0.000221 -0.0001538 -0.000053 +0.001013 -0.0013	+0.000203 -0.0003436	+o. 0000055	+o. ooooo8o
-i o	6— 2 6— 3 6— 2 6— 3 6— 3		+0.0001 +0.0003 0.0004			+0.0007 -0.0008 -0.0006 +0.0004 -0.0003	+0.0006 -0.0007 +0.0006 -0.0005 +0.0018		

A:	rg= i'g'+ig	$rac{d \mathrm{B}}{d g'} (n' \delta z') u$		$rac{d\mathrm{G}}{dg}(n\delta z) u'$		$rac{d \mathrm{G}}{d g'} (n' \delta z') u'$		$\frac{1}{2}r^4\frac{d^2\Gamma}{dr^2}r^4$	
	. 9 1 . 9	sin.	cos.	sin.	cos.	sin.	cos.	sin.	00a.
и o	i' i 7— 2	11	"	"	"	,, +o. 0018	+0.0003	11	11
1	7- 3	-0.00040	-0.00005	0, 00043	-0.00005	-o. oo 187	0, 00024		
-1	7— 2	—0. 00007	+0,00023			-0.00011	+0.00039		
0	7— 3	+0.00001	0.00014	0.00003	-o. oooo3	—o, oooo6	-0.00037		
ļı	7— 4					+0.0002	0, 0002		
—I	7— 3					0.0011	-0.0009		
٥	8— 3	0. 00000	+0.00024	+0.00001	+0.00007	-0.00002	+0.00009		
-1	8 3	o. ooo3	0.0000			-0.0007	-0.000I		
⊸ I	8— 4					+0.0015	-o. oo16		
_i	9— 3 9— 4	+0.00010	-o. oooo5			-0.0002 +0.00013	o. 0000 o. 00006		
oi	10— 4 10— 4	1	1	+0. 0000082 +0. 000001	-0.0000114 -0.000003	+0.0000323 +0.00013	-0.00004I1 -0.00008		

$Arg = n\gamma + i'g' + ig$	$rr'rac{d^{2}}{dr}$	$rac{\Gamma}{lr'} u u'$	$\frac{1}{2}r'^2\frac{d^2\Gamma}{dr'^2}\nu'^2$			
	sin.	608:	sin.	cos.		
 κ i' i ο ο ο I ο - I I ο - 2 -I I ο -I 2 ο ο 2 - I -I 2 - I ο 3 - I -I 3 - I I 5 - 2 -I 5 - I 5 - 2 I 5 - 3 			0.0000 +0.0001 -0.00009 -0.0007 -0.00025 0.0000 -0.000181 -0.000043 +0.0000575 -0.000058	" +0.0000219 -0.0000268 -0.000058 +0.0000 -0.00008 +0.0002 -0.00013 -0.0002 +0.000126 -0.000045 +0.0000446 -0.000055		
—I 5— 2 □ 7— 3 □ 10— 4	+0.000029 0.00003 +0.0000004	+0.00006 +0.00006 -0.0000015	+0.000292 +0.0000001	—0, 000055 —0, 0000008		

ŗ

The fourteen parts of the portion of δ^2 T factored by nt follow; for convenience the coefficients have been multiplied by 100000:

Arg=	$\mathbf{A}n$	$\delta^{z}z$	Ва	δν	Fn'	$\delta^{_2}z'$	Gδ	ν'
$\mu y + i^7 g' + ig$	nt sin.	nt cos.	nt sin.	nt cos.	nt sin.	nt cos.	nt sin.	nt cos.
и i' i	"	o. 3108	"		"	// 0. 9327	"	" —0. 1447
1 0— I	+ 0.0850	+ 0.3178	+0.007 9	+o. 1385	+ 0. 2281	+ 1.3868	o. oo81	+0. 2255
_I 0 0	— I. 8586	— o. 9437	o. 5523	-0. 2297	- 8. 6483	— 4. 8762	2. 2695	—1. 1106
0 0— 1	+ 1.7	+ 0.9	00 0	,,	+ 7.9	+ 4.7	+2.2	+1.0
I 0— 2	— I. I5	— o. 39	_o. 14	0.03	- z. 8 ₃	— o. 87	—o. 34	-0.13
1 о 1	+ 4	4			+20	—2 I	+3	3
0 0— 2	— 6	+ 5			—20	+20	— 3	+3
1 0— 3					+ 4	— 6		
I O 2	+ 6	+10			+16	+30		
o o 3	 7	—12			—17	28		
1 0-4					+ 6	+ 9		
_I I+ 3	— 7	- 2			12	— 5		
0 I+ 2	+17	+ 6			+42	+13		
1 1+1	—13	4			—44	-13		
-I I+ 2	+ 2	— 2			+ 5	- 7		
0 1+1	- 4	+ 7			—15	+24	-3	+4
1 1 0	+ 3.4	— 5.0	+0.5	-o. 7	+16.4	—25. 3	+2.7	4.0
-ı ı+ı					+ 0.5	+ 1.6	-0. z	0.0
0 1 0	I.2	— 1.5	o. 2	-o. 4	— 3⋅4	4. 2	—о. 7	0. 9
1 1-1	+ 0.5	+ 0.7	+0.4	+o. 5	+ 3.7	+ 4.6	+1.2	+1.6
-1 I o					2.3	+ 0.2	o. 7	+o. 1
o 1— 1					+ 2.3	0.0	+0.3	—o. I
-ı ı- ı	+ 0.5	— I.8			+ 3.3	— 9· 5	+0.7	−3.5
0 I— 2 —I I— 2	— I + 5	+ 1 + 3			— 3 +21	+11 +13	—I +3	+2 +2
0 1-3	— 6	- 3			20	— 13	13	1-
1 1-4		J			+ 5	+ 3		
_1 I— 3	— 6	+ 6			18	+15		
o I— 4	+ 7	— 7			+16	— 1 6		
1 2+ 1					+ 3	_ 2		
_I 2+ 2	0	- 9			+ 2	-16	[
0 2+ 1	1	+22			<u> </u>	+53		
I 2 0	'	-15.4			+ 4.2	—55. I	+1.2	Lor
-I 2+ I 0 2 0	+ 1.7 6.2	+ 1. 1 - 2. 5	-1.0	— 0. 5	+ 5.5 -21.9	+ 3.6 8.6	+1.2 -5.3	+0.5 -2.2
1 2— 1	+ 3.7	+ 1.9	+0.9	+0.5	+23.6	+ 9.7	+5.5	+2. I
_I 2 0	- 0. 24	- 0.10	+0.07	_o. o8	I. 00	- 0.40	+0.40	o. 8o
0 2— I	+ 0.36	- o. 16	+o. I2	0. 05	+ 1.88	— o. 17	+o. 26	+0.09
I 2— 2	O. 2	+ 0.1	0.2	+o. 1	- 2.2	+ 0.4	0.9	+o.5
-1 2- I	— o. I	- o. 3			- 0.3	- 2.4		
0 2— 2					+ 0.5 + 6	+ 2.0 + I	I	
-I 2- 2 0 2- 3			<i>t</i>		— 6	— I	1	
_I 2— 3					6	+14	1	
0 2-4			Į		+ 6	-14		
					1	1	<u> </u>	

Arg=	An	$\delta^2 z$	Вб	ìν	$\mathbf{F}n'$	$\delta^2 z'$	Gδ	ν'
$\varkappa \gamma + i^{\prime} g^{\prime} + i g$	$nt \sin$.	nt cos.	nt sin.	nt cos.	nt sin.	nt cos.	nt sin.	nt cos.
ж i' i I 3 о	"	"	"	"	+ 1"	+ 1"	"	"
O 3 O 3 O 3 O 3 O 1	$\begin{array}{c} + 9 \\ -21.7 \\ +11.5 \end{array}$	I + 3.0 I.6			+14 -51.5 +54.7	-2 + 6.8 - 7.3	+1.9 -2.0	0.3 +-0.3
-I 3 0 0 3- I	- I. I + I. 20	+ 0.7 - 2.35	—0. I →0. 29	+0.3 —1.13	- 2. 1 + 3. 63	0.8 2.29	+0.11 +0.1	0. 7 0. 99
I 3-2 -I 3-I 0 3-2	- O. 2	+ 1.1	-0. 2	+1.0	— 4·4 + 0·9 — 0·9	+ 4.2 + 0.4 - 0.7	-0. 2 +1. 4 -0. 9	+2.0 +0.9 -0.6
-1 3-2 -1 3-3 0 3-4					+ 2.3 + 1 - 1	1.0 + 6 6		:
o 3-4 -1 3-4 o 3-5					—12 +11	— 2 + 2		
1 4- 1 -1 4 0 0 4- 1	- o. 5 - o. 5	— 1.6 — 1.6			- 0.5 - 0.6 - 1.4	- 0.4 - 1.8 - 3.7	- - 0. I	+o. 3
1 4— 2 —I 4— I	+ 0.5	- o. I			+ 2.4 + 1.1	+ 6.7 + 0.1	—0. I +2. 3	-0. 5 0. 0
0 4-2 1 4-3 -1 4-2 0 4-3	+ 0.15	0.00	+0. 27	+0.01	0. 30 0. 9 0. 1	0. IO 0. O 0. 9 + I	0. 24 2. 0 0. 5	-0.01 0.0 +1.8
I 5-2 -I 5-I 0 5-2	+ 0.030 + 2.749 - 0.0328 + 2.734	+ 0.018 - 1.662 - 0.0050 - 1.656	+0.014 -0.007 +0.0068 +0.001	+0.005 +0.008 -0.0094 +0.007	+ 0. 179 - 0. 002 - 0. 0701 + 0. 133	+ 0. 185 + 0. 111 - 0. 0348 - 0. 050	-0. 167 -0. 313 -0. 0689 +0. 404	-0. 145 +0. 172 +0. 0230 -0. 249
o 5-3 -1 5-3 -1 5-3	+ 0.005	+ 0. 267	+0.083	+0.377	- 0. 695 + 0. 1 + 2	- 1. 330 + 0.5	+0. 341 0. 2	+2. 407 -1. 2
i 6 i i 6 3 i 6 2		— o. 3			- 0.3 + 0.4 - 5.5	+ 0.8 0.7 5.4	+0.2	о. з
o 6— 3 i 6— 4 —i 6— 3 o 6— 4	+ 1.1	+ I. 2 + I. 2			+ 3. I + 1. 4 + 7. 8 - 7	+ 2.9 + 1.4 - 2.7 + 3	0. 2 5. 9 +5	+0.3 +2.6 -2
o 6-4 1 7-3 -1 7-2 0 7-3		- 0.47			+ 0.08 - 5.04 + 3.46	- 0. 28 + 2. 17 - 2. 27	—0. 31 —0. 17	-0.07 +0.02
1 7— 4 —1 7— 3 o 7— 4	$\begin{array}{c} -0.3 \\ +6.7 \\ -12.7 \end{array}$	+ 1.0 - 9.4 +17.8			- 0.6 +33.8 -31.9 + 8	+ 2. I -46. 9 +44. 0	+0.4 -0.4	-0.4 +0.4
1 7— 5 —I 7— 4 0 7— 5	1	- 7			+ 3 - 4	-12 + 5 - 6	-3 +3	-4 +4

Arg=	$\mathbb{A} n \delta^2 z$		$\mathrm{B}\delta\nu$		$\mathbf{F} n' \delta^2 z'$		$G\delta\nu'$	
$ \mu y + i'g' + ig $	$nt \sin$.	nt cos.	$nt \sin$.	nt cos.	$nt \sin$.	nt cos.	$nt \sin$.	nt cos.
κ i' i —1 8— 2	"	"	11	"	" 0.9	+ 1.1	11	"
0 8 3	+ 0.08	— o. 13			+ 0.66	- 1.00	+0.03	0. 04
ı 8— 4	0.0	+ 0.1			+ o. 1	+ 0.6		
—ı 8— 3	+ 0.3	- 2.5			+ 1.9	—19. I	+0.2	— о. 9
0 8—4	0.5	+ 4.6			— 2·4	+17.4	—о. 1	+1.o
1 8— 5	— o. 3	— I. 9			0.6	- 4.6		
—I 8— 4	+14.2	+ 6.2			+53.2	+23.8	0,0	+o. 1
o 8— 5 1 8— 6	20 0	- 8			52	—22	+2	+1
_1 8— 5	+ 8	+ 3			+14 + 3	+ 6		
						_ 2		
—ı 9— 3		- 0.3			— I. 7	- 3.5		
0 9— 4 1 9— 5	+ 0.27 - 0.3	+ 0.63 - 0.2			+ 1.33 - 0.8	+ 3.22 - 0.6	+0.06	+o. 13
-I 9-4	- 0.3 + 4.7	- 0. 2 - 0. 5			+23.7	- 0.0 - 2. I		
0 9— 5	— 7	٥			-21	+ 2		
1 9—6	+ 2	0			+ 6	- I		
—ı 9— 5	— 3	+14			-11	+48		
o 9-6	+ 3 1	—18 + 6			+ 9 2	<u>46</u>		
						+12		
—I IO— 3	- 0.04	— 0, 03			— o. 55	o. 36	-0.02	-0.02
0 10— 4 1 10— 5	+ 0. 0646 - 0. 05	+ 0, 0489 0, 00	—0. 0026	-0.0013	+ 0. 4684 0. 18	+ 0. 3523 + 0. 02	+0. 0281	+0.0240
—I IO— 4	+ 0.73	- 0. 53			+ 4· 79	- 3.33	+0. 20	0. I4
0 10-5		+ 0.8			— 4. 2	+ 2.8		
1 10—6					+ 1	_ I		
—I IO— 5	+ 2	+ 6			+ 6	+22		
0 10—6	- 2	— 7			- 6	—2I		
1 10— 7 —1 10— 6	12	o			+ 2 -34	+ 6 o		
0 10-7	+13	0			+33	_ I		
1 10—8					-10	+ 1		
—I II— 4					+ 0.4	- 0.9		
0 11-5					- 0.4	+ 0.8		
-I II- 5	+ 1.0	+ 0.9			+ 4.6	+ 4.4		
o 11— 6	- I - 5	+ 1 + 3			— 4 —17	一 4 十 9		
0 11-7	-	3			+16	- 9		
. 1 11 8					— 5	+ 3		
_1 11 <u></u> 7		_ 8			— 6	-23	[
0 11—8	+ 3	+ 9			+ 6	+22		
o 12— 5	0.00	+ 0.03			+ 0.01	+ 0.15		
—I I2— 5	+ 0.2	0.0			+ 1.3	+ 0.3		
0 12— 6 —1 12— 6					— 1.3 — 4	— 0.4 + 5		
0 I2— 7					- 4 + 4	+ 3 - 5		
I I2 7					-10	—12		
o 12—8			per .		+10	+12		
_1 12— 8					+13	— 7		l
0 12-9	ļ				—1 3	+ 8		ļ
				1			<u> </u>	

	$rac{1}{2} rac{d { m A}}{d g} (n \delta z)^2$		$rac{d \Delta}{d g} (n \delta z) (n' \delta z')$		$rac{1}{2} \; rac{d ext{F}}{d g'} (n' \delta z')^2$		$rac{d\mathrm{B}}{dg}(n\delta z) u$	
	$nt \sin$.	nt cos.	nt sin.	nt cos.	nt sin.	nt cos.	$nt \sin$.	nt cos.
κ i' i ο ο ο ι ο— ι —ι ο ο	-0.0005	,,, +0. 0899 -0. 0845 -0. 0786		+0. 3707 -0. 3789		+0. 4147 -0. 5776	+0.0043 +0.0841	// +0. 0664 0. 0623 0. 0005
0 0— I I 0— 2 —1 0— I	+0. 1116 +0. 08	0. 0780 0. 08	+0. 9086 +0. 48	+0.2789 +0.07	-1.3 +0.66 -2	+0. 7933 -0. 4 +0. 14 +2	+0.03	—o. oı
0 0-2 0 1+1 1 1 0 0 1 0 1 1-1 -1 1 0 0 1-1 -1 1-1 0 1-2			-I. I +0. 5 -0. 2	+1.2 +0.8 -0.4	+2 +2 -2.3 +0.6 -0.6 +0.9 -0.9	-2 +2.6 +1.0 -1.1 -0.1 +0.1 +2.4 -2		
0 2 0 1 2— I —I 2 0 0 2— I —I 2— I	0. 09	0.01	+1.5 -1.0 -0.09 -0.37 +0.2	+0.7 0.6 +0.09 +0.23 +0.3	+1.4 -1.9 +0.29 -0.38 +0.1	+0.9 -1.2 -0.14 +0.07 +1.5	-0. I +0. OI	0. I 0. 00
I 3— I —I 3 0 — 3— I —I 3— 2 —I 3— I	—o. 18	+o. 16	0. 0 0. 07 0. 0	-0. 2 +0. 56 -0. 3	-1.4 -0.13 0.0 +0.1	0.0 +0.12 -0.1 +0.6	—o. 11	+0.07
i 4— 2 o 4— 2			+ 0.09	+0.01	+0.1	o, I		
I 5-2 -1 5-1 0 5-2 I 5-3 -1 5-2	-0.003 -0.0328 +0.012 -0.023	+0.008 +0.0118 -0.008 -0.035	+0. 198 +0. 028 -0. 0566 +0. 040 -0. 162	+0. 132 +0. 005 -0. 0211 0. 000 -0. 067	+0. 409 -0. 031 +0. 0271 -0. 018 -0. 361	+0. 219 +0. 053 -0. 0663 +0. 027 -0. 318	-0.017 +0.0160 +0.008	0. 006 0. 0196 0. 017
-I 6- 2 -I 6- 3					-0.2 +2.0	o. o o. 7	, i	
I 7— 3 —I 7— 2 D 7— 3	+0. 26	0. 02	0. 12 0. 28	-0.06 +0.13	0. 01 0. 22 +0. 16	+0.69 -0.02 +0.05	+0. 15	0. 01
o 8— 3 —1 8— 3 n 8— 4	+0,04	-0.03	+o. o8	0.00	+0.12 +0.4 -0.3	-0.08 -1.8 +1.7	+0.02	-0. 02
ø 9 4			+0.09	+0.38	+0. 23	+0.78		
—I IO— 3 D IO— 4 I IO— 5	+0.0202	+0.0082	0, 04 +0. 0608 0. 02	0. 03 +0. 0697 0. 00	—0. 19 +0. 1725 —0. 06	-0. 16 +0. 1730 -0. 02	+0.0148	+0.0027
—I IO— 4			+o. 45	0. 25	+1.48	<u></u> 0. 75	+0.003	o. oo6

$rac{ ext{Arg}=}{arkappa y+i'g'+ig}$	$rac{d\mathrm{B}}{dg'}(n'\delta z') u$		$rac{d \mathrm{G}}{d g} (n \delta z) u'$		$rac{d\mathrm{G}}{dg'}(n'oldsymbol{\delta}z') u'$		$rac{1}{2}r^2rac{d^2\Gamma}{dr^2} u^2$	
iy+i'g'+ig	nt sin.	nt cos.	$nt \sin$.	nt cos.	nt sin.	nt cos.	nt sin.	nt cos.
ж i' i о о о п о— п —п о о	+0. 0264 +0. 3933	" +0. 1647 —0. 1789 —0. 0976	" —0. 0127 +0. 4761	" +0. 1924 -0. 1857 +0. 0617	-0. 0527 +1. 5418	+0. 3172 -0. 4351 +0. 3467	+0. 0014 +0. 0065	+0. 0132 -0. 0130 -0. 0035
0	+0.11	—о. оз	+0.20	+o. o3	-1.8 +0.43 +1	0. 5 +0. 09	0.00	+0.01
1 1 0 0 1 0 1 1 1 1 0 0 1 1 1 1 1 1 1 1	0.0	∔0. 2	-0.4 0.0	+0.4 +0.2	-1.5 +0.5 -0.5 +0.9 -0.6 -0.1	+1.5 +1.0 -1.2 0.0 +0.1 +2.0	•	
0 2 0 I 2— I —I 2 0 0 2— I I 2— 2 —I 2— I	+0.3 -0.2 -0.23	+0.5 -0.4 +0.06	+0.5 0.3 0.08 0.15	+0.3 -0.2 +0.12 -0.04	+1.2 -1.3 +0.06 -0.22 +0.2 +0.2	+0.9 -0.8 +0.07 -0.02 0.0 +1.2	+o. o1	-0.02
1 3- I 0 3- I I 3- 2 -I 3- I	-0. 27 +0. 2	+0.2I 0.2	—o. oz	-0.02	+0.6 0.01 +0.1 +0.1	+0. I +0. 04 -0. 3 +0. I		
I 4— 2 0 4— 2					0. I +0. 09	+0. I -0. 02		
I 5— 2 —I 5— I 0 5— 2 I 5— 3 —I 5— 2	+0.009 -0.0417 +0.020 -0.068	+0. 029 -0. 0079 +0. 004 -0. 049	+0. 042 +0. 027 -0. 0480 +0. 003 -0. 026	+0. 031 +0. 021 -0. 0168 +0. 025 -0. 094	+0. 385 +0. 060 +0. 0102 -0. 060 -0. 067	+0. 315 -0. 003 -0. 0294 +0. 018 +0. 096	+0.0016	-0.0012
—I 6— 2 —I 6— 3 — 6— 4					+0.2 -0.2 +1	0. 0 +0. 3 -1		
-I 7-2 0 7-3 -I 7-3	-0. 31 +0. 40	+0.01 -0.04	+0.06	+0.02	-0. 25 +0. 09 -0. 4	-0. II +0. 07 +0. 4		
o 8— 3 —I 8— 3 o 8— 4	+0.13	0.11	o. I	+0.5	+0.07 +0.3	-0. IO -1. 4		
-I 9-3 0 9-4 -I 9-4 0 9-5	+ 0. 19	+0. 15	+ 0. 06	+0.13	-0. 2 +0. 22 +1. 9 -2	-0. 5 +0. 43 -0. 1		
-I IO- 3 0 IO- 4 I IO- 5 -I IO- 4	-0. 06 +0. 0619 -0. 01 +0. 14	0.00 +0.0067 +0.01 -0.27	+0. 0169 +0. 15	+0. 0111 -0. 10	-0. 11 +0. 0945 -0. 03 +0. 71	-0. 06 +0. 0607 +0. 01 -0. 50		

$egin{arg} ext{Arg}= \ ext{} arkappa arphi' ec{y}' + i argamma \end{aligned}$	$rr'rac{d^2}{dra}$	$rac{ ext{T}}{ ext{l}r'} u u'$	$rac{1}{2}r'^2rac{d^2\Gamma}{dr'^2} u'^2$			
uy+i'g'+ig	$nt \sin$.	nt cos.	$nt \sin$.	nt cos.		
 κ i' i ο ο ο I ο— I I ο— 2 I ο I ο I ο I ο I ο I ο I ο I ο I ο I ο I ο I ο I ο I ο I ο I ο I ο I ο I ο I ο I ο I ο I ο I ο I ο I ο I ο I ο I ο I ο I ο I ο I ο I ο I ο I ο I ο I ο I ο I ο I ο I ο I ο I ο I ο I ο I ο I ο I ο I ο I ο I ο I ο I ο I ο I ο I ο I ο I ο I ο I ο I ο I ο I ο I ο I ο I ο I ο I ο I ο I ο I ο I ο I ο I ο I ο I ο I ο I ο I ο I ο I ο I ο I ο I ο I ο I ο I ο I ο I ο I ο I ο I ο I ο I ο I ο I ο I ο I ο I ο I ο I ο I ο I ο I ο I ο I ο I ο I ο I ο I ο I ο I ο I ο I ο <l< td=""><td>+0. 0131 +0. 1481 +0. 10 +0. 2 -0. 06 -0. 06</td><td>" +0. I03I -0. I147 -0. 0014 +0. 02 -0. I +0. 08 -0. 06 -0. 04</td><td>" +o. o138 +o. 6303 +o. 19 +o. o5</td><td>" +0. 0950 -0. 1315 +0. 1561 +0. 06</td></l<>	+0. 0131 +0. 1481 +0. 10 +0. 2 -0. 06 -0. 06	" +0. I03I -0. I147 -0. 0014 +0. 02 -0. I +0. 08 -0. 06 -0. 04	" +o. o138 +o. 6303 +o. 19 +o. o5	" +0. 0950 -0. 1315 +0. 1561 +0. 06		
I 5-2 -I 5-I 0 5-2 I 5-3 -I 5-2 0 I0-4 -1 I0-4	-0.00 7 +0.0163 +0.016 -0.009 -0.0028	+0.012 -0.0023 -0.019 -0.058 -0.0007	+0.040 -0.005 +0.0324 -0.017 +0.020 -0.0040 -0.005	+0.046 +0.003 -0.0279 +0.008 -0.209 -0.0037 +0.001		

The fourteen parts of the portion of δ^2 T having the factor n^2t^2 follow; for convenience the coefficients are multiplied by 100000000:

Arg=	$\mathbb{A} n \delta^2 z$		$B\delta u$		$\mathrm{F}n'\delta^2z'$		$G\delta u$	
$n\gamma + i'g' + ig$	n^2t^2 sin.	n^2t^2 cos.	n^2t^2 sin.	$n^2t^2\cos$.	$n^2t^2\sin$.	n^2t^2 cos.	$n^2t^2\sin$.	nºtº cos.
κ i' i ο ο ο ι ο— ι	+0.020	+0. 022 +0. 025		+0.006 -0.015	o. 417	o. o31	+ 1.503	+ 0.065
-I 0 0 I 0-2	+0. 301 +0. 3	0. 515 0. 5	+0. 299 -0. 3	—0. 506 +0. 5	— 0. 726 + 0. 2	+ 1.644 - 0.5	+ 1.821 - 0.5	— 3.871 + 1.2
-1 1-1 I I-1					—¹3	— 3	+ 3 +12	2 + 2
-I 2 0 0 2-I -I 2-I	—2 +3⋅3	—I +2.4	—2 +1.9	-2 +1.4	— I + o.7 — 4	— I + 0.6 + I	$ \begin{array}{r} -3 \\ + 1.6 \\ + 2 \end{array} $	— 3 + 1.5 — 1
o 3— I —I 3— o 3— 2	+0.8 +1 -2	+0.4 -2 +4	+0.6 0	0. 1 2	+ 0.7 + 7 - 6	— o. 6 —II +II	+ 0.7 + 6 - 6	- 0.5 -10 + 9
-I 4- I 0 4- 2 -I 4- 2	+1	+1			+13 o	- 5 + 3 + 4	ю н 9	- 3 + 3 + 3
-I 5- I 0 5- 2 I 5- 3 -I 5- 2	—0. 10 +0. 069 —0. 08 +0. 99	-0. 13 +0. 203 -0. 06 -0. 20	0. 11 +0. 085 +0. 65	—0. 09 +0. 107 —0. 26	- 0.61 + 0.489 - 0.27 + 6.08	- 1.08 + 1.022 - 0.20 - 1.06	- 0.44 + 0.352 + 4.09	- 0.56 + 0.546
-I 7-3 o I0-4					+ I 0,009	+ 1 + 0.010		,

$rac{ ext{Arg}=}{\kappa y + i'g' + i'g'}$		$\frac{1}{2}\frac{dA}{dg}$	$(n\delta z)^2$	$\frac{d\mathbf{A}}{dg'}(n\delta z)$	$(n'\delta z')$	$rac{1}{2}rac{d\mathbf{F}}{dg'}($	$n'\delta z')^2$	$rac{d\mathbf{B}}{dg}$ (n	$\delta z) u$
$\mathcal{N} + i'g' - \mathcal{N}$	+ig	$n^2t^2\sin$.	$n^2t^2\cos$.	$n^2t^2\sin$.	n^2t^2 cos.	n^2t^2 sin.	n^2t^2 cos.	n^2t^2 sin.	n^2t^2 cos.
ж i ' 0 0	; 0	"	+0.010	"	o. 014	, , , , ,	// 0. 045	11	+0.008
I 0-	- I	+o. o35	-0.010	о. 007	0. 007	—o. 151	+0.024	O. OOI	-0.011
—ı o	0	+0.∞5	+0.085	0. 047	+0. 127	0. 681	+1.002	+0.019	+0.035
1 0	2	0, 0	+0.1	0.0	+o. 1	—о. 1	+o. 3		
0 2-	- т					+0.3	0, 0		
—I 2—	— І					+3	—I		
0 3-	- I			+0.5	o, I	!			
0 4-	- 2					0	+1		
—ı 5-	- г	o. o8	о. от	0. 17	—о. 14	-0.40	—о. 78	о. 11	o. o3
B 5-	- 2	+0.132	+0.033	+0. 244	+0. 202	+0. 329	+o. 761	+o. 146	+0.049
I 5-	- 3			—о. 11	0.06	0. 14	0. 15		
—r 5-	- 2	+0.09	-0.20	+0.65	—0. 46	+3.28	-0.43	+0.15	—o. 21
0 7-	- 3			0. 0	0. 3	o. 2	+0.3		
—r to-	- 3					о. 1	+0. z		
D 10-	- 4	+0.004	0.019	+0.026	0.061	+0. 114	—0. 154	-0.001	-o. o13

. A 1	rg=i'g'+ig	$rac{d\mathrm{B}}{dg'}(n')$	$\delta z') u$	$rac{d\mathrm{G}}{dg}(n$	$\delta z) u'$	$\frac{d\mathbf{G}}{dg'}(n')$	$\delta z') u'$	$\frac{1}{2}r^2\frac{d^2}{dt}$	$rac{ ext{T}}{ ilde{ u}^2} u^2$
* <i>y</i> +	·i'g'+ig	$n^2t^2\sin$.	n^2t^2 cos.	n^2t^2 sin.	n^2t^2 cos.	n^2t^2 sin.	n^2t^2 cos.	$n^2t^2\sin$.	$n^2t^2\cos$.
и	i' i	//	+0.013	"	// +0. 042	"	o. 015	"	// -0.002
1	о 1	+0.073	-0. 02 I	-o. 100	+0.055	—o. 16o	-o. o15	0. 117	+0.002
—ı	0 0	+0.028	+0. 252	o. o36	+0.050	—и. 269	+1.045	0.003	0. 005
1	0 2	0.0	+o. 1			0.0	+o. 1		
1	2— І					— υ. 4	+0.9		
0	2— I	+0.2	0.0	O. 2	0.0				
0	3— г	+o.6	—0. 2	+1.0	O. 2	+0.2	+0.1		
0	4 2	+o. 1	+0.1	+0. 1	+0.1	0, 0	+ 0. 2		
-1	5 I	о. 33	—о. 18	-0. 24	0. 15	— 0. 56	— 0. 95		
0	5— 2	+0.362	+0. 223	+0. 329	+0. 219	+ 0. 465	+o. 817	-0, 040	0.002
1	5 — 3	—o. 11	-o. o3	-0.014	0. 05	—о. 18	-0, 12		
—т	5— 2	+o.87	—o. 65	+0.73	-0.52	+3.67	o. 57		
I	6— 2					+1	—I		
o I	7— 3 7— 3	0.0	o. 3			—0. I +2	+o. 3		
٥	10 4	+0.001	—о. 037	+0.019	—o. o27	+ o . 037	o. o84		

$rac{ ext{Arg}=}{\kappa \gamma + i' g' + i g}$	$rr'rac{d^{2i}}{dra}$	$rac{\Gamma}{ir'} u u'$	$\frac{1}{2}r'^2\frac{d^2\Gamma}{dr'^2}\nu'^2$		
<i>77</i> + <i>19</i> + <i>19</i>	n^2t^2 sin.	n^2t^2 cos.	n^2t^2 sin.	nºtº cos.	
π i' i o o o o i o o o i o o o o i o o o o	+0. 146 +0. 014 +0. 6	+0.093 -0.112 +0.082 +0.3		-0.001 -0.007 +0.081	
0 2— I 0 3— I	+0.4 +0.6	0. 5 0. 1	o. 3 +-o. 3	o. o o. o	
0 4— 2 —1 5— 1	o. 25	+0,02	o 0. 25	+1 0.38	
o 5— 2 I 5— 3 —I 5— 2 o Io— 4	+0. 293 -0. 10 +0. 16	+0.014 -0.03 -1.04	+0. 211 -0. 10 +1. 31 -0. 001	+0. 344 -0. 05 -0. 13 +0. 006	

CHAPTER XVIII.

THIRD-ORDER PERTURBATIONS OF THE MEAN ANOMALY AND RADIUS-VECTOR OF JUPITER ARISING FROM THE MUTUAL ACTION OF THIS PLANET AND SATURN.

The summation of the fourteen parts of $\delta^2 T$, given in the preceding chapter, produces the following expression:

A	rg= -i'g'+ig		<u></u>	$\delta^2 { m T}$			
<i>жу</i> +	-i'g'+ig	sin.	cos.	nt sin.	nt cos.	n^2t^2 sin.	n^2t^2 cos.
н	i' i	11	"	11	"	"	11
٥	0 0		-0.0002131		+ 0.3198		+0.117
I	0 I		-0.0000013	+ 0. 2204	— o. o936	+o. 8o8	o. o58
_ı	0 0	—o. oo38635	+0.0080094	— 6.7600	— 5. 705 I	+0. 544	0. 494
٥	0— І	+0.0037	-0.0100	+ 8.7	+ 5.7		
I	0— 2	0, 000149	+0.002518	— z. 18	— I. I2	+0.2	+1.7
—I	o— 1	о. 036	— 0. 027	+25	26		
٥	0— 2	+0.040	+0.029	27	+26		
I	o— 3	o. oo8	-0, 004	+ 4	— 6		
1	0 2			+22	+40		
٥	o— 3			-24	4 0		
1	0— 4			+ 6	+ 9		
-1	1+3			19	— 7		
0	I+ 2			+59	+19		
1	1+1	,		—57	17		
—т	1+ 2	+0.002	+0,003	+ 7	— 9		
0	1+1	o. o35	0. 030	19	+31		
1	1 0	+0. 0340	+0.0299	+17.7	—29. 3		
1	1+1	-0.0026	-0.0003	+ o. 3	+ 1.6		
0	1 0	+0.0079	-0, 0044	— 3⋅7	— 3· 9		
1	ı— 1	-o. oo85	+0.0038	+ 4.5	+ 4.7	+3	<u>2</u>
—I	1 0	0.0001	+0.0020	I. 2	+ 0.2		
0	1— 1	0.0005	-0.0015	+ 1.1	+ 0.1		
—ı	1— I	0.0109	0.0030	+ 4.3	-10.4	1	—r
0	I— 2	+0.014	+0.001	— 4	+10		
I	ı— 3	-0.002	0.000				
—1	1— 2	+0.015	o. o37	+29	+18		
0	1 3	0.016	+0.037	26	—1 6		
I	1-4	+o. oo3	o. oo7	+ 5	+ 3		
<u>_1</u>	ı— 3			24	+21		
0	1 4			+23	23		

Arg=			$\delta^2 T$			-
$\begin{array}{c} \text{Arg} = \\ \varkappa y + i'g' + i \end{array}$	sin.	cos.	$nt \sin$.	nt cos.	$n^2t^2\sin$.	n^2t^2 cos.
и i' I 2+	i ''	"	+ 3 "		"	"
_I 2+	2 +0.020	+0.005	+2.	—25		
0 2+	10.069	—o. o17	— 7	+75		
I 2	0 +0.0751	+o. o156	+ 5.2	—70.5		
—I 2+	I0.0082	+0.0090	+ 8.4	+ 5.2		
0 2	0 +0.0230	-o. o363	29. 5	10.5		
I 2—	I —0. 022I	+0.0360	+29. O	+10.9	— o. 4	+ 0.9
—I 2	0 —0,0003	-0.0019	o. 65	— 1.16	— 8	— 7
0 2—	+0.00155	+0.00347	+ 1.19	- O. I2	+ 7.9	+ 5.4
I 2—	2 -0,0005	-0.0032	— 3·3	+ 1.1		
—ī 2—	1 +0.0112	0. 0055	+ 0.1	+ o. 3	+ 1	— I
0 2—	2 -0.0149		+ 0.5	+ 2.0		
—I 2—	2 —0.002	-0.012	+ 6	+ 1		
0 2—	3 0.000	+0.008	— 6	- 1		
—I 2—	3 +0.027	+0.007	— 6	+14		
0 2	4 —o. o28	—о. 007	+ 6	—14		
o 3+	1 +0.002	0.003				
1 3	0 +0.002	+0.001	+ 1	+ 1		
-ı 3+	I 0.000	+0.032	+23	— 3		
0 3	00.0002	—0. 1027	—71. 3	+ 9.5		
1 3—	1 +0.0017	+0.0918	+63.4	— 8. 5		
—ı 3	0 +0.0009	-0.0037	— 3. 2	0.7		
o 3—	1 +0.00577	+0.00643	+ 4.43	5.66	+ 6. o	1.3
1 3—	20.0081	0. 0077	4· 7	+ 7.4		
—r 3—	1 +0.0076	-0.0093	+ 2.5	+ 2.0	+14	25
0 3—	2 —o. oo87	+0.0111	— т. 8	 1.3	14	+24
I 3—	3 +o. ooo6	-o. oo13	l			
-r 3—	2 +0.0142	+0.0203	+ 2.3	- I.O		
o 3	3 —0.012	-o. o15				
—I 3—	- '	0. 002	+ 1	+ 6		
□ 3—	40, 008	+0.002	— 1	6		
_I 3—		+0.016	-12	- 2		
o 3—	5 0,000	-o. o16	+11	+ 2		
I 4—		+0.0029	- o. 5	- 0.4		
—ı 4		0.0009	— I. I	— 3·4		
¤ 4—	_	-0.0027	— I. 8	5. o		
I 4—		+0.0035	+ 2.3	+ 6.2	1	
—I 4—	1	0, 0004	+ 3.9	0.0	0	_ 8
0 4—		+0.0034	+ 0.06	— o. 11	+ 3	+13
I 4—	1 '	+0.0008	— 2.9	0.0		
—ı 4—		+0.0093	— o. 6	+ 0.9	+22	+ 7
0 4	1	-0.007	٥	+ 1		
—ı 4		-0.002				
—I 4—		+0.006			ŀ	
—I 4—	5 —0.012	+0.002				
			7		<u> </u>	'

Ana			$\delta^2 T$			
$ \begin{array}{c} \text{Arg} = \\ $	sin.	cos.	nt sin.	nt cos.	n^2t^2 sin.	$n^2t^2\cos$.
и i' i о 5— I	+0.0027	,, 0, 0023	"	"	"	и
I 5— 2	0. 004247	+0.003517	+ 1.110	+ 0.808		
—ı 5— ı	+0.001566	+0.002618	+ 2.508	— I. 25I	— 3. 6 <u>5</u>	-4.46
0 5 2	+0.0008236	+0.0017731	o. 2405	— 0. 2069	+ 3.466	+4.538
I 5— 3	+0.000859	+0, 002827	+ 3.268	1.893	1.23	o. 75
—I 5— 2	+0.003370	+0.000234	o. 954	+ 0.970	+22.72	<u>6. 70</u>
o 5— 3	-0,0021	0. 0004	— о. т	— o. 7		
I 5— 4	0. 0005	0. 0005				
— 1 5— 3	-0.005	+0.023	+ 2	0		
0 5—4	+0.006	-0, 022				
1 5- 5	0. 000	+0.003				
—ı 5— 4	0. 024	-o. 014				
o 5— 5	+o. o26	+0.014				
I 6 2	0. 0025	+0.0075				
—і 6— і	-o. ooo5	0.0003	— o. 3	+ o. 8		
0 6-2	+0.0018	+0.0017				
ı 6— 3	-0.0015	0.0010	+ o.6	— I.O		
—ı 6— 2	+o. oo84	-0.0049	- 5 ⋅3	— 5⋅7	+ r	—I
o 6— 3	0. 0063	+0.0039	+ 4.0	+ 4.4		
ı 6 4	-0.0040	+0.0029	+ 2.5	+ 2.6		
—ı 6— 3	0.0007	+0.0082	+ 3.7	— o. 5		
0 6 4	0.002	o. oo8	— т	٥		
—ı 6— 4	-0.022	-o. oo1				
o 6— 5	+0.020	+0.001				
—ı 6— 5	+0.007	-0.023				
в 6— 6	0. 007	+0.024				
1 7-3	-0.00392	-0.00051	+ 0.07	+ 0.41		*
—ı 7— 2	-o. 00200	—o. oo678	— 6. 25	+ 1.92	ļ	
0 7— 3	+0.00247	+0.00593	+ 5.69	- 2.52	— o. 3	0.0
I 7 4	0. 0037	-0.0015	— o. 9	+ 3.1		
—I 7— 3	+o. o666	+0.0655	+40.5	—56. 3	+ 3	+2
0 7—4	—о. 0731	-o. o7o5	—45. o	+62.2		
1 7— 5	+0.024	+0.022	+13	—1 9		
—I 7— 4	0. 009	+0.002	0	+ 1		
0 7—5	0, 001	—0. 006	I	— 2		
_r 8 2	-0.0013	0.0010	o. 9	+ 1.1		
o 8— 3	+0.00119	+0.00070	+ 1.23	- 1.51		
r 8— 4	-o. oo13	+0.0017	+ 0.1	+ 0.7		
—ı 8— 3	+0.0266	+0.0067	+ 3.1	25.7		
o 8— 4	0. 0282	—o. oo77	— 3⋅4	+25.2		
ı 8 5	+o. 0091	0.0000	0.9	- 6.5		
_r 8— 4	-0.0529	+o. o836	+67.4	+30. r		
o 8— 5	+o. o56	0. 090	7 0	29		
т 8—6	0. 017	+0.027	+22	+ 9		
		L				

Arg=			$\delta^2 { m T}$			
$\kappa \gamma + i^7 g' + i g$	sin.	cos.	$nt \sin$.	nt cos.	n^2t^2 sin.	n²t² cos.
$\begin{array}{cccc} \varkappa & i' & i \\ -1 & 8-5 \end{array}$	+0.001	+0.003	+ 3		"	"
o 8— 6	+0.003 +0.014	0. 005 0. 006				
-1 9-3 0 9-4	+0. 0059 -0. 00479	-0.0016 +0.00098	— 2. I + 2. 45	- 4·3 + 5·85		
1 9— 5 —1 9— 4	+0.0007 -0.0027	0.0011 +0.0362	- 1. 1 +33. 8	- 0.8 - 2.7		
0 9— 5 1 9— 6	+0.005 +0.001	-0.037 +0.012	-30 + 8	+ 2 - I		
-I 9-5 0 9-6	0. 080 -+0. 081	-0. 030 +0. 028	-14 +12	+62 -64		
1 9— 7 —1 9— 6	0. 027 0. 004	0.009 0.001	— 3	+18		
o 9-7	+0.006 +0.00081	+0.002 -0.00079	I.OI	— o. 66	—о. 1	+0. 2
0 IO 4 I IO 5	-0.0006663 -0.00012	+0.0004584 -0.00036	+ 0. 9933 — 0. 35	+ 0.7516 + 0.02	+o. 188	—o. 379
-1 10 4 0 10 5	+0.00212 -0.0030	+0.00753 -0.0076	+ 8.63 - 5.3	- 5.92 + 3.6		
1 10— 6 —1 10— 5	+0.002 0.037	+0.002 +0.003	+ I + 8	I +28		,
0 10— 6 1 10— 7	+0. 039 -0. 012	-0.006 +0.004	- 8 + 2	-28 + 6		
—I IO— 6	+0.008 0.007	0. 062 +-0. 064	-46 +46	0 — I		
1 Io— 8	+0.0006	0. 020	—IO	+ 1		
0 II— 5	-0. 0008 -0. 0082	+0.0006 -0.0006	+ 0.4 - 0.4	- 0.9 + 0.8		
o 11— 5	+0.008	+0.0055 -0.007	+ 5.6 5	$\begin{vmatrix} +5.3 \\ -3 \end{vmatrix}$	l I	
I II— 7 —I II— 6	0.002 0.012 +0.013	+0.002 0.032	22 22	+12		
0 11— 7 1 11— 8 —1 11— 7	-0.003 -0.003 +0.043	+0. 033 -0. 007	+22 -5 -8	-12 + 3		:
0 11—8	-0. 044	-0.004 +0.005	+ 9	—31 +31		
0 12— 5 —1 12— 5	+0.00057 +0.0025	—0, 00096 —0, 0075	+ 0.01 + 1.5	+ o. 18		
0 12— 6 —1 12— 6	0.0007 0.009	+0.0022 -0.008	— I. 3 — 4	- 0.4 + 5		
o 12— 7 —1 12— 7	+0.006 +0.025	+0.006 0.015	+ 4 -10	- 5 -12		
0 12— 8 —1 12— 8	-0. 024 +0. 009	+0.015 +0.026	+10	+12 - 7		
O 12— 9	-0.01	-0, 02	—13	+ 8		

In precisely the same manner as $\overline{W_0}$ and $\overline{\delta W_0}$ have, in preceding chapters, been derived from T and δ T we now get $\overline{\delta^2 W_0}$ from δ^2 T. In the case of the terms depending on the arguments 5g'-2g and 10g'-4g the motion of the argument has been equated. We proceed as at page 275, the only difference being that here terms multiplied by n^2t^2 are present. By adding T, δ T, and δ^2 T we obtain

In the case of the argument 5g'-2g we get \varkappa and the corrected integrating factor from

$$\log \mu = 6.9171965n$$
 $\log \mu = 1.8995167$

In the case of the argument 10g' - 4g the similar quantities are

$$\log \mu = 7.16317n$$
 $\log \mu = 1.59510$

The expression just written can then be transformed into

$$[-0.0718628 + 0.000009283nt - 0.00000000903n^2t^2] \sin (5g' - 2g + \kappa nt) + [-0.1794415 + 0.000023179nt - 0.00000000823n^2t^2] \cos (5g' - 2g + \kappa nt) + [-0.0051553 + 0.000000983nt - 0.0000000214n^2t^2] \sin (10g' - 4g + \kappa nt) + [-0.0052333 - 0.000000997nt + 0.00000000319n^2t^2] \cos (10g' - 4g + \kappa nt)$$

Integrating this the result is

$$\begin{aligned} \mathbf{W}_0 + \delta \mathbf{W}_0 + \delta^2 \mathbf{W}_0 = & \begin{bmatrix} \frac{1}{16.83882} - 0.0008402nt + 0.000000716n^2t^2 \end{bmatrix} \cos \left(\frac{5g' - 2g + \kappa nt}{2g + \kappa nt} \right) \\ & + \begin{bmatrix} -14.17103 + 0.0017254nt - 0.000000653n^2t^2 \end{bmatrix} \sin \left(\frac{5g' - 2g + \kappa nt}{2g + \kappa nt} \right) \\ & + \begin{bmatrix} 0.20113 - 0.00002881nt + 0.000000842n^2t^2 \end{bmatrix} \cos \left(\frac{10g' - 4g + \kappa nt}{2g + \kappa nt} \right) \\ & + \begin{bmatrix} 0.20714 - 0.00004586nt + 0.0000001256n^2t^2 \end{bmatrix} \sin \left(\frac{10g' - 4g + \kappa nt}{2g + \kappa nt} \right) \\ & = \begin{bmatrix} 5.83882 + 0.0108709nt - 0.000002704n^2t^2 \end{bmatrix} \cos \left(\frac{5g' - 2g}{2g + \kappa nt} \right) \\ & + \begin{bmatrix} 0.20113 - 0.00033041nt - 0.000000622n^2t^2 \end{bmatrix} \cos \left(\frac{10g' - 4g}{2g + \kappa nt} \right) \\ & + \begin{bmatrix} 0.20714 + 0.00024699nt - 0.0000001360n^2t^2 \end{bmatrix} \sin \left(\frac{10g' - 4g}{2g + \kappa nt} \right) \end{aligned}$$

If from the latter expression we subtract the following (obtained at page 276)

$$W_0 + \delta W_0 = \begin{bmatrix} "" & "" \\ 5.92153 + 0.0107729nt \end{bmatrix} \cos (5g' - 2g) \\ + [-14.29576 + 0.0068379nt] \sin (5g' - 2g) \\ + [-16574 + 0.00004901nt] \cos (10g' - 4g) \\ + [-17595 - 0.00003718nt] \sin (10g' - 4g) \end{bmatrix}$$

we get

$$\delta^{2}W_{0} = \begin{bmatrix} -0.08271 + 0.0000980nt & -0.000002704n^{2}t^{2} \end{bmatrix} \cos(5g' - 2g) \\ + \begin{bmatrix} 0.12473 - 0.0002872nt & +0.000003492n^{2}t^{2} \end{bmatrix} \sin(5g' - 2g) \\ + \begin{bmatrix} 0.03539 - 0.00037942nt - 0.0000000622n^{2}t^{2} \end{bmatrix} \cos(10g' - 4g) \\ + \begin{bmatrix} 0.03119 + 0.00028417nt - 0.0000001360n^{2}t^{2} \end{bmatrix} \sin(10g' - 4g) \end{bmatrix}$$

The value of $\overline{\delta^2 W_0}$ follows:

Arg=i'g'+ig	İ					
	cos.	sin.	nt cos.	nt sin.	n^2t^2 cos.	n^2t^2 sin.
i' i	"	II	" — 21. 12	"	" + 160.7	11
0— I	$+0.0037+k_1$	$+0.0088+k_2$	+808.55	391.49	2852. 5	338o. o
o— 2	0.0187+[8.38] k_1	+0. 0138+[8. 38]k ₂	+ 32.3	+ 5·7	68. 7	- 81.5
o— 3	- o . 0009	<u>+</u> 0. 0006	+ 5.8	8.6	— 2.5	- 2.9
I+ 2	-0,0021	+0.0018	+ 21	_ 8		
1+1	-0.0621	+o. o549	— 32. I	54.6		
1 0	-0.0321	—o. o176	+ 16.4	— 16. 6	+ 5	+ 3
1— 1	0.0006	+0.0074	+ 4.8	+ 0.3		
I 2	0.0106	+o. oo46	+ 0.4	+ 1.1	— 2	+ 2
I— 3	+0.0037	+0.0111	+ 9	6		
2+ 2	-0.002	0, 000	2	— 3		
2+ 1	o. o658	+o.0076	+ 1	 56		
2 0	—o. 1349	o. 2178	+180.9	— 66. ₃	2	5
2 I	+0, 0080	0. 0171	+ 4.3	— I.3	+ 51	— 37
2— 2	+0.0454	+0. 0229	+ 0.9	— 3. z	+ 5	+ 5
2 3	-0.0003	+0.0071	+ 2	— т		
2— 4	+0.0035	-0.0010	— т	2		
3+ 1	—u. 0028	+o. o104	8	О		
3 0	0. 0100	+o. 3867	—25 6. 2	— 34·5		
3— т	—о. 0398	+o. o387	— 24. 8	— 36.8	— 2 9	6
3- 2	-o. o467	0. 0575	15. I	+ 11.7	85	— 15o
3 3	+0.0103	0. 0183	+ 3	+ r		
3— 4	+0.0021	0.0002	+ 1	— г		
3 ─ 5	0,0000	0.0015	I	0		
4— I	-o. o427	o. o136	+ 9.5	— 26. 2		
4 2	+0.0003	—о. 0086	- 8.2	+ 0.3	+ 8	— 46
4 3	+o. o338	—о. 0188	- I. 5	- 2.7	+ 57	— 18
4 4	+0.0025	+o. ooo8				
4— 5	+0.0013	0. 0025				
4 6	0. 0035	—о. 0006				
5— т	+o. 3583	+o. 3211	— 82.6	+ 60.2		
5— 2	0. 08342	+o. 12451	+ 10.63	— 28. 04	— 268. о	+ 345.6
5— 3	-0.0120	+o. o2o6	- 3.4	+324.8	—1692	499
5— 4	-0.0023	0.0127	+ 2	+ 8	40	- 10
5— 5	0. 0035	+0.0017				

Arg=i'g'+ig			$\delta^2 W_0$	-		
Alg=vy+iy	cos.	sin.	nt cos.	$nt\sin$.	n^2t^2 cos.	$n^2t^2\sin$.
i' i	11	"	"	"	11	11
6 2	o. oo65	+o. oo56	+ 1.2	+ 2.3		
6— 3	—o. o335	-0. 0203	+ 21.2	— 22. 8	- 2	— 2
6— 4	-0.0030	0. 0092	+ 5	+ 1	l	
6— 5	-o. oo62	-0.0001				
6— 6	+0.0005	+0.0022				
7— 2	0. 0327	+0.0043	+ 0.4	— 2.3		
7— 3	+0.0126	o. o383	+ 38.3	+ 13.8	- 2	0
7— 4	+0. 3000	—о. 3003	+191.6	+266.7	+17	-11
7— 5	+0.0003	0.0073	+ 5	+ 7		
8— 3	0. 0062	+0.0004	— 4.8	— 6.7		
8 4	—0, 1562	+0.0406	— 18.9	-144.7		
8 5	-0. 0450	—o. o646	+ 54	29	<u>.</u>	
8— 6	+0.0001	0. 0024	+ 4	0		
9— 4	o. o214	— 0. ∞47	+ 9.1	21.9		
9— 5	0. 0034	-0.0721	+ 71.4	+ 6.2		
9— 6	0. 0322	+0.0104	- 4	23		
9— 7	0.0013	-o. ooo5	0	I		
10— 4	+o. o3473	+0.03076	— 37.31	+ 27.77	6. 1	—13.4
10 5	о. 163 0	+o. 406 5	<u>—326. 2</u>	—223 . 6		
ro— 6	o. o261	+0.0082	— 3	- 22		
10 7	+0.0010	+0.0148	11	— 1		
11 5	-0.0028	+0.0024	<u> </u>	— 3·5		
11 6	0, 0100	-0.0051	+ 7	— 7		
11— 7	0.0037	+0.0094	_ 6	- 4		
11 8	+0.0042	+0.0006	0	+ 3		
12— 5	+0. ∞346	+0.00572	+ 0.06	— 1.07		
12— 6	+0.0143	+0.0434	+ 7.8	1.5		
12— 7	-0.0048	+0.0040	— т	— 2	1	
12 8	+0.0039	+0.0022	- 2	+ 2		
12- 9	+0.0004	-0.0034	+ 2	0		

$\overline{\delta^2 W_0}$				
n^3t^3 cos.	n^3t^3 sin.			
+0,0000000039	11			
—0. 00000000165 —0. 0000000004	+0.00000000181 +0.00000000004			
	n³t³ cos. '' +0.0000000039 -0.0000000165			

Also, we have the expression of the following function, needed in the determination of $\delta^2 \nu$:

Arg=i'g'+ig			$-rac{1}{2}\left(rac{d\cdot\delta^2V}{d\gamma} ight)$	<u>v</u> ₀)		
	sin.	cos.	nt sin.	nt cos.	n^2t^2 sin.	n^2t^2 cos.
i' i 0— I	11	11	"	,,,	// +1426. 3	
1	+0.0169	—o. o366	—401.0	—193. 7 — 2. 7	+ 69	- 81
0— 2	+0.0175	+0.0111	- 31.4 6.4	+ 2.7 - 8.7		
0— 3	+0.0009	+0.0006	0, 4	- 8.7	+ 4	- 4
1+ 2	0.0021	0.0018	+ 16	+ 7		ļ
1+1	0, 0430	— 0. 0369	19.8	+ 34.8		
I O	-0.0079	+0.0030	+ 3.8	+ 4.3	+ 2	— I
1— 1	0.0001	+0.0024	— 1.5	+ 0.2		
I— 2	+0.0089	+0.0026	— 3	+ 8		
I— 3	—0. 0039	+0.0108	— 9	— 5		
2+ 2	0. 002	0,000	— I	+ 2		
2+ I	0. 0464	0. 0045	+ 1	+ 41		}
2 0	0. 0572	+0.0911	+ 76.8	+ 29.2	_ ı	+ 2
2— 1	o, ooo5	-0.0024	- 1.7	- 0.2	— 5	- 4
2 2	o. o289	+0.0141	0. 2	— o. 7	- 2	+ 2
2 3	—0.000 6	+0.0057	— 2	0		
2 4	o. oo61	-0.0016	+ 1	— 3		
3+ 1	0.0010	—o, от 14	— 7	+ 1		
3 0	0. 0052	0. 2208	-147. 2	+ 19.9		
3— 1	-0.0047	о. 0060	— 4.0	+ 4.3		
3— 2	+0.0181	0. 0224	+ 6.5	+ 5.0	+ 33	— 6 0
3— 3	—o. oo8o	о. 0139	— т	0		
3— 4	-o. 0 026	—u. 0001	О	— I		
3- 5	0, 0000	o. oo28	+ 2	О		
4 r	-0.0114	+0.0041	+ 2.6	8.9		
4— 2	0, 0004	-0. 0005	+ 2.2	0.0	0	_ 6
4 3	—o. o237	-0. OI 20	+ 0.7	- 1.0	— 28	— 9
4— 4	—o, oo18	+0.0001				
4- 5	0. 0006	0.0012				
4— 6	+0.0017	-0.0003				
5— 1	+o. 1805	—o. 1617	- 41.3	— 30. I		
5— 2	+0.001198	+0.002714	+ 2.897	— I. 578	— 2. 42	— 2.58
5— 3	+0,0047	+ 0.0098	+ 1.6	+162. o	+ 846	- 249
5— 4	+0.0027	—o. o106	— I	+ 8	+ 40	— 10
5— 5	+0.0061	+0.0029				
6— 2	0.0015	0, 0009	+ 0.4	- o. 5	•	
6 3	+0,0090	o. 005 I	— 5.5	— 6.o		
6— 4	+0.0011	-0.0072	— 3	а		
6 5	+0.0069	0,0000			1	
6— 6	0.0011	+0.0044				
	1			1	<u> </u>	<u> </u>

Arg=i'g'+ig			$-\frac{1}{2}\left(\frac{\overline{d}\cdot\overline{d^3V}}{d\gamma}\right)$	<u>v</u>)		
	sin.	cos.	$nt ext{ sin.}$	nt cos.	$n^2t^2 \sin$.	n^2t^2 cos.
i' i	"	и.	"	"	//	"
7— 2	—o. 0107	-0.0014	+ 0.2	+ 1.1		
7 3	0. 0024	0.0046	4. I	+ 2.2		
7— 4	—0. 1698	—0. 1698	—ro8. 9	+151.1		
7— 5	—0. 0046	0.0092	5	+ 7		
8— 3	-0.0012	+0.0007	- o.3	+ 0.7		
8— 4	+0.0652	+o. o153	+ 6.8	59.8		
8— 5	+0. 0347	—о. 0476	— 39	<u> </u>		
8— 6	+0.∞13	o. oo33	— 3	— I		
9— 4	+0.0050	0. 0014	— 2. I	— 3·7		
9— 5	+0.0039	0. 0444	— 43⋅3	+ 3.4		
9 — 6	+o. 0248	+0.0074	+ 3	— 20		
9— 7	+0.0022	+0.0003				
10 4	+0.00048	-o. ooo55	— o. 66	— o. 32		
10 5	+o. o8o9	+0. 2004	+160.8	-110.4		
10— 6	+0.0209	+0.0087	+ 4	18		
10 7	0.0019	+0.0132	+ 10	о		
11 5	+0.0007	+0.0007	+ 0.4	— 1.0	Į	
11— 6	+o. 0067	-0. 0047	5	— 4		
11— 7	+0.0034	+0.0092	+ 7	— 4		
11— 8	<u> </u>	+0.0007	+ 1	+ 6		
12- 6	0. 0074	+0.0226	— 4·4	— o. 9		
12— 7	+o. oo38	+0.0034	+ 1	_ 2		

Arg=i'g'+ig	$-\frac{1}{2}$	$\left(\frac{d \cdot \delta^3 \overline{W}_0}{d\gamma}\right)$
	n^3t^3 sin.	n^3t^3 cos.
i' i o— I o— 2	+0. 00000000082 +0. 00000000004	+0.0000000000 +0.00000000004

The rigorous equation determining z is

$$\frac{dz}{dt} = \mathbf{I} + \frac{\overline{\mathbf{W}} + \nu^2}{\mathbf{I} - \nu^2}$$

where for \overline{W} we ought to substitute

$$\overline{W} = \overline{W_0} + \left(\frac{\overline{dW_0}}{\overline{d\gamma}}\right) n \delta z + \frac{1}{2} \left(\frac{\overline{d^2W_0}}{\overline{d\gamma^2}}\right) (n \delta z)^2 + \dots$$

Here the several factors include terms of all dimensions with respect to the disturbing forces. Limiting ourselves to the terms of three dimensions we have

$$\frac{d(n\delta^3z)}{ndt} = \overline{\delta^2 \mathbf{W}_0} + \left(\frac{\overline{d\,\mathbf{W}_0}}{\overline{d\,\boldsymbol{\gamma}}}\right) n\delta^2z + \left(\frac{\overline{d\,\boldsymbol{\cdot}\,\delta\,\mathbf{W}_0}}{\overline{d\,\boldsymbol{\gamma}}}\right) n\delta z + \frac{\mathbf{1}}{2} \left(\frac{\overline{d^2\,\mathbf{W}_0}}{\overline{d\,\boldsymbol{\gamma}^2}}\right) (n\delta z)^2 + 2\,\boldsymbol{\nu}\delta\boldsymbol{\nu} + \boldsymbol{\nu}^2\frac{d\,\boldsymbol{\cdot}\,n\delta z}{ndt}$$

All the factors involved in the right member of this equation have already been given. But, as in forming the product $\left(\frac{\overline{dW_0}}{d\gamma}\right)n\delta z$ in the computation of the terms of the second order, we have corrected the two factors for the terms multiplied by nt, belonging to the arguments g, 2g, etc., and which result from the previous computation of δW_0 , these terms must be omitted from the factors $n\delta^2 z$ and $\left(\frac{\overline{d\cdot\delta W_0}}{\overline{d\nu}}\right)$.

The values of the five additional quantities involved in the expression of $\frac{d(n\delta^3z)}{ndt}$ follow:

	Arg=i'g'+ig	$\Big(rac{\overline{d { m W}_0}}{\overline{d \gamma}}\Big) n\delta^2 z$					
$\begin{array}{cccccccccccccccccccccccccccccccccccc$		cos.	sin.	nt cos.	$nt \sin$.	n^2t^2 cos.	n^2t^2 sin.
$\begin{array}{cccccccccccccccccccccccccccccccccccc$		"	"		"		"
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	0 I	+0.0154	+0.0458	+28.9	-14.4		
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	0 2	+0.001	+0.003	+ 3	+ 1		
$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$	o— 3	+0.002	+0.002	- - 1	— I		
$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$							
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	Ī+ 2	0.003	0.005	+ 3	— 1		
$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$	1+1	-o. oo5o	+0.0032	- 3. 1	- 4.9		
$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$	1 0	0, 0004	-0.0002	— o. 7	+ 0.6		
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	1— I	+0.0001	+0.0004	+ 1.0	o. ı		
$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$	I— 2	0.001	0, 000				'
$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$	İ						
$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$	2+ I	—o. o13	+0,002	0	12	ŀ	
$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$	2 0	o. oo85	— 0. 0139		- 4.0	- 3	+10
$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$	2 I	0.0011	+0,0020	+ 1.8	+ 0.2	9	十 7
$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$	2— 2	—0.0009	-0. 0 009		i	-11	- 2
$ \begin{vmatrix} 3 & 0 & -0.0003 & +0.0818 & -59.3 & -8.5 \\ 3-1 & +0.0022 & -0.0003 & -1.3 & +3.7 \\ 3-2 & -0.0006 & -0.0014 & +0.8 & -2.4 \end{vmatrix} $	2— 3	0,000	-0.001	}			
$ \begin{vmatrix} 3 & 0 & -0.0003 & +0.0818 & -59.3 & -8.5 \\ 3-1 & +0.0022 & -0.0003 & -1.3 & +3.7 \\ 3-2 & -0.0006 & -0.0014 & +0.8 & -2.4 \end{vmatrix} $	1	<u> </u>					
$ \begin{vmatrix} 3-1 & +0.0022 & -0.0003 & -1.3 & +3.7 & +13 & +3 \\ 3-2 & -0.0006 & -0.0014 & +0.8 & -2.4 & +3 \end{vmatrix} $	3+ 1	+0.001	+0.004	— 3	О	l	
3-2 -0.0006 -0.0014 + 0.8 -2.4	3 0	0.0003	+o. o818	—59. 3	— 8. 5		-
	3— 1	+0,0022	0.0003	— I.3	+ 3.7	+13	+ 3
3— 3 — 0.001 — +0.002	3— 2	— 0. 0006	-0.0014	+ o.8	- 2.4		
	3— 3	-0.001	+0.002				
	1						
4 0 -0.001 0.000	4 0	-0.001	0.000				
4-1 -0.0095 -0.0018 + 2.4 -6.5	4— 1	0.0095	-0.0018	+ 2.4	- 6.5		
4— 2 +0.0002 -0.0021 0.0 -0.1	4— 2	+0.0002	-0.0021	0.0	— o. 1		
4-3 -0.0007 +0.0008 + 0.2 + 1.5	4 3	0.0007	+0.0008	+ 0.2	+ 1.5		

Arg=i'g'+ig			$\left(\frac{\overline{dW_0}}{d\gamma}\right)$	$n\delta^2z$		
	cos.	sin.	nt cos.	$nt \sin$.	$n^2t^2\cos$.	n^2t^2 sin.
i' i 5— 0	11	"	+ 3	I	11	"
5— 1			+.55.9	—19. 2	+ 82	+414
5— 2 5— 3	+0. 000538 -0. 0022	-0.001328 +0.0006	— 2. 690 +24. I	— 1.682 +54.0	+ 35.76 -404	- 24.37 +118
5 4	9		+ 4	0	+ 30	+ 30
6— 2 6— 3	o. 0008 o. 0076	+0.0007 -0.0053	0.3 + 4.6	+ o. 1 - 5. 1		
6— 4	-0.001	0, 000		_		
7— 3 7— 4	+0.0016 +0.0595	0. 0011 0. 0562	0. 2 +33. I	+ o. 8 +45·7		
7 - 5	0,000	—0.002	+ 4	— 3		
8— 3 8— 4	+0.0002 0.0158	+0.0007 +0.0032	+ 0.9 — 1.1	+ 0.7 —12.3		
8— 5	o. ooo7	—0. 0010	+ 7	— 3		
9— 4 9— 5	0. 0007 0. 0014	-0. 0002 -0. 0069	+ o. ∠ + 5.7	- 0.4 + 0.5		
9— 6	0.007	+0.002	— 1	— 3		
10— 4 10— 5	-0.00010 -0.0221	—0. 00 009 —0. 04 20	+ 1.43 -32.2	— 0.39 —19.6	0.0	- o. 3
10 6	0.001	+0.001	2	+ 2		

Arg=i'g'+ig			$rac{\mathrm{I}}{2} \Big(rac{\overline{d^2 \mathrm{W}_0}}{d \gamma^2} \Big)$	$(n\delta z)^2$		
	cos.	sin.	nt cos.	$nt \sin$.	n^2t^2 cos.	n²√³ sin.
i' i o o o o — I	11	11	+0.007 -1.2	+1.3	 0. 05	"
ı— 1	+0.0001	0, 0003				
2— I	o. ooo1	+0.0002				! !
2 2	+0.0023	+0.0010				!
3— I 3 - 2	0.0003	—o. 0004	0. 2	—о. з		
5— 2	+0.000008	+0.000002	0.020	-0.020	0. 14	0. 15
5— 3	0,0014	0.0001				
7 – 3			0. 1	0.0		
8— 2 8— 3	+0.0010 0.0000	+0.0005 -0.0002				
10 4	+0.00009	+0.00009	0. 02	+0.01	о. 1	o. I

Arg=i'g'+ig	$\left(\frac{\overline{d} \cdot \delta \overline{W_0}}{d\gamma}\right) n \delta z$					
	cos.	sin.	nt cos.	nt sin.	n^2t^2 cos.	n^2t^9 sin.
i' i	"		" + o. 540	"	- 1.81	п :
o 1	+o، مرە	+0.0131	22. 2	+3.7		
O— 2	∔0.002	0.001	I	—I		
1+ 2	-0.001	0.002				
1+1	+0.0001	0.0020	+ 1.4	+1.3		
I O	-0. 0002	-0.0002	— o. 6	+0.3	+ 3	+ 3
1— 1	+o. 0003	-0.0011	— o. 7	+o. 1		
2+ 1			+ 1	-2		
2 0			- 3⋅3	+2.6	— 3	+ 4
2— I	0.0008	+0.0020	+ 0.5	-1.4	— 7	+ 4
z 2	+o. 0221	+0.0095				
2— 3	0.000	-0.001				
3+ I			— I	+1		
3 0	-0.0007	0.0010				
3— т	+0.0017	0.0012	0. z	+2.9	+ 9	+ 1
3— 2	-o. oo58	— 0. 0106	0.0	+2.0		
3— 3	+0.001	0.005				
4 0	0.002	+0.001				
4 1	+0.0004	-0.0010			_	
4— 2 4— 3	+0.0002 +0.0061	-0.0003 -0.0031	1.6	o. o	— I	+ 3
	l '					
5 o 5— r	0, 00I 0, 0000	+0.001 +0.0011			+30	+40
5— 2	+0.000560	-0.001114	2. 548	-1. 584	+35.38	—24. 65
5— 3	-0.0076	-0.0016	3.	,	+50	— 6
5— 4	-0.001	-0.002	+ 2	-2	+20	+30
6— 1	+0.0013	+0,0042				
6— 2	0, 0002	0, 0000				
6-3	+0.0003	+0.0008				
6— 4			— I	0		
7— z	-0.0091	+0.0011	Ĺ			
7-3	+0.0003 0.0030	+0.0001 +0.0006	- 1.8 - 0.4	—o. 1		ļ
7— 4 7— 5	-0.0030	0.000	+ 0.4 + 2	-2. 3 -5		
8— 2			· .			
8— 2 8— 3	+0.0097 +0.0002	+0.0041 +0.0005	+ 0.5	+0.3		
8— 4	-0.0004	+0.0008	— o. 5	—4. 2		
8— 5	+0.001	+0.001	— I	+1		
9-3	0. 0003	+0.0005				
9— 4	-0.0005	-0.0002	— o. 1	о. 1		
9— 5	-0.0015	+0.0016	+ 2.0	+o. 1		
9 6	0. 002	0.000				
10 4	-0.00027	-0.00024	+ 1.36	-0, 40		1
10 5	—0. 0030	+0.0171			1	
10— 6	+0.002	-0.001			[
		1		1	<u>l</u>	

A 1/ / 1 to	2 v δν			δν		
Arg=i'g'+ig	cos.	sin.	nt cos.	nt sin.	$n^2t^2\cos$.	n^2t^2 sin.
i' i	"	"		"	+ 2.06	"
1 0			+o. 3	-o. 4		
2— 1	+0.0008	-0.0011	о. 8	+o. I	+ 4	— 3
3— т	-0.0011	+0.0008	0.0	—1 .6	— 5	2
4— 2	_o. ooo1	+0.0003	+o. 5	0.0		
5— 2 5— 4	—o. 000295	+0.000669	+1.344	+ 0.834	—17. 94 +10	+12.41 +10
6— 2	+0.0001	-o. ooo1				
7 3 7 5	0, 0002 0, 001	o, 0000 0. 001	+0.9	+o. 1		
8— 3	0, 0000	-0.0003	0.4	-o. 2		
9— 4	+0.0002	+0.0001				
10 4	+0.00003	+0.00001	—о. 68	+0.18		

The single sensible term of $\frac{d \cdot \delta z}{dt} v^2$ is +0''.004nt. The addition of the six terms of $\frac{d \cdot \delta^3 z}{dt}$ gives the following expression for this quantity:

Arg=i'g'+ig			$rac{d \; . \; \delta^3 z}{dt}$			
	cos.	sin.	$nt \cos$.	$nt \sin$.	n^2t^2 cos.	n^2t^2 sin.
i' i o o o— I	,,, +0. 0298+k1	,,, +o. 0677+k2	- 20. 428 +814. 0	 400. 9	" + 156.93 2852	338o
0— 2 0— 3	—0. 0157+[8. 38]k ₁ +0. 0011	+0.0158+[8.38]k ₂ +0.0026	+ 34·3 + 6.8	+ 5·7 9.6	— 69 — 2	81 3
I+ 2 I+ I I 0 I- I I- 2	—0. 0061 —0. 0670 —0. 0327 —0. 0001 —0. 0116	-0.0052 +0.0561 -0.0180 +0.0064 +0.0046	+ 24 - 33.8 + 15.4 + 5.1 + 0.4	- 9 - 58. 2 - 16. 1 + 0. 3 + 1. 1	+ 8	+ 6
I — 3 2+ 2 2+ I 2	+0.0037 -0.002 -0.0788 -0.1434 +0.0068 +0.0689 -0.0003 +0.0035	+0.0111 0.000 +0.0096 -0.2317 -0.0140 +0.0325 +0.0051 -0.0010	+ 9 - 2 + 187.8 + 5.8 + 0.9 + 2 - 1	- 6 - 3 - 70 - 67.7 - 2.4 - 3.2 - 1	- 8 + 39 6	+ 9 29 + 3

25 AST-

Arg=i'g'+ig	$rac{d\ .\ \delta^3 z}{dt}$					
	cos.	sin.	nt cos.	$nt\sin$.	$n^2t^2\cos$.	$n^{2}t^{2}\sin$.
i' i 3+ i 3 o	o. 0018 o. 0110	+0. 0144 +0. 4675	— 12 —315.5	+ I - 43.0	п	"
3- 1 3- 2 3- 3 3- 4	—0. 0370 —0. 0434 +0. 0103 +0. 0021	+0. 0380 -0. 0699 -0. 0213 -0. 0002	-26.5 -14.3 $+3$ $+1$	- 32. I + II. 3 + I - I	— 12 — 85 — 2	— 4 —150 — 3
3-5 4 0 4-1 4-2 4-3 4-4 4-5 4-6	0. 0000 -0. 003 -0. 0518 +0. 0006 +0. 0392 +0. 0025 +0. 0013 -0. 0035	-0.0015 +0.001 -0.0164 -0.0107 -0.0211 +0.0008 -0.0025 -0.0006	- I + II.9 - 9.3 - I.3	0 - 32.7 + 0.2 - 1.2	+ 7 + 57	— 43 — 18
5 0 5— 1 5— 2 5— 3 5— 4 5— 5		+0.001 +0.3222 +0.122739 +0.0195 0.0147 +0.0017	+ 3 - 26.7 + 6.716 + 20.7 + 8	- I + 41.0 - 30.492 +378.8 + 6	+ 112 214.94 2046 + 20	+454 +308.84 -387 + 60
6— I 6— 2 6— 3 6— 4 6— 5 6— 6	+0.0013 -0.0074 -0.0408 -0.0040 -0.0062 +0.0005	+0.0042 +0.0062 -0.0248 -0.0092 -0.0001 +0.0022	+ 0.9 + 25.8 + 4	+ 2.4 - 27.9 + I	2	- 2
7— 2 7— 3 7— 4 7— 5	—0. 0236 +0. 0143 +0. 3565 —0. 0037	+0.0054 -0.0393 -0.3559 -0.0103	+ 0.4 + 37.1 +225.1 + 11	- 2.3 + 14.6 +310.1 - 1	- 2 + 17	— II
8— 2 8— 3 8— 4 8— 5 8— 6	+0.0107 -0.0058 -0.1724 -0.0510 +0.0001	+0.0046 +0.0011 +0.0446 -0.0736 0.0024	- 3.8 - 20.5 + 60 + 4	- 5.9 -161.2 - 31		
9— 3 9— 4 9— 5 9— 6 9— 7	0.0003 0.0224 0.0063 0.0412 0.0013	+0.0005 -0.0050 -0.0774 +0.0124 -0.0005	+ 9.2 + 79.1 - 5	- 22.4 + 6.8 - 26 - 1		
10— 4 10— 5 10— 6 *10— 7	+0. 03448 -0. 1881 -0. 0251 +0. 0010	+0.03053 +0.4656 +0.0082 +0.0148	35. 22 358. 4 5 11	+ 27.17 243.2 - 20 - 1	— 6. z	— 13.8

^{*} The terms corresponding to the divisions 11 and 12 are omitted, since they are the same as the similar terms of $\overline{\delta^2 W_0}$, given on page 395.

Arg=i'g'+ig	, $rac{d$, $\delta^3 z}{dt}$		
	n^3t^3 cos.	$n^3t^3 \sin$.	
i' i o— I o— 2		+0. 00000000181 +0. 0000000004	

On integrating this expression we arrive at $n\delta^3z$. In order to make the terms depending on the argument g disappear it is necessary to put $k_1 = -0''.0339$ and $k_2 = -0''.0759$. In the case of the terms involving the arguments 5g' - 2g and 10g' - 4g we equate the motions of the latter. By adding the values which have been obtained for $\frac{d \cdot n\delta z}{ndt}$, and $\frac{d \cdot n\delta^3z}{ndt}$ we get, taking the liberty of calling the sum $\frac{d \cdot n\delta z}{ndt}$,

$$\frac{d \cdot n\delta z}{ndt} = \begin{bmatrix} "" & "" & "" \\ 5.80177 + 0.0100762nt - 0.000002149n^2t^2 \end{bmatrix} \cos(5g' - 2g) \\ + [-14.01188 + 0.0056567nt + 0.000003088n^2t^2] \sin(5g' - 2g) \\ + [& 0.19539 - 0.0003068nt - 0.00000062n^2t^2] \cos(10g' - 4g) \\ + [& 0.20289 + 0.0002363nt - 0.000000138n^2t^2] \sin(10g' - 4g) \end{bmatrix}$$

For this expression may be substituted

$$\frac{d \cdot n\delta z}{dt} = \begin{bmatrix} "" & "" & "" \\ 5.80177 - 0.0005247nt + 0.000000471n^2t^2 \end{bmatrix} \cos (5g' - 2g + unt) \\ + [-14.01188 + 0.0012673nt - 0.000000525n^2t^2] \sin (5g' - 2g + unt) \\ + [0.19539 - 0.0000296nt + 0.000000079n^2t^2] \cos (10g' - 4g + unt) \\ + [0.20289 - 0.0000307nt + 0.000000092n^2t^2] \sin (10g' - 4g + unt) \end{bmatrix}$$

where, in the case of 5g'-2g, κ and the corrected integrating factor are determined by

$$\log n = 6.8788474n$$
 $\log n = 1.8971166$

and, in the case of 10g'-4g, by

$$\log \mu = 7.13560n$$
 $\log \mu = 1.59358$

Integrating the last expression we obtain

$$n\delta z = \begin{bmatrix} \frac{1}{2} & \frac{1}{2} & \frac{1}{2} \\ \frac{1}{2} & \frac{1}{2} \\ \frac{1}{2} & \frac{1}{2} & \frac{1}{2} \\ \frac{1}{2} & \frac{1}{2} & \frac{1}{2} \\ \frac{1}{2} & \frac{1}{2} & \frac{1}{2} \\ \frac{1}{2} & \frac{1}{2} & \frac{1}{2} \\ \frac{1}{2} & \frac{1}{2} & \frac{1}{2} \\ \frac{1}{2} & \frac{1}{2} & \frac{1}{2} \\ \frac{1}{2} & \frac{1}{2} & \frac{1}{2} \\ \frac{1}{2} & \frac{1}{2} & \frac{1}{2} \\ \frac{1}{2} & \frac{1}{2} & \frac{1}{2} \\ \frac{1}{2} & \frac{1}{2} & \frac{1}{2} \\ \frac{1}{2} & \frac{1}{2} \\ \frac{1}{2} & \frac{1}{2} \\ \frac{1}{2} & \frac{1}{2} \\ \frac{1}{$$

By developing this expression and subtracting therefrom the value of $n\delta z + n\delta^2 z$ we should have $n\delta^3 z$; but as this quantity has no particular interest we omit its derivation, and in the following value of $n\delta^3 z$ the terms corresponding to the arguments 5g' - 2g and 10g' - 4g are not given.

In writing a final form for the great inequality of Jupiter, we prefer to still further equate the motions of the arguments, so that the sum of the squares of the multipliers of nt in the coefficients may be a minimum. This gives, severally, in the cases of 5g'-2g and 10g'-4g

$$\log n = 6.8752079n$$
 $\log n = 7.12506n$

and the final form of $n\delta z$ will be

$$n\delta z = \begin{bmatrix} 1196.045 & -0.105371nt \end{bmatrix} \sin \left(5g' - 2g + \mu nt + 67 & 6 & 33.71 \right) \\ + & 0.00005546n^2t^2 & \sin \left(5g' - 2g + \mu nt + 48 & 46 & 1 \right) \\ + \begin{bmatrix} 11.0349 & -0.001654nt \end{bmatrix} \sin \left(10g' - 4g + \mu nt + 313 & 35.1 & 1 \right) \\ + & 0.00000477n^2t^2 & \sin \left(10g' - 4g + \mu nt + 311 & 21 & 1 \right) \end{bmatrix}$$

The great inequality excepted, the expression of $n\delta^3z$ follows. The proper number of decimals is restored to the factors of nt and n^2t^2 :

	$n\delta$	53 _Z
Arg=i'g'+ig	sin.	cos.
i' I	11 11 11	" " -0.00010214 n^2t^2 +0.000005231 n^3t^3
υ—· Ι	-0. $008207nt$ +0. $00002853n^2t^2$ +0. $0000000165n^3t^3$	-0. 004066 nt -0. 00003380 n^2t^2 +0. 0000000181 n^3t^3
0 2	$+0.0082-0.000172nt+0.0000034n^2t^2$ $+0.0000000002n^3t^3$	$+$ 0. 0071 $+$ 0. 00002 $8nt$ $-$ 0. 00000040 n^2t^2 $+$ 0. 0000000002 n^3t^3
o— 3	$-0.0004-0.000023nt+0.00000001n^2t^2$	+0.0008-0.000032nt-0.00000001n²t²
1+ 2 1+ 1 1 0 1- 1 1- 2 1- 3 2+ 2 2+ 1 2 0 2- 1	-0. 0025+0. 000100 nt -0. 0481-0. 000241 nt -0. 0822+0. 000382 nt +0. 00000019 n^2t^2 +0. 0002-0. 000085 nt +0. 0073-0. 000025 nt -0. 0014-0. 000035 nt -0. 0007-0. 000007 nt -0. 0439+0. 000011 nt -0. 1790+0. 002332 nt -0. 00000010 n^2t^2 -0. 0354-0. 000313 nt -0. 00000200 n^2t^3	$+0.0022+0.00037nt$ $-0.0401+0.000415nt$ $+0.0457+0.000400nt-0.0000015n^2t^2$ $+0.0109+0.00005nt$ $+0.0029+0.00005nt$ $+0.0043-0.000023nt$ $-0.0000+0.000011nt$ $-0.0053+0.000388nt$ $+0.2905+0.000841nt-0.0000011n^2t^2$ $-0.0704-0.000103nt-0.00000149n^2t^2$
2— 2 2— 3 2— 4	$-0.0577 - 0.00007nt + 0.0000005n^2t^2$ $+0.0001 - 0.000009nt$ $-0.0001 + 0.000003nt$	$+0.0272-0.000027nt+0.00000003n^2t^2$ +0.0023-0.00005nt -0.0003-0.00006nt
3+ 1 3 0 3- 1 3- 2 3- 3 3- 4	-0.0008-0.000054 nt -0.0094-0.002612 nt -0.1850-0.001274 nt -0.00000058 n^2t^2 +0.0549+0.000176 nt +0.00000107 n^2t^2 -0.0057-0.000017 nt +0.00000001 n^2t^2 -0.0008-0.000004 nt	-0. 0066 -0. $000005nt$ -0. 3892 +0. $000356nt$ -0. 1889 +0. $001538nt$ +0. $0000019n^2t^2$ -0. 0885 +0. $000140nt$ -0. $00000189n^2t^2$ -0. 0119 +0. $000006nt$ -0. $00000002n^2t^2$ -0. 0001 -0. $000004nt$
3 5	0.0000+0.000003nt	-0.0004+0.000000nt

Arc-i'a' ia	nd	\$3 ₂
Arg=i'g'+ig	sin.	cos.
i' i 4 0	,, ,, ,, ,, ,, ,, ,, ,, ,, ,, ,, ,, ,,	,, ,, ,, ,, ,, ,, ,, ,, ,, ,, ,, ,, ,,
4— I	-0. 0856+0. 000195 <i>nt</i>	+0.0272+0.000535nt
4— 2	$-0.0015+0.000234nt-0.00000018n^2t^2$	0. 0280+0. 000005 nt 0. 00000110 n^2t^2
4-3	$-0.0282+0.000009nt-0.00000041n^2t^2$	0. 01520. 000008nt0. 00000013n ² t ²
4— 4	-0.0010	+0.0003
4— 5	0.0004	—о. 0007
4— 6	+0.0008	0.0001
5 0	-0.0005+0.000015nt	-0.0005+0.000005nt
5— I	$+$ 0. 3539 $-$ 0. 000255 nt $+$ 0. 00000111 n^2t^2	—0. 3182—0. 000403 <i>nt</i> —0. 00000448 <i>n</i> ² <i>t</i> ²
5 3	-0.0274 -0.000218 nt +0.00002074 n^2t^2	$+$ 0. 0200 $+$ 0. 00379 $8nt$ $-$ 0. 0000039 $2n^2t^2$
5— 4	$+$ 0.0017 $-$ 0.000040 nt $-$ 0.00000010 n^2t^2	$-0.0074+0.000030nt+0.00000030n^2t^2$
5 5	+0.0012	+0,0006
6— 1	+ 0. 0009	0,0030
6— 2	-0.0175+0.000021nt	0. 01490. 000058nt
6— 3	$+0.0690-0.000442nt+0.00000003n^2t^3$	-0, 0418-0, 000478nt-0, 00000003n ² t ²
6 4	+0.0025-0.000025nt	o. 0058+-o. 000006nt
6— 5	+0.0024	0, 0000
6— 6	-0.000I	+0.0006
7— 2	—0. 0288+0. 000005 <i>nt</i>	o. 0066+o. 000028nt
7— 3	$-0.0745-0.002047nt+0.00000011n^2t^2$	$-0.2058+0.000806nt+0.000000000n^2t^2$
7— 4	-0. 2996-0. 001906nt-0. 00000014n ² t ²	$-0.2997+0.002625nt-0.00000009n^2t^2$
7— 5	+0.0017—0.000050 <i>nt</i>	-0.0047-0.000005 <i>nt</i>
8— 2	+0.0088	-0.0038
8 3	-0.0275-0.000172nt	-0.0059+0.000266nt
8— 4	+0. 2187+0. 000263nt	+0.05690.002070nt
8 5	+0.0286-0.000337nt	-0.0412-0.000174nt
8— 6	0. 0000—0. 0000I4nt	o. 0009+0. 000000nt
9— 3	0, 0005	—0. 0008
9— 4	+0.0580-0.000245 <i>nt</i>	0.01280.000596nt
9— 5	+0.0046-0.000575nt	-0. 0558+0. 000049nt
9— 6	+0.0173+0.000021nt	+0.0052-0.000109ni
9— 7	+0.0004 0.000000nt	-0.0001-0.00003nt
10— 5	+0. 1907+0. 003683nt	+0.4746-0.002499nt
10 6	+0.0127+0.000025nt	+0.0042-0.000101 <i>nt</i>
10 7	0.0003+0.000037 <i>nt</i>	+0.0050-0.00003nt
11 5	+0.0047+0.000028nt	+0.0042—0.000061nt
11— 6	+0.0064-0.000045 <i>nt</i>	-0.0032-0.000045 <i>nt</i>
11 7	+0.0014+0.000023nt	+0.0037-0.000015nt
11- 8	0.0012 0.000000 <i>nt</i>	+0.0002+0.000009nt
12- 5	—0. 0210—0. 000004 <i>nt</i>	+0.0341—0.000064 <i>nt</i>
12— 6	-0. 0122-0. 000067 <i>nt</i>	+0.0372—0.000013nt
12- 7	+0.0022+0.000005 <i>nt</i>	+0.0018-0.000009nt
12— 8		+0.0007+0.000006nt
12— 9	-0.00010.00005 <i>nt</i>	0.0008+0.000000nt

As it is not necessary for practical purposes that the radius-vector should be known to the same degree of accuracy as the longitude and latitude, we might neglect all the terms of three dimensions in it; but as it is extremely easy to derive from $\delta^2 W_0$ the portion of $\delta^2 \nu$ which depends on it, and the remaining portion is probably of considerably less importance, this quantity has been derived from the equation

$$\delta^2 \nu = -\frac{1}{2} \int \left(\frac{\overline{d \cdot \delta^2 W_0}}{d \gamma} \right) n dt$$

It is thought unnecessary to go to the labor of deriving the constant term, probably very small. Also the two terms factored severally by nt and n^2t^2 and independent of g and g' have been obtained by multiplying the similar terms having the argument -g by a factor whose logarithm is 8.3828:

	δ^{2}	ν		
Arg=i'g'+ig	cos.	sin.		
i' i	11 11 11	,, ,, ,, ,, ,, ,, ,, ,, ,, ,, ,, ,, ,,		
0 0	$-0.000098nt+0.00000034n^2t^2$			
o 1	$+$ 0. 0149 $-$ 0. 004044 nt $+$ 0. 00001427 n^2t^2	+0.0326+0.001966nt+0.00001690n ² t ²		
1 1	$+0.0000000082n^3t^3$	0. 0000000090 <i>n</i> ³t³		
0 2	$+0.0087-0.000157nt+0.0000034n^2t^2$	$-0.0056-0.000013nt+0.00000040n^2t^2$		
1 :	$+0.0000000002n^3t^3$	0. 0000000002 n^3t^3		
o— 3	$+0.0003-0.000021nt+0.00000001n^2t^2$	$-0.0002+0.000029nt+0.00000001n^2t^2$		
1+ 2	+0.0009-0.000067 <i>nt</i>	0.0007+0.000030nt		
1+1	+0.0308+0.000141nt	—0. 0264+0. 000248nt		
1 0	+0.0199-0.000094 <i>nt</i> -0.0000005 <i>n</i> ² <i>t</i> ³	$+0.0077+0.000107nt-0.00000002n^2t^2$		
ı— ı	-0.0002-0.000025nt	-0. 0040-0. 00000 <i>3nt</i>		
I 2	+0.0056—0.000019nt	-0.0016-0.000050nt		
I— 3	0. 00150. 000035nt	-0.0042+0.000019 <i>nt</i>		
2+ 2	+0.0007+0.000004nt	0.0000+0.000007 <i>nt</i>		
2+ 1	+0.0258—0.000005nt	0. 0025+0. 000227nt		
2 0	+0.0715-0.000954nt+0.00000001n ² t ⁹	+0. 1144+0. 000363nt+0. 00000002n ² t ²		
2— I	-0. 0026-0. 000087nt-0. 00000026n ² t ²	$+0.0118+0.000005nt+0.00000020n^2t^2$		
2— 2	-0, 0242-0, 000002 <i>nt</i> -0, 00000002 <i>n</i> ² <i>t</i> ²	$-0.0118+0.000006nt-0.00000002n^2t^2$		
2— 3	0. 00030. 000009nt	0.0026+0.000000 <i>nt</i>		
2— 4	—0. 0019—0. 000003 <i>nt</i>	+0.0005+0.000010nt		
3+ 1	+0,0005+0,00003 <i>2nt</i>	-0.0052+0.000005 <i>nt</i>		
3 0	+0.0045+0.001218nt	-0. 1838+0. 000165 <i>nt</i>		
3— т	+0.0235+0.000192nt	-0.0298+0.000207 <i>nt</i>		
3— 2	$+0.0230+0.000080nt+0.00000042n^2t^2$	$+0.0284-0.000062nt+0.00000076n^2t^2$		
3-3	-0.0045-0.000006 <i>nt</i>	+0.0078+0.000000nt		
3— 4	-0, 0009+0, 000000nt	0.0000+0.000004 <i>nt</i>		
3— 5	0.0000+0.000005nt	+0.0007+0.000000nt		
4 1	+0.0185—0.000043 <i>nt</i>	+0.0067—0.000146nt		
4 2	$-0.0010+0.000057nt+0.00000000n^2t^2$	$+0.0015+0.000000nt+0.00000015n^2t^2$		
4-3	-0.0171+0.00005 nt -0.0000020 $n^2\ell^2$	$+0.0086+0.000007nt+0.00000006n^2t^2$		

A	δ	ry
Arg=i'g'+ig	cos.	sin.
i'	11 11 11	и и и
4— 4	— 0. 0008	0.0000
4 5	0.0002	+0.0004
4 6	+0.0004	+o.0001
5 1	-0. 1784+0. 000408nt	—0. 1600—0 . 000 297 <i>nt</i>
5— 2	$-$ 0. 1966 $-$ 0. 002443 nt +0. 00000180 n^2t^2	+0. 3840-0. 001443nt-0. 00000192n ² t ²
5— 3	$+$ 0. 0064 $+$ 0. 000011 nt $+$ 0. 0000085 $8n^2t^2$	$-0.0099-0.001625nt+0.00000252n^2t^2$
5— 4	$+$ 0.0014 $-$ 0.000005 nt $+$ 0.00000020 n^2t^2	$+0.0053-0.000040nt+0.00000005n^2\ell^2$
5 5	+0.0020	-0.0010
6— 2	+0.0036-0.000010nt	-0.0021-0.00001 <i>2nt</i>
6— 3	+0.0152—0.000094 <i>nt</i>	+0.0086+0.000103 <i>nt</i>
6— 4	+0.0007-0.000019nt	+0.0045+0.000000nt
6 5	+0.0027	0.0000
6 6	0,0003	—o, oo12
7 2	+0.0131-0.00002nt	-0.0017+0.000013 <i>nt</i>
7— 3	-0.0127-0.000226nt	+0.0243—0.000121nt
7 4	-0. 1427-0. 000922nt	+0. 1430—0. 001279 <i>nt</i>
7 5	0.00210.000023nt	+0.0042-0.000032nt
8— 3	+0.0054+0.000013nt	+0.0032+0.000032nt
8— 4	+0.0827+0.000087nt	-0.0195+0.000768nt
8 5	+0.0195—0.000219nt	+0.0266+0.000118nt
8 6	+0.0005—0.000011nt	+0.0012+0.00004 <i>nt</i>
9 4	+0.0130—0.000056nt	+0.0035+0.000098nt
9— 5	+0.0028-0.000315nt	+0.03200.000025nt
9 6	+0.0104+0.000013nt	-0.0031+0.000084 <i>nt</i>
9— 7	+0.0007	-0.0001
10— 4	-0. 0223+0. 000246nt	—0. 0298—0. 000119nt
10 5	+0.0820+0.001652nt	-0. 2042+0. 001135nt
10 6	+0.0105+0.000020nt	0. 0044+0. 000091 <i>nt</i>
10 7	-0.0006+0.000034 <i>nt</i>	-0.0044+0.00000 <i>nt</i>
11- 5	+0.0012+0.00007 <i>nt</i>	-0.0012+0.000017nt
11— 6	+0.0043-0.000032nt	+0,0030+0.000025 <i>nt</i>
11 7	+0.0013+0.000028nt	o, 0036+0, 000015 <i>nt</i>
11 8	0.0023+0.00003 <i>nt</i>	-0.0002-0.000017nt
12— 6	o. 0063o. 000038nt	o. 0193+0. 000008nt
12— 7	+0.0018+0.000005nt	0.0016+0.000009nt

CHAPTER XIX.

CALCULATION OF THE SEVERAL PORTIONS OF 8°T'.

The fourteen parts of the portion of $\delta^2 T'$ not factored by n't or $n'^2 t^2$ are as follows:

Aı	rg=		A'n'	$'\delta^2z'$	B'6	$\delta u'$	F'1	$\imath\delta^2z$	G.	΄δν
А 1 иу′+	·i′g′-	⊦ig	sin.	cos.	sin.	cos.	sin.	cos.	sin.	cos.
н	i'	i	"	"	11	"	"	"	"	11
٥	0	0		0. 000397		+0.002185		+0.001252		_o. ooo69 6
-1	I	0		0. 000491		-0.001914		o. oo1353	l	+0.000999
—I	2	0		+0.00113		0. 00257		-0. 00207	ł	0.00036
0	I	0	o. 076 7	+0.0411	o. oo64	+0.0064	-0.0195	+0.0080	0.0007	+0.0012
I	0	0	+o. o88669	-0. 051402	+0.010129	—0. 004636	+0.015432	—o. oo8o46	+0.003443	-o. 00185 7
— I	3	0	+0.011	0. 008	+0.003	-0.004	+0.018	-0.015	+0.004	-0.002
0	2	0	—о. 161	+0. 245	—о. 038	+0.040	o. o46	+0.068	0.008	+0.006
1	I	0	+o. 206	-0. 334	+0.042	-0.049	+0,041	—о. обб	+0.007	-o. oo7
I	4	0	0.000	0.023	•		0. 001	-0, 020		
0	3	0	+0.014	+0.431	o. oo5	-0.020	+0.006	+o. 187	1	
I	2	0	0, 004	0. 784	0.001	+0.013	0, 002	—0. 229		
٥	4	0	+0. 12	0.04			+o. 11	— 0. 03		
I	3	0	0. 064	+o. o38			-o. o35	+0.015		
—ı—	- 2—	- I	0. 03	0. 02			-o. oı	-o. oi		
-1-	- I-	- 1	+o. 652	0. 147			+0.213	-0.045	0, 009	+0.002
0-	- 2-	- I	o. 43	+0. 10			-o. 18	+0.04	+0.02	0,00
1—	- 3	- І	+0.05	o. oı			+o. o3	0.01	-0.02	0.00
— I	0	- т	+o. 263	—o. 229	+0.028	-o. o38	+0.065	0. 054	+0.008	-0.007
0—	- I-	- т	0. 193	+0. 169	-0. OI7	+0.024	0.072	+0.061	-0.016	+0.015
1—	- 2—	- х	+o. o16	0, 021			+o. o26	-0. 024	+0.014	-0.012
— 1	1—	. I	+0.035	o. o88	0.001	0.010	+0.007	0.022	-0.001	-0, 002
0	0-	. 1	0.028	+0.072	+0.002	+0.008	0.009	+0.026	-0,001	+0.003
1	· I—	. 1	0,000	-o. oo8				,		,5
1	2—	. 1	0.0014	0. 0209	0. 0047	—0. 0211	-0.0017	0.0041	+0.0007	+0.0005
0	ı—	1	+0.006	+0.008	+o. oo6	+0. 020	+0.001	+0.004	0.000	+0.001
I	0	. 1	0.001	+0.012	·		,	,		' -, -, -, -
-1	3-		0. 0069	-o. oo68	+0,0046	+0.0036	+0.0001	+0.0008	0.0011	0.0007
o	2—	- 1	+0.0043	0.0259	-o. o166	-0.0128	-0.0073	-0.0113	+0.0025	+0,0009
1	ı—	1	+0.0166	+0.0443	+0.0108	+0.0120	+0.0093	+0.0132	0.0019	—0.000 7
—I	4—	_I	0, 0302	-0.0050	+0.0106	+0.0002	-o. oo38	+0.0031	0.0085	-0.0007
0	3	- 1	+0.1400	-0.0230	-0.0972	-0.0438	-0.0196	-0.0272	+0.0140	l I
I	2—	- 1	+0.0773	+0.0845	+0.0826	+0.0409	+0.0477	+0. 0290	0.0111	+0.0022
	_		,,,	1	,	1 0.0409	1 0. 04//	10.0290	0.0111	0.0010

Arg=	$\mathbf{A}'n'$	$\delta^2 z'$	B'0	$\delta v'$	$\mathbf{F}'n$	$\delta^2 z$	G'	δν
$rac{ ext{Arg}=}{\kappa \mathcal{Y}'+i'g'+ig}$	sin.	cos.	sin.	cos.	sin.	cos.	sin.	cos.
μ i' i —I 5— I	11	н	+0.003		o. 616	// +0. 122	+0.007	+0.002
0 4— 1	+1.145	—0. 220	+o. 017	0.000	+0.498	—о. 098	-0.020	⊹0. ∞1
I 3— I	—0. 1892	+o. o368	-0.0146	—o. ooo7	0. 0525	+0.0093	+0.0190	o. oo35
o 5— 1	+0.004	-o. o15		1				
I 4— I	+0.030	+0.014						
-I- I- 2	+0.03	0. 05						
0- 2- 2	0. 02	∔0.03						
_I 0— 2	+0. 22	+0.45			+0.07	+o. 16		i
0— I— 2	o. 16	-o. 33			-0.07	0. 15		
I 2 2	+0.02	+0.06			+o. o1	+0.03		
_I I— 2	+o. 25	+0.19	+0.02	+o. o2	+0. 06	+0.05		
0 0— 2	-0. 22	— 0. 14	—o, o2	0, 02	—o. oб	0. 05		
I— 1— 2	+o. o3	+o.01						
—I 2— 2	+0.094	+0.018	+0.015	0.000	+0.022	+0.004		
0 I— 2	0. 095	-0.011	—0. 011	0,000	-0.021	0.003		
<u>—</u> I 3— 2	+0.021	-0.007	+0.014	0. 007	+0.004	-0.002		
0 2— 2	-0. 025	+0.011	o. oo6	+0.003				
—I 4— 2	+0.0022	-0.0029	-0.0042	+0.0018	+0.0029	o. ∞36	-0.0004	+0.0009
0 3— 2	+0.021	—o. o18	+0.010	-0. 005	0.000	0.002	+0.002	0.002
I 2 2	0. 022	+0.020	0. 006	+0.005	-0. 002	+0.005		
—I 5— 2	-0.01236	+0.04481	+0.01920	-0. 05499	+0.01210	-o. o3234	—0. 0 0985	+0.01947
0 4-2	+0.0326	-0. 0799	—0. 0113	+0.0148	-0.0017	+0.0112	+0.0095	—o. o219
I 3— 2	o. o335	+o. 1346	0.0085	+0. 0448	—0. 0099	+0.0162	-0,0028	+0.0112
_1 6— 2	+0. 14474	+0. 35026	+0.00531	+0.01240	+0.00381	+0.00821	-0.00012	-0.00025
o 5— 2	+0.0042577	—0. 0026910	0. 0113662	—о. 0198853	0.0060156	—o. o136926	0, 0001245	—u. 001 39 62
I 4-2	+ 0. 14020	+0. 34072	+0, 00458	+0.00674	+0.00376	+0.01056	+0.00090	+0.00103
—I 7— 2	+0.090	+0.054	0,000	+0.003	+0.014	-0.004	0, 003	+0.003
o 6— 2	0.0519	-0.0073	+0.0128	-o. oo31	o. oo85	+o. oo61	+0.0057	0.0015
I 5— 2	0. 00406	-0.00712	—o. 01093	+0.00183	0.00374	-o. oo518	o. oo365	-o, ooo26
ı 8 2	+0.020	0. 001			1			
0 7 2	+0.019	+0.005					1	
ı 6— 2	-o. o51	-o. oo6						
o 8— 2	+0.032	—o. 019			:			
r o 3	+0.05	+0.02						
I I 3	— 0. 2 8	+0.21			-0.10	+0.07		
	+o. 2I	0. 17			+0.09	-o. o8		
I— I— 3		+0.03						
_I 2— 3	-o. II	+o. 25			0. 03	+0.07		
	+0.07	—0. 19			+0.03	0.06		
	o. oɪ	+0.03						
—ı 3— 3	+o. oi	+o. 10			0.00	+0.02		
o 2— 3	_o. oi	-0.09			0.00	0. 02	1	
_1 4 3	+0.012	+0.019						
1	o. oi	-0.02					ł	
	+ 0.014	+0.010			1		1	
	<u> </u>	!	<u> </u>		<u> </u>	1	<u> </u>	1

		$\mathbf{A}'n'$	δ^2z'	Β'δ	ν'	$\mathbf{F}'n$	$\delta^{2}z$	G'é	δν
μγ'+	g= $i'g'+ig$	sin.	cos.	sin.	cos.	sin.	cos.	sin.	cos.
	., .	"	//	"		"	<i>"</i>	"	"
—ĭ	i' i 6— 3	+0.018	+0.025	+0.089	+o. oo6	0.000	+o. oo8	+0.006	+0.001
0	5 3	_o. 127	-0.009	-0. 103	0.005	-0.012	0,000	,	<i>'</i>
1	4- 3	+0.003	-0.009						
-1	7 3	+o. 1584	-0. IO2I	-0.0002	-o, ooo6	+0. 0496	0. 0349	-0.0179	+0.0121
0	6— 3	— 0. 966	+0.651	+0.009	0, 011	-0. 423	+0. 298	+0.022	-0.015
1	5— 3		- 1	-0.010	+0.009	+0.516	о. 365		
-1	8 3	-0, 0049	+0. 1423	+0.0014	+0.0081	—0. 0049	+0, 0313	+0.0031	0, 0066
0	7— 3	-o. o831	0. 0234	+0.0034	—о. 0036	o. o132	0.0132	0.0039	+0.0084
1	6- 3	+0.0176	-0.0219	—0. 0038	—0.004 6	+0.0062	-o. 0028	+0.0029	-0.0046
-I	9-3	+o. o134	+0.0402	+0.0002	— 0. 0028	+0.0024	+0.0072	-0.0002	-0.0012
0	8 3	0.0247	— 0. 0590	+0.0016	+0.0277	0. 0038	—0. 0009	+0.0006	+0.0042
1	7- 3	+0.0062	0.0065	0.0017	-0. 0227	+0.0009	0.0079	-0.0004	-0.0042
-1	10 — 3	+0.006	+0.006			+0.025	+0.040		
α	9- 3	—o. o59	0, 082	0.004	0. 006	0.019	-o. o33	-0,002	0.000
1	8— 3	+0.0084	+0.0121	+0.0030	+0.0050	+0.0009	+0.0032	+0.0005	+0.0005
-1	2— 4	—о. 18	-o. 15			-0.07	0.05		1
0	I— 4	+0.15	+0.12			+ 0.06	+o. o5		
— т	3-4	—0. 17	0.04			0. 05	o. oı		
0	2 4	+o. 15	+0.04			+0.05	+o. o1		
_t	4 4	— 0. 07	+0.02						
0	3- 4	+0.06	-0. 02						
-1	5— 4	-0.02	+0,02						
—ı	7— 4	+o. o68	0.081	+0,009	+0.062	+0.035	-o, o15	0, 000	+o. 015
٥	6 4	—0. 105	+0.095	0, 006	о. 033	0. 095	+0.042	+0.001	-0, 032
1	5— 4					+0. 10	-0.04	0,00	+0.03
-1	8 4	0. 570	о. 565	+0.014	+0.012	167	0. 162		
٥	7— 4	+o. 308	+0.315	-o. o15	-0.012	+0. 132	+o. 133		
1	6 4					-0.015	-0.014		
1 -1	9— 4	-0. 309	—o. o78	0.007	+0.007	-0.064	0. 017	-0.004	-0,001
°	8— 4	+0. 226	+0.039	+0.010	0.009	+0.063	+0.010	+0.007	0, 004
1	7— 4	-0.013	+0.002	-0.003	0.001	0.016	+0.007		
_I	4	0, 06119	+0.01391	-0.01363	+0.00446	-0.02906	+0.00807	+0.01509	0, 00420
0	9— 4	+0.0529	0.0154	+0.0015	-0.0004	+0.0255	—o. oo8o	-0.0184	+0.0057
I	8— 4	+0.021	0,001	+0.014	0.004	-0.002	+0.002		
1 -1	11-4	+0.01289	0.01603	+0.00086	-0.00021	-0.00177	+0.00182	-0.0 0004	0.00007
0	10— 4	+0.007175 +0.02116	—0. 005886 —0. 02153	+0.001315 0.00230	0.001785	+0.001802	0.001870	-	+0.000222
1 1	9— 4	+0.0004		0.00230	+0.00256	+0.00029	+0.00019	-0.00048	+0.00005
0	11 4	'	0.0002						
_I	3— 5	+0.07	-o. 14						
0	2 5	0. 05	+0.12						
_I	4 5	0.00	—o. 13						
٥	3— 5	0, 00	+0.12						
-I	5— 5	—o. oз	—0. 06						
0	4- 5		+0.05						
1	8 5	+0.01	-o. o3	0. 04	+0.01	—о. 01	+0.01		
٥	7 — 5			+0.02	0. 01			•	
		· · · · · · · · · · · · · · · · · · ·						<u> </u>	

A.	rg=	$\mathbf{A}'n'$	δ^2z'	В'8	ìv'	$\mathbf{F}'n$	$\delta^2 z$	G'6	δν
жу′+	$\vec{i'g'}$ + ig	sin.	cos.	sin.	cos.	sin.	cos.	sin.	cos.
и	i' i	"	//	"	"	11	11	11	"
—I	9 5	+0. 364	o. 582	-0, 010	+ 0. 014	+0.113	о. 187	—о. 006	+0.010
0	8 5	—0. 24	+0.40	+0.01	o. oi	0, 09	+0.15	+0.02	-0. 02
1	7 — 5					+0.01	-0.02	—о. от	+o. 01
—ı	10— 5	+0, 035	—о. 311	-0.007	0,000	+0.004	0. 082	0,000	0.004
٥	9- 5	0. 026	+0.230	+0.001	0. 006	0.004	+0.083		
1	8— 5	0, 004	-0.026			-0.001	0.021	0,000	—o, oo8
—т	11— 5	-0. 032	0. 081	-0.012	-0.022	-0.009	0.018		
1	10 5	+0,042	+0.092	+0, 014	+0.026	+0.008	+0.017		
I	9 5	0. 006	0.006						
	12 5	-0. 0223	-0.0187	+0.0007	+0.0008	—o, oo58	0, 0036	о. оооб	+0.0003
1	11 5	+0.093	+o. o61	-0.003	-0.001	+0.037	+0.023	o. oo1	-0.001
I	10 5	;				0. 042	0, 026		
-1	13 5	+0.0094	0.0055	+0.0002	0.0000	+0,0010	—o. ooo6		
٥	12— 5	+0.0022	+0.0074	0. 0003	-0.0001	+0.0006	- 0.0014	0,0001	u. 0000
ı	11- 5	0.0013	0. 0008						
-1	4 6	+o. 10	+0.02						
0	3— 6	-o. o8	_o. o1					ł	
-1	5— 6	+0.09	0.02						
0	4 6	o. o8	+o. o1						
-1	9 — 6	+0. or	o. oi			ŀ			
0	8 6	0.00	+0.03						
—x	10— 6	+0.51	+0.19		·	i		l .	
0	9 — 6	—о. 36	—o. 12						
1	8— 6	+0.06	+0.02						
1	11 6	+0.29	0.04			i		i	
0	10— 6	—u. 22	+0.03						
1	9— 6	+o. o3	-o, oı					1	
—I	12— 6	+0.054	-o. o32					ļ	
0	11 6	0.041	+0.041						
—ı	13 6	o. o18	+0.050	1				ļ	
0	12 6	+0.008	0.022						
_I	10— 7	+0.05	-0, 02						
-1	11- 7	o. o4	+o. 35]			
0	10— 7	+0.03	0. 27						
-1	12- 7	+o. o8	+0. 22						
	11- 7	o. o6	o. 17						
_ī	13 7	+o. o5	+0.04						
	12 7	0. 05	o. o5						
1		L	1		1	I		I	

Ar _i	g=	i a	$\frac{1}{2}\frac{d\mathrm{A'}}{dg'}($	$n'\delta z')^2$	$rac{d\mathbf{A}'}{dg}(n\delta z)$	$(n'\delta z')$	$\frac{1}{2}\frac{dF'}{dg}$	$(n\delta z)^2$	$rac{d\mathrm{B}'}{dg'}(n$	'δz')ν'
<i>ky</i> +	<i>v y</i> +	*y	sin.	cos.	sin.	cos.	sin.	cos.	sin.	cos.
ж	i'	i	"	11	11	11	11	"	11	"
0	0	0		+0.001323		—o. ooo177		0.000105		-0.000118
_I	1	0		0.003627		—o. ooo367		+0.000106		+0.000541
-1	2	0		-0. 01414		+0.00014		+0.00022		0. 00290
0	I	0	0, 0063	+0.0032	+0. 0044	—o. oo45	+0.0015	-0. 0007	+0.0030	-0.0012
I	0	0	o. oo7885	-0. 002139	-0.003072	0.000028	0. 002474	+0.001186	-o. ooo383	+0.000970
—ı	3	0	+0,001	—o, oo4						
0	2	0	0. 010	+0.008	o. oo6	-o. ooi			0, 002	-0.003
ī	I	0	-0, 002	—o. o16	0.004	0.000			0. 003	+0.010
0	3	О	+0.007	+o. o13					+0.003	-0.014
1	2	o	-o. o17	—о. озз					-0.007	+0.019
· 0	4	О	+0.02	+0.04						
1	3	0	0.053	o. o5o						
-1	0-	. 1	+0.006	+0.024					_o. oog	+0.002
0	- 1		0,000	-0.008			1		0,009	1 5. 552
	ı—		+0.013	+0.014	+0.004	+0.009			+0. ∞5	0. 020
D	0-		-o. oo8	+0.012	— 0. 003	+0.009	1		-0.004	+0.015
— I	2-		+0.0053	_o. o187	+0.0001	-o. oo63	о. 0003	-0.0012	-0.0021	-0.0047
	ī.	,	+0.012	+0.084	+0.014	+0.067	+0.003	+0.014	+0.001	+0.004
ı	0—		1 0.012	0.004	1 0.024	0.007	0.004	-o. o18	1 0.001	1 0.004
-1	3-		+0.0299	+0.0111	+0.0108	+0.0075	+0.0013	+0.0017	+0.0154	+0.0193
0	2		+0.0014	+0.0231	+0.0027	+0.0076	-0.0001	-0.0001	-0.0067	-0.0098
1	1—		+0.0024	-0.0042	-0.0025	-0.0028	0,000.	0,0001	-o. 0048	-0.0035
—п	4		+0.0227	+0.0037	+0.0049	+0.0007			+0.0052	+0.0048
0	3—		-0.0119	+0.0040	0.0004	+0.0017	+0.0016	+0.0005	+0.0019	+0.0021
1	2—		+0.0050	—o. oo67	-0.0021	-0.0028	-0.0022	-0.0007	-o. oo85	-0.0052
-1	5		+0.005	_0.002				,	—o. oo7	+0.002
0	4		_o, o16	+0.013	o. oo6	+0.005	+0.001	0, 000	0.000	+0.002
1	3—		+0.0220	_o. o19o	+o. oo36	_o. oo65	+0.0012	0. 0006	0. 0108	-0.0047
0	5—		0.019	+0.029	, ,		l '		—o. ooუ	+0.005
1	4—		+o. o38	_o, o56					+0.012	-0. 02 1
0	6—		_0.017	+0.051						.=
1	5	I	+0.032	0. 095						
		i	_o. o3	0.00						
_'	I—			o, 001	0.013	-0.012			±0.006	Lo 600
1-1	Z— I—	2	o. o56 o o56		-0.00I	1			+0.026	+0.002
0	1—		+0.016	+0.013 +0.086		+0.015	0 072	1.0 00"	-0.011	0.001
-I	3	2	—o. 186	0.028	-0.09I	+0. 036 -0. 036	0.012 0.010	+0.005	+0.009	-0.005
0	2		+0.069		+0.047	—0. 019 —0. 0455	+0.010 0.0038	-0.004	0.005	+0.002
	4	2	—0. 0817	+0.1122	—0. 0350 +0. 022	+0.0455	+0.0038	+0.0047	-0.0131	+0.0169
0	3—		+0.035	0. 050 0. 04529	—0. 00072	—0. 027 —0. 01604	-0, 0002 -0, 00002	-0.003	+0.007	-0.009
1—1	5—		o. 00375 o. 0060	-0.04529 -0.0211	o, oo66		-0.0002 -0.0018	+0.00178	-0.00875	+0.00902
	4—			i l		-0, 0033 -0, 0043		0.0013	+0.0045	-0.0023
'	3—		+0.0015	+0.0038	+0.0008	-0.0043	+0.0014	-0.0007	+0.0027	0,0080
	6—		+0,00285	+0.01340	0. 00273 0. 0028286	-0.00425	-0.00131	-0.00289	—o. oo867	-0, 01349
°	5—			—o. o113586		+0.0074037		+0.0042305		+0.0137355
I	4	2	+0.00597	+0.00996	0.00034	—o. 00347	0.00090	—o. oo265	+0.00247	0. 01047

Aı mari I	rg= $-i'g'+ig$	$\frac{1}{2}\frac{dA'}{dg'}$	$n'\delta z')^2$	$rac{d\mathbf{A}'}{dg}(n\delta z)$	$(n'\delta z')$	$\frac{1}{2}\frac{d\mathrm{F}'}{dg}$	$(n\delta z)^2$	$rac{d\mathrm{B}'}{dg'}(n')$	$(\delta z') u'$
ny +	-i y +iy	sin.	cos.	sin.	cos.	sin.	cos.	sin.	cos.
ж	i' i	"	"	11	"	11	"	11	11
—ı	7- 2	+0.002	+0.003	-0.002	0.002			-0.004	0, 002
٥	6— 2	0.0053	-o. 0147	+0.0019	0.0070	+0,0011	-0.0017	0. 0096	0.0022
1	5— 2	+0.02512	+0.02192	+0.01108	+0.01018	+0.00134	+0.00148	+0.01919	+0.00687
—ı	3— 3	-0. O2	-o. o5					0,00	+0.03
0	2- 3	0.00	+0.03						
-1	4-3	о. 131	—о. 186	 0. 068	—o. o96	-0.011	-o. o15	+0.009	+o. oi i
0	3 3	+0.07	+0.10	+0.05	+0.06	+o. o1	+0.01		
-1	5- 3	0. 156	0. 083	-0.072	-0.034	0. 007	0,003	-0, 024	-o. o13
ø	4 3	+o. o83	+0.040	+0.046	+0.022	+0.006	+0.003	+0.014	+0.007
-1	6— 3	o. o85	0.015	-o. o33	0,006			o. o16	o. oo6
О	5— 3	+0.047	+0.004	+0.022	+0.002			+0.009	+0.002
-1	7- 3	0. 0264	+0.0048	0. 0039	0.0020	-0.0009	+0.0003	+0.0124	—о. 0107
0	6— 3	+0.017	-o. oo5	+0.008	+0,002	+0.001	0.000	0.001	+0.004
-I	8— 3	—o. oo68	-0.0018	+0.0001	0. 0025	+0.0009	-0.0020	+0.0039	-0. 0062
٥	7— 3	+0.0072	-0.0014	+0.0009	+0.0019	-0.0005	+0.0013	+0.0015	0.0021
I	6— 3	-o. oo8o	+0.0122	0. 0028	+0.0037			0.0040	+o. o128
-1	9— 3	-0.0024	-0.0005	-0.0001	-0.0013			+0.0003	-0.0012
О	8 3	+0.0073	+0.0185	+o. oo26	+0.0060	-0.0002	-0.0011	0, 0009	o. o137
1	7- 3	o. oo53	+o. 0081	-0.0012	+o. oo86	0,0000	+0,0020	+0.0015	+0.0245
0	9- 3	+0.023	+0.034	+0.019	+0.028	+0.004	+0.006	+0.002	+0.002
1	8 3	0. 007 г	—о. 0106	-0, 0030	0. 0046			0.0028	—o. oo35
-r	4 4	+0.04	0.02						
— I	5 4	+0. 15	—о. 16	+0.08	— 0. 09	+0.01	0. 02		
0	4— 4	0.07	+0.08	0.06	+0.06				
1	6 4	+o. o3	—о. 16	+0.02	o. o8			+0.01	о. оз
0	5— 4	0.02	+0.11	-o. oi	+0.05				
_ı	7— 4	-0.006	-0.097	-0.001	0. 042			+0.003	0.019
О	6 4	+0.006	. + 0. 061	+0.004	+0.017			+0.002	+0.010
—ı	8— 4	o. o16	0. 034	0,000	-0.007			+0.013	+0.014
٥	7— 4	+0.012	+0.022	0.005	-0.005			0.009	-0.012
-1	9— 4	o. o11	-o. oo6	0.000	-0.002			+0.003	+0.008
0	8— 4	+0.013	-0.002	+0.003	0, 006			+0.001	0.004
I	10— 4	+0.00546	0.00744	+0.00076	-0.00152	+0.00251	—o. ooo68	0.00479	+0.00209
0	9 4	+0.0040	0.0000	-0.0056	+0.0007	0.0018	+0.0005	0.0009	-0.0001
-1	11 4	+0.01013	-0.01421	+o. 00007	-0.00064			0.00013	+0.00080
0	10— 4	+0.000387	+0.001219	+0.000027	+0,000300	0. 000008	+0.000040	+0.000100	-0.000083
1	9 4	—0. 00907	+0.00932	-0.00020	+0,00008			+0.00067	-0.00107
0	11— 4	0.0002	+0.0012						
_ı	6— 5	+o. 14	+o. o8	+0.09	+0.05				
	5— 5	—0.09	-o. o5	— 0. 07	о. оз				
_ı	7 5	+o. 16	0.00	+0.07	0.00				
0	6— 5	0.09	0.00	_o. o6	0.00	1			
_I	8 5	+0. 10	0, 02	+0.02	o. or	1		+o. o1	0.01
0	7 5	0. 05	+0.03	0. 02	+0.01				
		<u> </u>		<u> </u>		<u> </u>			

	-							
$Arg = \\ \mathcal{V}' + i'g' + ig$	$\frac{1}{2}\frac{dA'}{dg'}$	$(n'\delta z')^2$	$rac{d{ m A}'}{dg}(n\delta z$	$rac{d { m A}'}{d g}(n \delta z) \; (n' \delta z')$		$(n\delta z)^2$	$rac{d\mathrm{B}'}{dg'}(n)$	$(\delta z') u'$
<i>17</i> + <i>9</i> + <i>19</i>	sin.	cos.	sin.	cos.	sin.	cos.	sin.	cos.
$ \begin{array}{c cccc} & i' & i \\ & -1 & 9-5 \\ & 0 & 8-5 \end{array} $	// +0.033 0.02	,, 0. 024 -+0. 01	"	"	"	"	_o. o16	+0.018
-I 10-5 0 9-5 -I 11-5	+0.022 0.006 +0.009	+0.014 0.007 0.002	+0.008	+0.014			0, 006 0, 014	0. 00 2 0. 023
o 10 5 -1 12 5	+0.000 0.0000	+0.015	+0.004 0.0020	+0.008 0.0029			+0.007 -0.0025	+0.014 —0.0010
o 11— 5 —1 13— 5	+0.032 +0.0179	+0. 025 -0. 0075		+0.018 -0.0016			+0.001 0.0002	+0.0003 +0.0003
0 12 5 1 11 5	-0.0013 -0.0004	+0.0070 0.0004	0. 0003	+0.0026			+0.0003	—0. 00 02
-1 7-6 o 6-6 -1 8-6	-0.03 +0.02 +0.02	+0. 12 -0. 08 +0. 11						
o 7-6 -r 9-6	0.01 +0.03	0. 08 +0. 04						
o 8 6 1 10 6 1 11 6	-0.02 +0.03 0.01	-0.03 +0.03 +0.02						
-1 12-6 o 11-6	-0.032 +0.013	+0.041 -0.019						
-1 13-6 0 12-6	0.036 +0.015	+0. 100 0. 038						
— i 8— 7 о 7— 7	-0.09 +0.07	0.00						
o 8-7	0. 08 +0. 06 0. 03	+0.03 0.03 0.02						
0 12-7	+0.01	+0.02						

Ar ny'+	·g=		$rac{d\mathrm{B}'}{dg}(n\delta)$	(z) u'	$rac{d{f G}'}{dg'}(n'$	$\delta z') u$	$rac{d{ m G}^{\prime}}{dg}$ (1	$\imath \delta z) u$	$\frac{\mathbf{I}}{2} r'^2 \frac{d^2}{dt}$	T',/2 V'2
hy +	<i>vg</i> +	-ig	sin.	cos.	sin.	cos.	sin.	cos.	sin.	cos.
н	i'	i	11	11	11	//	//	"	"	11
ő	o	ō		0. 000226		+0.000254		+o.000040		-0.000297
—·I	I	o		+o. 000223		-0. 000147		o. oooo28		+0.000338
-1	2	0	'	0.00010		0.00195		0. 00042		-0.00070
0	I	О	+0.0018	0. 0001	-0.0034	+0.0014	0.0021	+o. 0011	+o. ooo1	0.0011
1	o	О	-0.002155	+0.001478	-0.001393	+0.000899	+0.001197	-0.000521	0. 000554	+0.003166
0	2	0	+0.002	0.000						
I	¥	0	+0.002	+0.003	-o. oo1	+0.001			0.004	+0.005
ı	2	0	-0.001	+0.004						
—I	I —	1	+0.001	0. 004						
0	0	· I	-0.002	+0.006	,					
-1	2—	ı	-0.0011	-0.0029	+0.0001	+0.0015			0.0024	—o. oo82
0	I —	. 1			·				+0.001	+0.003
1	o—	· I							+0.001	+o. oo3
-1	3-	- т	+0.0025	+0.∞33	+0.0032	+0.0040	+0.0008	+0.0007	+0.0003	-0.0017
0	2—	· I	-0, 0024	0. 0038	-0.0020	0. 0007	-o. ono3	-0.0001	+0.0013	+0.0017
1	1—	· I	-0.0007	0. 0005	-0.0010	0. 0018			-0.0021	+0.0004
т	4-	- I	+0.0015	+0.0006	+0.0015	+0.0005			+0.0021	+o. ooo6
0	3	- I	+0.0011	+0.0006	+0.0002	+0.0005	-0.0001	+0.0001	+0.0011	+0.0009
1	2—	- I	0. 0027	0.0018	-0.0025	—o. oo16	—0, 0003	-0.0002	0.0042	0. 0024
0	4-	- 1	+0.002	0.000	+0.011	-0.003			0.000	+0.001
1	3—	- I	—0. 0019	0. 0007	—o. oo23	0.0000	0.0017	+0.0002	+0.0025	0. 0020
—ı	3	- 2							+0.008	0.003
—I	4-	- 2	-0. 0029	+0.0039	0, 0033	+0,0040	0. 0008	+0.0010	+0.0032	0.0000
0	3-	- 2	+0.002	0, 004			i			
—I	5—	- 2	0.00190	+0.00326	-0.00190	+0.00330	0. 00035	+0.00098	-0.00042	+0.00421
0	4	- 2	+0.0021	-0,0010	+0.0015	-0.0019	+0.0005	0.0003	+0.0001	0,0001
I	3-	- 2			+0.0011	0. 0022			+0,0002	0.0041
—ı	6	- 2	0.00167	0. 00324	-0.00161	-0. 00298	0, 00022	0.00041	-0.00024	+0.00023
0	5	- 2	+0.0017479	+0.0062521		+0.0003996		+0.0004123	—o. ooo9770	0.0010015
I	4-		+0.00004	-0. 00252	+0.00021	—o. oo16 7	+0.00011	—o. oooo5	+0.00192	+0.00135
٥			0.0041	0. 0009	-0.0018	-0. 0008	l .		0.0013	-0.0010
1	5—	- 2	+o. oo386	+0.00135	+0.00474	+0.00230	+0.00113	+0.00051	+0.00169	+0.00168
-1	5-	- 3	-0. 007	0.003						
1	6	- 3	0. 003	-0.002	0.002	0.000				
I	7-	- 3	+0.0029	-o. oo28	+0.0037	-0.0029	+0.0040	0. 0025	0.0007	-0.0007
0	6—	- 3	0, 002	+0.002	-o. o og	+0.006				
1	8—	- 3	+0.0003	-0.0017	+0.0009	-0. 0023	-0.0001	+0.0002	+0.0004	0.0009
0	7—	- 3	0.0002	+0.0004	+0.0015	0.0017	+0.0003	0. 0004	+0.0007	-0.0011
1	6—	- 3	-o. ooo8	+0.0017	0. 0022	+0.0041	1		-0.0012	+0.0026
—r	9—	- 3	+0,0001	+0.0007	0. 0003	0. 0009				
0	8	- 3	0, 0005	—o. oo65	+0.0001	0. 0013	+0,0001	-0. 0005	0.0000	+0.0003
1	7—	- 3	+o. 0004	+0.0056	+0. 0002	+0.0038	0.0000	+0.0010	1	
						l	<u> </u>	1		1

Ai	rg= -i'g'+ig	$rac{d\mathrm{B}'}{dg}(n\delta z) u'$		$rac{d\mathrm{G}'}{dg'}(n'\delta z') u$		$rac{d{ m G}'}{dg}(n\delta z) u$		$\frac{1}{2}r'^{2}\frac{d^{2}T'}{dr'^{2}} u'^{2}$	
"	* 9 T*9 :	sin. cos.		sin.	сов.	sin.	cos.	sin.	cos.
ж —I	i' i 8 4	"	"	// 	,, +0.004	"	"	"	"
-1	9— 4	0.000	+0.002	+0.002	+o. 002				
0	8 4	+0.002	o. oo1						
1	10— 4	+0.00050	-0.00018	+o. ooo68	-0.00033	0.00182	+0.00039	-0.00019	+0.00002
0	9— 4			+0.0050	0.0012	+0.0024	-0.0007		
-1	11 4	+0.00006	-0.00002	+0.00012	-0.00018			0.00000	+0.00002
0	10 4	0.000053	+0.000109	0. 000083	+0.000172	0, 000024	+0.000036	+0.000012	+0.000008
1	9 4			+0.00011	—о. 00003	+0.00006	0.00000	-0.00001	o. 0000I
-1	11 5	-0.003	-o. oo5						
0	10 5	+0.003	+o. oo6						
_r	12 5	0,0001	0,0000						
-1	13- 5	-0,0002	0.0000						
٥	12— 5	+0.0001	0.0000	0.0001	0.0000				,

$Arg = \kappa \gamma' + i'g' + ig$	$rr'rac{d^{2}}{dra}$	$\frac{\Gamma'}{lr'} u u'$	$\frac{1}{2}r^2\frac{d^2}{d}$	$rac{\mathrm{T}'}{r^2} u^2$
	sin.	cos.	sin.	сов.
χ i' i 0 0 0	0. 00 14	-0. 000028 +0. 000073 +0. 00001 -0. 0019	"	+0.000031 -0.000050 +0.00038
-1 3- I 0 2- I 5 3- I 1 2- I	-0.0002 +0.0007 +0.0013 -0.0016	-0. 0006 +0. 0007 +0. 0004 -0. 0008	+0.0002	+0.0003
—I 5— 2	-0.00012 -0.0001	+0.00106 +0.0008	0.00005	0.00016
-1 6-2 0 5-2 1 4-2 1 5-2 -1 7-3 0 7-3 -1 10-4 0 10-4	-0.00001 -0.0001883 +0.00050 +0.00052 0.0000 +0.0002 -0.00007 -0.000014	+0.00015 -0.0005367 +0.00070 +0.00039 -0.0001 -0.0004 +0.00002 +0.000003	+0.00002 -0.0000502 +0.00005 +0.00003	+0.00001 0.000056 +0.00006 +0.00003

The fourteen parts of the portion of $\delta^2\Gamma$ factored by n't follow; for convenience the coefficients are multiplied by 10000:

Arg=	$\mathbf{A}'n'$	$\delta^2 z'$	B/6	ν'	फ' ₁₁	$v\delta^2 z$	G/6	δv
Arg= $ \mu \gamma' + i'g' + ig $	n't sin.	n't cos.	n't sin.	n't cos.	n't sin.	n't cos.	n't sin.	n't cos.
и i' i	11	" + 3·3579	"	+ 0.7738	"	" + 0.8543	"	,, +0.3302
—I I O	+ 0.7826	4.6520	— o. 0752	— r. o5o3	+ 0. 1966	— 1. 0 570	+0.0030	0.4250
I 2 O	+ 0.49	— o. 35	+ o. 75	+ 1.41	+ 1.91	+ 1.40	-0. I2	0. 10
0 I 0	+ 3.85	+ 6.32	+ 3.99	+ 4.57	+ 1.37	+ 2.24	+o. 26	+0.42
1 0 0	— 11.0432	— 13.4758	— 4 . 8603	6. 3974	— 3. 3079	— 4. 2 943	-0. 2432	0. 4404
-I 3 o	I.9	— I. 8			— r. r	- 0.8		
0 2 0	+ 43.5	+ 18.0	+ 6.0	+ 3.5	+12.7	+ 4.8	+1.6	+0.8
I I O	— 71.0	— 28.5	—Io. 4	- 4.8	-14.8	— 5 .9	—I. 9	0.9
—I 4 0	— 4⋅3	+ 0.7			— 3.6	+ 0.6		
0 3 0	+ 78.4	- 15.9	— 3. 2	+ 2. I	+32.6	— 5.6		
I 2 0	143.4	+ 23.2	+ 5.2	— I. I	-39.9	+ 6.2		
-1 5 0					+ 8	+ 20		
0 4 0	— 7	— 24			— 7	19		
1 3 0	+ 6.6	+ 14.8			+ 3.5	+ 5.8		
0 4 1					+ 1	_ 2		
I 2_ I	+ 4	— 5			+ 2	- 2		
o— 3— 1	— 3	+ 1			i			
-I- I- I	+ 10.0	+121. I	— O. 2	— 3.5	+ 2.8	+ 38.5		
0— 2— I	— 7	8o	٥	+ 3	- 3	— 33		
I— 3— I	+ 1	+ 10			0	+ 6		
—t o— 1	+ 40.7	+ 64.0	+ 5.2	+ 7.7	+ 9.7	+ 14.7	+1.o	+1.3
0- 1 1	28.9	— 45.6	— 3.8	· — 5· 3	— 8. 9	— 13.4	о. 8	I. 2
1-2-1	+ 4.3	+ 4.6			+ 1.4	+ 1.4		
-1 I- I	+ 26.0	+ 14.5	+ 8.3	+ 4. 1	+ 5.9	+ 3.0	+1.2	+0.4
0 0— 1	— 23. 2	11.8	8.4	— 3·4	— 5. 3	- 3.0	0. 7	-0.2
1-1-1	+ 2.1	+ 0.4						
—I 2— I	+ 6.35	+ 0.63	+ 1.88	- 0.54	+ 1.60	- 0.05	+0.41	0. 10
0 1—1	— 7.8	- 0.3	— 2. 4	+ 0.4	— r. 6	+ 0.1	о. б	+0.3
1 0— I	+ 3.4	- 0.6	+ 0.9	- 0, 2	+ 0.2	0.0	1 = +6	
-I 3- I	+ 3.42	- 2.57	- 3.79	+ 3.91	— I. 59	+ 2.23	+1.26	—I. 3I
0 2— 1	— 12. 23	+ 5.25	+ 2.60	- 1.13	0.01	— o. 63	—1.87	+1.95
I I I	I '	— 8. 29	+ 2.10	- 3.09	+ 1.45	— I. 29	+1.18	I. 26
-1 4- I		+ 1.85	- 0, 02	- 2. 19	+ 0.51	+ 1.93	+0.07	0.40
1	- 8.84	— 32. 42	— 4· 34	+22.45	- 3.41	+ 1.29	0, 61	+2.03
I 2— I	1	— 17.72	+ 3.88	18.56	+ 3.02	— 6. 84	+0.58	—2. 3I
—I 5— I	1	_200.0	+ 0.6 - 2.8	+ 1.5	+35.2	+105.3 84.1	+1.5 1.6	+I. I —I. 2
	69. 3	—200. 9 —22. TO		— 9. I — 7. 22	—27. 6 ⊥ x 50		+o. 58	i
	+ 10.71	+ 32. 19 + 1.7	+ 2.13	+ 7.33	+ 1.59 + 0.3	+ 7. 15 - 0. 7	⊤o. 30	+0.57
1	- 0.5	+ 1.7			T 0.3	_ 5.7		
-	2.0	— 2.3 — 5.5			_ , , ,	_ 2.5	1	
I 4— I	3.4	— 5·5			— 1.4	1		
1 1_ 2		+ 6			+ 3	+ 2		
0-2-2	— 3	— 5					l	
	- 97	1		1	•	1	 	1

Arg=	A'n	$'\delta^2z'$	Β'	$\delta u'$	F'1	$\imath\delta^2z$	$G'\delta u$	
$ \mu y' + i'g' + ig $	n't sin.	n't cos.	n't sin.	n't cos.	$n't \sin$.	n't cos.	n't sin.	n't cos.
\varkappa i' i	"	"	,,	"	11	"	"	"
1 o 2	— 88	+ 27			—3o	+ 9]]
0- I- 2	+ 64	— 20			+27	- 8		
1-2-2	IO	+ 3			- 6	+ 2	1 .	!
I I 2	— 46	+ 45	 4	+ 5	—11	+12	+ 1	+1
0 0-2	+ 35	- 36	+ 4	— 4	+11	—11		
I I 2 -I 2 2	- 4	+ 5			_ 。			
0 I— 2	一 7·7 十 6.2	+ 23.8	- 1.5	+ 7.5	— 1.8	+ 5.9	— o. I	+0.7
1 0 2	0.2	- 19.3 + 1	+ 0.7	— 4· 3	+ 1.3	— 4.8]	
-I 3-2	+ 1.4	+ 6.6	+ 1.1	+ 2.5	+ 0.7	+ 1.8		
0 2-2	- 2.0	— 5.6	— o. 3	— 0. 9	— 0. 7 — 0. 2	— o. 8		
_I 4— 2	- 3. 5 ²	I.84	- 4. 24	— 2. 09	- 0. 2 - 0. 03	— 0. 8 + 0. 27	— I. II	—o. бі
0 3— 2	+ 5.7	+ 1,2	+ 3.7	+ 1.6	+ 2.7	+ 0.27 + 0.8	+ 0.3	+0.2
I 2- 2	+ 4.4	+ 3.5	+ 0.8	+ 0.8	- 2.5	- 0.7	+ 0.2	+0.2
I 5- 2	+ 8.775	— o. 555	-12.425	o. 504	—10. <u>576</u>	— o. 372	+ 9.712	+0. 376
0 4-2	- 4·47	- I. 28	+ 0.75	+ 0.87	+ 8.82	+ 0.09	11.49	- 9. 32
I 3- 2	+ 28.34	+ 1.66	+11.39	- 0.41	— 1.07	+ 0.34	+ 5.53	+0.08
—ı 6— 2	+ 60.421	— 36. 624	+ 1.743	o. 8o6	+ 0. 146	+ 0. 229	- 0.032	0, 050
0 5— 2	о. 7910	+ 0.7173	+ 1.3382	— 0. 7277	— o. 3565	— 1.8182	— o. 5769	+0.6036
I 4— 2	+ 58.658	- 35.067	- 3.395	+ 1.954	+ 0.236	+ 0.025	— o. 322	-0.052
—I 7— 2	+ 8.2	19.0	+ 0.9	— I.4			0.0	+0.3
0 6- 2	— 2. 13	+ 5.56	- 0. 20	+ 0.33	+ 0.05	+ o. 38	+ o. 10	0. 58
I 5— 2	+ 0.567	o. 765	— o. 7o3	+ 0.990	+ 0.045	 0. 649	— o. o66	+0.487
1 8 2	0.7	- 3.4						
0 7-2	+ 0.4	+ 1.8			i			
—ı o— 3	5	+ 8			2	+ 4		
o 1 3	+ 4	4			+ 2	- 3		
-r r 3	32	<u> </u>			-11	-20		
0 0-3	+ 26	+ 44			+11	+19		
ı— ı— 3	— 5	_ 8			- 3	- 4		
_1 2— 3	44	— 28	— 4	— 3	rr	- 7		
o I— 3	+ 35	+ 22	+ 4	+ 2	+10	+ 6]
I 0-3	- 5	- 3						
-r 3-3	— 2I	- 3	- 3	0	- 4	О		l
0 2-3	+ 21	+ 1	+ 3	0	+ 4	+ 1		
-I 4-3	6.4	+ 2.5	- o. 8	— o. 5				l
0 3-3	+ 7	- 4						- 1
—I 5— 3	— o.6	+ 4.5	+ 1.2	- 2.4	- 0. 2	+ 1.0	+ 0.4	—I. I
0 4— 3 1 3— 3	+ 1.0	- 3.0	— O. 2	+ 0.4	- o. 5	+ 1.1	0.8	+2.2
-i 6-3	+ 3.8	+ 1.9	- 4.3	21.2	+ 0.8	- 2.5	+ 0.6	—2. 0
0 5-3	+ 5.6	+ 27.9	+ 5.3	21. 2 +25. 0	+ 1.7 + 0.2	+ 2.6 + 0.8	— o. 3	—I. I
1 4— 3	_ I.7	— 0. 3	— o. 6	+25.0 - 2.6	+ 0.2	+ 0.8	+ 0.1	+0.5
_I 7— 3	- 20.42	— 23. 77	+ 1.91	+ 2.02	- 4· 93	0.9 5.15	+ 0, 1 + 0, 21	+0.5
o 6— 3	+142.2	+157.6	- 3.7	- 3. I	+61.0	+65.2	— 0.21 — 0.9	+0.25
I 5— 3	0.0	- 0.4	+ 0.8	+ 0.8	— 76. 4	—81.6	- 0.9 + 0.9	o. 7 +o. 7
							1 5.9	⊤0. /

Arg=	$\mathbf{A}'n'$	$\delta^2 z'$	Β′δ	īv'	$\mathbf{F}'n$	$\delta^2 z$	G ′δν	
$\mu y' + i'g' + ig$	$n't \sin$.	n't cos.	$n't\sin$.	n't cos.	$n't \sin$.	n't cos.	$n't \sin$.	n't cos.
и i' i —1 8— 3	// +27.74		" + 2.58	+1.13	" + 3·49	o. 51	o. o6	,, +0.03
0 7-3	- I.OO	+ 15.71	— 2.90	— 1 . 36	— o. 37	+ 3.00	0.00	-0.07
1 6-3	— 1.46	_ 2.52	+ o. 35	+o. 16	- o. 69	- I. O5		
—1 9— 3	+ 7.55	— 4.12	+ 0.64	o. o5	+ 0.69	— o. 36		
o 8— 3	- 3.53	+ 3.65	_ o. 76	-0. 02	0.47	+ 0.45	+ 0.02	-0.02
1 7-3	— o. 18	- 0.44	+ 0.13	-0.02	- 0.04	0,09	·	
1 10 3	+ 0.9	- I. 2	,5			,		
5 9 3	- 0. I	+ 0.6			+ 0.1	— O. 2		i
1 8-3	- 0.12	- 0.0I			,			
							ĺ	
-I I-4	<u> </u>	_ 2						
0 0-4	+ 5	+ 3					ļ	
—I 2— 4	+31	<u> </u>			+12	—11		
0 I 4	-25	+ 24			-10	+10		
I 0— 4	+ 6	— 5						
—I 3— 4	+ 14	- 37	+ 1	— 3	+ 3	— 9 ·		
0 2—4	-11	+ 30			- 4	+ 9		
I I-4	+ 2	— 5						
—I 4— 4	— 3	<u> </u>	— r	—2	0	<u> </u>		
0 3-4	+ 2	+ 16			0	+ 3		
<u>-1</u> 5-4	— 2	— 3					į	
0 4-4	+ 2	+ 3		_				
—I 6— 4	— 2	- 2	+ 1	0				
0 5-4	+ 4	+ 3	1 70 7	+2		— 6. г	4.6.	—2. 0
-I 7-4	-27.2	- 4.4	+13.1	—5. 7	2.8	+18.3	+ 5.1	-2.0 +4.2
5 6-4	+26.8	+ 13.7	9. I	+3.9	+ 5.9	—20	—10. 7 + 9	 4
I 5— 4 —I 8— 4		1 ****			4	+32.9	+ o. 5	
1	90.9	+122.5 66.4	— 0. 2 — 0. 1	0.0	-23.9 +20.0	26.4	0.7	+0.6
o 7— 4 1 6— 4	+50.7 — 2.7	+ 3.3	- 0.1	+0.3	— 2. 2	+ 2.8	0.7	10.0
1 0— 4	· ·	+ 60.2	— o. 3	+1.7	— I. 4	+11.7	0.0	o. I
0 8-4	-7.3 +5.2	— 39.6	+ 0.1	—1. o	+ 1.2	IO. 4	5.5	0, 1
			T 0.1	-1.0	+ 0.4	+ 0.8		
I 7— 4 —I IO— 4	+ o. 8 + 5. 898	+ 2.4 + 13.631	+ o. 185	-Lo. 525	+ 0.4 + 0.859	+ 1.971	o. o26	-0.029
		+ 13.031 - 9.88	- 0. 185 - 0. 18	+0. 525 0. 43	— 0.77	— 1. 86	0.520	0.029
0 9— 4 1 8— 4	- 4.10 + 0.6	+ 0.4	0, 10		+ 0.2	+ 0.1		
1	I .	+ 0.4	+ 0. 110	+0.091	+ 0.274	+ 0.200	0.011	-0.001
	+ 2.445	- 1. 7/2 - 1. 3203		-0.091 -0.0652	- 0. 274 - 0. 2580		+ 0.0075	+0.0028
0 10-4	- 1.7701 + 0.308	+ 0.077	— 0.0777 — 0.008	0.0052	+ 0.035	- 0.005	5.50/5	1 0. 0020
1 9-4			0.000	0.017				
— I 3— 5	+22	+ 15	ł		+ 9	+ 5		
5 2— 5	20	— 13			<u>8</u>	<u> </u>	[
— 1 4— 5	E	+ 3	l		+ 8	1 + 1		
D 3 5	20	— 3	1		— 7	_ 2	1	
—I 5— 5		— 3	1		!			
0 4-5	1 .	+ 3	1					
<u>—1</u> 6— 5		— 3			1.			
o 6— 5	1		1		+ 1	+ 2		
	!	1	<u> </u>	!			-	

Arg=	$\mathbf{A}'n'\delta^2z'$		Β'δν'		$\mathbf{F}'n\delta^2z$		G'δν	
	n't sin.	n't cos.	n't sin.	$n't \cos$.	$n't \sin$.	n't cos.	n't sin.	n't cos.
н i' i	8		"	,,	, ,,	"	"	"
—I 8— 5	ı	— 7	+6	+9	_ 2	<u> </u>	1	
0 7— 5 —1 9— 5	l '	+ 6	—5 10.7	<u>6</u>	+ 1	+ 3		
-1 9-5 0 8-5	—119. 2 + 78	52. 9	+0.7 —1	+0. 2	36.4	—I5. 9	ļ	
1 7— 5	+ 78 9	+35 - 4			+31 — 6	+13 - 2		
-r ro 5	1 -	+ 4.9	—r. 5	0.0	— 0 —14. 7	+ 1.4		
0 9-5		— 3·3	+0. 2	0.0	+13.4	— I. 2	1	
1 8-5		- 3· 3 + 1· 5	70.2	0.0	— 2. 0	+ 0.6		
-1 11-5		+ 9.8	-o. 7	+0. 5	- 2. 8 - 2. 8	+ 2.0		
0 10-5	1	— 7 ⋅4	0.7	70.3	+ 2.6	— I.8		
I 9— 5		+ 1.2	ļ					
—I I2— 5		+ 3.38	0, 05	+0.14	O. 27	+ 0.57		
0 11 5	-	— 2. 6] ,,,,	1 27 - 7	+ 0.2	— o. 6		
1 10-5	0.0	+ 0.3						ï
_1 13 5	1	+ 0.75	0, 00	+0.02	+ 0.01	+ 0.10		
0 12— 5	— o. o8	— o. 57	0, 00	0.02	0.00	— o. og		
_I 4— 6	_ 6	+16						
0 3-6	+ 4	—15						
_I 5_6	+ 1	+17						i
0 4—6	_ I	— 14						
—ı 6— 6	+ 4	+ 7						
0 5-6	4	— 6						
_r g 6	0	— 5			- 3	+ 2		
0 8-6	_ I	+ 6			+ 3	Б		İ
1 1o 6	+ 20	98			+ 6	—31		
0 9—6	— 13	+71			<u> </u>	+28		
r 8 6	+ 2	-11			+ 2	_ 6		
_1 11— 6	— 16	<u>_52</u>			4	—14		
о 10— б	+ 11	+41			+ 4	+13		
ı 9 6	— 2	— 4			— 1	_ 2		
—1 12— 6	- 12.4	-12.3			- 2.9	z. 8		
o 11 6		+ 9.7			+ 2.7	+ 2.7		
1 10— 6		— r						
— г 13— 6		— I. I			- o. 8	— O. 2		}
0 12— 6	+ 3.3	+ 0.9			+ o.8	+ 0.2		
1 6 7	— 11	+ 3						Į
<u>—</u> 1 10— 7	+ 3	- 4			— 2	— 3		Į
0 9—7	- 4	+ 3				-		•
ı ıı 7	+ 70	2			+23	o		
o 10 7	— 5 5	+ 2			—21	+ 1		
ı 97		0			+ 5	0		
—I I2— 7		-21			+11	 7		
o 11 7	— 31	+17			to	+ 6		
I 10 7	+ 5	 3						
—I I3— 7	+ 9	<u>13</u>			+ 2	4		
O 12 7	- 7	+11			- 2	+ 3		

Arg= $\kappa \gamma' + i'g' + ig$	$\mathbf{A}'n'\delta^2z'$		Β'δν'		$\mathbf{F}'n\delta^2z$		G'δν	
	$n't \sin$.	n't cos.	n't sin.	n't cos.	$n't \sin$.	n't cos.	n't sin.	n't cos.
н і' і	. "	"	"	"	11	,,	"	"
—ı 11— 8	+ 4	0						!
o 10—8	5	+ 3	i					
—I I2— 8	+12	+46	l		+4	+15		
o 11—8	9	—34			— 4	-14		
1 10—8	+ 2	+ 7	İ		ļ			
_т т3— 8	+22	+25			+7	+ 8		
o 12— 8	18	-21			<u>_6</u>	- 7		•
1 11-8	+ 4	+ 3						
—ı 13— 9	-24	+13						
0 12- 9	+20	—11						

Arg=		$rac{1}{2}rac{d{f A}'}{dg'}(n'\delta z')^2$		$rac{d\mathbf{A}'}{dg}(n\delta z$	$)(n'\delta z')$	$rac{1}{2}rac{d\mathrm{F}'}{dg}(n\delta z)^{\mathrm{a}}$		$rac{d\mathrm{B}'}{dg'}(n'\delta z') u'$	
κy'+'g'	+1g	$n't \sin$.	n't cos.	n't sin.	n't cos.	$n't \sin$.	n't cos.	$n't \sin$.	n't cos.
ж i' о о	i	11	.,, —0. 8003	"	,, —0. 6466	"	" —0. 1410	11	.,, —1. 2080
_ı ı	О	—о. 070 6	+2.0525	+0.0008	+1.1755	+0.0434	 -0. 1754	0. 6817	+1.8936
—I 2	О	+0.15	+o, 68	0.04	+o. 17	+0.04	+0, 06	0. 47	—о. 18
0 1	ю	—I. 47	—2. 73	o. 73	-1.22	+0.04	0. 35	о. 60	1.71
1 0	0	+2. 9783	+5.2970	+1.1542	+2.0917	0. 0403	+0.3853	+1.4470	+3.3846
0 2	0	2.8	—r. 8	2. z	-1.1	u. 4	0. 5	—ı. 5	1.1—
1 1	О	+7.6	+4.6	+3.9	+1.9	+0.4	+0,6	+3.5	+2.5
0 3	0	2. 5	+o. I					+1.1	0.0
I 2	0	+5 ⋅3	+0.3					—2. I	o. 1
0 4	0	—2	+1	,					
1 3	0	+4.6	⊸2. 7						
—I— 2-	— т	+2	8					— 1	+4
o— 3-	- ı	—2	+4						
-1- 1-	— r	I. 2	6. 2					+0.5	+2.5
0- 2-	— т	0	+3					0	—r
—I 0-	I	—7 ⋅ 5	—8. 9	-2.9	<i>−</i> 3·7	— о. 7	0. з	3. 3	—3. 2
0 1-	— т	+3.4	+3.7	+2.0	+2.5			+2. z	+2. I
-1 1-	- I	7 ⋅4	-2. 7	2.6	—о. 7	о. з	0.0	-4. 2	0.8
0 0-	— т	+3.6	+1.1	+2.3	+0.7			+3.0	+0.7
—ī 2-	_ ı	<u>—3.</u> 80	O. 2I	—r. 67	+0.21	o. o 7	+0.05	-2. 20	+0.08
O 1-	– 1	+2. I	о. б	+0.9	о. з	+o. I	0.0	+2. I	0. 3
1 0-	- I	—о. 8	 0. 2					—I. 2	+0.3
—I 3-	- ı	I. 33	+0. 29	—о. 31	10.0+	+0.03	+o. o8	+0.17	o. 6o
0 2-	_ ı	+o. 55	+0. 39	+1.00	0.69	+o. 18	-0.13	+1.82	—1.33
1 1-	— т	—I. 35	+o. 36	— 1. 16	+o. 82	0. 23	+0.11	—2. 92	+2.31
—1 4-	- r	o. 31	о. оз	0,00	0. 09			— 0. 07	—о. 33
0 3-	— x]	 0. 76	+3. 1 3	—о. 59	+0. 32	+0. 22	-0. 27	+1.24	2. 63
I 2-	— І	-0. 11	о. 39	—о. 13	+1.60	—o. 26	+0.40	—I. 95	+4.56

$\begin{array}{c} \text{Arg} = \\ \mathcal{N} \mathcal{Y}' + i'g' + ig \end{array}$	$\frac{1}{2}\frac{dA'}{dg'}$	$(n'\delta z')^2$	$\frac{d\mathbf{A}'}{dg}(n\delta z)$	$(n'\delta z')$	$\frac{1}{2}\frac{d\mathrm{F}'}{dg}(n\delta z)^{g}$		$rac{d\mathrm{B'}}{dg'}$ (n	$(\delta z') \nu'$
$\kappa \gamma' + i'g' + ig$	$n't \sin$.	n't cos.	n't sin.	n't cos.	n't sin.	n't cos.	n't sin.	n't cos.
$\begin{array}{cccc} & \mu & i' & i \\ & -1 & 5-1 \end{array}$	"	"	"	"	+o. 2	+o. I	"	"
0 4— 1	+0.7	+0.9	— 0. 3	+o. 1	-0. 2	—о. 1	+0.2	+0.7
1 3-1	o. 8 ₃	+0.50	+0.05	+0.33	+0.06	+0.03	0. 46	-1.33
0 5— I	+3.2	+3.2						
I 4 I	2.5	-r.8	—o. б	—о. з				
-I- I- 2	+8	+1	i				— 5	_r
0- 2- 2	— 5	0				1		1
—I 0— 2	+4	-2	[—2	+1
0— I— 2	-3	+1					1	
—I I— 2	+6	— 8	+3	—4			+2	- 4
0 0— 2	-2	+3	— 1	+1			— 2	+2
—I 2— 2	+0.7	6.8	+ 0.6	-2.7			+0.2	-4.9
0 I 2	о. з	+3.3	0.0	+2.0			-O. 2	+3.3
—I 3— 2	o. 1	—4. ī	о. з	—2. O			—1. 6	—3. 2
0 2 2	⊹ o. 8	+1.9	ł				+1.3	+2.2
-I 4— 2	+o. 22	—1.44	0.02	0. 54	+0.11	+0.01	+0.03	—0. 32
O 3— 2	+0.7	+1.0	-0.4	⊸o. 6	1		о. з	+o. 1
I 2 2	—о. 6	o. 7					0.9	0.8
—I 5— 2	+1.032	0. 269	+0. 166	-0.400	+o. 588	+0.315	0. 918	o. 446
0 4 2	+o. 67	+0.06	1.20	+0. 24	0. 44	0. 28	0. 37	+0.13
I 3 2	-1.41	-o. 25	+0.20	0. 01	ŀ		—1.4I	0. 24
—I 6— 2	+o. 8o9	0. 695	—о. 139	0. 049	-0.054	-0.006	o. 576	+0. 152
5— 2	0, 0504	+0. 1314	+0. 1409	-0. 1522	十0. 0777	0. 0295	+0. 1317	+0. 0589
I 4 2	o. 557	+0.109	0.012	0. 026	0. 064	+0.016	+0. 359	—o. 203
—I 7— 2	+0.8	I. 2						
0 6— 2	—о. 36	+0.27	+0.16	—о. 37	+0.08	o. 54	o. o8	+o. 25
I 5— 2	o. o82	0. 022	+0.263	0. 403	0. 054	+0.614	+1.023	—1. 77 5
—I O 3	o	+7						
-I I-3	+3	+4						
0 0-3	2	— 3						
—I 2— 3	+5	+2	+2	+1			+3	+1
5 I— 3	-4	2	.				2	—I
I 3— 3	+5	- - I	+2	0		i	+5	—I
0 2-3	-3	+1					-2	0
—I 4— 3	+2.9	O. I					+1.8	-2.6
0 3-3	—I	+1						
-I 5-3	+1.4	-0.5					+1.7	-2.4
5 4-3	-0.4	+0.7		16.5			0. 7	+1.3
-I 6-3	+1.1	+0.1	+0.3	+0.1			0, 0	-5⋅4
5 5- 3	0.0 +1.81	+3. 2 +0. 84	+0.1	+1.5	0 -0	1	0.0	+3. 1
-I 7-3 6-3	_0. I	+0.64 +0.6	+0.71 -0.2	+0.33	-0.08	+0.03	-0.72	-1.51
-I 8-3	_0. r _0. 09	_0. 32	+o. 68	0.0 ±0.22	+0. I	-0.2	+0.4	+0.7
D 7— 3	+2.80	+1.41	+0.78	+0. 22 +0. 37	+0.47	0. 04	+4.35	+1.67
i 6-3	+0.43	+0. 25	+0.11	+0.05	о. 38	+0.02	-2.78	—I. 04
	1 43	1 5.23	1 5	1 01 03			+o. 38	+0.07

Arg=	$\frac{1}{2}\frac{dA'}{dg'}$	$n'\delta z')^2$	$rac{d{ extbf{A}}'}{dg}(n\delta z)$	$)(n'\delta z')$	$rac{1}{2}rac{d{ m F}'}{dg}$	$(n\delta z)^2$	$rac{d\mathbf{B}'}{dg'}(n')$	'δz')ν'
**/ T* 9 T*9	$n't \sin$.	n't cos.	n't sin.	n't cos.	n't sin.	n't cos.	$n't \sin$.	n't cos.
Arg= ny'+i'g'+ig n i' i -1 9-3 0 8-3 1 7-3 -1 10-3 0 9-3 1 8-3 -1 3-4 0 2-4 -1 4-4 0 3-4 -1 5-4 -1 5-4 -1 6-4 -1 7-4 0 6-4 -1 7-4 0 6-4 -1 9-4 0 8-4 -1 10-4 0 9-4 1 8-4 -1 11-4 0 10-4 1 9-4 -1 9-5		n't cos. 0. 78 +-0. 23 +-0. 100. 40. 8 +-0. 3 +-53 +-43 +-21 +-2. 60. 5 +-4. 11. 6 +-9. 13. 7 +-4. 0282. 09 +-0. 5590. 5291 +-0. 2977 +-3					n't sin. 11.48 -1.29 +0.76 +0.2 -0.1 -0.05 0 +1 +3 +5.9 -2.2 +1.6 -0.8 -0.7 +0.3 +0.894 -0.42 +0.1 +0.512 -0.3023 -0.010 +2 -2	n't cos. '' -0. 20 +0. 10 -0. 13 -0. 3 +0. 1 -0. 06 +3 +2 -1. 5 +0. 5 -1. 7 +0. 9 +4. 6 -1. 7 +2. 097 -1. 04 +0. 2 +0. 353 -0. 2061 -0. 010 +5 -2
0 7— 5	+ I - 6. 2 + 2 - 10. 4 + 4. 9 - 4. 9 + 3. 0 - 1. 26 + 1. 2 - 0. 36						+2 -2 +2.3 -2 -4.3 +2.8 -2.1 +1.3 -0.44 +0.2 0.00 -0.01	

$ ext{Arg}= egin{array}{c} ext{} $	$rac{d\mathbf{B}'}{dg}(n)$	$\delta z) u'$	$rac{d\mathrm{G}'}{dg'}(n')$	$(\delta z') u$	$rac{d\mathbf{G}'}{dg}(nc)$	$\delta z) \nu$	$\frac{1}{2}r'^2\frac{d^2}{d}$	$\frac{T'}{r'^2} u'^2$
$\mathcal{H}\mathcal{Y}'+i'g'+ig$	n't sin.	n't cos.	n't sin.	n't cos.	n't sin.	n't cos.	n't sin.	n't cos.
$egin{array}{cccccccccccccccccccccccccccccccccccc$	"	,, 0. 4964	u		"		11	
—ı ı o	—0. 0364	+0.6393	+0.0729	+0.5673	+0.0447	+0. 1467	+o. o866	+o. 5888
-1 2 O	o. 21	—0.06	—o. o7	+o. o1	0.00	+0.03	u. 44	—о. 75
0 1 0	—0. 12	0. 67	0. 06	0. 72	0,00	—о. 16	2.6	4.9
1 0 0	+0.3637	+1.1388	—o. o351	+1.0488	+0. 0397	+0.3078	+o. 88o8	+1.7647
0 2 0	0. 7	-0.4	-0.4	o. 7	0.2	—о. з		
1 1 0	- - 1.0	+0.7	+0.7	+1.1	+0.2	+0.3	o. 3	+0, 3
-I 0- I	I, I	—I.I	—I. 2	0.4				
o- I- I	+0.8	+0.8		1				
0 0-1	—I. 3	—0. 2	—I. 2	+0.2	0. z	+0.1	-2.0	0.5
-1 z-1	+0.4 0.71	+0. I	+0. 5 0. 54	0. I		-Lo 10	+0.6 0.67	+0. 2 +0. 21
o I— I	+0.5	_0. I	+0.8	+0. 31 0. 4	—o. 15	+0, 12	· 1	0. I
1 0-1	70.3		—o. 3	0. 4 +0. 1			+o. 3	0. 1
r 3 r	+0.07	—o. 3 7	+0.02	0.00	+0.09	-0.02	+0.94	o. 85
0 2-1	+0.47	0.04	+0.24	+0.10	+0.03	-0, OI	+0.21	-0. 10
1 1-1	-o. 73	+0.44	—o. 63	-0. 05	-0.14	+o. o1	—I. 23	+1.00
_I 4— I	+0.03	_o. oɪ	0. 19	0, 27	+0.04	o. o6	+0.26	-o. 37
0 3—1	+0.41	-0.92	+0.75	_0. 23	+0.19	o. 15	-0.03	+0. 26
I 2— I	-o. 39	+0.86	_o. 89	+0.82	-0. 26	+0.19	0. 26	-0.03
r 5 r	5,	·				,	0, 0	+0.3
0 4 1			+o. 1	+o. 1	+o, 1	+o. 1	+o, 1	+0.3
ı 3— ı	—o. o6	0. 32	-0. 11	+0.09	0.03	—U. I2	-0. 27	-1.11
_I I- 2	+1	_ı						
—I 2— 2	0.0	— 0. 7	0. 3	— 0. 7				
0 I— 2	0.0	+0.6						
—I 3— 2							о. з	0. з
-I 4-2	+0.45	+0.07	o. o7	0.04			+1.36	+1.06
0 3— 2 I 2— 2	—o. 1	+0.3	+0.3	+0.5 0.6			-0.3	—0. 2
_I 5— 2	+o. 282	o. o36	—0. 3 +0. 110	0. 096	0. 471	<u> </u>	—0. 6 +0. 730	-0.5 +0.312
D 4— 2	-0. 26	+0.09	+1.27	+1.08	+0.62	+0.44	-0. 34	-0, 10
I 3— 2			—I. 34	-1. or	-0. 29	-o. 2I	+0.03	о. 16
_t 6- 2	-0. 242	+0. 125	+o. 173	—0. 326	+0.057	0.010	—о. 47 3	+0, 230
o 5— 2	+0. 1452	—o. 1137	-0. 0244	+0. 2988	0. 0362	+0. 0488	—0. 1419	+0.0641
I 4— 2	+0.067	0.043	0. 200	+0.096	+0.015	0.010	+o. 668	o. 3 5 4
o 6-2			+-0. 3 0. 24	—1.7 +1.78	— 0. 10	+0.72		
I 5— 2	+0. 024	0. 134	+0.064	0. 134	+0. 106	—o. 623	+o. 198	о. 139
—I 5— 3							o. 5	+1. o
—ı 6— 3	0.0	—I.O					o. I	+0.4
o 5— 3	0,0	+1.1					_	
-1 7-3	0, 36	—o. 31	+0.27	-0.22	+o. o8	0.00	—0. 60	-o. 64
o 6— 3 —1 8— 3	+0. I +0. 79	+0. 1 +0. 35	0. I +1. 20	+0. 1 0. 15	+0.27		+0.3	+0.3
0 7-3	—1. 07	-0. 35 -0. 43	—0.74	+0.05	+0. 31 -0. 24	0. 02 0. 02	—0. 35 +0. 14	-0. 23 +0. 09
i 6— 3	+0.13	+0.06	+0.11	+0.05		, 5. 02	+0.14 +0.15	+0.09 +0.11
, and a							, ,	,

Arg= ************************************	$rac{d\mathrm{B}'}{dg}(n\delta z) u'$		$rac{d\mathrm{G}'}{dg'}(n'\delta z') u$		$rac{d \mathbb{G}'}{d g} (n \delta z) u$		$rac{1}{2}r'^2rac{d^3\Gamma'}{dr'^2} u'^3$	
**Y'+*'g'+*g	n't sin.	n't cos.	n't sin.	n't cos.	n't sin.	n't cos.	n't sin.	n't cos.
ν i' i -1 9-3 ο 8-3 1 7-3	+0. 20 -0. 41 +0. 17	-0.02 +0.03 -0.04	+0. 36 -0. 31 +0. 13	" -0.33 +0.22 -0.03	// +0.07 0.07	,,, 0. 06 +0. 06	" 0. 09 +0. 05	" "0. 00 +0. 01
-I 7-4 0 6-4 -I 8-4 0 7-4	+1.3 +0.3	o. 3 o. 3	+1.6 -1.8	+0.4 0.4			+0.7 -0.4	-0.8 +0.4
0 7 4 0 8 4 0 8 4 -1 10 4 0 9 4 -1 11 4 0 10 4 1 9 4	-0.4 +0.1 +0.134 -0.12 +0.070 -0.0499 +0.001	+1. 2 -0. 9 +0. 360 -0. 30 +0. 052 -0. 0340 -0. 007	+0. 4 -0. 3 +0. 537 -0. 37 +0. 203 -0. 1606 +0. 015	+1.4 -0.8 +0.434 -0.30 +0.025 -0.0239 -0.007	+0. I -0. I +0. I06 -0. II +0. 038 -0. 0372 +0. 004	+0. 4 -0. 4 +0. 163 -0. 10 +0. 007 -0. 0075 -0. 002	+0. 3 0. 0 -0. 016 +0. 02 -0. 020 +0. 0122	-0. 4 -0. 5 +0. 2 -0. 135 +0. 09 -0. 021 +0. 0157

	$rr'rac{d^{2^{2}}}{dre}$	$rac{\Gamma'}{dr'} u u'$	$\frac{1}{2}r^2\frac{d^{2r}}{dr}$	$\frac{\Gamma'}{2} u^2$
**\forall \text{'} + \text{'} g \text{'} + \text{'} g \text{'}	$n't \sin$.	n't cos.	n't sin.	n't cos.
π i' i 0 0 0	" -0. 0066 -0. 16 0. 00 +0. 2023 -0. 28 +0. 25 +0. 09 -0. 44 -0. 02 +0. 06	" -0. 1840 +0. 2775 -0. 17 -0. 22 +0. 5023 +0. 09 -0. 33 0. 00 +0. 29 -0. 09 +0. 08	+0.0157 -0.19 +0.15 -0.0317 +0.02 0.00	" -0.0152 +0.0240 -0.12 +0.09 +0.0007 -0.06 +0.07
1 2— 1 1 3— 1	0. 03 0. 09	0. 10 0. 20	0.03	0.01
-I 4-2 -I 5-2 0 4-2 -I 6-2 0 5-2 I 4-2 I 5-2	+0. 57 +0. 128 -0. 10 -0. 126 -0. 0431 +0. 167 +0. 024	+0. 36 +0. 051 +0. 03 +0. 121 +0. 0853 -0. 156 -0. 032	-0.004 -0.011 -0.0061 +0.014 +0.004	-0.005 +0.008 +0.0082 -0.018 +0.019
-1 7-3 -1 8-3 0 7-3 -1 10-4 -1 11-4 0 10-4	-0. 22 -0. 09 +0. 07 -0. 025 -0. 009 +0. 0047	-0. 15 -0. 01 +0. 01 -0. 026 -0. 002 +0. 0007	+0, 0002	+0.0001

The fourteen parts of $\delta^2 T'$ which are multiplied by $n'^2 t^2$ follow; for convenience the coefficients are multiplied by 1000000:

Arg=	A'n'	'δ²z'	В′	δν'	F'1	$n\delta^2 z$	G.	δν
μγ'+i'g'+ig	$n'^2t^2\sin$.	$n'^2t^2\cos$.	n'^2t^2 sin.	n'2t2 cos.	n'^2t^2 sin.	$n'^2t^2\cos$.	n'^2t^2 sin.	n'2t2 cos.
$egin{array}{cccccccccccccccccccccccccccccccccccc$	11	o. ooo8	"	0. 009I	"	"	"	"
—ı ı o	—1. 1555	+ 0.3559	+1.9440	— o. o531	+0. 1035	—0. 1048	+0.0120	+0. 1442
—т 2 о	+3. o	— 2.3	+4.4	- 3.4	о. з	+0.3	+2. o	—ı. 8
0 1 0	+0.09	o. o6	-0. 12	+ 0. 10	+3.05	-2. 79	4. 18	+3.84
100	+3.287	— 2. 497	-4. 442	+ 3.342	—3. 856	+3.510	+3.600	—3. 307
—т з о	+o. 5	— I.4	+0.4	- 1.3				
0 2 0	o. I	+ 0.4	-o. ī	+ 0.4			0.2	+0.4
1 1 0			-0.3	+ 0.6				j
—ı o— ı								
o— I— I								ļ
-1 I-1	-o. 8	+ 1.9	—4. 0	+ 8.4			0, 2	+0.4
0 O I	+5.4	-11.4	+4.7	10.0				` '
1- 1- 1		'	—o. 5	+ 1.1				
I 2 I	—о. 36	1. 18	+0.21	+ 3.01	-o. 27	+o. 16	+0.14	0.00
0 1—1	0. 2	+ o. 1	+o. 1	2.6	+0.4	— о. 6	-o. 3	+o. 3
1 0— 1			0. 1	o. 3	o. 7	+0.7	+0.3	—o. з
—ı 3— I	-2.01	— 1.46	+7.32	+ 6.51	+1.48	+1.14	+0.98	+0.69
0 2— I	+9.76	+ 8.29	8. 56	7.58	-1.21	_o. 93	— 0. 76	-0.52
1 I— I			+o. 91	+ 0.79	+0.13	+0.10		
—I 4— I	+1.31	0.42	+2,48	+ 0.55	+0.51	+0.14	+0.39	-0.02
о 3— г	+1.01	+ 1.19	2. 30	— o. 77	-0.45	0.13	-0.31	_0. or
I 2 I	—о. 11	— 0. 14	0.00	— o. oı	+0.05	o. oi	+0.02	-0.02
—ı 5— ı	+0.4	o. 3	+0.2	0.2	'		,	
0 4— 1	—0. 2	+ 0.2	_0. 2	+ 0.1	l i			1
—I 2— 2	+8.3		—5. 8	, i				- 0
0 I— 2	4.5	+ 2.2 - 1.2	—5. 8 +3. 9	- 1.5 + 0.9	+3.9	+1.4	2.6 +5.4	-0.8 +1.8
I 0-2	4.2	2	13.3	7 0.9	—5·9	—2 —2	75.4	7-7-0
—I 3— 2	+2.3	— 2.4	—2. 6	+ 1.0			3. 3	+o. 3
0 2— 2	-1.o	+ 1.5	+1.2	- 1.2				
—I 4— 2	-4.04	+ 6.60	-3.34	+ 5.81	0. 73	+1.63	-0.42	+0.94
0 3— 2	+1.9	— 3⋅5	+2. I	- 3.8	+0.6	-1.4	+o. 3	—o. 8
—I 5— 2	—0. I45	+ 3.931	+0.084	+ 2.529	0. 016	+0.650	+0.050	+0.409
0 4-2 1 3-2	+0. 11 +0. 06	— 2.47 — 0.13	o. o5	— 1.76	0, 04 0, 03	—0.62 ⊥0.00	0.07	0. 36
r 6 2	+0.491	+ 0.13 + 0.972	+0. 329	+ 0.501	+0.03 +0.057	+0.09 +0.136	+0.060	+o. o76
0 5-2	-0.3414	o. 6896	—0. 2546	— 0. 3946	-0.057 -0.0520	-0. 136 -0. 1265	0.0550	-0.0689
I 4— 2	+0.052	+ 0.027	+0.031	- 0.010	+0.013	+0.013	+0.010	+0.004
—I 7— 2	+0.1	- 0.1					,	' '
0 6 2	0.11	o. o6						
I 5 2	+0.013	— o. oo3	+0,003	0.004	+0.004	0,000	+0.002	-0.001
—ı 3— 3	—ı	+ 8	0	— 5	o	+1		
0 2 3	ø	— 5	0	+ 3				
—ı 4— 3	+1.6	+ 3.1	—I. O	— 1.6				
o 3 3	—I	_ 2	+1	+ 1				
				<u> </u>	<u> </u>			

Arg=		$z'\delta^2z'$	Β'	$\delta u'$	F'2	$\imath\delta^{2}z$	G'	δν
$\mathcal{H}\mathcal{V}'+\mathbf{i}'g'+\mathbf{i}g$	n'^2t^2 sin.	$n^{\prime 2}t^{2}\cos$.	n'^2t^2 sin.	n'2t2 cos.	$n'^2t^2 \sin$.	$n'^2t^2\cos$.	$n'^2t^2\sin$.	n'^2t^2 cos.
ν i' i -1 5-3 0 4-3 -1 6-3 0 5-3 -1 7-3 0 6-3 -1 8-3 0 7-3	+3·9 -4·0 +2·5 -0·96 +0·8 -0·08	-1.5 +0.9 +0.7 -0.5 +0.80 -0.7 +0.26 -0.22	-4.5 +3.3 -2.2 +1.4 -0.44 +0.3 -0.02 +0.02	-1.5 +1.1 +0.6 -0.4 +0.45 -0.3 +0.12 -0.10	" -1.4 +1.2 -0.7 +0.6 -0.13 +0.1 -0.01 +0.01	// -0.3 +0.2 +0.2 -0.2 +0.13 -0.1 +0.03 -0.03	"0.80.3 +-0.30.06 0.00	" -0. 2 +0. I -0. I +0. 09 +0. 03 -0. 03
0 8-3 -1 5-4 0 4-4 -1 6-4 0 5-4 -1 7-4 0 6-4 -1 8-4 0 7-4 -1 9-4 0 8-4	-0.01 -3 +1 +1 0 -1.2 +0.9 -0.8 +0.7 -0.2 +0.2	-0.03 +2 -2 -5 +4 -2.9 +2.3 -0.6 +0.5 0.0	o 	-3 +3 -1.5 +1.3 -0.3				J
-1 10-4 -1 11-4 0 10-4	-0.065 -0.006 +0.0081	+0.024 +0.007 -0.0086	-0. 024 +0. 0026	+0.015 0.0044	0.008 0.0011	+0.004 -0.0009	0. 004 0. 0005	+0. 004 0. 0007

A	rg=		$rac{1}{2}rac{d{f A}'}{dg'}$	$(n'\delta z')^2$	$rac{d{ m A}'}{dg}(n\delta z)$	$(n'\delta z')$	$\frac{1}{2}\frac{d\mathbf{F}'}{dg}$	$(n\delta z)^2$	$rac{d\mathbf{B}'}{dg'}(n$	'δz')ν'
		⊢ <i>ıg</i>	n'^2t^2 sin.	$n'^2t^2\cos$.	$n'^2t^2\sin$.	$n'^2t^2\cos$.	$n'^2t^2\sin$.	$n'^2t^2\cos$.	$n'^2t^2\sin$.	n'^2t^2 cos.
и о —I —I	i' 0 1 2	i 0 0	+0. 3767 +0. 3	+0. 0350 -0. 0569 -0. 2	o. 1006	-0. 1436 +0. 0212	 0. 0I22	// +0.0004 +0.0006	o. 2158	+0.0031 +0.0016
o -1 -1 0	1 0 3 2	0 0 0 0	-0. 23 +4. 946 -0. 2 +0. 4	+0. 18 -4. 641 +0. 4 -1. 0	+0.0722	0. 0313	+o. o890	0. 0310	-0. 22 +0. 6146 +0. 3 -0. 1 +0. 5	+0. 16 -0. 3815 -0. 6 +0. 3 -1. 2
0- 	0- I- 0- 2-	- I - I - I	+0. 3 -0. 2 -0. 10	-0.4 +0.4 -0.83	+o. 25	+0. 29			+2.3 -1.0 +0.3	-1.9 +0.8 -1.0
0 —I	I 3 2 I	- I - I - I	+0.4 +0.61 -0.02 +0.9	+2.0 +0.21 +0.25 +1.9	0. 2 +-0. 16 0. 11	-0. I +0. II -0. I2	+0. I -0. 01	+0. 3 0. 02	-0. 01 -0. 22 +0. 33	-0. 03 -0. 12 +0. 29

$\mathop{\rm Arg=}_{\mathcal{V}'+i'g'+ig}$	$\frac{1}{2}\frac{dA'}{dg'}$	$n'\delta z')^2$	$\frac{d\mathbf{A}'}{dg}$ (n δz	$z)(n'\delta z')$	$\frac{1}{2}\frac{d\mathbf{F}'}{dg}$ ($(n\delta z)^2$	$\frac{d\mathbf{B}'}{dg'}$ (n'	$(\delta z') u'$
	$n'^2t^2 \sin$.	n'^2t^2 cos.	n'^2t^2 sin.	$n'^2t^2\cos$.	n'^2t^2 sin.	$n^{/2}t^2$ cos.	n'^2t^2 sin.	$n'^2t^2\cos$.
	"	,,	11	"	,,	,,	į,	"
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	+ 0. 02	-o. o5	+o. 35	o. o 7	+o. 10	-0.09	+2. 14	+o. 56
0 3-1	+1.09	+0.29	0. 20	0.03	-0. I4	+0. 04	—1.70	0. 41
I 2— I	0. 04	+0.04	+o. o9	+0.09	+0.06	+0.05	+0.70	+o. 13
—ı 5— ı							+0.6	0, 2
0 4— 1							о. т	0.0
1 3— 1	+0.28	+0.02					о. 30	+0.10
—I I— 2	—2	-I					+2	+2
—I 2— 2	+o. 8	+0.2					+0.9	+o. 1
—I 3— 2	3, I	+1.3						l l
0 2— 2	+1.2	-0.5	0.00	1000				- 1
-I 4-2 0 3-2	—1. 30 +0. 6	+1.49 0.8	o. o3	+0.23				i i
-I 5-2	o. 183	+1.960	+ 0. 182	+0.492	+o. 171	+0.004	0. 109	+2.402
0 4-2	+0.09	_o. 89	-0. 19	-0. 24	_o. 16	0,00	+0.03	— 0. 95
I 3— 2	0.00	+0. 18					0,00	+0.23
—I 6— 2	+o. 319	+0.780	+0. 171	+0. 147	+ 0. 066	+0.012	+0.511	+0.922
0 5— 2	—o. 2026	o. 4598	—о. 1186	o. o885	-o. o627	-—o. o158	—o. 2497	—о , 4606
I 4— 2	+0.081	+0. 147	+0.009	+0.004	+0.011	+0.003	0.039	0. 120
$\begin{array}{c cccc} -1 & 7-2 \\ 0 & 6-2 \end{array}$	0. 0 —0. 12	o. o o. o8					0. 13	_o, o6
1 5-2	+0. 145	+0.085	-0.024	-0, 004			_0.13 _0.321	—о. 168
		' -				\	J	
-I 4-3	-2.4	<u></u> −3.4	1		1			
0 3-3	+1	+2			1		1	
-i 5 3	-2.2	-1. I		1	1		1	
0 4-3	+1.3 2.7	+0.6	l,	+0.2			—3. 1	+0.6
—I 6— 3	+1.8	+0.3 -0.2	—0. 4	T0.2			+1.7	_o. 3
0 5-3	—0. 97	+0.59	—o. 11	+0.23			—I. 09	+o. 85
-I 7-3 - 6-3	+0.5	-0.5	0.0	-0.2			+0.5	—o. 5
_1 8-3	-0, 23	+0.48	_o. o ₃	-0.09	o. or	-0.08	+0.17	_o. 67
	+0.35	_0.90	+0.06	-0. 15	0.00	+0.07	-0.09	+0.35
-1 9-3	_0. 17	-0. I4	-0.05	-0.07			0.07	0. 30
0 8-3	+0.08	0. 10	+0.03	+0.04	+0.02	+0.03	+0.02	+0.18
1	· ·]		"			'
—I 5— 4	+3	— 3						
<u>-1</u> 6— 4	+1	-3						
0 5—4	0	+2						2. 6
—I 7— 4	o. 5	1.5					—I.O	1
0 6—4	ĺ		l		1		+0.5	+1.2 -0.7
-I 8— 4	0.4	-0.4					0. 9 +-0. 6	+0.5
0 7—4	+0.5	+0.5	+0.5		Í		+0.7	0.0
—I 9— 4	+1.3	0.0	I ~~``````	0.0			o. 3	0.0
o 8— 4	0.3	0.0	+0.177	—0. I22	+0.034	-o. o ₃₇	+0.355	-0. 206
<u>-1</u> 10 4	+0.697	—0. 326 +0. 14	+0. 177 -0. 13	+0.10	0.03	+0.03	0. 15	+0.09
0 9—4	0. 27	0. 160	+0.021	_0. 049	+0.002	-0.013	+0.055	-0.111
-I II 4	+0. 125 0. 0795	+0.1128	-0. 0181	+0.0389	-0.0025	+0.0104	-0.0311	+0.0642
D 10—4	+0.020	_0. 048		1			0.006	+0.002
1 9— 4	T0.020	J. 040				1		

Aı	g=	$\frac{d\mathbf{B}'}{dg}(ne)$	$\delta z) u'$	$\frac{dG'}{dg'}(n'e)$	$\delta z') u$	$rac{d{ m G}'}{dg}(nd$	$(z)\nu$	$\frac{1}{2}r'^2\frac{d^2}{d}$	$rac{\Gamma'}{r'^2} u'^2$
<i>Hy</i> '+	i'g'+ig	n'^2t^2 sin.	n'^2t^2 cos.	n'^2t^2 sin.	n'^2t^2 cos.	$n^{\prime 2}t^{2}$ sin.	n'^2t^2 cos.	n'^2t^2 sin.	$n'^2t^2\cos$.
,,,	i' i	"	//	11	"	,,	11	,,	,,
κ o	0 0		0. 2450		+0. 3354		0. 0047		+0.0016
—ı	1 0	0. 3185	+ 0. 2294	+o. 6051	-0. 3019	-0.0010	+0.0063	-1.3714	-o. oo46
—т	2 0			+0.1	о. т			}	
0	1 0	_	_	—о. 16	+0.09			+0.11	0. 07
1	0 0	+0.0138	0. 0189	+o. 1686	o. o186	-0. 027 I	+0.0056	+0.0575	0. 0617
_I	3 0	0.0	-0.4	0.0	—o. 7				- 1
0	2- 0	0.0	+0.5	+0.1	+0.7				- 1
1—1	o— 1							_o. 8	+0.6
-1	1— 1							0.0	+0.3
—I	2— I	—o. 35	-0.42	+0. 29	+0, 29			o. 37	—I. 94
°	1— 1	+0.2	+o. 3	-0.2	-0.2			+0. I	+0.7
I I	O I			±0.27	0 02			+0. I -0. 42	+0. 7 -0. 38
-r o	3— I 2— I	-0. 22 +0. II	-0. II +0. I3	+0. 21 -0. 16	0.03 0.01	0. 01	o. oı	+0.18	+0.19
ĭ	I— I	70.11	70.13	+0.02	+0.08	0.01	0.01	+0. 12	+0.09
_ı	4— I	+0.51	0. 13	+0.52	-0.14	+o. 14	—0. 08	+o. 88	+0. 25
0	3— 1	— 0. 35	+0.11	0.33	0.00	—0. 15	+0.04	— 0. 27	0.09
1	2— I		·	+0.13	+0.12		,	-0.40	-o. 11
1	3— т							o. 2I	+0.06
_ı	3— 2	— 0. 4	0.0	+0.4	+0.5			+1.9	о. 8
	3— 2 2— 2	+0.5	0.0	—0. 7	0.0			— I . 0	+0.4
-I	4 2	+0.02	_0, 25	+0.12	+0. 22			+0.42	—0. бі
0	3— 2	i '		0.0	_0. 2			—o. 2	+0.4
_ı	5— 2	+0.217	+0.512	+0. 274	+0. 554	+o. o6o	+o. 218	-0.052	+o. 899
0	4- 2	о. 17	0. 37	0. 04	0. 64	o. o5	-0. 22	+0.05	o. 43
1	3 2			0. I4	+0.24			+0.01	O. I2
-1	6— 2	+0.218	+0.154	+0. 225	+0.138	+0.080	+0.023	+0.244	+0.413
٥	5— 2	—o. 1600	o. o868	-0.1569	0. 1197	-0.0695	-0.0231	-0. II53	0. 1990
I	4 2	+0,004	-o. o32	+0.038	+0.033	+0.015	-0,002	-o. o53	—0. 116
_i	7— 2 6— 2			-0.3 +0.31	+0.03	+0. 16	+0.01		
1	5- 2	+0.005	0, 003	0.000	-0.008	—o. 133	-0.005	+0.008	o. oo4
1		' ' ' ' '							
-I	4- 3							+1.1 +0.8	+1.5 +0.2
-I	5— 3		102] ,	10.3			+0. 8 -0. 7	+0. 2 +0. I
i	6— 3 5— 3	-0.5 +0.4	+0.3 —0.2	0.5	+0.3	1		+0.5	_0. I
I	5— 3 7— 3	_0. 10	+0.28	_o. 11	+0.31	-o. oı	+0.09	-0.42	+0.37
0	6 3	0.0	-0.2	0. 0	-0.2			+0.2	0.2
—т	8— 3		—0. 2 6	0. OI	0. 11	+0.01	-o. o5	—о. оз	+0.13
٥	7— 3	-0.14	+0.35	0.00	+0.02	0. 01	+0.03	+0.02	0. 10
I	6— 3	+o. or	-0.04	1		1		\$	
-1	9— 3	— 0. 02	0. 06	0. 08	-0.07				
0	8— 3	o. o3	+0.03	+0.02	+0.03	+0.02	+0.01		
-1	8 4	о. з	—о. 1	0. 3	—о. 1		}	0. 3	-0.2
_I	9 4	+0.5	0.0	+o. 1	+o. I		†	0. 1	+o. 1
٥	8— 4	-0. 4	0.0				0.000	_0.016	10.073
I		+0.091	-0.007	+0.062	0.083	+0.021	-0.022	0.016	+0.012
0	9— 4	-0.09	+0.06	-0.05	+0.08	0,000	0, 009	+0.002	+0.001
	11-4	+0.016	0,006	-0.001 -0.0009	-0. 034 +0. 0229	+0.0002	+0.0079	+0.0008	-0.0023
۰	10— 4	—o. o118	+0.0035		+0.0229	1			3

Ar	g= $i'g'+ig$	$rr'rac{d^2 \Gamma}{drd}$	$\frac{r'}{r'} \nu \nu'$	$\frac{1}{2}r^2\frac{d^2}{d}$	$rac{\mathbf{T}'}{r^2} u^2$
ну'+	i'g'+ig	n'^2t^2 sin.	n'^2t^2 cos.	$n'^{2}t^{2}$ sin.	$n'^2t^2\cos$.
ж 0	i' i o o	"	,, +0.0692	"	+0.0007
—I	1 0	—0. 2521	+0.0253	+0.0448	0.0016
—ı	2 0	0,0	o. 5		
I	0 0	+0.0604	+0.4914	-0, 0099	+0.0170
O	2 0	0.0	—0. 2		
—I	I— I	—o. 6	+o. I		
0	o— 1	-o.6	+o. I		
I	2— I	-0. 25	—o. 19	-0.02	0.08
0	I— I	+0.2	+0.1	+0.1	+0.4
—I	0— I		-o. 10	0. I +0. 0I	0.4
-	3— I 2— I	+0.44 +0.71	_0.10 _0.17	0.00	0.00 +0.02
1	ı— ı	—0. 70	+0. 15	0.00	+0.02
_ı	4— I	+o. 53	-0. 32		
٥	3— I	O. 24	+0.15		
x	2— I	-0. I2	+0.06		
—ı	2 2	0.4	-1.0		
— r	3- 2	0, 2	0.5		
_ı	4— 2	+0.41	+o. 83		
٥	3— 2	о. з	о. 6		ı
-1	5- 2	+0.517	+0.496	— 0. 023	0. 024
٥	4 2	0. 37	-o. 37		
—ı	6 2	+0. 272	+0.073	O. O2 I	0, 003
٥	5— 2	—o. 1729	0, 0427	+o. o168	+0.0035
1	4 2	— 0. 024	0. 031		
'	5— 2	+0.004	-0.003		
—1	5— 3	I. O	+0.6		
Ø	4-3	+o. 6	-0.4		
—I	6— 3	—о. з	+o. 8		
٥	5-3	+o. 1	0. 4		
—I	7 3	0.00	+0.32		
0	6— 3	0.0	0. 1		
-1	8— 3	+0.05	+0.07		
0	7-3	0. 04	0. 05	l	
—т	10-4	0. 003	+0.019		
Б	10— 4	-0.0004	0.0037	l	

CHAPTER XX.

THIRD-ORDER PERTURBATIONS OF THE MEAN ANOMALY AND RADIUS-VECTOR OF SATURN ARISING FROM THE MUTUAL ACTION OF THIS PLANET AND JUPITER.

The summation of the fourteen parts of δ^2T' , given in the preceding chapter, produces the following expression:

Arg=			δ²T′	,		
$Arg = \mu y' + i'g' + ig$	sin.	cos.	n't sin.	n't cos.	$n'^2t^2\sin$.	$n'^2t^2\cos$.
u i' i	"	"	"	"	"	"
0 0 0		+0.003041		+ 0.9331	l	+ 0.0422
—ı ı o		—0. 005697	+ 0.3758	+ 0.3563	<u> </u>	+ 0. 2616
—I 2 O		-0.02333	+ 1.64	+ 2.03	十9- 5	<u> </u>
0 1 0	-o. 104 3	+0.0548	+ 6.54	+ 5.37	1.66	+ 1.45
100	+0. 100156	0. 059616	12. 4957	— 8. 686 ₂	+0. 124	+ 0.555
—т з о	+0.037	o. o33	— 3.0	 2.6	+1.2	— 4·4
0 2 0	0. 269	+0.363	+ 55.6	+ 21.2	— 0. 6	+ 2.9
1 1 0	+0. 284	o. 453	— 81. 1	— 28. I	+o.6	— 1.6
-1 4 o	0.001	—0. 043	 7 .9	+ 1.3		
0 3 0	+0.025	+0.597	+106.4	+ 19.3		
I 2 0	-o. o32	-1.010	-174.9	+ 28.5		
—ı 5 o			+ 8	+ 20		
0 4 0	+0.25	-o. o ₃	— 16	— 42		
1 3 o	—o. 152	+0.003	+ 14.7	+ 17.9		
0 4 1			+ 1	2		
—I— 2— I	0.04	—o. o3	+ 7	— 11		
o- 3- 1			5	+ 5		
-1- 1- 1	+0.856	—0. 19 0	+ 11.9	+152.4		
0— 2 I	—o. 59	+o. 14	— 10	—ro8		
I— 3— I	+0.06	—0. 02	+ I	+ 16		
-1 o- 1	+o. 361	— 0. 302	+ 39.9	+ 70.1	+1.5	— 1.3
0— 1— 1	—о. 298	+0. 261	— 34. o	— 56. ₄	-1.0	+ 0.8
I— 2— I	+0.056	o. o57	+ 5.7	+ 6.0		
-ı ı- ı	+o. o63	0. 123	+ 22.2	+ 17.4	5. o	+ 9.7
0 0 1	-o. o53	+o. 151	27.2	15.7	+9.3	—20. 9
I — I — I	0.000	-o. oo8	+ 2. I	+ 0.4	—o. 5	+ 1.1
—I 2— I	-0.0079	o. o88o	+ 0.15	+ 0.90	o. 91	<u> </u>
o I— I	+0.044	+0. 20 <u>5</u>	— 5.6	- I. 3	+0.7	+ 0.7
I 0 I	o. oo4	0.003	+ 2.2	— о. 6	o. 5	+ 0.4
					-	

Arg=			δ2Τ′		<u>-</u>	
ny'+i'g'+ig	sin.	COB.	n't sin.	n't cos.	n'^2t^2 sin.	$n^{\prime 2}t^{2}\cos$.
ж i' i —1 3— I	,, +0.0607	,, +0. 0422		,, + 0.41	// +8. 55	" + 6.55
D 2 I	-0.0223	-0. 0302	6.92	+ 3.70	о. 30	— o. 6o
1 1-1	+0.0261	+0.0564	+ 7.56	— 8.64	+ 0. 90	+ 1.69
—I 4— I	+o. oo6o	+0.0069	+ 1.61	— o. o6	+9.88	+ o. 18
o 3— I	+0.0320	—0. 0810	— 15.67	7.03	4 ⋅ 34	+ o. 38
I 2— I	+0.1774	+0. 1312	+ 17.66	— 37⋅53	+o. 38	+ 0.20
_1 5— 1	—o. 6o8	+0.123	+ 37.5	+108.3	+1,2	0.7
0 4 1	+1.632	o. 299	100. 6	-293. 2	—o. 5	+ 0.3
1 3-1	-0. 2247	+o. oo86	+ 13.27	+ 45. 11	0. 23	+ 0.18
-ı 6- ı	,	·	- O. 2	+ 1.0		
0 5— 1	-0. O22	+0.019	+ 1.2	+ ó. 9		
I 4- I	+o. o8o	0.063	7.9	IO. I		
о 6— г	-o. o17	+0.051				
1 5— 1	+0.032	—o. o95				
I I_ 2	+0.03	o. o5	+ 13	+ 8		
0— 2— 2	-0.02	+0.03	8	— 5		
_I 0— 2	+0.29	+o. 61	-116	+ 35		Į
0— I— 2	-0. 23	o. 48	+ 88	27		
I— 2— 2	+0.03	+0.09	16	+ 5		
I I 2	+o. 33	+o. 26	48	+ 46	0	+ I
0 0— 2	-o. 3o	0. 24	+ 45	45		
I— I— 2	+0.03	+o. oi	— 4	+ 5		1
—I 2— 2	+o. o88	+0.011	— 9.9	+ 22. I	+1.2	— o. 8
0 I— 2	—o. 123	+0.013	+ 7.7	- 21.0	+8.7	+ 2.9
I 0 2			О	+ 1	 5	— 2
—I 3— 2	-o. 233	+0. 103	+ 0.9	+ 1.3	5. o	— o. 6
0 2-2	+0.090	o. o35	0.4	— 3. z	+0.2	+ 0.2
—I 4— 2	0. 1369	+o. 1844	6. 25	— 5. II	8. 89	+16.89
o 3— 2	+0. 101	—0, 120	+ 12.3	+ 4.9	+5.0	—10. 7
I 2— 2	-o. o3o	+0.030	+ 0.5	+ 1.2		
—r 5— 2	—o. oo889	+0.06173	— 2. 871	- 2.045	+1.027	+15.032
0 4— 2	+0.0232	—0, 1062	6. 54	+ 1.05	—о. 86	- 9. 32
I 3— 2	-0.0470	+0. 1913	+ 39.97	— O. 21	0.04	+ 0.75
—ı 6— 2	+0. 14015	+0.35715	+ 61.696	— 37. 701	+3.022	+ 4.344
0 5— 2	0.0067136	o. o181338	+ 0.6473	+ 0.2683	—I. 9944	- 2.7721
I 4— 2	+0. 15947	+0. 35029	+ 55.634	— 33. 7 29	+ 0. 148	— o. o8o
—I 7— 2	+0.097	+0.055	+ 10.2	- 23.0	0. 2	+ 0.1
0 6— 2	-0.0610	—o. o341	- 2.72	+ 7.80	+0.11	— o. 16
I 5 2	+0.04632	+o. o3598	+ 1.413	<u> </u>	-0. 294	— o. 118
—I 8— 2	+0.020	-0.001	- 0.7	- 3.4		
0 7— 2	+0.019	+0.005	+ 0.4	+ 1.8		
ı 6— 2	-0.051	—o. oo6	I			
o 8— 2	+0.032	0. 019	1			
—ı o— 3	+0.05	+0.02	- 7 + 6	+ 19	[
o— I— 3	6.38	10.38	1	- 7 72	1	
—I I— 3	—о. 38	+0. 28	— 40	— 72		

Ara		- 1	$\delta^2 {f T}'$			
$\begin{array}{c} \text{Arg} = \\ \varkappa \gamma' + i'g' + ig \end{array}$	sin.	cos.	$n't \sin$.	n't cos.	$n'^2t^2\sin$.	n'^2t^2 cos.
н i ' i	11	11	11	11	"	"
o o— 3	+0.30	-0.25	+ 35	+ 60		
1 —1— 3	0.04	+o. o3	_ 8	— 12		
—ı 2— 3	-0. 14	+0.32	— 49	- 34		
0 I— 3 I 0— 3	+0, 10	-0. 25 +0. 03	+ 43 - 5	+ 27	ļ	
-r 3 3	_0,01 _0,01	+0.10	— 5 — 16	— 3 — 5	I	+ 4
0 2— 3	0, 01	0.08	+ 23	+ 3	U	- 2
—ı 4— 3	-o. 189	—o. 267	2.5	+ 0.3	— v. 7	- 0.4
0 3-3	+o. 12	+0. 15	+ 6	- 3	+ r	+ 1
—ı 5— 3	o. 252	o. 126	+ 3.4	+ 0.1	15. 2	- 3.8
0 4-3	+0. 149	+0.072	— г . б	+ 2.7	+10.3	+ 2.4
1 3— 3	' '	,	+ 1.4	- 4.5		, ,
r 6 3	0, 026	+0.011	+ 2.2	— 23.6	15.4	+ 4.2
0 5— 3	o. 164	_o. oo6	+ 11.3	+ 63. I	+ 9.3	- 2.4
1 4-3	+0.003	-0.009	— I. 7	- 3.3		
—I 7— 3	+0.1813	—o. 1425	— 22. 34	— 28. 28	4.39	+ 4.59
o 6— 3	—I. 344	+0.932	+199.1	+220.6	+ 2.4	- 3.0
1 5— 3	+o. 506	o. 356	— 74·7	— 8o. 5	' - '	
_1 8_3	-0.0057	+0. 1579	+ 41.02	— 1.48	0.06	o. I4
0 7— 3	o. o852	-o. o353	— 5.69	+ 17.78	+ 0.27	- o. 76
I 6— 3	+0.0032	+0.0032	0.49	- 2.78	+ 0.01	- 0, 04
	+0.0039 +0.0134	+0.0402	+ 12.73	- 6.03	0.39	0.64
0 8— 3	o. 0178	u. 0263	- 6. 35	+ 4.78	+ 0.15	+ 0.19
_	+0.0006	+0.0123	- 0.33 + 1.61	— 0.64	+ 0.13	7 0.19
, ,	+0.031	+0.0123	+ 1.4	— 1.9		
—I IO— 3				— I.O		
0 9-3	0, 036 0, 0006	-0. 051 +0. 0016	l .	1 .		
ı 8— 3	0,0000	+0.0010		+ 0.09		
<u>-1 1-4</u>			8	- 2		
0 0 4			+ 5	+ 3		
—I 2— 4	—о. 25	-0.20	+ 43	41		
o 1— 4	+0.21	+0.17	— 35	+ 34		
I 0— 4			+ 6	5		
—r 3— 4	0. 22	—o. o5	+ 18	— 41		
0 2-4	+o. 20	+0.05	— 15	+ 36	ľ	
I I 4			+ 2	— 5	Į.	
—ı 4— 4	o. o3	0.00	— 3	— 17	1	
0 3-4	+o. o6	0. 02	+ 1	+ 16		1
—I 5 4	+o. 22	0. 25	— т	— I	D	- I
0 4—4	—о. 13	+0.14	+ 2	+ 3	+ 1	— 2
ı 6 4	+o. o6	o. 27	+ 1	— 3	+ 2	—11
o 5— 4	o. o3	+o. 16	+ 4	+ 5	0	+ 9
—I 7— 4	+o. 108	о. 177	— 12. 8	— 16.5	- 3.5	- 8.5
o 6— 4	—о. 193	+0. 160	+ 11.4	+ 40.0	+ 2.3	+ 4.8
I 5 4	+o. 10	—о. 01	+ 5	24		
_r 8— 4	0. 722	— о. 738	—117. 1	+157.2	— 3·4	2.4
0 7 4	+0.423	+0. 443	+ 70.4	92. 2	+ 1.8	+ 1.5
ı 6 4	—o. 015	—0. 014	4.9	+ 6. r		
				·	<u> </u>	1

			$\delta^2 \mathrm{T}'$			
	sin.	cos.	n't sin.	n't cos.	$n'^2t^2\sin$.	n'^2t^2 cos.
и i' i —I 9—4	 0. 390	o. o85	— II. 6	+93.5	+2.8	+0.2
0 8—4 1 7—4	+0. 325 0. 032	+0.023 +0.008	+ 7.6 + 1.2	-60.5 + 3.2	0.8	0.0
-I IO-4 0 9-4 I 8-4	-0. 08575 +0. 0646	+0.01461 0.0189	+ 10. 200 - 7. 04	+24.440 -16.81	+1.317 -0.72	-0. 725 +0. 50
-I II-4 0 I0-4	+0.033 +0.02219 +0.010540	0. 003 0. 02872 0. 007515	+ 0.9 + 4.309 - 3.3849	+ 0.7 + 3.296 - 2.5618	+0. 214 0. 1310	—0. 374 —0. 2400
1 9 4 0 11 4	+0. 01023 +0. 0002	-0. 01044 +0. 0010	+ 0.812	+ 0.332	+0.014	o. o46
-I 3-5 0 2-5	+0.07 —0.05	-0. 14 +0. 12	+ 31 - 28	+20 -18		
0 3-5 -1 5-5	0. 00 0. 00 0. 03	-0. 13 +0. 12 -0. 06	+ 32 27 + 10	+ 4 - 5 - 3		
0 4— 5 —1 6— 5	+0.03 +0.23	+0.05 +0.13	- 9 + 3	+ 3 3		
o 5-5 -1 7-5	-0. 16 +0. 23	o. o8 o. oo				:
o 6— 5 —1 8— 5 o 7— 5	—0. 15 +0. 09 —0. 05	0. 00 —0. 05 +0. 03	+ I - 6 + 2	+ 2 1 + 4		
-I 9-5 o 8-5	+0.478 -0.32	-0.751 +0.53	—158.8 +108	70.9 +48		
1 7— 5 —1 10— 5	0. 00 +0. 056	-0. 01 -0. 371	— 15 — 93. 0	— 6 + 5.8		
0 9— 5 1 8— 5 —1 11— 5	0. 035 0. 005 0. 061	+0. 309 -0. 055 -0. 151	+ 66.7 - 6.7 - 25.1	- 4.4 + 2.1 +16.2		
o 10 5 1 9 5	+0.079 -0.006	+0.178 0.006	+ 18.3 - 0.8	—II.9 + I.2		
-I 12-5 o II-5 I I0-5	—0. 0326 +0. 188 —0. 042	-0. 0329 +0. 124 -0. 026	- 3.67 + 3.0 0.0	+ 6.63 6.0 + 0.3		
-I I3- 5 0 I2- 5	+0.0320 +0.0011	-0.020 0.0149 +0.0181	- 0.28 + 0.18	+ 0. 88 - 1. 14		
1 11— 5 —1 4— 6	0.0017 +0.10	0.0012 +0.02	6	+16		
o 3-6 -1 5-6	o, o8 +-o. o9	-0. 0I -0. 02	+ 4 + 1	—15 +17		
o 4-6 -1 6-6	o. o8	+0.01	— I + 4	-14 + 7		
o 5— 6 —I 7— 6 o 6— 6	-0.03 +0.02	+0. 12 -0. 08	4	<u> </u>		

Arg=			$\delta^2 { m T}'$			
$n\gamma'+i^7g'+ig$	sin.	cos.	n't sin.	n't cos.	n'^2t^2 sin.	n'2t2 cos.
κ i' i I 8 6	,, +0.02	+0.11	"	"	"	"
0 7—6	o. oi	o. o8			1	1
_r 9—6	+0.04	+0.03	3	— <u>3</u>	l .	
0 8 6	_0, 02	0.00	+ 2	+ 6		
r ro 6	+0.54	+o. 22	+26	—129	ł	
0 9—6	—0. 36	-0, 12	—18	+ 99	ł	
ı 8— 6	+0.06	+0.02	+ 4	— 17	l	
1 II 6	+o. 28	-0.02	-20	— 66		
о 10— 6	—0. 22	+0.03	+15	+ 54		
ı 96	+0.03	o. oɪ	— 3	_ 6		
—ı 12— 6	+0. 22	+0.09	—15. 3	— 15. 1		
o 11— 6	0. 28	+0.22	+12.3	+ 12.4		
и 10 6			— 2	I		
_r r 3 _ 6	-0. 054	+0.150	4·7	— I. 3		
0 12-6	+0.023	0. 060	+ 4.1	+ 1.1	ĺ	
<u>—1</u> 6— 7			11	+ 3		
—1 8— 7	— о. 09	0, 00				
0 7— 7	+0.07	0,00			i	
— 1 9— 7	o. o8	+0.03			1	
0 8— 7	+0.06	0.03		•	1	
_1 10— 7	+0.05	0.02	+ 1	- 7	ŀ	
0 9-7			— 4	+ 3		
_I II- 7	— 0. 04	+o. 35	+93	— 2		}
0 10— 7	+o. o3	o. 27	 76	+ 3	Ì	
I 9-7			+14	٥		
—ı 12— 7	+0.08	+o. 22	+51	— 28	1	
0 11 7	0, 06	—о. 17	41	+ 23		
1 10-7			+ 5	- 3		
—r 13— 7	+0.02	+0.02	+11	- 17		
0 12— 7	-0.04	0. 03	— 9	+ 14		
_1 II— 8			+ 4	o		
о 10— 8			5	+ 3		
—I 12— 8			+16	+ 61	ļ	
o 11—8			— r 3	48		1
1 10— 8			+ 2	+ 7		
i 13- 8			+29	+ 33		
0 12- 8			—24	- 28		
1 11 8			+ 4	+ 3		
— і 13— 9			24	+ 13		
0 12 9			+20	- 11		
		<u> </u>	1		<u> </u>	1

In precisely the same manner as $\overline{W_0}'$ and $\overline{\delta W_0}'$ have, in preceding chapters, been derived from T' and $\delta T'$ we now get $\overline{\delta^2 W_0}'$ from $\delta^2 T'$. In the case of the terms depending on the arguments 5g'-2g and 10g'-4g the motion of the argument has been equated. By adding T', $\delta T'$, and $\delta^2 T'$ we obtain

$$\mathbf{T}' + \delta \mathbf{T}' + \delta^2 \mathbf{T}' = \begin{bmatrix} ... & ... & ... & ... & ... \\ 1... & 1.238805 + 0.004092190n't - 0.0000019944n'^2t^2 \end{bmatrix} \sin \left(\frac{5g' - 2g}{2g} \right) \\ + \begin{bmatrix} 2.7810935 - 0.002383674n't - 0.0000027721n'^2t^2 \end{bmatrix} \cos \left(\frac{5g' - 2g}{2g} \right) \\ + \begin{bmatrix} 0.0796974 - 0.00029408n't - 0.0000001310n'^2t^2 \end{bmatrix} \sin \left(\frac{10g' - 4g}{2g} \right) \\ + \begin{bmatrix} -0.0812486 - 0.00022188n't + 0.0000002400n'^2t^2 \end{bmatrix} \cos \left(\frac{10g' - 4g}{2g} \right) \end{bmatrix}$$

In the case of the argument 5g'-2g we get \varkappa and the corrected integrating factor from

$$\log \mu = 7.1938508n$$
 $\log \mu = 1.4977415$

In the case of the argument 10q'-4q the similar quantities are

$$\log \kappa = 7.50649n$$
 $\log \mu = 1.1972902$

The expression just written can then be transformed into

```
 \begin{array}{l} " \\ \text{1.1238805} - 0.000253577n't + 0.0000003582n'^2t^2] \sin \left( 5g' - 2g + \varkappa n't \right) \\ + \left[ 2.7810935 - 0.000627487n't + 0.0000002271n'^2t^2 \right] \cos \left( 5g' - 2g + \varkappa n't \right) \\ + \left[ 0.0796974 - 0.00003328n't + 0.000001706n'^2t^2 \right] \sin \left( 10g' - 4g + \varkappa n't \right) \\ + \left[ -0.0812486 + 0.00003394n't - 0.000002854n'^2t^2 \right] \cos \left( 10g' - 4g + \varkappa n't \right) \\ \end{array}
```

Integrating this the result is

```
\begin{aligned} \mathbf{W}_{0}' + \delta \mathbf{W}_{0}' + \delta^{2} \mathbf{W}_{0}' &= \begin{bmatrix} -35.95457 + 0.00842664n't - 0.000011267n'^{2}t^{2} \end{bmatrix} \cos\left( 5g' - 2g + \kappa n't \right) \\ &+ \begin{bmatrix} 87.22464 - 0.01903107n't + 0.000007143n'^{2}t^{2} \end{bmatrix} \sin\left( 5g' - 2g + \kappa n't \right) \\ &+ \begin{bmatrix} -1.24551 + 0.0003825n't - 0.000002687n'^{2}t^{2} \end{bmatrix} \cos\left( 10g' - 4g + \kappa n't \right) \\ &+ \begin{bmatrix} -1.28572 + 0.0006191n't - 0.000004495n'^{2}t^{2} \end{bmatrix} \sin\left( 10g' - 4g + \kappa n't \right) \\ &= \begin{bmatrix} -35.95457 - 0.1278715n't + 0.00062367n'^{2}t^{2} \end{bmatrix} \cos\left( 5g' - 2g \right) \\ &+ \begin{bmatrix} 87.22464 - 0.0752141n't - 0.000086179n'^{2}t^{2} \end{bmatrix} \sin\left( 5g' - 2g \right) \\ &+ \begin{bmatrix} -1.24551 + 0.0045096n't + 0.00001743n'^{2}t^{2} \end{bmatrix} \cos\left( 10g' - 4g \right) \\ &+ \begin{bmatrix} -1.28572 - 0.0033789n't + 0.000003357n'^{2}t^{2} \end{bmatrix} \sin\left( 10g' - 4g \right) \end{aligned}
```

If from the latter expression we subtract the following (obtained at page 319)

$$W_0' + \delta W_0' = \begin{bmatrix} -36.20315 - 0.1261798n't \end{bmatrix} \cos (5g' - 2g) + \begin{bmatrix} 87.71763 - 0.0767907n't \end{bmatrix} \sin (5g' - 2g) + \begin{bmatrix} -1.02918 - 0.0006600n't \end{bmatrix} \cos (10g' - 4g) + \begin{bmatrix} -1.09555 + 0.0005106n't \end{bmatrix} \sin (10g' - 4g)$$

we get

$$\delta^{2}W_{0}' = \begin{bmatrix} 0.24858 - 0.0016917n't + 0.000062367n'^{2}t^{2} \end{bmatrix} \cos(5g' - 2g) \\ + [-0.49299 + 0.0015766n't - 0.000086179n'^{2}t^{2}] \sin(5g' - 2g) \\ + [-0.21633 + 0.0051696n't + 0.000001743n'^{2}t^{2}] \cos(10g' - 4g) \\ + [-0.19017 - 0.0038895n't + 0.000003357n'^{2}t^{2}] \sin(10g' - 4g)$$

The value of $\delta^2 \overline{W_0}'$ follows:

Arg=i'g'+ig			$\overline{\delta^2 W_0}'$			
111g—19 +19	cos.	sin.	n't cos.	n't sin.	n'^2t^2 cos.	$n'^2t^2\sin$.
i' i 0 0	"	"	+ 30.0165	"	,, + 46.8625	"
1 0	+o. 1045+k ₁	$+0.0438+k_2$	603.51	+1007.93	-437.40	<u></u> 627. 38
2 0	-0. 164+[8. 45] k_1	$-0.289+[8.45]k_2$	+ 37.6	+ 9.7	— 12.9	19.2
3 0	0.001	333	+ 55.5	+ 8.5	:	
4 0	0.011	0. 020	o. I	o. I		
—4— I			— o, 2	+ 0.3		
-3- ı	0, 002	+o. oog	+ 0.8	+ 0.4		
-2 I	+0. 130	+o. o31	+ 1.9	- 23.3		
—I— I	+0.074	+0.062	+ 8. o	— 13.6	+ 0.2	+ 0.1
0— I	+0. 02 I	+o. o3o	+ 4.6	— 5 .6	+ o. 1	+ 1.7
1 1	+0.0089	+0.0475	— 2.63	— o. 78	- 2.07	+ 2.28
2— I	—o. 1444	+o. 1034	 7⋅34	— v. 34	— 16.73	+ 12.78
3— I	+0. 2896	-0.4214	+ 65.58	+ 65.16	+ 2.67	+ 0.44
4— I	о. 3839	—о. 1381	+ 26.76	- 6o. 8 1	+ 0.32	+ o. 26
5— I	o. o31	-o. o33	+ 4.1	— 3.6		
6— 1	0.009	-0. 02 4	+ 0.1	— O. 2		
_2 _ 2	+0.004	+0.001	+ 0.4	o. 8		
—I— 2	+0.025	o. o58	— 11.3	- 3.5		
0— 2	+0.029	-0,020	- 3.9	— 3·5	0.0	— о. з
I— 2	0. 004	-0.008	— I.4	_ 2.3	+ 1.5	0.0
2— 2	0.092	-0.044	+ 0.6	+ 0.4	- 2.7	+ 0.4
3— 2	o. 09 7	о. 117	+ 10.4	+ 1.1	— 7⋅4	+ 0.5
4— 2	+o. 1342	+o. 8045	+368.07	— 44.88	- 31.78	+460.11
5— 2	+0. 268 7 6	0. 49996	18. 561	+ 13.919	十 59.597	81.901
6 2	—1. 6194	+1.1965	45. 27	— 8 5 . o ₃	+ 8.80	3.64
7— 2	0.013	+0.030	— I. 2	— 2.5		
8— 2	0.011	o. oo6				
-ı- 3	+0.005	0, 004	o. 5	_ 1.5		
0 3	o. o25	0.015	- 2.7	+ 4.7		
ı_ 3	0. OI2	-o. o25	— 3. I	+ 2.5		
2— 3	—о. 006	-o. oo6	+ 0.6	+ 0.6	— O. 2	o. 5
3— 3	o. o31	+0.044	+ 0.6	+ 0.8	0, z	0. I
4 3	-o. o61	+0.030	+ 0.9	- 0.4	- 3.5	+ 0.8
5 3	-0.073	+0.007	+ 4.3	— 6. g	- 7. I	_ 2.2
6— 3	—o. 3219	—o. 1746	+ 55-95	— 56. 94	- 8.11	- 8. 14

i' i 7-3 8-3 9-3 0-4 1-4 2-4		sin.	n't cos.	n't sin. " — 39.45	n'2t2 cos.	$n'^2t^2\sin$.
7-3 8-3 9-3 0-4 1-4	0. 1628 +-0. 0240 +-0. 0121	+0. 3788 0. 0495	88.71		"	
7-3 8-3 9-3 0-4 1-4	+0. 0240 +0. 0121	0. 0495	·	— 39·45		"
9— 3 0— 4 1— 4	+0, 0121		+ 6.87		+ 0.73	+ 1.46
0— 4 I— 4	·	—0. 0127		+ 6.24	— o. o2	— o. o6
1 4	0, 009		— I.OI	I. 20		
	0.009	1	— O. 2	0.0		
2— 4		+o. oo6	+ 2.2	+ 2. I		
	-o. oo7	+0.001	+ o.9	+ 2. I		
3— 4	+0.005	+0.004	— 0.4	+ o.6		
4 4	+0.023	+0.029	+ o. 1	— 0.3	+ o. 2	+ 0.5
5 4	+0.010	+o. o39	+ o.8	— o. 1	+ 0.5	+ 1.1
6— 4	0.003	 0. 017	- 2.2	- 2.0	o. 6	+ 1.7
7— 4	-o. 238	+o. 236	38.3	53.8	I. I	+ 0.7
8— 4	—0. 199	+o. o88	- 12.5	 5 9⋅5	+ 2.0	o. 5
9— 4	+1.9273	+0.4733	—163.35	+390.03	20. 53	—II. 42
10— 4	-o. 22537	0. 20540	+ 48. 531	— 36. 1 68	+ 1.557	+ 3.055
2— 5	+0.003	+0.003	+ 0.6	- 0.4		
3— 5	0.000	+0.002	+ 0.9	0.0		
4 5	+0.001	+0.001	+ 0.3	0.0		
5 5	+0.015	0.009	+ 0.5	+ 0.5		
6— 5	+0.019	0.000	+ 0.2	- o. 3		ļ
7 5	+0.015	+0.011	- 2.2	+ 0.1		
8— 5	+o. o68	+ 0. 104	— 26. о	+ ro.8		
9— 5	+0.011	+0.077	21.0	- 1.9		
10— 5	—о. 013	+o. o36	— 10.5	— 7⋅3		
11- 5	+0.0394	-o. ooo6	6.68	- 11.76		
12— 5	0. 0543	—o. o678	+ 0.91	+ 4.25		
3— 6	+0.002	o. oor	0.2	— O, 2		
4— 6	+0.002	+0.001	0.0	- 0.4		
5— 6			0.0	- 0.2		
6 6	0,002	0. 006				
7- 6	+0.002	0.006				
8— 6	+0.007	—o. oo6	- 0. I	+ 0.3	ł	
9— 6 10— 6	+0.060 +0.032	—0. 028 —0. 001	+ 2.7 2.6	+ 12.5 + 7.0		1
11 6	0.000	0.011	— 2.6	+ 2.2		1
12— 6	—0. 020	o. o58	- I. I	+ 0.3		1
5 7			— 1.0	o. 3		
7-7	0.003	0, 000		3	l	
8— 7	-0.004	0.001			1	-
9 7	+0.007	+0.001	0.0	+ 0.6	l	1
10— 7	-0.002	0.019	+ 6.3	0,0	l	
11— 7	+0.006	-0.014	+ 3.8	+ 2.0		
12— 7	0, 002	+0.001	+ 0.8	+ 1.3		
1o— 8	}		— o. i	o. 3		}
11—8			+ 0.7	— 3. ī		
12— 8	j		+ 1.5	— I. 5		
12- 9			— o.7	o. 3		

Arg=i'	a'⊥ia	$\overline{\delta^{21}}$	W ₀ ′
g/;	9 1-09	$n^{/3}t^3$ cos.	n'^3t^3 sin.
<i>i'</i>	i	// +0.0000001407	11
1	0	+0.0000001850	+0.0000000413
2	0	+0.000000051	+0.000000011

Arg=i'g'+ig		$-rac{1}{2} \Big(rac{ar{d} \cdot \delta^2 \mathrm{W_0'}}{d\gamma'} \Big)$					
	sin.	cos.	n't siu.	n't cos.	$n'^2t^2 \sin$.	$n'^2t^2\cos$.	
i' i I o 2 o 3 o	,, +0. 1646 -0. 046 +0. 005	-0. 1232 +0. 160 +0. 259	-297.69 + 23.3 + 44.0	—500.26 — 14.5 — 8.0	—214.75 — 12.3	+310.36 + 17.6	
4 0 -3- I -2- I	+0. 025 -0. 003 -0. 122	+0. 014 +0. 005 +0. 028	+ 0.8 - 0.9 - 2.1	+ I.4 0.0 - 2I.2			
-I- I I- I	-0. 068 -0. 021 +0. 0104	+0. 057 +0. 046 +0. 0926	- 7.8 - 7.2 + 0.32	— 13.8 — 6.0 — 1.05	- 0.2 + 1.8 + 1.31	o. o — 3. o + 1. 57	
2— I 3— I 4— I 5— I	+0. 0669 +0. 1711 +0. 1141 -0. 013	+0. 0596 +0. 1366 +0. 0212 +0. 020	+ 1.66 + 19.35 - 4.37 + 1.9	- 2. 14 - 37. 77 - 24. 32 + 1.0	+ 8.45 + 3.65 + 0.48	+ 6.34 + 0.25 - 0.30	
6— 1 —2— 2 —1— 2	0. 007 0. 004 0. 029	+0. 020 +0. 001 -0. 057	+ 0.1 - 0.4 + 10.9	+ 0.2 - 0.8 - 3.5			
0— 2 1— 2 2— 2 3— 2	0. 040 0. 012 +-0. 063 +-0. 062	-0. 032 -0. 003 -0. 030 -0. 069	+ 5.8 + 1.6 - 0.6 - 6.9	- 5.6 - 3.6 - 0.3 + 1.1	- 0.7 + 1.5 + 5.4	— 0.1 + 0.3 + 3.9	
4— 2 5— 2 6— 2 7— 2	0. 0774 +0. 15093 0. 7888 0. 019	+0. 4493 +0. 35737 -0. 5824 -0. 033	—166. 35 + 59. 296 — 18. 14 — 1. 3	- 22.48 - 35.980 + 34.45 + 1.8	+ 15.46 + 1.534 + 4.35	+225.67 + 2.073 + 1.79	
-I- 3 0- 3 I- 3 2- 3	-0.001 +0.028 +0.013 +0.003	-0. 002 -0. 021 -0. 027 +0. 013	+ 0.7 + 3.0 + 4.1 + 1.8	- 1.0 + 5.1 + 2.9 - 0.5			
3— 3 4— 3 5— 3 6— 3	+0.031 +0.052 -0.002 -0.0922	+0. 039 +0. 025 +0. 006 +0. 0893	+ 0.3 - 0.7 + 0.4 + 11.02	0.0 + 0.5 + 10.2 + 14.70	+ 0.3 + 3.4 + 5.6 + 4.88	0.0 + 0.7 1.7 5.11	
7— 3 8— 3 9— 3	+0.0023 +0.0053 +0.0066	+0. 1481 +0. 0270 +0. 0083	+ 36.51 + 5.90 + 0.70	- 3·33 - 2·73 - 0·49	— 0.06 — 0.12	0. 14 0. 20	

Arg=i'g'+ig			$-\frac{1}{2}(\overline{\frac{d}{\cdot}},$	$\frac{d^2 \overline{W_0'}}{d \gamma'}$		
	sin.	cos.	n't cos.	$n't ext{ sin.}$	$n'^2t^2\sin$.	$n'^2t^2\cos$.
i' i	11	"	11	11	11	"
I— 4	+0.017	+0.012	2.8	+ 2.8		
2 4	+o. o16	+o. oo3	— I. 2	+ 2.6		
3— 4	+0.001	+0.001	+ 0.2	+ 1.4		
4 4	0.022	+0.027	+ 0.1	+ 0.1	0, 0	+0.1
5— 4	-0. 008	+ 0. 036	+ 0.1	+ 0.5	0. 2	+1.5
6— 4	+0.002	- +0. 064	+ 4.4	— I.9	+o.6	+1.4
7— 4	+0. 194	+0. 191	+30. o	— 42. 7	+o. 8	+0. 6
8— 4	+0.146	+0.059	+10.8	— 39. 1	o. 9	0.4
9— 4	0. 9131	+o. 2253	+78.43	+186.46	十9.88	5 ⋅44
10 4	+o. 01622	—o. 0189 5	+ 2.470	+ 1.736	+0. 107	o. 1 99
2— 5	0. 004	+0.007	— 1.6	_ I.O		
3 5	0,000	+0.007	— I.9	- 0.2		
4 5	+0.001	+0.003	— o.6	+ 0.2		
5 5	0. 019	-0, 010	— O. 2	+ 0.2		
6— 5	0, 021	0.000				
7— 5	0. 014	+0.011	+ 1.9	+ 0.7		
8— 5	0. 070	+0.113	+22.9	+ 10.7		
9 5	0, 010	+0.073	+19.0	— I.7		
10 5	+0,022	+0.055	+ 8.9	— 6. ₃		
11- 5	+0.0300	+0.0323	+ 4.39	7.85		
12- 5	+ 0. 0261	—o. o134	— O. 24	+ 0.75		
3— 6	0.004	-0.001	+ 0. z	— o.7		
4— 6	o. 004	+0.001	0.0	— o.9		
6 6	+0.002	-0.007				
7— 6	-0.001	0.008		1		
8— 6	—o. oo6	0.003	+ 0.1	+ 0.9		
9— 6	—o. o53	0.021	2.2	+ 12.4		
10— 6	0. 034	+0.001	+ 2.3	+ 7.9		
11— 6	-o. oo3	0.003	+ 2.3	+ 2.4		
12— 6	+0.014	—o. o39	+ 1.2	+ 0.3		
5— 7			+ 0.5	— o. 1		
7— 7	+0.005	0.000				}
8 7	+0.005	0.002				
9 7	-o. oo3	-0.001	0.4	+ 0.5		
10- 7	+0.003	-o. o28	— 6.8	+ 0.2		
11 7	0. 007	0. 020	— 4·4	+ 2.4		
12— 7	0. 002	-0.002	— I.2	-+ 1.9		
10— 8			— o. 2	0.0		
11— 8			0.9	- 4.2		
12 8			— I.9	— 2.3		
12 9			+ 1.3	- 0.7		

, ,

Arg=i'g'+ig	$-\frac{1}{2}$	$\left(\frac{d \cdot \delta^2 W_0'}{d\gamma'}\right)$
	n'^3t^3 sin.	n'^3t^3 cos.
i' i I O 2 O	+0.0000000925 +0.0000000051	 0. 0000000206 0. 000000011

Similarly, as in the case of Jupiter, we have the equation

$$\frac{d_{}\cdot\delta^3z}{dt} = \overline{\delta^2 \mathbb{W}_0{}'} + \left(\overline{\frac{d\mathbb{W}_0{}'}{d\gamma'}}\right)n'\delta^2z' + \left(\overline{\frac{d_{}\cdot\delta\mathbb{W}_0{}'}{d\gamma'}}\right)n'\delta z' + \frac{\mathbf{I}}{2}\left(\overline{\frac{d^2\mathbb{W}_0{}'}{d\gamma'^2}}\right)(n'\delta z')^2 + 2\nu'\delta\nu' + \nu'^2\frac{d_{}\cdot\delta z'}{dt}$$

All the factors involved in the right member of this equation have already been given. But, as in forming the product $\left(\frac{\overline{dW_0'}}{d\gamma'}\right)n'\delta z'$, in treating the terms of the second order, we have corrected the two factors for the terms multiplied by n't, belonging to the arguments g', 2g', etc., and which result from the previous computation of $\delta W_0'$, these terms must be omitted from the factors $n'\delta^2 z'$ and $\left(\frac{\overline{d\cdot\delta W_0'}}{d\gamma'}\right)$.

The expressions of the five additional products involved in $\frac{d \cdot \delta^3 z'}{dt}$ follow:

Arg=i'g'+ig		$\Big(rac{\overline{d W_{0'}}}{d \gamma'}\Big) n'\delta^2 z'$					
	cos.	sin.	n't cos.	n't sin.	$n'^2t^2\cos$.	$n'^2t^2\sin$.	
i' i	11	"	+ 1. 3876	"	 —4. 2695	"	
1 0	o. 3845	0. 2190	+47.63	—62.77	o. 23	0, 00	
2 0	+0.013	+0.055	-12.8	+ 1.9	-1.9	— 3⋅5	
3 0	+0.002	+0.131	-23. 2	2.7	—о. 1	0. 2	
4 0	+0.013	+o. oo8	— 2. O	+ 2.0			
—3— I			0.3	+ 0.1			
—2— I	0. 043	-0.010	- o. 8	+ 8.2		1	
I I	0. 019	-o. o15	— 3. т	+ 4.6			
0 1	0. 003	-0.007	— I. 3	+ 0.9	2,0	3·7	
1— 1	+0.0111	—0. 0231	— o. o5	— o. 61	+2.13	— 4. 89	
2— 1	+0. 0080	+0.0113	+ 3.60	+ 3.51	-2. 37	+ 2.78	
3— т	+0.0139	+0.0689	—10. 88	+ 3.47	+6.32	+ 0.60	
4 I	+0. 3762	+o. o8o9	-24.44	+69.92	+o. 84	+ 1.12	
5— I	+0.010	+0.0006	— 2.4	+ 2.2			
—I— 2	-o. oo8	+0.016	+ 3.2	+ 1.0			
0— 2	-0.009	+0.006	+ 1.7	+ 1.6			
I— 2	-0.004	+0,001	+ 0.3	+ o.6	—1.3	+ o. 3	
z— 2	+0.002	+0,001	— о. 6	+ 0.4	+o. 3	— I. I	
3— 2	0. 001	0. 001	14.9	+ 9.5	 7.9	-23.9	

			$\left(\frac{\overline{d { m W}'_0}}{d\gamma'}\right)$	$n'\delta^2z'$		
Arg=i'g'+ig	cos.	sin.	n't cos.	n't sin.	$n'^2t^2\cos$.	$n^{\prime 2}t^{2}\sin$.
i' i	"	"	"	"	11	11
4 2	+0.0015	+o. oo63	—91.48	+15.79	3.27	—162.45
5— 2	+0.00594	-0.01510	— 9 . 967	— 3.022	+ 15.531	- 25. 272
6— 2	+0.0381	0, 0296	—52. 10	—69. 9 1	+147.14	— 76.41
7 2	o. oo7	0.000	— 3.0	— 3.6	+ 10.6	— 4·4
o 3	+o. oo6	+0.005	+ 0.7	1.3		
I — 3	+0.002	+0.005	+ o.8	— o. 5		
2— 3			+ 0.4	— о. 1	0.0	+ 0.5
4— 3			0.0	+ 0.7	+ 0.4	o. i
5- 3	+0.044	0, 001	— 2.9	+12.7	+ 0.6	0, 0
6— 3	+0. 3240	+0. 2040	—39. 72	+50.65	0.12	— o . o9
7— 3	+0.0454	—0. 0621	+11.93	+ 9. 18	+ 0.09	+ 0.30
8— 3	+0.0009	+0.0028	+ 2.23	+ 3.53	+ 0.08	o. 38
9— 3	0. 0188	+0.0256	+ 0.27	+ 0.52		
I— 4			0.4	0.4		
2 4			— O. 2	0.4		
5— 4			0.0	+ 0.4		i
6— 4	+0.017	o, oo8	+ 1.9	+ 3.9		
7— 4	+0.096	0. 096	+15.9	+21.1		
8 4		-0.017	+ 1.9	- 3⋅5		
9— 4	0. 4295	—0. 1185	+34.62	80.82	— o. 36	— о. 13
10— 4	-0.00229	0.00132	+ 3.311	2.898	— o. 111	— v. 153
11— 4	—o. 0009	+0.0022	+ 7.28	— I. 7I	— o. o4	— o. 39
7 – 5	0. 004	-0.001	+ 1.0	— o. 6		
8 5	—o. o23	—о. 038	+ 8.1	3.5		
9— 5	-0.004	-0. 023	+ 4.6	+ 0.3		
10 5	-0.002	+0.002	+ 1.5	+ 1.1		
11— 5	-o. 0082	+0.0175	+ 0.42	+· o. 86		
12 5	+0.0044	+0.0063	+ 0.05	— o, 1o		
9— 6	o. o18	+0,006	o, 6	- 3.2		
10— 6	-0.011	0. 002	+ o.6	- 1.9		
11— 6	0,000	0.000	+ 0.6	— o. 5		
12— 6	+0.005	+0.012	+ 0.2	— о. 1		

Arg=i'g'+ig	$\left(\frac{dW_0}{d\gamma}\right)$	$n'\delta^2z'$
;	n'^3t^3 cos.	$n^{\prime 3}t^3 \sin$.
i' i i o 2 o 3 o	0.000000031 +0.000000091 +0.000000013	

Arg=i'g'+ig	$rac{1}{2} igg(rac{ar{d}^2 \overline{\mathrm{W}}_0'}{ar{d} \gamma'^2}igg) (n' \delta z')^2$							
	cos.	sin.	n't cos.	n't sin.	n'^2t^2 cos.	$n'^2t^2\sin$.		
i' i	11	11	,, +0, 3610	"	 0. 4998	"		
10	-0.0181	—o. ∞59	+3.55	5.86	0. 25	+0.24		
2 0	-o. oo8	o. oo1	+2.8	I. 7	—о. 1	o. I		
o— 1	+0.004	+0.012			-0. 2	+0.4		
I— I	o. o176	+0.0627	+o. 36	o. 83	0. 27	+1.19		
2— I	-o. o162	+0.0207	+0. 12	—o. 95	o. o8	+0. 27		
3— 1	-0,0010	+0.0110	—1. oo	-2.53	o. o6	+0.07		
4 1			— 0. 29	—1. 76	+o. 29	+o. 28		
5— 1			+1.6	—1. 7	+0.3	+o. 3		
I— 2	-0.001	+0.003						
2— 2	0.010	0.004	o. 3	+o. 1	+0.9	+0.5		
3 - 2	+0.002	+0.003	o. 6	+0.3	+1.8	+2.0		
4— 2	+0.0105	+0.0365	-2.54	0.04	-0.02	+0.50		
5 2	+0.00426	+0.00003	—o. 685	0. 245	+0.041	-0. 151		
6— 2	+0.0195	0.0079	—I. 05	—r. 17	+0.83	0, 70		
7— 2 8— 2	-0,003	0.001 0.002	—о. 1	—о. 1	+2.7	o, I		
	0, 004							
3 3	-0,003	+0.003	100	اما				
4-3	0,002	+0.001	+0.2	+0.5	0.4	—o. I		
5— 3 6— 3	-0.001 +0.0012	+0,001 -0,0024	—0. 5 —1. 49	+2.6 +1.00	0. 4 0. 04	-0. 1 -0. 20		
7 3	+0.0012	-0.0094	-2. 12	+1.04	-0.13	-0.47		
8— 3	+0.0019	-o. o188	+o. 68	+o. 8o	-o. 13	+0.03		
9— 3	+0.0151	-o. 023I	+o. 78	+o. 67				
6— 4			— 0. 4	о. 1				
7— 4	-0.002	0, 000	+0.2	+0.2				
8— 4	0. 006	-0.005	+0.7	+2.4	0.7	0.0		
9— 4	-0.0142	—0.0062	o. 66	+2.70	—1. 09	0, 43		
10— 4	-0.01892	—o. 01948	+0.910	-0.704	+0.113	+0.191		
11-4	-0.0009	0.0017	+3.24	—о. 78	+0.09	+1.17		
10 5	o. oo6	+0.011	 0.4	—o. 3				
11— 5 12— 5	0. 0300 0. 0055	+0.0145 0.0001	0. 39 +0. 02	—1.05 —0.23	+0.09	0.02		
11— 6 12— 6	-0.002 -0.002	0. 002 0. 004						

Arg=i'g'+ig		$rac{1}{2} \Big(rac{d^2 \overline{W_0}'}{d \gamma'^2}\Big) (n' \delta z')^2$				
		n'^3t^3 cos.	$n'^3t^3 \sin$.			
i' I	i 0		,, 000000001			
3	0	+0.00000001 +0.00000005	+0.00000001			

Arg=i'g'+ig			$\left(\frac{\overline{d} \cdot \delta \overline{W_0}}{d \gamma'}\right)$	$n'\delta z'$		
	cos.	sin.	n't cos.	$n't \sin$.	n'^2t^2 cos.	n'^2t^2 sin.
i' i	"	"	,,, + 1.2216	"	- 0.0010	"
10	—0. 1265	—0. 1058	20. 70	+48.72	+ 0.12	+ 0.09
2 0	—o. oo5	-0.002	+ 3.0	— o. 5		
3 0	—o. oo5	-0.003	+ 2.3	+ 0.2		
4 0	—o. ∞8	+0.006	+ 1.6	+ 1.1		
5 °	-0.009	+0.004				
—4— I	-0.003	+0.004				
—3— I	-0, 004	+0.003	— o. 2	— o. 6		
—2— I			+ o. 1	- o. 8		
1 1	+0.002	+0.009	+ 1.7	2. I	— o. 5	— o. 8
0 1	0. 008	0.004	+ 1.9	— o. 7		
I I	+0.0132	о. 0396	+ 2.68	+ 0.74	— I. 26	— I.04
2— I	+0.0650	о. 0168	- 4. 27	+ 1.33	+ o. 18	- o. 31
3 1	+0.0185	-o, o118	+ 3.16	+ 6.40	+ 5.23	+ 1.67
4— 1	0.0031	+0.0128	— o. 18	+ 3.04	+ 0.39	+ 0.59
5— 1	+0.009	+0.024	— I. 3	+ 2.6		
6 I	+0.007	+0.019				
7— І	-o. oo3	+0.014				
0 2			— v. 6	- 1.0		
I- 2	+0.012	-o. oor	0.0	— o. 9		
z— 2	+0.074	+0.033	+ o. I	0.4	+ 1.5	- 0.3
3- 2	+0.047	+0.058	- 5.5	+ 5.4	- 8.5	-14.9
4 2	0, 0119	-0.0841	+ 2.04	+ 0.18	+ 6.39	+23.02
5— 2	+0.00045	—о. 01806	- 7.214	- 2.084	+15.183	24. 804
6 2	+0.0026	o. oo35	+ 0.81	+ 1.38	+20.27	11.76
7— 2 8— 2	+0.053	0.006	0.0	+ 0.2	+ 1.1	0.6
0 2	+0.030	+0.013				
1— 3	ŀ		o. 3	+ 0.1		
2— 3	+0.001	—о. 003				
3 3	+0.023	0.029			+ 0.5	o. 6
4 3	+0.032	-0.017	- 0.4	— o. 6	+ 0.6	0, 2
5— 3	+0.025	-0.011	+ 0.5	— 1.8	+ 1.2	+ 0.3
6-3	-0.0023	0. 0303	+ 9.93	2.19	+ 0.40	+ 0.39
7— 3 8— 3	—0.0054 —0.0045	+0.0247	+ 6.80	— I. I3	+ 0.14	+ 0.45
9— 3	+0.0045 0.0083	+0.0523 +0.0168	+ 1.41 + 0.09	+ o. 88 + o. 07	0,02	0.08
		·	T 0,09	T 0.07		
4— 4	-0,010	-o. o13				
5— 4	-0.004	-0. org	1.00			
6— 4	0.001	-0.009	+ 2.8	+ 0.9	+ 0.2	0.3
7— 4 8— 4	-0.007	0,000	+ 2.2	+ 1.6	+ 0, 2	— 0. 2
9— 4	—0. 047 —0. 1678	+0, 016 -0, 0215	— 0.7 +21.32	-12.6	— 0. r	0, 0
9— 4 10— 4	+0.03340	+0. 03602	+ 3.045	50, 00 2, 678	0. 16	- 0.02 - 0.082
11-4	+0.0009	+0.0038	— 0.09	- 2.078 - 0.13	— 0.059 + 0.02	- 0.062 + 0.16
	1 0009	1 3-		* 3	1 3.02	7 0.10

Arg=i'g'+ig	$\Big(rac{d\cdot\delta W_{o'}}{d\gamma'}\Big)n'\delta z'$							
	cos.	sin.	n't cos.	n't sin.	n'^2t^2 cos.	$n'^2t^2\sin$.		
i' i 6— 5 7— 5 8— 5 9— 5 10— 5 11— 5 12— 5 10— 6 11— 6 12— 6	" -0.005 -0.004 -0.006 0.000 +0.0252 +0.0188 +0.010		+0.8 +2.6 +1.7 +0.51 +0.03 +0.3 +0.5 +0.3	-0.3 +0.3 +1.1 +1.21 -0.02 -1.1 -0.5 0.0	"	"		

Arg=i'g'+ig	$\Big(rac{\overline{d}\cdot \delta \overline{\mathbf{W}_0'}}{d\gamma'}\Big)n'\delta z'$				
Arg—vy +vy	$n^{/3}t^3$ cos.	n'^3t^3 sin.			
i' i i o 2 o 3 o	+0. 000000006 +0. 000000092 +0. 00000005				

Anomital Lin	$2 u'\delta v'$							
Arg=i'g'+ig	cos.	sin.	n't cos.	$n't \sin$.	$n'^2t^2\cos$.	$n'^2t^2\sin$.		
i' i o o I o 2 o 3 o			" -0.7446 +0.82 +1.1 +0.4		+2. 1365 +1. 11 -1. 0	+ 0.77 1.8		
0— I I— I 2— I 3— I 4— I 5— I	+0.001 +0.0026 +0.0002 -0.0147 +0.0037	+0.002 -0.0022 -0.0096 +0.0054 +0.0007	+0.6 +0.09 0.17 1.38 0.37 0.0	0. 2 0. 38 1. 23 2. 72 +-1. 86 0. 1	0. 6 0. 05 +-0. 61 2. 14 +-0. 23	- I. 3 - I. 08 - I. 03 - 0. 62 + 0. 49		
2— 2 3— 2 4— 2 5— 2 6— 2 7— 2	+0.002 0.000 +0.0022 -0.00294 +0.0002	+0.001 +0.001 +0.0074 +0.00605 +0.0007	-0. 2 -4. 2 -1. 54 +5. 905 -0. 37	+0. I +3. 7 +0. 28 +2. 043 -0. 51	+0.4 -4.1 -0.62 -7.510 +3.28 +1.2	- 0. 2 - 7. 8 + 2. 79 + 12. 476 - 1. 30 - 0. 1		
5— 3 6— 3 7— 3 8— 3	+0.013 0.0002 0.0017 +0.0002	0.001 0.0074 0.0018 0.0009	-0.7 +3.93 -0.26 -0.38	+3·7 —1.16 —0.96 —0.58	0. 16 0. 05 0. 02	0. 13 0. 15 +- 0. 10		

	$2 u'\delta u'$							
Arg=i'g'+ig	cos.	sin.	n't cos.	n't sin.	$n'^2t^2\cos$.	$n'^2t^2\sin$.		
i' i 6— 4 7— 4 8— 4 9— 4 10— 4 11— 4	0. 021 +-0. 0038 +-0. 00038	+0.007 +0.0017 -0.00017	" +0.5 +0.7 -1.0 -1.23 -1.132 +0.39	+0. z +0. 6 -7. I +2. 43 +1. I32 -0. 04	+0.052	+0.073		
10— 5 11— 5 12— 5	-0.004 +0.0052 -0.0008	+0.006 +0.0018 -0.0011	0, 00	0. 04				

	$2 u'\delta u'$				
Arg=i'g'+ig	n'^3t^3 cos.	$n'^3t^3\sin$.			
i' i i o 2 o 3 o	+0.000000031 +0.000000046 +0.00000004				

Arg=i'g'+ig	$rac{d\ .\ \delta z'}{dt} u'^2$						
	cos.	sin.	n't cos.	$n't \sin$.	$n'^2t^2\cos$.	n'^2t^2 sin.	
i' i o o i o	//	"		+0.47	-0.0073	"	
1— I 2— I 3— I 4— I	+0.0004	—0,0001	+0. 14 +0. 11 +0. 02	+0. 10 +0. 08 -0. 08	0. 06 +0. 18 +0. 15	+0.31 +0.02 -0.05	
2— 2 4— 2 5— 2 6— 2	0. 0001 0. 00054	0.0012 +0.00053	—o. o19	+0.008	+0. 3 -0. 12 -0. 076 -0. 38	+0. 1 0. 94 0. 115 +0. 25	
6— 3 7— 3 9— 4 10— 4	+0.0003	+0.0004	-0. 06 +0. 12 +0. 06 -0. 037	+0. 08 +0. 09 -0. 23 +0. 001	-0.00I	-o. oo5	

Arg=i'g'+ig	$rac{d\ .\ \delta z'}{dt} u'^2$			
	n'^3t^3 cos.	$n^{\prime 3}t^3$ sin.		
i' i	.,, u. 0000000047	+0.000000075		

The addition of the six terms of $\frac{d \cdot \delta^3 z'}{dt}$ gives the following expression for this quantity:

Arg=i'g'+ig		,	$rac{d.\delta^3z'}{dt}$			-
	cos.	sin.	n't cos.	n't sin.	n'^2t^2 cos.	$n'^2t^2 \sin$.
i' i	"	"	// + 32. 1644	"	" + 44. 2214	"
1 0	$-0.4284+k_1$	$-0.2924+k_2$	572.51	+988.21	436. 65	6 26. 2 8
2 0	-0.166+[8.44] k_1	0. 240+[8. 14]k ₂	+ 31.7	+ 9.2	— 15.9	24.6
3 0	0.004	0. 205	+ 35.0	+ 6.0	— o. 1	— O. 2
4 0	о, 006	— 0. 006	- o. 5	+ 3.0		
5 0	0,009	+0.004				
—4 — 1	-0.003	+0.004	0. 2	+ 0.3		
—3— I	о. 006	+0.012	+ o. 3	o. r		
2 I	+0.087	+0.021	+ 1.2	- 15.9		
—ı— ı	+0.057	+0.056	+ 6.6	11.1	— o. 3	- 0.7
0— I	+0.015	+0.033	+ 5.8	5.6	— 2. 7	— z. 9
I— I	+0.0182	+0.0453	+ 0.45	— 1.86	- 1.58	— 3.23
2— I	—o. 0870	+o. 1089	- 7.92	+ 2.42	18. 21	+ 14.51
3— т	+o. 3063	o. 3479	+ 55.59	+ 69.86	+ 12.17	+ 2.11
4— I	o. 007 I	0. 0437	+ 1.50	+ 12.17	+ 2.07	+ 2.74
5— I	0.012	0.003	+ 2.0	— o.6	+ 0.3	+ 0.3
6— т	0, 002	-o. oo5	+ o.1	O. 2		
7— I	—o. ∞3	+0.014				
-2- 2	+0.004	+0.001	+ 0.4	— o. 8		
—I— 2	+0.017	-o. 042	8. 1	2.5		
0— 2	+0.020	-0.014	2.8	— 2 . 9	0.0	- 0.3
1— 2	+o. 00 3	-o. oo 5	— I.I	— 2. 6	+ 0.2	+ 0.3
2— 2	-0. 024	o. o13	0.4	+ 0.6	+ 0.7	— 0.6
3 2	0.049	o. o56	- 14.8	+ 20.0	— 26. I	44. I
4— 2	+o. 1364	+0.7694	+274.55	28.59	29.42	+323.03
5— 2	+o. 27593	o. 5265 1	— 30. 541	+ 10.619	+ 82. 766	119. 767
6— 2	—1.5590	+1.1562	97. 98	-155. 24	+179.94	— 93. 56
7— 2	+0.030	+0.023	— 4⋅3	— 6. o	+ 15.6	5.2
8— 2	+0.015	+0.005				
-ı- 3	+0.005	0. 004	o. 5	- 1.5		
o— 3	0. 019	-o. o1o	- 2.0	+ 3.4		
I 3	-o. o1o	-0.020	2.6	+ 2.1		
2 3	-o. oo5	0.009	+ 1.0	+ 0.5	— O. 2	0.0
3 3	-0.011	+0.018	+ o.6	+ o.8	+ 0.3	— o. 7
4— 3	-o. o31	+0.014	+ 0.7	+ 0.2	2.5	+ 0.5
5 3	+0.008	0.005	+ 0.7	+ 10.3	— 5⋅7	 2. 0
6 3	+0.0008	0.0107	+ 28.54	— 8. 56	— 8. o ₃	- 8. 17
7 3	0. 1184	+o. 3306	— 72. ·24	- 31.23	+ 0.78	+ 1.59
8 3	+0.0315	o. 0141	+ 10.81	+ 10.87	0.11	— o. 39
9— 3	+0.0001	+0.0066	+ 0.13	+ 0.06		

Arg=i'g'+ig			$rac{d \cdot \delta^3 z}{dt}$	·/-		
	608.	sin.	n't cos.	n't sin.	$n'^{2}t^{2}\cos$.	n'^2t^2 sin.
i' i 0— 4	"	"	// 0. 2	// O. O	//	"
I— 4	0.000	⊹o. ∞6				
2— 4	0.009 0.007	+0.001	+ 1.8 + 0.7	+ 1.7 + 1.7		
3-4	+0.005	+0.004	— 0.4	+ o.6		
3 4 4 4	+0.013	+0.016	+ o. i	— 0.3	+ o. 2	+ 0.5
5— 4	+0.006	+0.026	+ 0.8	+ 0.3	+ o. 5	+ 1.1
6— 4	+0.013	-0.034	+ 2.6	+ 2.9	- 0.4	+ 1.4
7— 4	—o. 151	+0. 140	— 19. 3	30. 3	— o. 9	+ 0.5
8— 4	-0. 2 69	+0.089	— II. 6	— 80. 3	+ 1.2	— o. 5
9-4	+1.3196	+o. 3288	—109. 24	+264. 11	22. 14	-12.00
10 4	—0. 21280	—o. 19035	+ 54.628	- 41. 315	+ 1.551	+ 3.079
11-4	0.0009	+0.0043	+ 10.82	— 2. 66	+ 0.07	+ 0.94
					,,	1 .51
2— 5	+0.003	+0,003	+ 0.6	- 0.4	i	
3 5	0.000	+0.002	+ 0.9	0.0		
4 5	+0.001	+0,001	+ 0.3	0.0		
5— 5 6— 5	+0.015	0.009	+ 0.5	+ 0.5		
	+0.014	0.000	+ 0.2	0.3		
7— 5 8— 5	+0.007	+0.009	— I. 2	— o.5		
1	+0.045	+0.066	— 17. I	+ 7.0		
9- 5	+0.001	+0.059	13.8	— I.3		
10— 5	—0. 025	+0.046	— 7·7	— 5·4		
11— 5	+0.0316	+0.0284	6.14	- 10.74	+ 0.09	0.02
12- 5	0. 0374	—o. o525	+ 1.01	+ 3.86		
3 6	+0.002	0.001	- 0.2	- 0.2		
4 6	+0,002	+0.001	0,0	· 0.4		
5— 6			0.0	O. 2		
6 6	0.002	—o. oo6				
7— 6	+0,002	-0.006				
8— 6	+0.007	0, 006	— o. I	+ 0.3		
9— 6	+0.042	-0.022	+ 2, I	+ 9.3	·	
10 6	+0,021	-0.001	— I.7	+ 4.0		
11— 6	0.008	0.004	1.5	+ 1.2	·	
12— 6	-0.002	-0.011	o, 6	+ 0.2		
5— 7			- 1.0	— o. 3	l	
7— 7	0.003	0,000				
8- 7	o. oo4	0.001				
9— 7	+0.007	+0.001	0.0	+ 0.6		
10— 7	0. 002	—0. 019	+ 6.3	0, 0		
11- 7	+o. oo6	0.014	+ 3.5	+ 1.9		
12- 7	-0.002	+0.001	+ 0.8	+ 1.3		
10 8	i		o. 1	- o. 3		
11 8	1	*	+ 0.7	— 3. 1	1	
12— 8			+ 1.5	— 1.5		
12 9			— o.7	— o. 3		

Arg=i'g'+ig		$\frac{d}{d}$	$\delta^3z'\over t$
		n'^3t^3 cos.	n'^3t^3 sin.
i' I	<i>i</i> o	// +0.0000001853	,, +0, 000000286
2	0	+0.0000002351	0. 0000000859
3	0	+0.00000027	—0. 000000003

On integrating this expression we arrive at $n'\delta^3z'$. In order to make the terms depending on the argument g' disappear it is necessary to put $k_1 = +o''.3287$ and $k_2 = +o''.2339$. In the case of the terms involving the arguments 5g' - 2g and 10g' - 4g we equate the motions of the latter. By adding the values which have been obtained for $\frac{d \cdot \delta z'}{dt}$, $\frac{d \cdot \delta^2 z'}{dt}$, and $\frac{d \cdot \delta^3 z'}{dt}$ we get, taking the liberty of calling the sum $\frac{d \cdot \delta z'}{dt}$,

$$\frac{d \cdot \delta z'}{dt} = \begin{bmatrix} -35.06817 - 0.1504365n't + 0.000082766n'^2t^2 \end{bmatrix} \cos(5g' - 2g) + \begin{bmatrix} 84.57304 - 0.0853558n't - 0.000119767n'^2t^2 \end{bmatrix} \sin(5g' - 2g) + \begin{bmatrix} -1.17743 + 0.0047807n't + 0.000001551n'^2t^2 \end{bmatrix} \cos(10g' - 4g) + \begin{bmatrix} -1.22444 - 0.0035990n't + 0.000003079n'^2t^2 \end{bmatrix} \sin(10g' - 4g)$$

For this expression may be substituted

$$\frac{d \cdot \delta z'}{dt} = \begin{bmatrix} \frac{\pi}{35.06817} + 0.0081298n't - 0.000015631n'^2t^2 \end{bmatrix} \cos \left(\frac{5g' - 2g + \kappa n't}{5g' - 2g + \kappa n't} \right) \\ + \begin{bmatrix} 84.57304 - 0.0196064n't + 0.000013638n'^2t^2 \end{bmatrix} \sin \left(\frac{5g' - 2g + \kappa n't}{5g' - 2g + \kappa n't} \right) \\ + \begin{bmatrix} -1.17743 + 0.0004987n't - 0.000003835n'^2t^2 \end{bmatrix} \cos \left(\frac{10g' - 4g + \kappa n't}{5g' - 2g + \kappa n't} \right) \\ + \begin{bmatrix} -1.22444 + 0.0005186n't - 0.000006152n'^2t^2 \end{bmatrix} \sin \left(\frac{10g' - 4g + \kappa n't}{5g' - 2g + \kappa n't} \right)$$

where, in the case of 5g'-2g, \varkappa and the corrected integrating factor are determined by

$$\log \mu = 7.2729790n$$
 $\log \mu = 1.5020293$

and, in the case of 10g'-4g, by

$$\log n = 7.54371n$$
 $\log \mu = 1.1992594$

Integrating the last expression we obtain

$$n'\delta z' = \begin{bmatrix} -1132.9347 + 0.285824n't - 0.00049661n'^2t^2 \end{bmatrix} \sin \left(5g' - 2g + \kappa n't \right) \\ + \left[-2677.8791 + 0.591358n't - 0.00043329n'^2t^2 \right] \cos \left(5g' - 2g + \kappa n't \right) \\ + \left[-18.4689 + 0.004811n't - 0.00006067n'^2t^2 \right] \sin \left(10g' - 4g + \kappa n't \right) \\ + \left[19.4491 - 0.010126n't + 0.00009734n'^2t^2 \right] \cos \left(10g' - 4g + \kappa n't \right) \\ + \left[19.4491 - 0.010126n't + 0.00009734n'^2t^2 \right] \cos \left(10g' - 4g + \kappa n't \right) \\ + \left[19.4491 - 0.010126n't + 0.00009734n'^2t^2 \right] \cos \left(10g' - 4g + \kappa n't \right) \\ + \left[19.4491 - 0.010126n't + 0.00009734n'^2t^2 \right] \cos \left(10g' - 4g + \kappa n't \right) \\ + \left[19.4491 - 0.010126n't + 0.00009734n'^2t^2 \right] \cos \left(10g' - 4g + \kappa n't \right) \\ + \left[19.4491 - 0.010126n't + 0.00009734n'^2t^2 \right] \cos \left(10g' - 4g + \kappa n't \right) \\ + \left[19.4491 - 0.010126n't + 0.00009734n'^2t^2 \right] \cos \left(10g' - 4g + \kappa n't \right) \\ + \left[19.4491 - 0.010126n't + 0.00009734n'^2t^2 \right] \cos \left(10g' - 4g + \kappa n't \right) \\ + \left[19.4491 - 0.010126n't + 0.00009734n'^2t^2 \right] \cos \left(10g' - 4g + \kappa n't \right) \\ + \left[19.4491 - 0.010126n't + 0.00009734n'^2t^2 \right] \cos \left(10g' - 4g + \kappa n't \right) \\ + \left[19.4491 - 0.010126n't + 0.00009734n'^2t^2 \right] \cos \left(10g' - 4g + \kappa n't \right) \\ + \left[19.4491 - 0.010126n't + 0.00009734n'^2t^2 \right] \cos \left(10g' - 4g + \kappa n't \right) \\ + \left[19.4491 - 0.010126n't + 0.00009734n'^2t^2 \right] \cos \left(10g' - 4g + \kappa n't \right) \\ + \left[19.4491 - 0.010126n't + 0.00009734n'^2t^2 \right] \cos \left(10g' - 4g + \kappa n't \right) \\ + \left[19.4491 - 0.010126n't + 0.00009734n''^2t^2 \right] \cos \left(10g' - 4g + \kappa n't \right) \\ + \left[19.4491 - 0.010126n't + 0.00009734n''^2t^2 \right] \cos \left(10g' - 4g + \kappa n't \right) \\ + \left[19.4491 - 0.010126n't + 0.00009734n''^2t^2 \right] \cos \left(10g' - 4g + \kappa n't \right) \\ + \left[19.4491 - 0.010126n't + 0.00009734n''^2t^2 \right] \cos \left(10g' - 4g + \kappa n't \right) \\ + \left[19.4491 - 0.010126n't + 0.00009734n''^2t^2 \right] \cos \left(10g' - 4g + \kappa n't \right) \\ + \left[19.4491 - 0.010126n't + 0.00009734n''^2t^2 \right] \cos \left(10g' - 4g + \kappa n't \right) \\ + \left[19.4491 - 0.00009734n'' + 0.00009734n''^2t^2 \right] \cos \left(10g' - 4g + \kappa n't \right) \\ + \left[19.4491 - 0.00009734n'' + 0.00009734n'' + 0.00009734n'' + 0.00009734n'' + 0.00009734n'' + 0.00009734n'' + 0.00009734n'' + 0.00009734n'' + 0.00009734$$

By developing this expression and subtracting therefrom the value of $n'\delta z' + n'\delta^2 z'$ we should have $n'\delta^3 z'$; but as this quantity has no particular interest we omit its derivation, and in the following value of $n'\delta^3 z'$ the terms corresponding to the arguments 5g'-2g and 10g'-4g are not given.

25 AST-29

In writing a final form for the great inequality of Saturn, we prefer to still further equate the motions of the arguments, so that the sum of the squares of the multipliers of n't in the coefficients may be a minimum. This gives, severally, in the cases of 5g'-2g and 10g'-4g

$$\log n = 7.2703565n$$
 $\log n = 7.52728n$

and the final form of $n'\delta z'$ will be

$$n'\delta z' = \begin{bmatrix} 2907.676 & -0.655990n't \end{bmatrix} \sin \left(5g' - 2g + \kappa n't + 247 & 4 & 5.37 \right)$$

$$+ & 0.00065602n'^2t^2 & \sin \left(5g' - 2g + \kappa n't + 221 & 41 & 33 & \right)$$

$$+ \begin{bmatrix} 26.8211 - 0.010659n't \end{bmatrix} \sin \left(10g' - 4g + \kappa n't + 133 & 31 & 9.3 & \right)$$

$$+ & 0.00011466n'^2t^2 & \sin \left(10g' - 4g + \kappa n't + 122 & 38 & \right)$$

The great inequality excepted, the expression of $n'\delta^3z'$ follows. The proper number of decimals is restored to the factors of n't and n'^2t^2 :

Ang-i/g/ Lig	$n'\delta^3z'$				
Arg=i'g'+ig	sin.	cos.			
i' i	11 11 11	и и и			
0 0		+0.00160822 <i>n</i> ′²ℓ²			
		$+0.0000147405n'^3t^3$			
10	—0. $058505n't$ —0. $00043656n'^2t^2$	0. 099694 $n't$ +0. 00062684 n'^2t^2			
	+0.0000001853n ¹³ t ⁸	—0. 0000000286n'3t3			
2 0	0. 0784+0. 001595 $n't$ 0. 00000800 n'^2t^2	$+$ 0. I177 $-$ 0. 000470 $n't$ 0. 00001250 n'^2t^2			
	$+$ 0. 0000001175 n'^3t^3	$+$ 0. 0000000429 $n^{\prime 3}t^{3}$			
3 0	$-0.0012+0.001167n't-0.00000003n'^2t^2$	$+0.0686-0.000200n't+0.00000007n'^2t^2$			
1	+0.0000000090n ¹³ t ³	$+0.0000000010n'^3t^3$			
4 0	-0.0015-0.00012n't	+0.0015 $-$ 0.000075 $n't$			
5 0	o. oo18	0.0008			
-4- I	+0.0005+0.000003n't	+0.0006+0.000005 <i>n't</i>			
—3— І	+0.00110.00005n't	+0.0022 $-$ 0.000002 $n't$			
2 I	-0.0194-0.000027n't	+0.0047—0.000355n't			
—ı— ı	$-0.0164-0.000189n't+0.00000009n'^2t^2$	$+0.0161-0.000319n't-0.00000020n'^2t^2$			
0 1	$-0.0060-0.000234n't+0.00000109n'^2t^2$	$+$ 0.0133 $-$ 0.000226 $n't$ $-$ 0.00000117 n'^2t^2			
I I	$-0.0123-0.000033n't+0.00000107n'^2t^2$	$+0.0305-0.000127n't-0.00000218n'^2t^2$			
2 I	$+0.1806+0.001763n't+0.00003768n'^2t^2$	$+0.2216+0.000346n't+0.00003003n'^2t^2$			
3— І	$+0.6187+0.010777n't+0.00002356n'^2t^2$	+0. 6942—0. 013431 <i>n't</i> —0. 00000408 <i>n'</i> 2 <i>t</i> 2			
4— I	$-0.0042+0.000102n't+0.00000136n'^2t^2$	$+$ 0.0289 $-$ 0.000800 $n't$ $-$ 0.00000181 n'^2t^2			
5 I	$-0.0048+0.000079n't+0.00000012n'^2t^2$	$+0.0012+0.000024n't-0.00000012n'^2t^2$			
6 1	o. 0006+o. 000003n't	+0.0014+0.000006n't			
7— 1	—o. 000 7	0.0031			
—z— 2	-0.0006-0.000006n't	+0.0001—0.000011 <i>n't</i>			
—I— 2	-0.0028+0.000136n't	0.00700.000042n't			
o 2	$-0.0040+0.000056n't+0.00000000n'2t^3$	—0. 0028—0. 000058 $n't$ —0. 0000006 n'^2t^2			
I 2	$-0.0008+0.000028n't$ -0.00000005 n'^2t^2	$-0.0013-0.000066n't+0.00000008n'^2t^2$			
2 — 2	$+0.0081+0.000013n't-0.00000024n'^2t^3$	$-0.0044+0.000020n't-0.00000020n'2t^2$			

Arg=i'g'+ig	$n'\delta^3z'$				
	sin.	cos.			
i' i	<i>II</i>	" " "			
3— 2	$+0.0254+0.000732n^{t}t+0.00001327n^{t2}t^{2}$	0.0290+0.001002 $n't$ 0.00002242 n'^2t^2			
4— 2	0. 1442 0. $027711n't$ +0. $00003043n'^2t^2$	$+0.8245-0.003021n't+0.00033417n'^2t^2$			
6— 2	-1.5236 $-0.009658n't$ $+0.00017413n'^2t^2$	-1. 1283+0. 015360n't+0. 00009056n'2t2			
7 2	$+0.0148-0.000216n't+0.00000767n'^2t^3$	$-0.0113+0.000305n't+0.00000256n'^2t^2$			
8 2	+0.0049	→o. 0017			
— I — 3	o. 0006+-o. 000006n't	0. 00050. 000018n't			
o— 3	+0.0026+0.000027 <i>n't</i>	-0.0013+0.000046n't			
I— 3	+0.0015+0.000040 <i>n't</i>	-0.0031+0.000033n't			
2— 3	$+$ 0.00090.000018 $n't$ +0.00000004 n'^2t^2	$-0.0016+0.000009n't+0.000000000n'^2t^2$			
3— 3	$+$ 0. 0025—0. 000013 $n't$ —0. 00000007 n'^2t^2	$+0.0040+0.000018n't$ 0.00000016 $n'^{2}t^{2}$			
4- 3	$+$ 0.0090 $-$ 0.000020 $n't$ $+$ 0.0000007 $2n'^2t^2$	$+0.0041+0.000006n't+0.00000014n'^2t^2$			
5— 3	0.00320.000029 $n't$ +0.00000233 n'^2t^2	$-0.0020+0.000420n't-0.00000082n'^2t^2$			
6 3	$-0.0010-0.001975n't+0.00000554n'^2t^2$	$-0.0060-0.000598n't-0.00000563n'^2t^2$			
7— 3	$+0.2477+0.016069n't-0.00000173n'^2t^2$	$+0.6988-0.006934n't+0.00000353n'^2t^2$			
8 3	$+0.0609+0.001963n't$ — $0.00000020n'^2t^2$	$+0.0293-0.001976n't+0.00000071n'^2t^2$			
9 3	+0.0001+0.000008n't	-0.0043-0.000004n't			
0 4	0.000002n't	0.000000n't			
1— 4	+0.0010-0.000020 <i>n't</i>	+0.0007+0.000019n't			
2— 4	+0.0009—0.000009 <i>n't</i>	+0.0001+0.000021n't			
3— 4	-0.0007+0.000006n't	+0.0006+0.000009n't			
4 4	—0.0022—0.000002 <i>n't</i> —0.0000003 <i>n'</i> 2 <i>t</i> 2	$+0.0027-0.000005n't+0.00000009n'^2t^2$			
5— 4	$-0.0012-0.000016n't-0.00000010n'^2t^2$	$+0.0053+0.000006n't+0.00000022n'^2t^2$			
6 4	-0.0033-0.000066 $n't$ +0.0000010 n'^2t^2	$-0.0086+0.000074n't+0.00000036n'^2t^2$			
7— 4	$+$ 0.0511 $+$ 0.00065 $8n't+$ 0.0000030 n'^2t^2	$+0.0474-0.001033n't+0.00000017n'^2t^2$			
8 4	$+$ 0. 1371 $+$ 0. 000600 $n't$ $-$ 0. 00000062 n'^2t^2	$+0.0455-0.004154n't-0.00000026n'^2t^2$			
9— 4	$-1.3837+0.011677n't+0.00002373n'^2t^2$	+0. 3398+0. 028248n't-0. 00001286n'2t2			
11 4	$-0.0010+0.001016n't+0.00000007n'^2t^2$	$-0.0031 + 0.000249n't - 0.00000088n'^3t^2$			
2 5	—0. 0003—0. 000006 <i>n't</i>	+0.0003-0.000004n't			
3— 5	0.0000—0.000010 <i>n't</i>	+0.0002+0.000000n't			
4— 5	0,00010,000004n't	+0.0001+0.000000n't			
5— 5	-0.0020-0.000007n't	0.0012+0.000007n't			
6— 5	—0. 0022—0. 000003n't	0.0000—0.000005n't			
7— 5	-0.0013+0.000022n't	+0.0017—0.000009n't			
8— 5	-0. 0102+0. 000387n't	+0.0149+0.000158n't			
9 5	o. 0003+o. 000404 <i>n't</i>	+0.0173—0.000038n't			
10 5	+0.0103+0.000319n't	+0.01900.000223n't			
11— 5	$-0.0229+0.000433n't-0.00000006n'^2t^2$	$+0.0198-0.000758n't-0.00000001n'^3t^3$			
12— 5	+0.0919—0.000242 <i>n't</i>	—o. 1255+o. 000927 <i>n't</i>			
3 6	-0.0002+0.000002 <i>n</i> ′ <i>t</i>	0, 00010, 000002n't			
4— 6	-0.0002+0.000000n't	+0.0001-0.000004n't			
5— 6	0.000000 <i>n't</i>	-0.00002n't			
6 6	+0.0002	—o. 0007			
7— 6	_o.0003	_o. ooo8			
8 6	-0,0010+0.000001 <i>n't</i>	_0.0009+0.000004n't			
9— 6	—0, 0071—0. 000036 <i>n't</i>	-0.0037+0.000158n't			

A //-/-	$n'\delta^3z'$				
Arg=i'g'+ig	sin.	cos.			
i' i	11 11 11	и и и			
10 6	-0.0043+0.000035n't	-0.0002+0.000082n't			
11— 6	+0.0020+0.000038n't	-0.0010+0.000031n't			
12— 6	+0.0007+0.000021n't	o. 0038+0. 000007n't			
5— 7	+0.000008n't	0.000002n't			
7— 7	+0.0003	0.0000			
8 7	+0.0004	o. 000I			
9 7	0. 0009+0. 000000n't	+0.0001+0.000007n't			
10 7	+0.0003-0.000085n't	-0.0026+0.000000n't			
11 7	-0.0009-0.000055n't	-0.0022+0.000030n't			
12 7	+0.0004 $-$ 0.000015 $n't$	+0.0002+0.000024n't			
10— 8	+0.000001n't	0. 000003n't			
11— 8	o. 000008n't	o. 000035n't			
12— 8	0.00001 <i>9n't</i>	0.000019n't			
12— 9	+0.000007n't	-0.00003n't			

As in the case of Jupiter, for the general value of $\delta^2 \nu'$, we employ the formula

$$\delta^2\nu' = -\,\frac{\mathrm{i}}{2}\!\int\!\Big(\frac{\overline{d\,\cdot\,\delta^2\mathrm{W_0}'}}{d\gamma'}\Big)n'dt$$

But in the terms which involve the argument 5g'-2g it has been discovered that the complementary portion of the right member has a sensible value. Consequently, for this argument we make use of the complete formula

$$\frac{d\cdot\delta^2\nu'}{n'dt} = -\frac{\mathrm{I}}{2}\bigg(\frac{\overline{d\cdot\delta^2\mathrm{W_0}'}}{d\gamma'}\bigg) - \frac{\mathrm{I}}{2}\bigg(\frac{\overline{d^2\mathrm{W_0}'}}{d\gamma'^2}\bigg)n'\delta^2z' - \frac{\mathrm{I}}{2}\bigg(\frac{\overline{d^2\cdot\delta\,\mathrm{W_0}'}}{d\gamma'^2}\bigg)n'\delta z' - \frac{\mathrm{I}}{4}\bigg(\frac{\overline{d^3\mathrm{W_0}'}}{d\gamma'^3}\bigg)(n'\delta^2z')^2$$

The expressions for the factors involved in the right member have all been given, except those for $-\frac{1}{2}\left(\frac{\overline{d^2\delta W_0}'}{d\gamma'^2}\right)$ and $-\frac{1}{4}\left(\frac{\overline{d^3W_0}'}{d\gamma'^3}\right)$. To a sufficient number of terms for our purpose the latter are:

Arg=i'g'+ig		$-rac{1}{2}(rac{ar{d}^2\delta \overline{W_0}'}{d\gamma'^2})$					
	cos.	sin.	n't cos.	n't sin.	$n^{\prime 2}t^{2}\cos$.	$n'^2t^2\sin$.	
i' i o o o i o o o o o o o o o o o o o o	-0. 4057 +0. 1443 -1. 6441	+0. 2489 —2. 8744	8.52 73.09 11.09	+91.21 + 2.00	—1268. 72 — 142. 12	—976. 23 —109. 38	
3 0 2 I I I 0 I I I	-0. 1175 +1. 2195 +1. 0988 +0. 9288 +0. 4011	-2. 5142 +0. 3504 +0. 9397 +1. 0075 +0. 4819	- 0.90 + 0.97 + 12.29 +151.54 + 33.83	— 1. 19 — 0. 48 — 4. 89 — 54. 69 + 23. 51	— 13.41 1	— 10. 35	

Arg=i'g'+ig	$-rac{\mathrm{i}}{2} \Big(rac{ar{d}^2ar{d} \overline{\mathrm{W}_0}}{ar{d} \gamma'^2}\Big)$					
	cos.	sin.	n't cos.	$n't \sin$.	$n'^2t^2\cos$.	n'^2t^2 sin.
i' i 2— I 3— I 4— I	+0.1176 +2.9733 +3.5992	" 0. 1709 1. 5995 0. 3508	" + 229.69 + 8.70 - 4.62	+306.74 + 61.11 + 5.87	"	"
I— 2 2— 2 3— 2 4— 2 5— 2 6— 2	+0. 5144 +0. 1096 -0. 5676 -3. 4317 -0. 1017 -0. 1658	- 0. 2865 - 0. 2139 - 1. 1824 -13. 7965 + 0. 0055 - 0. 0129	- 35.67 + 4.26 + 121.88 +3887.57 + 24.30	- 33.89 + 26.58 + 181.27 - 13.04 + 12.76		
6— 3 7— 3 8— 3	+2. 4988 +0. 1794 -0. 0064	+ 1.6449 + 1.5819 + 0.1474	- 3.57 - 51.87 + 12.32 + 0.59	+ 13.95 + 60.34 - 4.38 - 0.08		
7— 4 8— 4 9— 4 10— 4	—1. 9564 —1. 2025 +5. 7067 +0. 0459	+ 1.8079 + 0.6377 + 1.6780 + 0.0441	+ 12.64 + 2.38 + 9.68 + 0.18	+ 16.79 + 6.90 - 23.94 - 0.16		

Arg=i'g'+ig	$-rac{\mathrm{I}}{4}\Big(rac{d^3\overline{\mathrm{W}_0'}}{d\gamma'^s}\Big)$			
	sin.	cos.		
i' i 1 0	— 18.06 +16531 n't	5. 29 +26479 n't		
2 0	- 2.85 $+$ 3703 $n't$	- 0.83 + 5933 n't		
I— I	18. 77	— 128.95		
2— 1	+ 21.54	— 35. o5		
3— 1	+ 1.32	<u> </u>		
I— 2	+ 8.23	— 8.32		
2 2	+ 43.78	— 19. 21		
3— 2	+ 12.44	+ 12.83		
4 2	— 18. 70	— 152.23		
5— 2	+ 0.42	+ 0.83		

The multiplication being performed we get

$$-\frac{1}{2} \left(\frac{\overline{d^2 W_0'}}{\overline{d \gamma'^2}} \right) n' \delta^2 z' = \begin{bmatrix} -0.14019 - 62.646n't + 4.472n'^2t^2 \end{bmatrix} \sin (5g' - 2g) \\ + [-0.33710 + 36.383n't + 6.296n'^2t^2] \cos (5g' - 2g) \\ -\frac{1}{2} \left(\frac{\overline{d^2 \delta W_0'}}{\overline{d \gamma'^2}} \right) n' \delta z' = \begin{bmatrix} -0.00524 + 3.983n't - 5.024n'^2t^2 \end{bmatrix} \sin (5g' - 2g) \\ + [-0.00824 - 0.989n't - 7.943n'^2t^2] \cos (5g' - 2g) \\ -\frac{1}{4} \left(\frac{\overline{d^3 W_0'}}{\overline{d \gamma'^3}} \right) (n' \delta z')^2 = \begin{bmatrix} -0.00277 - 0.189n't + 1.040n'^2t^2 \end{bmatrix} \sin (5g' - 2g) \\ + [-0.00560 - 0.075n't + 2.563n'^2t^2] \cos (5g' - 2g) \end{bmatrix}$$

If we add these three quantities to the corresponding terms of $-\frac{1}{2}\left(\frac{\overline{d \cdot \delta^2 W_0'}}{\overline{d \gamma'}}\right)$ and $\frac{d \cdot \delta \nu'}{n'dt}$ and $\frac{d \nu'}{n'dt}$ we get

$$\frac{d\nu'}{n'dt} = \begin{bmatrix} \frac{1}{100} & \frac{1}{100} & \frac{1}{100} \\ -\frac{1}{100} & \frac{1}{100} & \frac{1}{100} & \frac{1}{100} \\ -\frac{1}{100} & \frac{1}{100} & \frac{1}{100} & \frac{1}{100} & \frac{1}{100} & \frac{1}{100} \\ -\frac{1}{100} & \frac{1}{100} & \frac{1}{100} & \frac{1}{100} & \frac{1}{100} & \frac{1}{100} & \frac{1}{100} & \frac{1}{100} \\ -\frac{1}{100} & \frac{1}{100} & \frac{1}{100} & \frac{1}{100} & \frac{1}{100} & \frac{1}{100} & \frac{1}{100} & \frac{1}{100} & \frac{1}{100} \\ -\frac{1}{100} & \frac{1}{1$$

This expression may be changed to

$$\frac{d\nu'}{n'dt} = \begin{bmatrix} -0.76561 + 0.0001408n't - 0.000000293n'^2t^2 \end{bmatrix} \sin(5g' - 2g + \kappa n't) + [-1.51056 + 0.0002776n't - 0.000000117n'^2t^2] \cos(5g' - 2g + \kappa n't)$$

where the proper number of decimals has been restored to the coefficients of n't and n'^2t^2 . The value of n' and the corrected integrating factor are given by the equations

$$\log \mu = 7.32699$$
 $\log \mu = 1.5054687$

On integrating the last expression we obtain

$$v' = \begin{bmatrix} v' & v' & v' \\ 24.7830 - 0.004750n't + 0.00000938n'^2t^2 \end{bmatrix} \cos(5g' - 2g + \kappa n't) + [-48.2213 + 0.008288n't - 0.0000375n'^2t^2] \sin(5g' - 2g + \kappa n't)$$

In order to put this in a final form we equate the argument still further, so that the sum of the squares of the coefficients of n't may be a minimum. This makes $\log n = 7.32535$, and we have the following expression

$$\nu' = \begin{bmatrix} 54.2171 - 0.009543n't \end{bmatrix} \quad \cos(5g' - 2g + \mu n't + 62 \ 47 \ 58.0)$$

$$+ 0.00001005n'^2t^2 \cos(5g' - 2g + \mu n't + 22 \ 9 \)$$

Omitting, then, the terms corresponding to the argument 5g'-2g the expression for $\delta^2\nu'$ follows. The proper number of decimals are restored to the coefficients of n't and n'^2t^2 :

, ,,,	$\delta^2 v'$				
Arg=i'g'+ig	cos.	sin.			
∮′ ∳ O O	+0.000821 $n't$ +0.00000613 n'^2t^2 -0.000000026 n'^3t^3	11 11 11			
1 0	$+0.2151+0.030390n't+0.00021469n'^{2}t^{2}$ $-0.000000925n'^{3}t^{3}$	—о. 1536—о. 050455n't+о. 00031064n' ² t ³ —и. 000000206n' ³ t ³			
2 0	$+$ 0. 0226 $-$ 0. 001156 $n't$ $+$ 0. 00000615 n'^2t^3 $-$ 0. 000000025 n'^3t^3	$+$ 0. 0806—0. 000731 $n't$ +0. 00000880 n'^2t^3 —0. 000000005 n'^3t^3			
3 0	o. 0018o. 001467n't	+0.0868—0.000267n't			
4 0	-0.0063-0.000020n't	+0.0035—0.000035n't			
3 I	o. 0005o. 000016n't	o. 0009+0. 000000n't			
2 I	-0.0272-0.000047n't	-0.0062+0.000473 <i>n</i> ′ <i>t</i>			
_I —I—	—0. 0195—0. 000224 $n't$ —0. 00000006 n'^2t^2	$-0.0164+0.000396n't+0.00000000n'^2t^2$			
0— I	-0.0085 - $-0.000290n't+0.00000072n'^2t^2$	$-0.0185 + 0.000242n't + 0.00000121n'2t^2$			
1-1	$+0.0069+0.000023n't+0.00000088n'^2t^2$	$-0.0624+0.000072n't-0.00000106n'^2t^2$			
2— I	$+0.1374+0.000397n't+0.00001749n'^2t^2$	-0. 1225+0. 000515 $n't$ -0. 00001312 $n'^2t'^2$			
3— 1	0. 34530. $003744n't$ 0. $00000706n'^2t^9$	$+0.2715-0.007283n't+0.00000048n'^2t^2$			
4— I	$-0.0763+0.000288n't-0.0000032n'^2t^2$	$+0.0138-0.001603n't-0.00000020n'^2t^3$			
5— I	+0.0052-0.000076n't	+0.0079+0.000040n't			
6— г	+0.0020—0.000003 <i>n't</i>	+0.0057+0.000006n't			
_2 2	—0. 0006—0. 000006 <i>n't</i>	-0.0001+0.000011n't			
I 2	-0.0049+0.000183n't	+0.0096+0.000059n't			
0— 2	-0.0081 + 0.000117n't	+0.0064+0.000113n't			
I— 2	$-0.0030+0.000040n't-0.00000018n'^2t^2$	$+0.0008+0.000091n't+0.00000003n'^2t^2$			
2 2	$+0.0212-0.000020n't+0.00000051n'^2t^2$	$+0.0101+0.000010n't-0.00000010n'^2t^2$			
3 2	$+0.0315-0.000351n't+0.00000275n'^2t^2$	$+0.0351-0.000051n't-0.00000198n'2t^2$			
4- 2	$-0.0825-0.016726n't+0.00001599n'^2t^2$	$-0.4821 + 0.002358n't - 0.00023345n'2t^2$			
6 2	$+0.7667+0.001759n't-0.00000421n'^2t^2$	$-0.5655 + 0.003342n't + 0.00000173n'^2t^3$			
7— 2	+0.0093+0.000064n't	-0.0162+0.000089n't			
-ı- 3	-0.0001 + 0.000008n't	+0.0002+0.000012n't			
u 3	+0.0038+0.000040 <i>n't</i>	+0.0028-0.000068n't			
ı— 3	+0.0020+0.000064 <i>n</i> ′ <i>t</i>	+0.0042-0.000045n't			
z— 3	+0.0005+0.000033n't	-0.0024+0.000009 <i>n't</i>			
3-3	$+0.0070+0.000007n't+0.00000007n'^2t^2$	$-0.0088+0.000000n't+0.00000000n'^2t^3$			
4 3	$+0.0151-0.000020n't+0.00000099n'^2t^2$	0.00720.000014 $n't$ 0.0000020 n'^2t^2			
5— 3	$-0.0008+0.000016n't+0.00000229n'^2t^2$	-0.0025 $-0.000416n't$ $+0.00000069n'^{2}t^{2}$			
6— 3	0. 0629+0. 000755 $n't$ +0. 00000337 n'^2t^2	—0. 0610—0. 001009 $n't$ +0. 00000352 n'^2t^2			
7— 3	$+0.0036+0.008112n't-0.00000013n'^2t^2$	$-0.3111+0.000740n't+0.00000031n'2t^2$			
8— 3	$-0.0105-0.001074n't+0.00000022n'^9t^9$	$+0.0511-0.000496n't-0.00000036n'^2t^2$			
9— 3	o, 0043o. 000045 <i>n't</i>	+0.0054—0.000032n't			
I 4	+0.0019—0.000031n't	0, 00130, 000031n't			
2 4	+0.0020—0.000015n't	0. 00040. 000033n't			
3— 4	+0.0001+0.000003n't	—0. 000I—0. 000020 <i>n't</i>			

Arg=i'g'+ig	8211				
	cos.	sin.			
i' i	и и и	и и и			
4— 4	$-0.0037+0.000002n't+0.00000000n'^2t^2$	$0.0046-0.000002n't-0.00000002n'^2t^2$			
5— 4	$-0.0016+0.000002n't-0.00000004n'^2t'^2$	$-0.0073-0.000010n't-0.00000030n'^2t'^2$			
6 4	$+0.0005+0.000112n't+0.00000015n'^2t^2$	$-0.0163+0.000048n't-0.00000036n'^2t^2$			
7— 4	$+0.0658+0.001023n't+0.00000027n'^2t^2$	0.0648+0.001455 $n't$ 0.00000020 n'^2t^2			
8— 4	$+0.0745+0.000559n't-0.00000046n'^2t^2$	$-0.0300+0.002022n't+0.00000020n'^2t^2$			
9 4	$-0.9570+0.008390n't+0.00001059n'^2t^2$	0. 23240. 019956 $n't$ +0. 00000583 n'^2t^2			
10 4	0. 20340. 003793 $n't$ 0. 00000160 n'^2t^2	$-0.2273+0.002651n't-0.00000298n'^2t^9$			
2 5	0.00040.000015n't	o. 0007+0. 000010n't			
3 5	0.0000—0.000020 <i>n't</i>	—0. 0008+0. 000002n't			
4— 5	+0.0001-0.000007n't	-0,0004-0.000002 <i>n't</i>			
5— 5	o. 0026o. 000003n't	+0.0013-0.000003n't			
6— 5	—o. oo33	0.0000			
7 5	—0. 0026+0. 000035n't	0.00200.00001 <i>3n't</i>			
8— 5	-0.0158+0.000518n't	0.02540.000242n't			
9— 5	-0.0030+0.000556n't	-0.0211+0.000050n't			
10— 5	+0.0091+0.000368n't	-0. 0228+0. 000261 <i>n't</i>			
11 5	+0.0207+0.000310n't	-0.0226+0.000554n't			
12- 5	+0,0631-0.000058n't	+0.03190.000180n't			
3 6	-0.0003+0.000002 <i>n't</i>	+0.0001+0.000006n't			
4 6	-0.0004+0.000000n't	-0.0001 + 0.000008n't			
6 6	+0.0002	+0.0008			
7 6	0.0001	+0.0010			
8— 6	0.0009+0.000001n't	+0.0004-0.000013n't			
9— 6	o. 0090o. 000037n't	+0.0036—0.000210n't			
10 6	0. 0069 + 0. 000047n't	0.00020.000161 <i>n't</i>			
11 6	-0.0008+0.000059n't	+0.0008—0.000062n't			
12 6	+0.0048+0.000041n't	+0.0134-0.000010n't			
5 7	+0.000004n't	+0.000001n't			
7— 7	- - 0.0005	0. 0000			
8 7	+0.0005	+0.0002			
9— 7	0.00040.000005 <i>n't</i>	+0.00010.000006n't			
10— 7	+0.0004-0.000092n't	+0.0038-0.000003n't			
11 7	—0. 0011—0. 000069 <i>n't</i>	+0.0031—0.000038n't			
12— 7	0, 00040. 000022n't	+0.0004—0.000035n't			
10 8	0.00002 $n't$	0.00000n't			
11 8	0.000010 <i>n't</i>	+0.000047n't			
12— 8	0.00C024n't	+0.000029n't			
12— 9	-0,000013n't	+0.000007#'t			

CHAPTER XXI.

PERTURBATIONS OF SATURN OF THE SECOND ORDER FROM THE ACTION OF URANUS AND FACTORED BY n't.

Having now pushed the approximation to the perturbations of the longitudes and radii-vectors of Jupiter and Saturn, so far as these arise from their mutual action, to a sufficient length, it remains to consider certain terms of the second order, with respect to disturbing forces, which involve the mass of Uranus as a factor.

In the first place the perturbations of Saturn, due to the action of Uranus, which have been determined in Chapter III, are of the first order with respect to the disturbing force. The elements of both planets have been regarded as constant. In this chapter, then, we determine the additional terms which arise in the perturbations from attributing to these elements their augmentations proportional to the time. Here it will be sufficiently accurate to neglect the variations of the elements which determine the position of the planes of the orbits relative to each other. Also the effect on the latitude of Saturn may be neglected.

The more important part of the terms we wish to derive arises from the variation of the function T' (denoted as T at page 130; but here we propose to give one accent to quantities belonging to Saturn and two to those belonging to Uranus). To find the variation of T' we therefore employ the abbreviated formula

$$\delta\mathbf{T}' = \frac{d\mathbf{T}'}{dg'}n'\delta z' + \frac{d\mathbf{T}'}{dg''}n''\delta z'' + r'\frac{d\mathbf{T}'}{dr'}\nu' + r''\frac{d\mathbf{T}'}{dr''}\nu'' + \mathbf{C}'\delta\frac{h'}{h_0'}$$

in which the latter factors of the five terms may be limited to their secular terms. By joining together the terms of one, two, and three dimensions, obtained in the preceding chapters, we have for Saturn

$$\begin{split} n'\delta z' &= -\left[0.82487\right] n't \sin \ \ g' - \left[1.02971\right] n't \cos \ \ g' \\ &- \left[8.97104\right] n't \sin \ 2g' - \left[9.17599\right] n't \cos \ 2g' \\ &- \left[7.4183\right] n't \sin \ 3g' - \left[7.6233\right] n't \cos \ 3g' \\ v' &= \left[8.97195\right] n't \\ &+ \left[0.52384\right] n't \cos \ \ g' - \left[0.72868\right] n't \sin \ \ g' \\ &+ \left[8.97104\right] n't \cos \ 2g' - \left[9.17599\right] n't \sin \ 2g' \\ &+ \left[7.5944\right] n't \cos \ 3g' - \left[7.7994\right] n't \sin \ 3g' \\ \delta \frac{h'}{h_{\bullet}'} &= -\left[9.2730\right] n't \end{split}$$

The corresponding quantities for Uranus must be derived from the theory of this planet. Availing ourselves of Professor Newcomb's determinations,* the unit of t being a Julian year, we have

$$\frac{de^{\prime\prime}}{dt} = -\circ^{\prime\prime}.\circ_{5420} \qquad \qquad \frac{d\pi^{\prime\prime}}{dt} = +2^{\prime\prime}.846$$

These data give

$$n''\delta z'' = - [9.70665]n't \sin g'' - [0.09803]n't \cos g''$$

$$- [7.7756]n't \sin 2g'' - [8.1671]n't \cos 2g''$$

$$- [6.1456]n't \sin 3g'' - [6.5370]n't \cos 3g''$$

$$v'' = [7.7764]n't$$

$$+ [9.40562]n't \cos g'' - [9.79700]n't \sin g''$$

$$+ [7.7756]n't \cos 2g'' - [8.1671]n't \sin 2g''$$

$$+ [6.3217]n't \cos 3g'' - [6.7131]n't \sin 3g''$$

The expressions for the factors $\frac{d\mathbf{T}'}{dg'}$ and $\frac{d\mathbf{T}'}{dg''}$ are readily derived by partial differentiation of the value of \mathbf{T}' , given in Chapter III (pages 130–133). It only remains to show how $r'\frac{d\mathbf{T}'}{dr'}$ and $r''\frac{d\mathbf{T}'}{dr''}$ are obtained. We have the formulæ

$$r' \frac{d\mathbf{T}'}{dx'} = \mathbf{V}' + \mathbf{X}'$$
 $r'' \frac{d\mathbf{T}'}{dx''} = -\mathbf{V}' - \mathbf{T}'$

where

$$\begin{split} & \mathbf{V}' = \mathbf{A}' \frac{d}{dg'} \bigg(a'r' \frac{d\Omega'}{dr'} \bigg) + \mathbf{B}'r' \frac{d}{dr'} \bigg(a'r' \frac{d\Omega'}{dr'} \bigg) \\ & \mathbf{X}' = \mathbf{M}' a' \frac{d\Omega'}{dg'} + \mathbf{N}' ar' \frac{d\Omega'}{dr'} \end{split}$$

The values of the factors involved in the right members of these equations have all been given, excepting that of $\left(r'\frac{d}{dr'}\right)^2 a'\Omega'$, A' and B' at page 74, M' and N' at page 212, $a'\frac{d\Omega'}{dg'}$ and $a'r'\frac{d\Omega'}{dr'}$ at pages 128–130. For the single remaining factor we have the equation

$$\left(r'\frac{d}{dr'}\right)^{2}\alpha'\Omega' = \frac{3}{4}\mu\left(\frac{\mathbf{a}''}{\triangle}\right)^{5}\left[\frac{r''^{2}}{\mathbf{a}''^{2}} - \alpha^{2}\frac{r'^{2}}{\mathbf{a}'^{2}}\right]^{2} - \mu\left(\frac{\mathbf{a}''}{\triangle}\right)^{3}\left(\frac{r''}{\mathbf{a}''}\right)^{2} + \frac{1}{4}\mu\frac{\mathbf{a}''}{\triangle} - (\mathbf{H})$$

The expressions for $\frac{a''}{\triangle}$, $\left(\frac{a''}{\triangle}\right)^3$, $\left(\frac{a''}{\triangle}\right)^5$, $\frac{r''^2}{a''^2}$, $a^2\frac{r'^2}{a'^2}$, and (H) have been given in Chapter III. We also readily get

$$\frac{3}{4} \left[\frac{r''^2}{a''^2} - \alpha^2 \frac{r'^2}{a'^2} \right]^2 = [9.6346] - 2[8.7253] \cos g'' + 2[7.0120] \cos 2g'' + 2[8.1956] \cos g' + 2[6.5608] \cos 2g' - 2[6.9890] \cos (g'' - g') - 2[6.9890] \cos (g'' + g')$$

^{*}An Investigation of the Orbit of Uranus, pp. 80, 81. The only alteration made is the putting the mass of Neptune at $_{17}$ $|_{00}$ 0 instead of $_{17}$ $|_{00}$ 0.

Making the single multiplication required and availing ourselves of all the data afforded in Chapter III we obtain the following expression:

$\mathbf{A}^{rg} = \mathbf{i}'g'' + ig'$	$\frac{1}{\mu} \left(r' \frac{d}{dr}\right)$	$a'\Omega'$		$\frac{1}{\mu} \left(r' \frac{d}{dr}\right)$	a' a' Ω'	$ \text{Arg} = \\ i'g'' + ig' $	$\frac{1}{\mu} \left(r' \frac{d}{dr'} \right)$	$a'\Omega'$
	cos.	sin.		cos.	sin.		cos.	sin.
i' i o o o o - I o - 2 I+ I I o I - I I - 2 I - 3 2+ I 2 o 0 2- I 2- 2 2- 3 2- 4 3 o 3- I	0. 47140. 0793 0. 00000. 0067 +-0. 0725 +-0. 13550. 01240. 00010. 0009 +-0. 24661. 11230. 01050. 00060. 0022 +-0. 0290	-0. 0495 +0. 0016 -0. 0022 +0. 1167 -0. 6836 +0. 0391 +0. 0007 -0. 0117 -0. 0170 -0. 4730 -0. 0325 -0. 0014 -0. 0004 +0. 0287	i' i 3— 4 3— 5 4— I 4— 2 4— 3 4— 4 4— 5 4— 6 5— 2 5— 3 5— 4 5— 5 5— 6 5— 7 6— 2 6— 3 6— 4	-0. 0597 -0. 0037 -0. 0001 +0. 0374 -0. 3184 +0. 4737 +0. 0112 -0. 0004 +0. 0081 -0. 0464 -0. 0233 +0. 3947 +0. 0592 +0. 0048 +0. 0006 -0. 0513	+0. 0193 +0. 0005 +0. 0057 -0. 0422 +0. 0194 +0. 5111 +0. 0667 +0. 0050 +0. 2743 -0. 2305 +0. 0007 +0. 0016 +0. 0009 -0. 0106 +0. 0416	i' i 6-7 6-8 7-3 7-4 7-5 7-6 7-7 7-8 8-4 8-5 8-6 8-7 8-8 8-9 9-5 9-6 9-7 9-8	+0.0095 +0.0025 +0.0012 -0.0123 +0.0302 +0.0661 -0.1677 -0.0301 -0.0013 -0.0029 +0.0447 -0.0866 -0.0161 -0.0133 -0.0018 +0.0111 -0.0074 -0.0579	-0. 0450 -0. 0041 -0. 0010 -0. 0014 +0. 0503 -0. 1414 +0. 0119 -0. 0133 -0. 0017 +0. 0119 -0. 0183 -0. 0627 +0. 0945 +0. 0182 +0. 0012 +0. 0044 -0. 0387 +0. 0487
3— 2 3— 3	—0. 0549 —0. 5614	0. 3160 +0. 8016	6— 5 6— 6	+0. 2083 0. 0844	+0. 0538 -0. 2700	9— 9 9—10	+0.0523 +0.0187	+0. 0295 +0. 0055

Thence we obtain the expression for V':

	7	7'		V'	
$Arg = \kappa \gamma' + i'g'' + ig'$	sin.	cos.	$Arg = \varkappa \gamma' + i'g'' + ig'$	ein.	cos.
ж i' i г о— г — г о о о о— г	 4. 568 0. 489 0. 346	0. 006 +0. 353 0. 167	ж i' i —I I о о і— I I І— 2	" +1.020 -0.522 -0.325	+5. 125 -2. 706 -1. 500
I 0— 2 —I 0— I 0 0— 2 I 0— 3	+0.028 +0.003 +0.003 +0.001	-0. 131 0. 010 +0. 001 +0. 002	-I I-I 0 I-2 I I-3 -I I-2	0. 014 0. 077 +0. 099 0. 003	-0. 428 +0. 306 -0. 081 -0. 002
-I I+ 2 0 I+ I I I 0 -I I+ I 0 I 0	-0.005 -0.025 +0.040 +0.377 0.000	0. 005 +0. 006 +0. 001 0. 452 0. 000	0 I - 3 I I - 4 -I 2 + 2 0 2 + I I 2 0	0.004 +0.005 0.000 0.000 +0.001	+0. 012 -0. 007 0. 000 +0. 001 -0. 002
I I I	o. 396	+0. 350	-I 2+ I	-0.008	—o. o53

$Arg = \varkappa \gamma' + i'g'' + ig'$	V		$Arg = \kappa \gamma' + i'g'' + ig'$		∇′
Alg—ny +vy +vy	sin.	cos.		sin.	cos.
н i' i 0 2 0	0,000	0.000	π i' i —I 4— 5	-0.011	,, —0. 052
1 2 I	- 0.044	+ 0.059	0 4 6	-0.004	+0. 107
—ı 2 0	+ 1.768	+ 0.131	I 4— 7	+0.003	0. 045
0 2— 1	— I. 247	+ 0.085	5—_ 1	+0.063	±0.018
I 2— 2	+ o. 370	0.456	i .		+0.018
I 2 I	13.875	+ 5.936	1 1	-0.051	0. 019 0. 009
0 2- 2	+12.592	5.402		+0.025	
I 2 3	— 2. 968	+ 1.255	1	-0. 589	+0. 383
—I 2— 2	+ 0.049	+ 0.430	0 5-3	+0.540	-o. 334
0 2— 3	+ 0.504	— o. 686	I 5 4	—o. 136	+0. 187
I 2-4	o. 251	+ o. 282	—I 5— 3	+0.061	—3. 482
—I 2— 3	0.001	+ 0.011	0 5— 4	-0.077	+3. 282
0 2— 4	+ 0.031	o. o48	I 5 5	0. 138	—I. 025
I 2 5	— 0.016	+ 0.024	—I 5— 4	+5.517	+3. 248
—ı 3+ ı	0.006	- o. ooi	0 5-5	—5 ⋅ 356	-3.001
0 3 0	0.000	0.000	1 5— 6	+1.597	+o. 88o
1 3—1	0.000	+ 0.008	—I 5— 5	+0.747	-0.072
· ·	1	o. 163	0 5—6	0. 977	0. 059
—i 3 o	+ 0. 225	_	1 5-7	+0.354	+0.041
0 3- 1	- 0. 154	+ 0.130	—ı 5— 6	+0.053	-o. o 25
I 3— 2	+ 0.014	0.120	o 5— 7	 0. 102	+0.021
—I 3— I	- 1.060	+ 3. 187	ī 5— 8	+0.044	0, 006
0 3-2 1 3-3	+ 0. 966 + 0. 029	- 2.761 + 0.877	_ı 6_ı	+0.007	0.003
1		—10.661	0 6— 2	-0.006	+0.002
ľ	- 7.465		1 6-3	+0.002	-0.002
1	+ 7.097	+ 9.956	—ı 6— 2	-0.024	+0. 100
1 '	- 1.938 - 0.739	- 2.719 - 0.087	0 6— 3	+0.025	0. 089
1	+ 1.048	+ 0.522	I 6-4	+0.008	+0.04 1
0 3— 4 1 3— 5	— 0. 392	- 0. 322 0. 239	—ı 6— 3	—o. 501	—o. 581
-I 3-4	- 0. 036	+ 0.002	0 6-4	+0.456	+0.548
0 3-5	+ 0.088	+ 0.026	ı 6— 5	-0. 207	o. 135
I 3—6	- 0.040	— 0.012	—ı 6— 4	+2.785	-0. 46 7
	}		0 6-5	-2.658	+0.444
—ı 4 o	+ 0.009	— o. o33	ı 6— 6	+0.822	-0. 243
0 4 I	— o. oo6	+ 0.022	—ı 6— 5	—I. 220	+3.831
I 4— 2	— o. o1o	- 0.011	0 6 6	+1.070	-3.719
-1 4- I	+ 0. 238	+ 0.456	ı 6— 7	—o. 311	+1.126
0 4— 2	- 0.192	— o. 393	_1 6_ 6	+0.160	+o. 576
1 4-3	+ 0. 149	+ 0.092	0 6-7	o. II3	-o. 7 35
—I 4— 2	- 3.721	— o. 695	ı 6 8	+0.029	+0. 264
0 4— 3	+ 3.417	+ 0.678	—ı 6— 7	+0.033	+0.046
I 4— 4	- 1.079 + 6.514	+ 0.027 - 7.007	0 6-8	o. o38	o. o81
-I 4-3 0 4-4	- 6. 107	+ 6.766	ı 6— 9	+0.013	+0.034
1 4-5	+ 1.757	— 1.961		10.013	7-5, 534
4 4	+ 0.039	- o. 830	—I 7— 2	+0.006	+0.012
0 4-5	— o. 306	+ 1.122	0 7-3	0. 005	0. 011
1 4 6	+ 0. 144	— o. 410	1 7— 4	+0,005	+0.003

$Arg = \kappa \gamma' + i'g'' + ig'$			7'	A	1 1 2/ 2// 1 2 2/	,	γ′
	T • 9 T • 9	sin.	cos.	Arg=κγ	'+i'g''+ig'	sin.	cos.
	i' - i - 3 - 4 - 7 - 5 - 7 - 4 - 7 - 5 - 7 - 6 - 7 - 7 - 6 - 7 - 7 - 8 - 7 - 8 - 7 - 8 - 3 - 4 - 5 - 8 - 5 - 6 - 5 - 6 - 5 - 6 - 5 - 6 - 7 - 7 - 8 - 3 - 4 - 5 - 6 - 5 - 6 - 5 - 6 - 7 - 7 - 8 - 7 - 9 - 8 - 5 - 6 - 5 - 6 - 5 - 6 - 7 - 7 - 8 - 7 - 9 - 8 - 5 - 6 - 8 - 7 - 7 - 8 - 7 - 9 - 9 - 9 - 9 - 9 - 9 - 9 - 9 - 9	-0. 132 +0. 119 -0. 046 +0. 465 -0. 447 +0. 108 +0. 743 -0. 721 +0. 291 -2. 405 +2. 323 -0. 706 -0. 389 +0. 491 -0. 180 -0. 016 +0. 015 -0. 004 -0. 002 -0. 002 -0. 002 -0. 015 +0. 535 -0. 507 +0. 188	-0. 017 +0. 019 +0. 011 -0. 554 +0. 518 -0. 207 +1. 964 -1. 886 +0. 567 -0. 188 +0. 098 -0. 019 +0. 186 -0. 191 +0. 063 +0. 011 -0. 009 +0. 006 -0. 140 +0. 132 -0. 045 +0. 307 -0. 299 +0. 066	1 I O I I O I I O I I O I I O I O	i' i 8— 8 8— 7 8— 8 8— 9 8— 8 8— 9 8— 10 9— 4 9— 5 9— 6 9— 7 9— 6 9— 7 9— 8 9— 7 9— 8 9— 9 9— 10 9— 9	-0. 357 -0. 221 +0. 273 -0. 091 -0. 186 +0. 198 -0. 068 -0. 015 +0. 014 -0. 008 +0. 138 -0. 127 +0. 039 -0. 158 +0. 157 -0. 031 -0. 711 +0. 669 -0. 203 +0. 736 -0. 679 +0. 190 +0. 169	+0. 280 -1. 375 +1. 318 -0. 403 -0. 236 +0. 293 -0. 106 -0. 018 +0. 017 -0. 003 -0. 024 +0. 019 -0. 018 +0. 471 -0. 441 +0. 144 -0. 707 +0. 668 -0. 191 -0. 348 +0. 336 -0. 070 -0. 125
-ı	8— 6 8— 7	—1. 241 +1. 191	+0. 783 -0. 767	0	9—11	—0. 155 +0. 011	+0. 165 —0. 082

In the next place we have the expression for X':

		Χ'		X'	
$Arg = \varkappa \gamma' + i'g'' + ig'$	sin.	cos.	$Arg = \kappa \gamma' + i'g'' + ig'$	sin.	cos.
κ i' i ο ο ο Ι ο Ι	+1.664 +0.158 -0.141 +0.022 -0.002 -0.002 +0.001	+0.006 -0.002 -0.071 0.000 +0.041 +0.001 -0.004 +0.003 +0.004 -0.007	π i' i -I I+ I 0 I 0 I I- I -I I 0 0 I- I I I- 2 -I I- I 0 I- 2 I I- 3 0 I- 3	-0. 127 +0. 020 +0. 120 -0. 225 -0. 008 +0. 133 -0. 037 -0. 012 -0. 006 0. 000	+0. 084 +0. 098 -0. 120 -1. 164 +0. 001 +0. 625 +0. 107 -0. 053 +0. 026 -0. 002
1 1 0	0.011	+0.003	1 1—4	-0.001	+0.002

Ammand Litall Link	X		Averaged Light Light	3	۲′
$Arg = \kappa \gamma' + i'g'' + ig'$	sin.	cos.	$Arg = \kappa \gamma' + i'g'' + ig'$	sin.	COS.
14 i' i -1 2+ 1 0 2 0 1 2- 1 -1 2 0 0 2- 1 1 2- 2 -1 2- 1 0 2- 2	"0.005 +-0.035 0.0000.4170.334 +-0.088 +-3.9650.009	+0. 010 +0. 001 -0. 014 -0. 013 +0. 144 +0. 069 -1. 709 +0. 003	7 6' 6 1 4-6 -1 4-5 0 4-6 -1 5-1 0 5-2 1 5-3 -1 5-2		-0.006 +0.008 +0.001 -0.008 +0.002 0.000 -0.031 -0.042
1 2— 3 -1 2— 2 0 2— 3 1 2— 4 -1 2— 3 0 2— 4 1 2— 5 -1 3+ 1 0 3 0 1 3— 1	-0. 244 +0. 005 +0. 019 -0. 017 +0. 001 +0. 002 -0. 001 0. 000 +0. 005 -0. 001	+0. 111 -0. 109 -0. 009 +0. 005 -0. 003 +0. 001 -0. 001 -0. 001 -0. 002 0. 000	o 5— 3 I 5— 4 —I 5— 3 o 5— 4 I 5— 5 —I 5— 4 o 5— 5 I 5— 6 —I 5— 5 o 5— 6 I 5— 7	+0.007 -0.007 -0.071 +0.060 +0.002 -0.700 +0.007 +0.020 -0.087 -0.001 +0.003	+0, 002 +0, 494 +0, 033 -0, 020 -0, 402 +0, 001 +0, 011 +0, 004 -0, 002 0, 000
-I 3 0 0 3-I I 3-2 -I 3-I 0 3-2 I 3-3	-0. 056 -0. 036 +0. 012 +0. 416 -0. 127 -0. 032	+0.029 +0.058 -0.001 -0.685 -0.179 +0.059	—I 5— 6 0 5— 7 I 5— 8 —I 6— 2 0 6— 3 I 6— 4	-0.007 -0.001 0.000 +0.009 0.004 0.001	+0.003 0.000 +0.001 -0.012 -0.008 0.000
-I 3-2 0 3-3 I 3-4 -I 3-3 0 3-4 I 3-5 -I 3-4	+1.512 -0.008 -0.071 +0.131 +0.004 -0.007 +0.006	+2. 139 -0. 009 -0. 092 +0. 027 +0. 007 -0. 008 0. 000	-1 6-3 0 6-4 1 6-5 -1 6-4 0 6-5 1 6-6 -1 6-5	+0.046 +0.029 -0.002 -0.335 -0.010 +0.012 +0.125	+0. 089 -0. 003 -0. 005 +0. 021 +0. 034 -0. 002 -0. 410
0 3—5 1 3—6 —I 4 0 0 4— I —I 4—1 0 4—2 I 4—3	0. 000 0. 001 0. 005 0. 000 0. 010 0. 054 +0. 002	+0.001 -0.001 +0.005 +0.009 -0.101 -0.019 +0.010	o 6— 6 i 6— 7 —i 6— 6 o 6— 7 i 6— 8 —i 6— 7	0. 000 0. 001 0. 013 0. 000 0. 000 0. 004	+0.005 +0.009 -0.058 -0.001 +0.001
-I 4-2 0 4-3 I 4-4 -I 4-3 0 4-4 I 4-5 -I 4-4 0 4-5	+0. 640 +0. 083 -0. 037 -1. 002 +0. 005 +0. 034 -0. 013 -0. 003	+0. 233 -0. 091 -0. 010 +1. 094 -0. 008 -0. 039 +0. 117 +0. 002	-I 7-2 0 7-3 -I 7-3 0 7-4 I 7-5 -I 7-4 0 7-5 I 7-6	0.000 -0.002 +0.014 +0.006 0.000 -0.064 +0.005 +0.002	0.002 0.000 +-0.0080.0050.001 +-0.050 +-0.0170.003

Angered Liled Lied	2	ζ′	$Arg = \varkappa \gamma' + i'g'' + ig'$		Χ'	
$Arg = \varkappa \gamma' + i'g'' + ig'$	sin.	cos.	Aign	T' 9 T'9	sin.	cos.
π i' i -1 7-5 0 7-6 1 7-7 -1 7-6 0 7-7 1 7-8 -1 7-7	-0. 058 -0. 018 +0. 002 +0. 222 -0. 002 -0. 006 +0. 034 +0. 002	"0. 205 0. 000 +-0. 006 +-0. 014 +-0. 001 0. 0000. 016	κ ο ι - ι ο ι	6' 6 8 8 8 9 8 8 8 9 8 10 9 9 4 9 6 9 5	-0.002 0.000 +0.014 0.000 0.000 +0.001 -0.001 -0.013	"0.00I0.002 +-0.019 +-0.00I0.00I +-0.002 0.000
0 8— 4 —1 8— 4	o. 000 	-0.002 +0.014	o —I	9— 6 9— 6	-0.002 +0.019	+0.003 0.036
o 8— 5 —1 8— 5 o 8— 6	+0.004 0.045 0.010	+0.003 -0.039 +0.006	i	9— 7 9— 8 9— 7	—0. 005 0. 000 +0. 050	0. 004 +0. 001 +0. 057
1 8-7 -1 8-6 0 8-7 1 8-8	+0. 001 +0. 114 -0. 001 -0. 003	+0.002 0.062 0.008 +0.002		9— 8 9— 9 9— 8 9— 9	+0.004 0.001 0.051 0.009	0.003 0.001 +0.023 +0.010
—ı 8— 7	+0.019	+0.112	1	9—11	0.001	0.000

The foregoing developments enable us to derive the expressions for the factors $r'\frac{dT'}{dr'}$ and $r''\frac{dT'}{dr''}$:

$\texttt{Arg} = \varkappa y' + i' g'' + i g'$	$r' rac{d}{d}$	$rac{dT'}{dr'}$	$r''rac{dT'}{dr''}$		
	sin.	cos.	sin.	cos.	
и i' i	"	,, +0, 006	"	"	
1 O— 1	-2. 904	0.008	+6. 232	+0.008	
—ı o o	—о. 331	+0. 282	+0.644	-o. 43 8	
0 0 1	+0. 205	—o. 167	— 0. 476	+0.211	
I 0— 2	+0.050	-0.090	0.010	+0. 157	
—ı o— I	+0.001	0.009	0. 004	+0.010	
0 0— 2	+0.001	0.003	0.005	0.000	
1 o— 3	+0.002	+0.005	0, 000	-0.002	
—I I+ 2	-o. oo7	-0.001	+0.004	+0.007	
0 1+1	-0.014	-0.001	+0.034	0, 008	
1 1 0	+0.029	+0.004	0. 051	-0.002	
-1 1+ 1	+0.250	о. 368	—0 . 499	+0.561	
0 I 0	+0.020	+0.098			
1 1— 1	0. 276	+0. 230	+0.524	0. 429	

Arg=νγ'+i'g''+ig'	r'd	$\frac{\Gamma'}{dr'}$	$r^{\prime\prime}rac{d\mathbf{T}^{\prime}}{dr^{\prime\prime}}$		
	sin.	cos.	sin.	cos.	
$\mathcal{H} = \hat{i}^{\dagger} = \hat{i}$	"	"	11	"	
—ı ı o	+ 0.795	+3.959	1.297	6. 555	
0 1—1	o. <u>53</u> 0	2. 705	+ 0.669	+ 3.504	
1 1— 2	— O. 192	0. 875	+ 0.408	+ 1.86o	
—ı ı— ı	— o. o51	-0. 321	o. o53	+ o. 560	
0 I— 2	0. 089	+0. 253	+ 0.160	— o. 409	
1 1-3	+ 0.093	-o. o55	— о. 138	+ 0.116	
—I I— 2	0.003	-0.002	+ 0.003	+ 0.004	
0 1—3	0.004	+0.010	+ 0.009	— o. o18	
r r— 4	+ 0.004	-o. oo5	— o. oo8	+ 0.010	
0 2+ 1	0.000	+0.001	0.000	0.001	
I 2 0	+ 0.001	0. 002	— o. oo2	+ 0.002	
—I 2+ I	— o. o13	0.043	+ 0.010	+ 0.064	
0 2 0	+ 0.035	+0.001			
I 2 I	0. 044	+0.045	+ 0.065	o. o75	
—I 2 0	+ 1.351	+0.118	2.415	0.087	
0 2 I	— 1. <u>5</u> 81	+0. 229	+ 1.759	— o. 179	
I 2— 2	+ 0.458	—о. 387	— o. 614	+ 0.628	
—I 2— I	— 9.910	+4. 227	+19.692	8. 444	
0 2— 2	+12.583	-5.399	—18. 131	+ 7.795	
1 2— 3	- 3. 212	+1.366	+ 4.555	— 1. 935	
—I 2 2	+ 0.054	+0.321	+ 0.017	0.620	
0 2— 3	+ 0.523	-0.695	o. 819	+ 0.986	
I 2— 4	— o. 268	+0. 287	+ 0.398	0.402	
—I 2— 3	0.000	+0.008	+ 0.004	0.019	
0 2-4	+ 0.033	-0.047	— o. o51	+ 0.071	
1 2— 5	0.017	+0.023	+ 0.027	— o. o36	
-i 3+ i	0.006	0.002	+ 0.007	+ 0.001	
0 3 0	+ 0.005	-0.002			
I 3— I	0,001	+0.008	+ 0.002	0. 011	
-I 3 0 0 3- I	+ 0.169	-0. 134 +0. 188	- 0. 310	+ 0.219	
1	— 0. 190		+ 0. 222	— o. 178	
I 3 2 3- 1	+ 0, 026 0, 644	0. I2I	— 0.039 + 1.644	+ 0.166	
0 3-2	- 0. 644 + 0. 839	+2.502	•	— 4. 220 — 2. 704	
i 3— 3	- 0.003	2. 940 +0. 936	— 1.532 + 0.064	+ 3.704	
-i 3- 3	— 5.953	-8. 522	+ 9.703	- 1. 219 +13. 813	
0 3—3	+ 7. 089	+9·947	— 9. 703 — 9. 291	—13. 913 —12. 965	
1 3-4	— 2.009	-2.811	+ 2.596	+ 3.614	
—I 3— 3	- o. 608	0.060	+ 0.958	+ 0. 158	
0 3-4	+ 1.052	+0. 529	— 1. 366	— 0. 727	
I 3— 5	0. 399	-0. 247	+ 0.513	+ 0. 329	
I 3 4	— 0.030	+0.002	+ 0.048	0,000	
0 3—5	+ 0.088	+0.027	0. 116	— 0. 039	
I 3-6	0.041	-0.013	+ 0.053	+ 0.019	
		1	1		

sin. coss. sin. coss. x i' i	$Arg = \kappa \gamma' + i'g'' + ig'$	$r'rac{d'}{d}$	$\frac{\mathbf{T}'}{r^J}$	$r' rac{dr}{dt}$	T '
-1		sin.	cos.	sin.	cos.
0 4—1	n i' i	11	"	"	11
1 4-2	—1 4 O	+0.004	0. 028	0. 014	+0.043
-1 4-1	o 4— I	0, 006	+o. o31	+0.011	o. o3o
0 4—2 —0.246 —0.412 +0.206 +0.532 1 4—3 +0.151 +0.102 —1.180 —0.137 —1 4—2 —3.081 —0.462 +4.679 +1.020 0 4—3 +3.500° +0.587 —4.324 —0.998 1 4—4 —1.116 +0.017 +1.385 +0.021 —1 4—3 +5.512 —5.913 —7.991 +8.631 —1 4—3 +5.512 —5.913 —7.991 +8.631 —1 4—5 +1.791 —2.000 —2.179 +2.451 —1 4—5 +1.791 —2.000 —2.179 +2.451 —1 4—5 +1.791 —2.000 —2.179 +2.451 —1 4—5 +1.791 —2.000 —2.179 +2.451 —1 4—6 +1.147 —0.416 —0.186 —5.58 —1 4—6 +0.147 —0.416 —0.186 —5.58	I 4— 2	0,010	0. OI I		+0.017
1	-ı 4- ı	+0.228	+9⋅355	—o. 261	о. 608
-1 4-2	0 4— 2	0. 246	-0.412	+o. 206	+0.532
0 4—3 +3.500° +0.587 -4.324 -0.998 1 4—4 -1.116 +0.017 +1.385 +0.021 -1 4—3 +5.512 -5.913 -7.991 +8.631 0 4—4 -6.102 +6.758 +7.506 -8.365 1 4—5 +1.791 -2.000 -2.179 +2.451 -1 4—4 +0.026 -0.713 -0.072 +1.021 0 4—5 -0.309 +1.124 +0.401 -1.384 1 4—6 +0.147 -0.416 -0.186 +0.508 -1 4—5 -0.009 -0.044 +0.012 +0.065 -1 4—7 +0.003 -0.045 +0.008 -0.133 -1 5—1 +0.055 +0.010 -0.075 +0.066 -1 5—1 +0.055 +0.010 -0.075 -0.029 0 5—2 -0.060 -0.017 +0.061 +0.030 -	1 4— 3	+0.151	+0. 102	—1. 18o	—о. 137
I 4—4 —I. 116 —I. 017 —I. 385 —I. 0.021 —I 4—3 —I. 5. 512 —I. 913 —I. 991 —I. 6.03 I 4—5 —I. 1791 —I. 2.000 —I. 179 —I. 2.451 —I 4—4 —I. 0.026 —I. 713 —I. 0.072 —I. 0.21 0 4—5 —I. 0.026 —I. 124 —I. 0.072 —II. 021 0 4—5 —I. 0.026 —II. 24 —II. 040 —II. 021 0 4—6 —II. 147 —II. 140 —II. 186 —II. 186 —II. 4—5 —II. 0.009 —II. 0.045 —II. 0.065 —II. 0.058 —II. 0.065 —II. 0.008 —II. 0.056 —II. 0.055 —II. 0.008 —II. 0.008 —II. 0.008 —II. 0.008 —II. 0.009 —II. 0.009 —II. 0.009 —II. 0.009 —II. 0.009 —II. 0.009 —II. 0.009 —II. 0.009 —II. 0.009 —II. 0.009 —II. 0.009 —II. 0.009 —II. 0.009 —II. 0.009 —II. 0.009 —II. 0.009 —III. 0.009 —III. 0.009 —III. 0.009	—I 4— 2		-0.462	+4.679	+1.020
-I 4-3	0 4 3	+3.500°	+0.587	-4 . 324	—о. 998
0 4— 4 —6. 102 —6. 758 —7. 506 —8. 365 I 4— 5 —1. 791 —2. 000 —2. 179 —2. 451 —I 4— 4 —0. 026 —0. 713 —0. 072 —1. 021 0 4— 5 —0. 309 —1. 124 —0. 401 —1. 384 I 4— 6 —0. 147 —0. 416 —0. 186 —0. 508 —1 4— 5 —0. 009 —0. 416 —0. 186 —0. 508 —1 4— 6 —0. 004 —0. 108 —0. 012 —0. 605 —1 4— 6 —0. 004 —0. 108 —0. 008 —0. 133 I 4— 7 —0. 005 —0. 015 —0. 006 —0. 075 —0. 029 0 5— 2 —0. 060 —0. 017 —0. 061 —0. 030 —0. 022 —0. 008 —1 5— 3 —0. 027 —0. 009 —0. 032 —0. 008 —0. 032 —0. 008 —1 5— 3 —0. 041 —0. 139 —0. 182 —0. 182	I 4— 4	—1. 116	+0.017	+1.385	+0.021
I	-r 4-3	+5.512	5.913	—7 . 99 1	
—I 4—4 4—0.026 —0.713 —0.072 +I.021 0 4—5 —0.309 +I.124 +0.401 —I.384 I 4—6 +0.147 —0.416 —0.186 +0.508 —I 4—5 —0.009 —0.044 +0.012 +0.065 0 4—6 —0.004 +0.108 +0.008 —0.133 I 4—7 +0.003 —0.045 —0.006 —0.075 —0.029 0 5—2 —0.060 —0.017 +0.061 +0.030 —0.032 +0.008 —I 5—2 —0.060 —0.017 +0.061 +0.030 —0.032 +0.008 —I 5—2 —0.481 +0.352 +0.749 —0.435 —0.435 —0.435 —0.435 —0.435 —0.435 —0.435 —0.435 —0.438 —0.182 —0.220 —0.435 —0.220 —0.435 —0.182 —0.220 —0.423 —0.220 —0.423 —0.220 —0.220 —0.183 —0.182	0 4—4	<u>6. 102</u>	+6.758	+7.506	—8. 365
0 4—5 —0. 309 —1. 124 —0. 401 —1. 384 —1 4—6 —0. 147 —0. 416 —0. 186 —0. 508 —1 4—5 —0. 009 —0. 044 —0. 012 —0. 065 0 4—6 —0. 004 —0. 108 —0. 008 —0. 133 1 4—7 —0. 003 —0. 045 —0. 006 —0. 075 —0. 029 0 5—1 —0. 055 —0. 010 —0. 075 —0. 029 —0. 030 0 5—2 —0. 060 —0. 017 —0. 061 —0. 030 —0. 032 —0. 008 —1 5—3 —0. 027 —0. 009 —0. 032 —0. 008 —1 5—2 —0. 481 —0. 352 —0. 749 —0. 435 0 5—3 —0. 547 —0. 376 —0. 691 —0. 378 —1 5—4 —0. 143 —0. 189 —0. 182 —0. 220 —1 5—5 —0. 143 —0. 189 —0. 182 —0. 220 —1	I 4 5	+1.791	2.000	-2. 179	+2.451
I 4-6 +0. 147 -0. 416 -0. 186 +0. 508 -I 4-5 -0. 009 -0. 044 +0. 012 +0. 065 0 4-6 -0. 004 +0. 108 +0. 008 -0. 133 I 4-7 +0. 003 -0. 045 -0. 006 +0. 056 -I 5-I +0. 055 +0. 010 -0. 075 -0. 029 0 5-2 -0. 060 -0. 017 +0. 061 +0. 030 I 5-3 +0. 027 -0. 009 -0. 032 +0. 088 -I 5-2 -0. 481 +0. 352 +0. 749 -0. 435 0 5-3 +0. 547 -0. 376 -0. 691 +0. 378 I 5-4 -0. 143 +0. 189 +0. 182 -0. 220 -I 5-3 +0. 547 +0. 376 +0. 182 -0. 220 I 5-4 -0. 143 +0. 189 +0. 182 -0. 220 -I 5-5 4.0. 189 +0. 182 -0. 220 I 5-6 -0. 136 -1. 045 +0. 139 +1. 255	—r 4— 4	+o. o26	0. 713	-o. o72	+1.021
-1 4-5	0 4- 5	—o. 309	+1.124	+0.401	1. 384
0 4—6 —0.004 +0.108 +0.008 —0.133 I 4—7 +0.003 —0.045 —0.006 +0.056 —I 5—I +0.055 +0.010 —0.075 —0.029 0 5—2 —0.060 —0.017 +0.061 +0.030 I 5—3 +0.027 —0.009 —0.032 +0.08 —I 5—2 —0.481 +0.352 +0.749 —0.435 0 5—3 +0.547 —0.376 —0.691 +0.378 I 5—4 —0.143 +0.189 +0.182 —0.220 —I 5—3 —0.010 —2.988 —0.155 +4.219 0 5—4 —0.017 +3.315 +0.171 —3.990 I 5—5 4.817 +2.846 —6.557 —3.839 0 5—5 4.4.817 +2.846 —6.557 —3.839 0 5—5 +0.660 —0.688 —0.888 +0.073 -I <th>I 4— 6</th> <th>+0.147</th> <th>—o. 416</th> <th>l .</th> <th>+o. 508</th>	I 4— 6	+0.147	—o. 416	l .	+o. 508
1 4-7 +0.003 -0.045 -0.006 +0.056 -1 5-1 +0.055 +0.010 -0.075 -0.029 0 5-2 -0.060 -0.017 +0.061 +0.030 1 5-3 +0.027 -0.009 -0.032 +0.08 -1 5-2 -0.481 +0.352 +0.749 -0.435 0 5-3 +0.547 -0.376 -0.691 +0.378 1 5-4 -0.143 +0.189 +0.182 -0.220 -1 5-3 -0.010 -2.988 -0.155 +4.219 0 5-4 -0.017 +3.315 +0.171 -3.990 1 5-5 -0.136 -1.045 +0.139 +1.255 -1 5-4 +4.817 +2.846 -6.557 -3.839 0 5-5 -5.349 -3.000 +6.380 +3.547 1 5-6 +1.617 +0.891 -1.913 -1.044 -1 5-5 +0.660 -0.068 -0.888 +0.073 0	—I 4— 5	—o. oog	-0,044	+0.012	
-I 5—I	0 4—6	o. 004	+0. 108	+0.008	о. 133
0 5-2 -0.060 -0.017 +0.061 +0.030 1 5-3 +0.027 -0.009 -0.032 +0.008 -1 5-2 -0.481 +0.352 +0.749 -0.435 0 5-3 +0.547 -0.376 -0.691 +0.378 1 5-4 -0.143 +0.189 +0.182 -0.220 -1 5-3 -0.010 -2.988 -0.155 +4.219 0 5-4 -0.017 +3.315 +0.171 -3.990 1 5-5 -0.136 -1.045 +0.139 +1.255 -1 5-4 +4.817 +2.846 -6.557 -3.839 0 5-5 5.349 -3.000 +6.380 +3.547 1 5-6 +1.617 +0.891 -1.913 -1.044 -1 5-5 +0.660 -0.068 -0.888 +0.073 0 5-6 -0.978 -0.061 +1.163 +0.082 -1 <th>I 4 7</th> <th>+0.003</th> <th>0.045</th> <th>o. oo6</th> <th>+o. o56</th>	I 4 7	+0.003	0.045	o. oo6	+o. o56
I 5-3 +0.027 -0.009 -0.032 +0.008 -I 5-2 -0.481 +0.352 +0.749 -0.435 0 5-3 +0.547 -0.376 -0.691 +0.378 I 5-4 -0.143 +0.189 +0.182 -0.220 -I 5-3 -0.010 -2.988 -0.155 +4.219 0 5-4 -0.017 +3.315 +0.171 -3.990 I 5-5 -0.136 -1.045 +0.139 +1.255 -I 5-4 +4.817 +2.846 -6.557 -3.839 0 5-5 -5.349 -3.000 +6.380 +3.547 I 5-6 +1.617 +0.891 -1.913 -1.044 -I 5-5 +0.660 -0.068 -0.888 +0.073 0 5-6 -0.978 -0.061 +1.163 +0.082 -I 5-7 +0.357 +0.041 -0.423 -0.053 -I<	I 5 I	+0.055	+0,010	— υ. 075	— 0. 029
-I 5- 2	0 5-2	1	-0.017	+o. o61	+0.030
0 5-3 +0.547 -0.376 -0.691 +0.378 1 5-4 -0.143 +0.189 +0.182 -0.220 -1 5-3 -0.010 -2.988 -0.155 +4.219 0 5-4 -0.017 +3.315 +0.171 -3.990 1 5-5 -0.136 -1.045 +0.139 +1.255 -1 5-4 +4.817 +2.846 -6.557 -3.839 0 5-5 -5.349 -3.000 +6.380 +3.547 1 5-6 +1.617 +0.891 -1.913 -1.044 -1 5-5 +0.660 -0.068 -0.888 +0.073 0 5-6 -0.978 -0.061 +1.163 +0.082 1 5-7 +0.357 +0.041 -0.423 -0.053 -1 5-6 +0.046 -0.022 -0.064 +0.028 0 5-7 -0.103 +0.021 +0.122 -0.023 1 <th>I 5— 3</th> <th>+0.027</th> <th>—o. 009</th> <th>0. 032</th> <th>+0,008</th>	I 5— 3	+0.027	—o. 009	0. 032	+0,008
0 5-3 +0.547 -0.376 -0.691 +0.378 1 5-4 -0.143 +0.189 +0.182 -0.220 -1 5-3 -0.010 -2.988 -0.155 +4.219 0 5-4 -0.017 +3.315 +0.171 -3.990 1 5-5 -0.136 -1.045 +0.139 +1.255 -1 5-4 +4.817 +2.846 -6.557 -3.839 0 5-5 -5.349 -3.000 +6.380 +3.547 1 5-6 +1.617 +0.891 -1.913 -1.044 -1 5-5 +0.660 -0.068 -0.888 +0.073 0 5-6 -0.978 -0.061 +1.163 +0.082 1 5-7 +0.357 +0.041 -0.423 -0.053 -1 5-6 +0.046 -0.022 -0.064 +0.028 0 5-7 -0.103 +0.021 +0.122 -0.023 1 <th>—I 5— 2</th> <th>o. 481</th> <th>+o. 352</th> <th>+0.749</th> <th>o. 435</th>	— I 5— 2	o. 481	+o. 352	+0.749	o. 435
-I 5-3 -0.010 -2.988 -0.155 +4.219 0 5-4 -0.017 +3.315 +0.171 -3.990 I 5-5 -0.136 -1.045 +0.139 +1.255 -I 5-4 +4.817 +2.846 -6.557 -3.839 0 5-5 -5.349 -3.000 +6.380 +3.547 I 5-6 +1.617 +0.891 -I.913 -I.044 -I 5-5 +0.660 -0.068 -0.888 +0.073 0 5-6 -0.978 -0.061 +1.163 +0.082 I 5-7 +0.357 +0.041 -0.423 -0.053 -I 5-6 +0.046 -0.022 -0.064 +0.028 0 5-7 +0.046 -0.021 +0.122 -0.023 I 5-8 +0.044 -0.021 +0.023 +0.006 -I 6-I +0.007 -0.003 -0.053 +0.003 -I<	o 5 3	I .	о. 376	0. 691	+o. 378
0 5-4 -0.017 +3.315 +0.171 -3.990 1 5-5 -0.136 -1.045 +0.139 +1.255 -1 5-4 +4.817 +2.846 -6.557 -3.839 0 5-5 -5.349 -3.000 +6.380 +3.547 1 5-6 +1.617 +0.891 -1.913 -1.044 -1 5-5 +0.660 -0.068 -0.888 +0.073 0 5-6 -0.978 -0.061 +1.163 +0.082 1 5-7 +0.357 +0.041 -0.423 -0.053 -1 5-6 +0.046 -0.022 -0.064 +0.028 0 5-7 -0.103 +0.021 +0.122 -0.023 1 5-8 +0.044 -0.021 +0.122 -0.023 -1 6-1 +0.007 -0.003 -0.053 +0.006 -1 6-1 +0.007 -0.003 +0.007 -0.002 1 6-2 -0.015 +0.088 +0.037 -0.119 0	I 5 4	0. 143	+0. 189	+o. 182	— 0. 220
I 5	—ı 5— 3	-0, 010	-2. 988	—0. 155	+4.219
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	0 5— 4	0.017	+3.315	+o. 171	3.990
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	I 5- 5	—о. 136	-1.045	+o. 1 39	+1.255
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	— I 5— 4	+4.817	+2.846	6. 557	—3.839
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	o 5— 5	− 5. 349	3.000	+ 6. 380	+3.547
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	1 5— 6	+1.617	+o. 891	-1.913	—1.044
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	—ı 5— 5	+o. 66o	o. o68	—о. 888	+0.073
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	o 5— 6	0. 978	-0.061	+1.163	+0,082
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	•		+0.041		i e
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	—ı 5— 6	+0.046	1	—o. o64	1
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	•	0. 103	+0.021	1	
0 6— 2 —0.006 +0.002 +0.007 —0.002 1 6— 3 +0.002 —0.002 —0.003 +0.003 —1 6— 2 —0.015 +0.088 +0.037 —0.119 0 6— 3 +0.021 —0.097 —0.038 +0.106 1 6— 4 +0.007 +0.041 —0.007 —0.049 —1 6— 3 —0.455 —0.492 +0.574 +0.713	ı 5— 8	+0.044	—o. oo5	-o. o53	+0.006
$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$	—ı 6— ı	+0.007	-	0. 009	+0.003
-1 6-2 -0.015 +0.088 +0.037 -0.119 0 6-3 +0.021 -0.097 -0.038 +0.106 1 6-4 +0.007 +0.041 -0.007 -0.049 -1 6-3 -0.455 -0.492 +0.574 +0.713			+0.002	1	0. 002
o 6— 3 +0.021 -0.097 -0.038 +0.106 I 6— 4 +0.007 +0.041 -0.007 -0.049 -I 6— 3 -0.455 -0.492 +0.574 +0.713		+0,002	1	0.003	+0.003
I 6 4 +0.007 +0.041 -0.007 -0.049 -I 6 3 -0.455 -0.492 +0.574 +0.713		0, 015	+0.088		
-r 6-3 -0.455 -0.492 +0.574 +0.713		+0.021	1	1	i
		+0.007	+0.041	1	
0 6-4 +0.485 +0.545 -0.523 -0.675	1	В	i	1	i
		+0.485	+0.545	—o. 523	
ı 6— 5 —0. 209 —0. 140 +0. 241 +0. 172	ı 6 5	0. 209	-0. 140	+0.241	+0. 172

$Arg = \varkappa y' + i'g'' + ig'$	$r' rac{d}{d}$	$rac{\Gamma'}{dr'}$	$r''rac{d}{dt}$	T'
	sin.	cos.	sin.	cos.
n i' i	//	"	"	"
—i 6— 4	+2.450	— 0. 446	—3. 2 83	+ 0.506
o 6— 5	—2. 668	+0.478	+3. 139	0. 483
и 6— 6	+o. 8 ₃₄	0. 245	— о. 975	+0. 273
— 1 6— 5	—1.095	+3.421	+1.400	 4⋅439
o 6— 6	+1.070	—3. 714	1. 225	+4. 315
r 6— 7	— 0. 312	+1.135	+ 0. 356	—1.311
— г 6— 6	+ 0. 147	+o. 518	0. 179	—о. 668
o 6— 7	—о. 113	o. 7 36	+0. 126	+o. 854
r 6—8	+ 0. 029	+o. 265	-0.032	0. 307
—r 6— 7	+0. 029	+0.041	—о. 038	0. 054
o 6— 8	-o. o ₃ 8	0.081	+0.043	+0.095
ı 6 9	+0.013	+0.034	o. o15	— 0. 040
—I 7— 2	+0.006	+0.010	o. oo6	0. 015
o 7— 3	0.007	0.011	+0.005	+0.013
1 7-4	+0.005	+0.003	— 0. 006	-0.004
—I 7— 3	0. 118	0.009	∔0. 154	+0.027
0 7—4	+0. 125	+0.014	0. 139	0. 029
ı 7— 5	0. 046	+0.010	+o. o55	0.010
—ı 7— 4	+ 0. 401	0. 504	o. 557	+o. 631
0 7— 5	-0. 442	+0. 535	+o. 536	— 0. 5 91
ı 7— 6	+0. 110	-0. 210	0. 133	+o. 238
—ı 7— 5	+o.68;	+1.759	o. 834	-2. 267
0 7—6	 0. 739	1. 886	+0.811	+2. 180
ı 7— 7	+0. 293	+0.573	— 0, 329	o. 659
— 1 7— 6	—2. 183	—о. 174	+2.733	+0. 205
o 7— 7	+2. 321	+0.099	— 2. 643	<u> </u>
r 7— 8	0. 712	-0.019	+o. 8o5	+o. o18
—ı 7— 7	— о. 355	+0. 170	+0.444	— 0. 210
o 7— 8	+0.491	<u>—</u> 0. 191	—о. 560	+o. 215
1 7— 9	o. 18o	+0.063	+0. 205	o. o7 I
—ı 8— 3	0. 014	+0.010	+0.019	0. 012
o 8— 4	+0.015	o. oi i	o. o18	+0.010
ı 8 5	0, 004	+0.006	+0.005	0.007
<u> </u>	-0.007	—о. 126	о. 003	+o. 161
o 8— 5	+ 0.002	+0.135	+0.008	—o. 152
ı 8— 6	o. o15	-o. o45	+0.015	+0.053
ı 8— 5	+0, 490	+o. 268	0. 604	—0. 362
o 8 6	o. 517	0. 293	+0. 573	+0.353
1 8— 7	+o. 189	+o. o68	o. 213	— 0. o8o
—ı 8— 6	—1. 127	+0.721	+1.410	—о. 876
o 8— 7	+1.190	0. 775	—1. 354	+ 0. 860
1 8— 8	—о. 360	+0. 282	+0.407	-0.314
—ı 8— 7	0. 202	— 1. 263	+0. 253	+1.540
o 8— 8	+0. 271	+1.317	0. 312	—r. 476
ı 8— 9	—o. o91	-0. 405	+ 0. 104	+0.452
	<u> </u>	I	L	<u> </u>

$Arg=\kappa y'+i'g''+ig'$	$r' \frac{d}{d}$	TT'	$r'' rac{d \mathbf{T}'}{d r''}$		
	sin.	cos.	sin.	cos.	
ж i' i —1 8— 8		o. 217	// +0. 207	// +0. 265	
o 8 9	+0. 198	+0. 293	O. 22I	0. 329	
1 810	—о. о68	0. 107	+o. o76	+0.119	
—I 9— 4	-o. o14	o. o16	+o. o16	+0.021	
0 9 5	+0.014	+0.017	0.015	0, 020	
r 9—6	0, 009	o. oo3	+0.009	+0.004	
—ı 9— 5	+o. 125	0. 024	—0. 156	+0.023	
o 9— 6	-0. 129	+0.016	+0. 145	o. o18	
1 9-7	+0. 039	о. о18	—o. o45	+0.019	
—ı 9— 6	—о. 139	+0.435	+o. 185	0. 526	
0 9 7	+0. 152	—o. 445	0. 184	+0, 494	
1 9—8	—o. o31	+0.145	+o. o37	—о. 163	
—I 9— 7	—0. 661	o. 650	+o. 786	+0.792	
o 9—8	+0.673	+ 0. 665	 0. 744	0. 749	
1 9-9	0. 204	-0. 1 92	+0. 229	+0.215	
—ı 9 — 8	+o. 685	—0. 325	—0. 812	+o. 384	
0 9-9	—о. 679	+o. 336	+0.751	о. 376	
1 9—10	+0. 190	—0. 070	-0, 212	+0.083	
-r 99	+0. 160	o. 115	о. 183	+0. 141	
. o 9—10	—o. 155	+0. 165	+0. 172	о. 183	
1 9—11	+0.010	-0.082	o. o17	+o. o88	

The following is a sufficiently exact expression for C'; it is derived from the equation

$$C' = 2 (T' + X' + \overline{T}')$$

$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$. cos.	$\ \operatorname{Arg}=\varkappa y'+i'g''+ig'\ $		
0 I 0 +0.0 I I I -0.0 0 I I -0.2 I I 2 +0.1		1	sin.	cos.
-I 2 0 +0.2 0 2- I -I.0 I 2- 2 +0.6 -I 2- I -3.1 0 2- 2 +7.3 I 2- 3 -3.6	-024 +0.116 -0.082 104 +0.532 -1.058 +0.530 100 +0.530 060 -0.050 460 -0.114 022 +0.270 664 -0.206 704 +1.598 -3.186	0 3— I I 3— 2 —I 3— I 0 3— 2 I 3— 3 —I 3— 2 0 3— 3 I 3— 4	-0. 006 +0. 058 -0. 130 +0. 074 -0. 336 +0. 624 -0. 250 -1. 452 +2. 928 -1. 458 +1. 119 +0. 129	+0.006 -0.054 +0.124 -0.094 +0.696 -1.434 +0.802 -2.026 +3.976 -1.974 +0.761 +0.067

	C	y	A 2004 1 51 011 1 501	C'		
$Arg = \mathcal{H} \mathcal{Y}' + i'g'' + ig'$	sin.	cos.	Arg = ny' + i'g'' + ig'	sin.	cos.	
1 4 1 1 0 4 2 1 4 4 2 0 4 3 1 4 4 4 4 4 1 4 5	+0. 026 -0. 074 +0. 066 -0. 636 +1. 292 -0. 686 +0. 950 -1. 840 +0. 912	+0. 102 -0. 202 +0. 110 -0. 184 +0. 332 -0. 116 -1. 060 +2. 128 -1. 058	# i' i 5-2 -1 5-2 -1 5-4 -1 5-4 -1 5-6 -1 5-6 -1 6-2 -1 6-2 -1 6-5	-0. 022 -0. 104 -0. 060 +0. 680 -1. 360 +0. 672 +0. 002 -0. 008 -0. 644	-0. 014 +0. 042 +0. 976 +0. 378 -0. 712 +0. 350 -0. 002 +0. 014 +0. 088	

In deriving the terms of $\delta T'$, all which afforded less than o''.0000005n't in $n'\delta z'$ were neglected. In the following expression for $\delta T'$ the coefficients have been multiplied by 1000000 in order to escape the necessity of writing so many zeros:

	δ	r ′		δ'.	\mathbf{r}'
$Arg = \mathcal{H} \mathcal{Y}' + i'g'' + ig'$	$n't \sin$.	n't cos.	$Arg = \mathcal{N}' + i'g'' + i'g$	n't sin.	n't cos.
π i' i -I I+2 0 I+I I I 0 -I I+I 0 I 0 I I-I -I I 0 0 I-I I I-2 -I I-I 0 I-2 I I-3 -I I-2 0 I-3 I I-4 -I 2+2 0 2+I I 2 0 -I 2+I 0 2 0 I 2-I -I 2 0 0 2-I I 2-2 -I 2-I		"" - 5.6 + 32.6 - 45.15 - 16.3 - 13.5 + 0.1 + 1.7 + 27.7 - 13 + 7 + 3 - 6 + 4 0 - 1 - 0.3 + 13.4 + 24.1 + 8.9 - 213.6 + 334.2 - 120.0 - 6.1	1	" + 44 - 24 - 7 - 10 + 11 - 5 + 4 - 4 + 2 - 4.1 + 4.58 - 74.02 + 111.57 - 45.12 + 208.5 - 250.4 + 84 - 5 - 8 + 72 - 150 + 83 + 10 - 40 + 20	+ 16 + 3 - 27 + 157 - 103 - 2 + 26 - 19 + 2 - 2.0 - 0.47 - 1.41 + 0.72 + 12.19 - 313.5 + 441.3 - 161 - 30 + 86 - 41 - 15 + 28 - 13 - 7 + 10
	<u> </u>				

Ana	δ	\mathbf{T}'	A	δ	${f T}'$
$Arg = \varkappa \gamma' + i'g'' + ig'$	n't sin.	n't cos.	Arg = ny' + i'g'' + ig'	$n't \sin$.	n't cos.
12 1 4 0 0 4 - 1 1 4 - 2 - 1 4 - 1 1 0 4 - 2 1 4 - 3 1 4 - 4 - 1 4 - 3 1 4 - 4 - 1 4 - 3 1 4 - 4 - 1 4 - 5 1 4 - 6 1 4 - 5 1 4 - 6 1 4 - 5 1 5 - 3 1 5 - 2 1 5 - 3 1 5 - 2 1 5 - 3 1 5 - 4 1 5 - 5 1 5 - 4 1 5 - 5 1 5 - 4 1 5 - 5 1 5 - 6 1 5 - 5 1 5 - 6 1 5 - 7 1 5 - 7 1 5	n't sin.	n't cos. 11 15.9 16.6 100.6 133.1 19.1 113.9 115 135 120 127 169 106 170 12.7 16.26 13.8 126.7 18 1211 1249 187 144 169 199 199 190 100 100 100 100 100 100 10	## 1/ 1 1 1 1 1 1 1 1 1	- 1. 44 + 13. 55 - 16. 3 + 3 + 42 - 53 + 25 - 137 + 156 - 53 - 32 + 40 + 10 - 80 + 30 - 10 - 0. 1 - 0. 0 - 10 - 0. 1 - 0. 6 + 19. 8 - 22 + 10 - 56 + 63 - 20 - 28 + 35 - 20 - 30	" + 0.39 - 17.19 + 20.9 - 12 + 85 - 96 + 31 + 8 - 20 + 8 + 36 - 70 + 20 - 20 - 10 - 10 - 3.9 + 4.1 - 1.7 + 10.6 - 8 + 1 + 45 - 54 + 22 - 77 + 81 - 30 - 20
o 5-7 i 5-8 -i 6-1 o 6-2	+ 10 - 10 - 2.32 + 2.920	- 20 + 10 - 0.32 + 0.467	1 7— 7 1 7— 8 —1 7— 7 0 7— 8 1 7— 9	+ 40 - 10 + 10 - 20 0	+ 30 10 20 + 30 10

From this expression for $\delta T'$ we derive, by the oft-repeated process, the expressions for $\overline{\delta W_0}'$ and $-\frac{1}{2}(\frac{\overline{d} \cdot \delta W_0}{d\gamma'})$:

Arg=i'g''+ig'	$\overline{\delta W_0}'$			$-rac{\mathbf{I}}{2}\Big(\overline{rac{d\cdot\delta\mathbf{W_0}'}{d\gamma'}}\Big)$				
	cos.	n't cos.	sin.	$n't \sin$.	sin.	n't sin.	CO8.	n't cos.
i' i 1+ 1	11	+ 24.9	o. 000I		u.	+ 13.5	"	+ 7.3
1 0	—0. 00038	— 56.9	+0.0044	— 79.6	0.00003	+ 4.9	0.00005	- 0.5
1— 1	0, 000I	— 28. 2	0.0000	— 39. I		+ 9.3		17.9
I— 2	+0,0001	+ 82	+0.0001	39	0.0000	— 42	+0.0001	21
I— 3		0		— 2		2		— I
2+ I		. 0		2		+ 1		+ 1
2 0	+0.0001	+ 100.3	+0.0003	— 53⋅7	0.0000	+ 36.8	0. 0002	+ 16.2
2— I	+0.00323	+1838.3	+0.00458	—1330. 7	+0.00018	— 270. O	-0.00024	- 198.3
2— 2 2— 3	0,0001	+ 22.9 - 6	0, 0000	— 0.8 — 15		— 10.4 + 5		+ 1.4
2- 4		_ 0 _ 2		— 15 — 2		+ 5 + 1		- 5 - 1
	0.0000		10.0017		0.0001	· ·		
3 ° 3 I	-0.0002 +0.000280	— 86.7 —2127.81	+0.0017 +0.041384	- 10.3 + 2.04	-0.0001 +0.000007	— 44.8	—0, 00009 —0, 000009	+ 5.3
3— 2	o. 1161	—4240. 7	+0.0772	—6428. 7	+0.0583	57⋅73+2030. 2	+o. o387	+ 3.46 3064.9
3-3	-0.0026	120	+0.0022	— 165	+0.0026	+ 116	+0.0022	— 158
3-4		+ 2	,	— 4	,	_ I	11 11 11 11	- 7
3— 5		_ 2		_ ı		— т		+ 1
4— I	-0. 00005	— 29. <u>5</u>	+0.00007	— 26.8		- 6.0		+ 6.7
4— 2	_0. 00025	+ 32.5	0,00000	— 442. 3	+0.00031	— 12.9	-0.00002	— I39. 9
4 3	+0.0003	+ 292	+0.0007	— 139	0.0002	219	+0.0004	— 95
4— 4	1	+ 21		+ 3		— 22		— г
4 5		— 5		— 13		— 9		5
4— 6	i	0		— 4		+ 1		0
5— 2	+0.00025	+ 69.7	+0.00023	79.5	+0.00001	- 11.1	-0.00001	— to. 1
5— 3	0. 0004	+ 336.7	+0.0018	+ 86.0	+0.0002	— 197.6	+0.0008	+ 49.9
5— 4	÷0. 0002	8	0,0000	- 82	0.0001	+ 1	0.0000	— 69
5— 5		+ 4		— 11		— з		— 12
5— 6		— 3		10		+ 4		_ 2
6— 2	+0.00004	— 27.62	+0.00027	+ 3.94		- 1.79		— o. o8
6 3	0. 0016	- 1 46.9	+0.0013	- 183.0	+0.0008	+ 66.2	+o. 0006	— 85. 7
6— 4		+ 24		 60		- 15	l	— 47
6— 5 6— 6		— 3I		_ 2	· ·	+ 28	· ·	4
6- 7		— I		+ 2 + 2		+ 9		— 4
j						+ 9		+ 1
7— 3		+ 0.7		— I5. o		+ 0.2	l	- 4.8
7 4		+ 26 16		— 14 — 15		16		- 10
7— 5 7— 6		8		- 15 + 13		+ 14 + 4		— I3 — II
7- 7		_ 2		+ 13 + 2		+ 4 + 3	1	+ II
7— 8		2		0		— I		T
		_		_				

We next must obtain the terms of $n'\delta^2z'$ and $\delta\nu'$, which undergo but one integration. These are given by the formulæ

$$\frac{d\cdot\delta^2z'}{dt} = -2\frac{d\nu'}{n'dt}n'\delta z' + \nu'^2$$

$$\frac{d \cdot \delta \nu'}{n'dt} = -\frac{1}{2} \left(\frac{\overline{d^2 W_0'}}{d \nu'^2} \right) n' \delta z'$$

Employing the subscript $\binom{m''}{m''}$ to denote the portions of the co-ordinates of Saturn proportional to the first power of the mass of Uranus, and which have been determined in Chapter III, the formulæ just given are expanded into

$$\begin{split} \frac{d \cdot \delta^2 z'}{dt} &= \left(\frac{d\nu'}{n'dt}\right)_{m''} & \times \text{ secular terms of } -2n'\delta z' \\ &+ (n'\delta z')_{m''} & \times \text{ secular terms of } -2\frac{d\nu'}{n'dt} \\ &+ (\nu')_{m''} & \times \text{ secular terms of } & 2\nu' \end{split}$$

$$\begin{split} \frac{d \cdot \delta \nu'}{n' dt} &= -\frac{\mathrm{I}}{2} \bigg(\frac{\overline{d^2 \mathbf{W}_0}'}{d \gamma'^2} \bigg)_{\!\!\! n''} \times \text{secular terms of} & n' \delta z' \\ &+ (n' \delta z')_{\!\!\! n''} &\times \text{secular terms of} &- \frac{\mathrm{I}}{2} \bigg(\frac{\overline{d^2 \mathbf{W}_0}'}{d \gamma'^2} \bigg) \end{split}$$

For the second factors of the terms of these equations we have the values

$$-2n'\delta z' \times \frac{1}{2}'' = [5.5104]n't \sin g' + [5.7152]n't \cos g'$$

$$+ [3.6566]n't \sin 2g' + [3.8615]n't \cos 2g'$$

$$+ [2.10]n't \sin 3g' + [2.31]n't \cos 3g'$$

$$-2\frac{dv'}{n'dt} \times \frac{1}{2}'' = [5.2094]n't \sin g' + [5.4142]n't \cos g' + [3.9577]n't \sin 2g' + [4.1526]n't \cos 2g' + [2.76]n't \sin 3g' + [2.96]n't \cos 3g'$$

$$2\nu' \times \frac{1}{2}'' = [3.9585]n't$$

$$+ [5.2094]n't \cos g' - [5.4142]n't \sin g'$$

$$+ [3.6566]n't \cos 2g' - [3.8615]n't \sin 2g'$$

$$+ [2.28]n't \cos 3g' - [2.48]n't \sin 3g'$$

$$-\frac{1}{2} \left(\frac{\overline{d^2 W_0'}}{\overline{d \gamma'^2}} \right) \times \frac{1''}{2} = -\left[4.9084 \right] n't \cos g' + \left[5.1132 \right] n't \sin g'$$
$$-\left[3.9577 \right] n't \cos 2g' + \left[4.1626 \right] n't \sin 2g'$$

The following expression for $-\frac{1}{2}\left(\frac{\overline{d^2W_0'}}{d\gamma'^2}\right)_{m''}$ is derived from the value of $-\frac{1}{2}\frac{dW_0'}{d\gamma'}$, obtained in Chapter III:

Arg=i'g''+ig'	$-\frac{1}{2} \left(\frac{\overline{d^2 W_0'}}{\overline{d \gamma'^2}} \right)_{m''}$		Arg=i'g''+ig'	$-rac{1}{2}\left(rac{d^{2}\lambda}{d\gamma} ight)$	$\left(\frac{\overline{W_0'}}{v'^2}\right)_{m''}$
	cos.	sin.	•	cos.	sin.
i' i 1+ 1 1 0 1- 1 1- 2 1- 3 2 0 2- 1 2- 2 2- 3 2- 4 3 0 3- 1 3- 2 3- 3 3- 4 3- 5 4- 1 4- 2	" - 0. 026 - 0. 147 - 0. 424 + 0. 014 + 0. 002 - 0. 027 - 0. 406 - 10. 134 - 1. 144 - 0. 108 + 0. 021 - 0. 032 + 5. 589 - 0. 663 - 0. 143 - 0. 016 - 0. 001 - 0. 027	-0. 005 -0. 089 +2. 144 +0. 336 +0. 032 -0. 023 +0. 018 -4. 352 -0. 561 -0. 059 +0. 029 -0. 011 +9. 883 +2. 931 +0. 320 +0. 030 0. 000 +0. 176	i' i 4-4 4-5 4-6 5-2 5-3 5-4 5-5 5-6 6-3 6-4 6-5 6-6 6-7 7-3 7-4 7-5 7-6	,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,	+0.609 +0.108 +0.014 +0.007 -0.108 +0.316 -0.118 -0.013 +0.088 +0.090 +0.020 -0.123 -0.028 +0.003 +0.009 +0.029 -0.066
4— 3	- o. 857	+0.310	7— 7	o. o53	0.005

The five products being now computed, and the first three added to $\overline{\delta W_0}'$ and the last two to $-\frac{1}{2} \left(\frac{\overline{d \cdot \delta W_0}'}{d \gamma'} \right)$, we have the following expressions for the portions of $\frac{d \cdot \delta^2 z'}{dt}$ and $\frac{d \cdot \delta \nu'}{n' dt}$, which have the factor n't, the portions independent of this factor being the same as for $\overline{\delta W_0}'$ and $-\frac{1}{2} \left(\frac{\overline{d \cdot \delta W_0}'}{d \gamma'} \right)$:

Arg=i'g''+ig'	$rac{d.\delta^{z}z'}{dt}$		$rac{d \cdot \delta u'}{n' dt}$		
	n't cos.	$n't \sin$.	n't sin.	n't cos.	
i' i i i i i i i i i i i i i i i i i i	+ 69.3 +156.9 - 13.5 +529 + 33	23. 0 +118. 3 65. 0 212 24	+ 42.4 + 53.3 + 2.0 -229 - 27	+ 6.5 -44.6 23.9 93 13	

Arg = i'g'' + ig'	$\frac{d}{d}$	$rac{\delta^2 z'}{lt}$	$\frac{d}{n'}$	$rac{\delta u'}{dt}$
	n't cos.	$n't \sin$.	n't sin.	n't cos.
i' i 2+ I 2 0 2— I	" - 61.2 +1187.6	+ 7 + 144.0 — 880.6	— 4 — 50.0 — 160.7	— 10 — 83.6 — 122.9
2— 2	+ 142.8	+ 330.8	- 43·7	+ 144.3
2— 3	+ 193	+1263	- 79	+ 544
2— 4	+ 6	+ 93	- 6	+ 70
3 ° 3 · 1 · 3 · 2 · 3 · 3 · 3 · 4 · 3 · 5	- 941.2	+ 342.9	- 432.7	— 164. 1
	-1025.44	+ 52.77	- 19.62	+ 1. 60
	-4225.0	-5443.2	+2003.2	—2559. 9
	+ 763	-1729	- 235	— 742
	+ 240	- 98	- 136	— 82
	+ 17	- 2	- 15	— 1
4— I	- 4.6	- 5.4	+ 1.4	+ 0.2 - 123.4 - 105 + 24 - 29 - 3
4— 2	+ 19.8	- 386.2	- 8.9	
4— 3	+ 379	- 165	- 257	
4— 4	+ 94	+ 57	- 58	
4— 5	+ 12	- 60	- 21	
4— 6	+ 2	- 7	- 1	
5— 2	+ 49.8	- 62.6	- 8.3	— 7.6
5— 3	+ 363.6	+ 96.5	- 209.0	+ 54·7
5— 4	+ 3	- 56	- 3	— 59
5— 5	+ 24	- 21	- 14	— 19
5— 6	- 18	- 20	+ 12	— 8
5— 7	- 1	+ 2	+ 1	— 1
6— 2	- 16.56 - 141.9 + 38 - 29 - 7 - 21	+ 3.54	- I.0I	— 0.09
6— 3		- 175.9	+ 63.8	— 82.5
6— 4		- 83	- 2I	— 56
6— 5		- 4	+ 27	— 5
6— 6		- 6	+ II	— 9
6— 7		+ 6	+ I2	+ 4
7— 3	+ 0.6	- 13.5	+ 3	- 45
7— 4	+ 28	- 14	- 18	- 11
7— 5	- 17	- 16	+ 16	- 14
7— 6	- 9	+ 13	+ 5	+ 11
7— 7	- 6	+ 3	+ 5	+ 3

By integrating the preceding expressions we obtain the values of $n'\delta^2z'$ and $\delta \nu'$. In the following statement of these values the proper number of decimals is restored to the coefficients multiplied by n't:

	$n'\delta^{\scriptscriptstyle 2}z'$			$\delta u'$				
$ ext{Arg} = i'g'' + ig'$	sin.	n't sin.	cos.	n't cos.	cos.	n't cos.	sin.	n't sin.
i' i	11	"	11	"	11	11	11	"
1+1	0,0000	+0.000051	+0.0001	+0.000017		—0, 000031		+0.000005
1 0	0.0001	+0.000447	0.0000	-0, 000337	0.0003	-0.000152	+0.0003	-0.000127
1—1	+0.0003	+0.000021	0,0000	-0,000100		+0.000003		+0.000037
1— 2	-0.0001	-0. 000321	+0.0002	-0.000129	-0.0001	-0.000139	-o. ooo i	+0.000056
I— 3		0.000012		-0.000009		-0.000010		+0.000005
2+ 1		0, 000000		-0.000004		+0.000002		-0.000006
2 0	+0.0004	—0. 000087	<u>—0.0006</u>	-0.000205	-0.0001	+0.000071	0. 0004	0.000119
2— 1	⊸ ∪. 0207	-o. oo3975	+0, 0286	—0. 002948	—o. ooo8	0.000538	-0.0010	+0.000411
2 2	+0.0003	-0.000110	+0.0001	+0.000255	+0.0001	-0, 000034	0,0000	-0.000111
2 — 3	+0.0002	-0.000084	0,0000	+0.000549	+0.0001	0. 000034	0.0000	-0. 000237
2 4		-0, 000002		+0.000028		-0,000002		—0. 000021
3 0	+0.0001	-o. ooo895	-0, 0025	-0.000326	0.0001	+0.000403	0.0012	0.000156
3— I	+0.0250	0. 019777	<u>—1. 1796</u>	o. oo1018	+0.0005	+0.000378	0. 0075	+0.000031
3— 2	+0. 1164	+0.004456	+0.0767	-0.005741	+o. o586	+-0.002113	—о. оз86	+0.002700
3 3	+0.0009	—0. 000392	+0.0013	0. 000887	+0.0011	-0.000121	-0.0012	+0.000381
3— 4		-0. 000081		-0.000033		-0.000046		+0.000028
3 5		-0. 000004		0.000001		-0.000004		0.000000
4— 1	0. 0001	-0.000011	-0, 0002	+0.000013		-0. 000003		0, 000000
4— 2	0. 0007	-0.000033	+0.0001	-0.000646	+0.0002	-0.000015	0.0000	+0.000206
4-3	-0.0003	-0.000237	+0.0006	-0.000103	-0, 0002	-0.000161	0. 0004	+0.000066
4— 4		0.000036		+0.000022		-0.000022		0. 000009
4— 5		-0.00003		0.000017		-0.00006		+0.000008
4 6		0.000000	l	-0.000002		0.000000		+0.000001
5— 2	0. 0020	0.000202	+0.0017	-0.000254	-0,0001	-0. 000034	-0.0001	+0.000031
5— 3	+0. 0004	-0.000292	+0.0017	+0.000077	+0.0002	0.000168	0.0008	0. 000044
5— 4	-0,0001	0, 000001	0.0000	-0.000025		-0.00001	İ	+0.000026
5— 5		-0.000007		-0.000006	İ	-0.000004		+0.000006
5— 6	1	+0.000004		-o. ooooo5		+0.000003		+0,000002
6— 2	+0.0007	0. 000160	-0, 0041	0.000034		+0.000010		-0.000001
6 3	+0.0016	+0.000158	+0.0012	-0.000196	+0. 0008	+0.000071	0. 0006	+0.000092
6— 4		0. 000020	ľ	-0.000044		0. 000011		+0.000030
6— 5		+0.000010		0.000001		+0.000009	İ	+0.000002
6— 6	1	+0.000002	1	-0.000002	l	+0.000003		+0.000002
6— 7		+0.000004		+0.000001		+0.000002		0.000001
7— 3	İ	0.000001	[-0.000025		+0.000001		+0.000008
7— 4		-0.000018	ł	-0.000009		-0.000012	1	+0.000007
7— 5	l	+0.000007	1	-0.000006		+0.000006		+0.000005
7— 6		+0.000003	1	+0.000004		+0.000001		-0.00003
7— 7		+0.000001	ĺ	+0.000001	1	+0.000001		-0.000001
			<u> </u>	<u> </u>		<u>.</u>	<u> </u>	1

Thinking that possibly the second-order terms in $\delta T'$ not factored by the time might sensibly affect the long-period inequality in the longitude having the argument 3g''-g', I have made a rough determination of them. But as the resulting quantity was quite small, it seems unnecessary to give more details in reference to it than the following:

I found

$$\frac{d\mathbf{T}'}{dg'}n'\delta z' = 0.000000 \sin(3g'' - g') - 0.000005 \cos(3g'' - g')$$

$$\frac{d\mathbf{T}'}{dg''}n''\delta z'' = + 0.000039 + 0.000009$$

$$r'\frac{d\mathbf{T}'}{dr''}v' = - 0.000013 + 0.000006$$

$$r''\frac{d\mathbf{T}'}{dr''}v'' = - 0.000007 + 0.000035$$

$$\delta \mathbf{T}' = + 0.000019 \sin(3g'' - g') + 0.000045 \cos(3g'' - g')$$

Whence, by twice integrating,

$$n'\delta^2z' = -\circ''.\circ\circ71\sin(3g'' - g') - \circ''.\circ167\cos(3g'' - g')$$

CHAPTER XXII.

PERTURBATIONS OF JUPITER PROPORTIONAL TO THE PRODUCT OF THE MASSES OF SATURN AND URANUS.

We now attend to the sensible inequalities of Jupiter and Saturn whose arguments involve not only the mean anomalies of these two planets but also that of Uranus. They all owe their sensible magnitude to large integrating factors. In the present chapter we investigate the inequalities of this kind which belong to Jupiter. They are only two in number, having severally the arguments 6g' - 2g - 3g'' and 6g' - 3g - 3g''.

If we divide the function T into the two portions, $T_{m'}$ and $T_{m''}$, severally produced by the action of Saturn and Uranus, and adopt a similar division and notation for $n\delta z$, $n'\delta z'$, $n''\delta z''$, ν , ν' , and ν'' , the portion of the correction δT of T, which produces the terms of the kind we are seeking, is

$$\begin{split} \delta \mathbf{T} &= & \frac{d\mathbf{T}_{\mathbf{m}'}}{dg} (n \delta z)_{\mathbf{m}''} + \frac{d\mathbf{T}_{\mathbf{m}'}}{dg'} (n' \delta z')_{\mathbf{m}''} &+ r \frac{d\mathbf{T}_{\mathbf{m}'}}{dr} \cdot \nu_{\mathbf{m}''} + r' \frac{d\mathbf{T}_{\mathbf{m}'}}{dr'} \cdot \nu'_{\mathbf{m}''} &+ \mathbf{C}_{\mathbf{m}'} \left(\delta \frac{h}{\overline{h}_0} \right)_{\mathbf{m}''} \\ &+ \frac{d\mathbf{T}_{\mathbf{m}''}}{dg} (n \delta z)_{\mathbf{m}'} + \frac{d\mathbf{T}_{\mathbf{m}''}}{dg''} (n'' \delta z'')_{\mathbf{m}'} + r \frac{d\mathbf{T}_{\mathbf{m}''}}{dr} \cdot \nu_{\mathbf{m}'} + r' \frac{d\mathbf{T}_{\mathbf{m}''}}{dr''} \cdot \nu''_{\mathbf{m}'} + \mathbf{C}_{\mathbf{m}''} \left(\delta \frac{h}{\overline{h}_0} \right)_{\mathbf{m}'} \end{split}$$

It has been assumed that all terms arising from inclination of orbits may be neglected. Of the ten terms of this formula it is discovered that two, the seventh and ninth, are quite insignificant. The first factors of the first five terms have been determined in Chapter VIII, and are there designated severally as A, F, B, G, and C. $T_{m''}$ is given in Chapter IV. The factors $r\frac{dT_{m''}}{dr}$ and $C_{m''}$ we have had no occasion to derive. The terms which here depend on them are so minute that it is accurate enough to estimate the few terms of these factors by a sort of induction. We assume that $r\frac{dT_{m''}}{dr}$ and $C_{m''}$ bear the same relation to $T_{m''}$ that $r\frac{dT_{m'}}{dr}$ and $C_{m'}$ do to $T_{m'}$. In this way we get, the coefficients in seconds of arc being expressed by their logarithms,

$$r\frac{d\mathbf{T}_{m''}}{dr} = -\left[9.36\right] \sin\left(3g'' - 2g\right) + \left[9.48\right] \cos\left(3g'' - 2g\right) \\ + \left[9.43\right] \sin\left(3g'' - 3g\right) - \left[9.92\right] \cos\left(3g'' - 3g\right) \\ + \left[8.52\right] \sin\left(3g'' - 4g\right) - \left[9.12\right] \cos\left(3g'' - 4g\right) \\ \mathbf{C}_{m''} = -\left[8.86\right] \sin\left(3g'' - 2g\right) + \left[8.98\right] \cos\left(3g'' - 2g\right) \\ + \left[8.93\right] \sin\left(3g'' - 3g\right) - \left[9.41\right] \cos\left(3g'' - 3g\right) \\ - \left[8.00\right] \sin\left(3g'' - 4g\right) + \left[8.60\right] \cos\left(3g'' - 4g\right)$$

The second factors of the formula have already been given, with the exception of $\delta(\frac{h}{h_a})$, which is given by the equation

$$\delta\left(\frac{h}{h_0}\right)_{m''} = -\frac{d \cdot (n\delta z)_{m''}}{ndt} - 2\nu_{m''}$$

It is sufficient to compute in δT the coefficients of the terms having the four arguments

$$-\gamma + 6g' - 2g - 3g''$$
 $-\gamma + 6g' - g - 3g''$ $6g' - 2g - 3g''$ $\gamma + 6g' - 3g - 3g''$

For those having the argument 6g'-2g-3g'' it is necessary to employ the complete formula, involving eight terms; but in the case of the remaining three arguments, which involve γ , it suffices to reduce the expression of δT to

$$\delta \mathbf{T} = \mathbf{F} (n' \delta z')_{m''} + \mathbf{G} \nu'_{m''}$$

In computing the terms with the argument 6g'-2g-3g'' the following are all the combinations of arguments (by subtraction) which give sensible results:

A, B, or C
$$(n\delta z)_{m''}$$
, $\nu_{m''}$, or $\delta\left(\frac{h}{h_0}\right)_{m''}$ For G $(n'\delta z')_{m''}$ or $\nu'_{m''}$ $6g'-3g$ with $3g''-g$ $5g'-2g$ with $3g''-g'$ $6g'-4g$ with $3g''-2g$ with $3g''-2g'$ $6g'-5g$ with $3g''-3g$ $3g'-2g$ with $3g''-3g'$ $6g'-6g$ with $3g''-4g$ $2g'-2g$ with $3g''-4g'$ $2g'-2g$ with $3g''-4g'$ $3g''-4g$ with $3g''-4g'$ $3g''-3g$ with $6g'-4g$ $3g''-3g$ with $6g'-5g$ $3g''-4g$ with $6g'-5g$ $3g''-4g$ with $6g'-6g$

In the terms of δT , containing γ in their arguments, the combinations giving sensible results are

For
$$\gamma + 6g' - 3g - 3g''$$
F or G $(n'\delta z')_{m''}$ or $\nu'_{m''}$
 $\gamma + 5g' - 3g$ with $3g'' - g'$
 $\gamma + 4g' - 3g$ with $3g'' - 2g'$
 $\gamma + 3g' - 3g$ with $3g'' - 3g'$

These details suffice to show how the terms we seek are to be obtained. But the results are limited, in point of precision, to quantities of two dimensions with respect to disturbing forces. However, in the coefficients of the terms having the arguments 6g'-2g-3g'' and $-\gamma+6g'-2g-3g''$, it is necessary to have their variations proportional to t, which are of three dimensions with respect to disturbing forces. As it is impossible to follow a rigorous process in getting these terms, on account of the numerous combinations, we are compelled to resort to very much abbreviated formulæ. There is no proof that the latter afford results sufficiently accurate for practical purposes, yet there is reason for thinking that they give the salient portion of these terms. It is deemed sufficient to put

$$\delta \mathbf{T} = \mathbf{F} (n' \delta z')_{m''} + \mathbf{G} \nu'_{m''}$$

Each of the four factors in the right member of this equation must be supposed to receive an augmentation proportional to nt. Operating then on the equation with the symbol δ we have

$$\delta^{2}T = F(n'\delta^{2}z')_{m''} + G\delta\nu'_{m''} + \delta F \cdot (n'\delta z')_{m''} + \delta G \cdot \nu'_{m''}$$

Of the factors involved in this $(n'\delta^2z')_{m''}$ and $\delta\nu'_{m''}$ have been determined in the preceding chapter. Of the two new quantities δF and δG introduced into the equation, when we recall that $F = \frac{dT}{dg'}$, it will be seen that an approximate expression for δF will be

$$\delta \mathbf{F} = \frac{d\mathbf{F}}{dg'} n' \delta z' + \frac{d\mathbf{G}}{dg'} \nu' + \frac{d}{dg'} \left[\mathbf{A} n \delta z + \mathbf{B} \nu + \mathbf{C} \delta \frac{h}{h_0} \right]$$

Of the quantities involved in this equation $\frac{d\mathbf{F}}{dg'}$ and $\frac{d\mathbf{G}}{dg'}$ have already been used in Chapter XVII for the determination of $\delta^2\mathbf{T}$; $\mathbf{A}n\delta z + \mathbf{B}\nu$ has been computed in Chapter XI; to the factors $n'\delta z'$ and ν' we attribute only their secular terms as values. In like manner we have

$$\delta \mathbf{G} = \frac{d\mathbf{G}}{dg'} n' \delta z' + \frac{d\mathbf{G}}{dg} n \delta z + \left(r' \frac{d}{dr'}\right)^2 \cdot \mathbf{T} \cdot \mathbf{v'} + \left(r \frac{d}{dr}\right) \left(r' \frac{d}{dr'}\right) \cdot \mathbf{T} \cdot \mathbf{v}'$$

All the first factors of the right member of this equation have been used in Chapter XVII. As before $n'\delta z'$, $n\delta z$, ν' , and ν may be supposed reduced to their secular terms.

After δT has been determined, it still remains to get the portion of $n\delta^2z$ which undergoes but one integration; this is

$$\left(\frac{\overline{dW_0}}{d\gamma}\right)n\delta z + \nu^2 = \left(\frac{\overline{dW_0}}{d\gamma}\right)_{m'}(n\delta z)_{m''} + \left(\frac{\overline{dW_0}}{d\gamma}\right)_{m'}(n\delta z)_{m'} + 2\nu_{m'}\nu_{m''}$$

The quantities involved here are so small that there is no necessity for considering any terms of three dimensions with respect to disturbing forces.

Giving to the factors involved their previously ascertained values, performing the multiplication, and preserving only the terms which are of use, we have the following expressions for δF and δG :

$Arg=\varkappa \gamma + i'g' + ig$		δ	F	$\delta \mathrm{G}$		
Arg=xy	++9++9	nt cos.	nt sin.	nt sin.	nt cos.	
н	i' i	11	"	"	11	
—I	3 - 2	-0,000523	—0, 000208	+0.000410	0. 000035	
0	2 2	-0.00041	+0.000304	—0.000067	+0.000081	
—ı	4— 2	0.002623	-o. oo8376	+0.004163	-0.012753	
0	3 2	0. 005872	+0.002898	+0.010443	+0.005455	
—ı	5— 2	+0.000948	—0. 004258	0. 001599	0.005215	
0	4 2	—0. 002740	o. o oo 160	+0.003667	0, 000542	
0	5— 2	—0. 000568	-0.000372	+0.000554	-0.000541	

The following expression is obtained for δT :

	δТ				
Argument.	sin.	cos.			
$ \begin{array}{c} -\gamma + 6g' - 2g - 3g'' \\ -\gamma + 6g' - g - 3g'' \\ 6g' - 2g - 3g'' \\ \gamma + 6g' - 3g - 3g'' \end{array} $	" +0.00099 —0.000001013nt —0.00067 +0.0005921—0.000001410nt —0.00015	// -0.00381 +0.000000422nt -0.00002 +0.0000322-0.0000002907nt +0.00009			

The logarithms of the integrating factors are

$$6g' - g - 3g''$$
 0.0032
 $6g' - 2g - 3g''$ 2.12820n
 $6g' - 3g - 3g''$ 9.9968n

It is found that the terms from $\left(\frac{\overline{dW_0}}{d\gamma}\right)n\delta z + \nu^2$ are insensible. By the application of the usual treatment to δT we get

$$n\delta z = \begin{bmatrix} -0.1396 + 0.000135nt \end{bmatrix} \sin (6g' - 3g - 3g'') + \begin{bmatrix} 0.4897 - 0.000056nt \end{bmatrix} \cos (6g' - 3g - 3g'') + \\ + [-9.3451 + 0.002545nt] \sin (6g' - 2g - 3g'') + [-1.2796 + 0.005246nt] \cos (6g' - 2g - 3g'') + \\ v = \begin{bmatrix} -0.0698 + 0.000067nt \end{bmatrix} \cos (6g' - 3g - 3g'') + [-0.2449 + 0.000028nt] \sin (6g' - 3g - 3g'') + \\ + [-0.0551 \end{bmatrix} \cos (6g' - 2g - 3g'') + [-0.0047] \sin (6g' - 2g - 3g'')$$

CHAPTER XXIII.

PERTURBATIONS OF SATURN PROPORTIONAL TO THE PRODUCT OF THE MASSES OF JUPITER AND URANUS.

Like those discussed in the preceding chapter these perturbations owe their sensible magnitude to large integrating factors. They are more numerous and larger than in the case of Jupiter. The formulæ for their determination are quite similar.

If we divide the function T' into the two portions, T'_m and $T'_{m''}$, severally produced by the action of Jupiter and Uranus, the portion of the correction $\delta T'$ of T', which produces terms of the kind we are seeking, is

$$\begin{split} \delta \mathbf{T}' = & \mathbf{A}' (n' \delta z')_{m''} + \mathbf{B}' \nu'_{m''} + \mathbf{C}' \delta \bigg(\frac{h'}{h_0'} \bigg)_{m''} + \mathbf{F}' (n \delta z)_{m''} + \mathbf{G}' \nu_{m''} \\ & + \frac{d \mathbf{T}'_{m''}}{d g'} (n' \delta z')_m + r' \frac{d \mathbf{T}'_{m''}}{d r'} \nu'_m + \mathbf{C}'_{m''} \delta \bigg(\frac{h'}{h_0'} \bigg)_m + \frac{d \mathbf{T}'_{m''}}{d g''} (n'' \delta z'')_m + r'' \frac{d \mathbf{T}'_{m''}}{d r''} \nu''_m \end{split}$$

A', B', C', F', and G' have been determined in Chapter VIII, the remaining five first factors have been employed in Chapter XXI. The factor

$$\delta \left(\frac{h'}{h_0'}\right)_{m''} = -\left(\frac{d \cdot n' \delta z'}{n' dt}\right)_{m''} - 2 \nu'_{m''}$$

The factors $(n''\delta z'')_m$ and ν''_m , being the Jupiter-perturbations of Uranus, must be derived from the theory of the latter planet. The terms they give rise to are very small. The following are sufficiently exact expressions for these factors:*

$$(n''\delta z'')_{m} \times \frac{1}{2}'' = -[4.49] \sin(2g - g'') - [2.03] \cos(2g - g'')$$

$$-[3.70] \sin(2g - 2g'') - [3.27] \cos(2g - 2g'')$$

$$-[3.10] \sin(2g - 3g'') - [2.88] \cos(2g - 3g'')$$

$$v''_{m} \times \frac{1}{2}'' = -[4.49] \cos(2g - g'') + [1.65] \cos(2g - g'')$$

$$+[3.55] \cos(2g - 2g'') - [3.41] \cos(2g - 2g'')$$

$$+[3.26] \cos(2g - 3g'') - [3.04] \cos(2g - 3g'')$$

The remaining factors have already been given.

As in the case of Jupiter it is necessary to consider some terms of three dimensions with respect to disturbing forces and which are factored by n't. This, however,

is only necessary for the terms of $\delta T'$ having the arguments $\delta g' - 2g - 3g''$ and $-\gamma' + \delta g' - 2g - 3g''$. Here we can reduce the expression for $\delta T'$ to

$$\delta \mathbf{T}' = \mathbf{A}' (n' \delta z')_{m''} + \mathbf{B}' \nu'_{m''} + \mathbf{A}'_{m''} (n' \delta z')_m + \mathbf{B}'_{m''} \nu'_{m}$$

Subjecting this equation to the operation δ we have

$$\begin{split} \delta^{2}\mathbf{T'} &= \mathbf{A'}(n'\delta^{2}z')_{m''} + \mathbf{B'}\delta\nu'_{m''} + \mathbf{A'}_{m''}(n'\delta^{2}z')_{m} + \mathbf{B'}_{m''}\delta\nu'_{m} \\ &+ \delta\mathbf{A'}(n'\delta z')_{m''} + \delta\mathbf{B'}\nu'_{m''} + \delta\mathbf{A'}_{m''}(n'\delta z')_{m} + \delta\mathbf{B'}_{m''}\nu'_{m} \end{split}$$

In this expression four new factors, $\delta A'$, $\delta B'$, $\delta A'_{m''}$, and $\delta B'_{m''}$, appear. Remembering that

$$\mathbf{A}' = \frac{d\mathbf{T}'}{dq'} \qquad \qquad \mathbf{B}' = r' \frac{d\mathbf{T}'}{dr'} \qquad \qquad \mathbf{A}'_{m''} = \frac{d\mathbf{T}'_{m''}}{dq'} \qquad \qquad \mathbf{B}'_{m''} = r' \frac{d\mathbf{T}'_{m''}}{dr'}$$

it will be seen that, with sufficient approximation, we have

$$\begin{split} \delta \mathbf{A}' &= \frac{d\mathbf{A}'}{dg'} n' \delta z' + \frac{d\mathbf{B}'}{dg'} \nu' + \frac{d}{dg'} [\mathbf{F}' n \delta z + \mathbf{G}' \nu] \\ \delta \mathbf{B}' &= \frac{d\mathbf{B}'}{dg'} n' \delta z' + \left(r' \frac{d}{dr'} \right)^2 \mathbf{T}' \cdot \nu' + \frac{d\mathbf{B}'}{dg} n \delta z + \left(r \frac{d}{dr} \right) \left(r' \frac{d}{dr'} \right) \mathbf{T}' \cdot \nu \\ \delta \mathbf{A}'_{m''} &= \frac{d\mathbf{A}'_{m''}}{dg'} n' \delta z' + \frac{d\mathbf{B}'_{m''}}{dg'} \nu' + \frac{d\mathbf{A}'_{m''}}{dg''} n'' \delta z'' + \frac{d\mathbf{G}'_{m''}}{dg'} \nu'' \\ \delta \mathbf{B}'_{m''} &= \frac{d\mathbf{B}'_{m''}}{dg'} n' \delta z' + \left(r' \frac{d}{dr'} \right)^2 \mathbf{T}'_{m''} \cdot \nu' + \frac{d\mathbf{B}'_{m''}}{dg''} n'' \delta z'' + \left(r' \frac{d}{dr'} \right) \left(r'' \frac{d}{dr''} \right) \mathbf{T}'_{m''} \nu'' \end{split}$$

Here the factors $n\delta z$, $n'\delta z'$, $n''\delta z''$, ν , ν' , and ν'' are to be reduced to their secular terms. The proper expressions for $n''\delta z''$ and ν'' have already been given (page 458). F' $n\delta z$ + G' ν has been determined in Chapter XIV. The first factors of the expressions for δ A' and δ B' have already been employed in the determination of the terms of three dimensions for Saturn. B' $_{m''}$ and G' $_{m''}$ have been derived in Chapter XXI. The terms which arise from the term having the factor $\left(r'\frac{d}{dr'}\right)^2$ T' $_{m''}$ are very small. It has been thought sufficiently accurate to estimate by induction the needed terms of this factor. They are

$$\left(r'\frac{d}{dr'}\right)^{2}\mathbf{T'}_{m''} = \begin{bmatrix} 9.28 &] \sin(3g'' - g') - [9.27 &] \cos(3g'' - g') \\ - [0.2248] \sin(3g'' - 2g') + [0.7693] \cos(3g'' - 2g') \\ - [1.3276] \sin(3g'' - 3g') - [1.4748] \cos(3g'' - 3g') \\ - [0.6241] \sin(3g'' - 4g') - [0.3256] \cos(3g'' - 4g') \\ - [9.64 &] \sin(3g'' - 5g') - [9.13 &] \cos(3g'' - 5g')$$

On account of the smallness of ν'' the last term of $\delta B'_{m''}$ has been neglected. Lastly, for the terms of $\delta T'$, having the argument $-\nu' + 6g' - 2g - 3g''$, it suffices to consider $\delta A'$ and $\delta B'$ alone, omitting altogether $\delta A'_{m''}$ and $\delta B'_{m''}$.

	δ.	A ′	δ Β′		
Argument.	cos.	cos. sin.		cos.	
	"	,,	,,	"	
$-\gamma'+3g'-2g$	-0.0012n't	+0. 0186 <i>n't</i>	+0.0007n't	+0.0050n't	
2g'—2g	+0.00283n't	o. 00572n't	-0.00264n't	+0.00107n't	
$-\gamma' + 4g' - 2g$	-0. 1954n't	+0. II02n't	+0.02985n't	+0.01707 <i>n't</i>	
39'-29	+0.09058n't	-0.04545 <i>n't</i>	-0. 15999n't	0. 08274n't	
$-\gamma'+5g'-2g$	-o. 1096n't	0. 0020n't	+0. 1374n't	-0.0132n't	
4g'—2g	+0.06126n't	+0.00251 <i>n't</i>	-0. 08552n't	+0.00898#'t	
5 <i>g</i> ′—2 <i>g</i>	+0.01685n't	+0.01075n't	-0. 01795 <i>n't</i>	+0.01542n't	

1		L'm''	δΒ' _{™''}		
Argument.	cos.	sin.	sin.	cos.	
3g''— g' 3g''—2g' 3g''—3g' 3g''—4g'	$ \begin{array}{c} -0.0002163n't \\ +0.0007007n't \\ +0.00001n't \\ +0.00044n't \end{array} $	+0.0000054n't $+0.0013700n't$ $+0.00029n't$ $+0.00010n't$	+0.000101 $n't$ -0.00028 $n't$ +0.00023 $n't$ -0.00161 $n't$	$ \begin{array}{c} "" \\ -0.00031n't \\ +0.00044n't \\ +0.00023n't \\ +0.00021n't \end{array} $	

Computing the terms of two dimensions of $\delta T'$, which have the argument 6g'-2g-3g'', we obtain severally for each of the ten terms

$$A'(n'\delta z')_{m''} = -0.0044383 \sin (6g' - 2g - 3g'') - 0.0003686 \cos (6g' - 2g - 3g'')$$

$$B'\nu'_{m''} = -0.0026341 + 0.0003563$$

$$C'\delta \left(\frac{h'}{h_0'}\right)_{m''} = +0.0000205 + 0.0001902$$

$$F'(n\delta z)_{m''} = -0.0000042 + 0.0000342$$

$$\frac{dT'_{m''}}{dg'}(n'\delta z')_{m} = -0.0032506 + 0.000025$$

$$B'_{m''}\nu'_{m} = -0.0024209 - 0.0002530$$

$$C'_{m''}\delta \left(\frac{h'}{h_0'}\right)_{m} = +0.0000094 - 0.0002299$$

$$\frac{dT'_{m''}}{dg''}(n''\delta z'')_{m} = -0.0000001 + 0.0000003$$

$$r''\frac{dT'_{m''}}{dr''}\nu''_{m} = +0.00000014$$

And their sum

$$\delta T' = -o''.0127282 \sin (6g' - 2g - 3g'') - o''.0001363 \cos (6g' - 2g - 3g'')$$

In like manner the terms having the argument $-\gamma' + 6g' - 2g - 3g''$ are composed as follows:

$$A'(n'\delta z')_{m''} = + 0.02049 \sin (-y' + 6g' - 2g - 3g'') + 0.01306 \cos (-y' + 6g' - 2g - 3g'')$$

$$B'\nu'_{m''} = + 0.01484 + 0.00461$$

$$C'\delta \left(\frac{h'}{h_0'}\right)_{m''} = + 0.00016 + 0.00028$$

$$F'(n\delta z)_{m''} = + 0.00008 + 0.00009$$

$$G'\nu_{m''} = + 0.00029 + 0.00034$$

$$r'\frac{d\Gamma'_{m''}}{dg'}\nu'_{m} = - 0.00019 + 0.00022$$

$$C'_{m''}\delta \left(\frac{h'}{h_{m}}\right) = - 0.00007 + 0.00020$$

And their sum

$$\delta T' = + \circ'' \cdot \circ 3512 \sin(-\gamma' + 6g' - 2g - 3g'') + \circ'' \cdot \circ 1799 \cos(-\gamma' + 6g' - 2g - 3g'')$$

In computing the terms of three dimensions having these arguments, it has been found that

$$A'(n'\delta^2z')_{m''} = + 0.000001691n't \sin(6g' - 2g - 3g'') + 0.000000669n't \cos(6g' - 2g - 3g'')$$

$$B'\delta\nu'_{m''} = + 0.000000657 - 0.00000066$$

$$A'_{m''}(n'\delta^2z')_m = - 0.000000071 + 0.00000253$$

$$\delta A'(n'\delta z')_{m''} = + 0.000000258 + 0.000002653$$

$$\delta B'\nu'_{m''} = + 0.00000171 + 0.000002409$$

$$\delta A'_{m''}(n'\delta z')_m = + 0.000000269 + 0.000000528$$

And their sum

$$\delta^2 T' = + \circ'' \cdot 000007169n't \sin(6g' - 2g - 3g'') + \circ'' \cdot 000012798n't \cos(6g' - 2g - 3g'')$$

In a similar manner for the terms belonging to the argument $-\gamma' + 6g' - 2g - 3g''$

$$A'(n'\delta^{2}z')_{m''} = -0.0000071n't \sin(-\gamma' + 6g' - 2g - 3g'') - 0.0000074n't \cos(-\gamma' + 6g' - 2g - 3g'')$$

$$B'\delta\nu'_{m''} = -0.0000004$$

$$\delta A'(n'\delta z')_{m''} = +0.0000007$$

$$\delta B'\nu'_{m''} = -0.0000002$$

$$-0.0000104$$

And their sum

$$\delta^{2}T' = -0.0000048n't \sin(-\gamma + 6g' - 2g - 3g'') - 0.0000275n't \cos(-\gamma' + 6g' - 2g - 3g'')$$

Adding to the previous terms those dependent on the arguments $-\gamma' + 7g' - 2g - 3g''$ and $\gamma' + 5g' - 2g - 3g''$, of the computation of which it is thought unnecessary to give any details, we have the following complete expression for $\delta T'$:

Argument.	sin.	cos.
$-\gamma' + 6g' - 2g - 3g''$ $-\gamma' + 7g' - 2g - 3g''$ $6g' - 2g - 3g''$ $\gamma' + 5g' - 2g - 3g''$	+0.03512 -0.0000048 $n't$ +0.01155 -0.0127282+0.000007169 $n't$ +0.00419	+0. 01799 -0. 0000275n't +0. 00092 -0. 0001363+0. 000012798n't -0. 00039

The logarithms of the integrating factors are

$$7g' - 2g - 3g''$$
 0.0081
 $6g' - 2g - 3g''$ 1.73316n
 $5g' - 2g - 3g''$ 9.9920n

The very familiar process being applied to $\delta T'$ we get

$$\delta \overline{W_0'} = \begin{bmatrix} 1.8193 - 0.000260n't \end{bmatrix} \cos (5g' - 2g - 3g'')
+ [-0.9874 + 0.001488n't] \sin (5g' - 2g - 3g'')
+ [-0.65875 + 0.0003878n't] \cos (6g' - 2g - 3g'')
+ [-0.02967 - 0.0006923n't] \sin (6g' - 2g - 3g'')
- \frac{1}{2} (\overline{\frac{d \cdot \delta \overline{W_0'}}{dy'}}) = [-0.9096 + 0.000130n't] \sin (5g' - 2g - 3g'')
+ [-0.4937 + 0.000744n't] \cos (5g' - 2g - 3g'')
+ [-0.00794] \sin (6g' - 2g - 3g'')
+ [-0.00028]] \cos (6g' - 2g - 3g'')$$

In order to have the value of $\frac{d \cdot \delta^2 z'}{dt}$ it is necessary to add to the first of these expressions the terms which arise from

$$\left(\frac{\overline{dW_0'}}{d\gamma'}\right)n'\delta z' + \nu'^2$$

When this is expanded it takes the form

$$\left(\frac{\overline{dW_0'}}{d\gamma'}\right)_{\!\!\!m}(n'\delta z')_{\!\!\!m'} + \left(\frac{\overline{dW_0'}}{d\gamma'}\right)_{\!\!\!m'}(n'\delta z')_{\!\!\!m} + 2\nu'_{\!\!\!m}\nu'_{\!\!\!m''}$$

These terms are significant only in the case of the argument 6g' - 2g - 3g''. All the factors involved have been already given. It is found that

$$\left(\frac{\overline{dW_0'}}{d\gamma'}\right)_m (n'\delta z')_{m''} = + 0.03468 \cos(6g' - 2g - 3g'') + 0.01438 \sin(6g' - 2g - 3g'')
\left(\frac{\overline{dW_0'}}{d\gamma'}\right)_{m''} (n'\delta z')_m = + 0.03505 + 0.01353$$

$$2\nu'_m \nu'_{m''} = - 0.01810 - 0.00707$$

And their sum = $+ 0.05163 \cos (6g' - 2g - 3g'') + 0.02084 \sin (6g' - 2g - 3g'')$

It is necessary to consider the terms of three dimensions factored by n't which arise from the same source, and which are given by the formula

All the factors of the six terms of this expression have been given in preceding chapters. It is found that

$$\left(\frac{\overline{dW_0}'}{d\gamma'}\right)_m (n'\delta^2 z')_{m''} = -0.0000094n't \cos (6g' - 2g - 3g'') - 0.0000056n't \sin (6g' - 2g - 3g'')$$

$$\left(\frac{\overline{dW_0}'}{d\gamma'}\right)_{m''} (n'\delta^2 z')_m = -0.0000193 + 0.0000356$$

$$2\nu'_m \delta \nu'_{m''} = +0.0000047 + 0.0000028$$

$$2\nu'_{m''} \delta \nu'_m = +0.0000100 - 0.0000184$$

$$-2\frac{d \cdot \delta \nu'_{m''}}{n'dt} (n'\delta z')_{m''} = -0.00000211 + 0.0000369$$

$$-2\frac{d \cdot \delta \nu'_{m''}}{n'dt} (n'\delta z')_m = -0.0000093 - 0.0000053$$

And their sum = $-0.0000444n't \cos(6g' - 2g - 3g'') + 0.0000460n't \sin(6g' - 2g - 3g'')$

In consequence

$$\frac{d \cdot \delta^2 z'}{dt} = \begin{bmatrix} " & " & " \\ 1.8193 & -0.000260n't \end{bmatrix} \cos(5g' - 2g - 3g'') \\ + \begin{bmatrix} -0.9874 & +0.001488n't \end{bmatrix} \sin(5g' - 2g - 3g'') \\ + \begin{bmatrix} -0.60712 & +0.0003434n't \end{bmatrix} \cos(6g' - 2g - 3g'') \\ + \begin{bmatrix} 0.05051 & -0.0006463n't \end{bmatrix} \sin(6g' - 2g - 3g'') \end{bmatrix}$$

And, by integration,

$$n'\delta^{2}z' = \begin{bmatrix} -1.7848 + 0.000255n't \end{bmatrix} \sin (5g' - 2g - 3g'') + \begin{bmatrix} -0.9698 + 0.001461n't \end{bmatrix} \cos (5g' - 2g - 3g'') + \begin{bmatrix} 30.951 - 0.01858n't \end{bmatrix} \sin (6g' - 2g - 3g'') + \begin{bmatrix} 3.738 - 0.03496n't \end{bmatrix} \cos (6g' - 2g - 3g'')$$

Neglecting any further consideration of terms in $\delta \nu'$, we get

$$\delta \nu' = \begin{bmatrix} -0.8921 + 0.000128n't \end{bmatrix} \cos (5g' - 2g - 3g'') + \begin{bmatrix} 0.4848 - 0.000730n't \end{bmatrix} \sin (5g' - 2g - 3g'') + \begin{bmatrix} 0.4295 \end{bmatrix} \cos (6g' - 2g - 3g'') - \begin{bmatrix} 0.0151 \end{bmatrix} \sin (6g' - 2g - 3g'')$$

This completes the determination of the inequalities of Saturn having the arguments 5g'-2g-3g'' and 6g'-2g-3g''. But there are certain other inequalities of long period depending on all three anomalies. The following is a list of all that seemingly could be of any importance, together with the logarithms of their integrating factors:

Argument.	Log. integrating factor.	Argument.	Log. integrating factor.
$g^{\prime\prime}+ 2g^{\prime}- g$	0.8771 <i>n</i>	6g'' - 7g' + 2g	1.1527
$g^{\prime\prime}-3g^{\prime}+g$	0.7796n	$7g^{\prime\prime} - 5g^{\prime} + g$	1.2051n
2g'' - 3g' + g	0.7340	$7g^{\prime\prime}-1\circ g^\prime+3g$	1.0191 n
3g'' + 4g' - 2g	1.0696	9g'' - 8g' + 2g	0.9133
$4g^{\prime\prime}+g^{\prime}-g$	1.0926n	10g'' - 11g' + 3g	1.3579n
$4g^{\prime\prime} - 4g^{\prime} + g$	0 9423n	10g'' - 6g' + g	1.9784 n
4g'' - 9g' + 3g	0.8312n		

As the inequalities having these arguments are evidently quite small it will suffice to compute them by the most abbreviated formulæ. We take for $\delta T'$ only the portion independent of γ' , and then have

$$n'\delta^2z'=\iint \delta \mathbf{T}'n'^2dt^2$$

We may limit $\delta T'$ to the following terms

$$\delta T' = A'(n'\delta z')_{m''} + B'\nu'_{m''} + A'_{m''}(n'\delta z')_{m} + B'_{m''}\nu'_{m}$$

The following expressions have been found for $\delta T'$ and $n'\delta^2z'$:

	δ	T'	$n'\delta^2z'$		
Argument.	sin.	cos.	sin.	cos.	
	11	"	"	"	
g''+2g'-g	+0.000025	+0.000422	0, 001	-0. 024	
$g^{\prime\prime}-3g^{\prime}+g$	+0.001579	+0.004755	0. 057	0. 172	
$2g^{\prime\prime}-3g^{\prime}+g$	+0.00137	0. 00748	0, 040	+0. 220	
3g'' + 4g' - 2g	+0.000414	+0.000272	-0.057	-0. 037	
4g''+ g'-g	+0, 000024	+0.000002	0, 004	0, 000	
$4g^{\prime\prime}-4g^{\prime}+g$	+0.001188	—о. 000898	-0.091	+0.069	
4g'' - 9g' + 3g	+0.000116	-0.000312	0. 005	+0.014	
6g'' - 7g' + 2g	+0.000812	+0.000096	— 0. 164	-0.019	
$7g^{\prime\prime}$ — $5g^{\prime}$ + g	+0.000039	0, 000026	-0.010	+0.007	
7g''-10g'+3g	—0. 000002	+0.000123	0.000	0, 013	
9g'' - 8g' + 2g	+0.000015	+0.000009	-0.001	0. 001	
10g''-11g'+3g	—o, ooooo51	+0.0000072	+0.003	-0.004	
10g''— $6g'$ + g	o. 0000001	+0.0000001			

CHAPTER XXIV.

PERTURBATIONS OF THE LATITUDE OF JUPITER OF THE SECOND ORDER WITH RESPECT TO DISTURBING FORCES.

The sensible terms of these perturbations of the latitudes of our two planets arise only from their mutual action. They are quite small, and hence admit some simplifications in their computation, besides those indicated by Hansen in the Auseinander-setzung.

The co-ordinate u being obtained through the equations *

$$\frac{1}{n}\frac{d\mathbf{R}_{0}}{dt} = \frac{h}{n}r\frac{\rho}{a_{0}}\sin\left(\omega - \hat{f}\right)\left(\frac{d\Omega}{dZ}\right)\cos i = \mathbf{U}$$

$$u = \overline{\mathbf{R}}_{0} + \left(\frac{\overline{d\mathbf{R}}_{0}}{d\gamma}\right)n\delta z$$

similarly with Hansen† we will put

$$\frac{d\cdot\delta\mathbf{R}_0}{ndt} = \mathbf{A}''n\delta z + \mathbf{B}''(\nu-c) + \mathbf{C}''\delta\frac{h}{h_0} + \mathbf{D}''\frac{u}{\cos i} + \mathbf{E}''\frac{u_1}{\cos i} + \mathbf{F}''n'\delta z' + \mathbf{G}''(\nu'-c') + \mathbf{H}''\frac{u'}{\cos i'}$$

We have

$$\mathbf{A}'' = \frac{d\mathbf{U}}{dg} \qquad \qquad \mathbf{B}'' = \mathbf{Y} + \mathbf{U}$$

where

$$\mathbf{Y} = \frac{h}{n} r^2 \frac{\rho}{a_0} \sin \left(\omega - \tilde{f}\right) \frac{d^2 \Omega}{dr dZ} \cos i = \mathbf{C} a^2 r \frac{d^2 \Omega}{dr dZ} \cos i$$

C being the quantity so denoted (page 76); $a^2r\frac{d^2\Omega}{drdZ}$ has already been derived in computing D, one of the factors involved in δT . Next we have

$$C'' = U$$

In the computation of D'' and E'' Hansen puts D'' = $D_1'' + D_2''$ and E'' = $E_1'' + E_2''$; but D_2'' and E_2'' are quantities of the second order with reference to sin i, sin i', and sin J, besides being of the order of the disturbing force. Hence, $D_2'' \frac{u}{\cos i}$ and $E_2'' \frac{u_1}{\cos i}$,

^{*}Auseinandersetzung, Abth. I, pp. 102, 103, gl. (45), (46).

[†]Auseinandersetzung, Abth. I, p. 133, gl. (83).

being of the third order with reference to the inclinations and of the second with reference to disturbing forces, may be neglected. We can then write

$$\begin{split} \mathbf{D}'' &= \mathbf{C}a^2 \bigg[a \frac{d^2 \Omega}{dZ^2} + \frac{e \sin f}{r \cos^2 \varphi} \frac{d\Omega}{df} - \frac{a}{r} \frac{d\Omega}{dr} \bigg] \cos i \\ &= \mathbf{C} \bigg[a^3 \frac{d^2 \Omega}{dZ^2} + \frac{er \sin f}{\cos^3 \varphi} \frac{d\Omega}{dg} - \frac{1 + 2e \cos f + e^2}{\cos^4 \varphi} ar \frac{d\Omega}{dr} \bigg] \cos i \\ \mathbf{E}'' &= -\mathbf{C} \frac{a^2}{r \cos \varphi} \frac{d\Omega}{df} = -\mathbf{C} \frac{a}{r} \mathbf{T} \end{split}$$

In addition we have*

$$\mathrm{F}'' = rac{d\,\mathrm{U}}{d\,a'}$$
 $\mathrm{G}'' = -\,(\mathrm{Y}\,+\,2\mathrm{U})$ $\mathrm{H}'' = \mathrm{C}a^2a'rac{d^2\Omega}{d\,Z\,d\,Z'}\cos\,i$

Thus, we can write

$$\begin{split} \delta \mathbf{U} &= \frac{d\mathbf{U}}{dg} n \delta z + \frac{d\mathbf{U}}{dg'} n' dz' + \mathbf{Y}(\nu - c - \nu' + c') + \mathbf{U} \bigg(\nu - 2\nu' + 2c' + \delta \frac{h}{h_0} \bigg) \\ &+ \mathbf{D}'' \frac{u}{\cos i} + \mathbf{E}'' \frac{u_1}{\cos i} + \mathbf{H}'' \frac{u'}{\cos i'} \end{split}$$

Here δU appears as the sum of seven products instead of eight, as with Hansen.

It is necessary, then, to compute the developments of the four factors Y, D", E", and H". By neglecting certain terms factored by sin² J we can put †

$$a^3 \frac{d^2 \Omega}{d Z^2} = -\mu \alpha^2 \left(\frac{\mathbf{a}'}{\triangle}\right)^3 \qquad \qquad a^2 a' \frac{d^2 \Omega}{d Z d Z'} = \mu \alpha \left[\left(\frac{\mathbf{a}'}{\triangle}\right)^3 - \left(\frac{\mathbf{a}'}{r'}\right)^3\right]$$

Of the factors involved in D" it is sufficient to put

$$\frac{er \sin f}{a \cos^3 \varphi} = 2[8.3833] \sin g + 2[6.7655] \sin 2g$$

$$\frac{1 + 2e \cos f + e^2}{\cos^4 \varphi} = [0.0010] + 2[8.6854] \cos g + 2[7.3688] \cos 2g$$

In addition

$$\left(\frac{a'}{r'}\right)^{3} = 1.0047 + 0.1689 \cos g' + 0.0142 \cos 2g' + 0.0012 \cos 3g'$$

$$C\frac{a}{r} = 2[9.6980] \sin (\gamma - g) - 2[8.3825] \sin \gamma + 2[8.3817] \sin (\gamma - 2g) + 2[7.12] \sin (\gamma - 3g)$$

In all these computations it is unnecessary to pay attention to the factor $\cos i$, as we intend to take the plane of the orbit at the epoch 1850 as the plane of reference, which makes $i_0 = 0$.

^{*}Auseinandersetzung, Abth. I, p. 136, gl. (97), (98), (99). †Auseinandersetzung, Abth. I, p. 120.

The following is the result of the computation of $\frac{D''}{C}$, the only quantity independent of γ which it is worth while to give:

Arg=i'g'+ig	D		Arg=i'g'+ig	$\frac{\mathbf{D}}{\mathbf{C}}$		Arg=i'g'+ig	D	// T
	608.	sin.		cos.	sin.		cos.	sin.
i' i o o o o o o o o o o o o o o o o o o	" -28. 33 + I. 4I + 0. I8 + 0. 02 + 0. 38 - 6. 46 - 7. 99 + I. 3I - 0. 03 + 0. 05 - 0. 44 - 6. 66 + 36. II + I. 26 + 0. 02	" + 3.76 - 0.10 + 0.03 - 0.30 - 4.07 + 38.74 + 0.04 - 0.08 - 0.02 - 0.88 + 5.88 + 15.71 + 0.48 + 0.07	i' i 3 0 3— 1 3— 2 3— 3 3— 4 3— 5 4— 1 4— 2 4— 3 4— 4 4— 5 4— 6 5— 2 5— 3	" 0.00 - 1.46 + 6.24 + 14.58 + 1.15 + 0.11 - 0.20 + 0.23 + 7.75 - 9.96 - 0.42 + 0.01 - 0.12 + 1.90	" - 0. 12 + 0. 29 + 8. 25 - 20. 17 - 0. 89 0. 00 - 0. 06 + 1. 89 - 3. 73 - 11. 21 - 1. 20 - 0. 08 + 0. 26 + 0. 15	i' i 5-4 5-5 5-6 6-3 6-4 6-5 6-6 6-7 7-6 7-8	" -I. 57 -7. 69 -0. 99 +0. 28 +0. 43 -4. 57 +I. 35 -0. 14 +0. 24 -I. 25 -0. 61 +2. 84 +0. 44	" -6. 29 +4. 22 +0. 07 +0. 20 -1. 63 +0. 16 +4. 86 +0. 69 -0. 26 -0. 62 +3. 06 -0. 10 +0. 21

We have now to multiply certain expressions already obtained by the factor C (value given at page 77), and thus obtain the expressions for the four following quantities:

	7	Y	I	D''	F	Ξ.,,	В	["
$Arg = \mathcal{U} + i'g' + ig$	cos.	sin.	sin.	cos.	cos.	sin.	sin.	cos.
κ t' t	" +0.032 +0.327 -0.320 +0.051 -0.083 -0.120 +0.181 +0.647 -0.646 -0.150 +0.157 +0.710 -0.699 -0.068	" +0. 145 +0. 753 -0. 749 -0. 120 +0. 048 +0. 097 -0. 054 +0. 435 -0. 435 +0. 042 -0. 100 -0. 153 +0. 140 -0. 044	-28.33 -2.75 +0.01 -0.04 +0.11 -0.11 +0.42 +3.34 -2.94 +3.74 -4.12 -0.94 +0.55 +0.07		0.00 -0.02 +0.01 -0.01 0.00 0.00 +0.02 -0.04 -0.24 +0.22 -0.12 +0.14 0.00	" +0.02 +0.09 -0.09 0.00 0.00 -0.02 -0.10 +0.22 +1.22 -1.20 -0.16 +0.04 -0.01	+21.32 +2.68 -0.62 +0.06 -0.17 +0.21 -0.52 -3.30 +2.71 -5.49 +5.92 +1.72 -1.16 -0.10	
1 1—4	0.000	+0.059	0. 00	+ 0.04	+0.02	+0.01	0. 02	o. o6

$Arg = \mu \gamma + i'g' + ig$	3	T	D	y <i>ii</i>	E	"	H	["
Arg=ny+ig+ig	cos.	sin.	sin.	cos.	cos.	sin.	sin.	cos.
и i' i	11	"	11	11	11	"	"	"
-I 2+ I	+0.076	+0.179	+ 0.30	— o. 37	+0.02	-0.01	— o. 28	+ 0.56
I 2 I	0. 022	0. 232	+ 0.02	+ 0.65	-0. I2	0.00	— o. 13	— I.00
—I 2 O	+o. 561	— 0. 557	+ 2.88	+ 3.16	o. 84	— 0. 12	— 3.86	— 4. 80
I 2— 2	—о. 556	+0.551	4. 64	— 2. 36	+1.56	+0.44	+ 5.51	+ 4.01
—I 2— I	+o. o85	+o. 164	—18. 29	+ 7.64	+7.58	+3. 25	+17.27	7.06
1 2-3	— 0. 139	0. 166	+17.90	— 7. 90	− 7.44	3.19	—16. 8 <u>2</u>	+ 7.53
<u>—1</u> 2— 2	o. o16	—o. 573	+ o. 68	— o. 33	O. 2I	+o. 18	— o. 76	+ o. 85
I 2— 4	+0.001	+0. 559	+ 1.07	— 0.43	-0. 51	— 0. 50	o. 88	o. 13
—1 2— 3	0. 026	+0.030	+ 0.04	+ v. 02	-0.01	0.00	— 0. 04	— O. O2
1 2 5	+0.026	+0.025	+ 0.03	0. 04	о. оз	0. 05	0.00	o. oı
i 3 o	+0. 233	—0. 046	+ 0.65	+ 0.24	<u> </u>	— 0. 09	— o. 9o	— o. 39
I 3— 2	—0. 267	o. o13	— o. 96	+ 0.16	+0.23	+0.24	+ 1.22	— o. o6
—I 3— I	-o. 372	o. 565	— 3 ⋅ 34	+ 3.87	+0.98	+1.49	+ 3.53	— 4. 26
ı 3— 3	+0. 364	+0.553	+ 2.57	— 4. 8 ₅	—о. 66	-1.91	- 2.80	+ 5. 18
—I 3— 2	+o. 168	—о. 107	— 7. o6	—10. <u>38</u>	+3. 18	-4. 59	+ 6.42	+ 9.58
1 3— 4	O. 172	+0.154	+ 7.32	+ 9.94	-3. 22	+4.43	— 6.73	9. 10
—ı 3— 3	-0.408	-0.072	0.04	+ 0. 29	+0. 23	+0.12	o. 3o	0. 27
1 3— 5	+o. 39o	+0. 087	+ 0.74	+ o. 68	o. 53	+0.32	— O. 34	— o. 62
—I 4 O	+0.049	+0.017	+ 0.10	— o. oı	-o. oı	0. 02	— o. 14	+ 0.01
1 4— 2	0. 048	0.042	— o. II	+ 0. 10	+0.01	+0.04	+ 0.15	— O. 12
I 4 I	— 0. 006	-0. 254	0. 22	+ 0.89	o, ot	+0. 27	+ 0.22	— I. 07
I 4-3	0, 044	+0. 268	— o. 18	- 1.07	+o. 16	0. 34	+ 0.18	+ 1.24
—I 4— 2	—0. 469	+0. 193	— 3⋅74	2.06	+1.54	— о. 68	+ 3.86	+ 2.06
I 4-4	+0.456	о. 183	+ 4.23	+ 1.43	—1.7 6	+0.42	- 4· 3I	— 1.46
-r 4-3	0. 093	—о. 165	+ 5.27	- 5.48	—2.4 I	—2. 55	 4.82	+ 4.94
I 4- 5	+0. 127	+0.173	 4.85	+ 5.61	+2.25	+2.57	+ 4.40	 5.08
—r 4— 4	—0. 106	+0. 269	o. 15	— o. 19	+0.′09	0, 22	+ 0. 10	0.03
1 4 6	+0. 118	0. 254	o. 33	+ 0.73	+0.13	+0.46	+ 0.34	o. 46
—ı 5— ı	+0.035	0.053	+ 0.04	+ 0.13	-0.02	+0.04	0.05	- 0.17
I 5— 3	o. o58	+0.048	— o. 13	— O. 12	+o. o6	-0.02	+ o. 16	+ 0. 16
—ı 5 2	— 0. 240	-0.040	— 0. 93	0.01	+o. 33	+0.04	+ 1.04	0.00
ı 5— 4	+0. 241	+0.078	+ 1.01	- o. 31	о. 35	о. 18	I. IO	+ o. 32
—r 5— 3	+0.062	+0.348	+ 0.94	— 3. IO	—0. 32	—1. 34	— o. 9o	+ 3.08
ı 5— 5	0.054	0. 335	— o. 48	+ 3.29	+o. 10	+1.42	+ 0.46	3.26
—ı 5— 4	— 0. 149	+0, 064	+ 3.79	+ 2.34	1.8o	+1.10	— 3.41	— 2. I4
ı 5— 6	+0.159	-o. o86	- 3.82	— 2. 03	+1.8o	—о. 96	+ 3.45	+ 1.82
—I 5— 5	+0. 160	+0. 103	+ 0.21	0.11	—о. 17	-0.09	o. o8	+ 0.07
I 5 7	-0. 144	-0.110	— o. 58	- 0.09	+o. 35	-0.01	+ 0.41	+ 0.12
_I 6— 2	<u>—0.</u> 045	-0.045	- o. 15	+ 0.08	+0.05	+0.04	+ 0.17	— o. 10
1 6— 4	+0.037	+0.062	+ 0.12	— o. 16	o. o3	o. o6	- 0.14	+ 0.18
—ı 6— 3	—o. 072	+0. 188	- o. 15	- o. 82	+0.10	o. 31	+ 0.19	+ o. 88
ı 6 5	+0.097	-0, 182	+ 0.38	+ 0.82	0. 20	+0.31	— o. 41	o. 87
—ı 6— 4	+0. 228	+0.007	+ 2.28	+ 0.20	-ı.oı	+0.02	- 2. 22	- 0.17
ı 6 6	0. 215	-0,012	— 2. <u>3</u> 2	+ 0.12	+1.03	+0.11	+ 2.24	O. I2
	0.215	0,012	2.32	7 0.12	+1.03	70.11	7 2.24	_ U. 12

A	1	Y	I)"	I	E''	H	["
$\mathbf{Arg} = ny + i'g' + ig$	cos.	sin.	sin.	· cos.	cos.	sin.	sin.	cos.
κ i' i —1 6—5	//	"	11	11	"	"	"	"
ı -	+o. o ₃ 8	+0. 123	0.84	+2.43	+0,40	+1.16	+0.77	-2.17
ı 6 7	0.051	—o. 132	+o. 6 ₃	-2.41	0. 30	—I. I4	—0. 5 6	+2.14
i 6 6	+0.082	-o. o87	+0.12	+0.16	0, 08	+0.11	—o. o6	-0.09
1 6 8	o. o86	+0.075	o. o5	—0 . 40	+0.04	—0. 22	+0.01	+o. 3o
—ı 7— 3			o. 11	-0. 14	+0.04	-0.04	+o. 12	+o. 15
1 7— 5		1	+ 0. 16	+0.11	0. 07	+0.02	—о. 1 9	O. I2
—I 7— 4	+0.134	+o. o86	+0.64	—о. 26	—о. 2 5	-o. 14	—о. 66	+0.29
1 7— 6	—o. 125	-0. 102	—о. 60		+0.23	+0.20	+0.62	—о. 43
—ı 7 — 5	+0.030	-0.131	+0.23	+1.55	O. I2	+0.70	-0. 2I	—I. 47
ı 7— 7	o. o33	+0. 121	-o. 4I	-1.52	+0. 20	0. 68	+0.40	+1.44
ı 7 6	+0.097	-0.009	—I. 45	0. 16	+0.70	0.07	+1.28	+0.15
ı 7—8	-0. 104	+0.016	+1.39	+0.02	о. 66	+0.01	—I. 24	0.02
—ı 7— 7			—0. 12	+0.10	+0.07	+0.07	+0.08	— 0. 06
ı 7— 9			+o. 25	-0.10	—о. 13	0.07	0, 20	+0.06

From the expression of R_0 given in Chapter II we derive that of $(\overline{\frac{dR_0}{d\gamma}})$:

Arg=i'g'+ig	$\left(\frac{\overline{d}}{d}\right)$	$\frac{\overline{R_0}}{l\gamma}$)	Arg=i'g'+ig	$\left(\frac{\overline{d}1}{d}\right)$	$\frac{\overline{R_0}}{\gamma}$)
	cos.	sin.		cos.	sin.
i' i o— 1	+0. 12 -0. 2825nt	+0. 28 +0. 1248nt	i' i 4 I 4 2	// +0.02 +0.01	+0. 02 +0. 05
0— 2 0— 3	+0.02 -0.0136nt -0.0007nt	-0, 02 +0, 0060nt +0, 0003nt	4— 3 4— 4 4— 5	0. 31 0. 03 0. 01	+0. 12 -0. 03 +0. 03
I+ I I O I- I I- 2 I- 3 2 O 2- I 2- 2 2- 3 3 O	+0. 14 +0. 18 +0. 06 +0. 41 +0. 01 -0. 01 -0. 09 +0. 13 +0. 01 +0. 04	-0.04 +0.12 -0.03 -0.10 0.00 +0.30 +0.09 +0.22 -0.14	5— I 5— 2 5— 3 5— 4 5— 5 5— 6 6— 3 6— 4 6— 5 6— 6	-0.07 +0.01 +3.60 +0.18 -0.01 +0.01 +0.01 -0.03 +0.03	-0. 16 0.00 +0. 34 +0. 11 +0.01 0.00 +0.01 +0.07 0.00 +0.01
3— I 3— 2 3— 3 3— 4	+0. 04 +0. 44 +0. 07 -0. 06	+0. 01 +0. 69 0. 00 -0. 01	7— 4 7— 5 7— 6	0.04 +0.03 0.00	+0.04 +0.01 0.01

In order to obtain a higher degree of precision in the second factors of the terms of δU , we attribute to $n\delta z$, ν , $n'\delta z'$, and ν' the values which result from adding together the terms of the first, second, and third orders with respect to disturbing forces. It is thought unnecessary to give here the expressions of these second factors, as they are so easily formed from data previously given.

The terms having the argument $-\gamma$ in δU are important, as they determine the amount of the secular motion of the plane of the orbit due to the square and product of the masses of Jupiter and Saturn. The following detail of the composition of these terms is therefore given:

$$\frac{dU}{dg}n\delta z = -\frac{n}{0.0002260}\cos(-\gamma) - 0.0006051\sin(-\gamma)$$

$$\frac{dU}{dg'}n'\delta z' = -0.0006676 - 0.0021977$$

$$U\left(\nu - 2\nu' + 2\nu' + \delta \frac{h}{h_0}\right) = -0.0002280 - 0.0006215$$

$$Y(\nu - \nu' + \nu') = -0.0004473 - 0.0012610$$

$$D''\frac{u}{\cos i} = -0.0000396 - 0.0000871$$

$$E''\frac{u_1}{\cos i} = -0.0000051 - 0.0000128$$

$$H''\frac{u'}{\cos i'} = -0.0001084 - 0.0002514$$

$$Sum = -0.0017220\cos(-\gamma) - 0.0050366\sin(-\gamma)$$

The following is the complete expression for δU :

Arg=		δ	U	
$ \mu + i g' + i g $	cos. nt cos.		sin.	$nt ext{ sin.}$
π i' i -I 0 0 I 0-2 -I 0- I I 0-3 -I I+2 I I 0 -I I+ I I I- I -I I- I -I I- I -I I- 2 -I I- 2 -I 2+ I	-0.0017220 +0.001 -0.0025 +0.002 +0.001 -0.0025 +0.0005 +0.0001 -0.0020 +0.001		-0.0050366 +0.002 +0.0015 -0.001 -0.003 +0.0028 +0.0008 +0.0015 -0.0004 +0.0001 +0.0001	+0.000033274 -0.00003 +0.00001 -0.000045 +0.000045 0.000000 +0.000049
I 2— I —I 2 0 I 2— 2 —I 2— I	+0.0029 -0.0019 +0.0017 -0.0008	0. 000005 0. 000049 +-0. 000047 0. 000004	+0.0033 +0.0031 -0.0020 +0.0003	-0. 000005 -0. 000050 +0. 000050 +0. 000021

Arg=	δυ						
н у +i'g'+ig	cos.	cos. nt cos.		$nt \sin$			
н i' i —1 3 о		"	// +0.0024	"			
I 3— 2	+0.0039	-0. 00000I	0.0017	+0.000005			
—ı 3— I	+0.0024	—о. 000040	+0.0024	+0.000025			
I 4+ I	0,001		+0.002				
1 4— I	+0.0008		0.0012				
—ı 4— ı	+0,0004	0.000004	+0.0022	0.000000			
r 4— 3	0.0003	+0.000011	0.0016	+0.000002			
—I 4— 2	+0.0002	+0.000008	0. 0003	+0.000024			
1 5 o	+0.002		+0.002				
I 5 2	+0.000027	+0.00000107	0, 000030	-0.00000037			
—I 5— 2	+0.001389	+0.00000166	+0.000612	+0.00000084			
r 5— 4	+0.002		0.000				
—I IO 4	+0.00100		—o. oo185				

By subjecting the preceding expression to the same treatment as that by which, in Chapter II, $\frac{u}{\cos i}$ was derived from $\frac{1}{n}\frac{d\mathbf{R}_0}{dt}$, we obtain the following:

Arg=i'g'+ig	$\overline{\delta R_0}$	
	sin.	cos.
<i>i' i</i> o o	и и	// // +0.0001247nt +0.0000254n²t²
o— 1	—0. 0050721 <i>n1</i> +0. 00001664 <i>n</i> 2 <i>t</i> 2	-0.0017371 <i>nt</i> -0.0003507 <i>n</i> ² <i>t</i> ²
0— 2	+0.0018-0.0001214nt $+0.00000040n^2t^2$	$+0.0011-0.0000415nt$ $-0.0000085n^2t^2$
o— 3	-0.0000044nt $+0.00000001n^2t^2$	-0.0000015nt -0.0000003n ² t ²
1+ 2	o. 000I	0.0002
1+ 1	-0.0059-0.000017 <i>nt</i>	o. 0056o. 000005 <i>nt</i>
1 0	0.0039+0.000081 <i>nt</i>	+0.0022+0.000107nt
ı— 1	+0.0003-0.000055nt	+0.0005-0.000011nt
1 2	+0.0035—0.000018nt	+0.0002+0.000082nt
1 3	0. 0005	+0.0006
2+ 1	0, 0004	+0.0004
2 0	-0.0158+0.000030 <i>nt</i>	+0.0190—0.000030 <i>nt</i>
2— I	0.00320.000103nt	-0.0070+0.000098 <i>nt</i>
2— 2	+0.0047+0.000023nt	+0.0016+0.000105nt
2— 3	+0.0001	0.0000

Arg=i'g'+ig	$\overline{\delta m R_0}$		
	sin.	cos.	
i' i 3— I 3— 2 3— 3 4 0 4— 2 4— 3 5— I 5— 2 5— 3 5— 4 5— 5	-0.0104+0.000015nt +0.0115-0.00019nt +0.0003-0.00005nt +0.0009 +0.0008-0.000013nt -0.0003-0.000020nt +0.0009+0.000080nt -0.000015nt +0.1071+0.000124nt +0.0026 +0.0001	-0.0032+0.000015nt -0.0120-0.000120nt -0.0003-0.00003nt +0.0012 -0.0047-0.000003nt -0.0008+0.000062nt +0.0072+0.000028nt +0.00002nt -0.0363-0.000063nt -0.0009 0.0000	
10— 5 10— 6	+0.0372 +0.0009	+0.0689 +0.0017	

In order to have the value of $\delta\left(\frac{u}{\cos i}\right)$ it is necessary to add to this expression the value of $\left(\frac{\overline{dR_0}}{\overline{d\gamma}}\right)n\delta z$, which follows:

Arg=i'g'+ig	${\left(rac{\overline{d}\mathrm{R}_0}{dy} ight)}n\delta z$	
	sin.	cos.
i' i	"	-0.0000057#2*t2
0— 1 0— 2 0— 3	-0.0000004 n^2t^2 +0.0000004 $6n^2t^2$ +0.0000002 n^2t^2	$+0.0000004n^{2}t^{2}$ $+0.0000135n^{2}t^{2}$ $+0.0000008n^{2}t^{2}$
1+ 1 1 0 1 1 1 2 2 0 2 1 2 2 2 3 2 4	-0.0007+0.00005nt -0.000034nt +0.00009nt +0.00014nt -0.0014-0.00090nt +0.0005-0.00010nt -0.00083nt -0.000146nt -0.00007nt	-0.0007-0.000007nt -0.000049nt -0.00001nt -0.000059nt +0.0020+0.000041nt +0.0006+0.000106nt -0.000039nt -0.000002nt 0.000000nt
3 0 3— 1 3— 2 3— 3 3— 4	-0.0005-0.00004nt -0.0016+0.000014nt -0.0011-0.000020nt +0.000054nt -0.00002nt	+0.0006+0.000010nt -0.0006-0.00006nt +0.0001-0.00002nt -0.000030nt -0.000012nt

Arg=i'g'+ig	$\left(rac{d\mathrm{R}_{0}}{d\gamma} ight)n\delta z$				
	sin.	cos.			
i' i 4 0	// // +0.0008	,, ,, +0.0010			
4— I	o. 000003nt	-0.000012nt			
4— 2 4— 3	0.0000—0.000011nt +0.000007nt	+0.0007 0.000000nt -0.000010nt			
4— 4	-0. 000007 <i>nt</i>	—0. 000008nt			
5— 0	—0. 000032nt	0.000030nt			
5— г	o. 0007o. 000655nt	+0.0006—0.000620nt			
5— 2	+0.000117 <i>nt</i>	o. 000069nt			
5— 3	+0.0009+0.000012nt	0. 000 0—0. 000904 <i>nt</i>			
5 4	+0.000101 <i>nt</i>	0.000015nt			
5 5	+0.00005 <i>nt</i>	+0.000002nt			
6 4	+o. 0004	+0.0019			
7— 2	+0.0008	0.0003			
7 4	+0.0018	-o. 000 1			
7— 5	+o. oo15	0.0008			
8— 5	0.0004	+0.0006			
9— 5	0.0000	0.0010			
10— 5	+0.0053	+0.0093			
10 б	-0.0014	+0,0002			

Thus we have the following expression for $\delta\left(\frac{u}{\cos i}\right)$:

Arg=i'g'+ig	$\delta\left(rac{u}{\cos i} ight)$					
	sin.	cos.				
€'	n n	" +0.0001247 nt +0.0000311 $n^{2}t^{2}$				
o— 1	—0. 0050721 <i>nt</i> +0. 00001660 <i>n</i> ² <i>t</i> ²	0. 0017371nt 0. 00003503n ² t ²				
0— 2	+0.0018-0.0001214nt +0.0000086n²t²	+0.0011—0.0000415nt +0.0000050n ² t ²				
o— 3	-0. 000004 nt +0. 0000000 $3n^2t^2$	$-0.0000015nt +0.0000005n^2t^2$				
I+ 2	<u></u> 0, 0001	-0.0002				
1+ 1	0. 0066 0. 00001 <i>2nt</i>	-0.0063-0.000012nt				
1 0	0.0039+0.000047 <i>nt</i>	+0.0022+0.000058nt				
1 1	+0.0003-0.000046nt	+0.0005—0.000012nt				
I 2	+0.0035-0.000004 <i>nt</i>	+0.0002+0.000023nt				
I— 3	0. 0005	+0.0006				

A	δ ($\frac{u}{\cos i}$)
Arg=i'g'+ig	sin.	cos.
i' i 2+ 1 2 0 2- 1 2 - 2 2 - 3 2- 4 3 0 3- 1 3- 2 3- 3 3- 4 4 0 4- 1 4- 2 4- 3 4- 4 5 0 5- 1 5- 2 5- 3 5- 4 5- 5 6- 4	-0. 0004 -0. 0172-0. 000060nt -0. 0027-0. 000203nt +0. 0047-0. 000060nt +0. 0001-0. 000146nt -0. 00002nt -0. 0120+0. 00002nt +0. 0104-0. 000212nt +0. 0003+0. 00004nt -0. 00002nt +0. 0017 -0. 000003nt +0. 0008-0. 000024nt -0. 0003-u. 000013nt -0. 00003nt +0. 0005-0. 00013nt +0. 0005-0. 00013nt -0. 00003nt +0. 0005-0. 00013nt -0. 00003nt +0. 00012nt +0. 00012nt +0. 00012nt +0. 1080+0. 00013nt +0. 00016nt +0. 0001+0. 00005nt +0. 0001	+0.0004 +0.0210+0.000011nt -0.0064+0.000204nt +0.0016+0.00006nt 0.0000-0.00002nt 0.00000nt +0.0038-0.000045nt -0.0119-0.00012nt -0.00012nt +0.0022 -0.000012nt -0.00002nt -0.00003nt -0.00003nt -0.00003nt -0.00003nt -0.00003nt -0.00003nt -0.00003nt -0.00003nt -0.00003nt -0.00003nt +0.00052nt -0.00003nt +0.00059nt -0.00067nt -0.00067nt -0.0009-0.000015nt 0.0000-1.00002nt +0.0019
7— 2 7— 4 7— 5 8— 5 9— 5 10— 5	+0.0008 +0.0018 +0.0015 -0.0004 0.0000 +0.0425 -0.0005	0.0003 0.0001 0.0008 +-0.0006 0.0010 +-0.0782 +-0.0019

The only terms of the third order with respect to disturbing forces in the latitude of Jupiter which it seems worth while to consider are the secular terms factored by the cube of the time. As these terms are scarcely appreciable after the lapse of 500 years a very rude computation of their coefficients suffices. If b, l, i, and θ denote severally the latitude, longitude, inclination of orbit, and longitude of the ascending node of Jupiter, all referred to the fixed ecliptic and equinox of 1850.0, we have

$$\sin b = \sin i \sin (l - \theta) = \sin i \cos \theta \sin l - \sin i \sin \theta \cos l$$

and

$$\frac{d(\sin i \cos \theta)}{dt} = \cos i \cos \theta \frac{di}{dt} - \sin i \sin \theta \frac{d\theta}{dt}$$
$$\frac{d(\sin i \sin \theta)}{dt} = \cos i \sin \theta \frac{di}{dt} + \sin i \cos \theta \frac{d\theta}{dt}$$

The following values of i and θ , adopted from the values given by Leverrier,* are sufficiently accurate for our purpose:

Date.	i	θ	$rac{di}{dt}$	$rac{d heta}{dt}$
1850 2350 2850 3350 3850	1 18 42.10 1 18 8.30 1 17 40.70 1 17 19.53 1 17 4.94	98 56 19.79 99 50 4.24 100 46 13.00 101 44 21.07 102 44 3.45	"0. 073673 0. 061480 0. 048825 0. 0358080. 022518	" +6. 29075 6. 60017 6. 86522 7. 08005 +7. 23977

From these we derive the values of the two functions, which follow, for the same dates.

Date.	$rac{d(\sini\cos heta)}{dT}$	$\frac{d(\sin i \sin \theta)}{d\mathbf{T}}$
1850		" 9. 51345
2350	13. 73032	8.61823
2850	14. 32572	7. 69386
3350 3850	14. 86245 —15. 33640	6. 74492 5. 77386

The unit of T is a century of Julian years. From these special values we obtain

and by integrating these equations

$$\sin i \cos \theta = \text{const.} - \text{i}_{3.0811}\text{T} - \text{o.o6}_{744}\text{T}^2 + \text{o.ooo}_{322}\text{T}^3$$

 $\sin i \sin \theta = \text{const.} - \text{g.5}_{134}\text{T} + \text{o.o8}_{786}\text{T}^2 + \text{o.ooo}_{238}\text{T}^3$

As these values correspond to a mass of Saturn $=\frac{1}{35^{12}}$ we augment them a little, and adopt as the terms of the sine of the latitude proportional to the cube of the time,

$$\sin b = + \circ''.000324$$
T³ $\sin l - \circ''.000240$ T³ $\cos l$

^{*}Annales de l'Observatoire de Paris, Mémoires, Tome XI, pp. 7, 47.

CHAPTER XXV.

PERTURBATIONS OF THE LATITUDE OF SATURN OF THE SECOND ORDER WITH RESPECT TO DISTURBING FORCES.

The formulæ to be employed here are precisely similar to those of the preceding chapter. The co-ordinate u' is obtained through the equations

$$\begin{split} \frac{\mathbf{I}}{n'} \, \frac{d\mathbf{R}_0'}{dt} &= \frac{h'}{n'} r' \frac{\rho'}{a'} \sin{(\omega' - \tilde{f'})} \left(\frac{d\Omega'}{dZ'} \right) \cos{i'} = \mathbf{U'} \\ u' &= \overline{\mathbf{R}_0'} + \left(\frac{\overline{d\mathbf{R}_0'}}{\overline{d\gamma'}} \right) n' \delta z' \end{split}$$

For the variation of U' we have

$$\begin{split} \delta \mathbf{U}' &= \frac{d \mathbf{U}'}{d g'} n' \delta z' + \frac{d \mathbf{U}'}{d g} n \delta z + \mathbf{Y}' (\nu' - c' - \nu + c) + \mathbf{U}' \left(\nu' - 2\nu + 2c + \delta \frac{h'}{h_0'} \right) \\ &+ \mathbf{D}'' \frac{u'}{\cos i'} + \mathbf{E}'' \frac{u_1'}{\cos i'} + \mathbf{H}'' \frac{u}{\cos i} \end{split}$$

Here we have

$$Y' = C'a'^2r'\frac{d^2\Omega'}{dr'dZ'}\cos i'$$

C' being the quantity so designated at page 78.

$$D'' = C' \left[a'^{3} \frac{d^{2} \Omega'}{dZ'^{2}} + \frac{e'r' \sin f'}{\cos^{3} \varphi'} \frac{d\Omega'}{dg'} - \frac{1 + 2e' \cos f + e^{2}}{\cos^{4} \varphi'} a'r' \frac{d\Omega'}{dr'} \right] \cos i'$$

$$E'' = -C' \frac{a'}{r'} \overline{\Gamma}'$$

$$H'' = C' a'^{2} a \frac{d^{2} \Omega'}{dZ' dZ'} \cos i'$$

By neglecting certain terms factored by sin2 J we can put

$$a'^{3}\frac{d^{3}\Omega'}{dZ^{2}} = -\mu'\left(\frac{\mathbf{a}'}{\Delta}\right)^{3} \qquad \qquad a'^{2}a\frac{d^{2}\Omega'}{dZdZ'} = \mu'\alpha\left[\left(\frac{\mathbf{a}'}{\Delta}\right)^{3} - \frac{\mathbf{I}}{\alpha^{3}}\left(\frac{\mathbf{a}}{r}\right)^{3}\right]$$

Of the factors involved in D" it is sufficient to put

$$\frac{e'r'\sin f'}{a'\cos^3\varphi'} = 2[8.4488]\sin g' + 2[6.8961]\sin 2g'$$

$$\frac{1 + 2e'\cos f' + e'^2}{\cos^4\varphi'} = [0.0014] + 2[8.7514]\cos g' + 2[7.50]\cos 2g'$$

In addition

$$\frac{1}{\alpha^3} \left(\frac{a}{r}\right)^3 = 6.192 + 0.895 \cos g + 0.065 \cos 2g + 0.005 \cos 3g$$

$$C'\frac{a'}{r'} = 2[9.6976] \sin (\gamma' - g') - 2[8.4478] \sin \gamma' + 2[8.4466] \sin (\gamma' - 2g') + 2[7.25] \sin (\gamma' - 3g')$$

In all these computations it is unnecessary to attend to the factor $\cos i'$, as it is intended to take the plane of the orbit at the epoch 1850 as the plane of reference, which makes $i_0' = 0$.

The following is the expression for $\frac{D''}{C'}$, the only quantity independent of γ' it is worth while to give:

Arg=i'g'+ig	_)'' ''	Arg=i'g'+ig		D ''	$\mathbf{Arg}{=}i'g'{+}ig$		<u>)''</u>
	cos.	sin.		cos.	sin.		cos.	sin.
i' i o o o I o o o o o o o o o o o o o o o		- 44.8 - 10.2 - 1.4 + 0.3 + 4.6 + 46.0 -298.4 + 22.3 + 0.3 - 0.7 - 0.3 - 1.7 - 64.2 + 94.9 + 62.7	i' i 4-2 5-2 0-3 1-3 2-3 3-3 4-3 5-3 6-3 2-4 3-4 4-4 5-4 6-4 7-4	" + 0.9 - 1.3 - 0.1 + 0.8 + 5.6 + 91.1 + 56.1 + 14.9 + 2.4 - 0.3 - 0.7 - 63.4 - 9.7 + 3.8 + 2.2	" + 16.0 + 2.4 - 0.1 - 6.2 - 9.9 -127.3 - 24.7 + 1.8 + 1.7 - 0.1 - 5.7 - 70.6 - 44.0 - 12.3 - 1.9	i' i 3-5 4-5 5-5 6-5 7-5 8-5 4-6 5-6 6-6 7-6 8-6 5-7 6-7 7-7 8-7	0.0 - 3.7 -48.7 -31.3 - 9.0 - 1.5 - 0.1 - 3.6 + 8.7 - 4.5 - 5.1 - 0.1 + 0.1 + 18.3 + 12.5	0.0 - 3.0 +27.2 + 0.4 - 5.0 - 2.2 - 0.2 + 1.6 +30.9 +20.7 + 5.9 + 0.1 + 3.0 - 0.9 + 5.4

We have now to multiply certain expressions already obtained by the factor C' (value given at page 78), and thus obtain the expressions for the following quantities:

Агд=	7	T .	D) //	Е	yı.	В	["
$Arg = \\ \varkappa \gamma' + i'g' + ig$	cos.	sin.	sin.	cos.	cos.	sin.	sin.	CO8.
и i' i	"	11	11	"	"	, , ,	"	11
—I I O	- 0.99	- 2.07	+175.0	+ 2.5	+ 0.2	+ 0.1	+426.7	— 2. I
—ı 2 o	+ 8.68	+ 5.75	+ 32.4	— 22.0	- I.O	+ 4.8	16.2	+ 18.5
1 0 0	— 8.80	6. 22	— 12. 8	+ 22.5	+ 1.0	4.8	+ 64.2	18.9
i 3 o	+ 1.32	+ 2.51	+ 2.7	— 5.6	0.5	+ 0.8	— 2. 7	+ 4.6
1 1 0	— 0. 32	1.88	+ 0.4	+ 3.2	+ 0.3 - 0.1	— 0.2	— o. 5	2.5
—I 4 0	- 0.04	+ 0.55	+ 0.1	— o.8		0.0	0.0	+ 0.7
1 2 0	+ 0.16	— o. 28	+ 0.2	+ 0.3	+ 0, 1	0.0	— o. 3	— o. 3
-ı- ı- ı	+ o. 18	— o. o6	- 0.2	0.0			+ 0.2	+ 0.1
I— 3— I	— o. 38	0.07	+ 0.5	- o. 3			— o. з	0.0
I o I	+ 1.34	+ 0.27	— 1.7	+ 0.4	— o. 3	+ 1.7	 2. 8	0.0
I— 2— I	— 1.8 ₇	— 1. 57	+ z.9	— 2. 9	— o. 3	+ 1.5	— 3⋅3	+ 1.9
-1 I- 1	+ 5.23	+11.53	— 7.8	+ 35.6	+ 8.9	42.5	+ 57.9	— 2 .9
ı— ı— ı	— 4. 8 ₅	—11.53	+ 11.1	— 18.6	— 2.7	+ 13.0	- 53.8	+ 22. U
—I 2— I	— I. 95	+ 2.00	— 34⋅3	—149. 3	55. 2	+260.9	- 31.6	—168. 7
1 0— 1	+ 1.88	0.06	+ 30. 2	+150.6	+55.0	264. 7	+ 40.6	+169.9
-ı 3— ı	+ 5.30	- 5.43	+ 24.8	+ 6.9	+ 3.5	+ 19.6	— 26. 7	— 32. 7
1 1-1	5.76	+ 5.63	29. 2	23.6	— 9. 9	+ 9.9	+ 23.4	+ 13.6
—ı 4— ı	+ 2.67	— o. 75	+ 7.4	+ 0.5	+ 1.6	+ 1.1	— 6.6	— 2. <u>5</u>
1 2— 1	2.08	+ 0.08	- 4.6	+ 0.7	— o. 8	— o. 5	+ 3.8	— o.6
—I 5— I	+ 0.60	+ 0.17	+ 1.3	- 0.4	+ 0.2	+ 0.2	I. I	+ 0.2
1 3 1	O. 32	0. 24	- 0,5	+ 0.4	+ 0.0	— O. 2	+ 0.4	— o. 3
—I 0— 2	0. 16	— o. 11						
I 2 2	+ 0.04	+ 0.20						
_I I— 2	+ 0.17	— o. 64	+ 0.3	+ 1.8	+ 0.8	— 4·3	+ 3.6	+ 0.6
I- I- 2	— I. 37	+ o. 88	+ 1.8	+ 1.8	0. 2	+ 0.9	− 4.5	— o. 5
_1 2— 2	+10.40	— 2. <u>39</u>	— 9.5	— 36. o	— 2.9	+ 31.5	— o.6	+ 3.1
I 0— 2	—IO. 49	+ 2, 10	+ 22. I	+ 30.6	+ 8. 1	— 29.5	10.5	+ 2.0
—I 3— 2	+ 2.42	+ 2.07	—112. I	+ 43.9	— 46. 2	— 16.7	+102.4	— 43.0
1 1— 2	0, 90	— 1.83	+112.4	51.0	+46. 2	+ 21.3	—103.8	+ 46.0
—I 4— 2	2.84	— 4. 14	— 24.8	+ 31.9	— 7.6	- 11.4	+ 23.0	— 28.3
I 2-2	+ 3.06	+ 4.59	+ I2. I	- 27.5	+ 2.4	+ 9.4	— 11.5	+ 24.0
_I 5— 2	0. 19	- 2.30	— I.I	+ 8.8	+ 0.2	— 2.5	+ 1.3	— 7 ⋅5
I 3— 2	— o. 17	+ 1.86	— I.4	- 5⋅4	o. 8	+ 1.3	+ 1.0	+ 4.5
—ı 6— 2	+ 0.28	— o. 57	+ 0.6	+ 1.4	+ 0.2	— o. 3	o. 5	— I.2
I 4— 2	— O, 29	+ 0.32	— o. 6	— o. 5	- 0.2	+ 0.1	+ 0.6	+ 0.4
_I I _ 3	o. o6	0.03			0, 0	— o. 3		
I I- 3	+ 0.07	+ 0.11			0.0	+ 0.1		
— I 2— 3	— o. 13	— 0. O2	— 0. 2	- 2.7	0.4	+ 2.6	— o. 3	+ 0.2
1 0-3	+ 0.12	+ 0.92	+ 0.5	+ 3.2	+ 0.6	- 2.4	0.0	— o. 5
-ı 3-3	— o. 18	— 7.96	+ 1.0	+ 0.3	+ 0, 2	— 3·5	— o. б	- 2.9
I I— 3	0.04	+ 8.09	+ 4.1	+ 6.4	+ 2.0	+ 0.5	- 4.0	— 3⋅5
	L.,	<u> </u>				ļ	<u> </u>	

Arg=		Y		D	"	E'	,	H	"
ку'+i ⁷ g	r'+ig	cos.	sin.	sin.	cos.	cos.	sin.	sin.	cos.
	i 1— 3	+2. 18		-43· 3	,, 62, 6	// —19. I	+27·4	" +38.9	+55.7
	2— 3	-1.83	+1.19	+46.1	+63.4	+20. I	28.0	-41.3	—56. 7
	5— 3	-2.84	+1.22	—28. 7	—14. 2	—11.1	+ 5.0	+25.0	+13.0
1 *	3— 3	+3.25	—1. 38	+24.4	+ 7.0	+ 9.1	- 1.8	-2I. I	- 6.6
1	6— 3	r.8r	0. 24	— 8. т	+ 0.5	- 2.7	— o. 5	+ 7.0	— 0. 2
1 4	4— 3	+1.51	+0.41	+ 5.1	- I.9	+ 1.5	+ 0.9	- 4.4	+ 1.6
_ı 7	7— 3	0.49	— о. 33	— I. 4	+ 0.9	— o. 3	— о. з	+ 1.2	— o. 7
	5— 3	+0. 29	+o. 28	+ o.6	- o. 8	+ o. 1	+ 0.3	- o. 5	+ 0.7
1			·						1
-1 3	3- 4	+0.12	—о, 11						1
1 1	1 4	+0.51	+0.24						i
I 4	4— 4	5.48	— 0. 99	2.3	+ 0, 2	3. I	o. 3	+ 3.4	— о. 1
	2— 4	+5.61	+1.17	— 1.3	+ 3.8	+ 1.5	— I.5	— о. з	— 3·4
1	5— 4	—1.67	2. I I	+31.2	−33.4	+14.1	+15.2	—27. 3	+29.5
1	3 4	+1.00	+1.77	—31.7	+35.6	-14.5	—I6. 2	+27.9	—31. 3
	6— 4	+0.35	+1.73	+ 5.9	22.5	+ 2.2	+ 9.2	 5⋅4	+19.6
1	4-4	-o. 47	2.07	2.0	+19.2	- 0.4	— 7.6	+ 2.2	-16.6
1	7-4	-0.44	+1.25	— I.7	- 6.6	— o. 8	+ 2.4	. + 1.3	+ 5.7
1 '	5-4	+0.52	—I. 08	+ 2.3	+ 4.2	+ 1.0	— I.4	— I.9	— 3·7
	8— 4	—o. 38	+0.35	— I.z	— I. 2	- o. 5	+ 0.3	+ 0.9	+ 1.0
1	6 4	+0.33	-0, 22	+ 0.9	+ 0.5	+ 0.3	- o. ı	— o. 8	o. 5
r	4— 5	0. 19	—o. 25		ļ		!		
1	2 5	+o. 36	-o. 15		1	1	!		
1	5 5	—1.43	+3.41	o. 1	2.6	o. 5	+ 2.5	+ 0.4	+ 3.1
	3— 5	+1.59	-3.52	2.6	+ 1.1	0.7	— I. 7	+ 2.0	— 1.8
1	6— 5	—1.89	+1.05	+23. I	+13.6	+10.6	6, 2	-20.0	—11. 6
1	4- 5	+1.60	0. 65	—24. 5	-13.7	-11.4	+ 6.4	+21.4	+11.9
т	7- 5	+o. 89	+0,04	+15.9	+ 0.8	+ 6.8	— o. 7	13.9	— o. 9
I	5— 5	1.17	+0.02	—13.7	+ 1.0	5.8	o. 3	+11.9	— o. 7
—I	8— 5	+0.79	+0.46	+ 4.8	- 2.4	+ 1.9	+ 1.0	4.3	+ 1.9
1	6— 5	o. 68	-o. 50	- 3.2	+ 2.5	— 1. 1	— I.O	+ 2.8	2.0
_I	9— 5	+0. 16	+0.34	+ 0.9	— I. 2	+ 0.2	+ 0.5	o. 7	+ 1.0
1	7- 5	0.08	-0.29	— o. 4	+ 0.9	0, 0	— o. 3	+ o. 3	0.7
	5— 6	-0.31	+0.13						
	3-6	+0.08	-0.30				1	1	
1	6 6	+1.95	+1.36	+ 2.2	- 0.5	+ 1.7	+ 0.6	— 2. 3	+ 0.7
	4— 6	—2.0I	—1.50	- I.7	— I. 2	— I.5 — 2 I	+ 0, 2	+ 1.9 ± 2.0	+ 0.8
	7-6	+0.56	+1.58	4.4	+14.5	2. I	6.9	+ 3.9	—I2. 5
1	5 6	0.34	—1. 36	+ 4.4	—15. 6 —10. 5	+ 2. I + 0.8	+ 7·4 - 4·5	- 3.9 - 1.5	+13.4 - 9.1
	8 6	+0.10	—o. 38	+ 1.9	+10.5	— I. 2	+ 3.9	+ 2.2	+ 7.9
	6— 6	—0. IO	+0.60 0.44	- 2.7 - 2.6	— 9. I	+ 1.1	- 1.3	- 2. 2 - 2. 2	- 2.8
	9 6	+0.39	1	+ 2.6 - 2.3	+ 3.2	— 0. 9	— o. 8	+ 1.9	+ 1.9
4	7-6	0.42 0.27	+0.40 -0.08		2.0	1	- 5.5	'	1.9
	10— 6 8— 6	+0. 31 —0. 26	+0.03	1				1	
	J U	0.20	13	<u> </u>				<u> </u>	

Arg≕	Y		D''		Ε"		Н"	
$ \kappa \gamma' + i^7 g' + i g $	cos.	sin.	sin.	cos.	cos.	sin.	sin.	cos.
π i' i —I 6— 7 I 4— 7 —I 7— 7 I 5— 7 —I 8— 7 —I 9— 7 I 7— 7 —I 10— 7 I 8— 7 —I 11— 7 I 9— 7	+0.06 -0.19 +1.10 -1.22 +1.17 -1.03 -0.08 +0.24 -0.23 +0.22 -0.06 +0.03	" +0. 24 -0. 13 -0. 98 +1. 00 -0. 20 +0. 10 -0. 08 +0. 11 -0. 33 +0. 35 -0. 26 +0. 22	+0.8 +0.3 -8.6 +9.3 -6.5 +5.4	+1.5 -1.5 -0.6 +0.4 +2.7 -2.7	+0.6 -0.2 -4.1 +4.3 -2.8 +2.4 -0.7 +0.5	-1. I +1. I +0. 3 -0. 3 -1. I +1. 3 -1. 0 +0. 8	-0.7 -0.1 +7.3 -7.9 +5.6 -4.8	-1.5 +1.5 +0.5 -0.3 -2.3 +2.3

From the expression of R_0' , given in Chapter II, we derive that of $\left(\frac{\overline{dR_0'}}{d\gamma'}\right)$:

Arg=i'g'+ig	$\binom{\overline{d}}{d}$	$\frac{\overline{R_0'}}{\gamma'}$	Arg=i'g'+ig	$\left(\frac{\overline{d}}{d}\right)$	$\frac{\overline{R_0'}}{\gamma}$)
	cos.	sin.		cos.	sin.
i' i o o o o o o o o o o o o o o o o o o		-1. 10 -1. 6004n't +0. 43 -0. 0898n't +0. 06 -0. 0056n't 0. 00 -0. 09 +4. 04 -0. 65 -1. 02 +0. 01 +0. 05	i' i 2-3 3 3-3 4-3 5-3 6-3 7-3 3-4 4-4 5-4 6-4 7-4 8-4 9-4 4-5 5-5 5-5	+0. 01 -0. 11 +0. 23 +0. 20 +0. 13 -0. 01 +0. 21 +0. 07 -0. 02 +0. 02 +0. 03 +0. 01 -0. 04 +0. 04 +0. 04 +0. 05	+0. 46 +0. 14 -0. 09 +0. 02 +0. 08 -0. 01 +0. 04 +0. 08 -0. 06 -0. 03 0. 00 -0. 01 -0. 09 -0. 03
0— 2 1— 2 2— 2 3— 2 4— 2 5— 2 6— 2 1— 3	+0.051.000.25 +-0.461.030.01 +-0.25 0.00	+0.30 +0.22 -0.22 +0.29 -8.62 -0.02 -0.08 +0.04	6— 5 7— 5 8— 5 5— 6 6— 6 6— 7 7— 7	-0. 02 -0. 03 -0. 01 -0. 04 -0. 01 -0. 02 -0. 02	0. 00 -0. 02 -0. 01 -0. 03 -0. 03 +0. 02 0. 00

The terms having the argument γ' in $\delta U'$ are important, as they determine the amount of the secular motion of the plane of the orbit due to the square and product of the masses of Jupiter and Saturn. The following detail of the composition of these terms is therefore given:

$$\frac{dU'}{dg'}n'\delta z' = -0.012147 \cos \gamma' - 0.007098 \sin \gamma'$$

$$\frac{dU'}{dg'}n\delta z = -0.004190 - 0.002847$$

$$U'\left(\nu' - 2\nu + 2e + \delta \frac{h'}{h_0'}\right) = +0.002876 + 0.002141$$

$$Y'(\nu' - e' - \nu + e) = -0.013664 - 0.008705$$

$$D''\frac{u'}{\cos i'} = +0.000950 + 0.000589$$

$$E''\frac{u_1'}{\cos i} = -0.003083 - 0.002182$$

$$H''\frac{u}{\cos i} = -0.00095 - 0.000065$$

$$Sum = -0.029353 \cos \gamma' - 0.018167 \sin \gamma'$$

The following is the complete expression for $\delta U'$:

Ann good tild tid		δι	U'	
$Arg = \mathcal{H} \mathcal{Y}' + i'g' + ig'$	cos.	n't cos.	sin.	n't sin.
# i' i -I I 0 I 0 0 -I 3 0 I I 0 -I I	"0.00750.0029353 +-0.0130.0090 +-0.00890.006 +-0.00110.011 +-0.01810.0259 +-0.0120.0130.0078 +-0.020 +-0.00182	+0.00036 +0.000312 +0.0003 -0.00015 -0.002608 +0.00255 +0.000424 -0.00117 +0.000560 -0.000502 +0.000015 -0.00030 +0.00022 +0.000545 -0.00044 +0.000159	+0. 0058 -0. 018167 +0. 005 -0. 0178 +0. 0282 -0. 017 +0. 0090 +0. 008 -0. 0189 +0. 0288 -0. 0046 +0. 0097 -0. 003 +0. 003 -0. 0104 +0. 023 -0. 00899	-0.000459 -0.0009439 +0.00002 +0.000040 +0.001085 -0.00010 +0.000150 -0.00010 +0.000642 -0.000616 +0.000025 -0.000020 -0.00114 -0.000307 +0.00025 -0.0000243
I 3— 2 —I 6— 2 I 4— 2 —I 7— 2 I 5— 2 —I 10— 4	+0.005 -0.0025 +0.0016 +0.024 -0.00003 -0.01219	0. 00000 0. 000044 +-0. 000024 0. 00001 0. 0000012	+0.027 +0.0001 0.0100 0.015 +0.00009 0.00344	-0.00002 -0.000034 +0.000018 -0.00001 +0.0000035 +0.0000036

By subjecting the preceding expression to the same treatment as that by which, in Chapter II, $\frac{u'}{\cos i'}$ was derived from $\frac{\mathbf{I}}{n'}\frac{d\mathbf{R}_0{}'}{dt}$, we obtain:

Arg=i'g'+ig	81	$\overline{R_0}'$		
Alg—ty Toy	sin.	cos.		
ŝ' ŝ	" "	" "		
0 0		-0.0035+0.002012n't		
		$-0.00002994n^{2}t^{2}$		
1 0	+0.0525—0.018170n't	0. 02920. 029324 n 't		
	0.00047195 n'^2t^2	+0.00035560n ¹² t ²		
2 0	-0.0033-0.000514 <i>n't</i>	+0.0153—0.000869 <i>n't</i>		
	0. 00001322 $n^{12}t^2$	+0.00000996n ¹² t ²		
3 0	-0.0005-0.000021 <i>n't</i>	+0.0006—0.000036#/t		
	0.0000056n'2t2	$+0.00000042n^{2}t^{2}$		
4 0	o. 000001n't	0.000002n't		
ľ	o. 00000003# ^{/2} t ²	+0.00000002 <i>n</i> ′² <i>t</i> ²		
		10.000.10.0000.44		
—I— I	-0.0003+0.000111n't	+0.0009+0.000031n't		
0— 1	-0.0042+0.000961n't	+0.0135+0.000608n't		
ı— ı	+0.0027-0.000572n't	+0.0217+0.000204n't		
2 I	+0.0506+0.001505n't	+0.0547—0.001682n't		
3— 1	+0.0614—0.000011n't	+0.0203+0.000036n't		
4— 1	+0,0006—0,000002 <i>n't</i>	+0.0003+0.000000n't		
O— 2	-0.0003+0.000007n't	—0. 0001—0. 000029 <i>n't</i>		
I— 2	-0.0014+0.000057n't	-0.0004-0.000131n't		
2— 2	+0.0011-0.000038n't	-0,0006+0,000020 <i>n't</i>		
3— 2	+0.0022—0.000403 <i>n't</i>	+0.0045-0.000214n't		
4— 2	+0.0293+0.000530n't	+0. 2995+0.000746n't		
5— 2	—0. 0068—0. 000097 <i>n't</i>	0.0331+0.000000n't		
6— 2	+0.0141-0.000130n't	+0.0005—0.000103 <i>n't</i>		
7— 2	0.00100.000004 <i>n't</i>	—0. 0006—0. 000003 <i>n't</i>		
7— 4	—0.0002	+0.0001		
8— 4	-0.0051-0.000001 <i>n't</i>	+0.0014-0.000002n't		
9— 4	—0. 1820—0. 000018n't	+o. 0513—o. 000054n't		
10 4	+o. 0153	o. oo43		
	<u> </u>	<u> </u>		

In order to have $\delta\left(\frac{u'}{\cos i'}\right)$, there must be added to this the following expression:

${ m Arg}{=}i'g'{+}ig$	$\left(\overline{rac{d \mathbb{R}_0'}{d y'}} ight)$	$n'\delta z'$	
5 7 7 2	sin.	cos.	
i' i	u II	+0.0009-0.000058n't	
1 0	-0.0525+0.000000n't	$-0.0000364n'^2t^2$ +0.0292+0.00006n't	
2 0	+0.00000249n'2t'2 -0.0017-0.000054n't	-0. 00000025 <i>n</i> ¹² <i>t</i> ² -0. 0073-0. 000022 <i>n</i> ¹ <i>t</i>	
	$+0.00002282n^{12}t^2$	$-0.00005455n'^2t^2$	
3 0	0. 00050. 000026n't	+0.0038+0.000003n't	
	$+$ 0.00000159 n'^2t^2	0. 00000383n ^{/2} t ²	
4 0	+0.0042	+o. oo59	
	+0.0000008n ¹² t ²	-0.00000019 <i>n</i> /2 <i>t</i> 2	
5 0	+0.0019	-0.0011	
—3— I	0. 0030	0. 0014	
—2— I	—0. 0020	+0.0004	
—ı— ı	+0.0002-0.000029n't	-0.0015-0.000079 <i>n't</i>	
O I	+0.0004—0.000059 <i>n't</i>	-0.0014+0.000101 <i>n't</i>	
1-1	-0. 0024-0. 001340n't	_0.0018+0.001657 <i>n</i> ′ <i>t</i>	
2— I	0.0013+0.000038n't	+0.0094+0.000090n't	
3— I	-0.0119-0.001114n't	-0, 0043-0, 001708n't	
4— 1	+0.00010.000215n't	-0, 0067-0, 000077n't	
5— 1	+0.0211-0.000013n't	-0. 02370. 000006n't	
6— 1	0, 0002	+0.0012	
—2— 2	+0.0003	-0.0015	
—I— 2	-0.0003-0.000007n't	-0.0007-0.000006n't	
0— 2	+0.00040.000037n't	+0.0003+0.000027n't	
I— 2	0. 000047n't	+0.000155n't	
2— 2	-0.0014-0.000145n't	+0.0039-0.000010n't	
3— 2	+0.0034—0.003065 <i>n't</i>	0. 00540. 002289 <i>n't</i> 0. 01400. 003025 <i>n't</i>	
4 2	+0.0019-0.013739n't -0.0008+0.003120n't	-0.0140-0.003023nt -0.0010-0.001650n't	
5— 2 6— 2	-0.0008+0.003120nt -0.0122+0.007447 $n't$	o. 0074o. 011948n't	
7— 2	-0.0032+0.000417n't	o. 0000—0. 000678n't	
8— 2	+0.00026n't	-0.000042n't	
	_o. 0007	0,0001	
-r- 3	-0.0007 $-0.000012n't$	-0.00007 <i>n't</i>	
1— 3 2— 3	-0.000012nt $-0.000037n't$	+0, 000001n't	
	+0.0010 -0.000025n't	$+0.00001n^{t}$	
3— 3 4— 3	-0.0052+0.000003n't	-0.0032-0.000016n't	
5— 3	-0.0304-0.000011n't	-0.0028-0.000012n't	
6 3	+0.0047+0.000010n't	-o. 0183-0. 000030n't	
7— 3	+0.0033-0.000014n't	-0.0092-0.000008n't	
8 3	+0.0009+0.000004n't	+0.0024+0.000027n't	
9-3	-0.0005	0.0004	

Arg=i'g'+ig	$\left(rac{\overline{dR}o'}{dy'} ight)n'\delta z'$			
	sin.	cos.		
i' i 5-4 6-4 7-4 8-4 9-4 10-4 11-4 6-5 7-5 8-5 9-5 10-5 11-5 8-6 9-6 10-6	-0.0027+0.00009n't +0.0012 +0.0017+0.00005n't +0.0108-0.000012n't +0.0591+0.000023n't -0.00028n't -0.0002-0.000100n't -0.0008 -0.0006 -0.0006 -0.0006 -0.0009 -0.0009 -0.0007 +0.0006	"" +0.0021+0.00001n't +0.0065 +0.0001-0.00004n't +0.0013+0.000033n't -0.0172+0.00014n't -0.00021n't -0.0018-0.000014n't -0.0012 +0.0011 -0.0017 -0.0012 -0.0013 -0.0003 -0.0001		
9— 7	+0.0005	—u. 0005		

Then we have the following expression for $\delta\left(\frac{u'}{\cos i'}\right)$:

Arg=i'g'+ig	$\delta\left(rac{u'}{\cos i'} ight)$			
	sin.	cos.		
i' i	11 и			
1 0	— 0. 018170 <i>n't</i> —0. 00046946 <i>n'</i> 2 <i>t</i> 2	-0. 00003358 n'^2t^2 -0. 029318 $n't$ +0. 00035535 n'^2t^2		
2 0	-0.0050-0.000568 $n't$ +0.00000960 n'^2t^2	+0.0080-0.000891 <i>n't</i> -0.00004459 <i>n'</i> ² <i>t</i> ²		
3 0	-0.0010-0.000047 $n't$ +0.00000103 n'^2t^2	+0.00440.000033 <i>n't</i> 0.00000341 <i>n'</i> 2 <i>t</i> 2		
4 0	+0.0042-0.000001n't $+0.00000005n'2t^2$	+0.0059-0.000002n't 0.00000017n'2f2		
5 0	+0.0019	0.0011		
3 I 2 I I I 0 I I I 2 I	-0.0030 -0.0020 $-0.0001+0.000082n't$ $-0.0038+0.000902n't$ $+0.0003-0.001912n't$ $+0.0493+0.001543n't$	-0. 0014 +0. 0004 -0. 0006-0. 000048n't +0. 0121+0. 000709n't +0. 0199+0. 001861n't +0. 0641-0. 001592n't		

Arg=i'g'+ig	δ($\delta\left(rac{u'}{\cos i'} ight)$			
111g—09 09	sin.	cos.			
i' i	n II	n 11			
3— І	+0.0495-0.001125n't	+0.0160-0.001672n't			
4— 1	+0.0007-0.000217 <i>n't</i>	—o. 0064—o. 000077 <i>n</i> ′ <i>t</i>			
5— I	+0.0211—0.000013 <i>n't</i>	-0.0237-0.000006 <i>n't</i>			
6— 1	—0.0002	+0.0012			
—2— II	+0.0003	-0.0015			
—I— 2	o. 0003o. 000007 <i>n't</i>	-0.0007-0.000006 <i>n</i> ′ <i>t</i>			
0— Z	+0.0001—0.000030n't	+0.0002—0.000002 <i>n</i> ′ <i>t</i>			
I 2	-0.0014+0.000010n't	-0.0004+0.000024 <i>n</i> ′ <i>t</i>			
2- 2	0.00030.000183 <i>n't</i>	+0.0033+0.000010n't			
3— 2	+0. 0056-0. 003468n't	—0. 0009—0. 002503 <i>n't</i>			
4 2	+0. 03120. 013209 <i>n't</i>	+0. 2855—0. 002279n't			
5— 2	-0.0076+0.003023n't	o. 0341o. 001650 <i>n't</i>			
6— 2	+0.0019+0.007317 <i>n't</i>	o. 0069o. 012051 <i>n't</i>			
7— 2	-0.0043+0.000413 <i>n't</i>	—0. 0006—0. 000681 <i>n't</i>			
8— 2	+0.000026n't	0. 000042n't			
-ı- 3	+0.0007	0, 0001			
I 3	—0. 00001 <i>2n't</i>	—0.000007 <i>n</i> ′ <i>t</i>			
2— 3	—o. 000037 <i>n't</i>	+0.000001 $n't$			
3— 3	+0.0010-0.000025n't	+0.0002+0.000013n't			
4 3	-0.0052+0.000003n't	o. 0032o. 000016 <i>n</i> ′ <i>t</i>			
5 3	-0. 0304-0. 00001 In't	o. 0028o. 00001 <i>2n't</i>			
6 3	+0.0047+0.000010n't	o. 0183o. 000030 <i>n't</i>			
7— 3	+ o . 0033—0. 000014 <i>n't</i>	—0, 0092—0. 000008n't			
8— 3	+0.0009+0.000004 <i>n</i> ′ <i>t</i>	+0.0024+0.000027 <i>n</i> ′ <i>t</i>			
9— 3	0.0005	0.0004			
5— 4	—0. 0027+0. 000009 <i>n</i> /t	+0.0021+0.000001n't			
6 4	+0.0012	+0.0065			
7— 4	+0.0015+0.000005n't	+0.0002-0.000004n't			
8— 4	+0.0057—0.00001 <i>3n't</i>	+0.0027+0.000031n't			
9— 4	-0. 1229+0. 000005n't	+0.0341+0.000050n't			
10— 4	+0.0153 $-$ 0.000028 $n't$	0.00430.000021 <i>n</i> ′ <i>t</i>			
11-4	-0.0002 $-$ 0.000100 $n't$	o. 0018o. 000014n't			
6— 5	o. ooo8	-0.0001			
7 5	— 0. 0030	+0.0012			
8 5	—o. oooб	+0.0011			
9— 5	0.0000	-0.0017			
10 5	—0. 0006	-0.0012			
11— 5	—0, 0009	0.0006			
8— 6	~-0.0009	-0.0013			
9— 6	-0.0007	0.0003			
10— 6	+0.0006	-0.000I			
9— 7	+0.0005	o. ooo5			

As in the case of Jupiter the only terms in the latitude of Saturn of three dimensions, which seem large enough to be taken account of, are the secular terms proportional to the cube of the time. According to Leverrier* we have

$$\sin i' \sin \theta' = ... + 0.015774 \sin (126 5 44 - 25.89t)$$

 $\sin i' \cos \theta' = ... + 0.015774 \cos (126 5 44 - 25.89t)$

But here θ' is counted from the equinox of 1800.0. Adding therefore 41' 53', the amount of precession for 50 years, the formulæ become

$$\sin i' \sin \theta' = ... + 0.015774 \sin (126 47 37 - 25.89t)$$

 $\sin i' \cos \theta' = ... + 0.015774 \cos (126 47 37 - 25.89t)$

Whence we deduce that the sine of the latitude of Saturn, referred to the fixed ecliptic of 1850.0, contains the terms

$$\sin b' = -$$
 o".ooo858T³ $\sin l' +$ o".ooo641T³ $\cos l'$

^{*}Annales de l'Observatoire de Paris, Mémoires, Tome II, p. 157.

CHAPTER XXVI.

FORMULÆ FOR THE MOTION OF THE PLANE OF THE ECLIPTIC AND FOR PRECESSION.

The subject announced in the title of this chapter properly belongs to the solar theory and the general stellar theory. But in order that the preceding theory may be compared, in a satisfactory manner, with observation, it is necessary to be able to reduce the theoretical positions of our planets to the moving planes of reference unavoidably employed by observers. The formulæ given by Leverrier or Hansen might be used for this purpose; but there is one imperfection attached to them: they are limited to the first and second powers of the time. On account of the lengthened series of observations we now possess it seems desirable to add to the formulæ the terms multiplied by the third power of the time. I have therefore made a partially independent investigation of this subject. The reader is, however, advised that this is only to serve a temporary purpose, and will be superceded when the solar theory, in other hands, shall have been finished.

Availing ourselves of the tables of the coefficients of the secular portion of the perturbative function given by Leverrier*, the rate of motion of the ecliptic has been computed for the three epochs 1600, 1850, and 2100. Thence have been inferred the two equations giving the position of the ecliptic of any date with reference to that of 1850. The following details are all it is thought necessary to give of this work.

The elements of the planets involved in the computation are, for each of the three epochs, the following:

	Date.	e	J	П	II'	π — Π'
Mercury .	1600 1850 2100	o. 2055529 o. 2056048 o. 2056561	0 / // 6 59 51.58 7 0 7.71 7 0 23.14	0 / // 27 38 49.01 28 34 4.99 29 29 24.41	52 29 13. 15 53 48 31. 10 55 8 1. 40	0 / // 47 4 44.97 46 33 8.63 46 1 28.61
Venus	1600 1850 2100	o. oo69689 o. oo68431 o. oo67189	3 23 25.47 3 23 35.01 3 23 44.53	52 53 6. 24 54 7 49.75 55 21 2. 38	22 59 17.01 25 1 46.65 27 4 20.21	76 34 41.11 75 19 53.08 74 5 9.80
Earth	{ 1600 1850 2100	o. 0168764 o. 0167711 o. 0166642			π 99 33 58.12 100 21 39.73 101 9 30.01	

^{*}Annales de l'Observatoire de Paris, Mémoires, Tome II, pp. 94-96,

	Date.	e	J	П	II'	π—Π
Mars	1600 1850 2100	o. 0930287 u. 0932680 o. 0935058	0 / // 1 51 8.91 1 51 2.24 1 50 56.75	0 ' '' 49 37 43. 23 51 57 45. 14 54 18 36. 97	282 14 55.75 284 53 57.15 287 33 40.79	0 , , , ,, 49 56 1 4. 89 48 23 54. 59 46 50 53. 04
Jupiter .	1600	o. 0478384	1 19 33.49	359 39 49 79	271 28 41.54	99 54 8.33
	1850	o. 0482580	1 18 42.10	1 25 19 94	272 58 11.39	98 56 19.79
	2100	o. 0486717	1 17 50.89	3 10 56 45	274 28 10.06	97 58 33.56
Saturn	1600	o. 0561499	2 30 14.84	345 54 49. 18	335 3 54. 64	113 39 8.94
	1850	o. 0560647	2 29 40.19	348 0 50. 68	337 46 8. 50	112 20 49.05
	2100	o. 0559786	2 29 4.84	350 7 20. 96	340 29 3. 36	111 2 9.05
Uranus .	{ 1600	o. 0464082	0 46 16.27	24 5 39·4	95 8 20.8	75 28 18.7
	1850	o. 0463414	0 46 19.72	27 7 45·3	97 36 12.7	73 13 54.4
	2100	o. 0462756	0 46 24.93	30 9 20.6	100 3 21.4	71 0 9.4
Neptune.	\begin{cases} 1600 \\ 1850 \\ 2100 \end{cases}		1 48 28.84 1 47 2.13 1 45 36.00			130 52 51.4 130 6 25.1 129 19 55.1

With these values of the elements have been computed the values of the two functions

$$-\frac{d\left(\frac{a'}{\triangle}\right)}{d\mathbf{J}} \qquad \qquad -\frac{\mathbf{I}}{\sin\mathbf{J}}\left[\cos\mathbf{J}\frac{d\left(\frac{a'}{\triangle}\right)}{d\mathbf{I}\mathbf{I}} + \frac{d\left(\frac{a'}{\triangle}\right)}{d\mathbf{I}\mathbf{I}'}\right]$$

(a' must be understood as belonging to the exterior of the two planets). The following are the results obtained:

	Date.	First function.	Second function.		Date.	First function.	Second function.
Mercury .	1600 1850 2100	o. 0186901 o. 0187709 o. 0188533	+0.0021313 +0.0021840 +0.0022337	Saturn	{ 1600 1850 2100	o. 0000386728 o. 0000385239 o. 0000383720	-0.000000065 -0.000000053 -0.000000042
Venus	1600 1850 2100	o. 09254530 o. 09260720 o. 09266871	0, 00001803 0, 00001370 0, 00000945	Uranus .	1600 1850 2100	0. 0000014416 0. 0000014435 0. 0000014463	+0.000000006 +0.0000000006 +0.0000000007
Mars	1600 1850 2100	o. 0229324 o. 0229104 o. 0228855	0.0000471 0.0001189 0.0001901	Neptune.	1600 1850 2100	o. 0000008752 o. 0000008636 o. 0000008520	o o o
Jupiter .	\begin{cases} 1600 \\ 1850 \\ 2100 \end{cases}	o. 0001327178 o. 0001313057 o. 0001298985	+0.000000952 +0.000000993 +0.000001029				

In computing these quantities all the terms given by LEVERRIER have been employed. In the case of the action of Mars it was found that the terms of the fifth order, with respect to the eccentricities and inclination, amount to about one per cent.

of those of the first order, thus showing a lack of rapid convergence. Hence, it appears very desirable that the secular action of Mars on the Earth should be determined by the use of Gauss' method.

If we put the first of the two quantities just obtained, equal to $k \cos K$, and the second equal to $k \sin K$, the rate of motion of the ecliptic of date, in reference to the ecliptic of 1850.0, is given by the formulæ

$$\frac{d(\sin i \sin \theta)}{dt} = \frac{n}{\sqrt{1-e^2}} \frac{m'}{1+m} k \cos (\pi - \Pi' - K)$$

$$\frac{d(\sin i \cos \theta)}{dt} = -\frac{n}{\sqrt{1-\theta^2}} \frac{m'}{1+m} k \sin (\pi - \Pi' - \mathbb{K})$$

in the case of the action of an interior planet. For the action of an exterior planet $\pi - \Pi$ is substituted for $\pi - \Pi'$. If the unit of t is the Julian year, and the coefficients are to be expressed in seconds of arc, we have, severally, for the three epochs:

Date.	$\log\left(\frac{n}{\sqrt{1-e^2}}\frac{1}{1+m}\right)$
1600	6. 1126579
1850	6. 1126572
2100	6. 1126564
1	<u></u>

It is now easy to find the action of each planet in changing the position of the plane of the ecliptic when the value of its mass is known. In the cases of Mercury, Venus, and Uranus the values here adopted differ somewhat from those given in Chapter I:

	$\frac{1}{m'}$	$rac{d(\sini\sin heta)}{dt}$			
	m'	1600.	1850.	2100.	
		"	"		
Mercury	7500000	+0.0024694	+0.0025049	+0.0025401	
Venus	408134	+0.0681659	+0.0744329	+0.0806656	
Mars	3093500	+0.0061692	+0.0063362	+0,0065001	
Jupiter	1047. 879	o. o28115o	-0. 0251149	0. 0221690	
Saturn	3501.6	o. oo57453	0.0054237	0.0050999	
Uranus	22640	+0.0000207	+0.0000239	+0.0000270	
Neptune	19700	0. 0000377	0. 0000366	-0.0000356	
Sum =		+0.0429272	+0.0527227	+0.0624283	

	$rac{d(\sini\cos heta)}{dt}$			
	1600.	1850.	2100.	
	"	"	"	
Mercury	-0.0021146	— 0. 0020956	0. 0020767	
Venus	-0. 2858925	-0. 2845280	—o. 2830271	
Mars	—o. oo73665	-0.0072112	-0. 0070499	
Jupiter	—o. 1617 37 8	—0. 1604628	— 0. 1591487	
Saturn	o. 013111 7	-0.0131883	0. 0132566	
Uranus	0. 0 000799	0. 0000791	0. 0000783	
Neptune	o. 000043 5	0. 0000435	-0.0000434	
Sum =	0. 4703465	o. 4676085	—o. 4646 8 07	

From these data, adopting the century as the unit of time, it is easy to derive the following formulæ:*

$$\sin i \sin \theta = + 5.2723\text{T} + 0.19501\text{T}^2 - 0.000240\text{T}^3$$

 $\sin i \cos \theta = -46.7608\text{T} + 0.05666\text{T}^2 + 0.000506\text{T}^3$

Whence also

$$\cos i = 1 - [92.4155]T^2 + [89.58]T^3$$

In deriving suitable formulæ for precession we set out from the exceedingly simple differential equations first stated by Poisson

$$\frac{d\omega}{dt} = \frac{1}{\operatorname{C} n \sin \omega} \frac{dV}{d\psi} \qquad \qquad \frac{d\psi}{dt} = -\frac{1}{\operatorname{C} n \sin \omega} \frac{dV}{d\omega}$$

where

$$\nabla = -\frac{3}{2} \left(C - \frac{A + B}{2} \right) \left[m' \frac{z'^2}{r'^5} + m'' \frac{z''^2}{r''^5} \right]$$

Here ω denotes the inclination of the equator to a fixed plane, ψ the amount of backward motion of its node on this plane, A, B, and C are the moments of inertia of the Earth about its principal axes, C being supposed to belong to the axis of rotation, n is the angular velocity of this rotation, supposed constant, m' and m'' are the masses severally of the Sun and Moon, r' and r'' the distances of their centers from the center of the Earth, and z' and z'' the projection of these distances on a plane perpendicular to the equator. However, denoting by δ' and δ'' the declinations of the two bodies, it is better to write V thus

$$V = -\frac{3}{2} \left(C - \frac{A + B}{2}\right) \left[\frac{m'}{r'^3} \sin^2 \delta' + \frac{m''}{r''^3} \sin^2 \delta''\right]$$

^{*}Leverrier's value of the coefficient of T², in the expression for sin i sin θ, +0".1964 (Annales, Tome II, p. 104), appears to agree with that found here. But Hansen and Olufsen's value, +0".1887 (Tables du Soleil. p. 21), seems to be in error; at least I am unable otherwise to explain the discordance.

Were there a third body producing sensible motion in the axis of the Earth it would be only necessary to add to the last factor of V a term altogether similar to the two which are already there.

When we treat precession alone it suffices to substitute for the terms $\frac{m'}{r'^3}\sin^2\delta' + \frac{m''}{r''^3}\sin^2\delta''$ their secular portions. In the case of the first of these, neglecting all periodic perturbations, we can assume that the Sun moves about the Earth in an ellipse whose elements are slowly changing. Assuming that the ecliptic of 1850.0 is the fixed plane of reference for the measurement of ω and ψ , if β' and λ' denote the latitude and longitude of the Sun referred to the ecliptic and mean equinox of the same date, we have

$$\sin \delta' = \sin \beta' \cos \omega + \cos \beta' \sin \omega \sin (\lambda' + \psi)$$

But taking the orbit longitude l' of the Sun we have

$$\cos \beta' \cos (\lambda' - \theta) = \cos (l' - \theta)$$

$$\cos \beta' \sin (\lambda' - \theta) = \cos i \sin (l' - \theta)$$

$$\sin \beta' = \sin i \sin (l' - \theta)$$

Here i and θ denote the quantities which have been thus designated in the just concluded treatment of the motion of the ecliptic. By substituting these values in the equation for $\sin \delta'$ we get

$$\sin \delta' = [\sin i \cos \omega + \cos i \sin \omega \cos (\psi + \theta)] \sin (l' - \theta) + \sin \omega \sin (\psi + \theta) \cos (l' - \theta)$$

From the theory of elliptic motion we know that $\frac{a^3}{r^3}\cos 2f$ and $\frac{a^3}{r^3}\sin 2f$ have no non-periodic terms. Thus, for $\sin^2 \delta'$, in the expression of V, one may substitute

$$\frac{\mathrm{I}}{2}[\sin\,i\,\cos\,\omega+\cos\,i\,\sin\,\omega\,\cos\,(\psi\,+\,\theta)]^2+\frac{\mathrm{I}}{2}\mathrm{sin}^2\,\omega\,\sin^2\left(\psi\,+\,\theta\right)$$

and for $\frac{a'^3}{r'^3}$ may be substituted its non-periodic term $(1-e'^2)^{-\frac{3}{2}}$. But calling the mean obliquity of date ω' , and ψ' the general precession, the formulæ, which connect ω' , ψ' with ω , ψ are

$$\begin{array}{ll} \sin \, \omega' \sin \, (\psi' + \theta) = & \sin \, \omega \sin \, (\psi + \theta) \\ \sin \, \omega' \cos \, (\psi' + \theta) = \sin \, i \cos \, \omega + \cos \, i \sin \, \omega \cos \, (\psi + \theta) \\ \cos \, \omega' & = \cos \, i \cos \, \omega - \sin \, i \sin \, \omega \cos \, (\psi + \theta) \end{array}$$

As the addition or subtraction of a function independent of ω and ψ to V does not impair its use for our purposes, it is plain we may substitute for $\sin^2 \delta'$

$$-\frac{1}{2}\cos^2\omega' = -\frac{1}{2}[\cos i\cos\omega - \sin i\sin\omega\cos(\psi + \theta)]^2$$

To ascertain the non-periodic part of $\frac{\sin^2 \delta''}{r''^3}$ is more difficult, as the solar perturbations of the Moon have to be considered. However, some simplifications occur.

It is well known that the plane of the Moon's orbit follows the ecliptic in its motion. Then, if β'' and $\lambda'' + \psi'$ denote the latitude and longitude of the Moon referred to the ecliptic and mean equinox of date,

$$\sin \delta'' = \sin \beta'' \cos \omega' + \cos \beta'' \sin \omega' \sin (\lambda'' + \psi')$$

$$\frac{\sin^2 \delta''}{r''^3} = \frac{\sin^2 \beta''}{r''^3} \cos^2 \omega' + \frac{\sin 2\beta''}{r''^3} \sin (\lambda'' + \psi') \sin \omega' \cos \omega'$$

$$+ \frac{1}{2} \frac{\cos^2 \beta''}{r''^3} \sin^2 \omega' - \frac{1}{2} \frac{\cos^2 \beta''}{r''^3} \cos 2(\lambda'' + \psi') \sin^2 \omega'$$

Now it is evident that the two terms of the last equation, which have the factors $\sin(\lambda'' + \psi')$ and $\cos 2(\lambda'' + \psi')$, are wholly periodic, and thus may be rejected. Furthermore, from the expression we may subtract $\frac{\sin^2 \beta''}{r''^3}$, which does not contain ω or ψ . Thus, for our purpose, we may substitute for $\frac{\sin^2 \delta''}{r''^3}$

$$\frac{1}{2} \frac{1-3\sin^2\beta''}{r''^3} \sin^2\omega'$$

The non-periodic term of the first factor of this, corresponding to elliptic values for the co-ordinates, is readily discovered. For the non-periodic term of $\frac{a''^3}{r''^3}$ is $(1-e''^2)^{-\frac{3}{2}}$, and the orbit longitude and the longitude of the node of the Moon being denoted by l'' and Ω'' and its inclination by i''

$$\sin^2\beta'' = \sin^2i'' \, \sin^2(l'' - \Omega'') = \frac{1}{2} \, \sin^2i'' - \frac{1}{2} \, \sin^2i'' \, \cos\, 2(l'' - \Omega'')$$

But, as before mentioned, $\frac{a''^3}{r''^3}\cos 2(l''-\Omega'')$ does not contain any non-periodic term. Hence, the non-periodic part of $\frac{a''^3}{r''^3}(1-3\sin^2\beta'')$ is

$$(1 - e^{\prime\prime 2})^{-\frac{3}{2}} \left(1 - \frac{3}{2} \sin^2 i^{\prime\prime}\right)$$

To obtain the terms of the constant part of this function, which arise from solar perturbation, we take from Pontécoulant* the following terms of $\frac{a''^3}{r''^3}$:

$$\frac{a''^3}{r''^3} = (\mathbf{1} - e''^2)^{-\frac{3}{2}} + \frac{\mathbf{1}}{2}m^2 - \frac{9}{3^2}m^4 + \frac{55}{16}m^5 + \frac{2159}{96}m^6$$

$$+ \left[\frac{771}{128}m^2 + \frac{8145}{256}m^3 + \frac{681789}{4096}m^4\right]e''^2$$

$$+ \left[\frac{3}{4}m^2 + \frac{153}{64}m^3 + om^4\right]e'^2$$

$$+ \left[3m^2 + \frac{19}{2}m^3 + \frac{135}{6}me''^2\right]\cos 2\mathcal{E}$$

$$+ 3e''\cos \varphi + \frac{45}{8}me''\cos (2\mathcal{E} - \varphi)$$

^{*} Théorie Analytique du Systême du Monde, Tome IV, pp. 216, 226, 303.

From the value of $\sin^2 \beta''$ we have *

$$\mathbf{1} - 3\sin^2\beta'' = \mathbf{1} - \frac{3}{2}\gamma^2 \left[\mathbf{1} + \frac{9}{64}m^2 + \frac{\mathbf{14}\mathbf{1}}{128}m^3 + \frac{7103}{2048}m^4 + \frac{771}{256}m^2e''^2 + \frac{463}{64}m^2e'^2 - \left(\frac{3}{4}m + \frac{3}{16}m^2 \right)\cos 2\xi + \frac{109}{16}m^2e'' \cos \varphi + \frac{3}{2}me'' \cos (2\xi - \varphi) \right]$$

By the multiplication of these factors it is found that the constant term of $\frac{a''^3}{r''^3}(1-3\sin^2\beta'')$, which we denote by N, is

$$\begin{split} \mathbf{N} &= (\mathbf{1} - e^{\prime\prime 2})^{-\frac{3}{2}} \left(\mathbf{1} - \frac{3}{2} \sin^2 i^{\prime\prime} \right) + \frac{1}{2} m^2 - \frac{9}{32} m^4 + \frac{55}{16} m^5 + \frac{2159}{96} m^6 \\ &+ \left[\frac{771}{128} m^2 + \frac{8145}{256} m^3 + \frac{681789}{4096} m^4 \right] e^{\prime\prime 2} \\ &+ \left[\frac{3}{4} m^2 + \frac{153}{64} m^3 + 0 m^4 \right] e^{\prime 2} \\ &- \left[\frac{123}{128} m^2 - \frac{9}{256} m^3 + \frac{8853}{2048} m^4 \right] \gamma^2 \\ &- \frac{13329}{512} m^2 e^{\prime\prime 2} \gamma^2 - \frac{1533}{128} m^2 e^{\prime 2} \gamma^2 \end{split}$$

This quantity may be regarded as absolutely constant, as e'^2 , the only symbol which varies in it, is multiplied by a small factor. However, if it is desired to consider its variability, the resultant term unites with the similar term arising from the action of the Sun, and the final formulæ are not rendered thereby more complex. On substitution of the numerical values of the quantities involved, it is found that at the epoch 1850

$$N = 0.9952929$$

It will be seen that the two terms of V involve severally the factors $\frac{m'}{a'^3}$ and $\frac{m''}{a''^3}$. But it will be more convenient to replace them by the following equivalents:

$$\frac{m'}{a'^3} = \frac{m'}{m+m'}n'^2 \qquad \qquad \frac{m''}{a''^3} = \frac{m''}{m+m''}n''^2$$

where m denotes the mass of the Earth.

If, therefore, we put

$$\mathbf{H} = \frac{3}{4} \frac{\mathbf{C} - \frac{\mathbf{I}}{2}(\mathbf{A} + \mathbf{B})}{\mathbf{C}} \left[\frac{m'}{m + m'} \frac{n'^2}{n^2} (\mathbf{I} - e'^2)^{-\frac{3}{2}} + \frac{m''}{m + m''} \frac{n''^2}{n^2} \mathbf{N} \right]$$

it will be perceived that this quantity is independent of the assumed units of measurement; moreover it is nearly constant, its variability arising from that of e^{2} . It is sufficiently accurate to assume that it is of the form a + bt. If we put

$$\Omega = H \cos^2 \omega' = \dot{H} [\cos i \cos \omega - \sin i \sin \omega \cos (\psi + \theta)]^2$$

our differential equations become

$$\frac{1}{n}\frac{d\omega}{dt} = \frac{1}{\sin \omega}\frac{d\Omega}{d\psi} \qquad \qquad \frac{1}{n}\frac{d\psi}{dt} = -\frac{1}{\sin \omega}\frac{d\Omega}{d\omega}$$

These equations fulfill the law of dimensions as the left members are the ratios of two angular velocities, and the right members also are functions of ratios. They can be written

$$\begin{split} \frac{d\omega}{dt} &= 2 \text{H} n \sin i \cos \omega' \sin (\psi + \theta) \\ \frac{d\psi}{dt} &= 2 \text{H} n \cos \omega' \left[\cos i + \sin i \cot \omega \cos (\psi + \theta) \right] \end{split}$$

It is convenient to have differential equations determining ω' and ψ' directly, and thus avoid the arriving at them through the mediation of ω and ψ . It is plain from the preceding expressions for Ω and the differential equations for ω and ψ that the complete differential of $\cos \omega'$ is equal to the partial differential of its equivalent in terms of ω and ψ taken with respect to t as far as it is implicitly involved. This gives

$$\frac{d \cdot \cos \omega'}{dt} = -\left[\sin i \cos \omega + \cos i \sin \omega \cos (\psi + \theta)\right] \frac{di}{dt} + \sin i \sin \omega \sin (\psi + \theta) \frac{d\theta}{dt}$$
$$= -\sin \omega' \cos (\psi' + \theta) \frac{di}{dt} + \sin i \sin \omega' \sin (\psi' + \theta) \frac{d\theta}{dt}$$

Consequently

$$\frac{d\omega'}{dt} = \cos(\psi' + \theta)\frac{di}{dt} - \sin i \sin(\psi' + \theta)\frac{d\theta}{dt}$$

In order to arrive at an expression for $\frac{d\psi'}{dt}$, we differentiate the first of the equations which show the relation of ω' , ψ' to ω , ψ . Thus

$$\cos \omega' \sin (\psi' + \theta) d\omega' + \sin \omega' \cos (\psi' + \theta) (d\psi' + d\theta) = \cos \omega \sin (\psi + \theta) d\omega + \sin \omega \cos (\psi + \theta) (d\psi + d\theta)$$

Substituting in the right member of this the values of $d\omega$ and $d\psi$ which have been just given, it reduces to

$$2Hn \sin \omega' \cos \omega' \cos (\psi' + \theta)dt + [\cos i \sin \omega' \cos (\psi' + \theta) - \sin i \cos \omega']d\theta$$

Also employing the valve of $d\omega'$, previously given, the equation is transformed into

$$\sin \omega' \cos (\psi' + \theta) d\psi' = 2 \operatorname{H} n \sin \omega' \cos \omega' \cos (\psi' + \theta) dt - \cos \omega' \sin (\psi' + \theta) \cos (\psi' + \theta) di$$
$$- \left[2 \sin^2 \frac{i}{2} \sin \omega' \cos (\psi' + \theta) + \sin i \cos \omega' - \sin i \cos \omega' \sin^2 (\psi' + \theta) \right] d\theta$$

Whence we derive

$$\frac{d\psi'}{dt} = 2 \operatorname{H} n \cos \omega' - \cot \omega' \sin (\psi' + \theta) \frac{di}{dt} - \left[2 \sin^2 \frac{i}{2} + \sin i \cot \omega' \cos (\psi' + \theta) \right] \frac{d\theta}{dt}$$

The expressions for $\frac{d\omega'}{dt}$ and $\frac{d\psi'}{dt}$ can be simplified by putting

$$k \cos K = -\sin \theta \frac{di}{dt} - \sin i \cos \theta \frac{d\theta}{dt} = -\frac{dp}{dt} - p \tan \frac{i}{2} \frac{di}{dt}$$
$$k \sin K = \cos \theta \frac{di}{dt} - \sin i \sin \theta \frac{d\theta}{dt} = \frac{dq}{dt} + q \tan \frac{i}{2} \frac{di}{dt}$$

where p and q have the usual significations

$$p = \sin i \sin \theta$$
 $q = \sin i \cos \theta$

Then the two differential equations take the form

$$\begin{split} \frac{d\omega'}{dt} &= k \sin (\psi' + \mathbf{K}) \\ \frac{d\psi'}{dt} &= {}_{2}\mathbf{H}n \cos \omega' - {}_{2} \sin^{2}\frac{i}{2}\frac{d\theta}{dt} + k \cot \omega' \cos (\psi' + \mathbf{K}) \ . \end{split}$$

They are readily integrated in powers of the time by the use of Maclaurin's Theorem. Let us suppose that at the epoch 1850.0 we have $\omega' = 23^{\circ}27'31''.83$, $\frac{d\psi'}{dT} = 5025''.787$. $_{2}Hn$ is diminishing at the rate of 0''.003656 in a century. The term $_{2}\sin^{2}\frac{i}{2}\frac{d\theta}{dT}$, which is excessively small, is equivalent to $_{2}\sin^{2}\frac{i}{2}\frac{d\theta}{dT}$. With these have been calculated, at intervals of 500 years, the following quantities:

$\log k$	К	<i>∞′</i>	ψ′
	0 / //	0 / //	U / //
1. 6790634	268 26 24.02	23 35 16.72	13 55 46.39
1.6758217	266 0 11.29	23 31 25.20	— 6 58 21.06
1.6726250	263 34 1.36	23 27 31.83	0 0 0.00
1.6694575	261 7 42.41	23 23 38.08	+ 6 59 16.80
1.6663071	258 41 0.53	23 19 45.42	+13 59 29.35
	1. 6790634 1. 6758217 1. 6726250 1. 6694575	1. 6790634 268 26 24. 02 1. 6758217 266 0 11. 29 1. 6726250 263 34 1. 36 1. 6694575 261 7 42. 41	1. 6790634 268 26 24. 02 23 35 16. 72 1. 6758217 266 0 11. 29 23 31 25. 20 1. 6726250 263 34 1. 36 23 27 31. 83 1. 6694575 261 7 42. 41 23 23 38. 08

The rates of motion of ω' and ψ' can be obtained from the differential equations. They are

Date.	$rac{d\omega'}{d ext{T}}$	$rac{d\psi'}{d ext{T}}$
ł	"	,,
850	<u>-46. 02522</u>	+5003. 78451
1350	46. 53860	5014. 73750
1850	46. 76080	5025. 78700
2350	46. 68988	5036. 86128
2850	-46. 32694	+5047.88573

From these quantities are inferred the formulæ

$$\begin{aligned} \omega' &= 23^{\circ}27'31''.83 - 46''.7608T - 0''.00757T^{2} + 0''.001956T^{3} \\ \psi' &= 5025''.7870T + 1''.10739T^{2} + 0''.000174T^{3} - 0''.0000488T^{4} - 0''.00000023T^{5} \end{aligned}$$

which substantially give again the values of ω' and ψ' employed in computing the rates of motion.

CHAPTER XXVII.

REFERENCE OF THE LONGITUDES AND LATITUDES OF JUPITER AND SATURN TO THE MEAN EQUINOX AND ECLIPTIC OF DATE.

In order to have the greatest simplicity in the formulæ we assume, in the case of each planet, the mean plane of its orbit at the epoch 1850.0 as the plane from which its latitude in the first instance is to be counted. In the interval, 1600-2100, that is, 250 years on each side of the epoch, the maximum latitude of Jupiter, referred thus to its plane, will be about 40"; the similar quantity for Saturn will be about 58". Thus we can put $\cos i = 1$, $\cos b = 1$ whenever they multiply quantities of the order of the disturbing forces. Then, in Hansen's equations (21)*, we have $i_0 = 0$, n = 2, and they become

$$\cos b \sin (l - \theta_0 - \Gamma) = \sin (f + \pi - \theta_0) - \frac{1}{2} sq$$

$$\cos b \cos (l - \theta_0 - \Gamma) = \cos (f + \pi - \theta_0) + \frac{1}{2} sp$$

$$\sin b = s$$

From these we derive

$$\cos b \sin (l - f - \pi - \Gamma) = -\frac{1}{2} sq \cos (f + \pi - \theta_0) - \frac{1}{2} sp \sin (f + \pi - \theta_0)$$

$$\cos b \cos (l - f - \pi - \Gamma) = 1 + \frac{1}{2} sp \cos (f + \pi - \theta_0) - \frac{1}{2} sq \sin (f + \pi - \theta_0)$$

But

$$p \cos (v - \theta_0) - q \sin (v - \theta_0) = -s$$

$$q \cos (v - \theta_0) + p \sin (v - \theta_0) = \frac{ds}{dv}$$

Consequently

$$\cos b \cos (l - f - \pi - \Gamma) = \mathbf{1} - \frac{1}{2} s^2$$

$$\cos b \sin (l - f - \pi - \Gamma) = -\frac{1}{2} s \frac{ds}{dv}$$

Neglecting terms of the fourth order with respect to disturbing forces these equations give

$$l = f + \pi + \Gamma - \frac{1}{2} s \frac{ds}{dv}$$

Thus, $f + \pi$ denoting the amount of description of angle by the radius vector, the two latter terms of the equation represent the reduction required to refer this angle to the chosen fixed plane.

Since $s = \frac{a_0}{\bar{r}}u$, for the computation of Γ , we have *

$$\Gamma = \frac{1}{2 \cos \varphi_0} \int a_0^2 \frac{d\Omega}{dZ} u n dt$$

The second term of the reduction can be made to undergo the following transformations:

$$-\frac{1}{2}s\frac{ds}{dv} = -\frac{1}{4}\frac{\overline{r}^2(1+\nu)^2}{a^2\cos\varphi}\frac{d\cdot s^2}{ndt} = -\frac{1}{4}\frac{\overline{r}^2}{a^2\cos\varphi}\frac{d\cdot \left(\frac{a^2}{r^2}u^2\right)}{ndt}$$
$$= -\frac{1}{4\cos\varphi}\left[\frac{d\cdot u^2}{ndt} - 2\frac{d\cdot\log\overline{r}}{ndt}\cdot u^2\right]$$

In the case of Jupiter it is found that the largest terms of Γ are

$$\Gamma = -0''.0001 \sin(5g' - 2g) - 0''.0002 \cos(5g' - 2g)$$

it is therefore quite insignificant. For the second term it is sufficient to take

$$u^{2} = + 0.00000023n^{2}t^{2} - 0.00000015n^{2}t^{2} \cos(-2g) + 0.00000017n^{2}t^{2} \sin(-2g)$$

$$\frac{d \cdot u^{2}}{ndt} = + 0.00000046nt - 0.00000030n^{2}t^{2} \sin(-2g) - 0.00000034n^{2}t^{2} \cos(-2g)$$

Thence, with sufficient approximation,

$$-\frac{1}{2}s\frac{ds}{dx} = + \circ''.000000075n^2t^2\sin(-2g) + \circ''.000000083n^2t^2\cos(-2g)$$

In the case of Saturn we have

^{*}Auseinandersetzung, Abth. I, s. 81, gl. (23).

Let i denote the inclination of the plane of the primitive orbit on the ecliptic of date, and θ the longitude of its ascending node, counted on the plane of the primitive orbit from the same point of departure as for l, and Ω the longitude of the same node, counted on the plane of the ecliptic of date from the mean equinox of date. Then, if λ and β denote the longitude and latitude of the planet referred to the mentioned equinox and ecliptic, we shall have

$$\sin \beta = \cos i \sin b + \sin i \cos b \sin (l - \theta)$$

$$\cos \beta \sin (\lambda - \Omega) = -\sin i \sin b + \cos i \cos b \sin (l - \theta)$$

$$\cos \beta \cos (\lambda - \Omega) = \cos b \cos (l - \theta)$$

In these equations i, θ , and α depend only on i_0 , θ_0 , the values of i and θ for the epoch 1850.0, and on the quantities which determine the position of the ecliptic of date with respect to the ecliptic of the epoch. If the change in the measure of orbit longitudes is denoted by $\alpha - \theta_0 + \alpha$ the foregoing equations may be written

$$\sin \beta = \cos i \sin b + \sin i \cos b \sin (l - \theta_0 + \alpha)$$

$$\cos \beta \sin (\lambda - \Omega) = -\sin i \sin b + \cos i \cos b \sin (l - \theta_0 + \alpha)$$

$$\cos \beta \cos (\lambda - \Omega) = \cos b \cos (l - \theta_0 + \alpha)$$

The three quantities, i, α , and α , are determined by the equations

$$\sin i \cos (\Omega - \theta'' - \psi') = -\sin i'' \cos i_0 + \cos i'' \sin i_0 \cos (\theta'' - \theta_0)$$

$$\sin i \sin (\Omega - \theta'' - \psi') = -\sin i_0 \sin (\theta'' - \theta_0)$$

$$\cos i = \cos i'' \cos i_0 + \sin i'' \sin i_0 \cos (\theta'' - \theta_0)$$

$$\sin i \cos \alpha = \sin i_0 \cos i'' - \cos i_0 \sin i'' \cos (\theta'' - \theta_0)$$

$$\sin i \sin \alpha = \sin i'' \sin (\theta'' - \theta_0)$$

where i'' and θ'' are the quantities denoted as i and θ in the preceding chapter, and there used to determine the position of the ecliptic of date with respect to the ecliptic of 1850.0; ψ' denotes the general precession. For the first two of these equations we may substitute

$$\sin i \cos (\Omega - \theta_0 - \psi') = \sin i_0 - \cos i_0 \sin i'' \cos (\theta'' - \theta_0) - 2 \sin i_0 \sin^2 \frac{1}{2} i'' \cos^2 (\theta'' - \theta_0)$$

$$\sin i \sin (\Omega - \theta_0 - \psi') = -\cos i_0 \sin i'' \sin (\theta'' - \theta_0) - \sin i_0 \sin^2 \frac{1}{2} i'' \sin 2(\theta'' - \theta_0)$$

and instead of computing α it will be more accurate to derive $\Omega - \theta_0 + \alpha - \psi'$, which is a very small angle. By putting

$$\gamma = -\cos i_0 \sin i'' \cos (\theta'' - \theta_0) - \sin i_0 \sin^2 \frac{1}{2} i'' [1 + \cos^2 (\theta'' - \theta_0)]$$

$$\delta = \cos^2 \frac{1}{2} i_0 \sin i'' \sin (\theta'' - \theta_0) + \sin i_0 \sin^2 \frac{1}{2} i'' \sin 2(\theta'' - \theta_0)$$

$$\epsilon = -2 \sin i_0 \sin^2 \frac{1}{2} i'' \sin^2 (\theta'' - \theta_0)$$

$$\zeta = 2 \sin^2 \frac{1}{2} i_0 \sin i'' \sin (\theta'' - \theta_0) - \sin i_0 \sin^2 \frac{1}{2} i'' \sin 2(\theta'' - \theta_0)$$

we can write

$$\sin i \cos (\Omega - \theta_0 - \psi') = \sin i_0 + \gamma - \frac{1}{2}\varepsilon$$

$$\sin i \sin (\Omega - \theta_0 - \psi') = -\delta + \frac{1}{2}\zeta$$

$$\sin i \cos \alpha = \sin i_0 + \gamma + \frac{1}{2}\varepsilon$$

$$\sin i \sin \alpha = \delta + \frac{1}{2}\zeta$$

From these four equations we derive

$$\sin^2 i \sin (\Omega - \theta_0 + \alpha - \psi') = \zeta \sin i_0 + \gamma \zeta - \delta \varepsilon$$

whence, since $\Omega - \theta_0 + \alpha - \psi'$ is so small an angle,

$$\Omega - \theta_0 + \alpha - \psi' = \frac{\zeta \sin i_0 + \gamma \zeta - \delta \varepsilon}{\sin^2 i}$$

In the equation which gives the value of $\sin \beta$ we can put $\cos b = 1$, since it is multiplied by the small factor $\sin i$. Thus

$$\sin \beta = \cos i \sin b + \sin i \sin (l - \theta_0 + \alpha)$$

For convenience of tabulation we shall separate β into two parts, so that $\beta = \beta_0 + \Delta \beta$, where β_0 will be obtained from the formula

$$\sin \beta_0 = A \sin l + B \cos l$$

A and B being expressible in powers of the time. In doing this we shall remove from the term $\cos i \sin b$ the portion which can be regarded as a function of the same form as $\sin \beta_0$, and unite it with the latter. Let what is left of $\sin b = s = \frac{a}{\bar{r}}u$, after this removal, be denoted as $\Delta(\sin b)$. Then $\Delta\beta$, being purely periodic and amounting at most to a few seconds, is given with sufficient exactness by the formula

$$\Delta \beta = \frac{\cos i}{\cos \beta_0} \Delta(\sin b) = \frac{\cos i}{\cos \beta_0} \Delta\left(\frac{a}{r}u\right)$$

By putting

$$p'' = \sin i'' \sin \theta'' \qquad q'' = \sin i'' \cos \theta''$$

quantities which have been determined in the preceding chapter, we can write the formula for the latitude in either of the two forms

$$= \cos i \sin b + \left[-\sqrt{1 - p''^2 - q''^2} \sin i_0 \cos \theta_0 + p'' \sin^2 \frac{1}{2} i_0 \sin 2\theta_0 - q'' (\cos i_0 \cos^2 \theta_0 + \sin^2 \theta_0) \right] \sin l + \left[-\sqrt{1 - p''^2 - q''^2} \sin i_0 \sin \theta_0 + p'' (\cos^2 \theta_0 + \cos i_0 \sin^2 \theta_0) - q'' \sin^2 \frac{1}{2} i_0 \sin 2\theta_0 \right] \cos l + \left[-\sqrt{1 - p''^2 - q''^2} \sin i_0 \sin \theta_0 + p'' (\cos^2 \theta_0 + \cos i_0 \sin^2 \theta_0) - q'' \sin^2 \frac{1}{2} i_0 \sin 2\theta_0 \right] \cos l + \left[-\sqrt{1 - p''^2 - q''^2} \sin i_0 \sin \theta_0 + p'' (\cos^2 \theta_0 + \cos i_0 \sin^2 \theta_0) - q'' \sin^2 \frac{1}{2} i_0 \sin 2\theta_0 \right] \cos l + \left[-\sqrt{1 - p''^2 - q''^2} \sin i_0 \sin \theta_0 + p'' (\cos^2 \theta_0 + \cos i_0 \sin^2 \theta_0) - q'' \sin^2 \frac{1}{2} i_0 \sin 2\theta_0 \right] \cos l + \left[-\sqrt{1 - p''^2 - q''^2} \sin i_0 \sin \theta_0 + p'' (\cos^2 \theta_0 + \cos i_0 \sin^2 \theta_0) - q'' \sin^2 \frac{1}{2} i_0 \sin 2\theta_0 \right] \cos l + \left[-\sqrt{1 - p''^2 - q''^2} \sin i_0 \sin \theta_0 + p'' (\cos^2 \theta_0 + \cos i_0 \sin^2 \theta_0) - q'' \sin^2 \frac{1}{2} i_0 \sin 2\theta_0 \right] \cos l + \left[-\sqrt{1 - p''^2 - q''^2} \sin i_0 \sin \theta_0 + p'' (\cos^2 \theta_0 + \cos i_0 \sin^2 \theta_0) - q'' \sin^2 \frac{1}{2} i_0 \sin 2\theta_0 \right] \cos l + \left[-\sqrt{1 - p''^2 - q''^2} \sin i_0 \sin \theta_0 + p'' (\cos^2 \theta_0 + \cos i_0 \sin^2 \theta_0) - q'' \sin^2 \frac{1}{2} i_0 \sin^2 \theta_0 \right] \cos l + \left[-\sqrt{1 - p''^2 - q''^2} \sin i_0 \sin^2 \theta_0 + p'' (\cos^2 \theta_0 + \cos^2 \theta_0) \right] \cos l + \left[-\sqrt{1 - p''^2 - q''^2} \sin^2 \theta_0 + \cos^2 \theta_0 + \cos^2 \theta_0 \right] \cos l + \left[-\sqrt{1 - p''^2 - q''^2} \sin^2 \theta_0 + \cos^2 \theta_0 \right] \cos l + \left[-\sqrt{1 - p''^2 - q''^2} \sin^2 \theta_0 + \cos^2 \theta_0 \right] \cos l + \left[-\sqrt{1 - p''^2 - q''^2} \sin^2 \theta_0 + \cos^2 \theta_0 \right] \cos l + \left[-\sqrt{1 - p''^2 - q''^2} \sin^2 \theta_0 + \cos^2 \theta_0 \right] \cos l + \left[-\sqrt{1 - p''^2 - q''^2} \sin^2 \theta_0 + \cos^2 \theta_0 \right] \cos l + \left[-\sqrt{1 - p''^2 - q''^2} \sin^2 \theta_0 + \cos^2 \theta_0 \right] \cos l + \left[-\sqrt{1 - p''^2 - q''^2} \sin^2 \theta_0 + \cos^2 \theta_0 \right] \cos l + \left[-\sqrt{1 - p''^2 - q''^2} \sin^2 \theta_0 + \cos^2 \theta_0 \right] \cos l + \left[-\sqrt{1 - p''^2 - q''^2} \sin^2 \theta_0 + \cos^2 \theta_0 \right] \cos l + \left[-\sqrt{1 - p''^2 - q''^2} \sin^2 \theta_0 + \cos^2 \theta_0 \right] \cos l + \left[-\sqrt{1 - p''^2 - q''^2} \sin^2 \theta_0 + \cos^2 \theta_0 \right] \cos l + \left[-\sqrt{1 - p''^2 - q''^2} \sin^2 \theta_0 \right] \cos l + \left[-\sqrt{1 - p''^2 - q''^2} \sin^2 \theta_0 \right] \cos l + \left[-\sqrt{1 - p''^2 - q''^2} \sin^2 \theta_0 \right] \cos l + \left[-\sqrt{1 - p''^2 - q''^2} \sin^2 \theta_0 \right] \cos l + \left[-\sqrt{1 - p''^2 - q''^2} \sin^2 \theta_0 \right] \cos l + \left[-\sqrt{1 - p''^2 - q''^2} \sin^2 \theta_0 \right] \cos l + \left[-\sqrt{1 - p''^2 - q''^2} \sin^2 \theta_0 \right] \cos l + \left[-\sqrt{1 - p''^2 - q''^2} \sin^2 \theta_0 \right] \cos l + \left[-\sqrt{1 - p''^2 - q''^2}$$

The rigorous equation, which gives the value of $\sin b$, being

$$\sin b = \frac{r_0}{r} \int \frac{a_0 n_0 dt}{\sqrt{1 - e_0^2}} r_0 \sin (\vec{f} - f) \left[\frac{d\Omega}{dZ} + \frac{r^2 + r r_0 + r_0^2}{r_0^3 r^2} \delta r \sin b \right]$$

where r_0 and f denote elliptic values and \bar{f} an f which is constant in the integration, it is easy to see that the constant factor, which multiplies the force, is

$$\frac{m'}{1+m}\alpha^2\left(\frac{a_0}{a}\right)^3\sin \mathbf{J}$$

But the factor actually employed in the determination of u was

$$\frac{m'}{1+m}\alpha^2\frac{a_0}{a}\sin J$$

Hence, in deriving $\sin b$ from u, we ought to multiply the latter by

$$\left(\frac{a_0}{a}\right)^2 \frac{a}{\bar{r}}$$

We have severally in the cases of Jupiter and Saturn

$$\log\left(\frac{a_0}{a}\right)^2 = 0.0000085$$
 $\log\left(\frac{a_0'}{a'}\right)^2 = 9.9996292$

From the equations connecting λ and β with l and b there is obtained, with a sufficient degree of approximation,

$$\lambda - l - \Omega + \theta_0 - \alpha = -\tan^2 \frac{1}{2} i \sin 2 (l - \theta_0 + \alpha) + \frac{1}{2} \tan^4 \frac{1}{2} i \sin 4 (l - \theta_0 + \alpha)$$

$$- 2 \tan \frac{1}{2} i \tan b \cos (l - \theta_0 + \alpha) + 2 \tan^3 \frac{1}{2} i \tan b \cos 3 (l - \theta_0 + \alpha)$$

By substituting in this the value, which has been obtained for $\Omega - \theta_0 + \alpha - \psi'$, we get

$$\lambda = l + \psi' + \frac{\zeta \sin i_0 + \gamma \zeta - \delta \varepsilon}{\sin^2 i} - \tan^2 \frac{1}{2} i \sin 2 (l - \theta_0 + \alpha) + \frac{1}{2} \tan^4 \frac{1}{2} i \sin 4 (l - \theta_0 + \alpha)$$
$$- 2 \tan \frac{1}{2} i \tan b \cos (l - \theta_0 + \alpha) + 2 \tan^3 \frac{1}{2} i \tan b \cos 3 (l - \theta_0 + \alpha)$$

The part of the second line of this formula, which depends on the portion $\Delta(\sin b)$ of $\sin b$, is, with sufficient approximation,

$$-\frac{\sin i}{\cos \beta_0} \Delta (\sin b) \cos (l - \theta_0 + \alpha) = -\tan i \cdot \Delta \beta \cdot \cos (l - \theta_0 + \alpha)$$

For the remainder of $\sin b$, which can be regarded as identical with $\tan b$, we can write

$$\tan b = A \sin (l - \theta_0 + \alpha) + B \cos (l - \theta_0 + \alpha)$$

A and B being expressible in powers of the time. Substituting this value in the last line of the equation for λ it becomes

$$- B \tan \frac{i}{2} - A \tan \frac{i}{2} \left(1 + \tan^2 \frac{i}{2} \right) \sin 2 \left(l - \theta_0 + \alpha \right) + A \tan^3 \frac{i}{2} \sin 4 \left(l - \theta_0 + \alpha \right)$$

$$- B \tan \frac{i}{2} \left(1 - \tan^2 \frac{i}{2} \right) \cos 2 \left(l - \theta_0 + \alpha \right) + B \tan^3 \frac{i}{2} \cos 4 \left(l - \theta_0 + \alpha \right)$$

If, therefore, we adopt two new quantities I and η , such that

$$\tan^2 \frac{1}{2} I \cos 2\eta = \tan^2 \frac{i}{2} + A \tan \frac{i}{2} \left(I + \tan^2 \frac{i}{2} \right)$$
$$\tan^2 \frac{1}{2} I \sin 2\eta = B \tan \frac{i}{2} \left(I - \tan^2 \frac{i}{2} \right)$$

which may be replaced by the equations

$$\sin I \cos \eta = \sin i + A \cos i$$

 $\sin I \sin \eta = B \cos i$

the equation for λ can be written

$$\lambda = l + \psi' + \frac{\zeta \sin i_0 + \gamma \zeta - \delta \varepsilon}{\sin^2 i} - B \tan \frac{i}{2} - \tan^2 \frac{1}{2} I \sin 2 (l - \theta_0 + \alpha + \eta)$$
$$+ \frac{1}{2} \tan^4 \frac{1}{2} I \sin 4 (l - \theta_0 + \alpha + \eta)$$
$$- \tan i \cdot \Delta \beta \cos (l - \theta_0 + \alpha)$$

As the tabulation of perturbations, both secular and periodic, for a fourth co-ordinate, the reduction to the ecliptic, appears a work of supererogation, we will give a method by which it can be avoided. Let the equation for λ be written

$$\lambda = f + \pi + ht - \tan^2 \frac{1}{2} i_0 \sin 2 (f + \pi - \theta_0) + \frac{1}{2} \tan^4 \frac{1}{2} i_0 \sin 4 (f + \pi - \theta_0) + \delta R$$

In this formula ht denotes the term, proportional to the first power of the time, in the development of the expression

$$\psi' + \frac{\zeta \sin i_0 + \gamma \zeta - \delta \varepsilon}{\sin^2 i} - B \tan \frac{i}{2}$$

in powers of the time; and δR denotes the remainder of this expression plus the secular and periodic perturbations of what is generally known as the reduction to the ecliptic. If we do not go beyond 300 years from the epoch, δR , for either Jupiter or Saturn, scarcely exceeds 10". Quantities dependent on its square may then be neglected. We have

$$\frac{dz}{d\lambda} = \frac{a^2 n \cos \varphi \cos i_0}{\bar{r}^2 \cos^2 \beta_0}$$

Consequently, if we equate the argument $q + n\delta z$ by applying to it the correction

$$\Delta(n\delta z) = \frac{\bar{r}^2 \cos^2 \beta_0}{a^2 \cos \varphi \cos i_0} \delta \mathbf{R}$$

we shall obtain the proper value of $\lambda - \pi - ht$ by entering a table calculated for this quantity, but in which the term δR has been ignored. $\Delta(n\delta z)$ is a quantity which can be developed as a function of g and g', and having precisely the same form as $n\delta z$, its addition in nowise complicates the latter quantity; the only change being that some of the coefficients are modified by trifling amounts.

On account of this modification of the fundamental argument the expressions for ν and β_0 must receive corrections. The correction for ν is

$$\Delta \nu = -\frac{d \cdot \log r}{dg} \Delta(n\delta z) = \left[e \sin g - \frac{3}{2} e^2 \sin 2g \right] \Delta(n\delta z)$$

The correction to $\sin \beta_a$ is

$$\Delta(\sin \beta_0) = -\frac{d(\sin \beta_0)}{dq} \Delta(n\delta z) = -\tan i \cos^2 \beta_0 \cos (f + \pi - \theta_0) \cdot \delta \mathbf{R}$$

These corrections are quite minute.

Application of the formulæ to Jupiter.

Supposing that

$$A \sin f + B \cos f$$

are the terms to be removed from $\cos i \sin b$, we have, for determining $\Delta \beta$,

$$\varDelta\beta = \frac{\cos i}{\cos \beta_0} \frac{a_0^2}{\mathbf{a}^2} \frac{a}{\overline{r}} u - \mathbf{A} \frac{\sin f}{\cos \beta_0} - \mathbf{B} \frac{\cos f}{\cos \beta_0}$$

A and B can be determined so that no terms of the form $kT \sin g + k'T \cos g$ appear in $\Delta \beta$. From special values computed for eight points of the circumference at two epochs, using elliptic values of the co-ordinates augmented by the secular terms, it is found that

$$\frac{a_0^2}{a^2} \frac{a}{r} \frac{\cos i}{\cos \beta_0} = 0.9998907 - 0.000077T$$

$$+ [0.0482118 + 0.0000010T] \cos g$$

$$+ [0.0000010 + 0.000002T] \sin g$$

$$+ [0.0024471 + 0.0000098T] \cos 2g$$

$$+ [-0.0000134 + 0.0000072T] \sin 2g$$

$$+ [0.0001444 - 0.0000015T] \cos 3g$$

$$+ [-0.0000144 + 0.0000015T] \sin 3g$$

$$+ [0.0000138 - 0.0000031T] \cos 4g$$

In this expression g ought to be replaced by $g + n\delta z$; it is sufficient to take for $n\delta z$ the two terms having the arguments 5g' - 2g and 5g' - 3g. The additional terms, which thus should be joined to the expression, are

+ 0.0000554
$$\cos (5g' - g)$$
 - 0.0001298 $\sin (5g' - g)$ - 0.0000188 $\cos (5g' - 2g)$ - 0.000012 $\sin (5g' - 2g)$ - 0.0000554 $\cos (5g' - 3g)$ + 0.0001298 $\sin (5g' - 3g)$ + 0.0000188 $\cos (5g' - 4g)$ + 0.000012 $\sin (5g' - 4g)$

In a similar way have been obtained the two expressions

$$\frac{\sin f}{\cos \beta_0} = \\ [0.998031 - 0.0000160T] \sin g + [-0.000007 - 0.000185T] \cos g \\ + [0.048106 + 0.0001633T] \sin 2g + [-0.000002 - 0.000185T] \cos 2g \\ + [0.002674 + 0.0000169T] \sin 3g + [-0.000007 - 0.0000185T] \cos 3g \\ + [0.000159 + 0.0000015T] \sin 4g + [-0.000001 - 0.0000016T] \cos 4g \\ + 0.001146 \sin (5g' - g) + 0.0002687 \cos (5g' - g) \\ - 0.000388 \sin (5g' - 2g) + 0.0002687 \cos (5g' - 2g) \\ + 0.001146 \sin (5g' - 3g) + 0.002687 \cos (5g' - 3g) \\ - 0.000388 \sin (5g' - 4g) + 0.000024 \cos (5g' - 4g)$$

$$\frac{\cos f}{\cos \beta_0} = - 0.048252 - 0.0001648T \\ + [0.997577 - 0.0000196T] \cos g + [-0.000007 + 0.0000159T] \sin g \\ + [0.048094 + 0.0001630T] \cos 2g + [-0.000007 + 0.00001780T] \sin 2g \\ + [0.002672 + 0.000014T] \cos 3g + [-0.000007 + 0.00001780T] \sin 3g \\ + [0.000159 + 0.000014T] \cos 4g + [-0.000001 + 0.000017T] \sin 4g \\ + 0.001145 \cos (5g' - g) - 0.002686 \sin (5g' - g) \\ - 0.000388 \cos (5g' - 2g) - 0.00024 \sin (5g' - 2g) \\ - 0.001145 \cos (5g' - 3g) + 0.002686 \sin (5g' - 3g) \\ + 0.000388 \cos (5g' - 4g) + 0.00024 \sin (5g' - 4g)$$

Adding together all the first-order terms with those of the second order, and changing the parts of the coefficients multiplied by nt and n^2t^2 into the equivalents having the factors T and T², we have the expression for u, which it is suitable to employ here. The equations, which then result for determining A and B, are

A[
$$0.998031 - 0.0000160T$$
] + B[$-0.000007 + 0.0000159T$] = $-14.6842T - 0.04638T^2$
A[$-0.000007 - 0.0000185T$] + B[$0.997577 - 0.0000196T$] = $6.5083T - 0.09804T^2$

Whence we derive

$$A = - 14.7132T - 0.04681T^{2}$$

$$B = + 6.5240T - 0.09842T^{2}$$

Since $f = l - 11^{\circ}$ 56' 9".33, as far as these terms are concerned, we have, in joining to them the terms of the third order, obtained at the end of Chapter XXIV,

$$\cos i \sin b = [-13.0458T - 0.06615T^{2} + 0.000324T^{3}] \sin l + [-9.4259T - 0.08661T^{2} - 0.000240T^{3}] \cos l$$

By employing the expressions for p'' and q'', found in Chapter XXV, we get the remaining portion of $\sin \beta_0$, which is due to the motion of the ecliptic; it is

$$\sin \beta_0 = [46.7603T - 0.05665T^2 - 0.000506T^3] \sin l + [5.2691T + 0.19508T^2 - 0.000240T^3] \cos l$$

It is not worth while to add here the two portions together, as the first has been computed with the values of the masses of the planets adopted at the beginning of this investigation, and which will receive some modifications, in consequence of the comparison of the theory with observation, to be given in the following chapter. But in deriving the motion of the ecliptic, in Chapter XXV, regard has been taken of these modifications.

The following is the expression we obtain for $\Delta\beta$:

A 21 at 1 2 a	Δ	Δβ		Δβ	
Arg=i'g'+ig	sin.	cos.	Arg=i'g'+ig	sin.	cos.
i' i o o o o o o o o o o o o o o o o o o	sin. "" -0. 0061 +0. 0001 +0. 0051 +0. 1024-0. 0005T +0. 4420+0. 0041T -0. 1112-0. 0027T -0. 2579-0. 0010T -0. 0108 0. 0000T +0. 0042+0. 0004T -0. 0247+0. 0014T +0. 4575-0. 0060T -0. 0922+0. 0008T -0. 0033-0. 0002T +0. 0060-0. 0002T +0. 0366-0. 0002T +0. 0366-0. 0002T -0. 5398-0. 0101T	-0.0175+0.005T -0.028 -0.0135 -0.0007 -0.0006 +0.0160+0.0002T -0.3041+0.0057T -0.0591-0.0004T -0.0175+0.0001T -0.3414-0.0015T +0.4287+0.0055T +0.2009+0.0058T -0.0564+0.0003T -0.0028 -0.000T +0.0015-0.0001T +0.0421+0.0001T -0.0113+0.0004T +0.8570-0.0064T	i' i 4 0 4— I 4— 2 4— 3 4— 4 4— 5 5 0 5— I 5— 2 5— 3 5— 4 5— 5 6— 6 6— 1 6— 2 6— 3 6— 4 6— 5 6— 6	" +0.0058 +0.0406 0.0000T -0.0246-0.0007T +0.2286-0.0012T +0.0200 0.0000T +0.0043-0.0001T -0.0674+0.0036T +0.1936+0.0002T -3.5340+0.0005T -0.1763-0.0005T -0.0044-0.0001T -0.0025 +0.0002 +0.0065 -0.0317 +0.0134 -0.0119 -0.0018	" +0.0024 -0.0238 0.0000T +0.1424-0.0001T +0.0924+0.0035T -0.0067+0.0002T +0.0074+0.0001T +0.1707+0.0005T -0.0014-0.0006T +0.3195-0.0042T +0.0592-0.0008T +0.0064+0.0004T +0.0024 +0.0007 +0.018 +0.0186 +0.0465 +0.0033 +0.0030
3— 3 3— 4 3— 5	-0.0541-0.0005T +0.0189-0.0002T +0.0012	+0.0165-0.0004T -0.0030+0.0001T -0.0001	6— 7 7— 2 7— 3	-0. 0011 +0. 0036 -0. 0040	-0.0008 -0.0015 +0.0029

A	Δβ		h :/-/	Δβ	
Arg=i'g'+ig	sin.	cos.	Arg=i'g'+ig	sin.	cos.
i' i 7— 4 7— 5 7— 6 7— 7 7— 8	" +o. 0383 -o. 0075 -o. 0017 -o. 0016 +o. 0002	" +0. 0373 +0. 0074 -0. 0037 -0. 0005 -0. 0005	6' i 8- 7 8- 8 9- 5 9- 6 9- 7	+0.0011 0.0000 +0.0001 -0.0025 +0.0008	" -0. 0010 +0. 0007 +0. 0038 -0. 0007 -0. 0015
8— 3 8— 4 8— 5 8— 6	+0. 0008 -0. 0087 -0. 0050 -0. 0032	+0. 0009 -0. 0033 +0. 0067 -0. 0029	10— 4 10— 5 10— 6 10— 7 10— 8	+0.0012 +0.0361 -0.0008 +0.0002 +0.0007	+0.0027 +0.0631 +0.0029 -0.0010 +0.0003

At intervals of 500 years have been computed the following quantities:

Date.	$\frac{\zeta \sin i_0 + \gamma \zeta - \delta \varepsilon}{\sin^2 i}$	$-B \tan \frac{i}{2}$	I	$\theta_0 - \alpha - \eta$
	"	//	0 / //	0 / //
850	5. 2875	-1.7083	1 22 1.106	102 42 45.06
1350	-2. 6210	o. 8381	1 20 21.264	100 49 23.15
1850	0.0000	0.0000	1 18 42.100	98 56 19.79
2350	+2.5717	+0.8 060	1 17 3.627	97 3 34.81
2850	+5.0899	+1.5800	1 15 25.862	95 11 8.78

Thence the reduction to the ecliptic and mean equinox is

$$\lambda - l = + 27.029 \sin (2l + 342^{\circ} 7' 20'') + 0''.002 \sin (4l + 324^{\circ})$$

$$+ [5026.4708 + 0''.4211 \sin (2l + 104^{\circ} 37'.9)]T$$

$$+ [1.10576 + 0''.00351 \sin (2l + 223^{\circ} 9')]T^{2}$$

$$+ [0.000169 + 0''.000020 \sin (2l + 340^{\circ})]T^{3}$$

$$- 0.0000488T^{4} - 0''.0000023T^{5}$$

We have here, then, h = 50''.264708, and for δR the sum of the inequalities of the reduction

$$\begin{split} \delta \mathbf{R} &= \Gamma - \frac{1}{2} s \frac{ds}{dv} - \tan i \cos (l - \theta_0 + \alpha) \cdot \Delta \beta \\ &+ o''.4211 \mathrm{T} \sin (2l + 104^{\circ} 37.'9) \\ &+ [1''.10576 + o''.00351 \sin (2l + 223^{\circ} 9')] \mathrm{T}^2 \\ &+ [o''.000169 + o''.000020 \sin (2l + 340^{\circ})] \mathrm{T}^3 \end{split}$$

From eight computed special values it is found that

$$\frac{ndz}{d\lambda} = 1.002333 - 0.094641 \cos l - 0.019961 \sin l + 0.002958 \cos 2l + 0.001332 \sin 2l - 0.000061 \cos 3l - 0.000060 \sin 3l$$

Also, in like manner we get, when δR is limited to the three latter lines of the expression above.

$$\frac{ndz}{d\lambda}\delta R = \begin{bmatrix} & & & & & & \\ & + 0.0019 & \\ & + 0.0379 & \sin nz - 0.0477 & \cos nz \\ & - 0.2606 & \sin 2nz + 0.3283 & \cos 2nz \\ & - 0.0126 & \sin 3nz + 0.0158 & \cos 3nz \\ & - 0.0006 & \sin 4nz + 0.0007 & \cos 4nz]T \end{bmatrix}$$

$$+ \begin{bmatrix} & & + 1.11086 \\ & + 0.00016 & \sin nz - 0.10630 & \cos nz \\ & - 0.00134 & \sin 2nz - 0.00482 & \cos 2nz \\ & + 0.00004 & \sin 3nz - 0.00020 & \cos 3nz]T^2 \end{bmatrix}$$

$$+ \begin{bmatrix} & & + 0.000169 \\ & - 0.000003 & \sin nz - 0.000016 & \cos nz \\ & + 0.000001 & \sin 3nz - 0.000001 & \cos 2nz \\ & + 0.000001 & \sin 3nz - 0.000000 & \cos 3nz]T^3 \end{bmatrix}$$

In this, for nz, ought to be substituted $g + n\delta z$. But we may take for $n\delta z$ its eleven largest terms and neglect its square. When this is done, and we also obtain the terms which arise from the first line of the value of δR , we have the following complete expression for $\Delta(n\delta z)$:

Arg=i'g'+ig	extstyle ext			
	sin.	cos.		
i' i	и и п п	// // // // // // // // // +. 0019T+1. 11086T³+. 000187T³		
o— 1	+0.0008—.0379T—.00037T²+.000004T³	o. 0000—. 0477T— . 10632T ² —. 000012T ³		
O 2	$+.2606T+.00111T^2000002T^3$	+. 3283T 00461T2 000016T2		
o 3	$+.0126T00007T^{2}$.000000T ³	+. 0158T . 00000T2 000002T3		
0 4	+.0006T .00000T ⁹	+ 0007T+ . 00001T²		
I+ 2	0.0002	+0.0012		
1+1	+0.0032—.0001T	+0.00530001T		
1 0	+0.0009 +.00002T ³	—0.0025 .00000T³		
1— 1	—0. 0029	-o. oo78		
I— 2	—o. 0007 —. 00002T³	+0.0013 .0000T ²		
1— 3	-0.0005+.0001T	+0.0029—.0001T		

Ana-ilal Li-	$ extstyle \varDelta(n\delta z)$			
Arg=i'g'+ig	sin.	cos.		
i' i	11 11 11	п п п		
2+ 1	+0.0039—.0002T	o. 0001+. 0002T		
2 0	-0.00510001T .00000T ³	+0.0049+.0004T00003T2		
2— I	—0. 0061 —. 00002T ²	o. 0007 00005T²		
2 2	+0.0051 .00000T ²	-o. 0055 +. 00003T ²		
2-3	+0.00240002T+.00002T3	+0.0010—.0002T+.00005T2		
2 4	-o. 0006 0003T	o. 0000—. 0002T		
3 0	о. 0001 . 0000Т	+0.00190002T		
3— 1	-0.0095 $+.00002$ T ³	—0. 0067		
3— 2	— 0. 0003	0, 0025		
3-3	+0.0101 —.00002T2	+0.0057 —.00001T ⁹		
3- 4	+0.0002+.0002T	+0.0006 .0000T		
4— I	<u></u> 0. 0016	0, 0004		
4 2	-0.0012	+0.0025		
4-3	+0.0016	+0.0002		
4 4	+0.0010	-0.0027		
5+ I	—. 0001T	. 0000T		
5 0	0.00200024T+.00002T ²	-0.00090007T+.00007T2		
5 I	$-0.0001+.0002T+.00027T^2$	+0.00220003T00013T2		
5— 2	+0.0004 .0000T ²	-0.0399 +.00004T ³		
5— 3	-0.000700028T ²	—0. 0042 +. 00012T2		
5— 4	+0.0058+.0012T00012T2	+0.0406—.0021T—.00009T2		
5— 5	+0.0008+.0003T+.00001T2	+0.0020+.0001T00001T ²		

The terms of this expression not multiplied by T or its powers represent nearly the periodic perturbations of the reduction of the longitude to the ecliptic.

The correction which must be applied to the common logarithm of $\frac{r}{\bar{r}}$, on account of this change in the fundamental argument, is determined in a similar way, and is (in units of the seventh decimal):

Arg = i'g' + ig	$-rac{d(\mathrm{com.}\log r)}{dz}\mathcal{\Delta}(\delta z)$			
		cos.	sin.	
i' i o o o o o I o = 2 o = 3 o = 4 o = 5	-0.010T +0.132T +0.026T -0.131T -0.016T -0.001T	o. $000T^2$ o. $0000T^3$ o. $000T^2$	-0. 166T+1. 098T ² -0. 0002T ³ -0. 032T+0. 027T ² +0. 165T+0. 070T ² +0. 020T +0. 002T	
5— I 5— 3 5— 5		-0. 003T ²	+0.02-0.001T -0.04-0.001T +0.02	

The correction to be applied to $\sin \beta_0$, on the same account, is

$$-\frac{d(\sin \beta_0)}{dz}\Delta(\delta z) = \begin{bmatrix} 0.0044\text{T} - 0.02504\text{T}^2 + 0.000075\text{T}^3] \sin l \\ + [0.0019\text{T} + 0.00395\text{T}^2 - 0.000179\text{T}^3] \cos l \\ + [-0.0048\text{T} + 0.00002\text{T}^2] \sin 3l \\ + [-0.0005\text{T} - 0.00003\text{T}^2] \cos 3l \end{bmatrix}$$

Application of the Formulæ to Saturn.

Proceeding in exactly the same way as for Jupiter it is found that

In this expression g' ought to be replaced by $g' + n'\delta z'$; it is sufficient to take for $n'\delta z'$ the three terms having the arguments 2g' - g, 4g' - 2g, and 5g' - 2g. The additional terms, which should be joined to the expression, are

+ 0.0000572 cos (
$$g'-g$$
)
- 0.0000572 cos (3 $g'-g$)
- 0.0000117 cos (3 $g'-2g$) - 0.0000921 sin (3 $g'-2g$)
+ 0.0001482 cos (4 $g'-2g$) - 0.0003652 sin (4 $g'-2g$)
+ 0.0000117 cos (5 $g'-2g$) + 0.0000921 sin (5 $g'-2g$)
- 0.0001482 cos (6 $g'-2g$) + 0.0003652 sin (6 $g'-2g$)

In a similar way have been obtained the two expressions

$$\frac{r'}{a'}\sin f' = \frac{0.0000003 - 0.0005529\text{T}}{ + [0.9980325 + 0.0000145\text{T}] \sin g' + [0.000051 - 0.000386\text{T}] \cos g'}$$

$$+ [0.0279551 - 0.0003436\text{T}] \sin 2g' + [0.0000014 - 0.0005547\text{T}] \cos 2g'}$$

$$+ [0.0011714 - 0.0000241\text{T}] \sin 3g' + [0.0000051 - 0.0000387\text{T}] \cos 3g'}$$

$$+ [0.0000583 - 0.0000016\text{T}] \sin 4g' + [0.0000017 - 0.0000026\text{T}] \cos 4g'}$$

$$+ 0.0000032 \sin 5g' - 0.0000001\text{T} \cos 5g'$$

$$\frac{f'}{a'}\cos f' = -0.0840851 + 0.0003454T$$

$$+ [0.0000051 + 0.0000233T] \sin g' + [0.9988249 + 0.0000241T] \cos g'$$

$$+ [-0.0000014 + 0.0005448T] \sin 2g' + [0.0279697 - 0.0003438T] \cos 2g'$$

$$+ [-0.0000051 + 0.0000388T] \sin 3g' + [0.0011718 - 0.0000241T] \cos 3g'$$

$$+ [0.0000011 + 0.0000026T] \sin 4g' + [0.0000583 - 0.000016T] \cos 4g'$$

$$+ 0.0000001T \sin 5g' + 0.0000032 \cos 5g'$$

 $\Delta \beta'$ is obtained from its equation, put in the form

$$\varDelta\beta' = \frac{a}{\bar{r}} \sec. \beta_0' \left\lceil \frac{{a_0'}^2}{\bar{a}'^2} \cos i' \cdot u' - A \frac{\bar{r}'}{\bar{a}'} \sin f' - B \frac{\bar{r}'}{\bar{a}'} \cos f' \right\rceil$$

It is found that

$$A = + 23.8966T - 0.21464T^{2}$$

$$B = + 33.4890T + 0.16184T^{2}$$

Since $f' = l' - 90^{\circ}$ 6' 46".22 we have, as far as these terms are concerned, joining to them the terms of the third order, obtained in Chapter XXV,

$$\cos i' \sin b' = \begin{bmatrix} & '' & '' & '' \\ & 33.4419\text{T} + 0.16226\text{T}^2 - 0.000858\text{T}^3 \end{bmatrix} \sin l' \\ + \begin{bmatrix} -23.9625\text{T} + 0.21432\text{T}^2 + 0.000641\text{T}^3 \end{bmatrix} \cos l'$$

The remaining portion of $\sin \beta_0'$, due to the motion of the ecliptic, is

$$\sin \beta_0' = \begin{bmatrix} '' & '' & '' \\ 46.7526T - 0.05662T^2 - 0.000506T^3 \end{bmatrix} \sin l' + \begin{bmatrix} 5.2524T + 0.19509T^2 - 0.000240T^3 \end{bmatrix} \cos l'$$

For the same reason, as in the case of Jupiter, we do not add these two portions. The following expression is obtained for $\Delta \beta'$:

Δβ΄		$oldsymbol{eta}'$		$\Delta eta'$	
Arg=i'g'+ig	sin. cos.		Arg=i'g'+ig	sin.	cos.
i' i 0 0 1 0 3 0 4 0 5 0 -3- I -2- I 0- I 1- I 2- I	+0.0604—0.0012T —0.0002—0.0003T +0.0034 +0.0020 —0.0023 +0.0029 +0.0206+0.0013T —0.7897+0.0207T —0.7224—0.0132T —2.0366+0.0316T	"" -0. 3294-0. 0109T -0. 1948-0. 0015T -0. 0186+0. 0001T +0. 0043 -0. 0011 -0. 0013 +0. 0015 +0. 0161-0. 0015T +1. 6202+0. 0131T -0. 4281+0. 0040T -2. 0693-0. 0364T	i' i 3-1 4-1 5-1 6-1 0 1 2 1 2 3 4 2	" " " -0.7177+0.0002T +0.0309-0.0001T +0.0245+0.0002T +0.0011 +0.0002 +0.0004-0.0002T -0.019-0.0002T +0.2524+0.0014T +0.0851 0.0000T -0.1903-0.0052T +1.0807+0.0061T	" " -0. 0636-0. 0018T -0. 0483+0. 0002T -0. 0288+0. 0001T -0. 0004 -0. 0012 +0. 0024-0. 0001T +0. 0630-0. 0003T +0. 0533-0. 0025T -0. 0729+0. 0008T -0. 1002-0. 0016T -8. 6028+0. 0143T

Arg=i'g'+ig	Δ	β'	$\operatorname{Arg}=i'g''+ig'$	2	1β'
	sin.	cos.	Arg—i y +iy	sin.	cos.
i' i 5— 2	 0. 1334+0. 0048T	// // +0. 3444—0. 0028T	i' i I+ 2	// // 0, 000I	// // o. 0005
6— 2	+0. 2366-0. 0001T	+0.0733-0.0075T	1+ 1	0.0038	-0.0202
7— 2	+0.0101—0.0003T	+0.0033—0.0008T	ı o	0. 0657	—o. o557
8— 2	+0.0004-0.0005T	+0.0001+0.0009T	1 1	+o. o381	+0.0078
			1 2	+0.0183	_o. o ₃₃₄
—1 — 3	+0.0007	·o. 000I	I— 3	+0.0011	0.0015
o— 3	-0.0010	+0.0023	_		_
1 3	+0.0008—0.0003T	+0.0072—0.0002T	z+ I	—o. 0028	+0.0008
2 3	+0.0003-0.0002T	+0.0868 o.0000T	2 0	—o. o384	+0.0196
3- 3	+0.0247—0.0002T	+0.0329+0.0001T	2 I	+0.0615	с. 1010
4- 3	0.0728+0.0001T	—0. 0259 0. 0000T	2 2	+0.0044	-o. o33o
5- 3	0.1169 0.0000T	+0.0080-0.0003T	2-3	+0.0085	+0.0003
6— 3	—0.0877—0.0001T	+0.0395 0.0000T		10.0008	0.0018
7- 3	+0.0245 0.0000T	0.0418 o.0000T	3+ 1	+0.0008	-0.0018
8— 3	-0.0007 o.0000T	-0.0017+0.0001T	3 0	+0.0114	-0.0328
9-3	0.0005	—o. ooo5	3— 1	-o. o368	—o. o326
2 4	-0.0021	0.0018	3— 2	+0.6067	+0. 2214
2-4	-0.0318 0.0000T	+0.0018	3— 3	+0.0378	+0.0116
3-4	-0.0129+0.0001T	+0.0071+0.0002T	3-4	+0.0014	+0.0029
4 4		+0.0132+0.0001T	4— I	-0.0043	0.0023
5— 4 6— 4	—0.0010+0.0001T	-0.0142 0.0000T	4 2	+0.0264	0.0051
1	0.00510.0001T 0.00710.0001T	0.0117+0.0001T 0.00840.0001T	4— 3	+0.0050	-0.0242
7— 4 8— 4	-0.0020-0.0001T		4— 4	+0.0007	-0.0004
	-0.0825-0.00011	+0.0003-0.0002T			
9-4	+0.0086 0.0000T	+0.02720.0011T -0.0030+0.0001T	5— I	O. 00II	+0.0003
10— 4 11— 4	+0.0001—0.0001T	-0.0019+0.0001T	5— 2	+0.0027	
11-4	+0.0001-0.00011	0.0019-0.00011	5-3	—о. 0097	0, 0207
3 5	0.0013	-0.0002	5 4	+0.0046	-0.0016
4 5	0.0057	-0. OI2I	6 3	0.000#	0.0000
5 5	-0.0073	0. 0049	6— 2 6— 3	0.0007 0.0112	—0.0009 —0.007I
6 5	+0.0035	0. 0007	6-4	+0.0113 +0.0032	+0.0071
7— 5 .	+0.0021	0.0020	6— 5	+0.0032 +0.0005	-0.0016 +0.0013
8— 5	+0.0013	-0.0020	- 3	, 0.0003	7-0.0013
9— 5	+0.0001	-o. oo34	7 3	+0.0006	0.0000
10- 5	0. 0009	-0.0021	7 4	+0.0005	0. 0015
11-5	0.0016	-0.0013	7 5	+0.0007	+0.0007
			7- 6	0.0005	+0.0002
4 6	0.0004	0.0006			
5 – 6	+0.0043	0.0033			
6— 6	+0.0015	0.0038			
7-6	+0.0006	+0.0012			
8 6	+0.0008	+0.0003			
9 6	+0.0007	+0.0001			
10— 6	+0.0012	0. 0002			
6— 7	+0.0019	+0.0015			
7-7	+6.0019	+0.0003			

Date.	$\frac{\zeta \sin i_0' + \gamma \zeta - \delta \varepsilon}{\sin^2 i'}$	$-B an rac{i'}{2}$	I'	$\theta_0' - \alpha' - \eta'$
850	,, 9, 2472	., +8. 8607	o / // 2 31 47.88	0 / // 117 30 7.86
1350	4 ⋅ 5577	+4. 3939	2 30 45.37	114 56 2.11
1850	0.0000	0.0000	2 29 40.19	112 20 49.05
2350	+4.4200	-4. 3113	2 28 32.51	109 44 23.86
2850	+8.6959	—8. 5 306	2 27 22.41	107 6 42.41

At intervals of 500 years have been computed the following quantities:

Thence the reduction to the ecliptic and mean equinox is

$$\lambda' - l' = + 97.774 \qquad \sin(2l' + 315 \ 18 \ 22) + 0.023 \qquad \sin(4l' + 270 \ 37) \\ + [5025.8141 + 1.7921 \quad \sin(2l' + 54 \ 33.2 \) + 0.0008 \quad \sin(4l' + 7 \)]T \\ + [1.10629 + 0.01737 \quad \sin(2l' + 148 \ 11 \) + 0.00002 \quad \sin(4l' + 90 \)]T^3 \\ + [0.000179 + 0.000115 \quad \sin(2l' + 239 \ 38 \)]T^3 \\ + [-0.0000023T^5$$

We have, then, h = 50''.258141, and for $\delta R'$ the sum of the inequalities of the reduction

$$\begin{split} \delta \mathbf{R}' &= \Gamma' - \frac{1}{2} s' \frac{ds'}{dv'} - \tan i' \cos (l' - \theta_0' + \alpha') \cdot \Delta \beta' \\ &+ \left[\mathbf{1}''.792\mathbf{1} \sin \left(2l' + 54^{\circ} 33'.2 \right) + o''.0008 \sin \left(4l^{\circ} + 7^{\circ} \right) \right] \mathbf{T} \\ &+ \left[\mathbf{1}''.10629 + o''.01737 \sin \left(2l' + 148^{\circ} \mathbf{1}\mathbf{1}' \right) + o''.00002 \sin \left(4l' + 90^{\circ} \right) \right] \mathbf{T}^2 \\ &+ \left[o''.000179 + o''.000115 \sin \left(2l' + 239^{\circ} 38' \right) \right] \mathbf{T}^3 \end{split}$$

By the method of computing special values, when $\delta R'$ is limited to the three latter lines of the expression above, we get

$$\frac{n'dz'}{d\lambda'}\delta R' = \begin{bmatrix} & & & & \\ & -0.0123 \\ & +0.1737 & \sin & n'z' + 0.2462 & \cos & n'z' \\ & -1.0271 & \sin & 2n'z' - 1.4547 & \cos & 2n'z' \\ & -0.0575 & \sin & 3n'z' - 0.0815 & \cos & 3n'z' \\ & -0.0035 & \sin & 4n'z' - 0.0048 & \cos & 4n'z']T \end{bmatrix}$$

$$+ \begin{bmatrix} & +1.11323 \\ & -0.00256 & \sin & n'z' - 0.12278 & \cos & n'z' \\ & +0.01543 & \sin & 2n'z' - 0.01008 & \cos & 2n'z' \\ & +0.00082 & \sin & 3n'z' - 0.00052 & \cos & 3n'z']T^2 \end{bmatrix}$$

$$+ \begin{bmatrix} & 0.000179 \\ & -0.000006 & \sin & n'z' - 0.000038 & \cos & n'z' \\ & +0.000056 & \sin & 2n'z' + 0.000102 & \cos & 2n'z' \\ & & -0.000000 & \sin & 3n'z' + 0.000005 & \cos & 3n'z']T^5 \end{bmatrix}$$

In this expression for n'z' ought to be substituted $g' + n'\delta z'$. For $n'\delta z'$ it will be sufficient to take its more important terms, and its square can be neglected. When this is done, and we also obtain the terms which arise from the first line of the value of $\delta R'$, we have the following complete expression for $\Delta(n'\delta z')$:

A	$\Delta(n$	$(\delta z')$
Arg=i'g'+ig'	sin.	cos.
i' i	<i>''</i>	// // // // // // // // // // // // //
0 0	, m , m , (m)	-0.0123T+1.11325T ² +0.000147T ³
1 0	+o. 1739T—o. 00499T2—o. 000006T3	+0.2461T— .12232T ² — .000064T ³
2 0	—1.0272T+ .01597T2— .000011T3	-1.4547T01217T ⁹ + .000146T ³
3 0	+0.0003—.0575T—.00005T ² —.000023T ³	+0.0043—.0815T+.00151T ² —.000006T ³
4 0	+0.0002— .0035T— .00007T ²	+0.00040048T+.00017T ²
5 0	0,0001	0, 0001
2 I	—0. 0003	o. ooo5
-ı- ı	+0.0295— .0004T	o. 0262 0009T
o I	+0.0142+ .0024T00003T ²	+0.0220— .0029T— .00002T ²
I— I	+0.02350008T+.00001T ²	+0.0175+.0001T00013T2
2— I	+0.0229+ .0004T	+0.0005— .0002T
3— 1	+0.05410007T .00000T ²	+0.0255+.0012T+.00013T2
4 I	$+0.0144+.0020T00003T^2$	-0.0044+.0031T+.00002T2
5— 1	-0.0001+ .0002T	+0.0012+.0002T
6— 1	o. voo3	+0.0009
—I— 2	+0.0005	—o. oo13
0— 2	0.0047	—0. 0029
1— 2	0.0017+ .0004T	o. 0003+ . 0003T
2— 2	o. 0030+ . 0063T+ . 00004T²	+0.0043+.0043T00005T2
3— 2	-0.0949+.0266T+.00025T2	+0.1671+.0059T00024T2
4 2	+0.0154— .0020T+ .00081T2	0.04440002T00032T ²
5 2	+0.0432— .0016T— .00020T²	+0.1792— .0002T— .00002T ²
6— 2	+0.00100041T00082T2	—0.0079+.0009T+.00031T²
7— 2	o.00540136T00022T2	+0.0005+.0216T—.00015T ²
8— 2	-0.00020011T	o. 0000+ . 0018T
o- 3	+0.0001	—o. ooo1
1-3	+0.0007	-0.0017
2 — 3	0.0003	o. ooo6
3— 3	+0.0007	0.0005
4 3	+0.0014	+o. 0002
5 3	+0.0033	-0.0002
6— 3	+0.0011	—0.0004
7— 3	+o. 0016	0.0017
8— 3	—o. 0002	+0.0010
2 4	+0.0007	+0.0002
3— 4	+0.0003	0.0002
4 4	+0.0003	0.0000
5— 4	+0.0002	0.0003

Arg=i'g'+ig		$\varDelta(n'\delta z')$
Alg=1 y +1y	sin.	cos.
i' i 6— 4 7— 4 8— 4 9— 4 10— 4	+0.0001 +0.0002 +0.0021 -0.0006 +0.0015 -0.0002	" " " " " " " " " " " " " " " " " " "
3— 5 4— 5 5— 5 6— 5	0. 0000 +0. 0001 +0. 0002 +0. 0001	+0.0002 +0.0001 +0.0002 +0.0001

The reduction which must be applied to the common logarithm of $\frac{r'}{\bar{r}'}$, on account of this change in the fundamental argument, is determined in a similar way, and is (in units of the seventh decimal):

Arg=i'g'+ig	$-rac{d(ext{com.}\log r')}{dz} extstyle d(\delta z')$				
	cos.	sin.			
i' i o o i o o o o o o o o o o o o o o o	-0. 05T+0. 001T ² +0. 0008T ³ +0. 60T-0. 009T ² 0. 0000T ³ +0. 13T-0. 002T ² +0. 0008T ³ -0. 59T+0. 009T ² 0. 0000T ³ -0. 08T 0. 000T ² 0. 000T ²	0.85T-1.311T ² -0.0002T ³ 0.19T-0.037T ² +0.0005T ³ +-0.84T+0.004T ² 0.0001T ³ +-0.12T			
2— 2 3— 2 4— 2 5— 2 6— 2	+0. I +0. 002T ² -0. I +0. 008T ² +0. 002T ² 0. 0 +0. 008T ²	+0. I 0. 000T² 0. 0 +0. 003T² 0. 000T² -0. I +0. 003T²			

The correction to the latitude on the same account can be divided into two portions; the first, which is periodic and dependent on the position of Jupiter, can be added to $\Delta\beta'$; the second, which is a function of l', can be applied to $\sin \beta_0'$. The first portion is

A '/ -/ 1	$\Delta(\Delta eta')$		A 1/2/11/2	arDelta(arDeltaeta')		
Arg=i'g'+ig	sin.	cos.	Arg=i'g'+ig	sin.	cos.	
i' i 2 0 4 0 —2— I ———————————————————————————————	0.0000 0.0000 0.0008 0.0001 0.0008	-0.0001 -0.0001 +0.0003 -0.0005 +0.0001	i' i 5— 1 I— 2 2— 2 3— 2 4— 2	-0.0003 +0.0002 +0.0033 -0.0006 +0.0011	,,, +0.0002 0.0000 -0.0026 +0.0007 -0.0082	
I— I 2— I 3— I 4— I	-0.0010 -0.0015 -0.0008 -0.0013	-0.0005 -0.0011 +0.0002 -0.0001	5— 2 6— 2 7— 2 8— 2	0. 0000 -0. 0023 +0. 0001 +0. 0001	+0.0012 -0.0032 +0.0002 0.0000	

The portion to be added to the expression for $\sin \beta_0$ is

CHAPTER XXVIII.

PRELIMINARY COMPARISON OF THE PRECEDING THEORY WITH OBSERVATION AND DERIVATION OF APPROXIMATE CORRECTIONS FOR THE ELEMENTS EMPLOYED IN THE CALCULATION OF THE PERTURBATIONS.

If the elements of the orbits of Jupiter and Saturn which have been employed in the preceding investigation were sufficiently approximate the expressions arrived at would need no further modification, except for possible changes in the values of the planetary masses. But as this is almost certainly not the case, we proceed to obtain approximate corrections for the provisionally adopted elements by a comparison of the preceding theory with observation. As the adopted planes of the orbits represent quite closely the observed latitudes of the planets, we need seek only the corrections of the four elements which give the position in orbit. Consequently comparison has been made only with normals in heliocentric longitude formed about the time of opposition. The thorough investigation of the values of the attracting masses must be deferred until the whole series of the observations, properly reduced, is taken in hand. The number of normals used here is very small on account of the great labor of making comparisons without the assistance of tables. There are only as many as are absolutely necessary for our purpose.

In forming the normals, Greenwich observations, taken precisely as they stand in the published volumes, without the application of any corrections, have been exclusively employed. Before 1830 the data have been derived from the Reduction of the Greenwich Observations of the Planets from 1750 to 1830. After 1830 the tabular longitude is from the English Nautical Almanac. Equal weights have been assigned to all the observations, and afterwards, in the discussion, all the normals have received equal weight.

We take up Saturn first, as the discussion of the observations of this planet will give us some information as to the mass of Uranus, which will be of service afterwards in treating Jupiter.

The normals constructed are as follows:

Greenwich M. T.	No. of observa- tions.	Tabular longitude.	Correction.	Observed heliocentric longitude.
1753, June 24.0	5	272 54 10.69	-18. 36	272 53 52. 33
1757, Aug. 11.0	7	318 47 10.89	-17. 82	318 46 53. 07
1761, Oct. 2.5	7	8 7 58.71	+ 0. 30	8 7 59. 01
1811, June 15.0	5	263 22 22.66	- 6. 31	263 22 16. 35

Greenwich M. T.	No. of observa-	Tabular longitude.	Correction.	Observed heliocentric longitude.
		0 / //	11	0 / 1/
1822, Oct. 30.0	6	36 40 22.56	+13.86	36 40 36.42
1837, May 4.0	10	223 50 29.0	— I. 74	223 50 27. 26
1844, July 26.0	11	303 57 52. 1	+11.99	303 58 4.09
1851, Oct. 24.0	12	30 49 43.9	+10.48	30 49 54.38
1858, Jan. 15.0	13	114 54 24.4	— 9.29	114 54 15.11
1866, Apr. 29.0	12	219 1 5.2	 4.81	219 1 0.39
1874, Aug. 3.0	12	310 57 53.6	+ 8.17	310 58 1.77
1882, Nov. 15.0	9	52 42 8.9	 7⋅35	52 42 1.55

The values of t in Julian years, and counted from the epoch 1850.0, and of the mean anomalies of Jupiter, Saturn, Uranus, and Neptune, for the dates of these normals, are:

t	g	g'	g''	g'''
	0 / 1/	0 / //	0 / //	0
96. 51747	98 47 21.27	185 9 38. 35	166 35 56	80. 94
92. 38604	224 10 25.64	235 39 4.49	184 18 6	89.96
88. 24230	349 55 56.09	286 17 32.68	202 3 26	99.02
38. 54620	58 9 40.65	173 38 6.13	55 0 6	207.59
27. 17044	43 24 18.10	312 39 35.40	103 44 46	232. 44
—12. 65982	123 47 17.28	129 59 45.30	165 55 23	264. 14
- 5.43190	343 8 55.59	218 19 45.70	196 53 39	27 9. 93
+ 1.81246	203 0 28.66	306 51 48.83	227 56 9	295.76
8. 04107	32 2 25.20	22 59 3.27	254 37 30	309.37
16. 32580	283 28 26.97	124 13 59.18	290 7 28	327.47
24. 58864	174 14 35.72	225 12 51.46	325 31 48	345.52
+32.87338	65 40 37.49	326 27 47.38	1 1 47	3. 62

By substituting these values in the several portions of the formula obtained for $n'\delta z'$ in the preceding chapters, we get the following quantities:

Perturbations of $n'z'$ by—					
Jupiter.	Uranus.	Jupiter × Uranus.	Neptune.	n'z'	f'
1 11	"	"	11	0 "	0 / //
—33 27. 245	56. 249	+29.860	—0. 730	184 35 43.99	184 6 52.44
36 26.311	-42. 067	+28.493	+1.189	235 2 25.79	229 59 9.61
43 59.803	7.428	+26. 439	+2.278	285 33 54.17	279 16 16.34
-34 54 392	-45.461	+25.517	0. 218	173 2 51.58	173 46 28.19
-43 10.712	-42.490	+20.603	—3. 207	311 55 59.59	306 55 35.95
52 49·437	2. 190	+22.848	+2.479	129 7 19.00	133 53 19.05
—40 24.661	41. 397	+20.990	+0.556	217 39 1.19	213 56 8.67
<u>—46 12. 502</u>	—IO. 227	+17.502	o. 288	306 5 43.32	300 41 23.28
—53 55.68o	+27.624	+17.479	—3. o87	22 5 49.61	24 40 47.77
-43 37. 181	6. 234	+19.561	+0. 346	123 30 35.67	128 39 33. 20
—22 31. 183	—20. 115	+17.024	+0.954	224 50 18. 14	220 31 40.13
33 15. 246	+17.727	+13.680	+0.618	325 55 4.16	322 5 59. 24

The $n'\delta z'$ must be understood as the $n'\delta z'$ before the modification of the preceding chapter is applied. In order to have the heliocentric longitude referred to the actual equinox of date it is necessary to add to f': first, π' , precession, nutation, and the secular part of the reduction to the ecliptic, and, second, the periodic part of the last. Thus we have the following quantities:

π' + precession + nutation.	Periodic reduction.	Calculated longitude.
0 / //	1 11	0 / //
88 46 6.19	+0 59.31	272 53 57-94
88 49 12.36	—I 19.83	318 47 2.14
88 52 38.04	o 44. 3o	8 8 10.08
89 34 26.32	+1 22.38	263 22 16.89
89 44 12.09	+0 47.62	36 40 35.66
89 56 0.11	+1 6.96	223 50 26.12
90 2 30.79	—о 38.74	303 58 o. 72
90 7 59.83	+0 28.48	30 49 51.59
90 13 34. 10	o 8.48	114 54 13.39
90 20 28,85	+0 53.28	219 0 55.33
90 27 14.62	—о 58.57	310 57 56. 18
90 34 30.67	+1 24.68	52 41 54.59

The equations of condition under three different suppositions are

				Supp. I.	Supp. II.	Supp. III.
0.896⊿]	L' — 0.8644(100	oΔn') — 0.140Δε	e' + 1.864 <i>e'</i> ∠		- 7.36	− 7.73
0.934	- 0.862 6	- 1.509	+ 1.184	= - 9.07	- 10,01	- 10.18
1.023	- 0.9026	<u> </u>	- 0.410	= - 11.07	- 9.63	- 9.44
0.896	- 0.3453	+ 0.211	+ 1.857	= - 0.54	- 1.86	- 1.89
1.073	- 0.2917	– 1. 631	- 1.312	= + 0.76	– 0.98	- 0.66
0.928	- 0.1175	+ 1.418	+ 1.281	= + 1.14	+ 2.56	+ 2.98
0.913	— 0 . 0496	- 1.094	+ 1.544	= + 3.37	+ 1.99	+ 2.18
1.063	+ 0.0193	- 1.750	- 1.125	= + 2.79	+ 3.36	+ 3.96
1.110	+ 0.0892	+ 0.859	- 1.957	= + 1.72	+ 5.43	+ 6.46
0.936	+ 0.1528	+ 1.539	+ 1.149	= + 5.06	+ 5.98	+ 6.47
0.921	+ 0.2265	- 1.276	+ 1.411	= + 5.59	+ 5.38	+ 5.14
1.095	+ 0.3602	— 1.2 60	- 1.705	= + 6.96	+ 9.51	+ 9.48

Supposition I is obtained by subtracting the calculated from the observed longitudes. The remaining suppositions will be explained shortly. The normal equations resulting from these equations are

```
Supp. I.
                                                                                   Supp. II.
                                                                                                Supp. III.
  11.655\Delta L' - 2.414(100 \Delta n') - 6.836\Delta e' + 2.350e'\Delta n' = + 2.05 \text{ or } + 6.25 \text{ or } + 8.82
                                                                  = + 27.08 \text{ or} + 30.32 \text{ or} + 30.59
                                                 — 3.064
- 2.414
              + 2.739
                                   + 3.043
- 6.836
                                  + 21.554
                                                 + 3.830
                                                                  = + 21.55 \text{ or } + 27.09 \text{ or } + 27.82
              + 3.043
+ 2.350
              -3.064
                                  + 3.830
                                                 + 25.555
                                                                  = - 16.70 \text{ or } - 33.61 \text{ or } - 36.63
```

The solution of these equations gives

I. II. III.

"" " "

$$\Delta L' = + 2.688$$
 or $+ 3.688$ or $+ 4.049$
 $\Delta n' = + 0.13188$ or $+ 0.13630$ or $+ 0.13662$
 $\Delta e' = - 0.134$ or $+ 0.520$ or $+ 0.694$
 $e' \Delta \pi' = + 0.701$ or $- 0.100$ or $- 0.272$

The residuals (observation-calculation), severally, in the three suppositions are

	I.	II.	III.
	"	"	"
1753, June 24.0	+ 2.05	+ 1.36	+ 1.06
1757, Aug. 11.0	- 1.23	- ∘. 79	<u> </u>
1761, Oct. 2.5	- 1.89	- 0.11	+ 0.02
1811, June 15.0	+ 0.33	- 0.38	- 0.44
1822, Oct. 30.0	+ 2.42	- 0.24	- 0.26
1837, May 4.0	- 0.52	+ 0.12	+ 0.20
1844, July 26.0	+ 0.33	+ 0.01	+ 0.34
1851, Oct. 24.0	+ 0.23	- 0.03	+ 0.31
1858, Jan. 15.0	- 0.95	- 0.52	0.38
1866, Apr. 29.0	- 0.06	- 0.23	- 0.17
1874, Aug. 3.0	— 1.04	- 0.31	- 0.41
1882, Nov. 15.0	+ 0:28	+ 1.02	+ 0.53

The residuals of Supposition I are not altogether satisfactory, and, on comparing them with the portions of the perturbations which are proportional to the mass of Uranus, it is suggested that a better agreement would be obtained by diminishing this mass. Hence, I concluded to put the value at $\frac{1}{22640}$, which is about the average of all the results which have been obtained from the observations of the satellites at the Washington Observatory. This has given rise to the numbers of the column headed Supposition II. It will be seen that the residuals of (II) are fairly satisfactory, and it does not seem worth while, in this preliminary investigation, to inquire whether we should do better with another value of the mass of Uranus.

The pertubations being now corrected for the changes in the elements shown by (II), and for the similar ones to be given hereafter for Jupiter, the resulting numbers appear under Supposition III, to which we hold as being the best which can be done at present. The residuals of (III) are to some extent better than those of (II).

We now pass to Jupiter. The normals are formed as follows:

Greenwich M. T.	No. of observa- tions.	Tabular longitude.	Correction.	Heliocentric longitude from observation.
		0 / //	"	0 / //
1757, May 3.5	7	223 44 36.85	+ 6.59	223 44 43.44
1759, July 9.5	8	287 33 42.20	+10.70	287 33 52.90
1819, Aug. 5.5	12	312 16 54.91	+ 6.78	312 17 1.69
1855, Aug. 22.0	16	327 44 57.70	— 5.46	327 44 52.24
1858, Dec. 16.0	9	77 11 8.30	+ 5.87	77 11 14.17
1861, Feb. 16.0	11	142 29 48. 10	+ 8.31	142 29 56.41
1864, May 16.0	9	232 58 30.70	+17.35	232 58 48.05
1867, Aug. 23.0	6	332 18 32.80	+ 0.77	332 18 33.57
1870, Dec. 19.0	6	81 53 54.70	+ 7.63	81 54 2.33
1874, Mar. 18.0	12	176 56 16.60	+ 7.27	176 56 23.87
1877, June 19.0	11	268 41 48.00	+15.26	268 42 3.26
1878, July 20.0	7	301 49 21.10	— o. 17	301 49 20.93
1880, Oct. 7.0	12	14 30 48.20	+ 0.18	14 30 48.38

The values of t in Julian years, counted from 1850.0, and of the mean anomalies of Jupiter, Saturn, Uranus, and Neptune for the dates of these normals, are:

t		g			g'			$g^{\prime\prime}$		g'''
	0	,	//	0		,,	0	,	11	0
92. 65847	215	54	33.83	232	19	19. 25	183	8	4	89. 37
<u> </u>	282	7	58. 96	258	59	21.65	192	29	5	94. 14
30. 40520	305	14	9.63	273	7	38. 17	89	53	7	225. 37
+ 5.6399 7	319	10	21.25	353	38	24. 50	244	20	11	304. 12
8. 9582 5	59	52	44.57	34	ΙI	35.59	258	33	18	311.37
11. 12936	125	46	13.19	60	43	36. 17	267	51	29	316. 11
14. 37372	224	14	0.04	100	22	34. 98	281	45	35	323. 20
17. 64271	323	26	39.05	140	19	37.89	295	46	8	330. 34
20 . 9664 6	64	19	0.62	180	56	49. 90	310	0	33	337.61
24. 21082	162	46	47 - 47	220	35	48.71	323	54	40	344. 69
27. 46612	261	34	30. 84	260	22	49.35	337	51	35	351.81
28. 55031	294	28	45.59	273	37	49.41	342	30	20	354. 17
+30.76796	1	46	5 9· 39	300	43	57-72	352	0	29	359.02
1 3 1 - 1 - 1										

By substituting these values in the several portions of the formula obtained for $n\delta z$ in the preceding chapters, multiplying the part due to the action of Uranus by the factor $\frac{21000}{22640}$, we get the following quantities:

Perturbation of nz by—										
Sat	turn.	Uranus.	Saturn × Uranus.	Neptune.		nz			ſ	
/	,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,	"	"	"	0	,	"	0	,	"
+18	36. 578	—0, 140	8. 244	—о. 389	216	13	1.63	213	6	14. 83
14	0.876	+0. 205	8. 205	0. 104	282	21	51.73	276	54	7 - 47
12	31. 844	o. 164	6. 581	-0.031	305	26	34. 70	300	46	53.00
19	50. 624	+o. 518	5. 380	+0.057	319	30	7.07	315	44	32.43
18	3. 316		4. 846	—о. обо	60	10	43.03	65	7	0. 23
19	59. 079	— 0. 164	5. 161	0. 184	126	6	6. 76	130	24	39. 61
19	8.804	+0.052	5. 609	+0.172	224	33	3. 46	220	50	7. 14
8	15. 384	+1.595	4-957	0. 029	323	34	51.04	320	8	1.98
14	13.009	—0. 098	4. 496	-0.004	64	33	9. 03	69	40	12.63
22	54. 849	0. 133	5. 074	0.091	163	9	37.02	164	40	26. 55
13	19. 365	—1. 18 <u>5</u>	5. 089	+0. 239	261	47	44. 17	256	22	43.46
9	33. 806	0. 584	4.830	+o. 14 8	294	38	14. 13	289	29	23. 34
+ 9	27. 323	+1.446	-4. 256	0. 094	1	56	23. 81	2	8	20.61

Applying to f the longitude of the perihelion, precession, nutation, and the reduction to the ecliptic, we have the calculated longitude as follows:

	π + precession + nutation.		Periodic reduction.	Calculated longitu		
0	,	11	"	0	,	"
10	38	20.02	-+25.85	223	45	0.70
10	40	5.98	8. 92	287	34	4.53
11	30	38. 14	-25.01	312	17	6. 13
12	0	43.61	-26.78	327	44	49. 26
12	3	47.02	- 18.66	77	11	5.91
12	5	45.97	26. 96	142	29	58.62
12	8	23.83	+26.97	232	58	57.94
I 2	10	52.55	-25.89	332	18	28. 64
12	13	26. 08	+15.28	81	53	53.99
12	16	16. 18	—11.17	176	56	31.56
12	19	17. 07	+ 9.68	268	42	10. 21
12	20	17.64	-19.13	301	49	21.85
12	22	12.45	+ 4.92	14	30	37.98

The equations of condition under three different suppositions are

				Supp. I.	Supp. II.	Supp. III.
0.9244	L — 0.8562(100	o⊿n) — 1.073⊿o	e + 1.575e2	$\Delta \pi = -17.26$	- 22.97	- 17.26
1.015	- 0.9184	– 1. 996	- 0.315	= - 11.63	- 16.34	— 11.61
1.054	- 0.3204	— 1.744	- 1.113	= - 4.44	– 8.81	4.50
1.074	+ 0.0606	- 1.422	— 1.537	=+ 2.98	- 4.12	+ 2.96
1.045	0.0936	+ 1.837	0.926	=+8.26	+ 1.98	+ 8.13
0.942	0.1048	+ 1.502	+ 1.209	=-2.21	- 8.47	- 2.39
0.932	0.1339	— 1.286	+ 1.419	= -9.89	— 15.82	- 9.99
1.079	0.1904	- 1.309	- 1.641	=+ 4.93	+ 1.98	+ 4.93
1.038	0.2175	+ 1.896	- 0.776	= + 8.34	+ 3.44	+ 8.24
0.912	0.2208	+ 0.517	+ 1.818	= - 7.69	- 14.65	- 7.84
0.981	0.2694	1.936	+ 0.397	= - 6.95	- 11.29	- 6.98
1.0,36	0.2958	- 1.905	- 0.747	= - 0.92	- 4.20	- 0.90
1.103	+ 0.3392	+ 0.077	- 2.125	= + 10.40	+ 0.94	+ 10.42

The normal equations resulting from these equations are

```
Supp. I. Supp. II. Supp. III. Supp. III. ^{''} 13.318\DeltaL -0.097(100\Delta n) -7.008\Delta e -3.836e\Delta\pi = -21.25 or -87.59 or -21.94 -0.097 +2.128 +2.599 -1.481 = +28.73 or +30.40 or +28.63 -7.008 +2.599 +30.443 +3.462 = +91.19 or +116.47 or +90.69 -3.836 -1.481 +3.462 +22.344 = -100.19 or -98.05 or -100.59
```

Their solution gives

I. II. III.
$$\Delta L = -1.540 \quad \text{or} \quad -6.923 \quad \text{or} \quad -1.615$$

$$\Delta n = +0.07024 \quad \text{or} \quad +0.07491 \quad \text{or} \quad +0.06989$$

$$\Delta e = +2.574 \quad \text{or} \quad +2.210 \quad \text{or} \quad +2.546$$

$$e \Delta \pi = -4.683 \quad \text{or} \quad -5.424 \quad \text{or} \quad -4.711$$

The residuals (observation-calculation), severally in the three suppositions, are

	I. "	II.	ш.
1757, May 3.5	+ 0.30	+ 0.75	+ 0.35
1759, July 9.5	+ 0.05	+ 0.27	+ 0.05
1819, Aug. 5.5	- 1.29	- 1.31	- 1.36
1855, Aug. 22.0	+ 0.66	- 2.33	+ 0.65
1858, Dec. 16.0	+ 0.15	- 0.58	+ 0.12
1861, Feb. 16.0	+ 0.31	+ 0.51	+0.28
1864, May 16.0	+ 0.55	+ 0.16	+ 0.53
1867, Aug. 23.0	+ 0.93	+ 2.01	+ 0.94
1870, Dec. 19.0	- 0.10	+ 0.58	- 0.10
1874, Mar. 18.0	— 0.66	— 1.2 6	– 0.67
1877, June 19.0	- 0.49	- 0.08	- 0.48
1878, July 20.0	0.00	+ 0.92	+ 0.05
1880, Oct. 7.0	- 0.44	+ 0.33	0.39

Supposition I corresponds to Bessel's value $\frac{1}{35^{\circ}1.6}$ of the mass of Saturn, while (II) results from using the value $\frac{1}{3482.2}$, recently derived by Prof. A. Hall from observations of Japetus. The residuals of (II) are generally larger than those of (I), and, in consequence, I shall hold to Bessel's value, although it is possible that when the observations are more properly reduced a better showing may result for the larger mass. In fine, Supposition III results from (I) by applying to the perturbations the corrections due to the adopted changes in the elements.*

^{*}It will be noticed that some of the numbers given in this chapter differ slightly from those stated in the Astr. Nachr., Nos. 2705–2706. This is because at the time of the publication of the latter the term — B tan $\frac{i}{2}$, in the reduction of orbit to ecliptic longitude (in formula on page 523), had not been noticed. Hansen determines his $n\delta z$ in such a way that it contains no term rigorously proportional to the time. This differs from the course followed by those who employ other methods of perturbation. They make the orbit longitude, as measured along a fixed ecliptic until the node is reached and then on the plane of the orbit, to have no perturbations proportional to t. But Hansen regards the term $2 \sin^2 \frac{i}{2} \frac{d\theta}{dt}$ as belonging to the reduction to the ecliptic.

CHAPTER XXIX.

RECTIFICATION OF THE FORMULÆ FOR THE PERTURBATIONS ON ACCOUNT OF THE CORRECTIONS
OF THE ELEMENTS JUST DETERMINED

Hansen has treated this matter,* but the expressions he derives are suitable to the employment of the eccentric anomaly as independent variable. As the modifications, to be made in order to render them applicable when the mean anomaly or the time is employed as independent variable, are not readily perceived, we will, as briefly as possible, develop them here.

We shall suppose that the elements which define the positions of the planes of the two orbits are known at the outset with sufficient exactitude to insure the desired degree of accuracy in the expressions of the perturbations so far as it depends on them. We can also suppose that the terms of two dimensions, with respect to disturbing forces, require no sensible correction on account of changes made in the elements; and we may assume that the same is true for u and u'. Hence, we shall limit our attention to determining the effects produced in the first-order terms of $n\delta z$, ν , $n'\delta z'$, and ν' .

Consequently, we can assume

$$\frac{1}{n} \frac{dW_0}{dt} = T = Aa_0 \frac{d\Omega}{dg} + Ba_0 r \frac{d\Omega}{dr}$$

$$n\delta z = \int \left[\int Tn dt \right] n dt$$

$$\nu = \text{const.} - \frac{1}{2} \int \left(\frac{\overline{d} \cdot \left[\int Tn dt \right]}{d\gamma} \right) n dt$$

The augmentation of the elements being denoted by Δa , $\Delta a'$, Δe , $\Delta e'$, $\Delta \pi$, and $\Delta \pi'$, we have

$$\begin{split} \varDelta\mathbf{T} &= \frac{d\mathbf{T}}{da}\varDelta a + \frac{d\mathbf{T}}{da'}\varDelta a' + \frac{d\mathbf{T}}{de}\varDelta e + \frac{d\mathbf{T}}{de'}\varDelta e' + \frac{d\mathbf{T}}{d\pi}\varDelta \pi + \frac{d\mathbf{T}}{d\pi'}\varDelta \pi' \\ \mathbf{T} &= \frac{a}{\cos\varphi}\bigg[\,_2\frac{\rho}{r}\cos\left(f-\omega\right) - _1 + \frac{_2\rho}{a\cos^2\varphi}\big[\cos\left(f-\omega\right) - _1\big]\,\bigg]\frac{d\Omega}{d\upsilon} + \frac{_2a}{\cos\varphi}\frac{\rho}{r}\sin\left(f-\omega\right)r\frac{d\Omega}{dr} \end{split}$$

T may be regarded, then, as a function of a, φ , ρ , r, f, ω , f', r', π , and π' ; or, what is the same thing, as a function of a, φ , ρ , r, r', $f + \pi$, $\omega + \pi$, and $f' + \pi'$. And it is evident that, instead of taking the partial derivatives of T with respect to $f + \pi$, $\omega + \pi$,

and $f' + \pi'$, we may take them with respect to g, γ , and g', provided that Δg , $\Delta \gamma$, and $\Delta g'$ are determined by the equations

$$\Delta g = \frac{\frac{df}{de}}{\frac{de}{dg}} \Delta e + \frac{\mathbf{I}}{\frac{df}{dg}} \Delta \pi$$

$$\Delta \gamma = \frac{\frac{d\omega}{de}}{\frac{d\omega}{d\gamma}} \Delta e + \frac{\mathbf{I}}{\frac{d\omega}{d\gamma}} \Delta \pi$$

$$\Delta g' = \frac{\frac{df'}{de'}}{\frac{df'}{dg'}} \Delta e' + \frac{\mathbf{I}}{\frac{df'}{dg'}} \Delta \pi'$$

and that we conceive r, ρ , and r' to be augmented by $r\Delta \nu$, $\rho\Delta\beta$, and $r'\Delta\nu'$, such that

$$\Delta \nu = \frac{\Delta a}{a} - \frac{\cos \varepsilon + e}{\cos^2 \varphi} \Delta e - \frac{e \sin \varepsilon}{\cos \varphi} \Delta \pi$$

$$\Delta \beta = \frac{\Delta a}{a} - \frac{\cos \eta + e}{\cos^2 \varphi} \Delta e - \frac{e \sin \eta}{\cos \varphi} \Delta \pi$$

$$\Delta \nu' = \frac{\Delta a'}{a'} - \frac{\cos \varepsilon' + e'}{\cos^2 \varphi'} \Delta e' - \frac{e' \sin \varepsilon'}{\cos \varphi'} \Delta \pi'$$

Then, we have

$$\varDelta\mathbf{T} = \frac{d\mathbf{T}}{d\sigma}\varDelta g + \frac{d\mathbf{T}}{d\sigma'}\varDelta g' + r\frac{d\mathbf{T}}{dr}\varDelta \nu + r'\frac{d\mathbf{T}}{dr'}\varDelta \nu' + a\frac{d\mathbf{T}}{da}\frac{\varDelta a}{a} + \frac{d\mathbf{T}}{d\varphi}\varDelta \varphi + \frac{d\mathbf{T}}{d\nu}\varDelta \gamma + \rho\frac{d\mathbf{T}}{d\rho}\varDelta \beta$$

The coefficients of the first four terms have already been used for the computation of the second-order terms. Also

$$\begin{split} a\frac{d\mathbf{T}}{da} &= \mathbf{T} - \frac{4\rho}{\cos^3\varphi} [\cos{(f-\omega)} - \mathbf{1}] \frac{d\Omega}{dv} \\ \mathbf{T} &= \frac{a}{\cos\varphi} \frac{d\Omega}{dv} \end{split}$$

In computing the second-order terms we have derived the value of

$$\mathbf{X} = -\frac{2a}{\cos \alpha} \frac{\rho}{r} \cos (f - \omega) \cdot \frac{d\Omega}{dv} - \frac{2a}{\cos \omega} \frac{\rho}{r} \sin (f - \omega) \cdot r \frac{d\Omega}{dr}$$

whence

$$a\frac{d\mathbf{T}}{da} = \mathbf{T} - 2(\mathbf{T} + \mathbf{X} + \mathbf{T}) = \mathbf{T} - \mathbf{C}$$

where C has also been employed in treating the second-order terms. In the next place

$$\frac{d\mathbf{T}}{d\varphi} = \frac{e}{\cos\varphi} \left[\mathbf{T} + 2(\mathbf{T} + \mathbf{X} + \bar{\mathbf{T}}) \right] = \frac{e}{\cos\varphi} \left[\mathbf{T} + \mathbf{C} \right]$$

Consequently, as

$$\log h = \text{const.} - \frac{1}{2} \log a - \log \cos \varphi$$

and thence

$$\frac{\Delta h}{h} = -\frac{1}{2} \frac{\Delta a}{a} + \frac{e}{\cos \varphi} \Delta \varphi$$

we shall have

$$\varDelta\mathbf{T} = \mathbf{A}\varDelta g + \mathbf{F}\varDelta g' + \mathbf{B}\varDelta \nu + \mathbf{G}\varDelta \nu' + \mathbf{C}\left(\frac{\varDelta h}{h} - \frac{\mathbf{i}}{2}\frac{\varDelta a}{a}\right) + \mathbf{T}\left(\frac{\varDelta a}{a} + \frac{e\varDelta e}{\cos^2\varphi}\right) + \frac{d\mathbf{T}}{d\varphi}\varDelta \gamma + (\mathbf{T} + \mathbf{T})\varDelta \beta$$

The computation of the first five terms of this formula is then quite similar to that of the second-order terms, and we may put

$$L = A\Delta g + F\Delta g' + B\Delta v + G\Delta v' + C\left(\frac{\Delta h}{h} - \frac{1}{2}\frac{\Delta a}{a}\right)$$

Integrating, we derive

$$\begin{split} \varDelta \mathbf{W}_0 &= \int \mathbf{L} n dt + \left(\frac{\varDelta a}{a} + \frac{e \varDelta e}{\cos^2 \varphi}\right) \mathbf{W}_0 + \varDelta \beta (\mathbf{W}_0 + \int \mathbf{T} n dt) \right. \\ &+ \frac{d \mathbf{W}_0}{d \gamma} \varDelta \gamma \\ &= \int \mathbf{L} n dt + \left(\frac{\varDelta a}{a} + \frac{e \varDelta e}{\cos^2 \varphi}\right) \mathbf{W}_0 + \varDelta \beta (\mathbf{W}_0 + \overline{\mathbf{W}_0} + 2\nu) + \frac{d \mathbf{W}_0}{d \gamma} \varDelta \gamma \\ \\ \varDelta (n \delta z) &= \int \left[\left(\overline{\int \mathbf{L} n dt} \right) + \left(\frac{\overline{d} \mathbf{W}_0}{d \gamma} \right) \varDelta g + 2(\mathbf{W}_0 + \nu) \varDelta \nu + \left(\frac{\varDelta a}{a} + \frac{e}{\cos^2 \varphi} \varDelta e \right) \overline{\mathbf{W}_0} \right] n dt \\ &= \int \left[\left(\overline{\int \mathbf{L} n dt} \right) - 2 \frac{d \nu}{n dt} \varDelta g + 2 \left(\frac{d}{\cdot \delta z} + \nu \right) \varDelta \nu \right] n dt + \left(\frac{\varDelta a}{a} + \frac{e}{\cos^2 \varphi} \varDelta e \right) n \delta z \\ \\ \varDelta \nu &= -\frac{1}{2} \int \left[\left(\overline{\frac{d}{\cdot \int \mathbf{L} n dt}} \right) + \left(\overline{\frac{d^2 \mathbf{W}_0}{d \gamma^2}} \right) \varDelta g + \left(\overline{\frac{d \mathbf{W}_0}{d \gamma}} \right) \frac{d \cdot \varDelta g}{dg} + \left(\frac{\varDelta a}{a} + \frac{e}{\cos^2 \varphi} \varDelta e \right) \left(\overline{\frac{d \mathbf{W}_0}{d \gamma}} \right) \right. \\ &+ \left(\overline{\frac{d \mathbf{W}_0}{d \gamma}} \right) \varDelta \nu + 2 (\mathbf{W}_0 + \nu) \frac{d \cdot \varDelta \nu}{dg} \right] n dt \end{split}$$

But from formulæ to be given shortly it will be seen that

$$\frac{d \cdot \Delta g}{dg} = 2 \frac{\Delta a}{a} - 2 \Delta \nu - \frac{e}{\cos^2 \varphi} \Delta e$$

Hence

$$\begin{split} \varDelta\nu &= -\frac{\mathrm{i}}{2} \int \left[\left(\overline{\frac{d \cdot \int \mathrm{L} n dt}{d \gamma}} \right) + \left(\overline{\frac{d^2 \overline{\mathrm{W}_0}}{d \gamma^2}} \right) \varDelta g + \left(\overline{\frac{d \overline{\mathrm{W}_0}}{d \gamma}} \right) \left(3 \frac{\varDelta a}{a} - \varDelta \nu \right) + 2 (\overline{\mathrm{W}_0} + \nu) \frac{d \cdot \varDelta \nu}{d g} \right] n dt \\ &= -\frac{\mathrm{i}}{2} \int \left[\left(\overline{\frac{d \cdot \int \mathrm{L} n dt}{d \gamma}} \right) + \left(\overline{\frac{d^2 \overline{\mathrm{W}_0}}{d \gamma^2}} \right) \varDelta g + 2 \overline{\mathrm{W}_0} \frac{d \cdot \varDelta \nu}{d g} \right] n dt - \nu \left(\varDelta \nu - 3 \frac{\varDelta a}{a} \right) \end{split}$$

The expressions for Δg and Δv are

$$\begin{split} \varDelta g = & \frac{2\varDelta e}{\cos^2\varphi} \bigg[\bigg(J_{\frac{e}{2}}^{(0)} - J_{\frac{e}{2}}^{(3)} \bigg) \sin g + \frac{\mathrm{I}}{4} (J_{e}^{(1)} - J_{e}^{(3)}) \sin 2g + \frac{\mathrm{I}}{9} \bigg(J_{\frac{3}{2}^{e}}^{(2)} - J_{\frac{3}{2}^{e}}^{(4)} \bigg) \sin 3g + \ldots \bigg] \\ & + \frac{\varDelta\pi}{\cos\varphi} \bigg[\mathrm{I} + \frac{3}{2} e^2 - \frac{2e}{\mathrm{I}} \bigg(J_{\frac{e}{2}}^{(0)} + J_{\frac{e}{2}}^{(2)} \bigg) \cos g - \frac{2e}{4} (J_{e}^{(1)} + J_{e}^{(3)}) \cos 2g - \frac{2e}{9} \bigg(J_{\frac{3}{2}^{e}}^{(2)} + J_{\frac{e}{2}}^{(4)} \bigg) \cos 3g - \ldots \bigg] \\ \varDelta\nu = & \frac{\varDelta a}{a} - \frac{\varDelta e}{\cos^2\varphi} \bigg[\frac{1}{2} e + \bigg(J_{\frac{e}{2}}^{(0)} - J_{\frac{e}{2}}^{(2)} \bigg) \cos g + \frac{\mathrm{I}}{2} (J_{e}^{(1)} - J_{e}^{(3)}) \cos 2g + \frac{\mathrm{I}}{3} \bigg(J_{\frac{3}{2}^{e}}^{(2)} - J_{\frac{3}{2}^{e}}^{(4)} \bigg) \cos 3g + \ldots \bigg] \\ & - \frac{e\varDelta\pi}{\cos\varphi} \bigg[\bigg(J_{\frac{e}{2}}^{(0)} + J_{\frac{e}{2}}^{(2)} \bigg) \sin g + \frac{\mathrm{I}}{2} (J_{e}^{(1)} + J_{e}^{(3)}) \sin 2g + \frac{\mathrm{I}}{3} \bigg(J_{\frac{3}{2}^{e}}^{(2)} + J_{\frac{3}{2}^{e}}^{(4)} \bigg) \sin 3g + \ldots \bigg] \end{split}$$

We have yet to ascertain the corrections due to the change of the integrating factors. T being a function composed of such terms as

$$T = A \sin (\varkappa \gamma + i'g' + ig) + B \cos (\varkappa \gamma + i'g' + ig)$$

we have

$$W_0 = -\frac{A}{i'\frac{n'}{n} + i}\cos\left(n\gamma + i'g' + ig\right) + \frac{B}{i'\frac{n'}{n} + i}\sin\left(n\gamma + i'g' + ig\right)$$

Whence

$$\varDelta \mathbf{W}_{0} = \left[\frac{i'\mathbf{A}}{\left(i'\frac{n'}{n} + i\right)^{2}} \cos\left(n\gamma + i'g' + ig\right) - \frac{i'\mathbf{B}}{\left(i'\frac{n'}{n} + i\right)^{2}} \sin\left(n\gamma + i'g' + ig\right) \right] \varDelta \frac{n'}{n}$$

But

$$\int W_0 n dt = \frac{A}{\left(i'\frac{n'}{n} + i\right)^2} \sin\left(u\gamma + i'g' + ig\right) - \frac{B}{\left(i'\frac{n'}{n} + i\right)^2} \cos\left(u\gamma + i'g' + ig\right)$$

whence

$$\Delta \mathbf{W}_0 = -\frac{d \cdot \int \mathbf{W}_0 n dt}{dg'} \Delta \frac{n'}{n}$$

and

$$\Delta \overline{\mathbf{W}_{0}} = -\frac{d \cdot (\overline{\int \mathbf{W}_{0} n dt})}{dg'} \Delta \frac{n'}{n} = -\left(\overline{\int \frac{d \mathbf{W}_{0}}{dg'} n dt}\right) \Delta \frac{n'}{n}$$

In like manner

$$-\frac{\mathbf{I}}{2}\!\left(\overline{\varDelta\frac{d\mathbf{W}_0}{d\gamma}}\right)\!=\!\frac{\mathbf{I}}{2}\!\left(\overline{\int\frac{d^2\mathbf{W}_0}{d\gamma dg'}ndt}\right)\!\varDelta\frac{n'}{n}$$

Thus, we have, for getting the corrections of the perturbations due to a change in the integrating factors, the very simple formulæ

$$\Delta(n\delta z) = -2 \left[\int \frac{d \cdot (n\delta z)}{dg'} n dt \right] \Delta \frac{n'}{n}$$

$$\Delta v = -2 \left[\int \frac{dv}{dg'} n dt \right] \Delta \frac{n'}{n}$$

On account of the smallness of the eccentricities of the major planets it often happens that the corrections $\Delta\pi$ and $\Delta\pi'$ are quite large, while the effects of these corrections on the positions of the planets, being more properly represented by the products $e\Delta\pi$ and $e'\Delta\pi'$, are quite small. In these cases it may be reasonably feared, since Δg and $\Delta \gamma$ contain the term

$$\frac{1+\frac{3}{2}e^2}{\cos\varphi}\Delta\pi$$

and $\Delta q'$ the term

$$\frac{1 + \frac{3}{2}e'}{\cos \varphi'} \Delta \pi'$$

that it will not be sufficiently approximate to consider the corrections of the perturbations as equivalent to linear functions of Δg , Δv , $\Delta g'$, $\Delta v'$, etc., the terms involving the squares of Δg and $\Delta g'$ and their products with Δv , $\Delta v'$, etc., becoming sensible on account of the largeness of $\Delta \pi$ and $\Delta \pi'$.

A little consideration, however, shows that this difficulty may be readily surmounted. Let us suppose that putting, for the sake of brevity,

$$\mathbf{E} = \frac{\mathbf{I} + \frac{3}{2}e^2}{\cos \varphi} \qquad \qquad \mathbf{E}' = \frac{\mathbf{I} + \frac{3}{2}e'}{\cos \varphi'}$$

we substitute for Δg , $\Delta \gamma$, and $\Delta g'$ the expressions

$$\Delta g = \mathbf{E} \Delta \pi + \Delta(g)$$

$$\Delta \gamma = \mathbf{E} \Delta \pi + \Delta(\gamma)$$

$$\Delta g' = \mathbf{E}' \Delta \pi' + \Delta(g')$$

so that

$$\begin{split} \varDelta(g) = & \quad \frac{2\varDelta e}{\cos^2\varphi} \bigg[\bigg(J_{\frac{s}{2}}^{(0)} - J_{\frac{s}{2}}^{(2)} \bigg) \sin g + \frac{\mathrm{I}}{4} \bigg(J_{\epsilon}^{(1)} - J_{\epsilon}^{(3)} \bigg) \sin 2g + \frac{\mathrm{I}}{9} \bigg(J_{\frac{3}{2}s}^{(2)} - J_{\frac{3}{2}s}^{(4)} \bigg) \sin 3g + . \quad . \quad . \bigg] \\ & - \frac{2e\varDelta\pi}{\cos\varphi} \left[\bigg(J_{\frac{s}{2}}^{(0)} + J_{\frac{s}{2}}^{(2)} \bigg) \cos g + \frac{\mathrm{I}}{4} \bigg(J_{\epsilon}^{(1)} + J_{\epsilon}^{(3)} \bigg) \cos 2g + \frac{\mathrm{I}}{9} \bigg(J_{\frac{3}{2}s}^{(3)} + J_{\frac{3}{2}s}^{(4)} \bigg) \cos 3g + . \quad . \quad . \bigg] \end{split}$$

with a similar expression for $\Delta(g')$. Now, when g, γ , and g' are augmented by their increments Δg , $\Delta \gamma$, and $\Delta g'$, the variation of the arguments due to the terms $\mathbf{E} \Delta \pi$ and $\mathbf{E}' \Delta \pi'$ may be retained within the functional signs sin and cos, and the corrections of the perturbations exhibited as a linear function of $\Delta(g)$, $\Delta(g')$, etc. Thus the general argument $n\gamma + i'g' + ig$ becomes

$$n\gamma + i'g' + ig + (n + i)\mathbf{E}\Delta\pi + i'\mathbf{E}'\Delta\pi'$$

The presence of the two terms ending this expression evidently has no influence on the coefficient when integrations are performed, or when we go through the operation of putting $\gamma = g$. Hence the following precept:

In the preceding formulæ, for obtaining the corrections of the perturbations arising from changes in the elements, we may everywhere substitute $\Delta(g)$ and $\Delta(g')$ for Δg and $\Delta g'$, provided that at the end, when the expressions for the perturbations have been reduced to series of terms of the form

$$\mathbb{K} n^k t^k \sin_{\cos} \left(i'g' + ig + \varkappa \right)$$

we replace * by

$$\varkappa + i \mathbf{E} \Delta \pi + i' \mathbf{E}' \Delta \pi'$$

or, which applies to any form the perturbations may be in, we everywhere replace g by $g + E \Delta \pi$, and g' by $g' + E' \Delta \pi'$.

In applying these formulæ to Jupiter and Saturn it was assumed that

$$\Delta e = + 2.566$$
 $\Delta e' = + 0.527$
 $e \Delta \pi = - 4.550$ $e' \Delta \pi' = - 0.093$
 $\Delta n = + 0.06958$ $\Delta n' = + 0.12853$

From these numbers we derive

$$\log \frac{\Delta a}{a} = 3.6280n$$

$$\log 2\Delta \frac{n'}{n} = 4.2648$$

$$\log 2\Delta \frac{n}{n'} = 5.0548n$$

$$\log \left(\frac{\Delta a}{a} + \frac{e\Delta e}{\cos^2 \varphi}\right) = 3.2479$$

$$\log \left(\frac{\Delta a'}{a'} + \frac{e'\Delta e'}{\cos^2 \varphi'}\right) = 4.2563n$$

$$E\Delta \pi = -1'34''.75$$

$$E'\Delta \pi' = -1''.67$$

$$\Delta(g) = 2 \begin{bmatrix} 5.0955 \end{bmatrix} \sin g + 2 \begin{bmatrix} 5.3440 \end{bmatrix} \cos g$$

$$+ 2 \begin{bmatrix} 3.1766 \end{bmatrix} \sin 2g + 2 \begin{bmatrix} 3.4251 \end{bmatrix} \cos 2g$$

$$+ 2 \begin{bmatrix} 1.5587 \end{bmatrix} \sin 3g + 2 \begin{bmatrix} 1.8073 \end{bmatrix} \cos 3g$$

$$\Delta(g') = 2 \begin{bmatrix} 4.4073 \end{bmatrix} \sin g' + 2 \begin{bmatrix} 3.6553 \end{bmatrix} \cos g'$$

$$+ 2 \begin{bmatrix} 2.5535 \end{bmatrix} \sin 2g' + 2 \begin{bmatrix} 1.8016 \end{bmatrix} \cos 2g'$$

$$+ 2 \begin{bmatrix} 1.0007 \end{bmatrix} \sin 3g' + 2 \begin{bmatrix} 0.2489 \end{bmatrix} \cos 3g'$$

$$\Delta \nu = - \begin{bmatrix} 3.8606 \end{bmatrix}$$

$$- 2 \begin{bmatrix} 4.7945 \end{bmatrix} \cos g + 2 \begin{bmatrix} 5.0430 \end{bmatrix} \sin g$$

$$- 2 \begin{bmatrix} 3.1766 \end{bmatrix} \cos g + 2 \begin{bmatrix} 3.4251 \end{bmatrix} \sin g$$

$$- 2 \begin{bmatrix} 1.7348 \end{bmatrix} \cos g + 2 \begin{bmatrix} 3.3543 \end{bmatrix} \sin g'$$

$$- 2 \begin{bmatrix} 2.5535 \end{bmatrix} \cos g' + 2 \begin{bmatrix} 3.3543 \end{bmatrix} \sin g'$$

$$- 2 \begin{bmatrix} 2.5535 \end{bmatrix} \cos g' + 2 \begin{bmatrix} 1.8016 \end{bmatrix} \sin 2g'$$

$$- 2 \begin{bmatrix} 1.1768 \end{bmatrix} \cos g' + 2 \begin{bmatrix} 1.8016 \end{bmatrix} \sin 2g'$$

$$- 2 \begin{bmatrix} 1.1768 \end{bmatrix} \cos g' + 2 \begin{bmatrix} 1.8016 \end{bmatrix} \sin 2g'$$

$$- 2 \begin{bmatrix} 1.1768 \end{bmatrix} \cos g' + 2 \begin{bmatrix} 1.8016 \end{bmatrix} \sin g'$$

Application to Jupiter.

The value of L is found to be:

Arg-va	$\nu + i'g' + ig$	1		Angress I stat I s		L	
Aig—n)	T• 9 T•9	sin.	cos.	$Arg = \mathcal{H} \mathcal{Y} + i'g' + i$	sin.	cos.	
и г г г г г г г г г г г г г г г г г г г	i' i 0- 1 0- 2 0 0 1- 1 1 0 1- 1 1 0 2 0 2- 1 2- 2 2- 1 3 0 3- 1 3- 2	-0. 0003461 +0. 0004 -0. 0005 -0. 0002 0. 0000 +0. 00201 -0. 00317 +0. 0011 -0. 0004 +0. 0007 -0. 00086 +0. 0002	" +0.0000208 -0.000013 +0.0006866 -0.0003 +0.0001 +0.0001 +0.0001 +0.00161 -0.00244 +0.0008 +0.0002 0.0000 -0.00008 0.0000	$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	+0.0001 -0.00014 -0.0026 +0.000111 -0.0001230 +0.000074 -0.001195 +0.0008 0.000 -0.0001 +0.0002 -0.0003	" +0.0009 -0.00120 -0.0006 0.000 +0.000177 -0.0002187 +0.000049 +0.000201 -0.0002 -0.001 +0.0001 -0.0001 -0.0005 -0.0006	
i	3— I 3— 2	-0.0018- +0.0017	+0. 0029 0. 0036	-I 7-3 0 IO-4	-0.0002 +0.0000010	0. 0001 0. 0000020	

The remainder of the necessary operations being performed, we obtain:

4 // / 1 / 1	$\Delta(n)$	$a\delta z)$	Δν			
Arg=i'g'+ig	sin.	cos.	cos.	sin.		
i' i	11	11	o. 0000052nt	11		
0 1	—0. 000687 <i>2nt</i>	0. 0003428nt	o. 0003436 <i>nt</i>	+0.0001714nt		
0 2	0.0000177 <i>nt</i>	0, 0000020 <i>nt</i>	-0, 0000177 <i>nt</i>	+0.0000020nt		
o— 3	-0.0000006nt	0.0000000nt	0.0000009nt	0,0000000 <i>nt</i>		
I 0	o, 0008 o, 0000	+0.0008 +0.0003	+0.0002 0.0000	+0.0002 -0.0002		
2 I	+0.0545	+0.0406	+0.0073	-0.0059		
2— 2	+0.0023	0, 00II	+o. ooo8	+0.0004		
2 — 3	+0.0005	0.0009	+ 0.0006	+0,0019		
3— 1 3— 2 3— 3	+0.0082 0.0130 +0.0006	+0.0010 +0.0221 +0.0011	—0. 0014 —0. 0051	0.0005 0.0081		

A //-/ 1.5	4	$l(n\delta z)$		Δν
Arg=i'g'+ig	sin.	cos.	cos.	sin.
i' i 4 2 4 3	+0.0015 +0.0038	+0.0092 +0.0011	0. 0000 +0. 0024	 0. 0015 0. 0006
5— 2 5— 3 5— 4	+0. 1207 -0. 0926 -0. 0015	+0. 0903 +0. 0155 +0. 0010	0. 0042 0. 0458 0. 0014	+0.0067 -0.0076 -0.0014
6— 3 6— 4	o. 0009 	+0.0007 +0.0006	-0.0002	-0,0002
7— 3 7— 4	—0. 0005 +0. 0009	+0.0017 +0.0004	+0.0004	-0.0003
10-4	—o. 0067	+0.0082		

Application to Saturn.

The value of L' is:

A 700—140	el tålal Läa	I	7	$Arg = \varkappa \gamma' + i'g' + ig$	I	
Alg—n)	v'+i'g'+ig	sin.	cos.	Aig—n/ Ti y Tiy	sin.	cos.
-I - O - I - O	i' i i o o o o o o o o o o o o o o o o o	"0.0036 +-0.0027970.020 +-0.0115 +-0.002 0.000 +-0.004 +-0.00110.005	"0.0004160.001912 +-0.015020.01010.0040.007 +-0.0080.0027 +-0.003	" i' i	-0.003 +0.017 -0.011 +0.00055 +0.0009 -0.00137 +0.0012451 -0.00029 -0.00006	-0.001 -0.027 +0.021 -0.01219 +0.0098 -0.00130 +0.0022934 -0.00016 +0.00001
—r	o— I 3— I	.+0.005 -0.0243	+0.001 -0.0210	—I 5— 3	+0.008 0.013	+0.002 0.002
1 1 1	2— I I— I 4— I 3— I 2— I	+0.0195 -0.0013 -0.0101 +0.0084 0.0007	+0. 0144 -0. 0014 -0. 0015 +0. 0011 +0. 0003	-I 6-3 -I 5-3 -I 7-3 -I 8-3 -I 8-3	+0. 010 -0. 009 +0. 0021 -0. 001 +0. 0001 -0. 0001	-0.003 +0.003 -0.0022 +0.001 -0.0006 +0.0006
—I	2— 2 I— 2 0— 2	+0.0026 0.093 +0.09	+0, 0008 0, 030 +0, 02	—I 10— 4	+0.00012 -0.000015	-0.00007 +0.000025

The remainder of the necessary operations being performed, we obtain:

	$\Delta(n$	'δz')	Δ	ν'
Arg=i'g'+ig	sin.	cos.	cos.	sin.
i' i	"	"	// +0.0006 +0.000027 <i>n't</i>	"
1 0			+0.0029	+0.0028
	o. 001886n't	0.002755 <i>n't</i>	+0.000942n't	
2 0	o. ooo5	+0.0010	, , , , , , , , , , , , , , , , , , , ,	3,,
	o.00030n't	-0. 000046n't	+0.000030n't	-o. 000046n't
3 0	-0.000001n't	-0.000002n't	+0,000001n't	-0.000002n't
0 I	0. 0004	+0.0012	0,0000	0. 0004
1-1	0. 0027	+0.0015	0.0008	0. 0019
2 I	—о. 1877	—o. 1455	0. 0523	+0.0397
3— 1	-0. 022I	-0.0017	+0.0083	0.0004
I 2	-0.0010	+0.0003	+0.0013	— 0. 0003
2 2	-o. ooo7	+0.0007	0.0003	0.0003
3 2	о, ообт	+0.0020	0.0046	0.0020
4— 2	+0.0178	0, 4020	+0.0094	+o. 1967
5— 2	0. 2931	0. 2678	+0.0075	+o. o108
6 2	+0.0017	0.0003	0. 0009	-0,0002
4 3	+o. 0003	0.0000	0. 0006	0.0000
5— 3	0.0012	+0.0004	0.0012	0. 0004
6— 3	0, 0028	+0,0029	—0. 0016	-0.0017
7— 3	+0.0009	0.0053	+0.0002	+0.0011
9— 4	+0.0019	0.0012	+0.0010	+0.0005
10— 4	+0.0159	o. o187		

In addition to the corrections here stated it must be understood that in all the arguments g is to be replaced by $g + E \Delta \pi$, and g' by $g' + E' \Delta \pi'$.

CHAPTER XXX.

ADDITION OF THE SEVERAL PORTIONS OF THE EXPRESSIONS FOR THE CO-ORDINATES OF JUPITER
AND SATURN AND REDUCTION OF THEM TO THEIR FINAL FORM.

In this final chapter we snall be engaged in putting the expressions we have arrived at in a final form. In the first place, it is determined to change the values of the masses of four of the major planets so that they stand as follows:

Mercury,
$$\frac{i}{7500000}$$
 Earth, $\frac{i}{327000}$ Venus, $\frac{i}{408134}$ Uranus, $\frac{i}{22640}$

The remaining four still retaining the values of their masses, which were stated in Chapter I. Consequently to the terms of the perturbations of Jupiter, which have its own mean anomaly as argument, ought to be added the following corrections:

$$\Delta(n\delta z) = + 0.0001609nt \sin(-g) + 0.0015450nt \cos(-g) + 0.000019nt \sin(-2g) + 0.0000186nt \cos(-2g) + 0.000000nt \sin(-3g) + 0.000004nt \cos(-3g)$$

$$\Delta v = + 0.0020 + 0.000019nt + 0.00007 \cos(-g) + 0.000018in(-g) + 0.0000019nt \cos(-g) + 0.000019nt \cos(-2g) + 0.0000186nt \sin(-2g) + 0.000001nt \cos(-3g) + 0.000007nt \sin(-3g)$$

$$\Delta \left(\frac{u}{\cos i}\right) = - 0.0000051n. + 0.00001414nt \sin(-g) + 0.000007nt \cos(-g) + 0.000001nt \cos(-2g) + 0.0000017nt \cos(-2g) + 0.0000017nt \cos(-2g) + 0.0000017nt \cos(-3g)$$

In addition the small terms dependent on the elongations of Jupiter, severally from Venus and the Earth, ought to be modified to suit the new values of the masses of the latter planets; also the remaining periodic terms due to the action of Uranus ought to be multiplied by the factor $\frac{21000}{22640}$.

For the same reason the terms of the perturbations of Saturn, having its own anomaly as argument, ought to receive the additions

$$\Delta(n'\delta z') = -0.006157n't \sin g' + 0.011276n't \cos g' + 0.0002 \sin 2g' + 0.0001 \cos 2g' - 0.000086n't \sin 2g' + 0.000158n't \cos 2g' - 0.00002n't \sin 3g' + 0.00004n't \cos 3g'$$

$$\Delta v' = +0.0192 + 0.000586n't - 0.0058 \cos g' + 0.005638n't \sin g' + 0.003078n't \cos g' + 0.005638n't \sin g' - 0.0002 \cos 2g' + 0.0001 \sin 2g' + 0.000086n't \cos 2g' + 0.000158n't \sin 2g' + 0.00008n't \cos 3g' + 0.00007n't \sin 3g'$$

$$\Delta\left(\frac{u'}{\cos i'}\right) = +0.0008 + 0.00026n't - 0.000282n't \sin 2g' - 0.000087n't \cos 2g' - 0.000087n't \cos 2g' - 0.000087n't \cos 2g' - 0.00003n't \sin 2g' - 0.00004n't \cos 3g' - 0.00004n't \cos 3g' - 0.00004n't \cos 3g' - 0.00004n't \cos 3g' - 0.000004n't \cos 3g' - 0.000004n't \cos 3g' - 0.000004n't \cos 3g' - 0.00004n't \cos 3g' - 0.00004n't \cos 3g' - 0.00004n't - 0.0004n't - 0.0004n't - 0.0004n't - 0.0004n't - 0.0004n't - 0.00004n't - 0.0004n't - 0.0004n't - 0.0004n't - 0.0004n't - 0.0004$$

In addition the small terms dependent on the elongations of Saturn, severally from Venus and the Earth, ought to be modified to suit the new values of the masses of the latter planets; also the remaining periodic terms due to the action of Uranus ought to be multiplied by the factor $\frac{21000}{22640}$.

Hansen's co-ordinate ν is not that which it is convenient to tabulate. We adopt $\log (1 + \nu)$ in its place. Consequently, neglecting all higher powers of ν than the second, we add to ν the quantity $-\frac{1}{2}\nu^2$. The expressions for this, severally in the cases of Jupiter and Saturn, follow:

Arg=i'g'+ig	$-rac{\imath}{2} u^2$						
	cos.	sin.					
i' i o o	$\frac{1}{1}$ $\frac{1}$	u u u					
0 I	-0.0071 $-0.00007nt$ $-0.0000010n^2t^2$	$-0.0047+.000008nt+.00000005n^2t^3$					
O 2	$+.00000009n^2t^2$	+.00000118n²t²					
o 3		+.0000005 <i>n</i> ² <i>t</i> ²					
1+1	+0.0004+.000002nt	+0.0005+.000002nt					
1 0	+0.0090+.000050nt	+0.0037000029nt					
1— 1	+0.0021+.000005nt	-0.0030000006nt					
I— 2	-0.0007000036nt	+0.0003—.000048nt					
r— 3	—. 000002nt	00000Int					

Arg=i'g'+ig	$-\frac{1}{2}\nu^2$							
	cos.	sin.						
i' i	<i>11</i>	,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,						
2+ I	.000000nt	+. 000002nt						
2 0	+0.0017+.000028nt	+0.0036+.000038nt						
2 I	$-0.0079+.000090nt00000002n^2t^3$	+0.0094+.000237nt+.00000001n ³ t ³						
2 2	+0.0011+.000038nt	+0.0013000020nt						
2 3	+.000228nt	—. 000103nt						
2— 4	+.000012nt	—. 000005 <i>nt</i>						
3 0	+0.0009—.000001 <i>nt</i>	0, 0029, 000008nt						
3— т	$+0.0197+.000016nt+.00000002n^2t^2$	-0.0074000071 nt +.00000001 n^2t^2						
3— 2	+0.0029+.000018nt	+0.0004000006nt						
3— 3	-0.0035000080nt	+0.0060000008 <i>nt</i>						
3 4	—. 000007 <i>nt</i>	000025nt						
4— 1	+0.0006+.000007nt	+0.0004000006nt						
4 2	+0.0004+.000017nt	+0.0047+.000007nt						
4- 3	-0.0023000006nt	-0.003100001 <i>2nt</i>						
4 4	—0. 0095+. 000006nt	-0, 0105 000020nt						
4— 5	—. 000006nt	.000000nt						
5 1	—. 000026nt	+. 000001nt						
5— 2	$+0.0002000116nt+.00000009n^2t^2$	+0.0002-,000142nt00000006n³t°						
5-3	+0.0006+.000001 <i>nt</i>	+0.0019+.000015nt						
5— 4	$+0.0025000130nt00000005n^2t^2$	+0.0095+.000120nt+.00000005n ² t ²						
5 5		+0.0020+.000004 <i>nt</i>						
6— 2	0.0000 .000000 <i>nt</i>	+0.0001000002nt						
6— 3	-0.0001+.000002nt	-0.0003000001 <i>nt</i>						
6 4	+0.0013000002nt	-0.0051 .000000nt						
6 5	-0.0015000001 <i>nt</i>	0.0000—.000002nt						
7-3	+0.0005+.000003nt	-0.0003 .000000nt						
7 4	+o. oo56	-o. ooi i						
7— 5	+0.0195	+0.0105						
8 3	0.0000+.00002 <i>nt</i>	+0.0005+.000001nt						
8— 4	-0.0013	-0.0003						
8 5	_o. oo35	—о. 0060						
8— 6	+0.0010	0. 0020						
9— 4	—o. ooo1	0.0000						
9 5	0.0000	0. 0007						
9— 6	+0.0015	-0.0010						
10— 4	0.0000+.000003nt	+0.0001—.000001 <i>nt</i>						
10 5	0, 0011	+0.0015						
10— 6	 0. 0070	-0.0010						

	$-\frac{1}{2}\nu'^3$								
Arg = t'g' + ig	2	3							
	cos.	sin.							
i' i	" " " " " " " " " " " " " " " " " " " "	,, ,,							
1 O	-0. 2024+. 000068 $n't$ 00004837 n'^9t^2 +0. 0509 001417 $n't$ 00000468 n'^9t^2 - $\frac{15''}{10^{10}}n'^3t^3$	$+0.0844+.002225n't+.00000199n'^2t^2+\frac{12''}{10^{10}}n'^3t^3$							
2 0	$+0.0144000216n't+.00002110n'2t^2-230n'3t^3$	$+0.0157+.000052n't+.00004341n'2t^2+85n'3t^3$							
3 0	$+0.0023000036n't+.00000116n'^2t^2-20n'^3t^3$	-0.0038 $-0.00002n't+0.0000238n'^2t^2$ $0n'^3t^3$							
4 0	$000001n't+$, $00000006n'^{2}t^{2}$	$.000000n't+.00000013n'^2t^2$							
-ı ı	-0. 0039 000104n't	-0.0037+.000068n't							
0— I	0. 0074 002537 $n't$ +. 00000030 n'^2t^2	$-0.0040+.001055n't+.00000065n'2t^2$							
I— I 2— I	$-0.0274+.000878n't+.00000002n'^2t^2$ $+0.0580+.002085n't0000030n'^2t^2$	$+0.0745+.001653n't+.00000054n'^2t^2$ $+0.1051+.001722n't+.00000051n'^2t^2$							
3— 1	$+0.1415+.001139n't+.00000107n'2t^2$	-0.0577 $-0.01260n^{t}$ $+0.0000031n^{t}$ t^{2}							
4— r	—0. 0207—. 000115 $n't$ —. 00000011 n'^2t^2	0. 0065 $000062n't$ $00000024n'^2t^2$							
5 1	o. 0000—. 000007 <i>n't</i>	o. 0000+. 000007n't							
0— 2	-0.0014000029n't	+0.0009+.000037n't							
1 2	-0,0008+,000072n't	+0.0028+.000465n't							
2— 2 3— 2	$+0.0487+.000125n't0000020n'^2t^2$ $+0.0137+.004334n't+.00000205n'^2t^2$	$+0.0195+.000239n't+.00000010n'^2t^2$ $-0.0439003474n't+.00000390n'^2t^2$							
3— 2 4— 2	-0.0373 $-0.00415n't$ $+0.0000031n'^2t^2$	-0.1328 $000207n't$ $00000139n'^2t^2$							
5— 2	$-0.0013004672n't + .00000375n'^{2}t^{2}$	+0.0199002169n't00000624n'2t2							
6 2	$+0.0001+.000289n't00000164n'^2t^2$	$-0.0009+.000643n't+.00000065n'^2t^2$							
7- 2	$+$. 000013 $n't$ —. 00000060 n'^2t^2	$+.000010n't+.00000005n'^2t^2$							
I— 3	.000000n't	+. 000003n't							
2-3	+. 000105n't +0. 0093+. 000067n't	+. 000007n't -0.0135+.000033n't							
3— 3 4— 3	-0.0018000017n't	-0.0094000060n't							
5-3	-0. 1480+. 000040n't	—0. 0109—. 000220 <i>n't</i>							
6— 3	$+0.0247000160n't+.00000008n'^2t^2$	$+0.1088+.000006n't+.00000006n'^2t^2$							
7— 3	$+0.0129+.000051n't+.00000002n'^2t^2$ $-0.0014.00000n't+.00000001n'^2t^2$	$-0.0203+.000028n't+.00000007n'2t^2$ $+0.0005+.000025n't00000005n'9t^2$							
8— 3									
2— 4	+. 000002n't	, 000000n't							
3— 4 4— 4	+, 000010n't 0, 0034+, 000015n't								
5— 4	0.0039—.00002In't	-0.0009+.000001n't							
6 4	-0.0081000043n't	+0.0221000016n't							
7— 4	-0.00550004In't	+0.0100—.000037n't -0.0346+.000337n't							
8— 4	+0. 1315+. 000044n't 0. 0394+. 000061n't	-0.0340+.000337nt -0.0148000122n't							
9— 4 10— 4	$+0.0016+.000047n't00000003n'2t^2$	$+0.0032000047n't00000004n'2t^2$							
11 4	—. 000017 <i>n't</i>	+. 00000In't							
4 5	—. 000010n't	—. 000005n't							
5— 5	000005n't	—. 000007n't							
6— 5	, 00000In't	+. 000005n't							
7— 5	+0.0047—.000003n ^t t +0.0020—.000003n ^t t	+0.0026+.000006n't +0.0034+.000001n't							
8— 5 9— 5	+0.002000003nt +0.000200001nt	+0.0021 .000000n't							
10— 5	+0,0008	-0.0012							
11-5	o. oo17	-0.0014							
12- 5	+0.0002 .000000n't	+0.0005+.000002n't							
7— 6	+.000002n't	+.000001 <i>n't</i>							
8— 6	+.000002n t	+.00002n't +.00002n't							
9 6	.000000 <i>n't</i>	T. 00000211 0							

If we apply to the elements of Jupiter and Saturn, given in Chapter I, the corrections of Supposition III in Chapter XXVIII, we obtain the following system of values:

Epoch 1850, Jan. o.o, Greenwich M. T.

0 / //		0	,	11
L = 159 56 24.98	$\mathbf{L}' =$	14	49	38.09
= 11 54 31.67	$\pi' =$	90	6	41.37
$\theta = 98 \ 56 \ 19.79$	$\theta' =$	112	20	49.05
i = 11842.10	i' =	2	29	40.19
e = 0.04825511	e' =	0.05	6 06	025
n = 109256''.62552	n' = 1	4399	96′′.	21506

In order to tabulate the radius vector of a planet it is necessary to have a clear understanding of the linear unit one wishes to employ. Let us suppose that it is desired that the semi-axis major of the Earth's orbit connected with its sidereal mean motion by the well-known equation should be represented by unity. Then m_0 denoting the Earth's mass and n_0 its mean motion the semi-axis major of Jupiter is given by the equation

$$a = \left[\frac{1 + m}{1 + m_0} \frac{n_0^2}{n^2}\right]^{\frac{1}{3}}$$

and that of Saturn by an equation entirely similar. For m_0 we take the value given at the beginning of this chapter, and we put

$$n_0 = 1295977''.41516$$

It is here understood that n_0 is the constant of the Earth's orbit, which is exactly analogous to the constants n and n', severally belonging to the orbits of Jupiter and Saturn. This gives

$$\log a = 0.7162374088 \qquad \qquad \log a' = 0.9794956385$$

In the expressions for the co-ordinates which follow, the inequalities of the fundamental argument and of the latitude are given the form

$$k_0 \sin (\chi + K_0) + k_1 T \sin (\chi + K_1) + k_2 T^2 \sin (\chi + K_2) + k_3 T^3 \sin (\chi + K_3)$$

and that of common logarithm $\left(\frac{r}{\bar{r}} = r + \nu\right)$ the form

$$k_0 \cos(\chi + K_0) + k_1 T \cos(\chi + K_1) + k_2 T^2 \cos(\chi + K_2) + k_2 T^3 \cos(\chi + K_3)$$

The unit of T is a century of Julian years, and it is counted from 1850.0. K is so taken that k may be positive, except in the absolute terms, where K is supposed to

vanish and k receives its proper sign. The k belonging to the common $\log (1 + \nu)$ are uniformly expressed in units of the seventh decimal.

The values of the constituents of the arguments occurring in the formulae are

$$g = 148$$
 1 53.31 + 109256.62552 t
 $g' = 284$ 42 56.72 + 43996.21506 t
 $g'' = 220$ 10 10.35 + 15425.752 t
 $g''' = 291$ 48 8.61 + 7864.935 t
 $9 - 24 = 84$ 1 + 1997384.73 t
 $5 - 24 = 299$ 52 + 1186720.79 t
 $9 - 5 = 229$ 8 + 2062645.15 t
 $4 - 5 = 84$ 59 + 1251981.21 t

Inequalities of the fundamental argument of Jupiter.

To form the value of $n\delta z$ it is necessary to add together the following expressions:

- I. The first-order terms due to the action of Saturn (pages 103-105).
- II. The first-order terms due to the action of Uranus; as given at page 160 they must be multiplied by the factor $\frac{21000}{22640}$.
- III. The first-order terms due to the action of Neptune (page 191).
- IV. The small terms arising from the action of the four interior planets, given at pages 193-196. Those coming from Venus and Earth must be modified to correspond to the masses adopted at the beginning of this chapter.
- V. The second-order terms arising from the mutual action of Jupiter and Saturn (pages 290-292).
- VI. The third-order terms arising from the mutual action of Jupiter and Saturn (pages 404, 405)
- VII. The second-order terms arising from the joint action of Saturn and Uranus; as given at page 479 they must be multiplied by the factor $\frac{21000}{22640}$.
- VIII. The terms of $\Delta(n\delta z)$, given at pages 528, 529.
 - IX. The terms of $\Delta(n\delta z)$, given at pages 551, 552.

In passing from terms multiplied by nt to those multiplied by T the logarithm of the factor to be employed is 1.7240226, and in deriving the K we remember that $E\Delta\pi = -98''.082$ and $E'\Delta\pi' = -4''.883$.

	n8z									
χ	k_0	K ₀	k_1	K ₁	k_3	K ₂	k ₃	K ₃		
$egin{array}{ccc} g' & g & & & & & & & & & & & & & & & & $	"	0 / "	,, + 0.0019	0 / "	,, +0. 83320	0 /	,, +0. 016208	0 /		
0 I			100. 6962	227 27 58.93	0. 69738	298 22. 3	0. 000358	45 55		
0— 2	0. 236	35 8	o. 796o	224 50.8	0. 02672	284 46	0.000013	274		
o— 3	0.047	137	0. 0108	223 54	0.00073	275 38	0.000002	90		
0— 4	0.002	103	0,0002	0	0,00001	0				
1 + 3	0, 005	147								
1+ 2	0. 128	123 20	0. 0057	21 16						
1+ 1	1. 237	215 13.9	0.0332	116 11						
ı o	11. 156	150 56 7	0. 1755	49 46	0.00070	322 44				
I— I	79. 843	79 12 7	0.0045	244 58		J - ++				
I 2	1. 508	90 37.7	0. 0237	131 4	0,00002	180				
1 3	0. 108	108 27	0.0026	199 51						
1— 4	0.018	212 27								
2+ 2	0.013	205 33	0.0007	123						
2+ 1	0.487	184 19	0.0213	86 39						
2 0	6.813	123 49. 3	0. 1752	13 51.3	0.00044	230 21				
2— I	123.012	1 24 45.6	1. 2671	301 24.3	0.00704	216 56				
2— 2	194. 634	336 53 42.3	0. 0222	354 34	0.00018	39				
2— 3	2. 811	331 31.6	0. 0649	22 42	0. 00005	68				
2— 4	0. 054	305 46	0.0024	10 29						
2— 5	u. 002	300								
3+ 1	0. 062	275 52	0, 0029	185 11						
3 0	3. 685	270 58.7	0. 1418	174 15						
3— 1	14. 038	312 11 30	0, 2316	210 12.5	0.00170	161 23	:			
3— 2	82. 649	127 22 51	1. 1498	30 1.0	0.00609	299 34				
3 3	16. 228	57 42 44	0.0147	150 34	0.00007	279				
3 4	0. 405	38 13	0.0078	100 26						
3 5	0.014	327 36	0, 0004	50				:		
4 0	0, 015	177 16		l						
4 I	o. 684	191 30	0. 0304	84 0						
4— 2	16.838	98 28 1	o . 4607	0 32.9	0. 00313	260 45				
4 3	14. 978	26 2 35	0. 2044	288 17.2	0.00121	197 39				
4 4	3.611	129 27.5	0.0039	36 49						
4 5	0. 152	104 21	0.0024	168 36				!		
4— 6	0. 009	33		ļ		- 1		- 1		
5 0	0.004	45	0. 0048	17 56	0.00007	74	ļ			
5— I	0. 776	1 46. 6	0. 2567	11 47.2	0. 01314	284 55				
5— 2 —81". 97009 <i>t</i> }	1196. 138	67 8 55.03	5. 5814	247 9. I	0. 15562	48 49.7				
5— 3	160. 938	176 27 45.4	4. 7607	80 53.6	0. 05892	349 26. 2				

				$n\delta z$				
χ	k_0	K ₀	k_1	\mathbf{K}_{1}	k_2	\mathbf{K}_2	k_3	К ₃
g'-g	"	0 1 11	"	0 / //	"	0 / //	"	0 / //
5- 4	3. 666	133 33.4	0.0293	72 9	0. 00085	118 10		
5— 5	1. 121	206 52.3	0.0015	134 17	0.00001	315		
5— 6	0.068	178 43	0.0009	245				
5— 7	0.004	120						
6— г	0.004	320						
6— 2	0. 150	29 31	0. 0088	290 27				
6— 3 6— 4	1. 181	150 52.8	0, 0944	289 28	U. 00012	315		
6 5	0.803	74 35·9 179 13	o. 0398 o. 0114	336 28 82 55				
6 6	0. 373	285 43	0.0003	158				
6— 7	0.032	254 31	0, 0004	310				
6— 8	0.002	225	<u> </u>					
7 2	0. 008	213	0.0015	88 4				
7— 3	1. 916	214 9.8	0. 0775	116 10.0	0. 00031	0		
7— 4	2. 897	223 47.6	0. 1111	125 23.8	0. 00046	212 21		
7— 5	0. 294	161 34	0.0093	64 35	1			
7— 6 7— 7	o. 305 o. 138	258 47 2 15	0, 0041	159 35 270				
7— 7 7— 8	0.138	329 46	0,0002	342				
7-9	0.001	301		34-				
8— 2	0.010	340 29	Ì					
8— 3	0. 278	198 I	0, 0132	104 13			1	
8— 4	1.862	13 32.6	0.0878	277 18				
8 5	0. 319	304 25	0.0132	207 56			1	
8— 6	0. 137	234 50	0,0044	139 г				
8— 7	0. 124	336 33	0.0014	238 51				
8— 8	0.054	77 42					l	
8— 9	0. 008	47						
8—10	0.001	16						
9— 3	0.009	170				!		ļ
9 4	0. 528	344 38	0.0281	247 56	1			
9— 5	0. 504	272 23	0. 0251	175 17			1	
9— 6	0. 107	14 51	0. 0035	280 37	1			
9— 7	0.063	312 30	0.0017	218 51	1		1	
9— 8	0. 054	53 34	0.0007	318				
9— 9	0.022	154 15					1	
9—10	0. 004	124			1			
10— 4 —145". 72t	11.024	313 41.0	0. 0876	133 41	0.01338	311 27		
10— 5	3. 578	63 18. 1	0. 2075	325 50. 1	1			
10 6	0.097	16 23	0.0044	289 54			1	
10 7	0. 034	93 32	0,0011	352				
10— 8	0. 030	28 18	0, 0008	285				
10 9	0.025	129 29						
10-10	0.009	230			1			
10—11	0.002	201						

2				nδz	;	· · · · · ·		
χ	k_0	K ₀	k_1	K ₁	k_2	K ₂	k_3	K ₃
g' g 11— 4	,, 0. 005	0 / "	"	0 / //	"	0 / //	"	0 / "
11- 5	0.097	34 14	0.0029	294 49			l	
11- 6	0.079	321 52	0.0029	225 9				
11— 7	0. 040	66 2	0.0010	328				
11— 8	0.012	168 13	0.0001	90				
11 9	0.015	104 11	0.0003	D	1		Ī	
1110	0.012	208 35			Í			
11—11	o. 004	304						
11—12	0.001	276						
12— 5	0.065	35 13	0.0028	266 49				
12 6	0.055	293 31	0. 0030	190 14				
12— 7	0, 023	38 45	0.0004	293			Ī	
12 8	0.017	144 9	0.0004	40				
12 9	v. 004	223	0,0002	198				
12—10	0.007	184						
1211	0.005	284			i			<u>'</u>
12-12	U. 002	12			Į.			
$g^{,\prime}$ g								
1+1	0.010	183						
I O	0. 273	174 41						
1—1	0.910	156 57						
I— 2	0. 006	188						
2 0	0.010	190					1	
2— I	0.519	136 42						
2— 2	0. 464 0. 012	132 49 130 44						
2— 3					1			
3 0	100.0	235						
3— I 3— 2	0. 091 0. 145	132 12 126 54						
3-23	0.034	287 32						
3— 4	0.002	283			1			
4— 1	0.015	128 38						
4-1	0.015	121 9						
4-3	0, 013	282 16						
4-4	0, 004	83			1			
5— I	0. 003	127			1			
5— 2	0.008	115			İ			
5-3	0,003	277						
5— 4	0.002	78						
5 5	0.001	237						
6— т	100,0	117			1			
6— 2	0, 002	109			I			
6 3	0.001	270						
6— 4	0.001	72	}					
7— 1	0.015	116 6						
7— 2	0.004	103						
					•	j .		

	$n\delta z$									
χ	k_0	K ₀	k_1	K ₁	k_2	K ₂	k_3	K ₃		
g' g g'' 6 2 3 6 3 3	,, 8. 749 0. 472	o / // 187 50.0 105 59	0. 2864 0. 0072	64 10 337 27	И	0 / //	"	0 / //		
g''' g I O I— I I— 2	o. 011 o. 286 o. 004	99 21 31 37 35								
2 0 2— I 2— 2 2— 3	0. 002 0. 178 0. 101 0. 002	61 243 29 242 47 242								
3— I 3— 2 3— 3	0. 002 0. 002 0. 006	209 151 273								
\$-24 \$-24	0. 070 0. 121	0								

Inequalities of the logarithm of the radius-vector of Jupiter.

To form the expression for the common logarithm $\left(\frac{r}{\bar{r}} = 1 + \nu\right)$ it is necessary to add the nine portions correspondent to those of $n\delta z$, and, in addition, the terms of $-\frac{1}{2}\nu^2$, given at pages 555, 556. The logarithm of the factor for passing from seconds of arc in ν to units of the seventh decimal in the final form of the co-ordinate is 1.3233592.

χ		Common $\log rac{r}{ar{r}}$						
, A	k ₀	K ₀	k_1	K ₁	k_2	\mathbf{K}_2	k_3	K ₂
g' g 0- 0 0- 1 0- 2 0- 3 0- 4 1+ 3 1+ 2 1+ 1 1 0 1- 1 1- 2 1- 3		323 32 31 43 133 10 111 323 49 308 0 33 51 341 13.9 79 11 23 87 58.9	17. 308 1059. 214 25. 498 1. 155 0. 065 0. 081 0. 451 0. 857 0. 051 0. 289 0. 055	227 27 21.2 227 13.5 229 24 228 49 208 37 294 30 229 1 236 42 130 59 196 40	0. 024 7. 291 0. 366 0. 087 0. 001	297 58.8 285 46 272 26 270	0. 0037 0. 0001	45 ²⁵ 45
I 4	0. 33	206 40						ļ

				Common $\log \frac{r}{\bar{r}}$				_
х	k_0	K₀	k_1	K,	k_2	K_2	k_3	K ₃
$g' g \\ 2+ 2$	0. 31	o / " 18 52	0.009	0 / //		0 /		0 /
2+ I	7. 42	1 54	0. 298	265 2				
2 0	61.05	305 11.4	1.601	193 19.5	0.001	297	1	
2— I	383. 02	356 11 17	2. 917	300 58.5	0.021	217		
2— 2	2303. 37	336 53 56.2	0. 242	352 6	0, 002	135		
2- 3	62. 33	333 10.5	0.874	22 59				į
2— 4	1.94	319 56	0. 041	3 11				
2— 5	0. 10	329			1			
3+ I	1.39	94 40	0.058	355 38	,			
3 0	43. 89	90 51	1.688	353 42. 1				
3— I	56. 45	133 2.4	o. 858	29 I	0.001	333		
3— 2	738.42	126 35 32	10. 215	30 3.6	0.051	298 58		
3— 3	241.37	58 30 46	0. 154	121 7				
3 4	9. 52	44 11	0. 121	98 36				
3- 5	0. 34	356 55	0.009	45				
4 0	0. 23	355 51	0.006	248				
4— I	4. 61	24 58	0. 083	91 34				
4— 2	85. 28	94 3.3	2, 283	358 30.5	0, 009	270		
4- 3	193. 21	27 0.6	2, 652	288 26. 2	0.012	197		
4 4	59. 81	127 50.9	0. 051	358 51				
4 5	3.50	109 14	0.040	168 36				
4 6	0, 20	52 55						
5 0	0. 12	215	0. 152	197 54				
5— I	8. 14	180 47	2. 691	192 9.0	0.003	158	ĺ	
5— 2	229. 34	237 53.6	9. 058	143 57.1	0. 162	46 23	1	
5- 3	1679. 20	176 23 44	49. 701	80 52.5	0. 525	343 42	1	
5- 4	65. 06	141 13.3	0. 931	73 6	0.011	326		
5- 5	20. 58	204 48	0. 042	243 34				}
5— 6	1.56	184 1	0.017	241	ŀ			
5 7	0.11	129 51	0. 003	207	l			
6— I 6— 2	0. 05	137	0.040	102.57	l			
6- 3	0. 92 8. 78	203 41 145 29	u. 040 u. 365	102 57 46 48				
6 4	20.79	76 42	0. 565	337 5				
6 5	13.52	180 38	0. 192	80 47				
6 6	6. 92	283 56	0.008	117				
6 7	0.71	260 4	0.006	307			1	
6 8	0. 06	236						
7— 2	0. 18	7 25	0.019	283	1		i	
7-3	5.50	214 14	0. 216	118 29				
7— 4 7— 5	34. 30 5. 17	223 11.6 167 55	1. 313 0. 159	125 13 68 47			l	
7- 6	5· 43	259 28	0. 139	158 59			1	
7-7	2. 68	0 22	0, 004	147			l	}
7— 8	0. 34	335 14	0.003	27	l			}
7 — 9	0.03	312						
<u> </u>				1	<u> </u>		<u> </u>	1

χ		Common	$\log rac{r}{ar{r}}$				Commo	n $\log rac{r}{ ilde{r}}$	
	k _o	K ₀	k_1	K1	X	k_0	K_0	k_1	K ₁
g' g 8— 3	1.09	o , 13 26	0, 024	o , 259	g'' g I— 2	0. 13	0 /		0 /
8— 4	16.42	12 48	0. 775	276 18				İ	
8— 5	4. 89	304 I	0. 193	208 46	2 0	0.06	114		
8— 6	2.42	239 46	0.073	142 35	2— 1	4.55	136 22		
8— 7	2. 31	337 34	0. 029	232 53	2— 2	6.70	132 49		
8— 8	1.08	75 50	0.003	243	2-3	0. 27	130		
8— 9	0.18	50 5			2— 4	0.01	132		
9- 3	0.08	359	0.003	117	3 1	0.71	131 32		
9 4	2.61	340 31	0, 109	240 8	3— 2	1.96	127 7		
9 5	6. 53	272 59	0. 312	175 24	3— 3	0. 56	287		
9— 6	1.75	10 57	0, 066	275 I	3— 4	0.04	285		
9- 7	1. 18	316 51	0. 033	211		0.00	705		
9 8	1.04	54 49	0.016	315	4— I	0.09	125		
9— 9	0.45	151 37			4-2	0.44	122 282		•
9—10	0. 09	125			4-3	0. 21	83		
10 4	3.47	123 36	0. 190	31 11	4 4	0.00	\ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \		
10 5	37. 04	63 11.2	2. 298	325 46	5 2	0.09	116		
10— 6	1.81	22 44	0. 082	2 96 1	5 3	0. 05	277		
10-7	o. 68	88 14	0. 028	356	5— 4	0, 04	80		
. ro 8	0.57	33 57	0. 015	287	5— 5	0.01	239		
10— 9	0.49	131 13	0.007	31	6 2	0.03	110		
10—10	0. 19	226 10			6-3	0,01	270		
1011	0, 04	203			6-4	0.01	75		
11- 5	0.65	31 58	0. 017	290	7 2	0. 04	103		
11 6	1.10	322 57	0. 045	220	-		5		
11 7	0.70	67 0	0. 031	330	g' g g'' 6 2 3	1.08	175 11		
11— 8	0. 25	162 23	0.011	79	6-3-3	4. 97	105 59	0.076	337 27
11— 9	0. 29	112 53	0.009	7		. ,,	3 37		337 -7
11—10	0, 23	208 41			g''' g	0.06	22		
11-11	0.08	2 99 36			1— 1	2.83	31 37		
12— 6	0.49	296 9	0.037	189	I— 2	0.07	34		
12— 7	0.39	39 39	0.009	299	2 0	0.04	242		
12— 8	0, 26	145 5	0.004	237	2— 1	1.75	243 22		
12— 9	0.09	236 55	0.005	346	2- 2	1.52	242 44		
12—10	0.15	186 6	0.003	90	2-3	0.06	242		
12—11	0.11	284							
12—12	0.04	10			3— 1	0.02	207		
g'' g					3- 2	0.03	161		
1+ 1	0. 12	3	ļ		3-3	0. 10	274		
10	0, 24	8		İ	& .—5t	1.48	0		
I I	8. 46	156 57			t−24	2. 55	0		

Periodic inequalities of the latitude of Jupiter.

We have only to change the expression given (pages 526, 527) to the form here adopted and to take account of the corrections to the angles K arising from $E\Delta\pi$ and $E'\Delta\pi'$.

х	Δβ					Δβ			
	k_0	K ₀	k_1	K ₁	χ	k_0	Ko	$k_{\rm l}$	K ₁
g' g ○ ○	,, +0.037	0 /	"	0 /	g' g 5— 4	,, o. 187	o , 161 37	,, o, ooog	o / 238
0— 2	0. 015	66			5 5	0, 008	125	0.0004	104
o— 3	0.001	82			5— 6	0.003	136		
I+ 2	0.005	3 5 3		,	6— г	0.001	74		
1+1	0. 104	8 51	0.0005	158	6— 2	0.007	16		
Ιυ	0.536	325 28	0,0070	54 16	6— 3	0.037	150		
1 1	0. 126	208 1	0.0027	188 27	6 4	0.037	74		
I— 2	0. 265	193 10	0.0043	103 27	6 5	0.012	165		
I 3	0.012	204	0. 0004	90	6— 6	0, 003	121		
2+ I	0. 018	283	0.0004	14	6 7	0.001	216		
2 0	0. 342	265 52	0.0021	313			İ		
2— I	0.627	43 9	0, 0081	137 30	7— 2	0.004	337		
2— 2	O. 22I	114 42	0.0059	82 11	7— 3	0. 005	144		
2- 3	0. 056	267	0.0004	57	7 4	0, 053	44		
2— 4	0.003	282	0,0002	О	7— 5	0.011	135		
3+ 1	0.003	33	0.0001	225	7— 6	0.004	245		
3 0	0.056	49	0,0002	153	7-7	0.002	198		
3— r	u. 165	356 6	0, 0006	38	7-8	0,001	292		
3— 2	1.013	122 15	0.0120	212 25	8— 3	0.001	48		
3-3	0.057	163 7	0.0006	218	8 4	0.009	201	i	
3-4	0.019	351	0.0002	153	8 5	0.008	127		
3- 5	0.001	355			8 6	0.004	222		
4 0	0.006	22			8 7	0.001	318		
4— 1	0.047	329 38			8 8	0.001	90		
4— 2	0. 144	99 51	0.0007	188	9— 5	0. 004	89		
4- 3	0. 247	22 5	0.0037	109	9 6	0.003	196		
4— 4	0.021	342	0.0002	90	9- 7	0, 002	298	<u> </u>	
4- 5	0,009	60	0.0001	135	10 4	0.003	66		
5 0	0.009	111	0.0001	315	10 5	0.073	60 20		
5— 1	0. 184	111 34	0. 0036	8	10— 6	0.003	106		
5 2	0. 194	359 38	0.0006	288	10 7	0.001	281		
5— 3	3. 548	174 54.5	0. 0077	327 12	10 8	0.001	23		

We derive f from $nz = g + n\delta z$ by the formula

$$f = nz + 19900.870 \sin nz + 599.861 \sin 2nz + 25.072 \sin 3nz$$

+ 1.198 sin 4nz + 0.062 sin 5nz + 0.003 sin 6nz

Then

com.
$$\log \bar{r} = 0.71522495 - \text{com.} \log (1 + e \cos f)$$

In addition $l = f + \pi$, and we derive R from

$$R = + 27''.029 \sin(2l + 342^{\circ} 7' 20'') + 0''.002 \sin(4l + 324^{\circ})$$

The heliocentric longitude of Jupiter, referred to the mean equinox of date, is

$$\lambda = f + R + \pi + 50''.264708t$$

In order to get the equation which determines $\sin \beta_0$, we note that the correction of $\frac{u}{\cos i}$ (page 554), on account of changes in the values of the disturbing masses, requires that the A and B of page 525 should receive severally the corrections $-o''.oo_75T$ and $+o''.oo_37T$, so that the equation for $\cos i \sin b$ now becomes

$$\cos i \sin b = \begin{bmatrix} -13.0524T - 0.06615T^2 + 0.000324T^3 \end{bmatrix} \sin l + \begin{bmatrix} 9.4311T - 0.08661T^2 - 0.000240T^3 \end{bmatrix} \cos l$$

If we add this to the expression for the portion of $\sin \beta_0$, which arises from the motion of the ecliptic (page 526), and also take account of the correction $-\frac{d (\sin \beta_0)}{dz} \Delta(\delta z)$, given at page 530, we obtain

$$\sin \beta_0 = \left[\sin i_0 \cos \theta_0 + 33.7123 \text{T} - 0.14784 \text{T}^2 - 0.000107 \text{T}^3 \right] \sin l$$

$$+ \left[-\sin i_0 \sin \theta_0 + 14.7021 \text{T} + 0.11242 \text{T}^2 - 0.000659 \text{T}^3 \right] \cos l$$

$$+ \left[-0.00048 \text{T} + 0.00002 \text{T}^2 \right] \sin 3l$$

$$+ \left[-0.0005 \text{T} - 0.00003 \text{T}^2 \right] \cos 3l$$

Inequalities of the fundamental argument of Saturn.

To form the value of $n'\delta z'$ it is necessary to add together the following expressions:

- I. The first-order terms due to the action of Jupiter (pages 106-108).
- II. The first-order terms due to the action of Uranus; as given at pages 138, 139, they must be multiplied by the factor $\frac{21000}{22640}$.
- III. The first-order terms due to the action of Neptune (page 179).
- IV. The small terms arising from the action of the four interior planets, given at pages 196-198. Those coming from Venus and the earth must be modified to correspond to the masses adopted at the beginning of this chapter.
 - V. The second-order terms arising from the mutual action of Jupiter and Saturn (pages 335-337).

- VI. The third-order terms arising from the mutual action of Jupiter and Saturn (pages 450-452).
- VII. The second-order terms due to the action of Uranus, and given at pages 474, 475; they must be multiplied by the factor $\frac{21000}{22640}$.
- VIII. The second-order terms due to the combined action of Jupiter and Uranus. As given at pages 485, 486 they need to be multiplied by $\frac{21000}{22640}$.
 - IX. The terms of $\Delta(n'\delta z')$ given at pages 534, 535.
 - X. The terms of $\Delta(n'\delta z')$ given at page 553.

In adding these several portions we pass from terms factored by n't to those factored by T by multiplying by the factor whose logarithm is 1.3289902; and, in deriving the K, we take account of the corrections dependent on the quantities $E\Delta\pi$ and $E'\Delta\pi'$.

		•		$n'\delta z'$				
χ	k_0	\mathbf{K}_{o}	k_1	\mathbf{K}_1	k_2	K_2	. k ₃	K ₃
g' g	11	0 / //		0 / "	" +1.79397	0 /	// 0.028256	0 /
1 0			268.8347	237 59 29.70	1.72526	I42 22.2	0.001825	349 12
2 0	2.612	121 24.3	5.4941	237 21 17	0. 10462	119 22.0	0, 001261	26 28
3 0	0.648	91 39	0. 1945	243 35.3	0.00676	113 0	0, 000064	4
4 0	0. 026	4	0. 0113	239 34	0, 00044	115 45		
5 0	0.003	214	0. 0005	239				
-4- I	0.006	21	0.0001	59				
-3- ı	0.006	76	0, 0001	202				
2 I	0. 195	165 51	0. 0078	264 34				
-ı ı	0. 362	141 48	0.0177	228 48	0.00010	294		
0— I	12. 089	86 45 53	0. 1460	209 10	0.00072	310 12		
1-1	7. 196	189 35 2	o. 2961	303 39.0	0.00123	293 56		
2— I	421. 948	181 25 43.70	4. 1702	122 26 58	0.02192	38 34		
3— I	33. 511	121 13 45.6	0. 8283	31 8.0	0.01086	350 52	i	
4— 1	0. 101	90 31	0. 0323	16 39	0.00100	306 15		
5- I	0.043	159 30	0, 0034	29 24	0.00008	315	· '	
6— г	0.003	124	0.0001	135			l	
7— I	0.003	257						
-2- 2	0, 004	141	0.0003	241	ŀ		i	
—I— 2	0.076	244 22	0.0031	342				
0— 2	0. 164	114 12	0, 0020	276	0,00003	270	1	
1 2	2, 764	250 7.6	0.0385	289 55	0, 00004	122		
2 2	32. 025	156 58 9	0. 0156	7 59	0.00017	235	1	
3— 2	26. 138	135 33 5	0. 9096	42 1.5	0.01219	301 7		
4— 2	683. 664	277 23 44 39	16. 5281	179 34 55	0. 15242	84 31.9		
5— 2 —82".00170#}	2907.855	247 6 43. 27	13. 9914	67 6 36	o. 29 863	221 43.0		
6 2	1.719	255 17.3	2. 0642	125 59.7	0.08871	27 56.8		
7— 2	0. 034	323 7	0. 0809	125 33	0. 00340	15 41		
8— 2	0, 006	339	0.0041	124 44				

24	<u>-</u>			$n'\delta z'$. ••			
χ	k_0	\mathbf{K}_0	k_1	K 1	k_2	\mathbb{K}_2	k_3	K ₃
$g' g \\ -\mathbf{I} - 3$	0. 003	o / // 208	0, 0004	o ' '' 289	"	0 /	t/	0 /
o— 3	0, 029	335	0.0010	62				
1-3	0. 139	269 30	0.0015	348			}	
2 3	0. 190	142 54	0.0019	345	0,00002	ō		
3— 3	6. 513	234 22.9	0,0022	357	0.00008	246		
4-3	4. 600	203 15.5	o. o66o	107 21	0.00033	11		
5— 3	3. 250	174 37.3	0, 0903	77 49	0.00112	340 41		
6— 3	3⋅339	157 20.7	0. 1382	58 30	0. 00359	314 36		
7-3	6. 247	31 24.2	0. 2540	289 53.7	0.00179	116 10		
8— 3	0. 654	18 10	0.0451	303 37	0.00034	106		
9— 3	0. 057	110 32	0.0002	130				
10-3	0.002	59						
0— 4	0,001	291						
1-4	0.011	22	0, 0006	135				
2 4	0, 021	25	0.0005	93				
3— 4	0. 122	205 21	0,0006	356				
4-4	1.910	312 8.4	0.0004	62	0, 00004	109		
5— 4	1. 290	281 50.3	0. 0194	185 6	0,00011	115	1	
6 4	0.692	249 33	0. 0201	152 59	0.00017	75		
7— 4	0.375	41 51	0, 0134	300 15	0.00016	30		
8 4	1. 486	14 35.8	0.0774	277 44	0.00031	203		
9 4	8. 824	163 42 22	0. 5281	67 33.6	0, 01228	331 39		
10— 4 —148".145 <i>t</i> }	26. 795	133 37 11	0. 2274	313 37. 1	0, 05217	122 44		
11-4	0.002	197	0, 0199	13 57	0, 00040	275		
I— 5	0.001	0	ì		ŀ			
2- 5	0. 006	115	0.0002	219	1			
3- 5	0, 010	106	0, 0002	194				
4— 5	0, 069	280 55	0. 0003	353	1		İ	
5— 5	0.661	29 42	0,0003	132				
6— 5	0.479	0 7	0.0073	263 43	1			
7— 5	0. 219	332 12	0,0062	237 19	1			
8— 5	0. 120	121 33	0. 0054	22 6				1
9— 5	0. 145	90 5	0. 0068	355 15			Ī	
10 5	0. 129	59 45	0.0070	326 14				
11 5	0.211	39 34	0, 0166	300 19			1	
12- 5	0. 241	213 4	0.0181	108 0				
2 6	0.001	73					1	
3— 6	0.003	194	0.0001	333				
4— 6	0, 006	200	0.0002	286				
5— 6	0. 038	356 15	0.0003	86				
6 — 6	0. 251	106 44	0, 0003		1			
7— 6	0, 200	78 29	0. 0030	346				
8— 6	0.092	50 55	0, 0024	312	Ī			
9— 6	0. 047	199 40	0.0019	105				1
<u> </u>			<u> </u>	<u> </u>	•		•	

		n'	δ <i>z'</i>				n' č	\tilde{z}'	
x	k_0	K ₀	k_1	K ₁	X	k_0	K ₀	k_1	K ₁
g' g 10— 6	,, o. 052	o / 169 12	0,0012	o ′ 65	g'' g' 3+ 1	0.001	305	"	0 /
11-6	0. 026	135 9	0.0007	39	3 0	0. 060	306 36	0. 0189	200 8
12 6	0.013	103 13	0.0004	24	3— 1	28. 520	321 46 31	0. 3917	182 56.8
5— 7	0.003	298	0.0002	343	3- 2	23. 356	119 19 47	0. 1437	307 48
6- 7	0.021	72 38	0.0003	155	3— 3	1. 372	66 35	0.0192	246 2
7-7	0. 099	183 15	•••••	-33	3- 4	0. 044	50 6	0.0017	202 38
8 7	0. 086	156 23	0.0013	60	3— 5	0, 002	45		
9 7	0. 045	130 9	0.0012	34	4 0	0.001	284		
10 7	0.017	275 8	0.0011	177	4 1	0.054	288 22	0.0003	123
11-7	0. 023	242 24	0.0011	153	4-2	0.912	83 39	0.0128	267 4
12-7	0.010	219	0.0005	114	4-3	0. 703	18 8	0.0052	203 20
6 8	0.002	-			4-4	0. 257	129 39	0,0009	148
7— 8	0.002	25 152			4 5	0.014	111	0.0004	256
8 8	0.011	260 19	0.0001	125	4— 6	0.001	106		
9— 8	0.040	233 52	0.0005	135	5— I	0.003	242		
10— 8	0.023	205 38	0.0005	109	5 2	0. 297	48 8	0. 0064	231 28
11-8	0, 007	352	0.0005	256	5— 3	0. 429	341 6	0.0060	164 40
12— 8	0.011	325	0,0005	225	5— 4	0, 140	92 57	0.0005	270
					5-5	0.072	207 39	0.0002	207
8— 9	0,006	227			5 6	0.006	187	0.0001	315
9 9	0.017	336							
10— 9	0.019	313	0.0001	217	6 2	0. 119	4 38	0.0032	191 48
11-9	0.011	286	0.0002	195	6 3	0. 244	124 25	0.0050	309 0
12 9	0.002	57	0,0001	346	6— 4	0. 055	61 29	0.0009	245
9-10	0. 003	302			6— 5 6— 6	0. 043	172 12	0.0002	0
10—10	0.007	50			6— 7	0.023	284 39 263		
11-10	0.009	29			0- /	0.002			
12—10	0.006	2			7-3	0. 016	89 21	0.0005	270
10—11	0.001	20			7— 4	0.019	22 15	0.0004	207
11-11	0.003	125			7— 5	0.015	135 29	0.0001	315
12—11	0. 004	106			7— 6	0.016	250 29		
11—12	0,001	97			7-7	0. 008	I		
12—12	0, 002	195			7— 8	0.001	340		
					8— 3	0.007	53		
$g^{\prime\prime} g^{\prime}$	0. 021	179 15	0, 0011	20	8— 4	0.011	347		
1 0	0. 926	145 45	0.0111	322 51	8— 5	0.005	98		
1— I	8. 036	79 2.1	0.0020	280 47	8— 6	0.006	214		
I 2	0. 153	99 26	0. 0068	201 39	8 7	0. 006	328		
1-3	0.004	97	0.0003	213	8 8	0.003	77		
2+ 1	0, 002	153	1000.0	270	9— 4	0. 003	131		
2 0	0. 113	139 36	0.0044	246 39	9— 5	0.001	73		
2— I	7.682	354 17. 1	0. 0979	216 34	9— 6	0.002	177		
2- 2	12. 380	336 43.3	0.0054	113 4	9— 7	0.002	290		
2 — 3	0. 235	330 22	0.0110	98 45	9— 8	0.002	45		
2— 4	0.007	330	0, 0006	90	9— 9	0.001	153		

		n'é	δz'				n'	Sz'	
X	k_0	K ₀	k_1	K1	χ	k_0	K ₀	k_1	K1
g" g' 10-7 10-8 10-9 g"' g' 1+1 1 0 1-1 1-2 1-3 2 0 2-1 2-2 2-3	0. 001 0. 001 0. 002 0. 101 1. 717 0. 027 0. 001 0. 012 0. 904 1. 052 0. 026	256 9 124 270 287 29 312 59 309 1 303 269 30 84 44 86 17 87 22	// //	0 /	$g''' g' \\ 4-3 \\ 4-4 \\ 4-5 \\ 5-2 \\ 5-3 \\ 5-4 \\ 5-5 \\ 6-6 \\ g' g g'' \\ 2-1+1 \\ 3-1-1 \\ 3-1-2 \\$	0.010 0.015 0.001 0.001 0.001 0.002 0.003 0.001 0.022 0.168 0.207	67 262 102 308 261 270 288 21 79 43	// //	0 /
2— 4 3— I 3— 2 3— 3 3— 4 4— I 4— 2	0.001 0.031 0.103 0.093 0.004 0.001 0.009	90 166 12 197 18 39 58 42 284 308			4-2+3 4-I-4 5-2-3 6-2-3 7-2-6 γ-5 5-5	o. 063 o. 106 1. 884 28. 917 o. 153 o. 038 o. 066	213 2 37 11 208 34 6 56.0 353 26	o. 0294 o. 7830	80 14 242 4

Inequalities of the logarithm of the radius-vector of Saturn.

To form the expression for $\log \frac{r'}{\bar{r}'}$ we combine together the ten portions of ν corresponding to the ten portions of $n'\delta z'$ and besides apply to the sum the value of $-\frac{1}{2}\nu'^2$ (page 557).

7		$\text{Common log } \frac{r'}{\bar{r'}}$										
χ	k_0	K ₀	k_1	K1	k_2	K_2	k_3	K ₃				
<i>g' g</i> ○ ○	+1825.0	0 / //	+ 41.95	0 / "	+o. 674	0 /	+0,0003	0 /				
1 0	187. 3	295 24.7	2832.89	57 59 18.5	18. 084	322 22.6	0.0197	167 40				
2 0	49. 9	293 9	78. 60	58 38.5	1.838	303 11	0. 0049	205 31				
3 0	14. 2	271 43	2. 12	77 46	0. 127	302 49	0. 0004	166				
4 0	0, 6	311	0.04	82	0.008	299						
3 т	0, 2	111			l .							
2 I	4.6	165	0.22	263 45								
—ı— ı	10.4	140 34	0. 36	235 18	0. 001	180						
о— 1	82.0	110 49	1.15	219 39	0.020	299						
1— I	3780.8	79 45 10	3. 19	304 47	0, 010	25						

χ				Common log	$s rac{r'}{\overline{r'}}$			
Λ 	k_0	K ₀	k_1	K 1	k_2	K ₂	k ₃	K ₃
g′ g 2— I	2442. I	0 / // 176 2 37	21.60	0 / "	0. 204	o / 36 17		0 /
3— І	241, 2	305 54.4	6. 21	207 37	0.058	188 31		
4 I	35. I	342 36	0, 45	126 52	0.006	134		
5 1	0. 7	309	0.08	214		-54		
6— 1	о. 1	294						
-2- 2	0. 1	158						
—I— 2	1.8	241 2	0.09	341				
0— 2	3⋅7	210 18	0. 11	316				
I— 2	55. 2	98 52	0. 26	257 18	0.002	189		
2 2	643. 5	156 34.5	0.32	14 5	0.003	D		
3— 2	420. 9	141 57.8	11. 31	46 59	0. 051	339 5		
4— 2	7001.9	277 15 19	170.48	179 38.4	2. 252	85 53		
5— 2 } 88".928t	1141.0	62 49 32	4. 36	242 49	0. 077	6 8		
6 2	18. 3	77 17	19.45	306 10	0. 055	209 17		
7— 2	0.6	114	1.06	306 55	0.006	185		
8— 2			0.06	307				
—ı— 3	0. I	224	0.01	303				1
o 3	o. 8	319	0.04	58				
I— 3	Ι. υ	46	0, 04	61				
2- 3	5⋅3	178 39	0.05	342				
3— 3	147. 1	233 56.0	0.04	32	0.001	O		
4- 3	102. 0	206 23.8	1. 36	107 2	0,010	11 30		
5— 3	59.7	177 52	1.80	78 59	0, 023	343 18		
6— 3	17.3	178 3	2.86	51 41	0.048	314 0		
7— 3	34. 6	32 39	2. 39	340 42	0.004	254		
8— 3	4.9	210 27	0. 39	153 48	0.005	61		
9 3	0.7	275	0. 02	139	1			
o — 4	0. 1	298			1			
1 4	0.4	43	0, 02	134	1			
2-4	0.5	17	0,02	115	1			
3- 4	2.8	229 44	0.01	8				
4— 4	44. 5	311 30	0.01	122				
5— 4	31.5	285 3	0.42	184 23	0,003	98		
6— 4	14.9	259 21	0. 35	157 31	U, 004	67		
7— 4	8. 1	37 4	0. 52	302 47	0.003	37		
8— 4	21.5	15 52	0.91 8 55	284 18	0.005	204		1
9 4	93. 1	163 39	8. 55 1. 81	67 13	0, 116	331 16		
10— 4	11.0 0.2	306 25 102	0.02	215 3	0. 033	118 28		
2— 5	0. 2	113	0. 01	214				
3-5	0. 2	106	10.0	199	1			
4-5	1.5	296 38	0.01	0	1			
7)		J. J.						

7-5 5.5 337 30 0.14 240 1-1 39.0 79 3 0.01 8-5 2.7 116 7 0.17 24 1-2 2.5 95 57 0.06 9-5 3.7 118 23 0.21 354 1-3 0.1 95 10-5 2.7 63 43 0.18 325 2 0 1.0 328 4 0.06 11-5 3.6 36 26 0.26 300 2-1 35.5 350 35 0.28 12-5 0.7 263 0.07 113 2-2 154.1 336 43.3 0.05 3-6 0.1 191 2-3 5.3 332 13 0.10 4-6 0.1 191 2-4 0.2 332 0.01 5-6 0.8 8 0.01 69 3 0.6 126 0.18 6-6 5.9 105 37 0.07 341 3-2 237.4 119 5.6 1.43 <th></th>	
5 - 5 15.6 28 45 0.01 184 1 + 1 0.3 356 0.01 6 - 5 11.9 3 8 0.16 263 1 0 3.2 345 3 0.08 7 - 5 5.5 337 30 0.14 240 1 - 1 59.0 79 3 0.01 8 - 5 2.7 116 7 0.17 24 1 - 2 2.5 95 57 0.06 9 - 5 3.7 118 23 0.21 354 1 - 3 0.1 95 10 - 5 2.7 63 43 0.18 325 2 0 1.0 328 4 0.06 11 - 5 3.6 36 26 0.26 300 2 - 1 35.5 350 35 0.28 12 - 5 0.7 263 0.07 113 2 - 2 154.1 336 43.3 0.05 3 - 6 0.1 191 0.2 3 0 0.6 126.0 0.18 3 - 6 0.1 191 0.0	K ₁
6-5 II.9 3 8 0.16 263 I 0 3.2 345 3 0.08 7-5 5.5 337 30 0.14 240 I-I 1 59.0 79 3 0.01 8-5 2.7 1116 7 0.17 24 I-2 2.5 95 57 0.06 9-5 3.7 118 23 0.21 354 I-3 0.1 95 10-5 2.7 63 43 0.18 325 2 0 1.0 328 4 0.06 11-5 3.6 36 26 0.26 300 2-I 35.5 350 35 0.28 11-5 0.7 263 0.07 113 2-2 154.1 336 43.3 0.05 3-6 0.1 191 0.07 341 3-2 154.1 336 43.3 0.05 3-6 0.1 191	0 /
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8-5 2.7 116 7 0.17 24 1-2 2.5 95 57 0.06 9-5 3.7 118 23 0.21 354 1-3 0.1 95 10-5 2.7 63 43 0.18 325 2 0 1.0 328 4 0.06 11-5 3.6 36 26 0.26 300 2-1 35.5 350 35 0.28 12-5 0.7 263 0.07 113 2-2 154.1 336 43.3 0.05 3-6 0.1 191 2-3 5.3 332 13 0.10 3-6 0.1 191 2-4 0.2 332 0.01 5-6 0.8 8 0.01 69 3 0 0.6 126 0.18 6-6 5.9 105 37 37 3-1 26.4 137 55 0.16 7-6 5.0 80 27 0.07 341 3-2 2.1 69 58 0.17 9-6 1.0 191 57 0.06 96 3-4 1.1 57 13 0.02 </th <th>140</th>	140
9-5 3.7 118 23 0.21 354 1-3 0.1 95 10-5 2.7 63 43 0.18 325 2 0 1.0 328 4 0.06 11-5 3.6 36 26 0.26 300 2-1 35.5 350 35 0.28 12-5 0.7 263 0.07 113 2-2 154.1 336 43.3 0.05 3-6 0.1 191 2-3 5.3 332 13 0.10 5-6 0.8 8 0.01 69 3 0 0.6 126 0.18 6-6 5.9 105 37 0.07 341 3-2 237.4 119 5.6 0.18 8-6 5.0 80 27 0.07 341 3-2 237.4 119 5.6 1.43 8-6 2.4 56 33 0.06 317 3-3 22.1 69 58 0.17 9-6 1.0 191 57 0.06 74 3-5	277 202
10 - 5 2.7 63 43 0.18 325 2 0 1.0 328 4 0.06 11 - 5 3.6 36 26 0.26 300 2-1 35.5 350 35 0.28 12 - 5 0.7 263 0.07 113 2-2 154.1 336 43.3 0.05 3 - 6 0.1 191 2-3 5.3 332 13 0.10 4 - 6 0.1 191 2-3 5.3 332 13 0.10 5 - 6 0.8 8 0.01 69 3 0 0.6 126 0.18 6 - 6 5.9 105 37 3 0.07 341 3-2 237.4 119 5.6 0.18 8 - 6 5.9 105 37 0.07 341 3-2 237.4 119 5.6 1.43 8 - 6 2.4 56 33 0.06 317 3-3 22.1 69 58 0.17 9 - 6 1.0 191 57 0.06 96 3-4	202
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3 - 6	217 25
3-0 0.1 191 2-4 0.2 332 0.01 5-6 0.8 8 0.01 69 3 0 0.6 126 0.18 6-6 5.9 105 37 0.07 341 3-2 237.4 119 5.6 1.43 8-6 5.0 80 27 0.07 341 3-2 237.4 119 5.6 1.43 8-6 2.4 56 33 0.06 317 3-3 22.1 69 58 0.17 9-6 1.0 191 57 0.06 96 3-4 1.1 57 13 0.02 10-6 1.3 171 26 0.06 74 3-5 0.1 52 11-6 0.7 144 0.03 47 4-1 0.4 104 12-6 0.1 120 0.02 15 4-2 6.7 80 4 0.09 5-7 0.1 279 4-3 9.7 1951 0.07 4-4 4-4 4-4 4-4 4-4 4-4 4-4 128 12 0.01	106
4-0 0.1 191 5-6 0.8 8 0.01 69 3 0 0.6 126 0.18 6-6 5.9 105 37 3-1 26.4 137 55 0.16 7-6 5.0 80 27 0.07 341 3-2 237.4 119 5.6 1.43 8-6 2.4 56 33 0.06 317 3-3 22.1 69 58 0.17 9-6 1.0 191 57 0.06 96 3-4 1.1 57 13 0.02 10-6 1.3 171 26 0.06 74 3-5 0.1 52 11-6 0.7 144 0.03 47 4-1 0.4 104 12-6 0.1 120 0.02 15 4-2 6.7 80 4 0.09 5-7 0.1 279 4-3 9.7 19 51 0.07 6-7 0.4 83 4-4 4.4 128 12 0.01 7-7 2.4 182 5 0.03 59 5-2 1.1 38 31 0.02 8-7 2.2 158 51 0.03 59 5-2 1.1 38 31 0.02 9-7 1.1 135 7 0.03 35 5-3 5.2 342 27 0.07 10-7 0.4 265 0.02 171 5-4 2.2 93 59 0.01 11-7 0.6 247 0.03 150 5-5 1.3 206 15 12-7 0.3 222 0.02 122 5-6 0.1 190 7-8 0.2 158 88 1.0 258 9-8 1.0 236 0.02 140 6-4 0.8 65 50 0.02	98
6—6 5.9 105 37	90
7-6 5.0 80 27 0.07 341 3-2 237.4 119 5.6 1.43 8-6 2.4 56 33 0.06 317 3-3 22.1 69 58 0.17 9-6 1.0 191 57 0.06 96 3-4 1.1 57 13 0.02 10-6 1.3 171 26 0.06 74 3-5 0.1 52 11-6 0.7 144 0.03 47 4-1 0.4 104 12-6 0.1 120 0.02 15 4-2 6.7 80 4 0.09 5-7 0.1 279 4-3 9.7 19 51 0.07 6-7 0.4 83 4-4 4.4 128 12 0.01 7-7 2.4 182 5 5 3 5-2 342 27 0.07 8-7 2.2 158 51 0.03 35 5-3 5.2 342 27 0.07 10-7 0.4 26	20 33
8— 6 2. 4 56 33 0.06 317 3— 3 22. 1 69 58 0.17 9— 6 1.0 191 57 0.06 96 3— 4 1.1 57 13 0.02 10— 6 1.3 171 26 0.06 74 3— 5 0.1 52 11— 6 0.7 144 0.03 47 4— 1 0.4 104 12— 6 0.1 120 0.02 15 4— 1 0.4 104 5— 7 0.1 279 4— 3 9.7 19 51 0.07 6— 7 0.4 83 4— 4 4.4 128 12 0.01 7— 7 2.4 182 5 5 3 5— 2 1.1 38 31 0.02 9— 7 1.1 135 7 0.03 35 5— 2 1.1 38 31 0.02 10— 7 0.4 265 0.02 171 5— 4 2.2 93 59 0.01 11— 7 0.6 247 0.03 150 5— 5 1.3 206 15 0.01	35 5 I
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9-7 1.1 135 7 0.03 35 5-3 5.2 342 27 0.07 10-7 0.4 265 0.02 171 5-4 2.2 93 59 0.01 11-7 0.6 247 0.03 150 5-5 1.3 206 15 12-7 0.3 222 0.02 122 5-6 0.1 190 7-8 0.2 158 6-2 0.2 172 8-8 1.0 258 6-3 2.4 123 27 0.05 9-8 1.0 236 0.02 140 6-4 0.8 65 50 0.02	
10-7 0.4 265 0.02 171 5-4 2.2 93 59 0.01 11-7 0.6 247 0.03 150 5-5 1.3 206 15 12-7 0.3 222 0.02 122 5-6 0.1 190 7-8 0.2 158 6-2 0.2 172 8-8 1.0 258 6-3 2.4 123 27 0.05 9-8 1.0 236 0.02 140 6-4 0.8 65 50 0.02	225
11— 7 0.6 247 0.03 150 5— 5 1.3 206 15 12— 7 0.3 222 0.02 122 5— 6 0.1 190 7— 8 0.2 158 6— 2 0.2 172 8— 8 1.0 258 6— 3 2.4 123 27 0.05 9— 8 1.0 236 0.02 140 6— 4 0.8 65 50 0.02	166
127 0.3 222 0.02 122 5-6 0.1 190 78 0.2 158 6-2 0.2 172 88 1.0 258 6-3 2.4 123 27 0.05 98 1.0 236 0.02 140 6-4 0.8 65 50 0.02	270
7— 8	
8_8 1.0 258 6—3 2.4 123 27 0.05 6—8 1.0 236 0.02 140 6—4 0.8 65 50 0.02	
8_ 8	
9-8 1.0 236 0.02 140 6-4 0.8 65 50 0.02	307
	256
11—8 0. I 334 0. OI 252 6—6 0. 4 283	
12— 8 0.2 325 0.01 228 6— 7 0.1 266	
8-9 0.1 231 7-3 0.1 84	
9— 9	327
10-9 0.5 313 0.01 216 7-5 0.3 139	
11— 9 0.3 293 0.01 191 7— 6 0.3 252	
7-7 0.2 350	
9—10 0.1 304 7 7 10—10 0.2 48 8—4 0.1 348	
0.1 210	
II-II 0. I 122 8-7 0. I 329	
12—11 0.1 105 8—8 0.1 75	

χ		Commo	$\log rac{r'}{ar{r}'}$		x	Common $\log \frac{r'}{r'}$				
~	k_0	Κο	k_1	K ₁		k_0	K ₀	k_1	K 1	
g''' g'		0 /		υ <i>I</i>	a''' a'		J /		0 /	
1 0	0, 2	337			g''' g' 4— 2	O. I	307			
I I	15.4	312 58			4-3	O. I	148			
I— 2	0.5	310			4-4	0.3	353			
2— O	0.2	86								
2 I	7.6	84 55			5— 5	O. I	307			
2 2	14. 8	86 17		ì						
2- 3	o. 6	87			$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	19.8	208 34	0.31	80 14	
3— г	0.2	173			6— 2— 3	8.4	2 4			
3— 2	1.3	195 39								
3 3	1.5	40 12			₽—₽	o. 8	0			
3— 4	0. I	42			ბ — ზ	1.4	О			

Periodic inequalities of the latitude of Saturn.

We take the terms of $\Delta\beta'$ given at pages 531, 532, and multiply the co-efficients which involve g'' in their arguments by $\frac{21000}{22640}$, and afterwards add the first portion of $\Delta(\Delta\beta')$ given on page 536. To these can be joined the very small terms due to the action of Neptune (page 179). The whole is then changed to the form adopted in the chapter.

		Δ	β'				Δ	3'	
χ	k_0	K ₀	k_1	K ₁	χ	k_0	\mathbf{K}_0	k_1	K ₁
g' g 0 0 2 0 3 0 4 0 5 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0	0. 329 0. 204 0. 019 0. 005 0. 002 0. 003 0. 002 0. 026 1. 803 0. 841 2. 905 0. 721	287 13 269 51 331 209 41 37 116 2 210 41 225 28.5 185 4	0. 0020 0. 0245 0. 0482 0. 0018	311 32 22 163 10 310 59 276	$\begin{array}{cccccccccccccccccccccccccccccccccccc$	0.001 0.002 0.063 0.258 0.116 0.215 8.679 0.370 0.245 0.011 0.001 0.003	0 / 279 81 91 47 11 58 319 33 207 35 277 12.5 111 9 16 42 19	0.0002 0.0004 0.0029 0.0008 0.0054 0.0155 0.0056 0.0075 0.0009	207 237 299 18 90 197 9 66 57 329 47 269 18
4— 1 5— 1 6— 1	0. 057 0. 037 0. 001	301 28 310 15 340	0.0002 0.0002	117 27	1— 3 2— 3 3— 3	0. 007 0. 087 0. 041	84 89 53 53 11		

			Δβ'				Δ	<i>β'</i>	
X	k_0	K ₀	k_1	K ₁	X	k_0	K ₀	k_1	K ₁
g' g	"	0 /	"	0 /	g'' - g'	//	0 /	"	0 /
4 3	0, 077	199 40			I 2	0. 035	298 43	İ	
5-3	0. 117	176 9			I— 3	0.002	306		
6— 3	0.096	155 49		•	2+ 1	0.003	164		
7-3	0. 048	300 27			2 0	0, 040	152 57		
8 3	0.002	247			2 I	0.110	301 20		
9 3	0.001	225			2- 2	0. 031	277 36		
2 4	0, 003	139			2 3	0.008	2		ľ
3- 4	0.033	167 31			3+ 1	0.002	294	1	
4-4	0.018	134 26			3 0	0. 032	289 10		
5— 4	0.014	266 3			3 - 1	0.032	221 32		
6— 4	0.013	246 33			3— 2	0. 599	20 3		
7— 4	0.011	230			3-3	0. 037	17 4		
8 4	0.002	171			3— 4	0.003	64		
9 4	0. 087	161 51	0.0012	250	1		208		
Io- 4	0,009	341			4— 1	0.005			
11 4	0, 002	273			4-2	0.025	349 4 281 40		
3— 5	0.001	189			4-3	0.023	331		
4- 5	0.013	245			<u>[</u>]			ŀ	
5-5	0.009	214			5— 1	100.0	165		
6-5	0.004	349			5-2	0. 003	333		
7-5	0.003	317			5— 3	0.021	244 54		
8- 5	0.002	303			5 4	0.005	341		
9- 5	0.003	272			6 2	0.001	232		
10 5	0.002	247			6 3	0.012	32		
11-5	0.002	219			6— 4	0,003	333	ĺ	
		_			6 5	0, 001	69		
4 6	0.001	237			7— 3	0.001	0		
5— 6	0.005	323			7— 4	0.001	288		
6 6	0.004	292		i	7— 5	0.001	45		
7-6	0.001	63			$g^{\prime\prime\prime}$ g^{\prime}				
8— 6	0.001	21			1+1	0. 002	137		
9— 6	0.001	8			10	0.005	146		
10 6	0.001	351			1 1	0.001	4		
6— 7	0.002	. 38			1 2	0.002	I 20		
7— 7	0.002	9	1		2 0	0. 003	276		
$g^{\prime\prime}$ g^{\prime}			İ	ĺ	2— I	0.018	98 27		
$rac{g}{1+rac{1}{1}}$	0.019	259 21	ĺ		2 2	0.001	111		
10	0. 080	220 17							
1— 1	0. 036	11 34		1	3— 2	0.004	232		j

We derive f' from $n'z' = g' + n'\delta z'$ by the formula

Then

com.
$$\log \bar{r}' = 0.97812861 - \text{com. } \log (1 + e' \cos f')$$

In addition, $l' = f' + \pi'$, and we derive R' from

$$R' = +97''.774 \sin(2l' + 315^{\circ} 18' 22'') + o''.023 \sin(4l' + 270^{\circ} 37')$$

The heliocentric longitude of Saturn, referred to the mean equinox of date, is

$$\lambda' = f' + R' + \pi' + 50''.258141t$$

In order to get the equation which determines $\sin \beta_0'$, we note that the correction of $\frac{u'}{\cos i'}$ (page 555), on account of changes in the values of the disturbing masses, requires that the A and B of page 531 should receive severally the corrections -0''.0507T and -0''.0662T, so that the equation for $\cos i'$ sin b' now becomes

$$\cos i' \sin b' = \begin{bmatrix} 33.3758T + 0.16226T^2 - 0.000858T^3 \end{bmatrix} \sin b' + [-23.9117T + 0.21432T^2 + 0.000641T^3] \cos b'$$

If we add to this the expression for the portion of $\sin \beta_0'$, which arises from the motion of the ecliptic (page 531), and also take account of the correction $-\frac{d(\sin \beta_0')}{dz'} \Delta(\delta z')$, given at page 536, we obtain

$$\sin \beta_0' = \begin{cases} \sin i_0' \cos \theta_0' + 80.1664T + 0.06123T^2 - 0.001471T^3 \\ + [-\sin i_0' \sin \theta_0' - 18.6681T + 0.42811T^2 - 0.00027T^3] \cos l' \\ + [-0.0208T - 0.00035T^2] \sin 3l' \\ + [-0.0330T - 0.00023T^2] \cos 3l' \end{cases}$$

ADDENDA.

Page 301. Insert in the table beginning in the middle of this page the following line:

1 0 0 1 -0.018886 | +0.033370 | +0.000304 | -0.000132 | +0.000034 | -0.00066 | +0.000147 | -0.000095 |

Page 377. Insert in the table on this page the following line:

Page 379. Insert in the table on this page the following line:

Page 380. Insert in the table occupying the lower half of the page the following line:

-I o o | +0.0000403 | -0.0000593 | +0.0002053 | -0.0000693 |

Page 384. In the columns headed $\frac{1}{2} \frac{d\mathbf{F}}{dg'} (n'\delta z')^2$ add the terms corresponding to the argument -1 9— 4:

+3.5 | 0.0

Page 416. Insert in the table occupying the lower half of the page the following line:

1 1 0 0 1 -0.000544 | +0.000973 | -0.000254 | +0.000341 |
25 AST-37

